

# Merging matrix elements & parton showers

Frank Krauss

IPPP Durham

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or: How to embed matrix elements  
without destroying the accuracy of the shower

(independent of the shower)

This talk is primarily based on  
S.Hoeche, F.K., S.Schumann, & F.Siegert, JHEP 0905 (2009) 053  
see also: K.Hamilton, P.Richardson, J.Tully, arXiv:0905.3072 [hep-ph]  
for an implementation with angular ordered showers

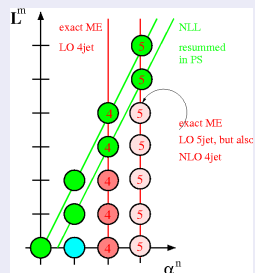
## Matrix elements vs. parton showers

- Different perturbative expansions: fixed order vs. log order.
- Different realms of applicability.

## ME vs. PS

- MEs: hard, large-angle emissions; all interferences.
- PS: soft, collinear emissions; resummation of large logarithms, not all interferences.
- **Combine both, avoid double-counting.** (positive and negative)

## $\alpha_s$ vs. Log



## Reminder: The parton shower

- Remember Sudakov form factor (no emission probability):

$$\Delta_a(t, t_0) = \exp \left\{ - \int_{t_0}^t \frac{dt'}{t'} \int_{\zeta_{\min}}^{\zeta_{\max}} d\zeta \sum_{b=q,g} \mathcal{K}_{ab}(\zeta, t') \right\}.$$

- Here:  $\mathcal{K}_{ba}(\zeta, t)$  = splitting kernels of evolution

( $\implies$  Altarelli-Parisi splitting functions for DGLAP evolution)

Also:  $\zeta_{\max}$  = resolution criterion,  $t, t'$  = evolution parameters.

- Starting from a scale  $T$ , find next emission off parton  $a$  at  $t$  through

$$\#_{\text{random}} = \mathcal{P}_a(T, t) \equiv \frac{\Delta_a(T, t_0)}{\Delta_a(t, t_0)},$$

with  $t_0 = \mathcal{O}(\text{few } \Lambda_{\text{QCD}}^2)$  as infrared cut-off.

( $\implies$  add ratio of PDFs for initial state shower: backward evolution trick)

## Strategy for merging

S.Catani, F.K., R.Kuhn and B.R.Webber, JHEP 0111 (2001) 063  
F.K., JHEP 0208 (2002) 015

- Basic idea: Decompose phase space into hard, wide-angle and soft, collinear region through jet measure. Use MEs in hard region (jet production), PS in soft region (jet evolution).
- Realise that parton shower approximation to matrix element is at LO is product of splitting functions.
- (Leading) Logarithmic HO corrections are included through Sudakov form factors and running of  $\alpha_S$ .
- Therefore: replace product of splitting functions with ME, keep HO effects of shower.
- In original papers above: Reweight ME with appropriate Sudakov form factors and ratios of  $\alpha_S$ , run a vetoed shower. In  $e^+e^-$  for angular-ordered shower: NLL accuracy achievable.
- Question(s): Accuracy in IS shower, relationship to other merging procedures (e.g. CKKW-L, MLM)

## A new attempt to formalise merging

- Goal: Make preservation of log accuracy in shower explicit.
- First replace kernels in QCD evolution equations with

$$\mathcal{K}_{ab}(\xi, \bar{t}) = \mathcal{K}_{ab}^{\text{ME}}(\xi, \bar{t}) + \mathcal{K}_{ab}^{\text{PS}}(\xi, \bar{t}).$$

with ( $Q$  is jet measure of jet clustering algorithm)

$$\begin{aligned}\mathcal{K}_{ab}^{\text{ME}}(\xi, \bar{t}) &= \mathcal{K}_{ab}(\xi, \bar{t}) \Theta \left[ Q_{ab}(\xi, \bar{t}) - Q_{\text{cut}} \right] \quad \text{and} \\ \mathcal{K}_{ab}^{\text{PS}}(\xi, \bar{t}) &= \mathcal{K}_{ab}(\xi, \bar{t}) \Theta \left[ Q_{\text{cut}} - Q_{ab}(\xi, \bar{t}) \right].\end{aligned}$$

- Yields modified Sudakov form factor (decomposes trivially):

$$\Delta_a(t, t_0) = \Delta_a^{\text{ME}}(t, t_0) \cdot \Delta_a^{\text{PS}}(t, t_0).$$

and no-emission probabilities (interpretation see below)

$$\mathcal{P}_a(T, t) = \mathcal{P}_a^{\text{ME}}(T, t) \cdot \mathcal{P}_a^{\text{PS}}(T, t).$$

## The PS regime: Truncated showers

- Look into PS-splitting kernel:

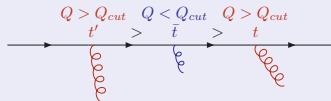
$$\mathcal{K}_{ab}^{\text{PS}}(\xi, \bar{t}) = \mathcal{K}_{ab}(\xi, \bar{t}) \Theta \left[ Q_{\text{cut}} - Q_{ab}(\xi, \bar{t}) \right].$$

⇒ Do not generate emissions in jet regime

(In original algorithm: vetoed shower -  $Q_{ab} < Q_{\text{cut}}$  is not present)

- But: evolution parameter  $t$  may be different from jet parameter  $Q$  ⇒ **Truncated showering**

Introduced in P.Nason, JHEP 0411 (2004) 040



- NB: In original algorithm, these emissions have been dealt with by radiating off the outgoing legs - in principle: logarithmically correct, in practice: may lead to unphysical colour flows

(Especially for angular-ordered showers, less severe if  $t \simeq Q$ )

## The ME regime: Sudakov reweighting

- Look into ME-splitting kernel:

$$\mathcal{K}_{ab}^{\text{ME}}(\xi, \bar{t}) = \mathcal{K}_{ab}(\xi, \bar{t}) \Theta \left[ Q_{ab}(\xi, \bar{t}) - Q_{\text{cut}} \right] .$$

⇒ Generate emissions in jet regime only

( $Q_{ab} < Q_{\text{cut}}$  is not present)

- But these emissions are dealt with by higher order ME's  
⇒ Reject complete event.

(Simple to see: This is the Sudakov rejection of original method)



## The algorithm in a nutshell

- Select parton level event (ME: flavours, colours, momenta) according to corresponding (partial) cross section
- Cluster backwards with “inverted” shower (kinematics): yields  $\{t, \xi, \phi\}$  of “hard nodes” (branching kinematics)  
(Implementation of non-QCD splitting functions helps)
- Reweight with ratios  $\alpha_s(\mu_{\text{node}})/\alpha_s(\mu_{\text{ME}})$  (QCD emissions)
- Start shower at highest scale, run truncated showers until scale of next hardest emission node. Reject event if new jet was produced
- Insert next node and repeat
- Obviously: If  $Q = t$ , then truncated shower not necessary

This is essentially [L.Lonnblad, JHEP 0205 \(2002\) 046](#) for FS dipole showers.

Note: This procedure is **independent** of both **shower** and **jet measure**

## ME & PS: Theoretical uncertainties

Uncertainties related to ME-PS merging

- Choice of parton shower implementation
- Choice of the jet criterion  $k_T$ -measure, soft eikonal, ...
- Value of the phase-space separation cut,  $Q_{\text{cut}}$
- Maximum number of jets from hard MEs,  $N_{\text{max}}$

Uncertainties related to pQCD methods

- Scale uncertainties from MEs
- Scale uncertainties from PSs
- PDF uncertainties

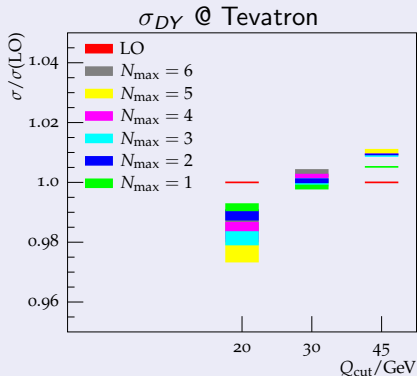
## Two implementations currently available

- SHERPA - uses truncated CS-shower for initial and final state
- HERWIG++ - uses truncated angular ordered shower for final state

## Results (DY @ Tevatron): Total cross sections

Consequence of the method:

- Cross section unaltered to LO accuracy  
(due to unitarity of PS simulation)  
→ can employ this to cross-check simulation
- Variation of  $Q_{cut}$  and/or  $N_{max}$  should not affect  $\sigma_{tot}$  too much

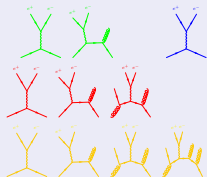
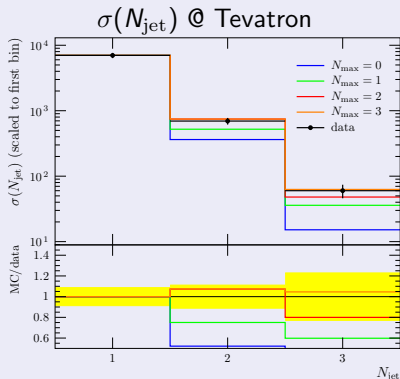


# Results (DY Tevatron): Jet multiplicity

Data from Data: PRL100(2008)102001

Consequence of the method:

- Jet rates and -spectra improved compared to pure PS simulation
- (due to usage of HO real ME's)
- Note: minor corrections to total cross section might still have big effect on rare events !



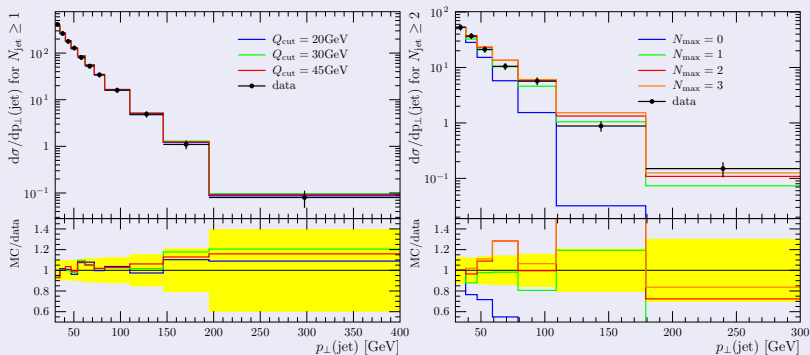
# Results (DY Tevatron): Jet spectra

Data from Data: PRL100(2008)102001

Consequence of the method:

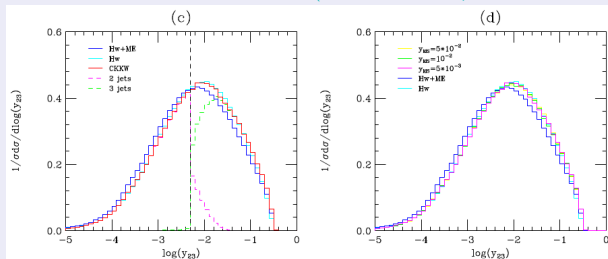
- Radiation pattern unaltered to PS accuracy
- Variation of  $Q_{cut}$  should not affect distributions too much

(But  $Q_{cut}$  must be in range where PS approximation is valid !)



# ME & PS: The necessity of the truncated shower

(Use HERWIG++ as example: truncated showers not so visible in  $p_{\perp}$ -ordered showers)

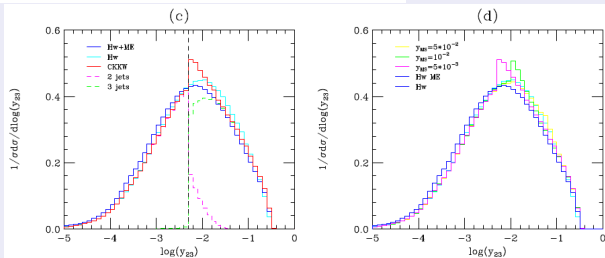


Truncated shower  
enabled

arXiv:0905.3072

Truncated shower  
disabled

arXiv:0905.3072



## Forthcoming attractions in SHERPA, v.1.2.0

(All results above with SHERPA v.1.2.0)

- Including new ME generator COMIX:
  - Will allow for significantly higher multiplicities:  $pp \rightarrow V + (\leq 6)j$ ,  
 $Q\bar{Q} + (\leq 6)j$ ,  $(\leq 6)j$  quite painless,  
(even more feasible - but painful due to integration)
  - No more libraries written out, compiled and linked.
- Including new Catani-Seymour shower  
(+ merging, of course);
- Automated Catani-Seymour subtraction  
(generic interface, massive dipoles work in progress).
- Automated decay chains for **all** heavy particles  
(up to now only user-defined decay chains feasible);

# COMIX - a new matrix element generator for Sherpa

T.Gleisberg & S.Hoeche, JHEP 0812 (2008) 039

- Colour-dressed Berends-Giele amplitudes in the SM
- Fully recursive phase space generation
- Example results (cross sections):

$gg \rightarrow ng$	Cross section [pb]				
$n$	8	9	10	11	12
$\sqrt{s}$ [GeV]	1500	2000	2500	3500	5000
Comix	0.755(3)	0.305(2)	0.101(7)	0.057(5)	0.019(2)
Maltoni (2002)	0.70(4)	0.30(2)	0.097(6)		
Alpgen	0.719(19)				

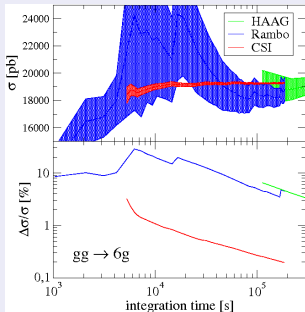
$\sigma$ [ $\mu\text{b}$ ]	Number of jets						
$b\bar{b} + \text{QCD jets}$	0	1	2	3	4	5	6
Comix	470.8(5)	8.83(2)	1.826(8)	0.459(2)	0.1500(8)	0.0544(6)	0.023(2)
ALPGEN	470.6(6)	8.83(1)	1.822(9)	0.459(2)	0.150(2)	0.053(1)	0.0215(8)
AMEGIC++	470.3(4)	8.84(2)	1.817(6)				



# COMIX - a new matrix element generator for Sherpa

T.Gleisberg & S.Hoeche, JHEP 0812 (2008) 039

- Colour-dressed Berends-Giele amplitudes in the SM
- Fully recursive phase space generation
- Example results (phase space performance):



## Using Catani-Seymour splitting kernels

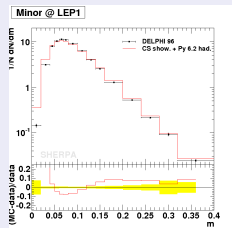
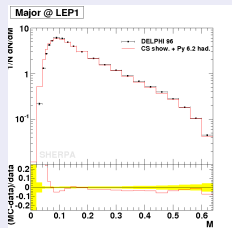
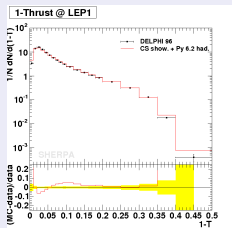
First discussed in: Z.Nagy and D.E.Soper, JHEP **0510** (2005) 024;  
Implemented by M.Dinsdale, M.Ternick, S.Weinzierl Phys.Rev.**D76** (2007) 094003,  
and S.Schumann& F.K., JHEP **0803** (2008) 038.

- Catani-Seymour dipole subtraction terms as universal framework for QCD NLO calculations.
- Factorisation formulae for real emission process:  
Full phase space coverage & good approx. to ME.
- Added benefit: All particles always on-shell

Matching/merging with ME improved.

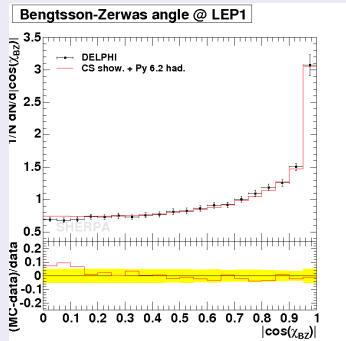
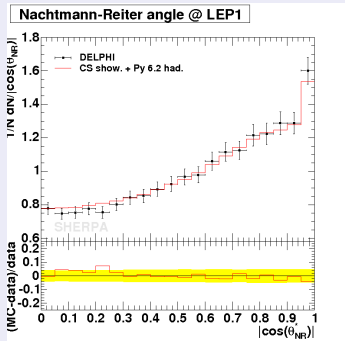
# Results in $e^+e^-$ collisions at LEP1

S.Schumann & F.K., JHEP 0803 (2008) 038.



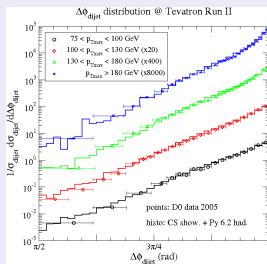
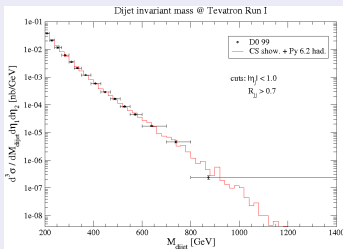
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# CS-Shower: Results in $p\bar{p}$ collisions

S.Schumann & F.K., JHEP 0803 (2008) 038.



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