

First Magurele School in High Energy Physics,  
October 27, 2008

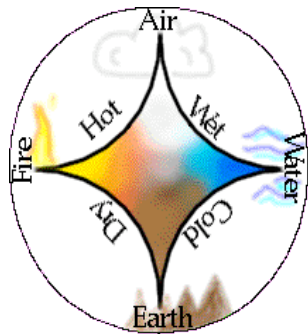
# Structure Functions at HERA

Cristinel DIACONU  
CPP Marseille & DESY



# The (very) early days

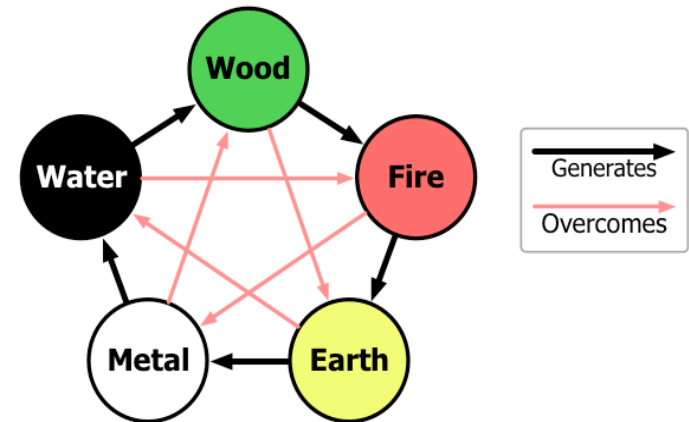
- Something must be fundamental, the 'bulding blocks'
- Models:
  - Aristotel, Heraclit et al., 4+1 elements “air,fire, water, earth”+quitessence



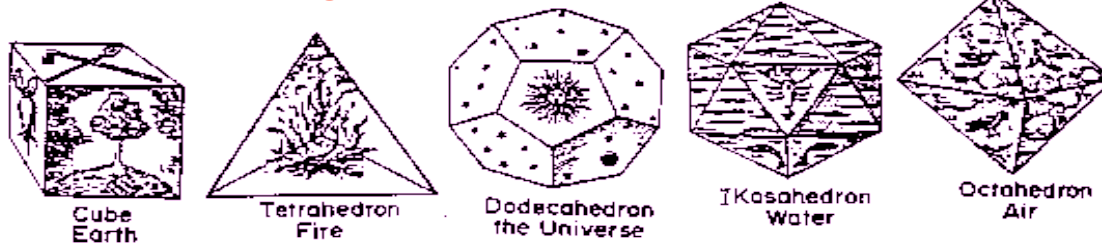
The 5<sup>th</sup> element



Asian version



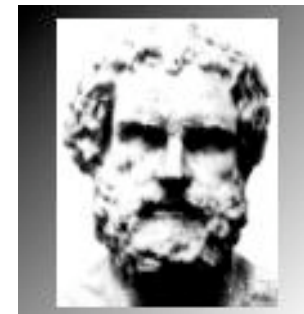
- **Plato's model (geometrical, mistic faith in mathematics)**



- **Leucip, Democrit: “Elementary particles” =atoms+space**

By convention there is color, by convention sweetness,  
by convention bitterness, but in reality there are atoms and space.

Democritus (400 BC)



# Elements, elements....

- Lavoisier, Davy: show at least one of the 4/5 elements are composed, there are chemical elements
- composed of atoms
- Mendeleev: tabulate the ~50 elements discovered by ~1850
  - chemical properties repeat
  - able to predict new elements
    - ==>>substructure!

| Property                           | Ekasilicon         | Germanium                 |
|------------------------------------|--------------------|---------------------------|
| atomic mass                        | 72                 | 72.59                     |
| density (g/cm <sup>3</sup> )       | 5.5                | 5.35                      |
| melting point (°C)                 | high               | 947                       |
| color                              | gray               | gray                      |
| oxide type                         | refractory dioxide | refractory dioxide        |
| oxide density (g/cm <sup>3</sup> ) | 4.7                | 4.7                       |
| oxide activity                     | feebly basic       | feebly basic              |
| chloride boils                     | under 100°C        | 86°C (GeCl <sub>4</sub> ) |

## On the Relationship of the Properties of the Elements to their Atomic Weights

D. Mendelejeff, *Zeitschrift für Chemie* 12, 405-406 (1869);

Ueber die Beziehungen der Eigenschaften zu den Atomgewichten der Elemente. Von D. Mendelejeff. — Ordnet man Elemente nach zunehmenden Atomgewichten in verticale Reihen so, dass die Horizontalreihen analoge Elemente enthalten, wieder nach zunehmendem Atomgewicht geordnet, so erhält man folgende Zusammenstellung, aus der sich einige allgemeinere Folgerungen ableiten lassen.

|       |          |           |            |            |            |
|-------|----------|-----------|------------|------------|------------|
|       |          |           | Ti = 50    | Zr = 90    | ? = 180    |
|       |          |           | V = 51     | Nb = 94    | Ta = 182   |
|       |          |           | Cr = 52    | Mo = 96    | W = 186    |
|       |          |           | Mn = 55    | Rh = 104,4 | Pt = 197,4 |
|       |          |           | Fe = 56    | Ru = 104,4 | Ir = 198   |
|       |          | Ni = 59   | Co = 59    | Pd = 106,6 | Os = 199   |
| H = 1 |          |           | Cu = 63,4  | Ag = 108   | Hg = 200   |
|       | Be = 9,4 | Mg = 24   | Zn = 65,2  | Cd = 112   |            |
|       | B = 11   | Al = 27,4 | ? = 68     | Ur = 116   | Au = 197?  |
|       | C = 12   | Si = 28   | ? = 70     | Sn = 118   |            |
|       | N = 14   | P = 31    | As = 75    | Sb = 122   | Bi = 210?  |
|       | O = 16   | S = 32    | Se = 79,4  | Te = 128?  |            |
|       | F = 19   | Cl = 35,5 | Br = 80    | J = 127    |            |
|       | Li = 7   | Na = 23   | K = 39     | Rb = 85,4  | Cs = 133   |
|       |          |           | Ca = 40    | Sr = 87,6  | Ba = 137   |
|       |          |           | ? = 45     | Ce = 92    | Pb = 207   |
|       |          |           | ?Er = 56   | La = 94    |            |
|       |          |           | ?Yt = 60   | Di = 95    |            |
|       |          |           | ?In = 75,6 | Th = 118?  |            |

- Die nach der Grösse des Atomgewichts geordneten Elemente zeigen eine stufenweise Abänderung in den Eigenschaften.
- Chemisch-analoge Elemente haben entweder übereinstimmende Atomgewichte (Pt, Ir, Os), oder letztere nehmen gleichviel zu (K, Rb, Cs).
- Das Anordnen nach den Atomgewichten entspricht der *Werthigkeit* der Elemente und bis zu einem gewissen Grade der Verschiedenheit im chemischen Verhalten, z. B. Li, Be, B, C, N, O, F.

# GMR



"as if you fired a 15-inch shell at a piece of tissue paper and it came back and hit you."

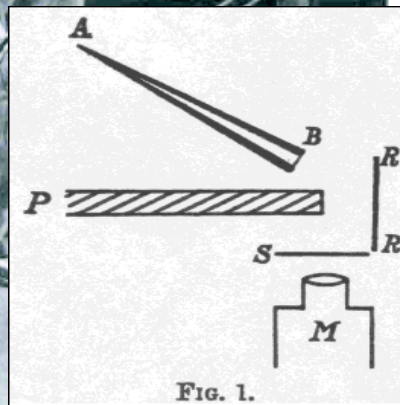
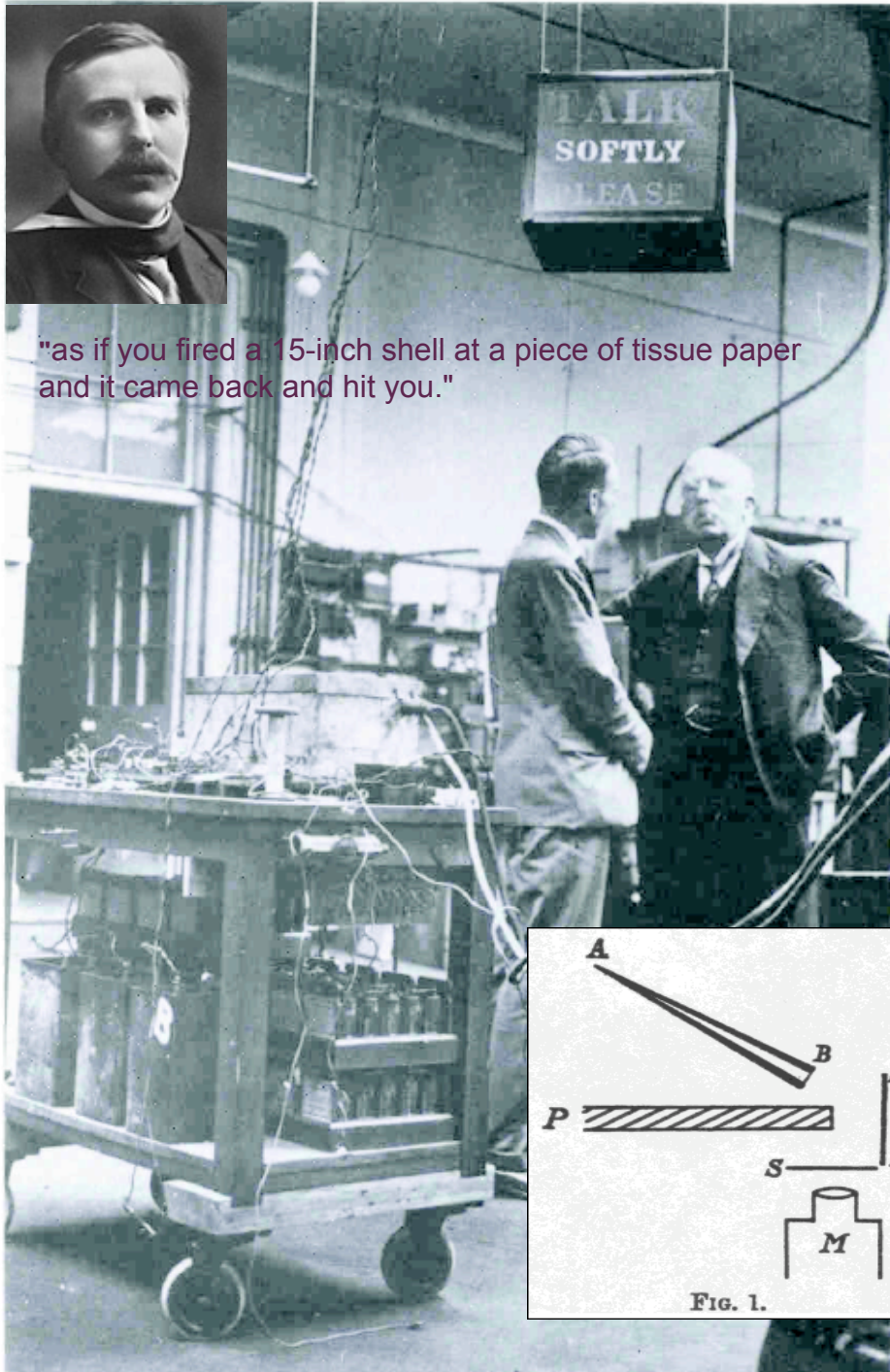
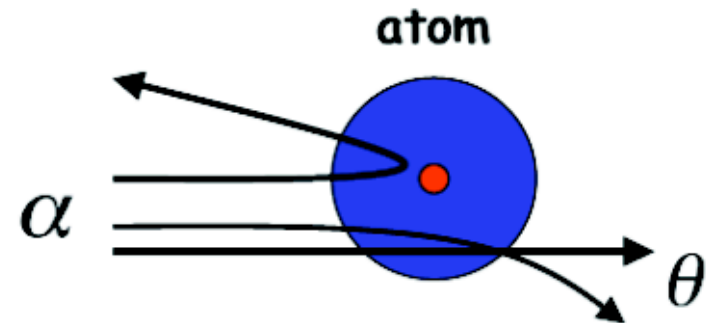


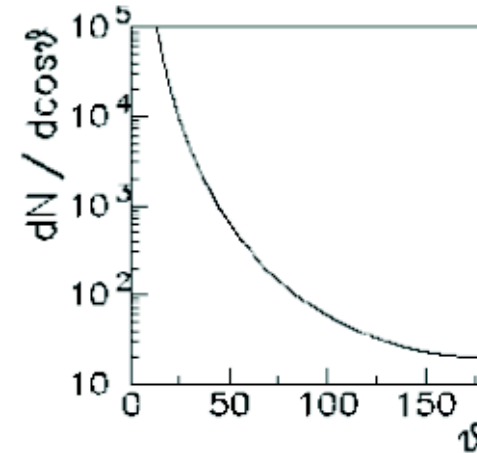
FIG. 1.

Discovery of the atomic nucleus 1909



↪ positively charged massive atomic nucleus

$$r_{\text{nucleus}} \approx r_{\text{atom}} / 10000 \approx 10^{-14} \text{ m}$$



$$\frac{dN}{d\Omega} \propto \frac{Z^2}{E^2} \frac{1}{4 \sin^4 \theta / 2}$$

$$E_{\alpha} = 5.5 \text{ MeV}$$

A "punctual" particle can probe a composed particle: the beginning of the "beam microscopy"

# Proton resists bombardement: elastic scattering

PHYSICAL REVIEW

VOLUME 79, NUMBER 4

AUGUST 15, 1950

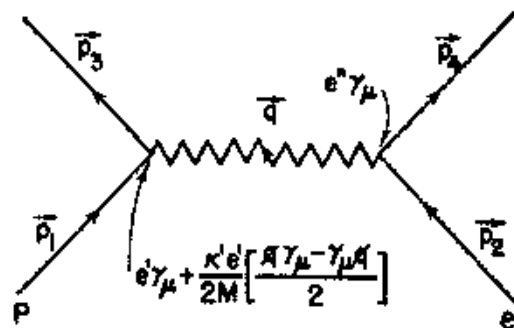
## High Energy Elastic Scattering of Electrons on Protons

M. N. ROSENBLUTH

*Stanford University, Stanford, California*

(Received March 28, 1950)

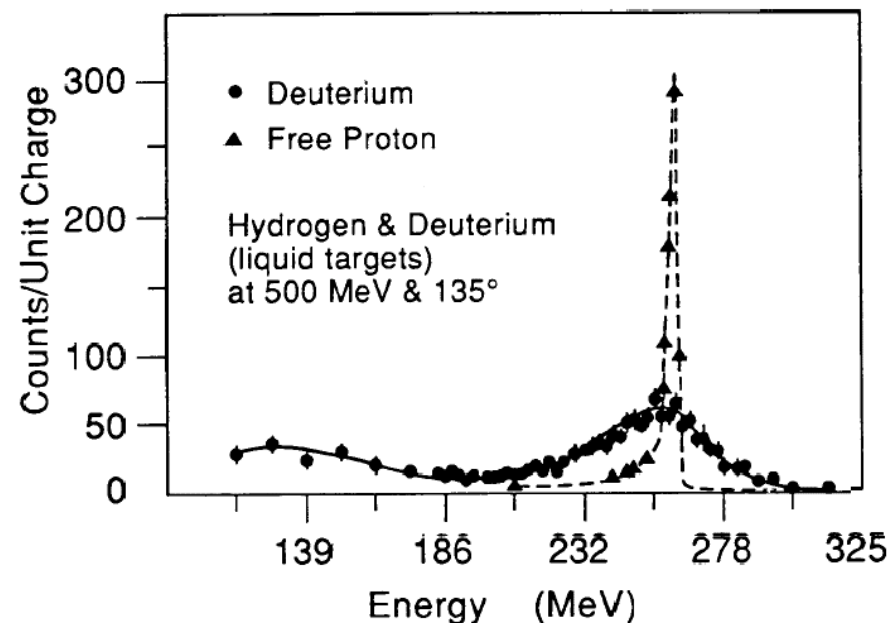
FIG. 1. Diagram for the elastic scattering of a physical proton and a physical electron. (The letter "q" with the bar through it in this figure is the same as the German letter, q, used in the text.)



### I. INTRODUCTION

**T**HE Stanford linear electron accelerator program is expected to make available large currents of relativistic electrons with various energies ranging from 6 to 1000 Mev. Among the experiments of considerable interest which may then be performed is the elastic scattering of electrons on protons. This may be done on a hydrogen gas or liquid target. Despite the smallness of the cross section at high energies, the expected large intensity of the beam should render the experiments possible.

Hofstaeder



# Electron Scattering from the Proton\*†‡

ROBERT HOFSTADTER AND ROBERT W. McALLISTER

*Department of Physics and High-Energy Physics Laboratory,  
Stanford University, Stanford, California*

(Received January 24, 1955)

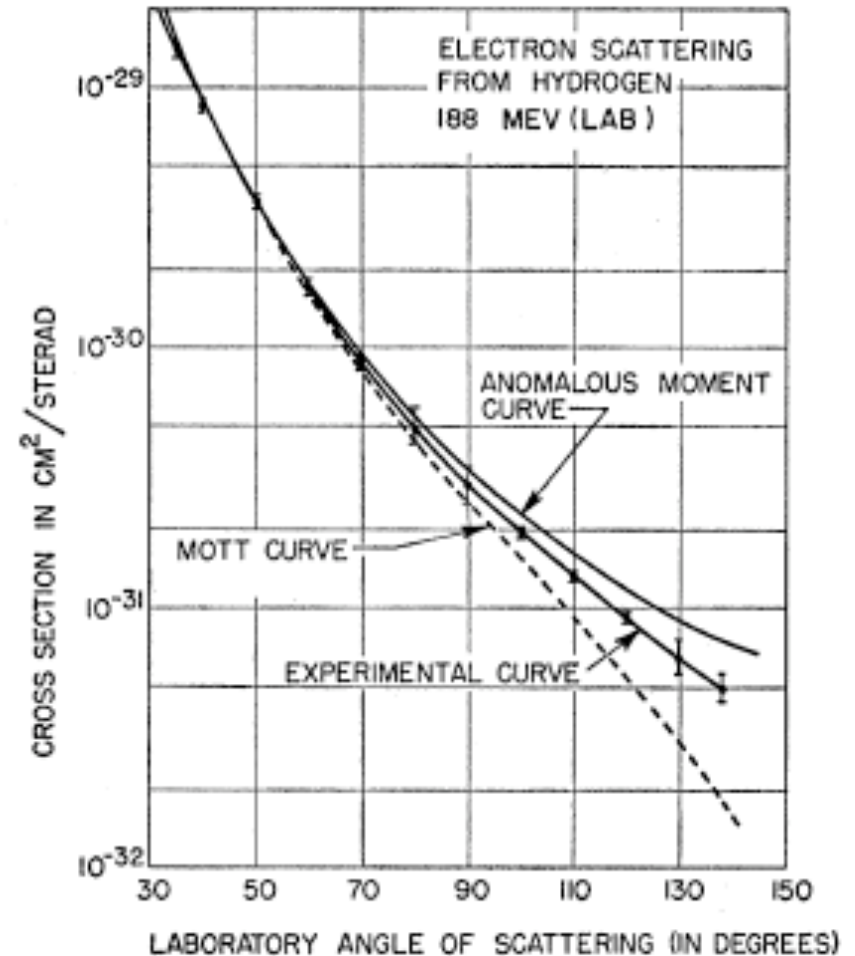
WITH apparatus previously described,<sup>1,2</sup> we have studied the elastic scattering of electrons of energies 100, 188, and 236 Mev from protons initially at rest. At 100 Mev and 188 Mev, the angular distributions of scattered electrons have been examined in the ranges 60°–138° and 35°–138°, respectively, in the laboratory frame. At 236 Mev, because of an inability of the analyzing magnet to bend electrons of energies larger than 192 Mev, we have studied the angular distribution between 90° and 138° in the laboratory frame. In all cases a gaseous hydrogen target was used.

$$P_{obs} = F(q)P_{point-particle}$$

$$d = h/q$$

Accountable by elastic scattering  
over finite size (~1fm) charge distribution

To “resolve” the proton, need more energy!  
Go to inelastic regime! When  $Q^2 \gg M_p$  Deep Inelastic Scattering



proton were a spherical ball of charge, this rms radius would indicate a true radius of  $9.5 \times 10^{-14}$  cm, or in round numbers  $1.0 \times 10^{-13}$  cm. It is to be noted that if our interpretation is correct the Coulomb law of force has not been violated at distances as small as  $7 \times 10^{-14}$  cm.

# SLAC experiments at high energy (1960)

High Energy electrons (20~GeV) new technology (klistrons)

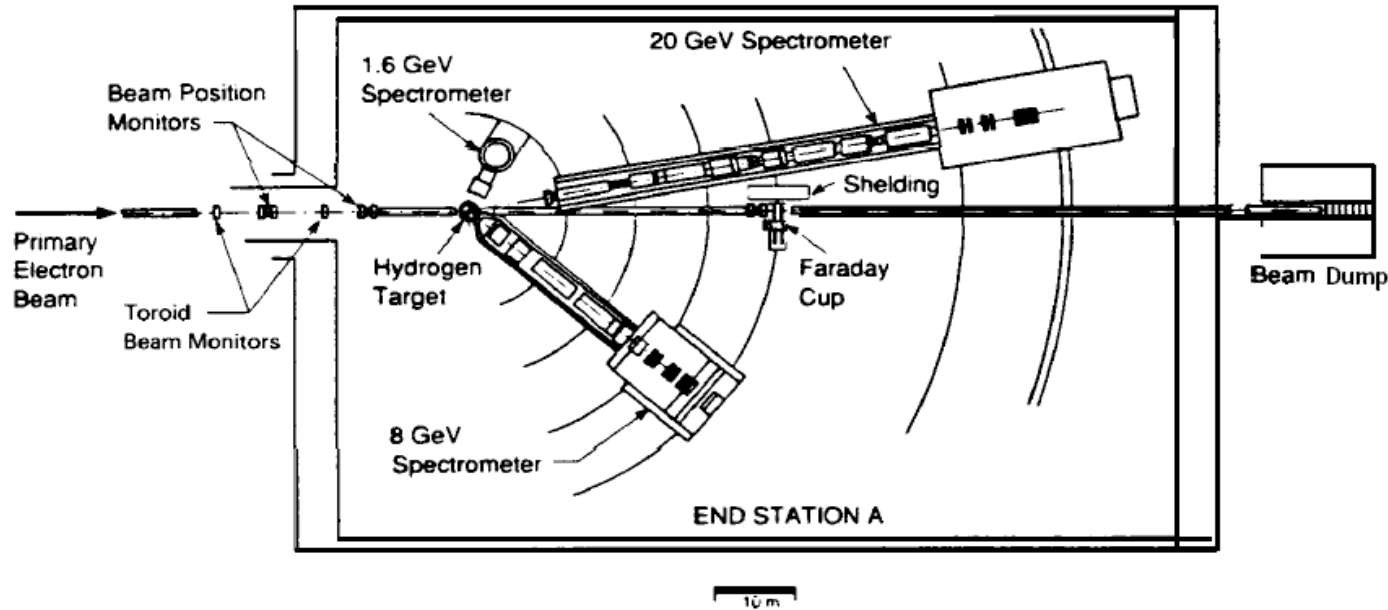
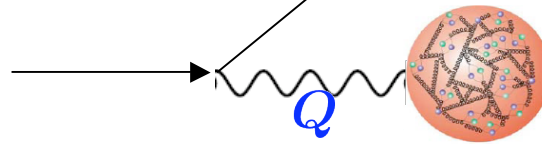


Fig. 14. Layout of spectrometers in End Station A. All three spectrometers can be rotated about the pivot. The 20 GeV spectrometer can be operated from about  $1\frac{1}{2}^\circ$  to  $25^\circ$ , the 8 GeV from about  $12^\circ$  to over  $90^\circ$ . The 1.6 GeV spectrometer coverage is from  $\sim 50^\circ - 150^\circ$ .



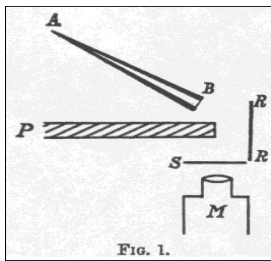
# A short history of resolving matter structure



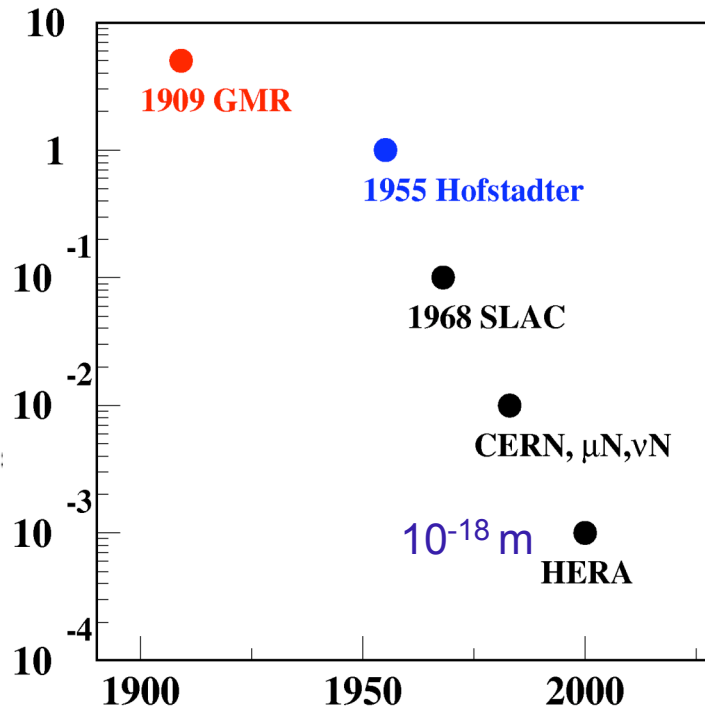
~100 years ago

Geiger, Marsden. (1909)  
Rutherford(1911)

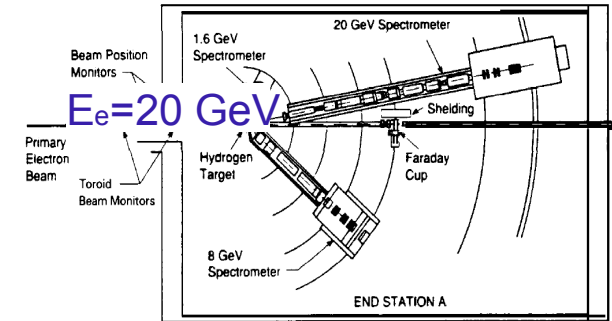
$E_\alpha = 5.5 \text{ MeV}$



$$\delta \text{ [fm]} \simeq \frac{200 \text{ MeV}}{Q}$$



40 years ago: partons

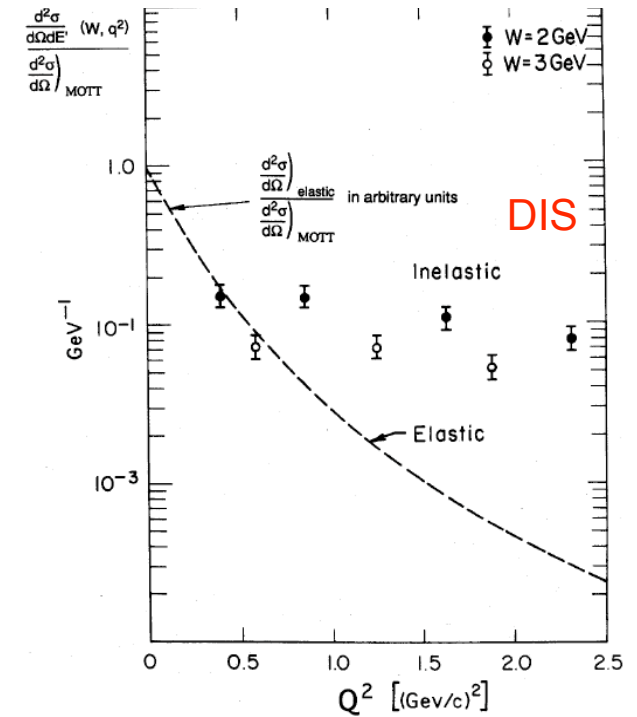
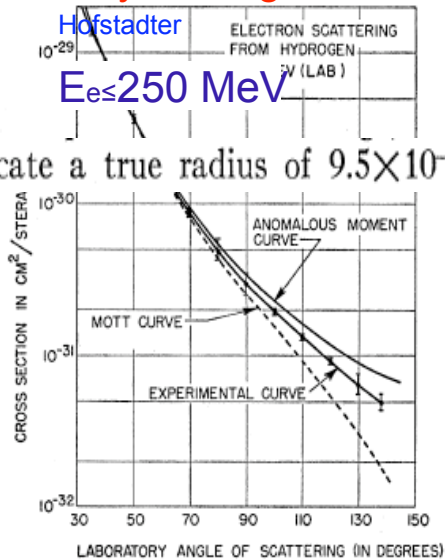


53 years ago

Hofstadter

$E_e \leq 250 \text{ MeV}$

indicate a true radius of  $9.5 \times 10^{-14} \text{ cm}$ .



[polarised collisions since mid 70's]

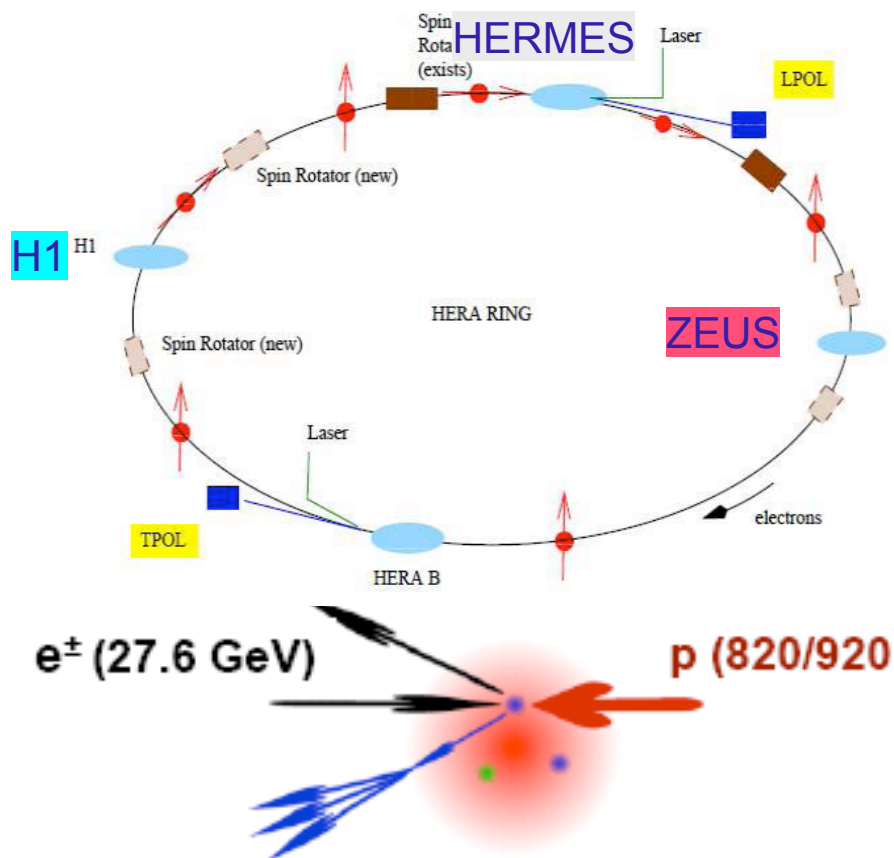


24 years ago

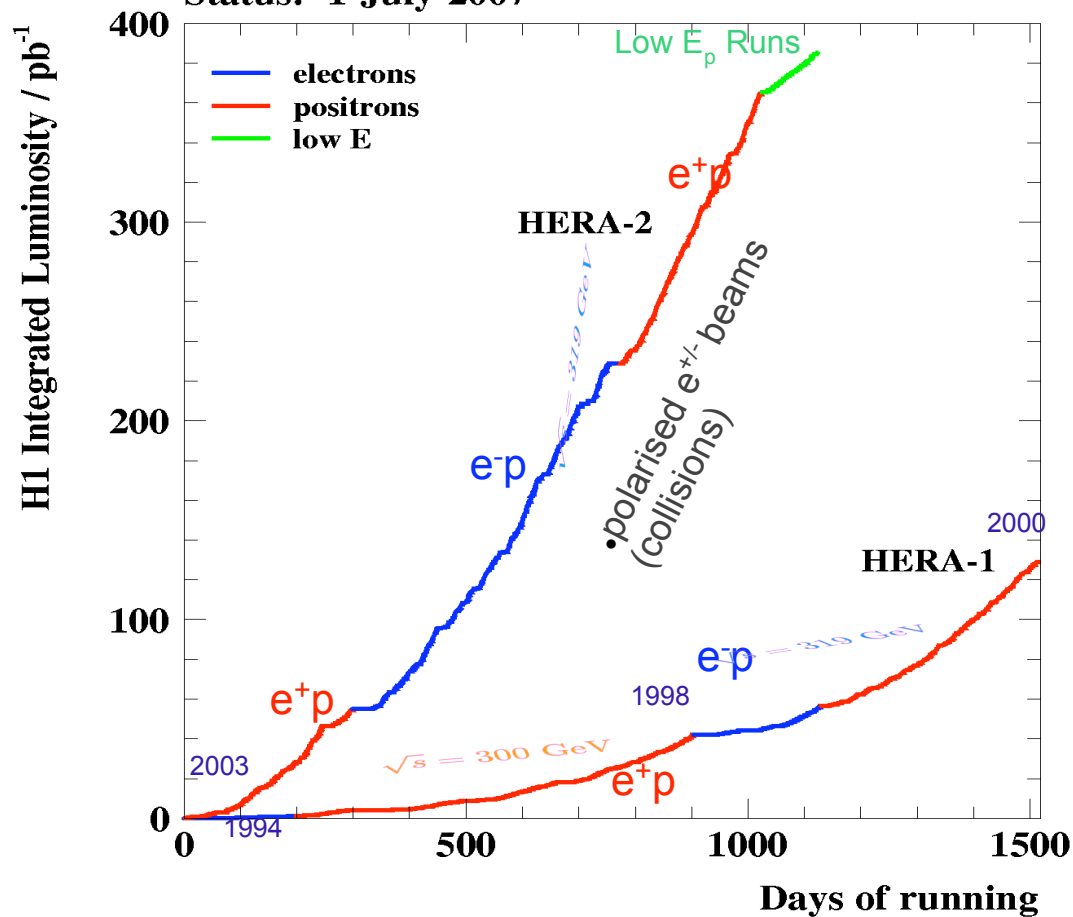


Volker Soergel and the Minister of Science of Germany, Heinz Riesenhuber,

# HERA Collider: end in 2007



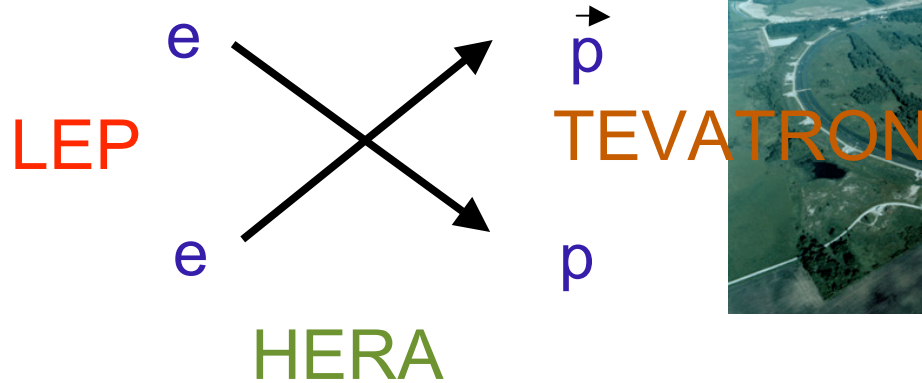
Status: 1-July-2007



- HERA 1: 1992-2000 ~120 pb<sup>-1</sup>/expt
- HERA 2: 2003-2007
  - Luminosity upgrade (x3)
  - Polarised electrons/positrons

~200 pb<sup>-1</sup> e<sup>-</sup>p  
 ~300 pb<sup>-1</sup> e<sup>+</sup>p

# Colliders at Fermi Scale



->  $e^+e^-$  collider(2000)  
 $E_{cm} = 90-209$  GeV  
 Lumi=900 pb<sup>-1</sup>/exp.(phys)  
 ALEPH,DELPHI  
 L3,OPAL

SLC: polarized  $e^+e^-$   
 at Z peak



->  $e^\pm p$  collider  
 $E_{cm} = 320$  GeV  
 H1, ZEUS  
 HERA I 120 pb<sup>-1</sup>/expt(phys.)  
 HERA II 2007 ->700 pb<sup>-1</sup>(delivered, $e^\pm, \pm P_e$ )

->  $pp$  collider: CDF, D0

Run I  $E_{cm} = 1.8$  TeV  
 130 pb<sup>-1</sup>/exp.(phys.)

Run II  $E_{cm} = 1.96$  TeV  
 1fb<sup>-1</sup> delivered  
 2009 -> 4-8 fb<sup>-1</sup>

# HERA

construction started in 1984  
physics: 1992-2007

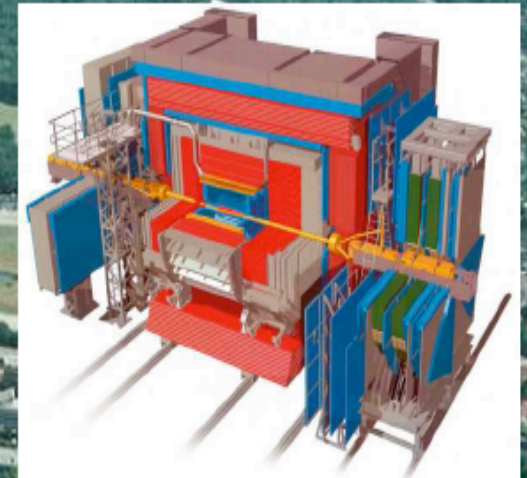
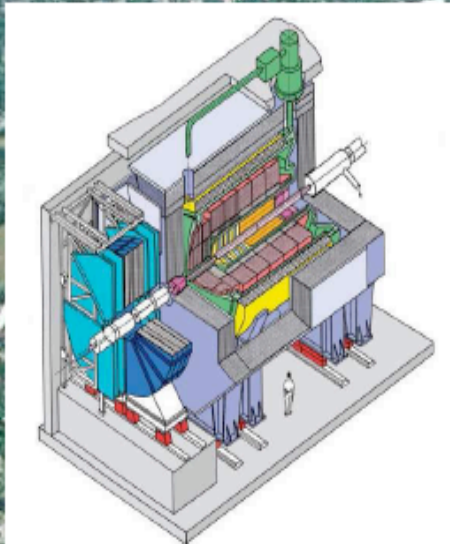
HERMES  
(e-A fixed target)

H1

AOL Arena  
(SV Hamburg)

ZEUS

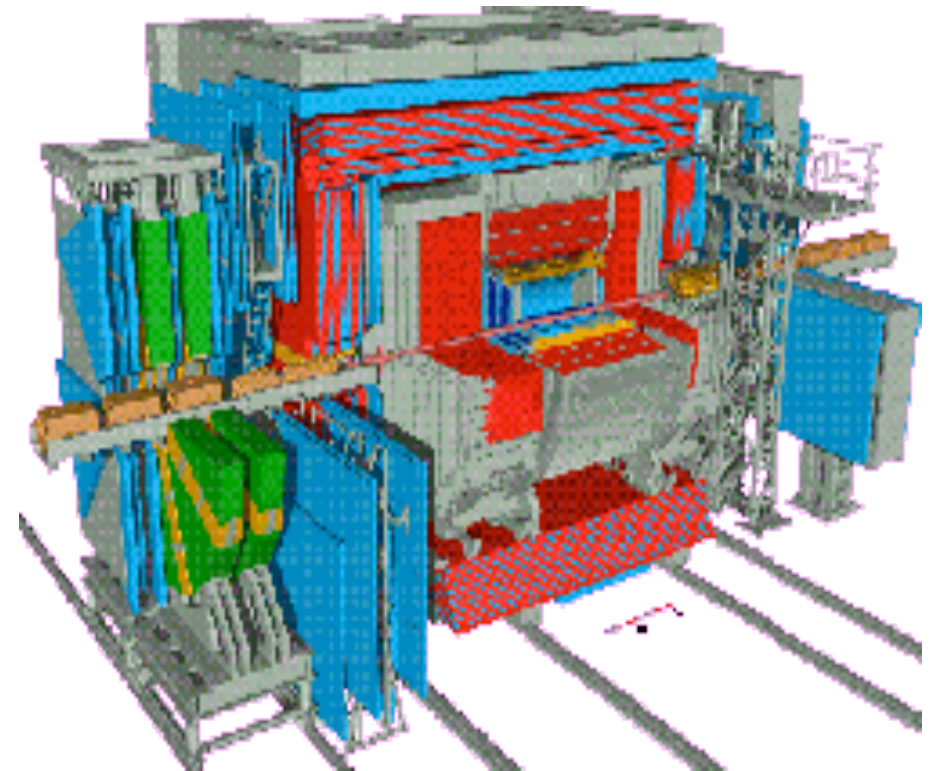
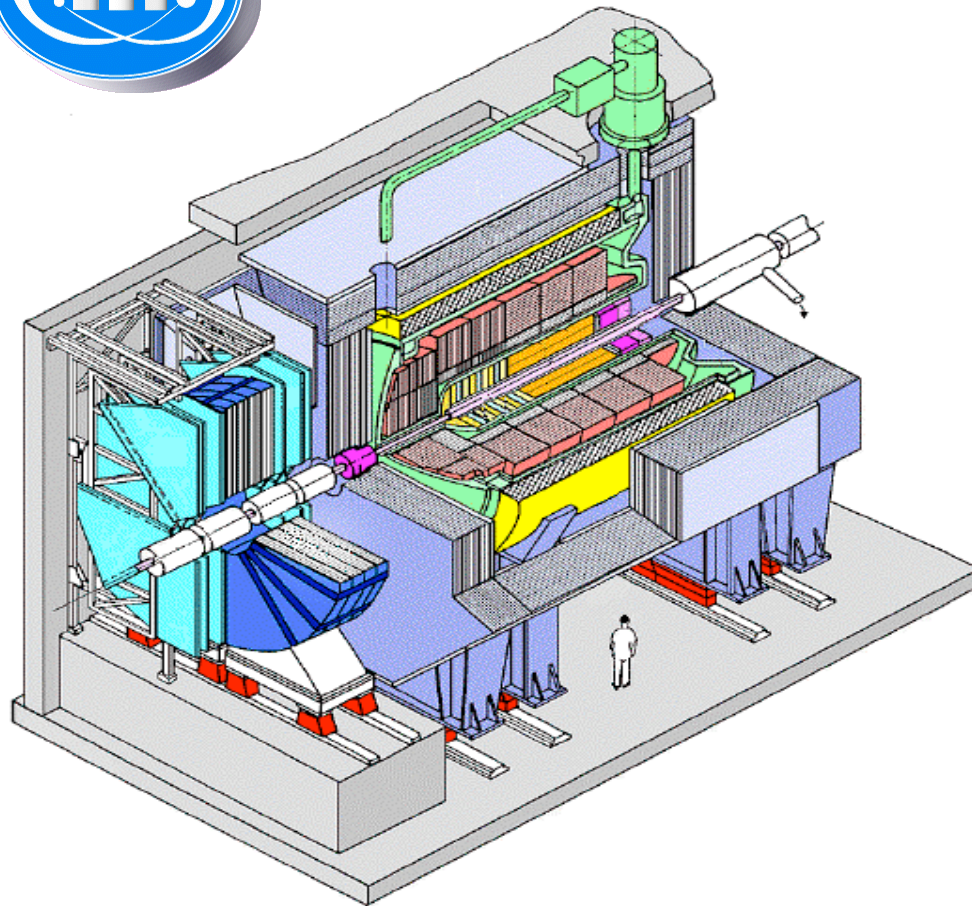
HERA



$$E_e = 27.6 \text{ GeV} \quad E_p = 920 \text{ GeV}$$
$$\sqrt{s} = 319 \text{ GeV} \quad \bullet E = 54 \text{ TeV}$$

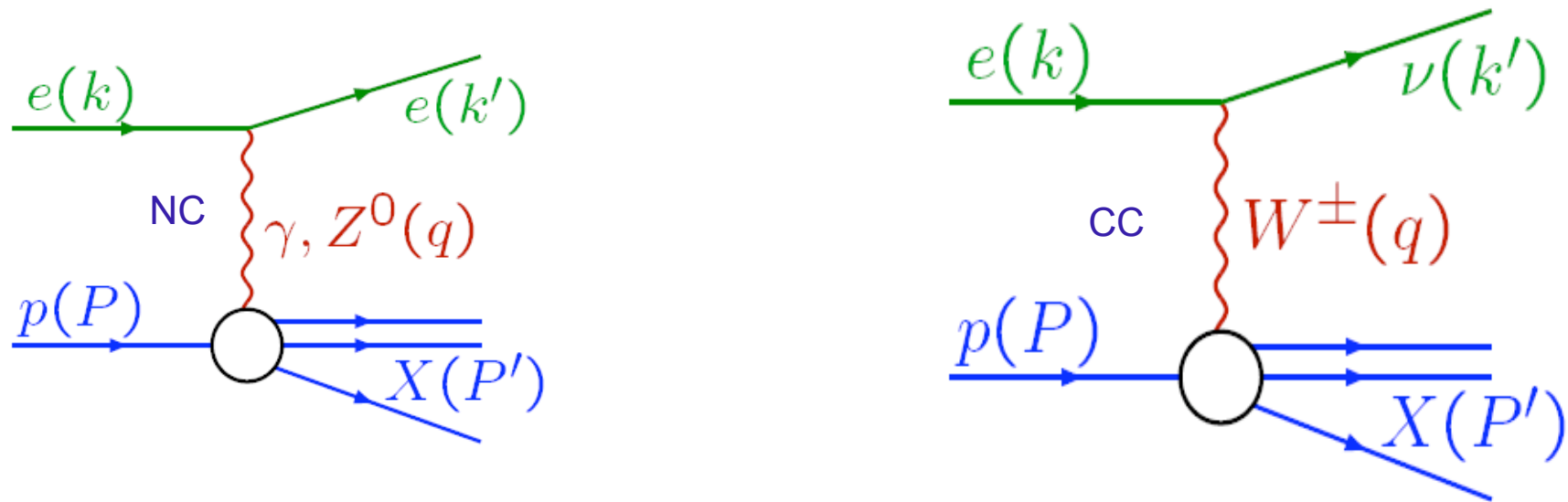
fixed target

# H1 and ZEUS detectors



$4\pi$  detectors, excellent tracking and calorimetry

# Deep-Inelastic Scattering



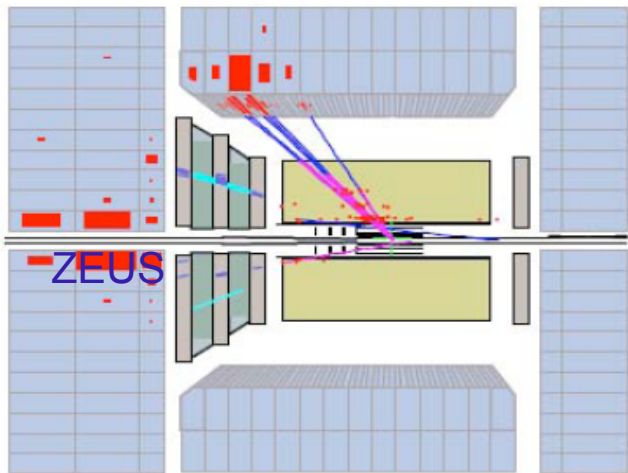
- $Q^2 = -q^2 = -(k - k')^2$   
virtuality/resolving power
- $x = \frac{Q^2}{2P \cdot q}$  Bjorken scaling variable,  
momentum fraction of the scattered  
parton
- $y = \frac{q \cdot P}{k \cdot P}$  inelasticity

Related by  $Q^2 = xys$

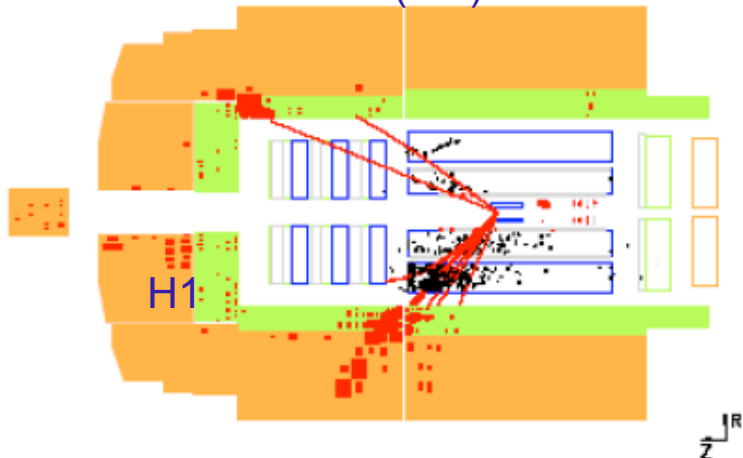
Partons = Quarks + Gluons (QCD improved quark parton model)

# DIS at HERA

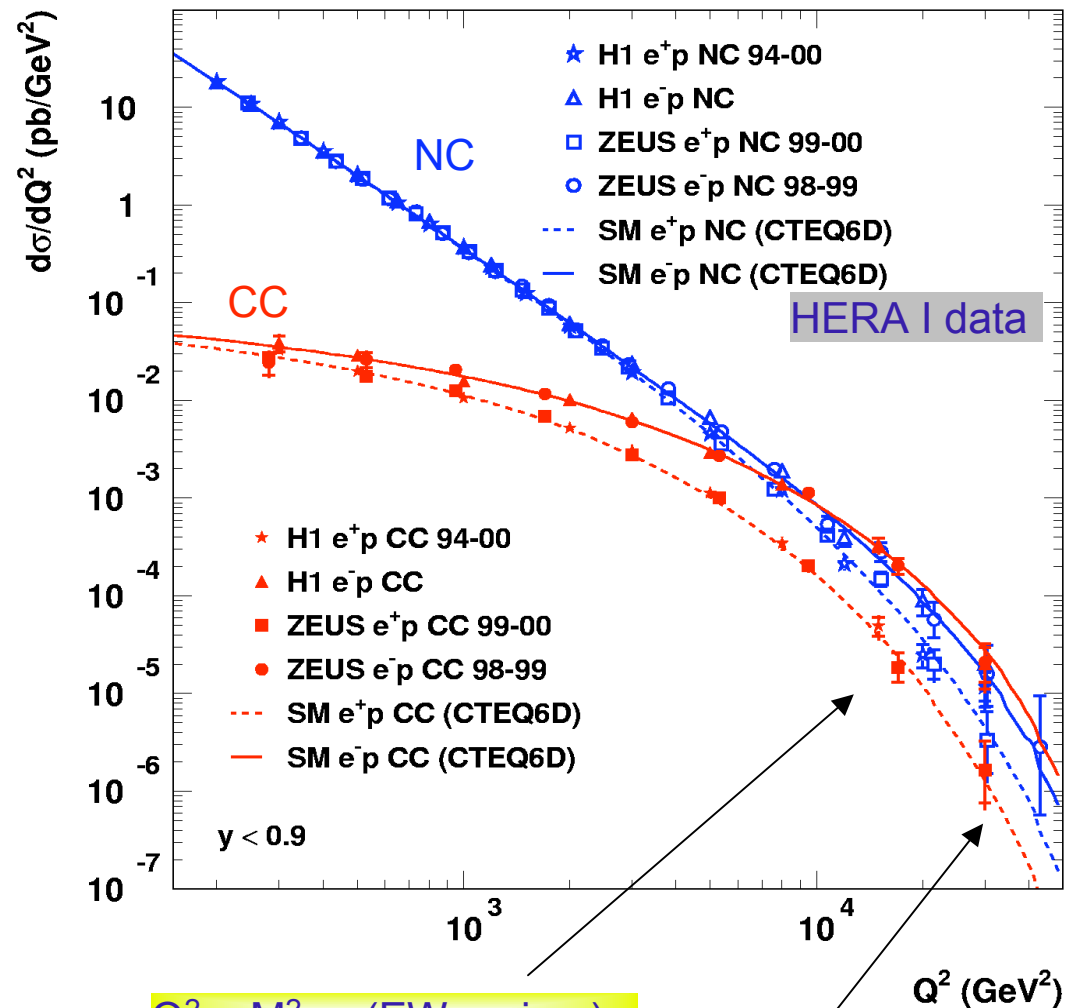
Charged Current (CC)



Neutral Current (NC)



HERA



$Q^2 \sim M_{W,Z}^2$  (EW regime)

$r_{\text{quark}} < 10^{-18} \text{m}$   
"p"/1000

# DIS: Cross sections, structure functions, partons

$$\tilde{\sigma}_{NC}^{\pm} = \frac{d^2\sigma_{NC}^{e^{\pm}p}}{dx dQ^2} \frac{xQ^4}{2\pi\alpha^2 Y_{\pm}} = \tilde{F}_2 - \frac{y^2}{Y_{\pm}} \tilde{F}_L \mp \frac{Y_{\pm}}{Y_{\pm}} x \tilde{F}_3, \quad Y_{\pm} = 1 \pm (1-y)^2$$

Leading Order picture of the proton

$$F_2 \left[ F_2, F_2^{\gamma Z}, F_2^Z \right] = x \sum_q \left[ e_q^2, 2e_q v_q, v_q^2 + a_q^2 \right] (q + \bar{q}) \quad \text{quarks}$$

gluons from scaling violations

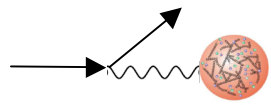
$$F_3 \left[ xF_3^{\gamma Z}, xF_3^Z \right] = 2x \sum_q \left[ e_q a_q, v_q a_q \right] (q - \bar{q}) \quad \text{(valence) quarks}$$

$$F_L \quad F_L \sim x\alpha_s g \quad \text{gluons}$$

CC: similar decomposition, but different quarks combinations accessed  
flavour sensitive (separate in e+p/e-p)



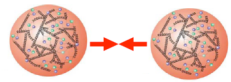
# The PDF's mechanics: factorisation and evolution



$$\sigma_{DIS} \equiv \mathcal{C}_{\text{lepton-parton}} \otimes f(x, Q^2)$$

perturbative QCD      non-perturbative

factorisation



$$\sigma_{pp \rightarrow FS} \equiv \mathcal{C}_{\text{parton-parton}} \otimes f(x, Q^2) \otimes f(x, Q^2)$$

$\parallel$   
 $E^2_{\text{CM parton-parton}}$

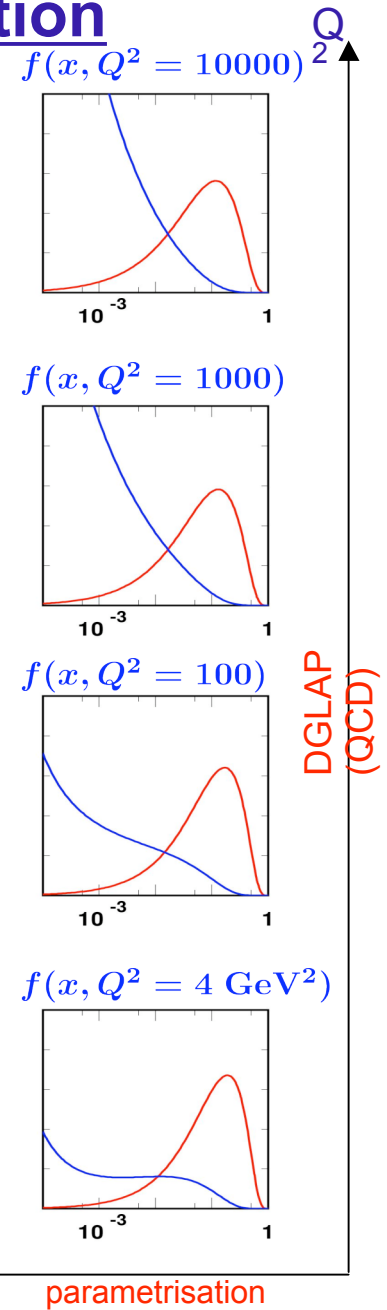
Input at scale  $Q^2_0$ : parameterisation assumed (typically 20 parameters)

Evolution in  $Q^2$  calculable in QCD (DGLAP):

$$\frac{\partial}{\partial Q^2} f_i(x, Q^2) = \sum P^{i,j} \otimes f_j(x, Q^2)$$

The PDF's play two (equivalent) roles:

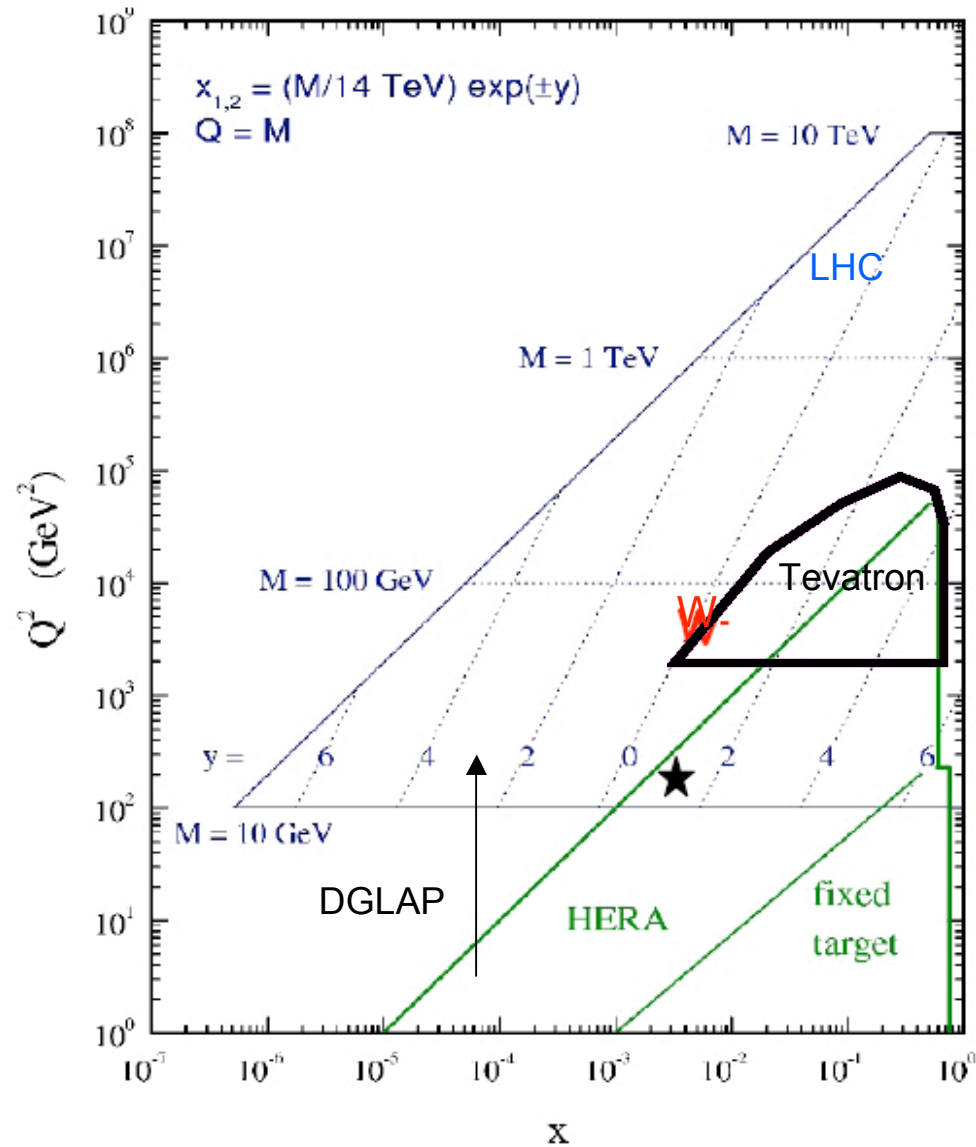
- nucleon chemistry: understand how the baryonic matter is made
- predictions via factorisation ansatz (for instance for LHC)



# DIS versus hadronic colliders

Example:  
 pp: W (at rest) corresponds to  
 $Q^2 = M_W^2 = 6400 \text{ GeV}^2$   
 $x = 0.005$  for LHC  
 $x = 0.2$  for Tevatron

For  $M = 1 \text{ TeV}$  (LHC)  $x > 0.005$



DIS data is the support for LHC predictions (beware the very low  $x$ !)  
 A number of improvements expected from Tevatron (in particular at high  $x$ )

## The data for PDF's

| Process                       | Experiments           | Constraints      |
|-------------------------------|-----------------------|------------------|
| DIS Collisions                | H1,ZEUS               | q,g              |
| DIS Fixed Target              | BCDMS, NMC,E665,SLAC  | q,g              |
| pp collision :jets, W/Z asym. | CDF,D0                | g, u/d at high x |
| DIS neutrino-N                | NuTev,Chorus,CCFR     | q,g (s)          |
| pp/pN Drell Yan               | E605,E702, E866/NuSea | q,g              |

Global fits: determination of PDF's using the available data sets

[Ex: MSTW08 2743 measurements]

MSTW, CTEQ, AKP, NNPDF (DIS data), HERAPDF (HERA averaged data, see later)

**PDF4LHC:** Common effort to converge on technical and physics issues

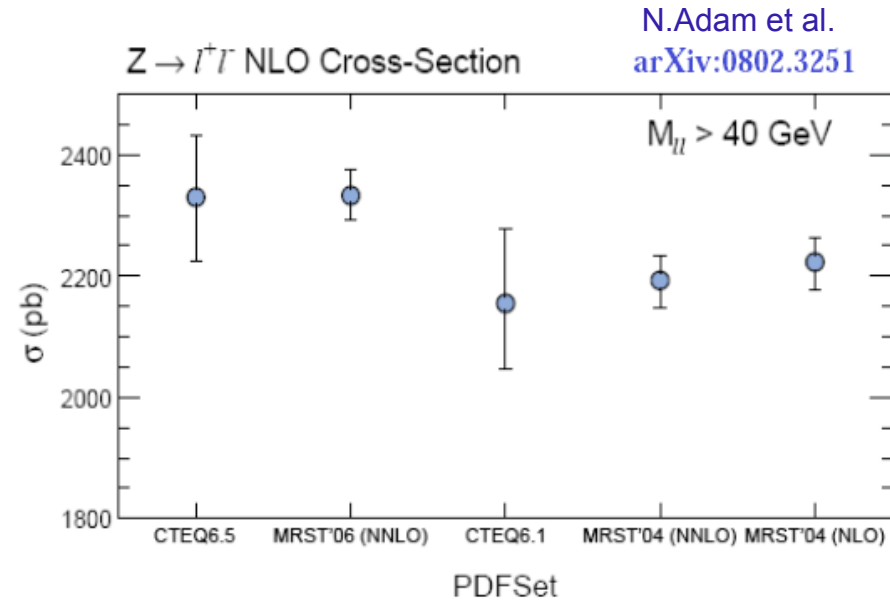
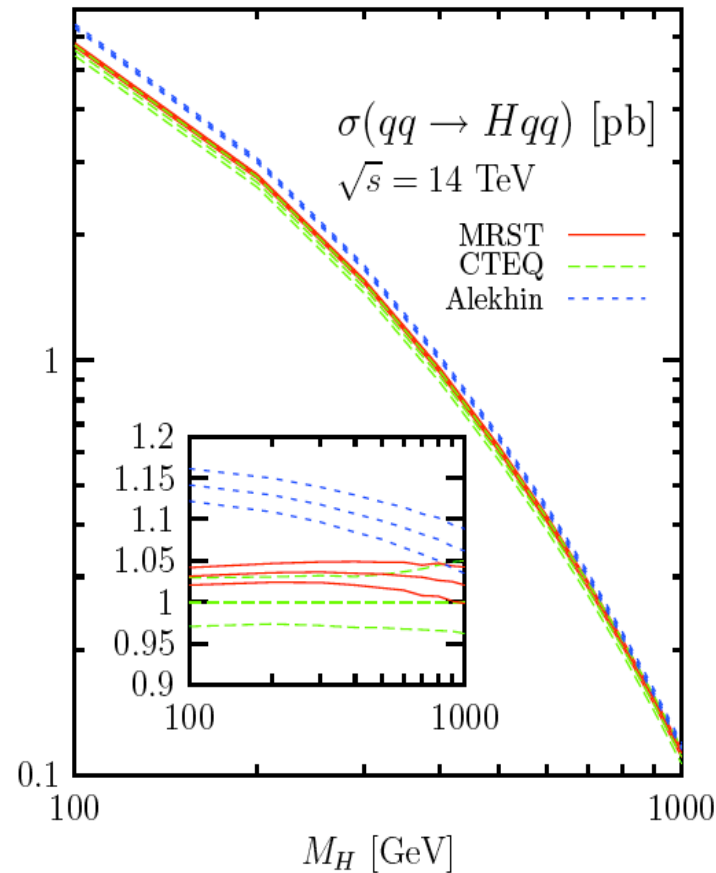
Difficult issues:

“model” uncertainties: parametrisation, flavour/sea-valence decompositions...

“unknown” systematics: “tensions” between data sets, tolerances

PDF errors determination

# Predictions for LHC, some examples



N.Adam et al.  
 arXiv:0802.3251

Total Theoretical Uncertainty (%)

| Uncertainty             | Cross-Section $\Delta\sigma$ | Acceptance $\Delta A$ |
|-------------------------|------------------------------|-----------------------|
| Missing $O(\alpha)$ EWK | $0.38 \pm 0.26$              | $0.96 \pm 0.21$       |
| Total QCD Uncertainty   | $1.51 \pm 0.75$              | $2.55 \pm 0.79$       |
| PDF Uncertainty         | 3.79                         | 1.32                  |
| Total Uncertainty       | $4.1 \pm 0.3$                | $3.0 \pm 0.7$         |

Various fits give incompatible results

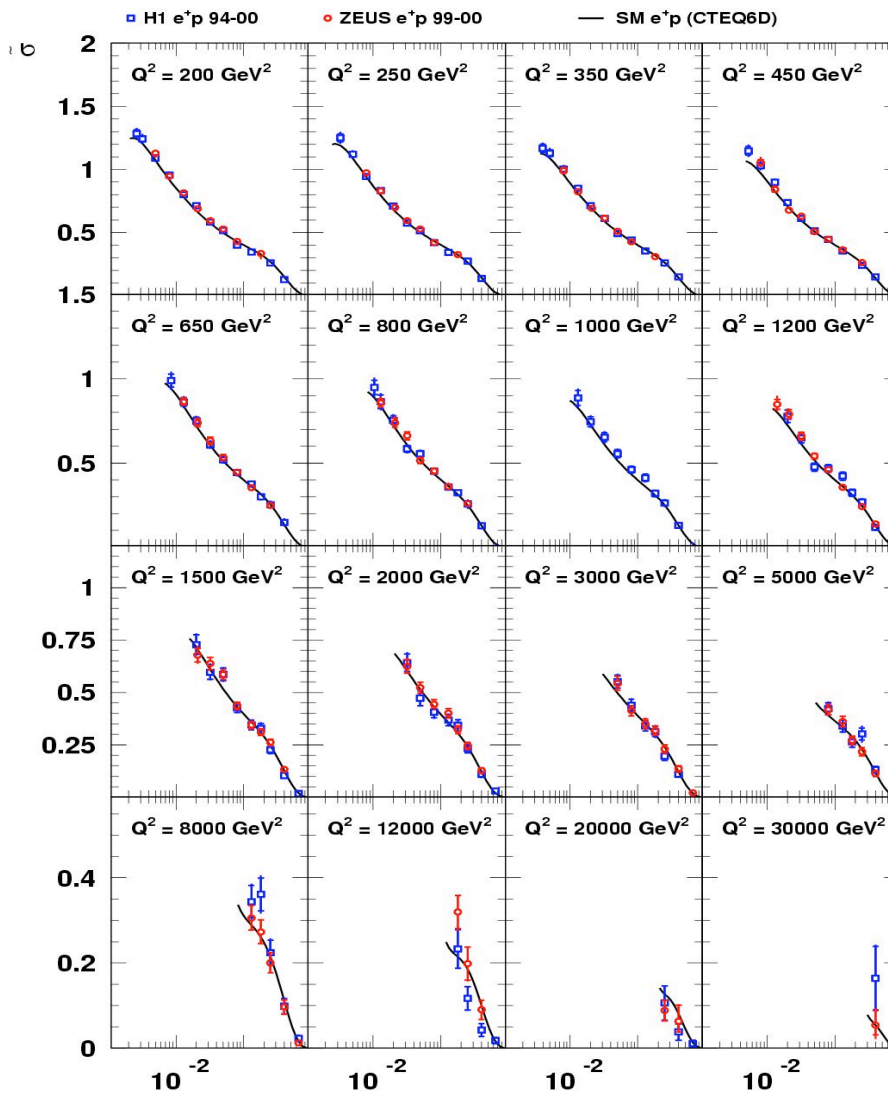
PDF error dominant for some standard signals

The variations in the  $P_T$  spectra due to PDF's can be limiting factor for non-resonant searches

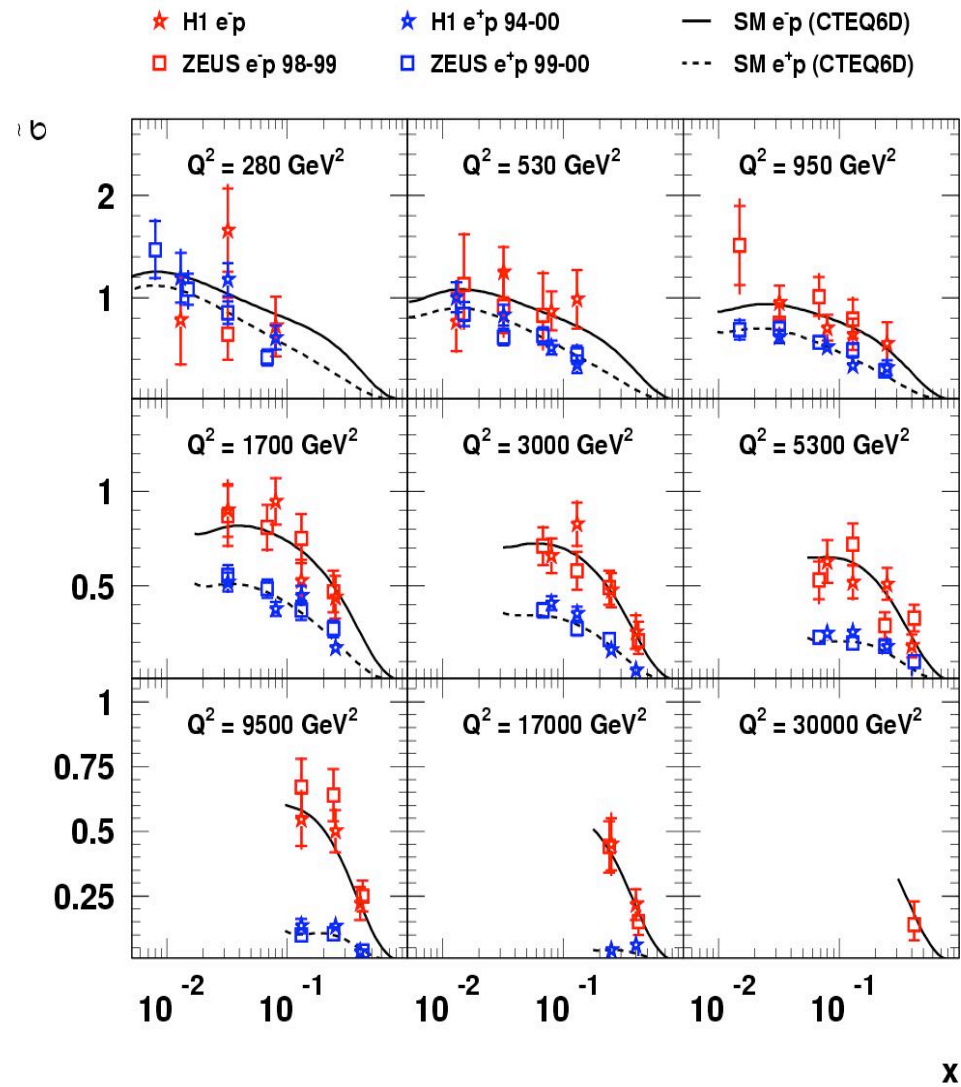
More precise data for PDF's is the best medicine =>

# DIS data from HERA

## HERA $e^+p$ Neutral Current



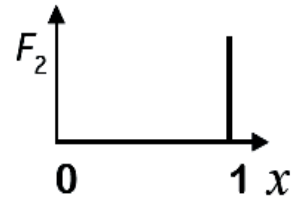
## HERA Charged Current



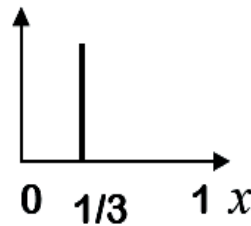
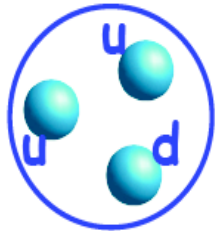
NC: precise and well in agreement with QCD

CC: provide flavour separation H1/ZEUS data used in pdf fits separately

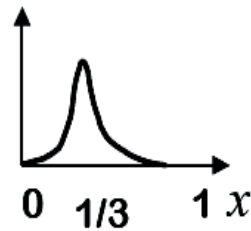
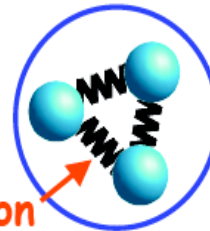
# Phenomenology of F2



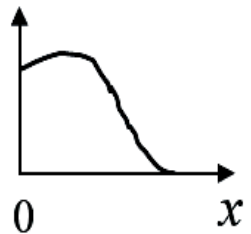
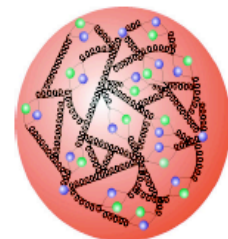
no substructure



3 free valence quarks



3 bound quarks



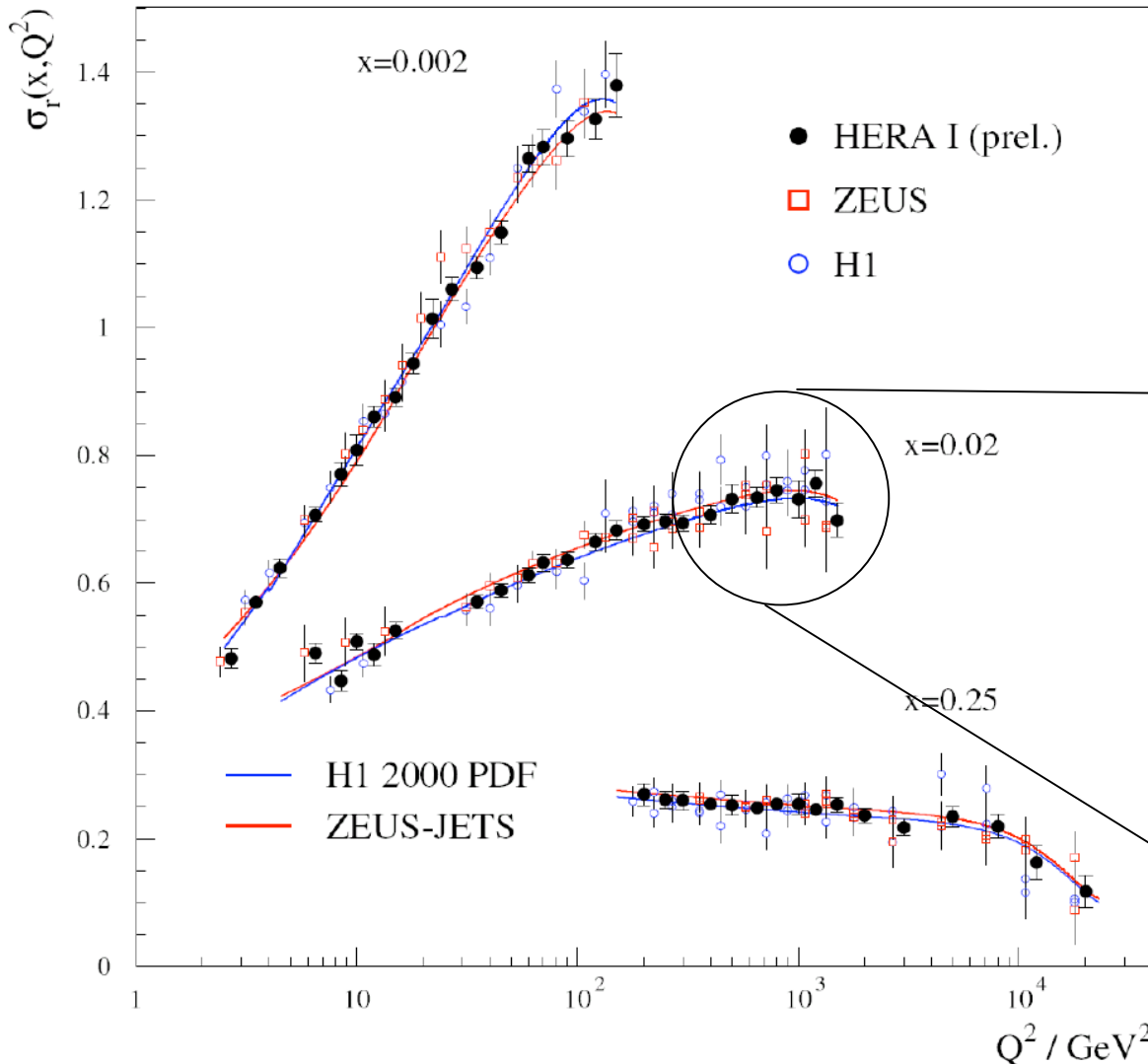
Valence quarks  
Sea quarks  
gluons

# H1-ZEUS cross section combinations

Coherent treatment of experimental effects in the average procedure (Lagrange multipliers method)

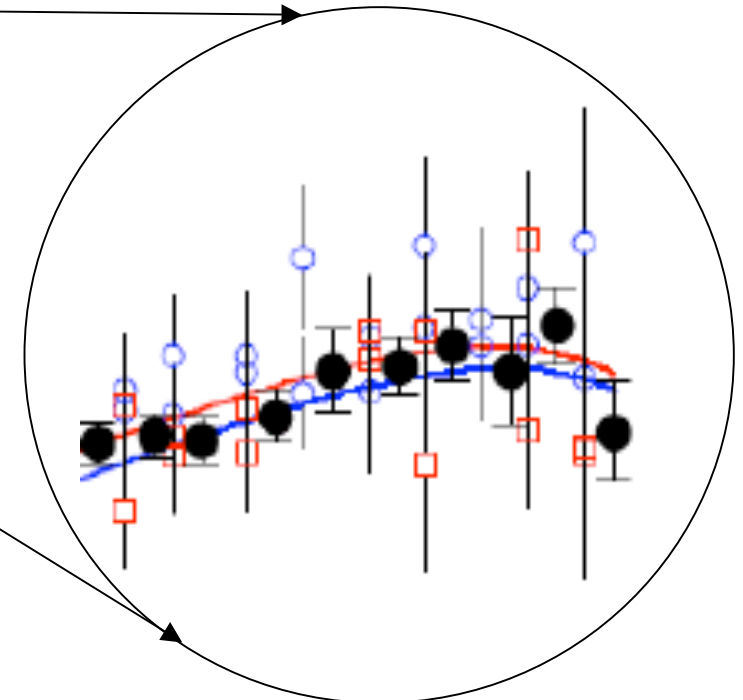
HERA I  $e^+p$  Neutral Current Scattering - H1 and ZEUS

$$\chi^2(\{F_2^{true}\}, \{\alpha\}) = \sum_i \frac{\left[ F_2^{i,true} - \left( F_2^i + \sum_j \frac{\partial F_2^i}{\partial \alpha_j} \alpha_j \right) \right]^2}{\sigma_{F_2}^2} + \sum_j \frac{\alpha_j^2}{\sigma_{\alpha_j}^2}$$



1153 individual NC/CC (HERA I data) averaged to 554 points

HERA Structure Functions Working Group



Improvements beyond the naively-expected  $\sqrt{2}$ : “cross calibration”

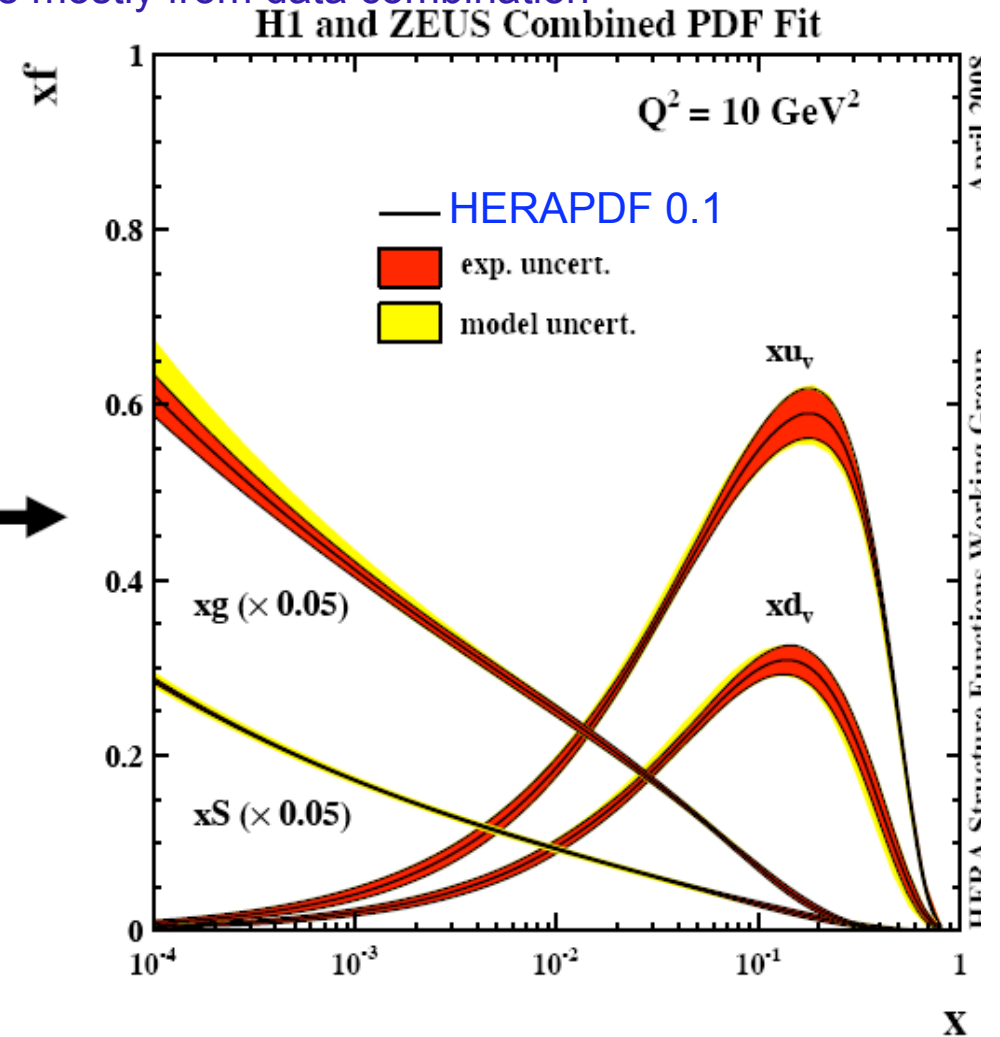
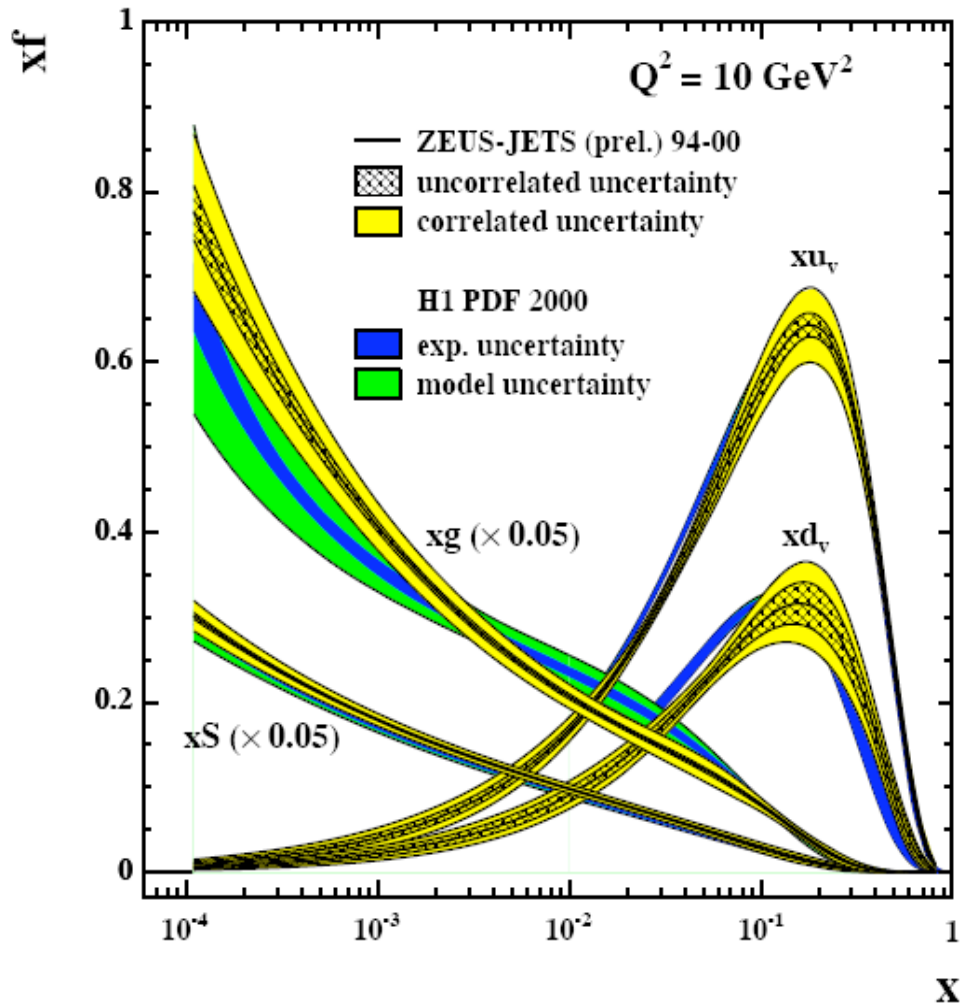
# The common fit of the combined HERA I data

Partons parametrized at  $Q_0^2 = 4 \text{ GeV}^2$  (Data  $Q^2 > 3.5 \text{ GeV}^2$ )

Experimental+Model uncertainties taken into account

Errors of the fit estimated using  $\Delta\chi^2=1$

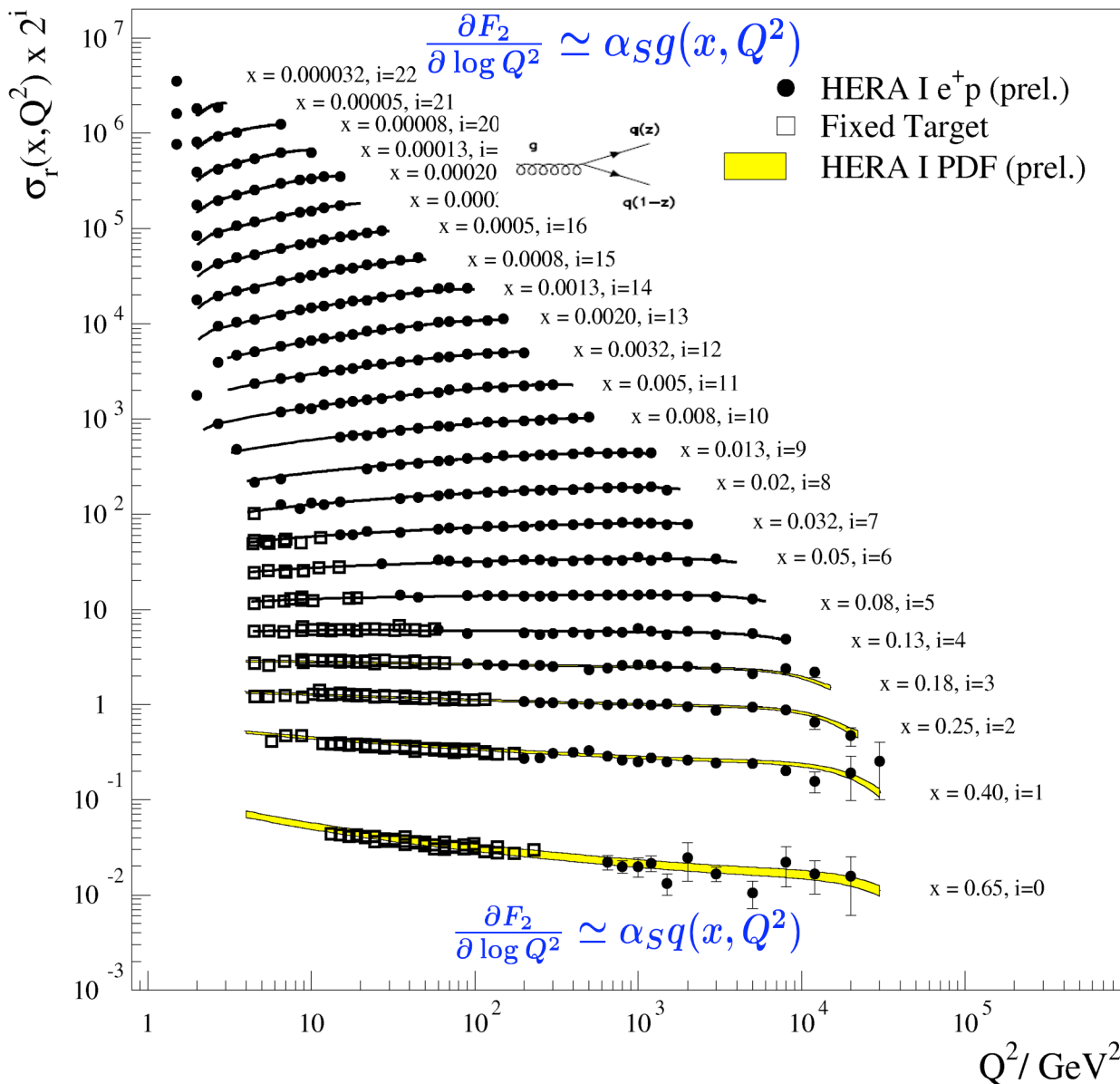
Improvement in precision is visible, originate mostly from data combination





# The combined data compared to the fit

## H1 and ZEUS Combined PDF Fit



April 2008

$$\tilde{\sigma}_{NC}^{\pm} = \frac{d^2 \sigma_{NC}^{e^{\pm}p}}{dx dQ^2} \frac{xQ^4}{2\pi\alpha^2 Y_+}$$

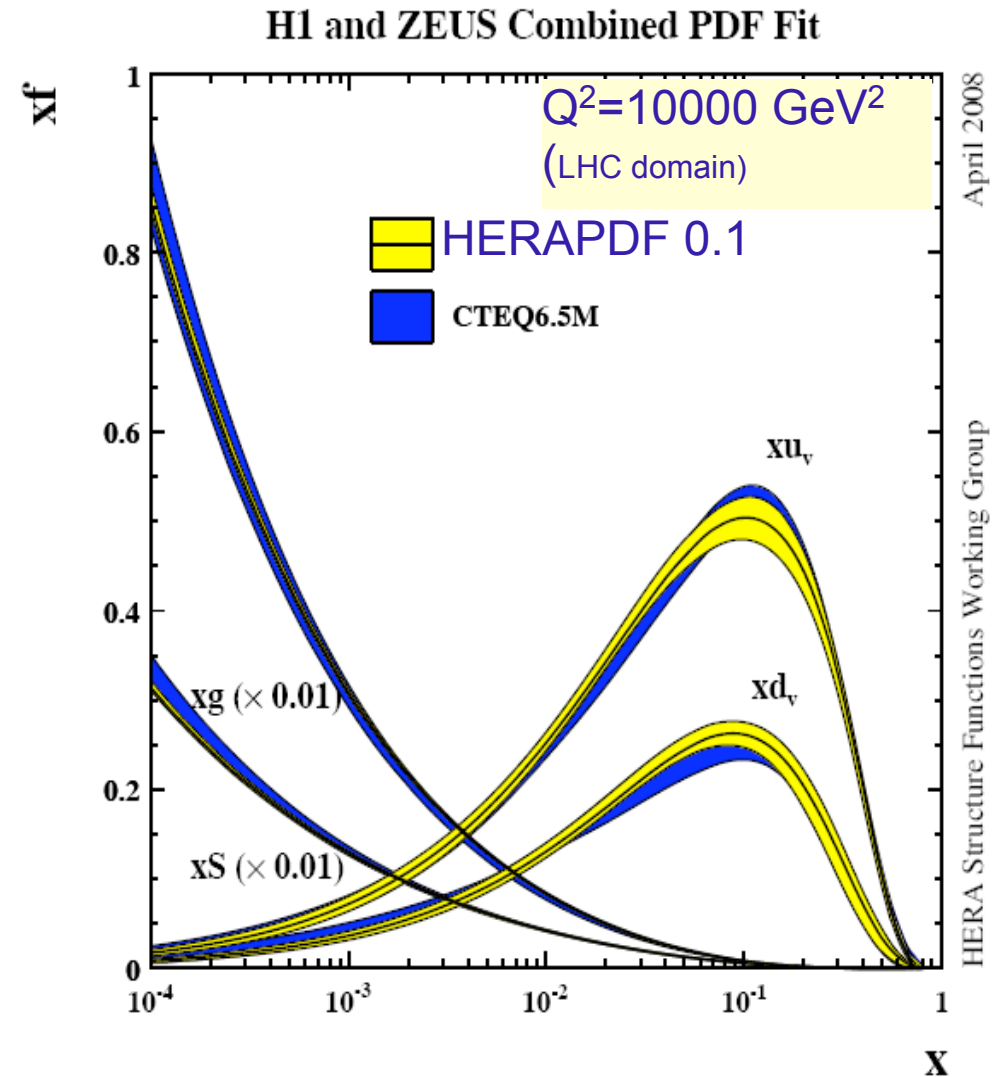
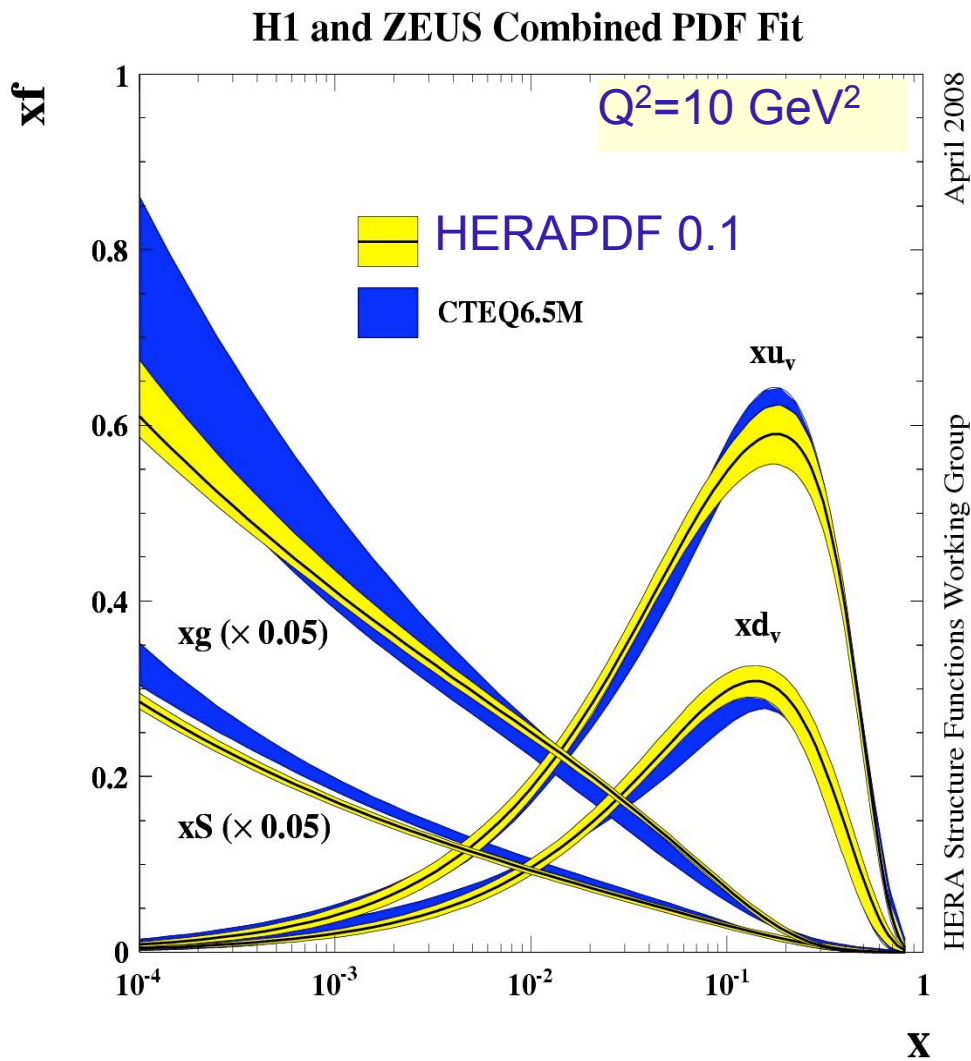
Precise data in the scaling violations regions (gluon)

Coherent data sets combined: vast coverage of the proton "map"

Dramatic increase in precision

HERA Structure Functions Working Group

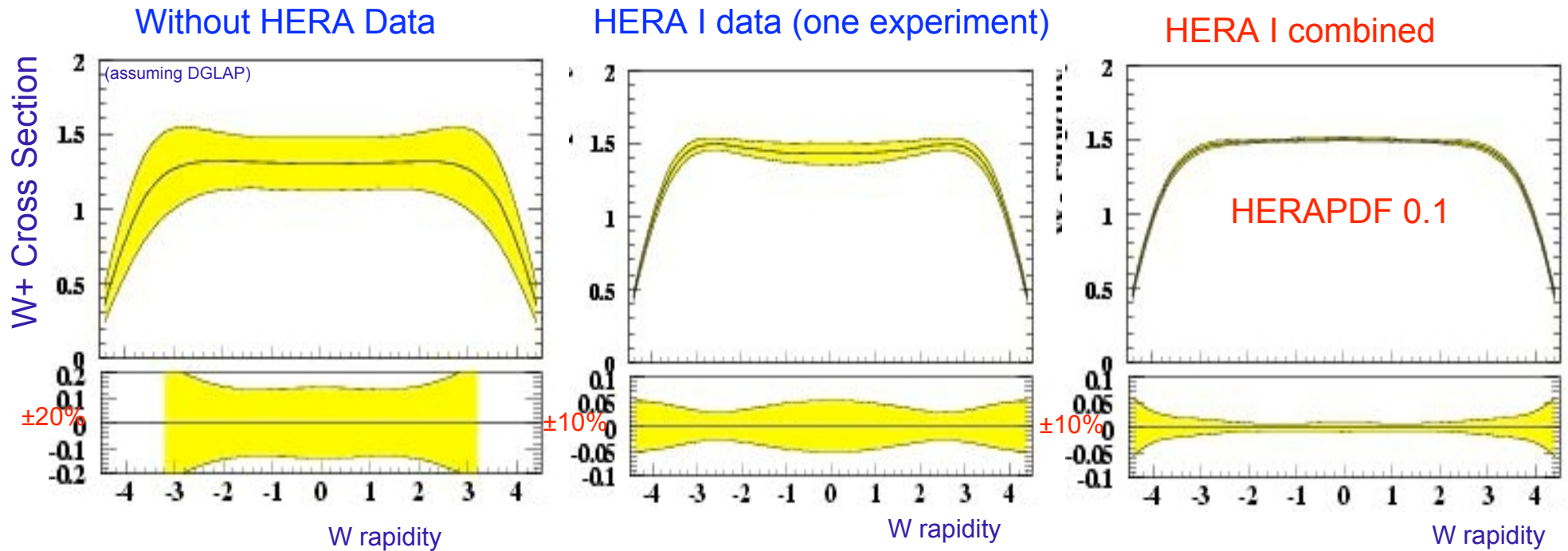
# Side by side with global fits



Improvement most notably at low x  
The data precision is driving the improvement  
Treatment of errors and parametrisation issues

# Predictions for W/Z boson production at LHC

A.Cooper-Sarkar and E.Perez



Only the fit uncertainty shown here, no model variations  
The step in experimental precision is significant  $\sim 2\%$

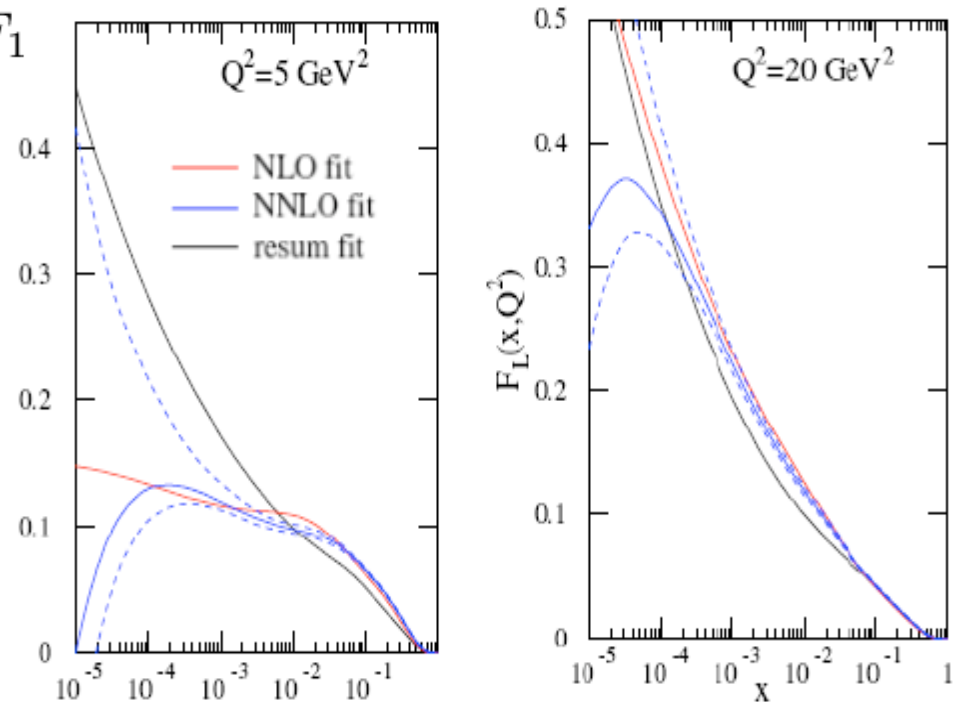
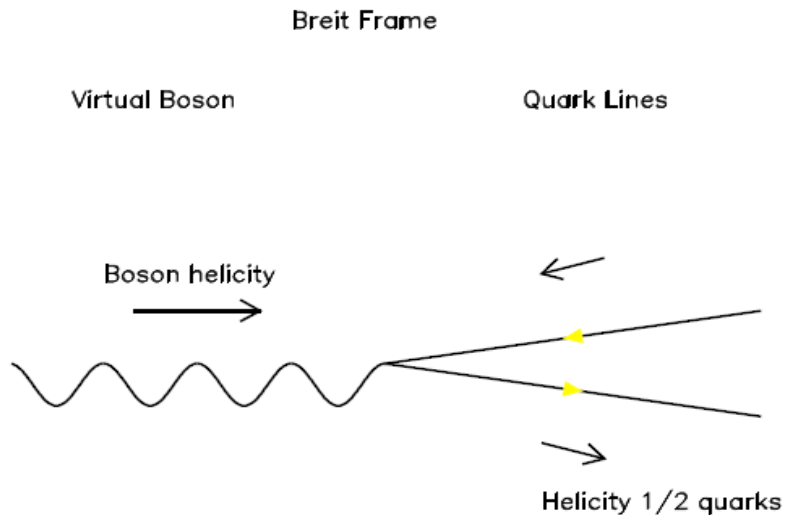
More data to be included (low  $Q^2$ , bulk, HERA II data high  $x/Q^2$ ) => ultimate precision

# Longitudinal Structure Function $F_L$

$$\sigma_r = F_2(x, Q^2) - \frac{y^2}{Y_+} \cdot F_L(x, Q^2)$$

$$R = \sigma_L / \sigma_T = (F_2 - 2xF_1) / 2xF_1 = F_L / 2xF_1$$

=0 for spin 1/2 partons in QPM  
(Callan-Gross)



R.Thorne, DIS08

$$F_L(x, Q^2) \sim \alpha_s x g(x, Q^2)$$

Altarelli, Martinelli, 1978

Fundamental form factor of the proton  
Proportional to the gluon, important for PDF's  
Discriminate between theoretical approaches

# Direct $F_L$ measurement

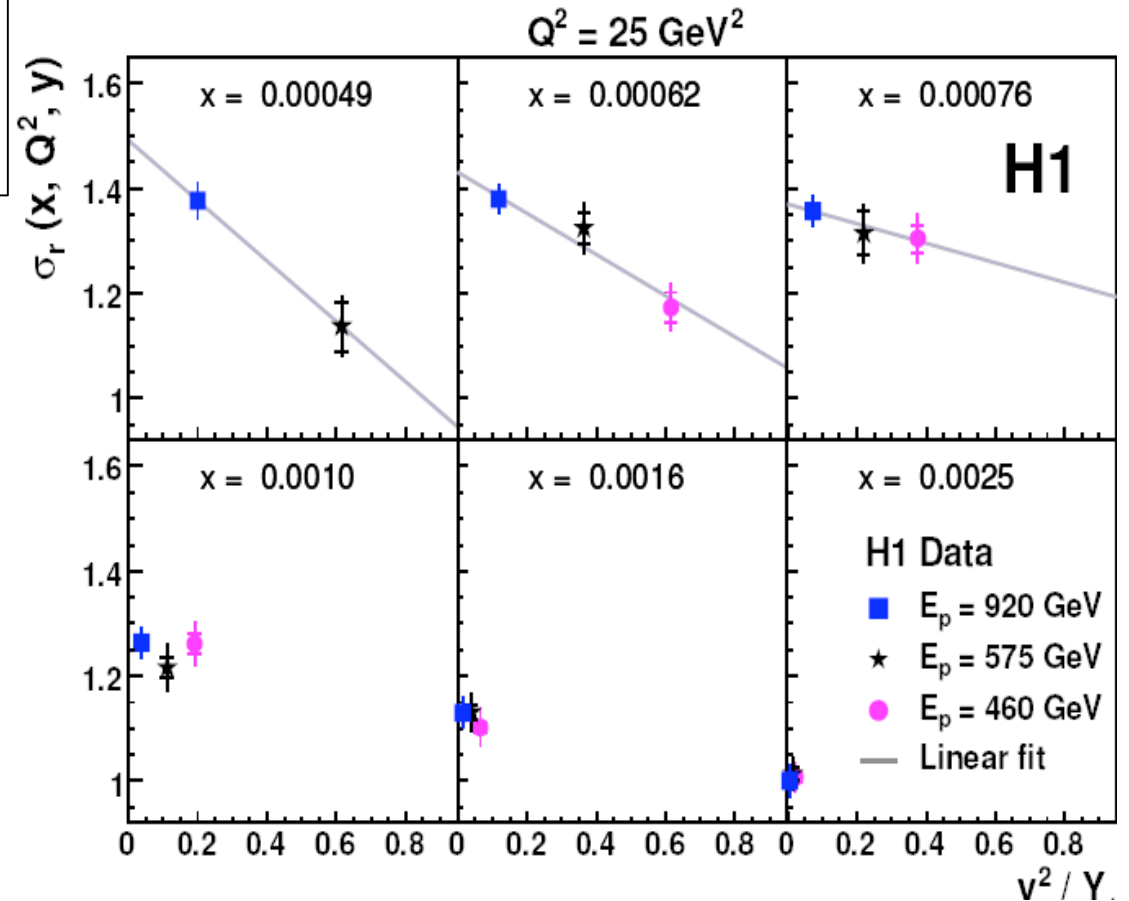
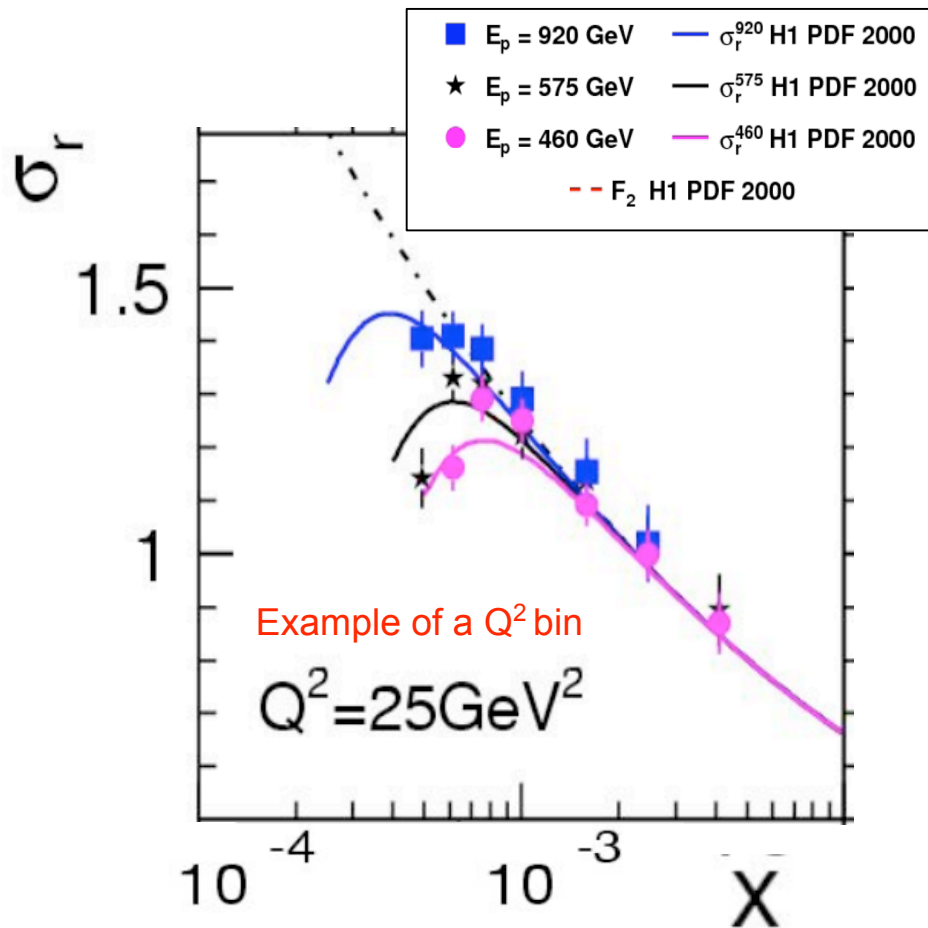
Method:

keep  $x, Q^2$  constant, vary  $y$ :  $ys=y's'=Q^2/x$

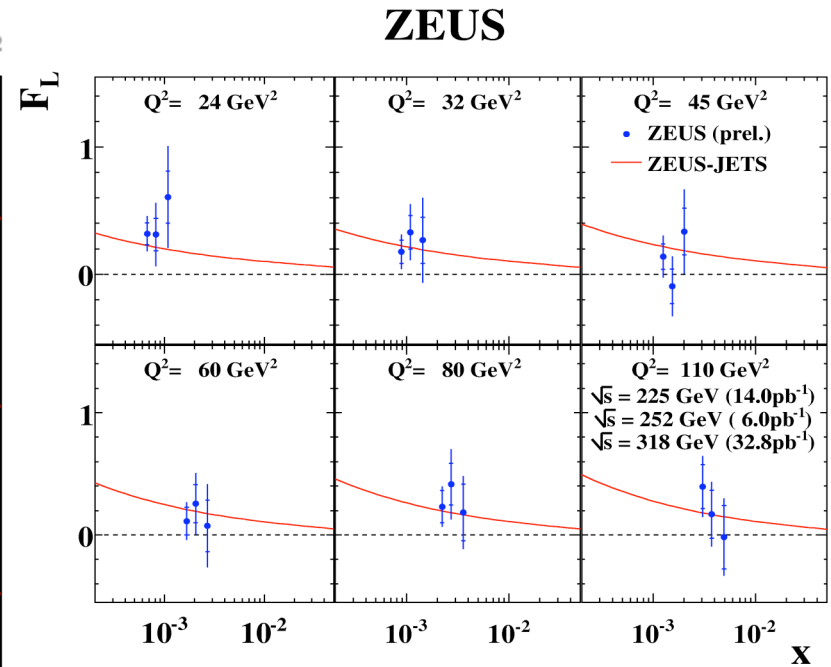
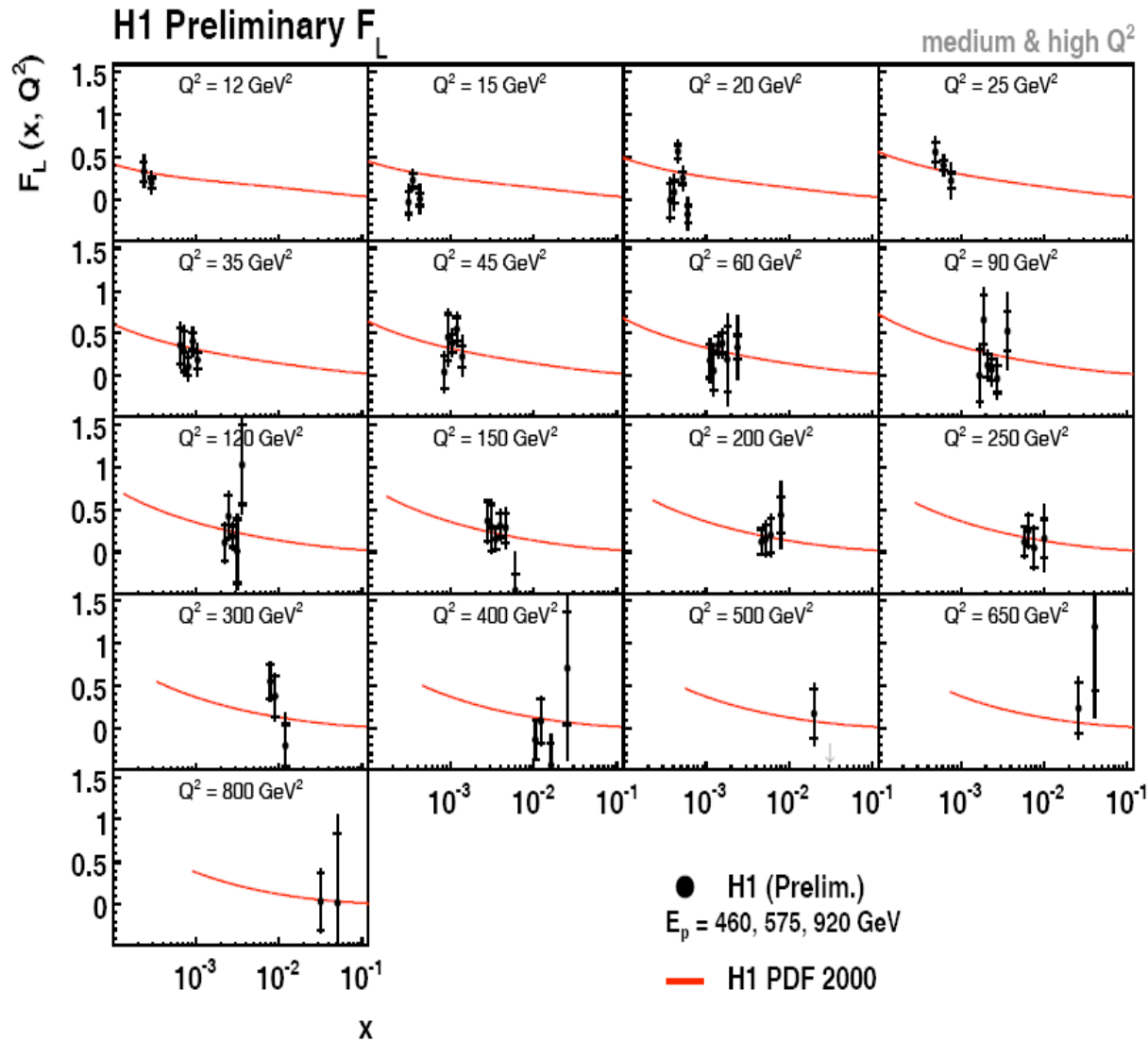
Vary  $s$  : Special Runs  $E_p=460,575$  GeV

$$F_L \sim C(y) * (\sigma(E_p^1) - \sigma(E_p^2))$$

$$\sigma \sim F_2(x, Q^2) + f(y) F_L(x, Q^2)$$

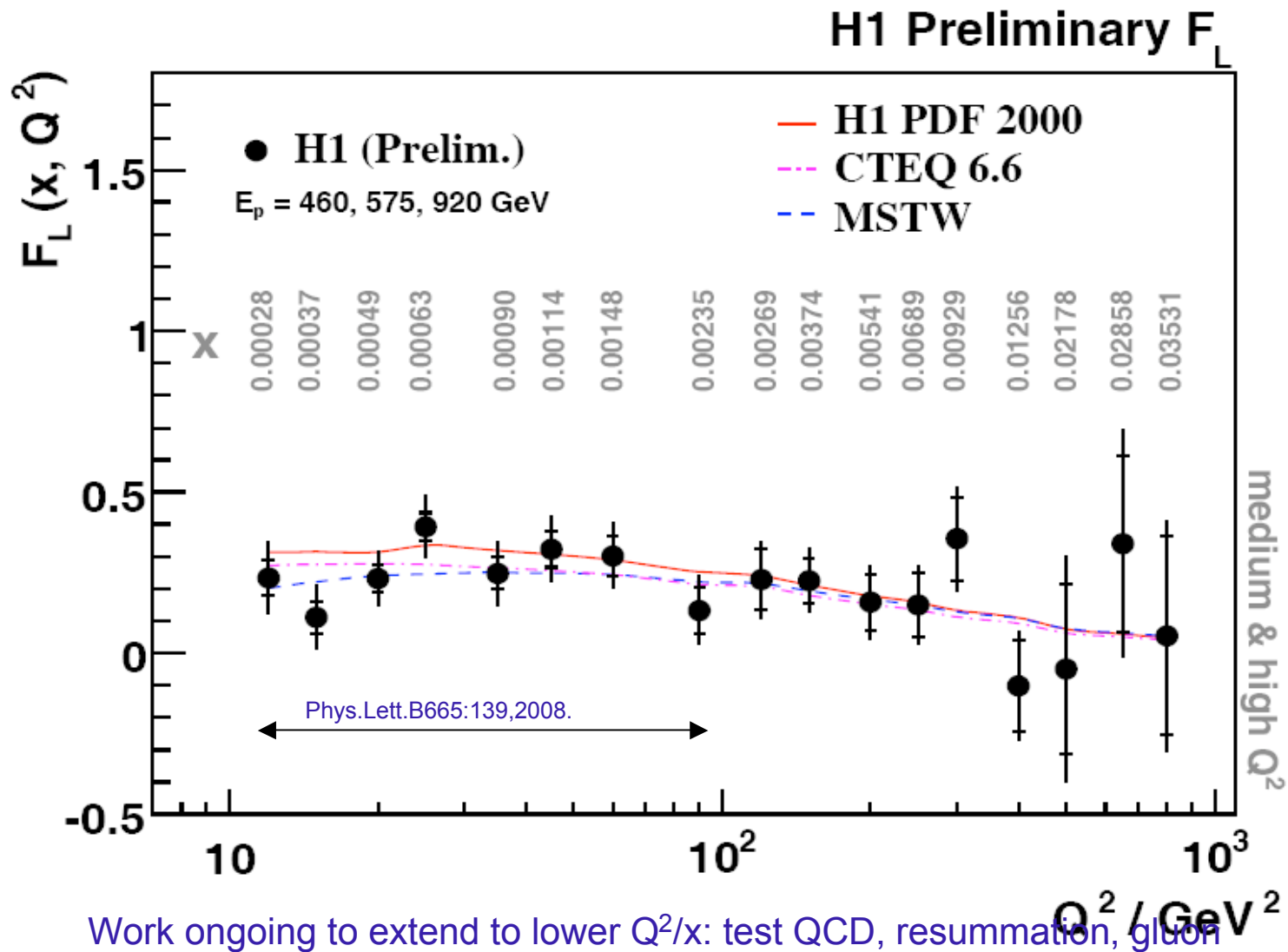


# Direct $F_L$ measurement



Measurements compatible with QCD predictions

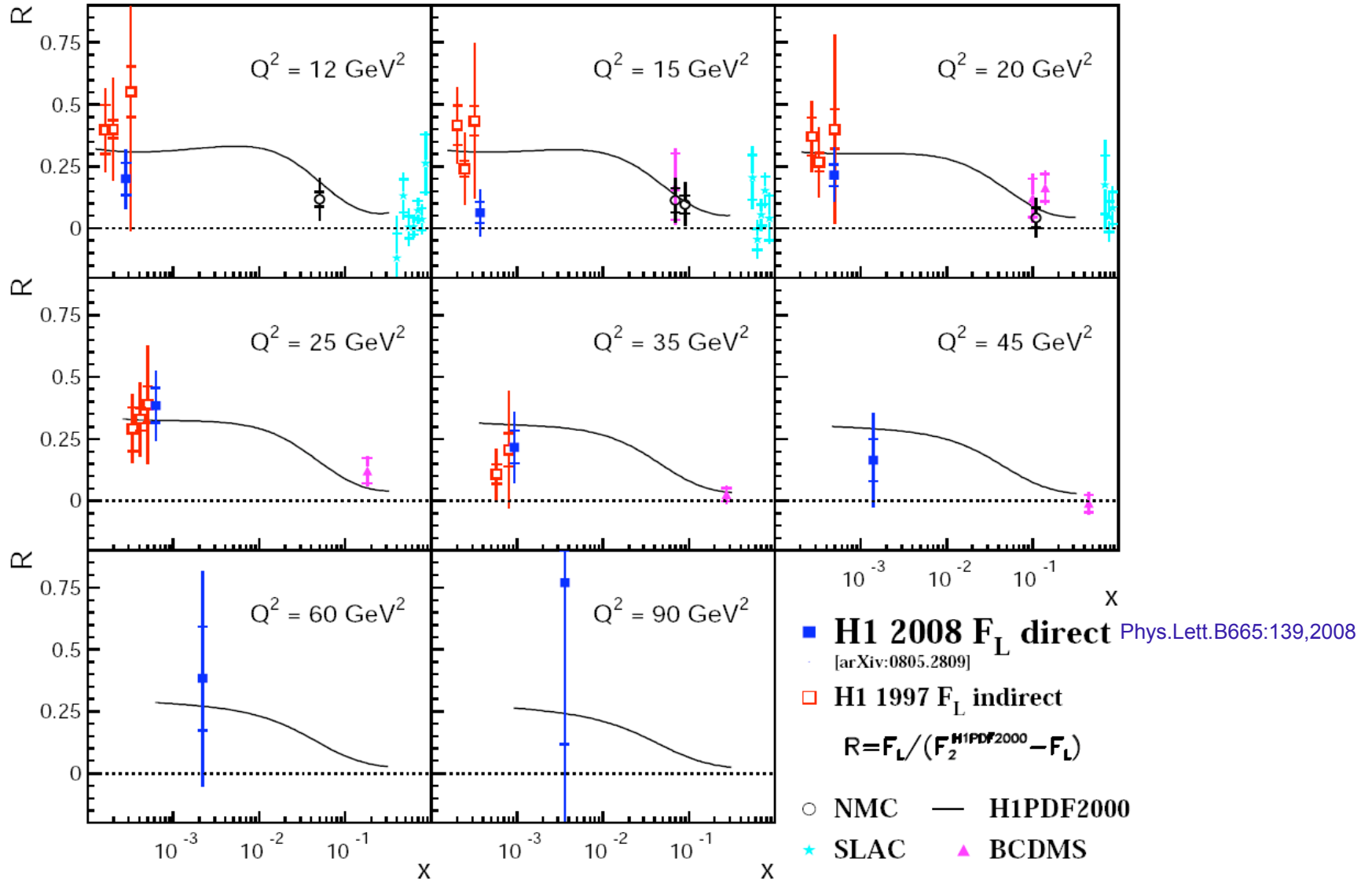
# $F_L$ averaged in each $Q^2$ -bin



# Comparison with target data and indirect determinations

The gluon “turn-on” at low x clearly visible

$Q^2$  range  
of the first  
publication  
“medium  $Q^2$ ”

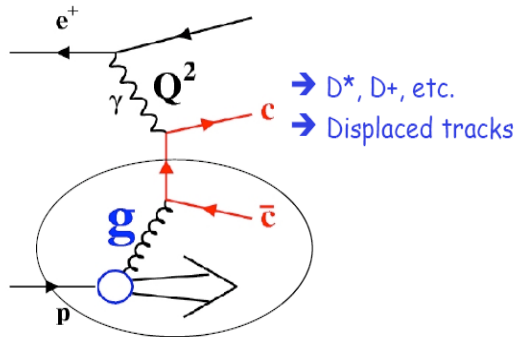




# Proton's charm

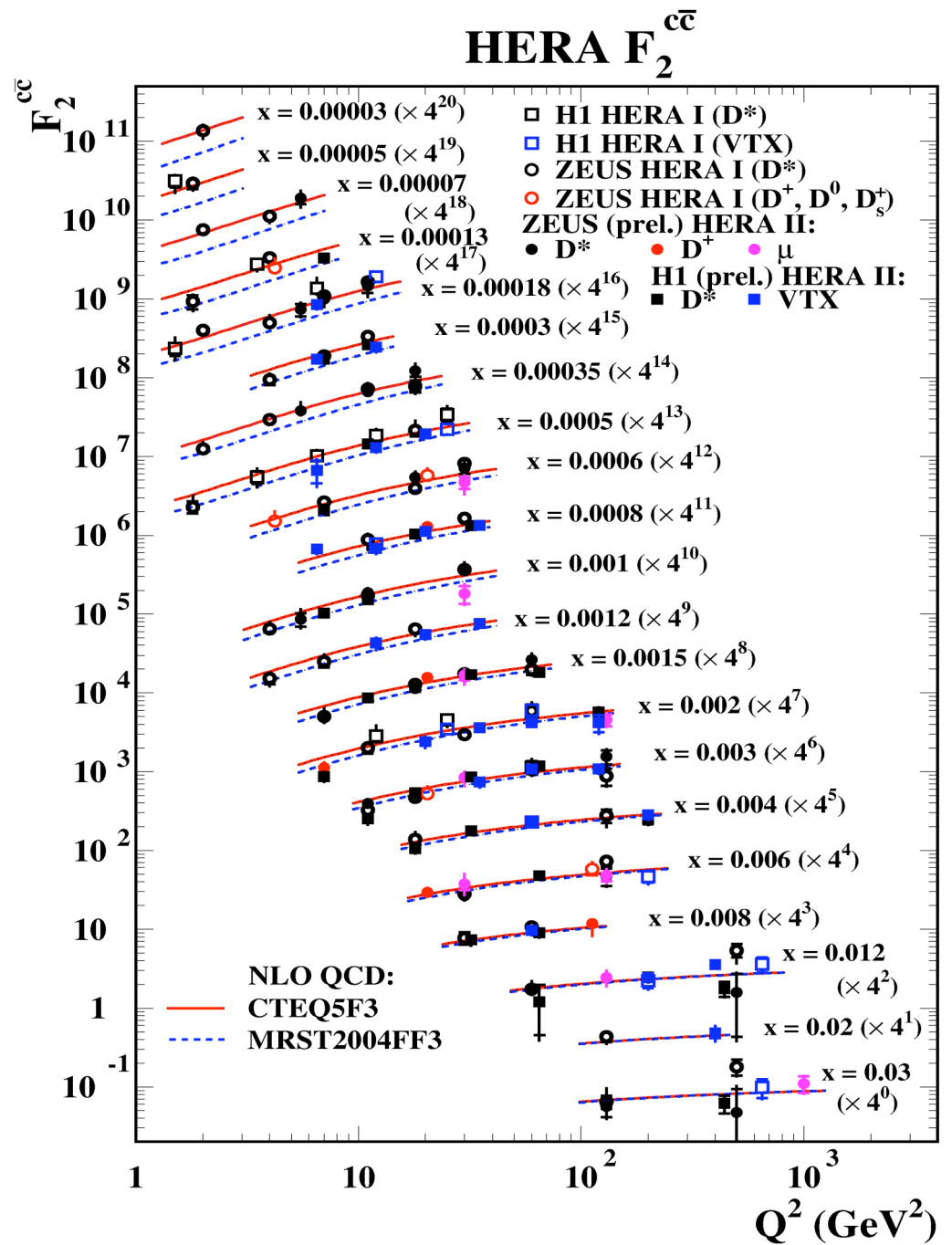
$$\sigma_r^{cc/bb} = F_2^{cc/bb} - y^2/Y_+ F_L^{cc/bb}$$

Tags: D\*, lifetime  
 But more QCD into the game  
 Fortunately, large quark mass helps



Produced via boson-gluon fusion  
 sensitivity to the gluon

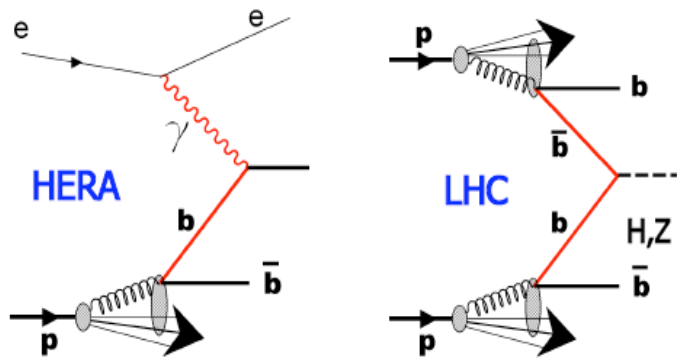
Precision to 5% (or less) possible  
 Theory has to follow  
 (mass schemes, NLO etc, )  
 especially visible for  $Q^2 \leq m_c^2$



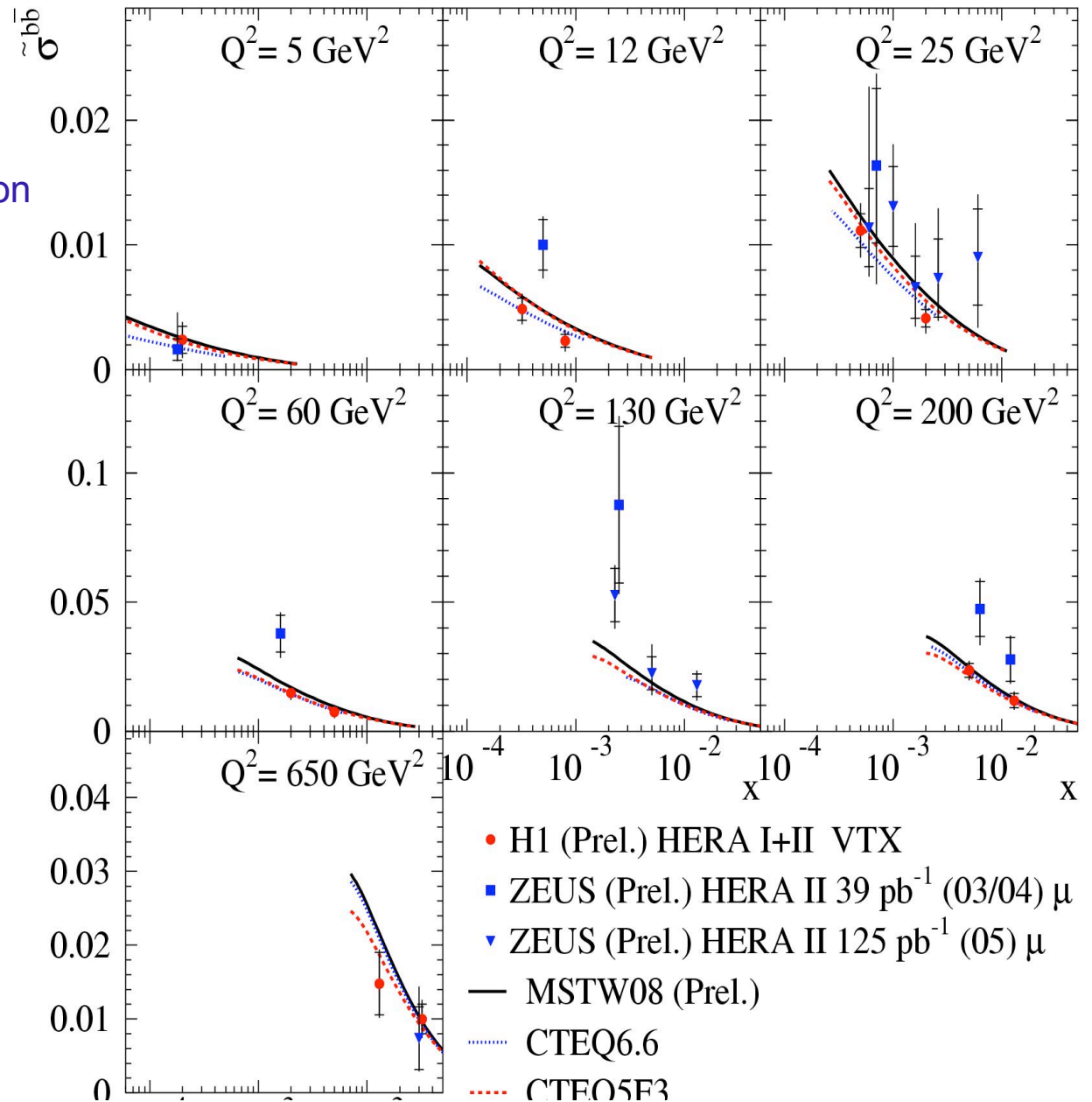
# Proton's beauty

HERA II data with lifetime methods  
 More data available for ultimate precision

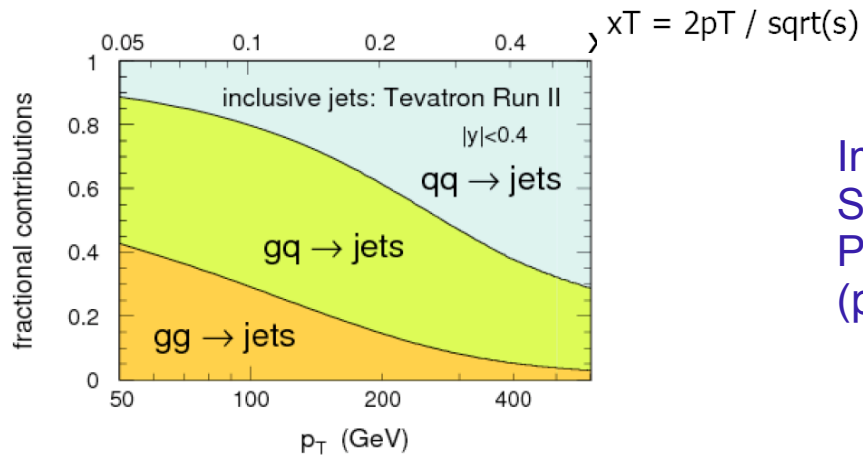
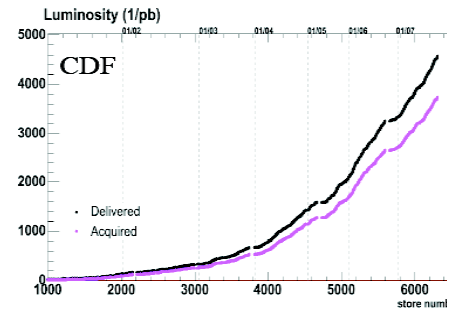
Flavour control in PDF is crucial  
 for some aspects of the LHC physics



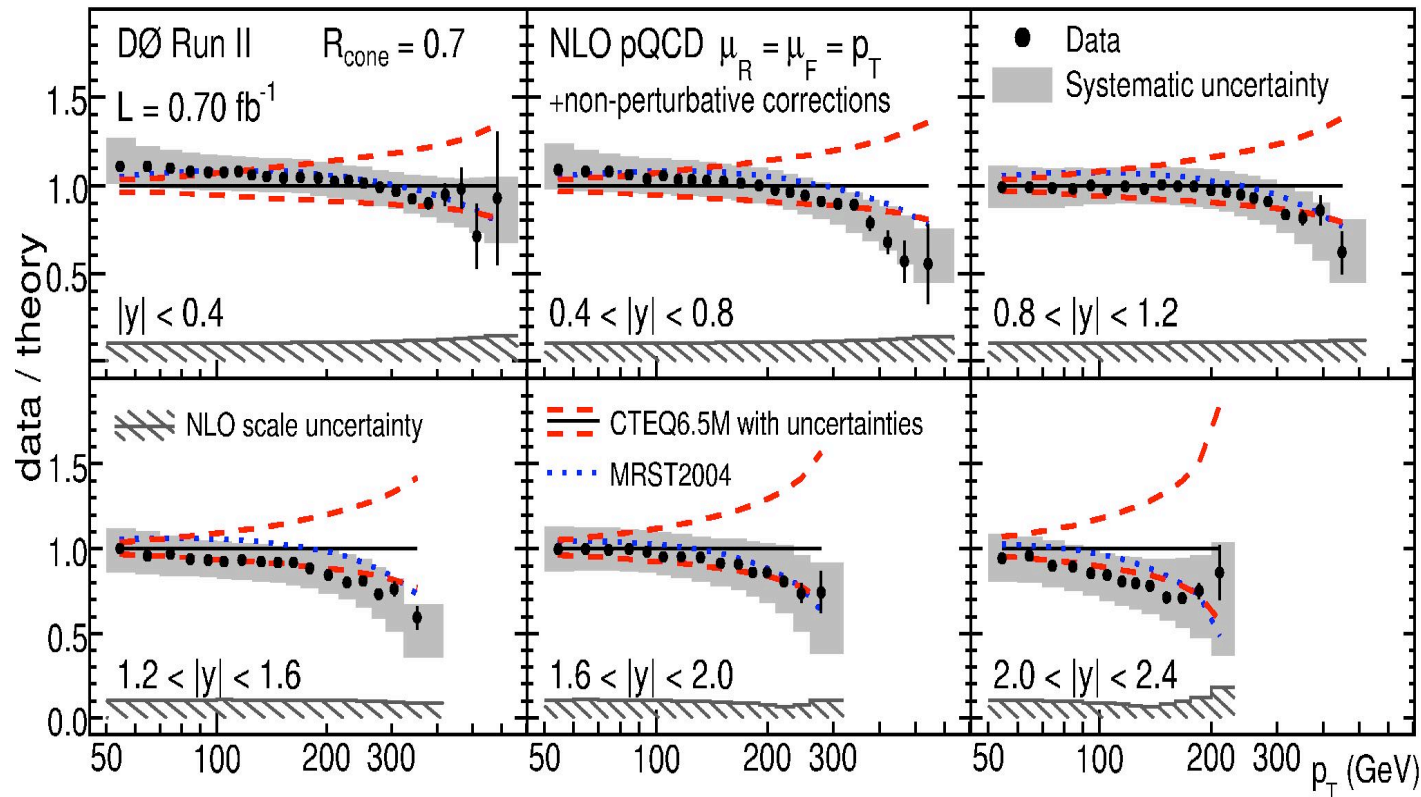
## H1+ZEUS BEAUTY CROSS SECTION in DIS



# Jets production at Tevatron



Impressive achievement in energy scale control (1%)  
 Sensitive to gluon at high x  
 Precision with present global fits  
 (partially) Included in MSTW, more to come

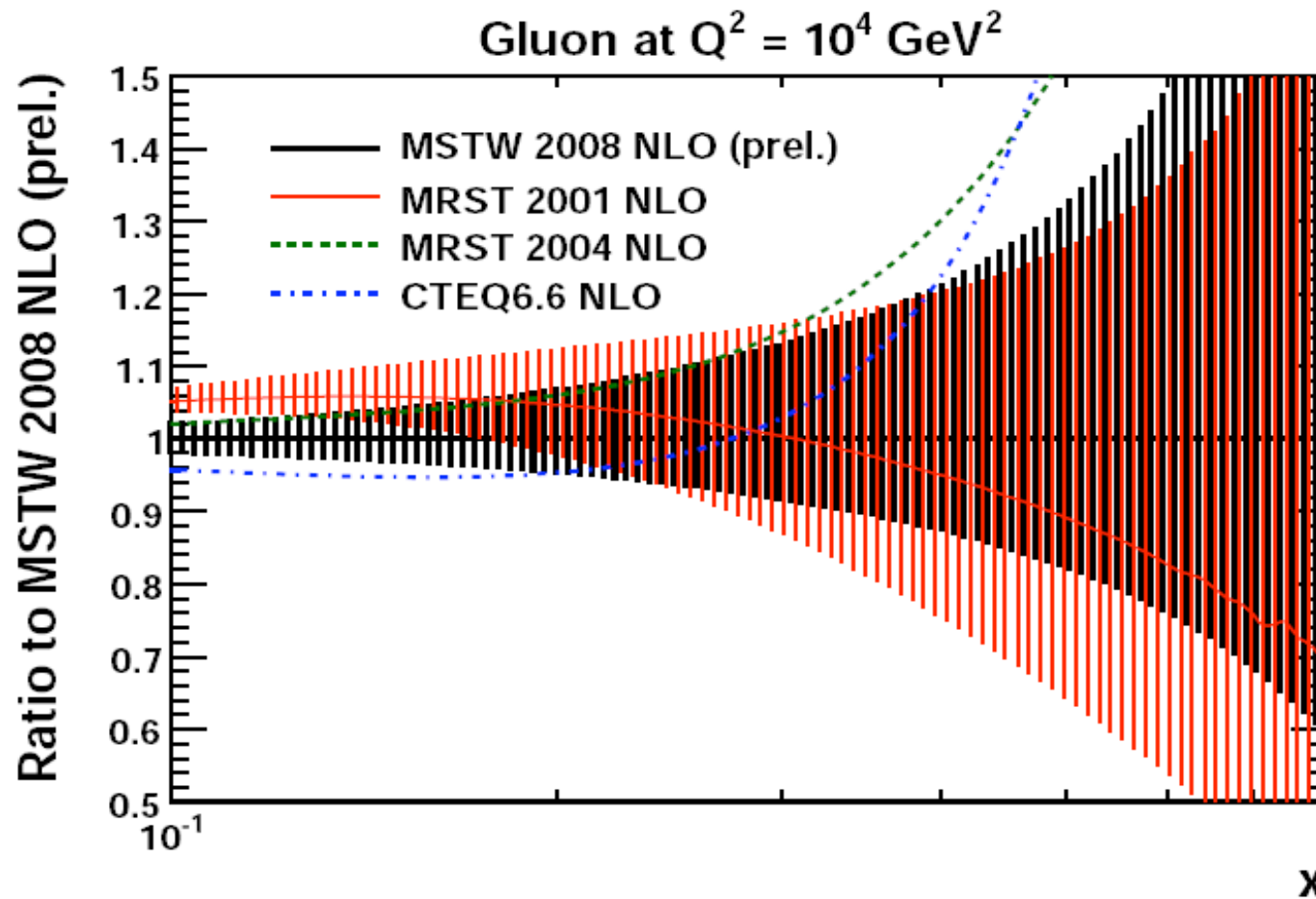


Similar study by CDF  
 Consistent data  
 to be included in the fit

# Impact of the high $E_T$ jet data on gluon at high $x$

MSTW 2008 analysis

G. Watt, DIS 2008



New data prefer smaller gluon at high  $x$

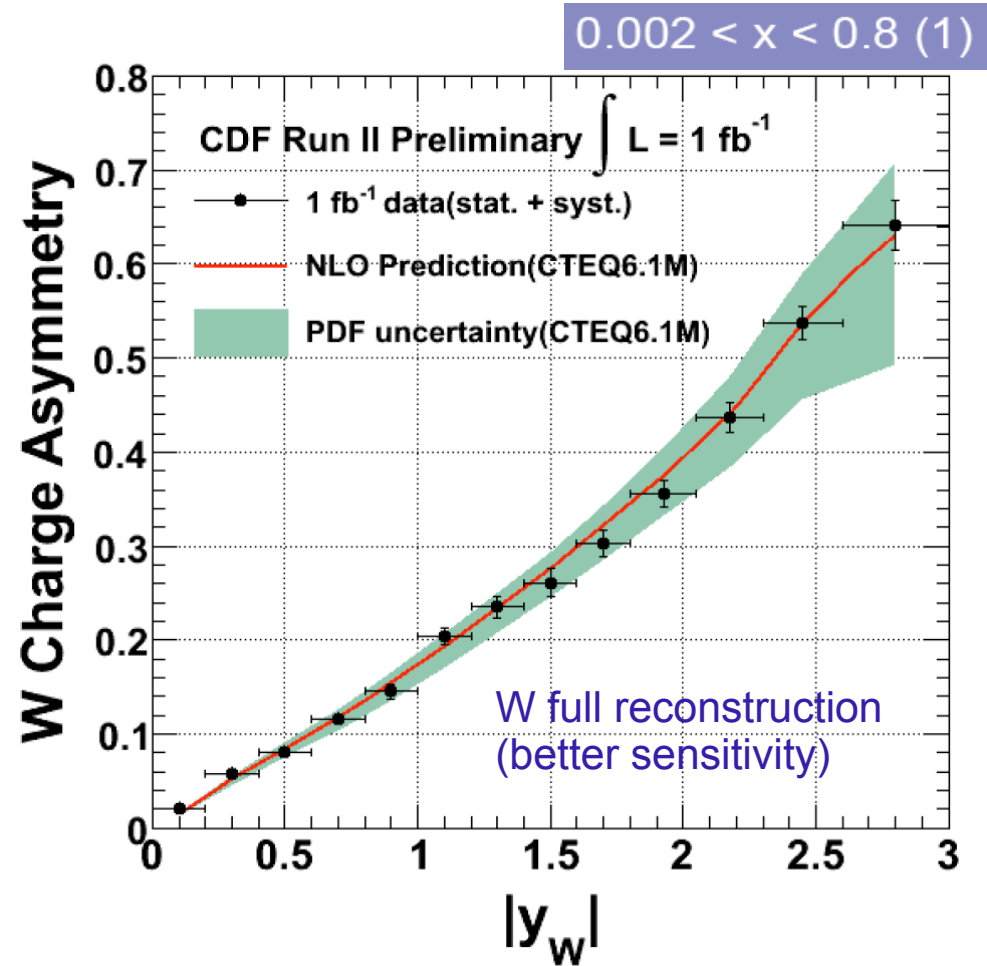
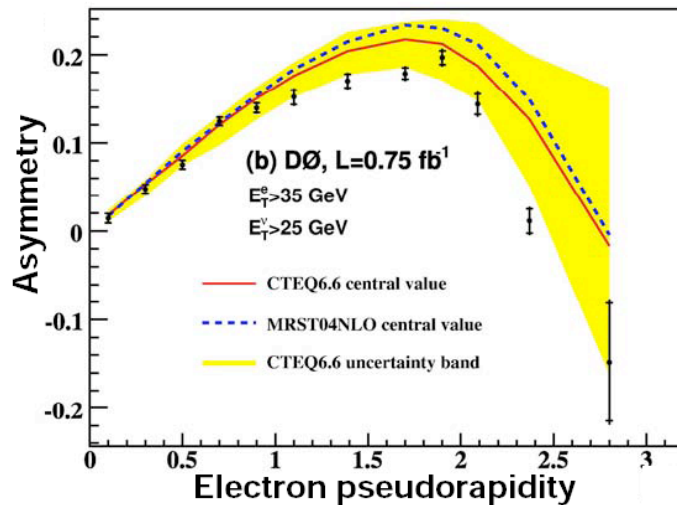
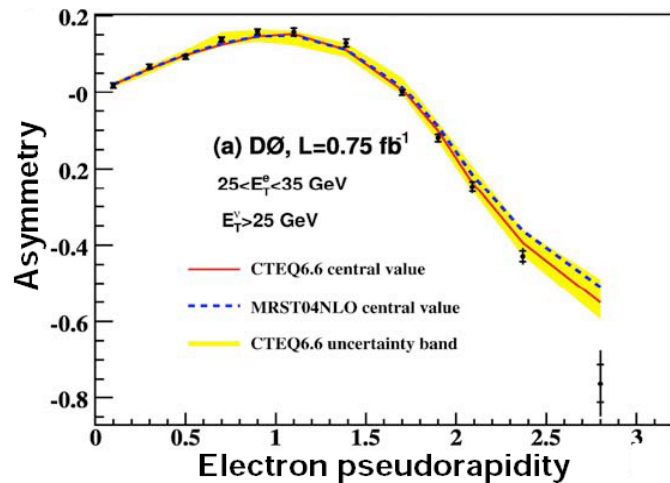
# W asymmetry at Tevatron

$$Q^2 \approx M_W^2, \quad x_{1,2} = \frac{M_W}{\sqrt{s}} e^{\pm y_W}$$

$$A_W(y) = \frac{d\sigma(W^+)/dy - d\sigma(W^-)/dy}{d\sigma(W^+)/dy + d\sigma(W^-)/dy} \approx \frac{u(x_1)d(x_2) - d(x_1)u(x_2)}{u(x_1)d(x_2) + d(x_1)u(x_2)}$$

$$x_{1,2} = x_0 \exp(\pm y), \quad x_0 = \frac{M_W}{\sqrt{s}}$$

New electron data, in ET bins



Promising precision for u/d ratio at high x

# HERA II results with polarized beams

HERA can run with  $e^\pm$   
and both e-beam polarisations ( $P=0.25-0.4$ )

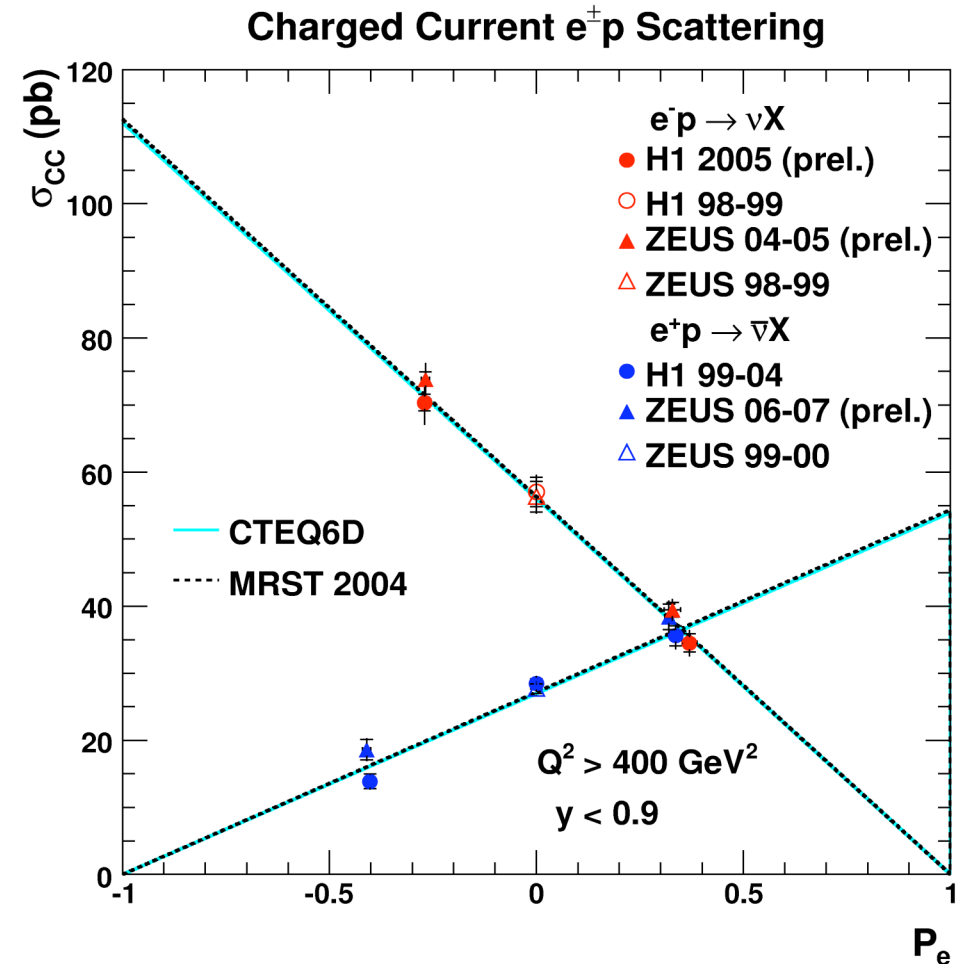
$$\sigma^{e^\pm p}(\mathbf{P}) = (\mathbf{1} \pm \mathbf{P})\sigma_{\mathbf{P}=0}^{e^\pm p}$$

CC: linear dependence established in  
DIS at HERA

Compatible with V-A structure  
(no RH currents)

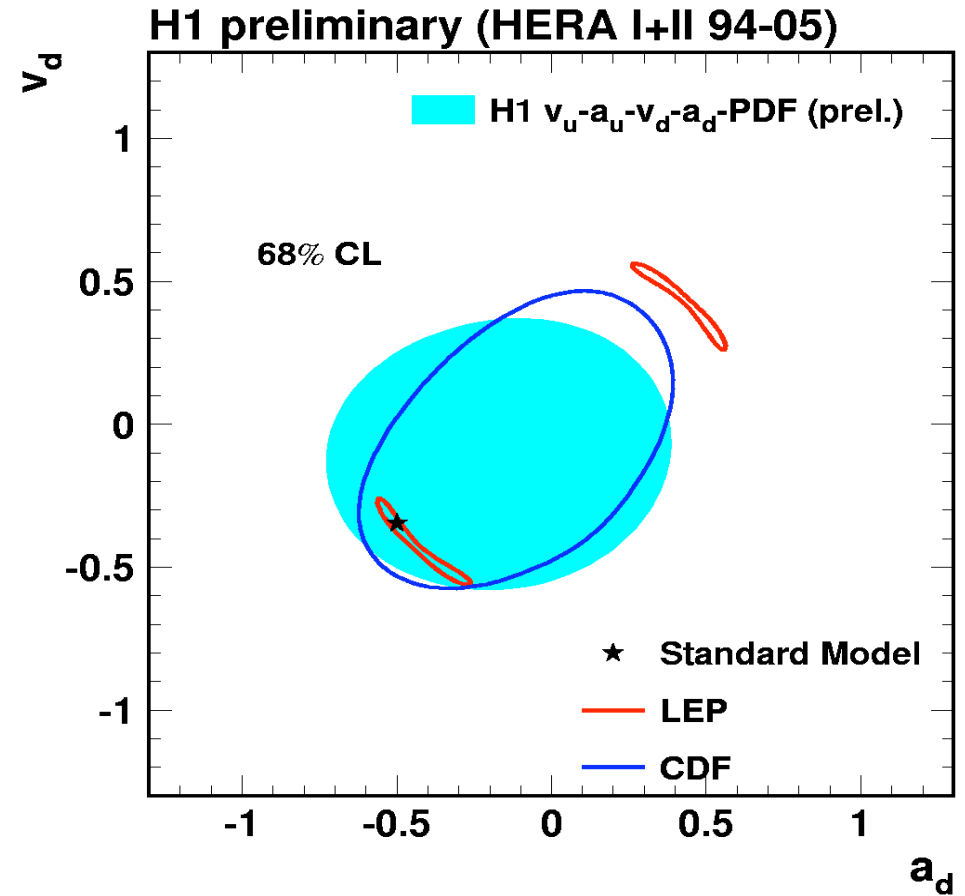
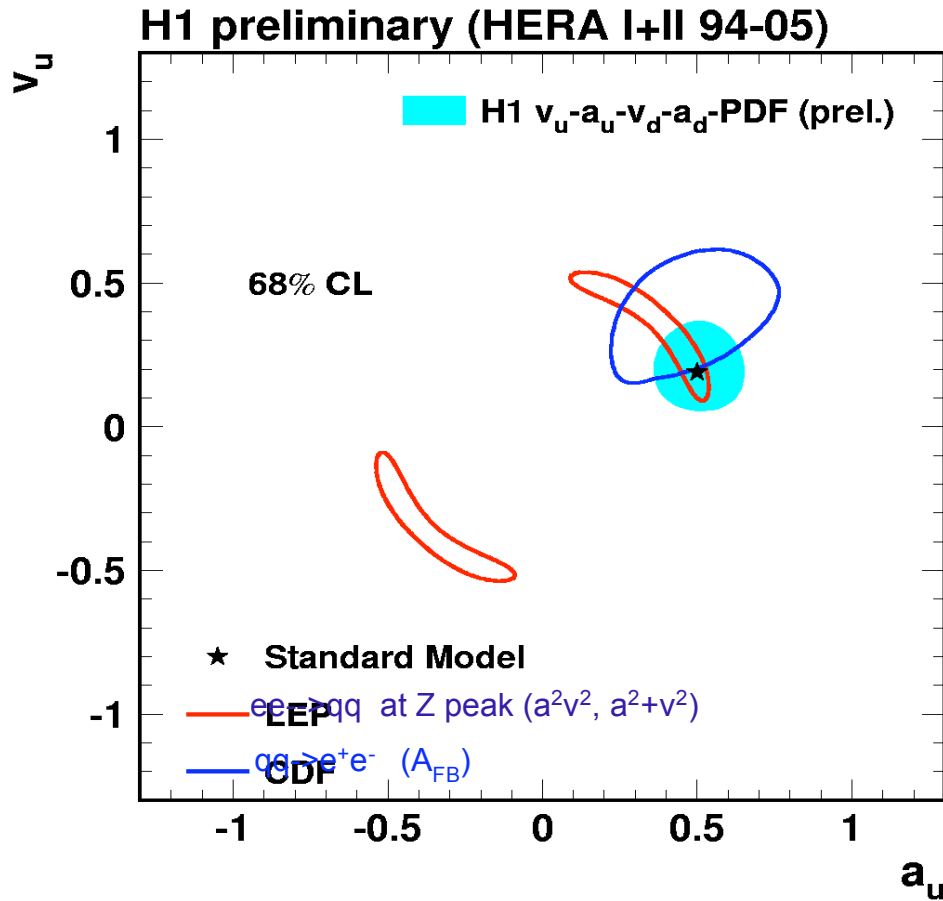
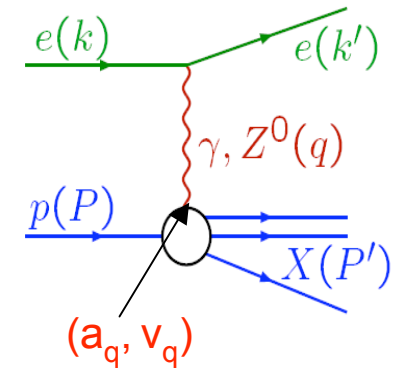
CHARM (1979):  
 $\nu_\mu N \rightarrow \mu X$

It may be concluded that positive muons produced  
by interactions of high-energy antineutrinos with  
nuclei have a longitudinal polarization oriented along  
their momentum direction. Within the experimental

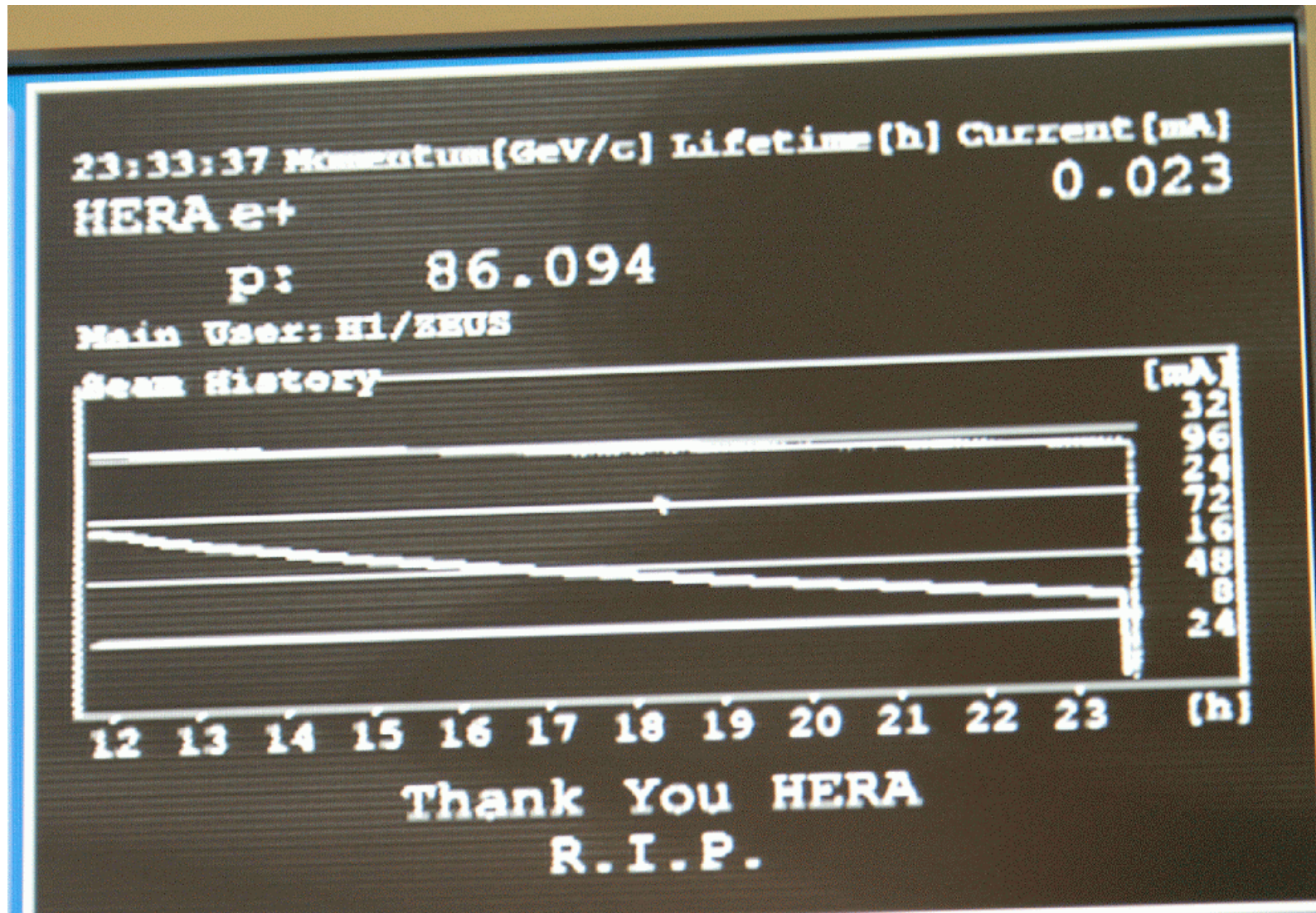


# Light quark couplings to Z

NC/CC data => full QCD/EW Fit: PDF's+light quarks couplings  
 Now taking advantage of polarisation @HERA II : **new fit**



## HERA end of run: June 30, 2007, 23h30

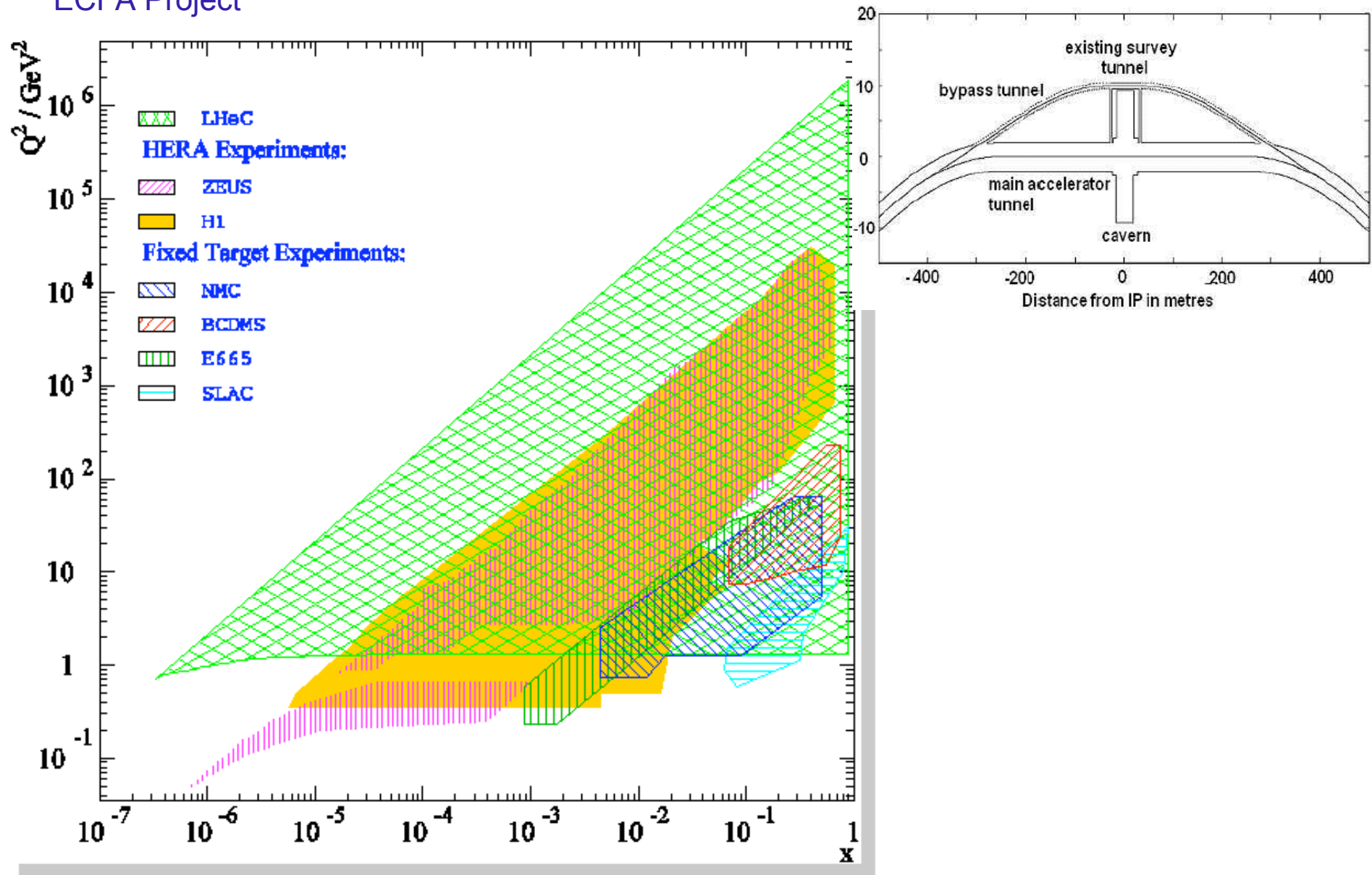


It will take a few more years to fully analyse the data...



# LheC e(70 GeV) x p(7 TeV)

ECFA Project



## Instead of conclusions...

if all the efforts that we expend on the discussions on which form of field theory one should use were devoted to arguing for a higher-energy accelerator so that we can do more experiments over the next generation and really learn more about the basic structure of matter.

Murray Gell-Mann, Rochester Conference, 1966

Dogmas are absolutely essential for the progress of Science but they become tragic if they succeed in stopping experimentation designed to prove them wrong.

Abdus Salam, Rochester Conference, 1976

Backup

# Gluon counting

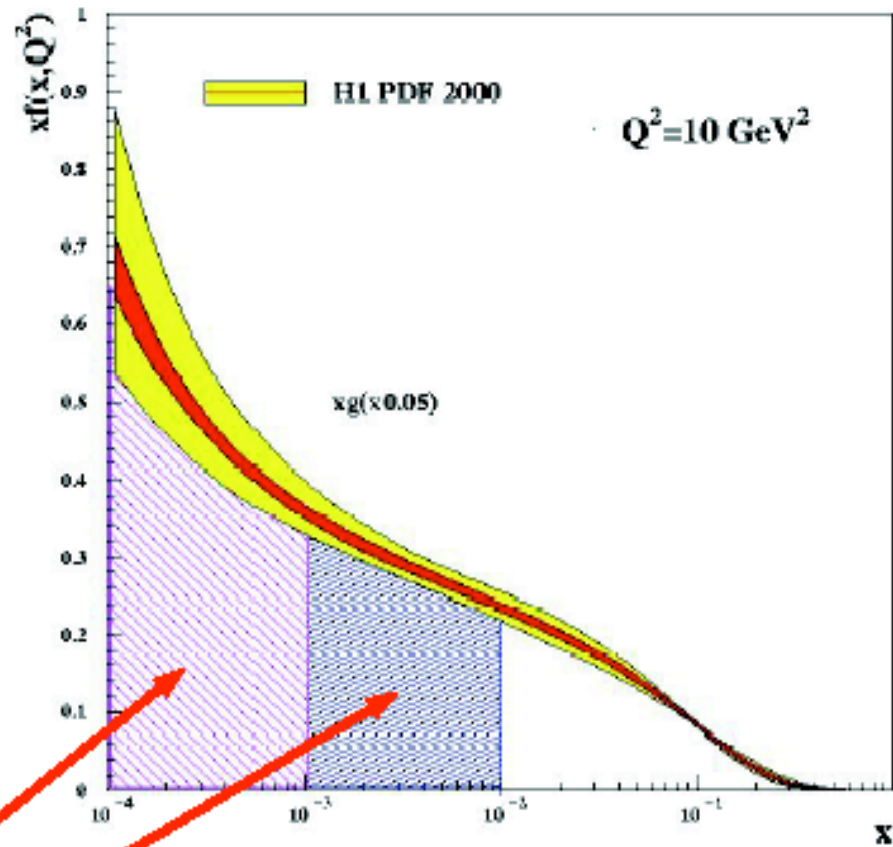
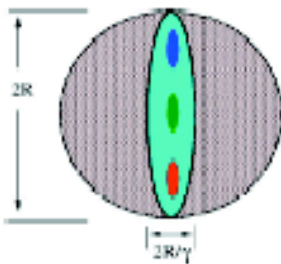
- number of gluons in long. phase space  $dx/x$  :  $xg(x, \mu^2)dx/x$

- occupation area:  
nr of gluons  $\times$  (trans size)<sup>2</sup>

$$g(x, \mu^2) \frac{1}{\mu^2}$$

- saturation starts when:

$$\frac{\alpha_s(\mu^2)}{\mu^2} xg(x, \mu^2) \frac{dx}{x} \geq \pi R^2$$



- gluon density is very large: ~ 90 or 45 Gluons !!!!!
- with  $R \sim 1 \text{ GeV}^{-1}$  we obtain:

$$\frac{0.2}{100 \cdot 10^{-1}} 100 \sim \pi$$



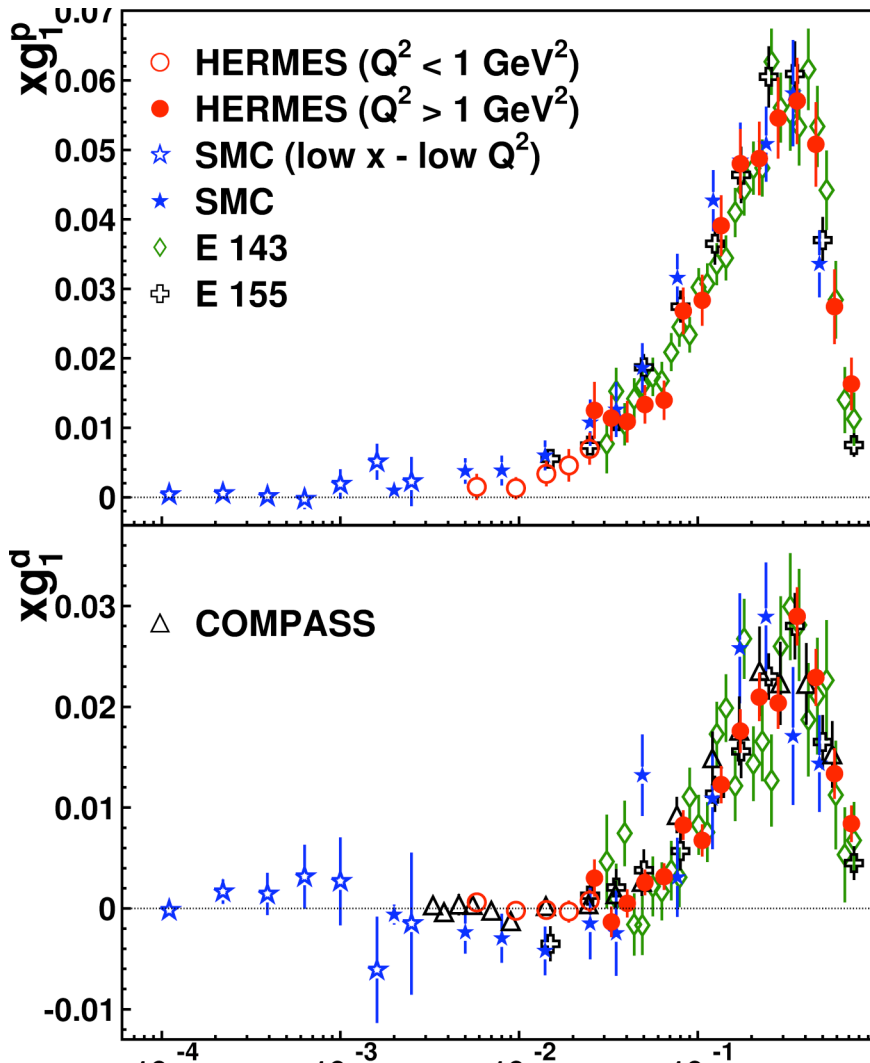
# The spin $\frac{1}{2} = \frac{1}{2} \Delta\Sigma + \Delta G + L_z^q + L_z^G$

Polarised lepton beam, polarised (H,D,...) targets

$$\sigma_{LL} \equiv \frac{1}{2}(\sigma^{\leftarrow} - \sigma^{\rightarrow})/2 \simeq g_1^{p,n}(x, Q^2) = \frac{1}{2} \sum_q e_q^2 [\Delta q^{p,n}(x, Q^2) + \Delta \bar{q}^{p,n}(x, Q^2)]$$

$$\Delta\Sigma \simeq 0.33$$

Use final states and angular distributions to further pin down the spin



**momentum distribution**

$$q(x)$$



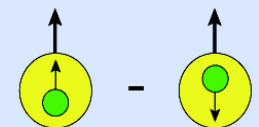
**helicity distribution**

$$\Delta q(x)$$



**transversity distribution**

$$\delta q(x) = h_1^q(x)$$



helicity basis

basis of transv. spin eigenstates

all three DFs needed for complete description of the nucleon!

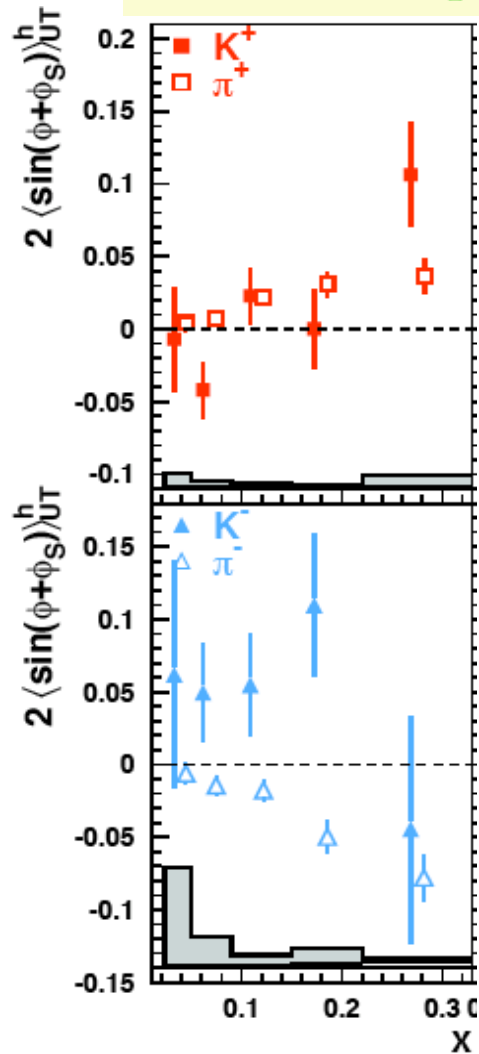
Level arm in  $Q^2$  not large:

gluon contribution not constrained  
=> semi-inclusive data

## Asymmetries

### Collins

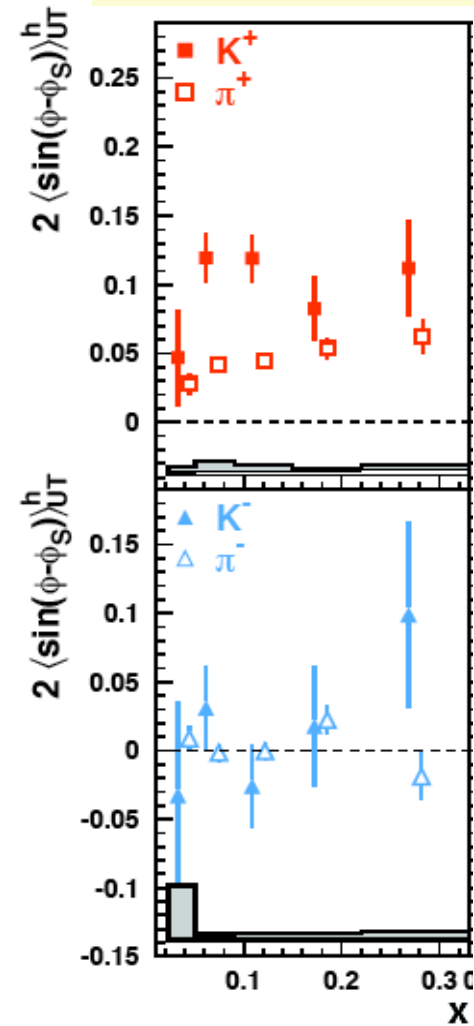
$$A_C \propto \delta q \otimes H_1^\perp$$



information from another process on Collins FF (BELLE) allows extraction of  $\delta q$  (eg Anselmino et al Phys.Rev.D75:054032,2007)

### Sivers

$$A_S \propto f_{1T}^\perp \otimes D_1^q$$



describes correlation between intrinsic transverse quark momentum ( $p_T$ ) and transverse nucleon spin

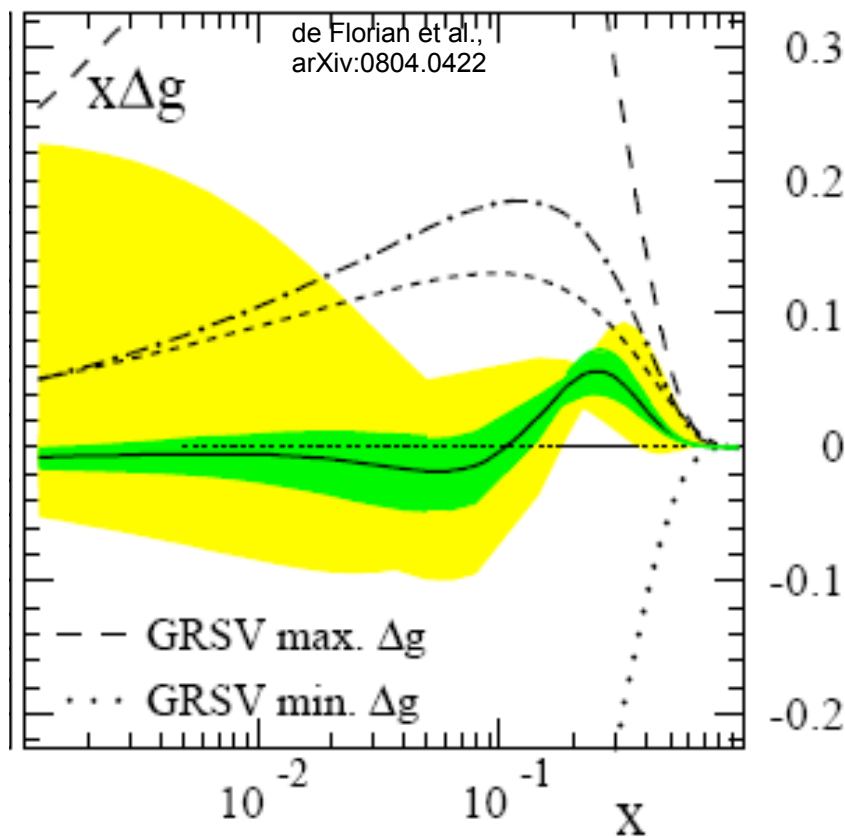
Implies non-zero angular momentum

# Gluon contribution to the spin

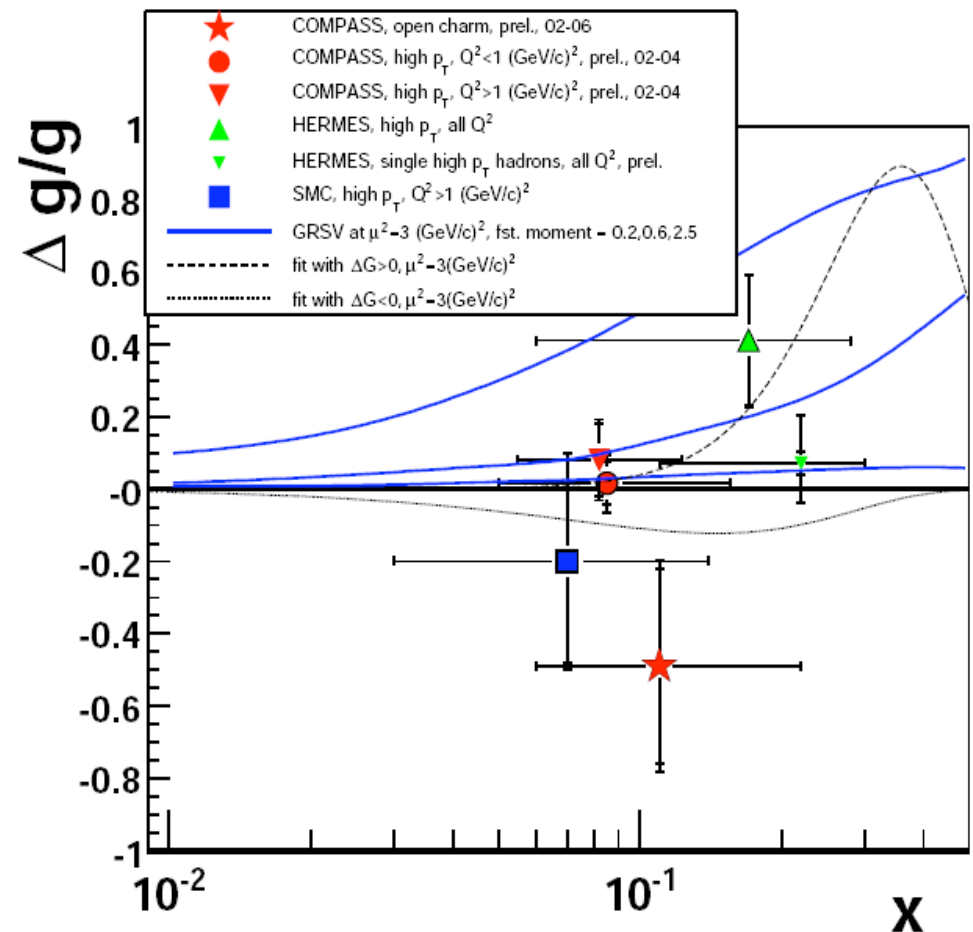
Understanding the gluon is crucial for the proton structure

Extracted via semi-inclusive processes: meson production in polarised DIS and pp (RHIC)

Global pol-analysis: extract polarised PDF's

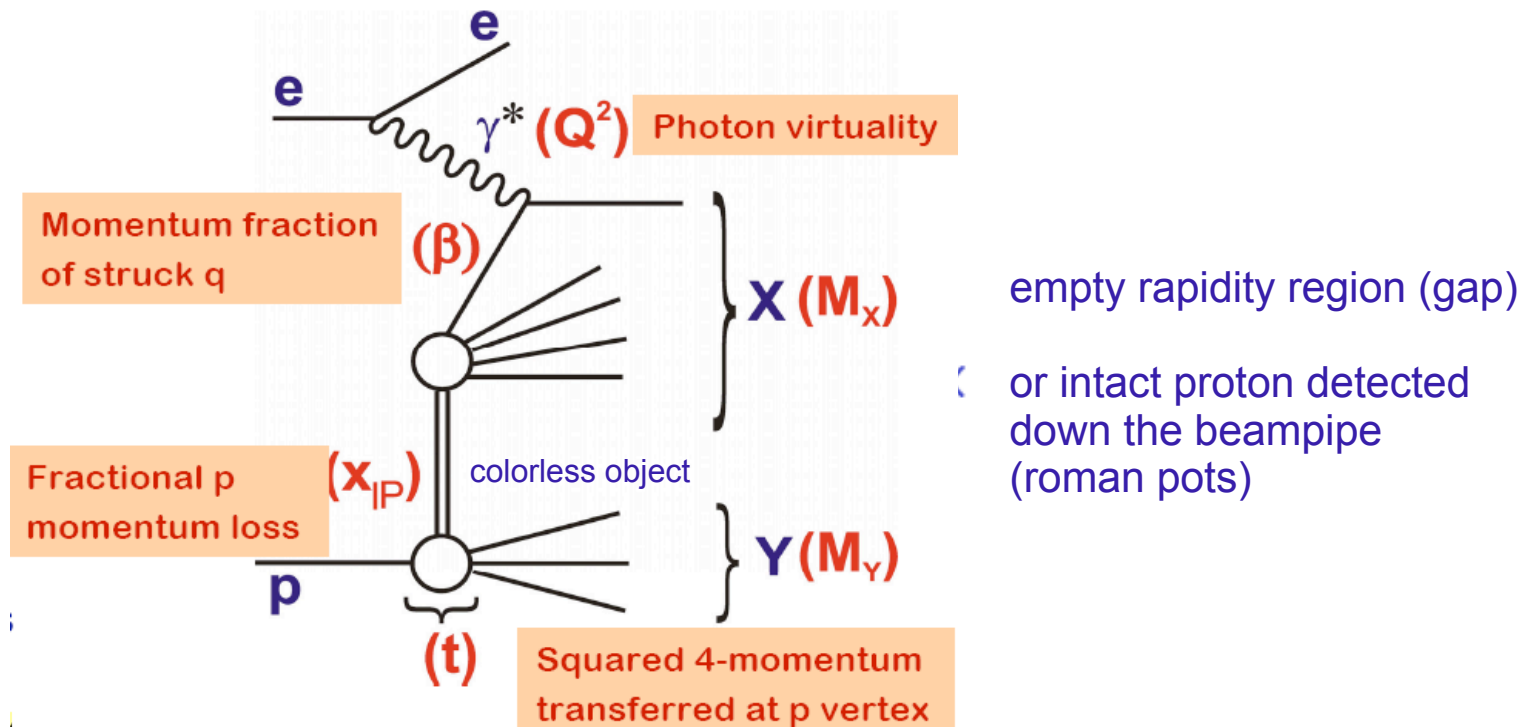


Extreme options now excluded  
Extend x range in pp at RHIC



# Hard Diffraction at HERA

10% of DIS events are diffractive:  
 produced via the exchange of a colourless exchange



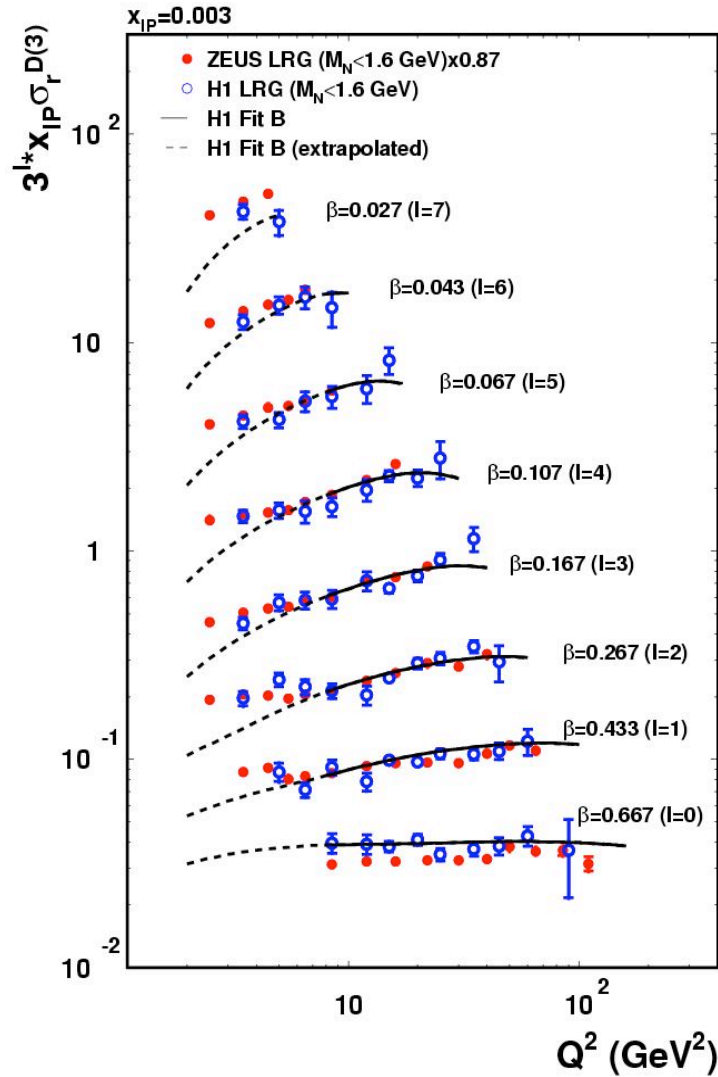
$$\frac{d\sigma_{diff}^{INC}}{dx_{IP} dt d\beta dQ^2} \propto \frac{1}{Q^4} F_2^{D(4)}(x_{IP}, t, \beta, Q^2)$$

assuming factorisation: structure of the diffractive exchange

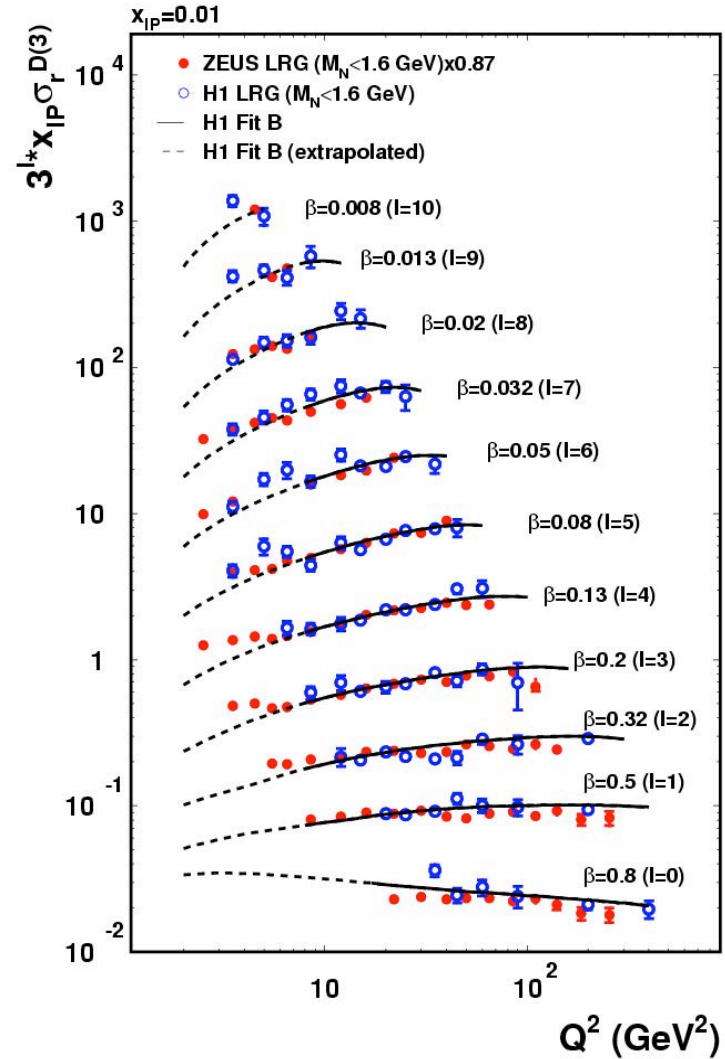


# H1 and ZEUS $M_N < 1.6$ GeV

HERA inclusive diffraction



HERA inclusive diffraction

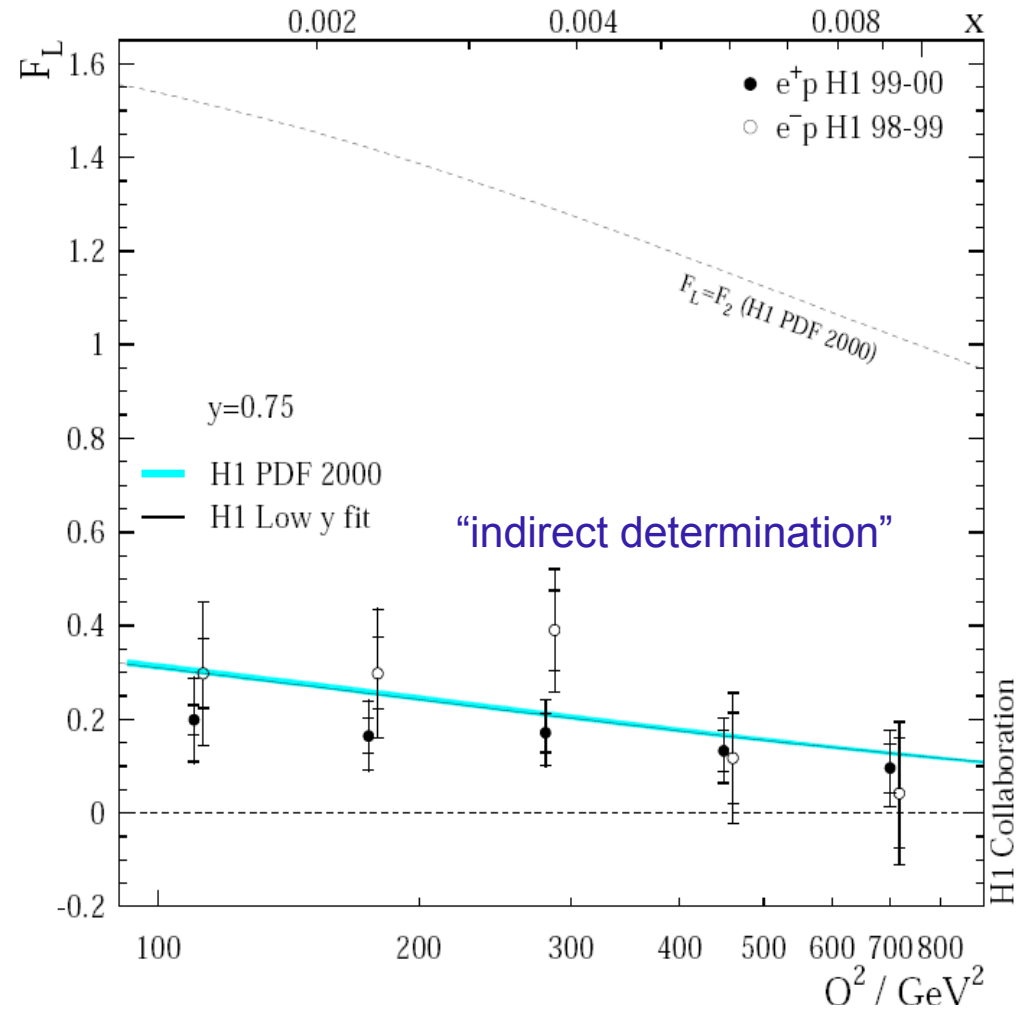
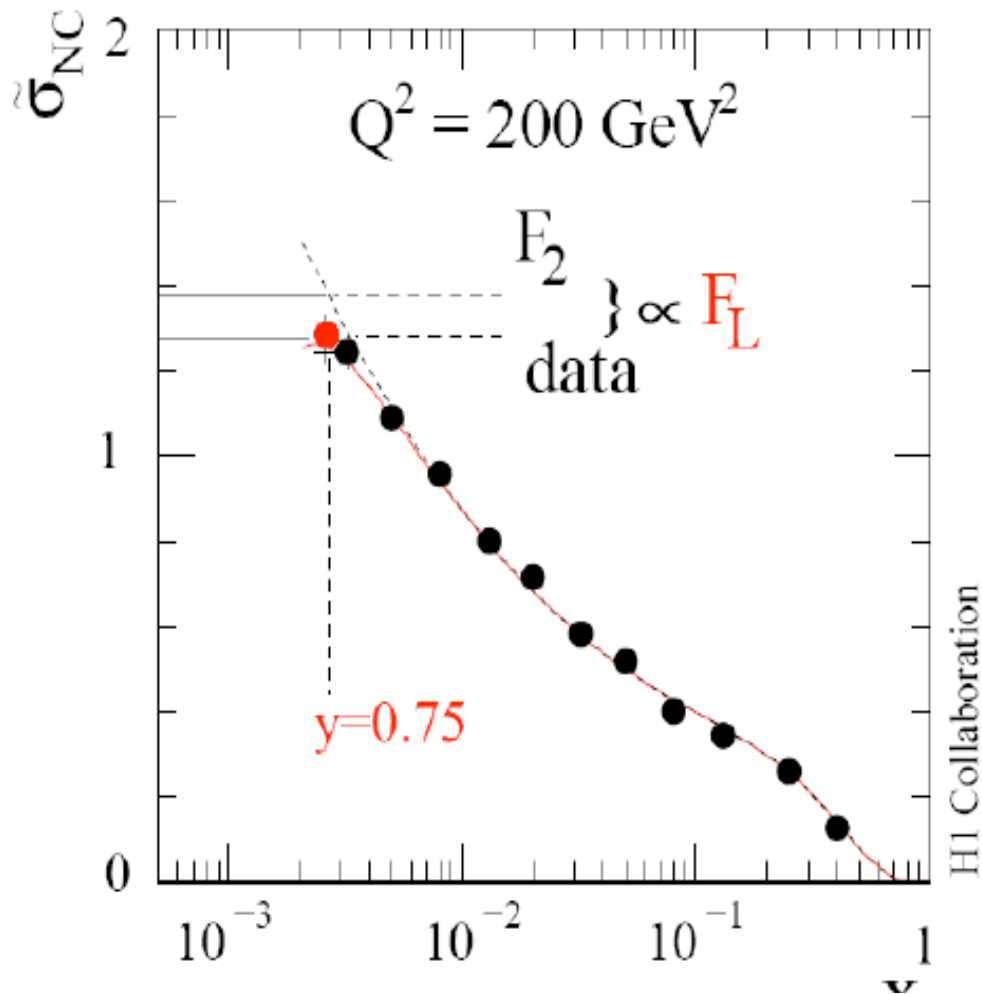


H1 and ZEUS corrected to the same phase space  
Ready for combination, more data to come

# Indirect Determination

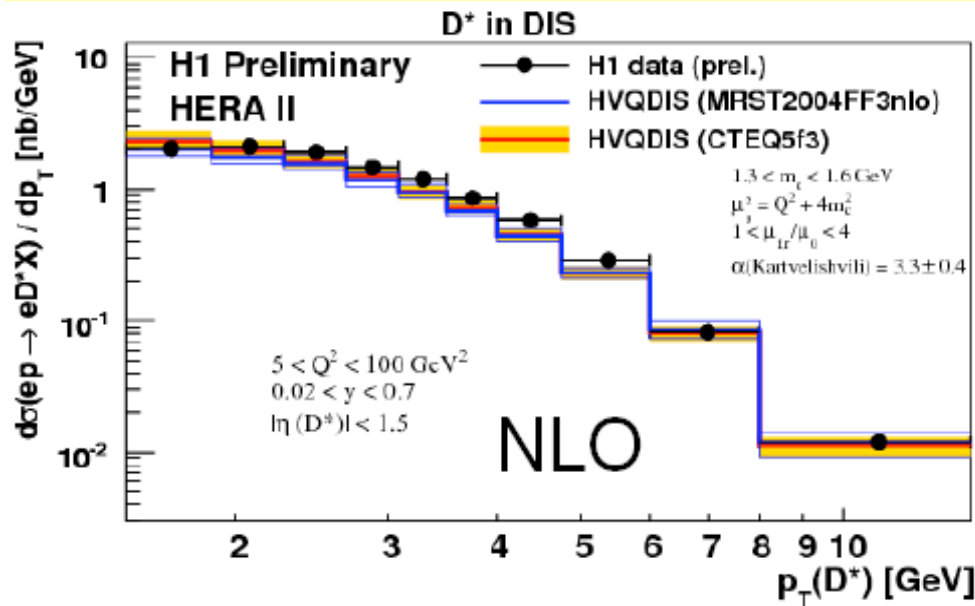
$$\sigma_r = F_2(x, Q^2) - \frac{y^2}{Y_+} \cdot F_L(x, Q^2)$$

see bending at high  $y$   
assume  $F_2 \rightarrow$  extract  $F_L$

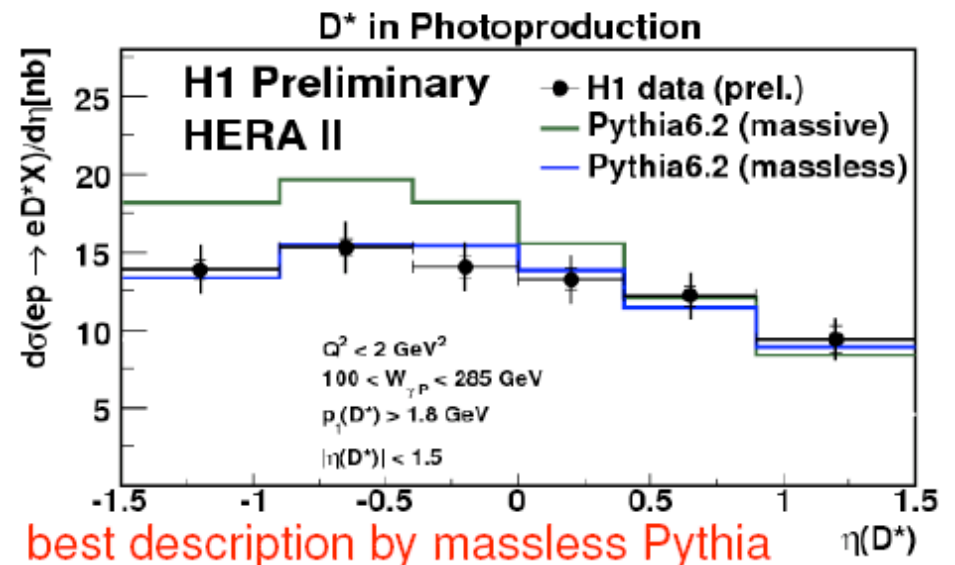
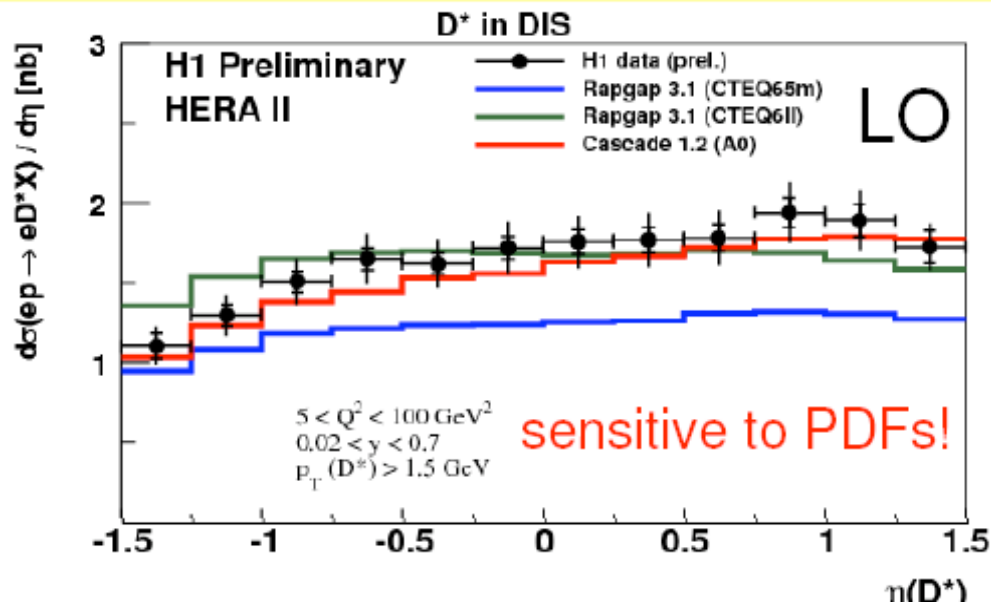
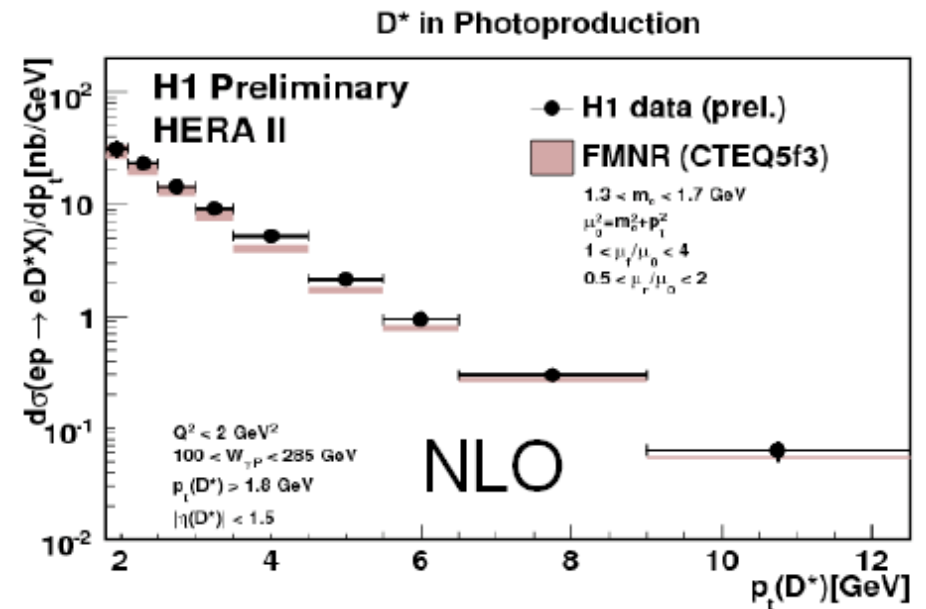


# More charm with HERA II data

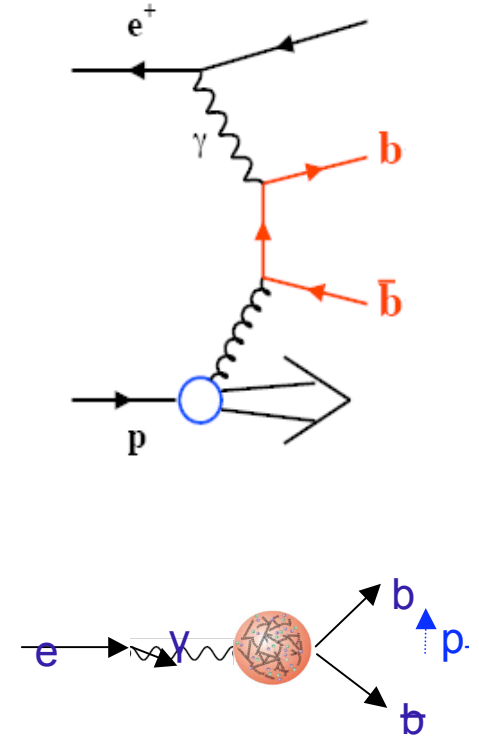
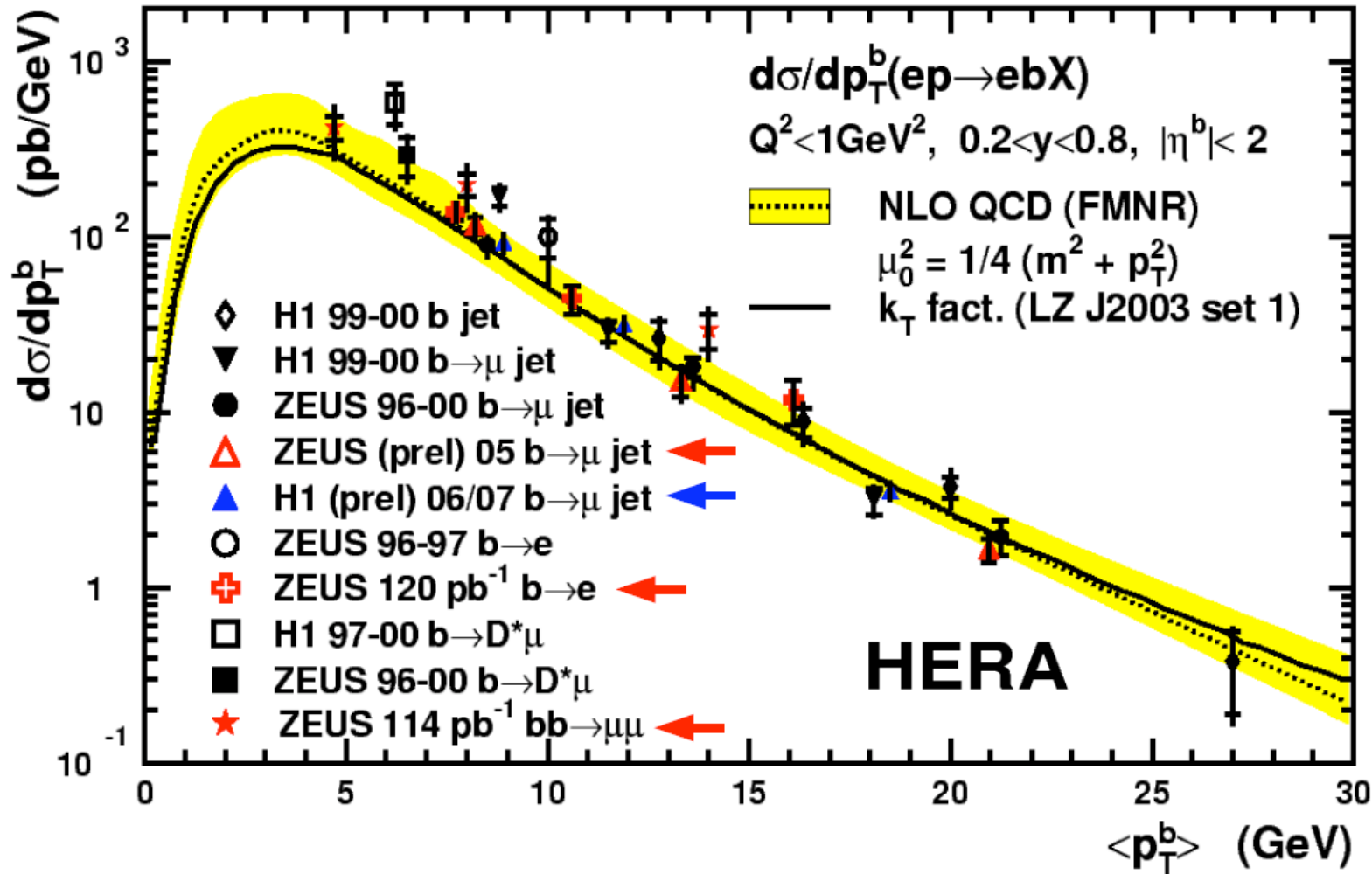
## DIS



## Photoproduction



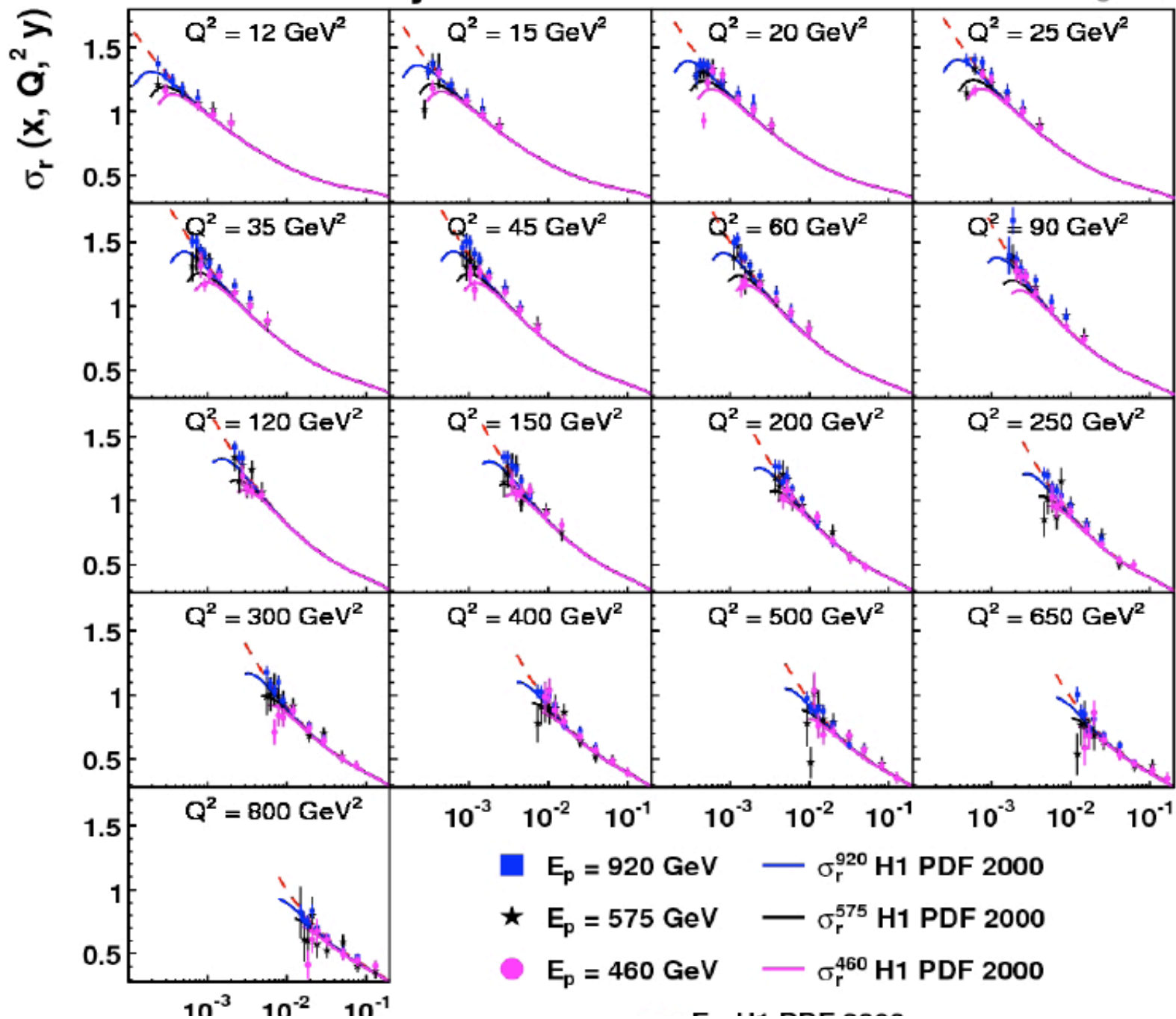
# Photo-Produced Beauty



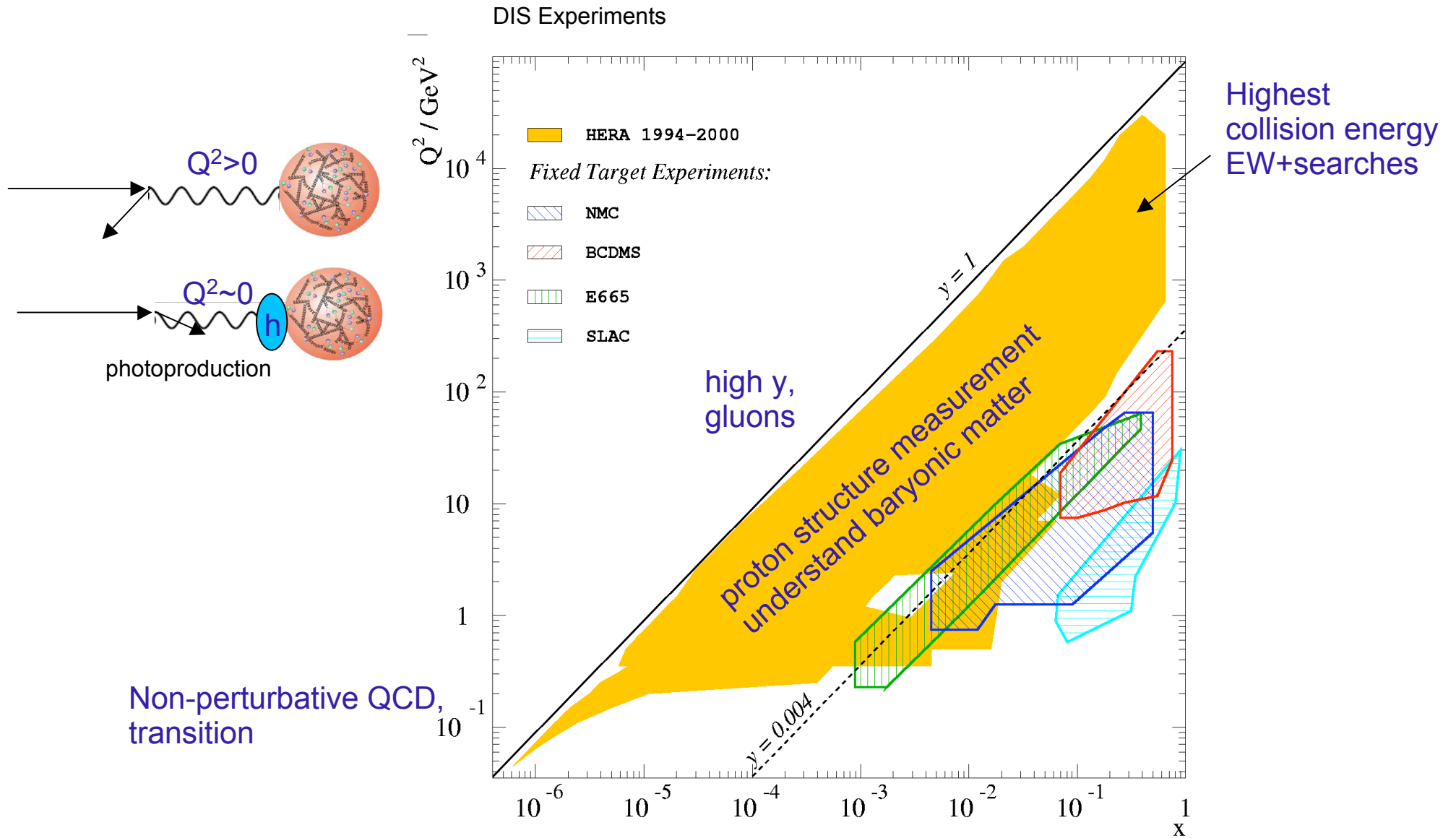
Recent precise measurements in agreement with theory

# H1 Preliminary

medium & high  $Q^2$



# The proton map in the kinematic plane



Use the final state processes (exclusive)  
for more on QCD, for finer phase space

# MSTW 2008 (input data)

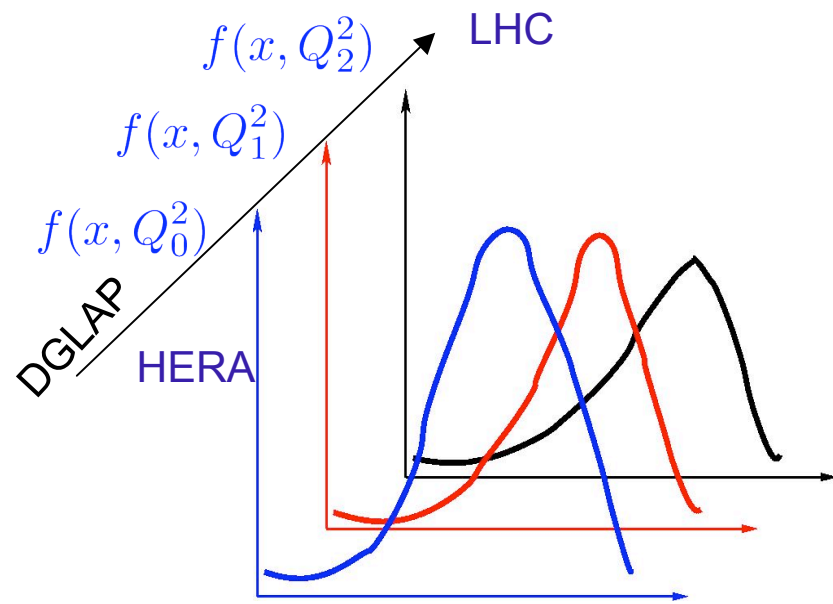
| Data set                               | $N_{\text{pts.}}$ |
|--|-------------------|
| H1 MB 99 $e^+p$ NC                     | 8                 |
| H1 MB 97 $e^+p$ NC                     | 64                |
| H1 low $Q^2$ 96-97 $e^+p$ NC           | 80                |
| H1 high $Q^2$ 98-99 $e^-p$ NC          | 126               |
| H1 high $Q^2$ 99-00 $e^+p$ NC          | 147               |
| ZEUS SVX 95 $e^+p$ NC                  | 30                |
| ZEUS 96-97 $e^+p$ NC                   | 144               |
| ZEUS 98-99 $e^-p$ NC                   | 92                |
| ZEUS 99-00 $e^+p$ NC                   | 90                |
| H1 99-00 $e^+p$ CC                     | 28                |
| ZEUS 99-00 $e^+p$ CC                   | 30                |
| H1/ZEUS $e^\pm p$ $F_2^{\text{charm}}$ | 83                |
| H1 99-00 $e^+p$ incl. jets             | 24                |
| ZEUS 96-97 $e^+p$ incl. jets           | 30                |
| ZEUS 98-00 $e^\pm p$ incl. jets        | 30                |
| DØ II $p\bar{p}$ incl. jets            | 110               |
| CDF II $p\bar{p}$ incl. jets           | 76                |
| CDF II $W \rightarrow l\nu$ asym.      | 22                |
| DØ II $W \rightarrow l\nu$ asym.       | 10                |
| DØ II Z rap.                           | 28                |
| CDF II Z rap.                          | 29                |

| Data set                           | $N_{\text{pts.}}$ |
|------------------------------------|-------------------|
| BCDMS $\mu p$ $F_2$                | 163               |
| BCDMS $\mu d$ $F_2$                | 151               |
| NMC $\mu p$ $F_2$                  | 123               |
| NMC $\mu d$ $F_2$                  | 123               |
| NMC $\mu n/\mu p$                  | 148               |
| E665 $\mu p$ $F_2$                 | 53                |
| E665 $\mu d$ $F_2$                 | 53                |
| SLAC $ep$ $F_2$                    | 37                |
| SLAC $ed$ $F_2$                    | 38                |
| NMC/BCDMS/SLAC $F_L$               | 31                |
| E866/NuSea $pp$ DY                 | 184               |
| E866/NuSea $pd/pp$ DY              | 15                |
| NuTeV $\nu N$ $F_2$                | 53                |
| CHORUS $\nu N$ $F_2$               | 42                |
| NuTeV $\nu N$ $xF_3$               | 45                |
| CHORUS $\nu N$ $xF_3$              | 33                |
| CCFR $\nu N \rightarrow \mu\mu X$  | 86                |
| NuTeV $\nu N \rightarrow \mu\mu X$ | 84                |
| <b>All data sets</b>               | <b>2743</b>       |

- Red = New w.r.t. MRST 2006 fit.

H1, ZEUS:  $F_2^{e^\pm p}(x, Q^2)$   
 BCDMS:  $F_2^{\mu p}(x, Q^2), F_2^{\mu d}(x, Q^2)$   
 NMC:  $F_2^{\mu p}(x, Q^2), F_2^{\mu d}(x, Q^2), \frac{F_2^{\mu n}(x, Q^2)}{F_2^{\mu p}(x, Q^2)}$   $\Rightarrow q, \bar{q}$  at all  $x$   
 SLAC:  $F_2^{\mu p}(x, Q^2), F_2^{\mu d}(x, Q^2)$   $\Rightarrow g$  at moderate and small  $x$   
 E665:  $F_2^{\mu p}(x, Q^2), F_2^{\mu d}(x, Q^2)$   
 CCFR:  $F_2^{\nu(\bar{\nu})p}(x, Q^2), F_3^{\nu(\bar{\nu})p}(x, Q^2)$   
  
 E605, E702, E866:  $pN \rightarrow \mu\bar{\mu} + X$   $\Rightarrow \bar{q}, (g)$   
 E605: Drell-Yan  $p, n$  asymmetry  $\Rightarrow \bar{u}, \bar{d}$   
 CDF:  $W$  rapidity asymmetry  $\Rightarrow u/d$  ratio at high- $x$   
 CDF, DØ: Inclusive jet data  $\Rightarrow g$  at high- $x$   
 CCFR, NuTeV: Dimuon data  $\Rightarrow s, \bar{s}$  sea

**No prompt photon data are included in the fits nowadays**



low x remain delicate theoretically  
 large  $\ln x$  corrections/validity DGLAP  
 experimental data is crucial in this regime



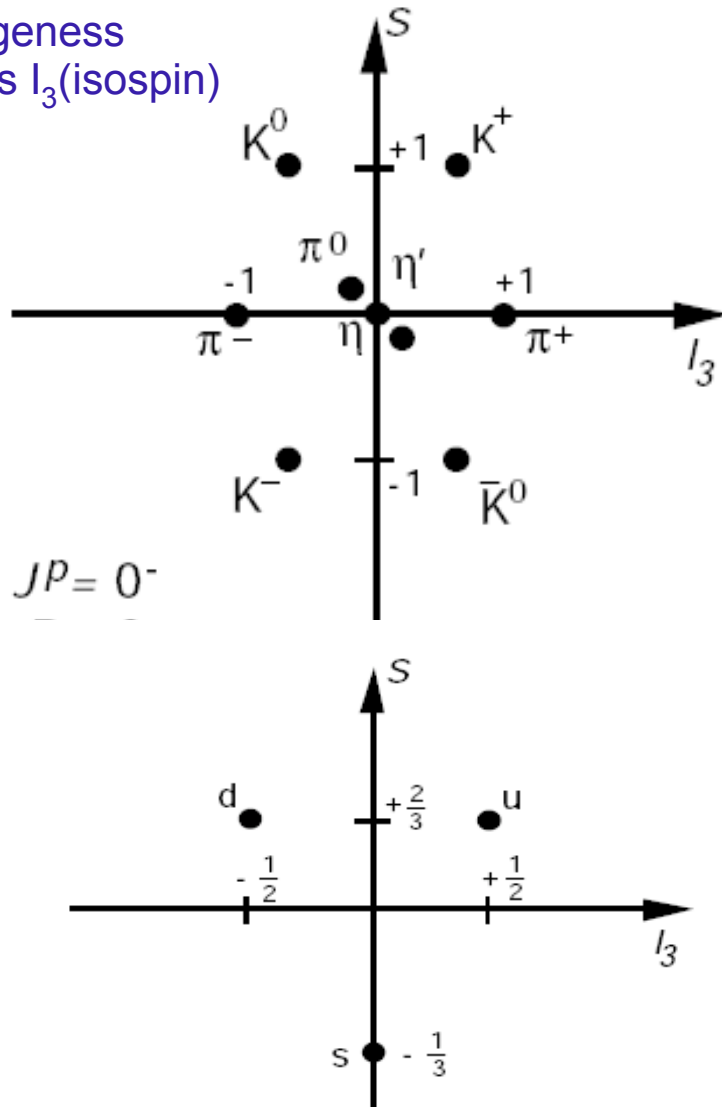
# Hadrons from quarks

e(1896) p(1908) n(1932)

30-60's plenty of new "particles": hadrons

lots of "chemistry" and "zoology": Mendeleev (economical) method: do a table!

strangeness  
versus  $I_3$ (isospin)



|   | $I$           | $I_z$          | $S$ | $Q$            |
|---|---------------|----------------|-----|----------------|
| u | $\frac{1}{2}$ | $+\frac{1}{2}$ | 0   | $+\frac{2}{3}$ |
| d | $\frac{1}{2}$ | $-\frac{1}{2}$ | 0   | $-\frac{1}{3}$ |
| s | 0             | 0              | -1  | $-\frac{1}{3}$ |

fractional charge!

fractional charges

