

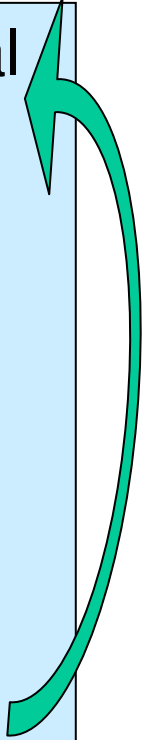


PDF sensitivities using W, Z, γ^* at LHCb

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Pseudo-data fits to deduce improvements in PDFs

- From eigenvector phase space (assume multinomial distribution), choose one set: 'truth'
 - Generate many pseudo-data sets corresponding to given luminosity
 - Fit each pseudo-data set: 'pseudo-measurement'
 - Compare pseudo-measurement to truth
 - centre of distribution gives bias
 - width of distribution gives precision
 - Repeat
- 

What is fit? (MSTW,CTEQ,Alekhin)

We considered $\frac{d\sigma}{dy}$ for W_+, W_-, Z .

$f_0 = \frac{d\sigma}{dy}$: distribution obtained with central eigenvectors

$f_i = \frac{d\sigma}{dy} (\lambda_i = 1, \lambda_{\neq i} = 0)$: distribution with i^{th} e.v. moved 1σ

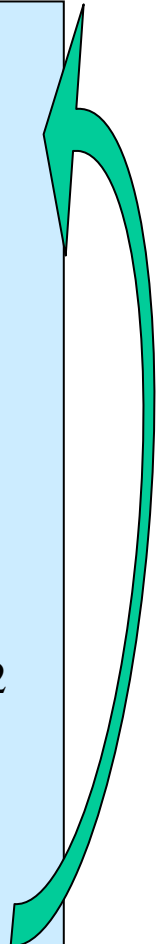
Fit

$$\chi^2(\lambda_0, \lambda_i) = \sum_{j=1}^{\#bins} \left[\frac{x_j - \lambda_0 (f_0 + \lambda_i (f_i - f_0))}{\sigma_j} \right]^2 + \sum_{i=1}^{\#e.v.} \lambda_i^2$$

Normalisation
(Luminosity)

data in j bins, each with uncertainty σ

Eigenvalues



Results for precision on luminosity shown at DIS09....

0.1 fb ⁻¹				
	MSTW08	CTEQ66	Alekhin	NNPDF
W+	1.8	2.4	2.0	2.9
W-	1.9	2.6	2.2	2.7
Z	1.9	2.4	2.2	2.4
WWZ	1.7	2.3	1.8	2.0
1 fb ⁻¹				
	MSTW08	CTEQ66	Alekhin	NNPDF
W+	1.6	2.2	1.8	2.4
W-	1.6	2.3	2.1	2.4
Z	1.7	2.1	1.9	1.8
WWZ	1.3	2.1	1.4	2.2
10 fb ⁻¹				
	MSTW08	CTEQ66	Alekhin	NNPDF
W+	1.3	2.0	1.5	2.5
W-	1.2	1.9	1.6	3.0
Z	1.4	1.9	1.9	1.9
WWZ	0.8	1.7	1.0	-

Percentage statistical uncertainty on fitted luminosity

Precision doesn't scale with $\frac{1}{\sqrt{N_{events}}}$

Covariance matrix

$$\chi^2(\lambda_0, \lambda_i) = \sum_{j=1}^{\#bins} \left[\frac{x_j - \lambda_0(f_0 + \lambda_i(f_i - f_0))}{\sigma_j} \right]^2 + \sum_{i=1}^{\#e.v.} \lambda_i^2$$

Before:

$$V_{ij} = \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}$$

After:

$$V_{ij} = \begin{pmatrix} <1 & \neq 0 & \neq 0 & \neq 0 \\ \neq 0 & <1 & \neq 0 & \neq 0 \\ \neq 0 & \neq 0 & <1 & \neq 0 \\ \neq 0 & \neq 0 & \neq 0 & <1 \end{pmatrix}$$

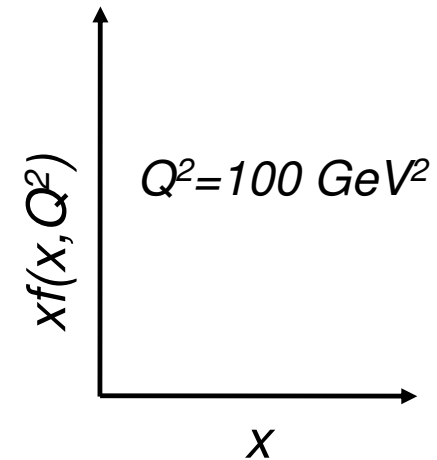
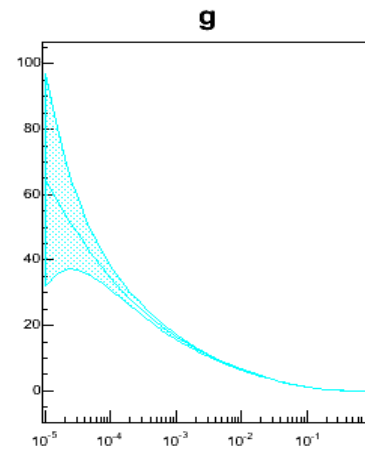
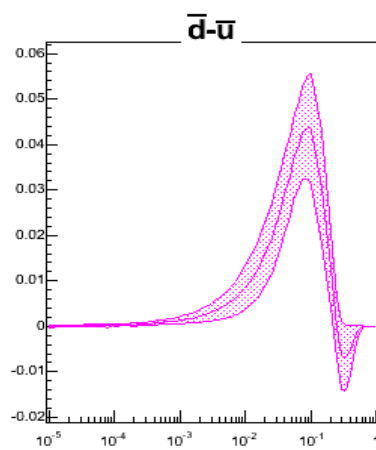
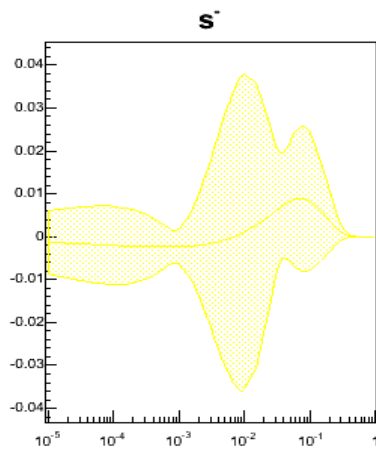
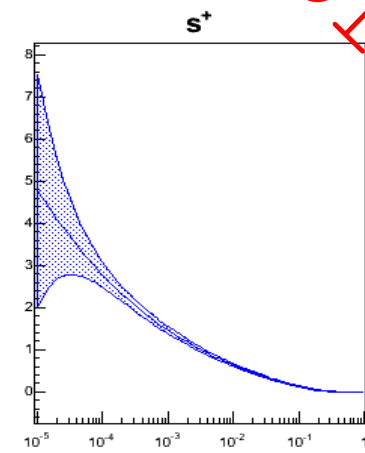
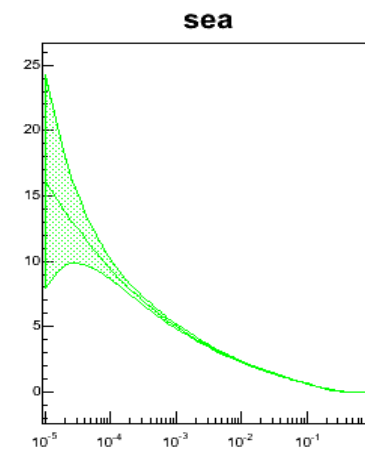
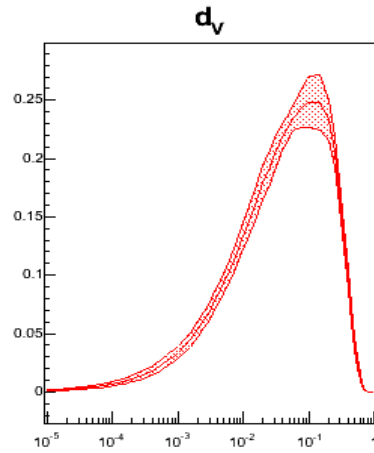
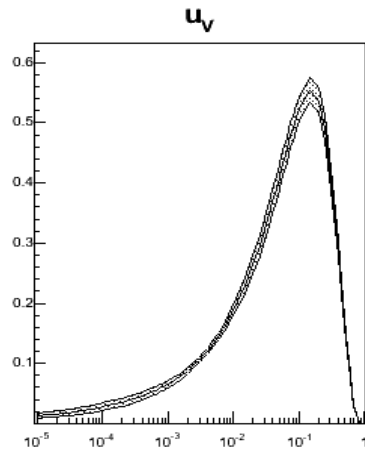
For any quantity $f(\lambda_i)$

$$\delta_f = \sum_{ij} \frac{\partial f}{d\lambda_i} V_{ij}^{-1} \frac{\partial f}{d\lambda_j}$$

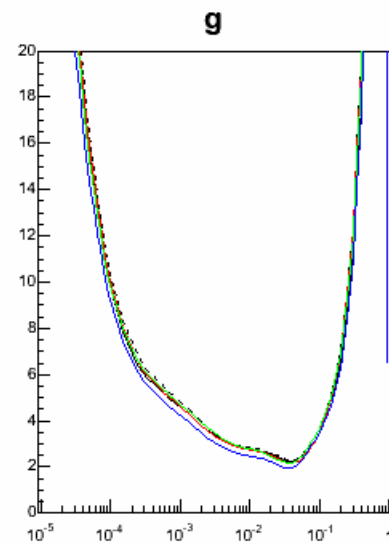
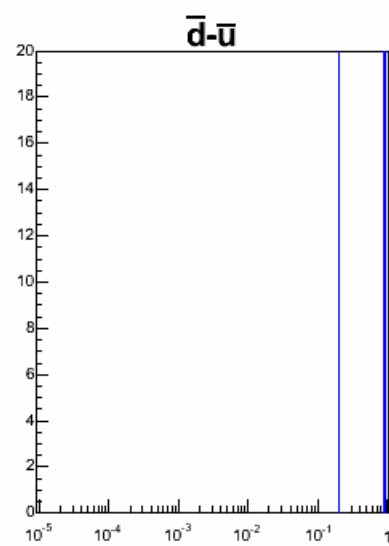
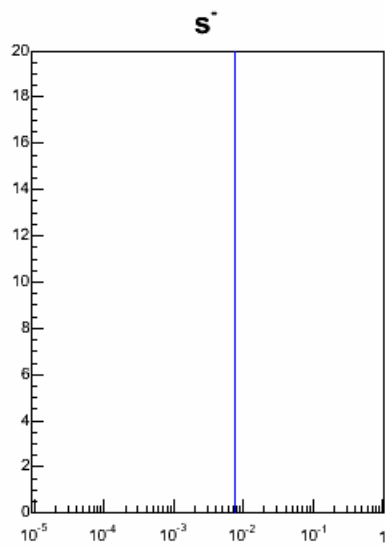
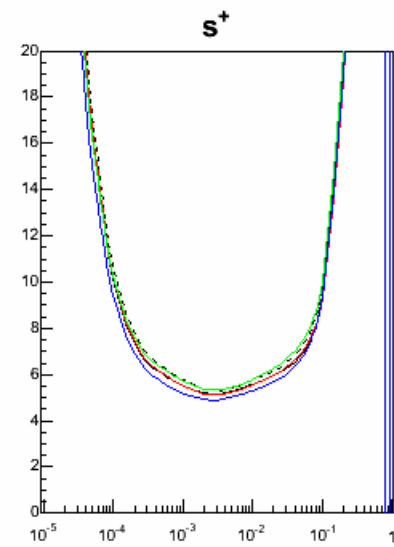
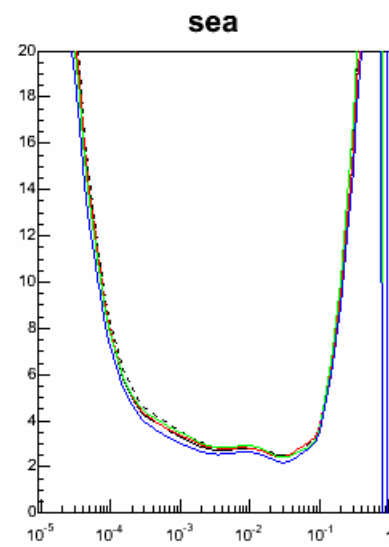
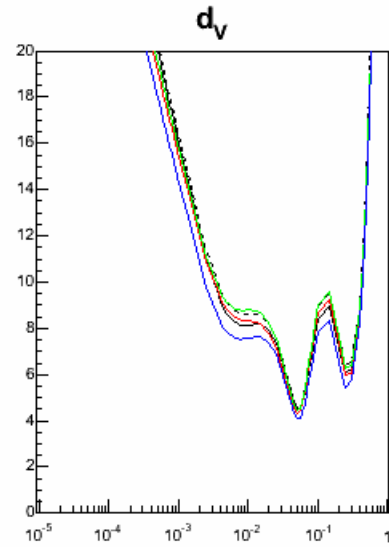
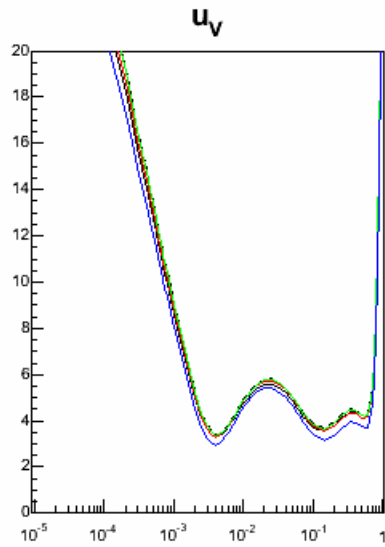
so modified PDFs can be deduced.

MSTW08 PDF

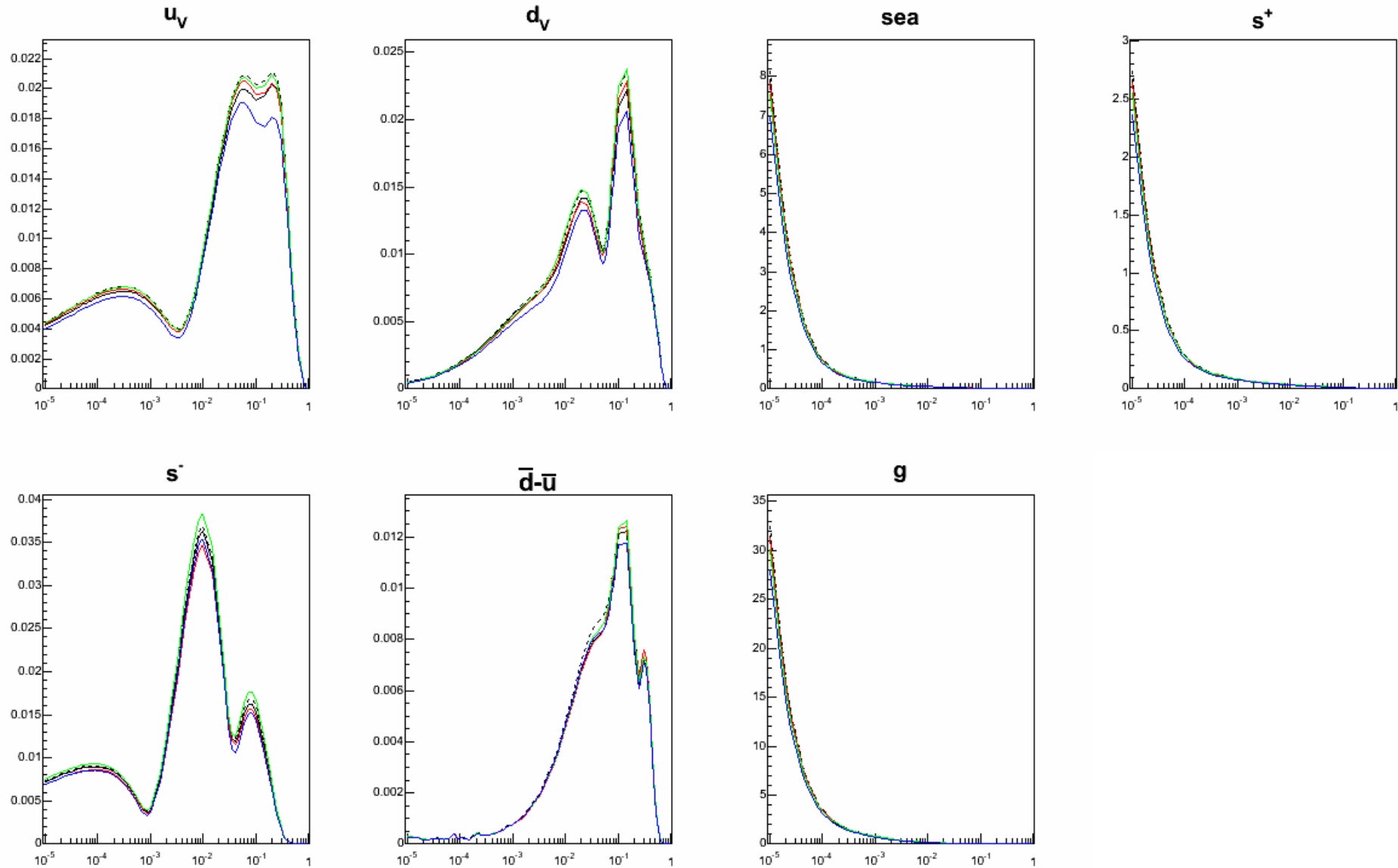
theory



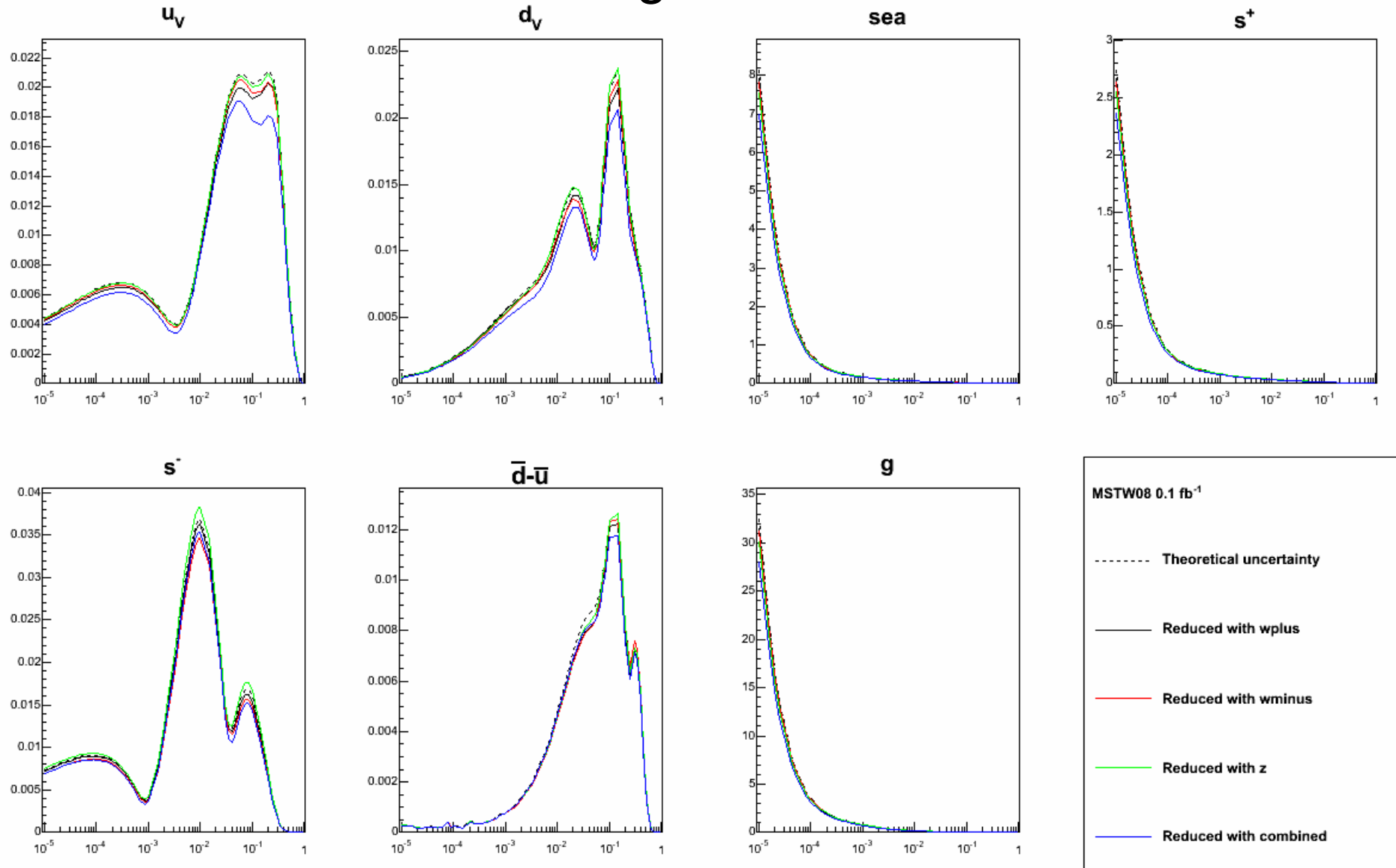
% uncertainty for MSTW08 $Q^2=100 \text{ GeV}^2$



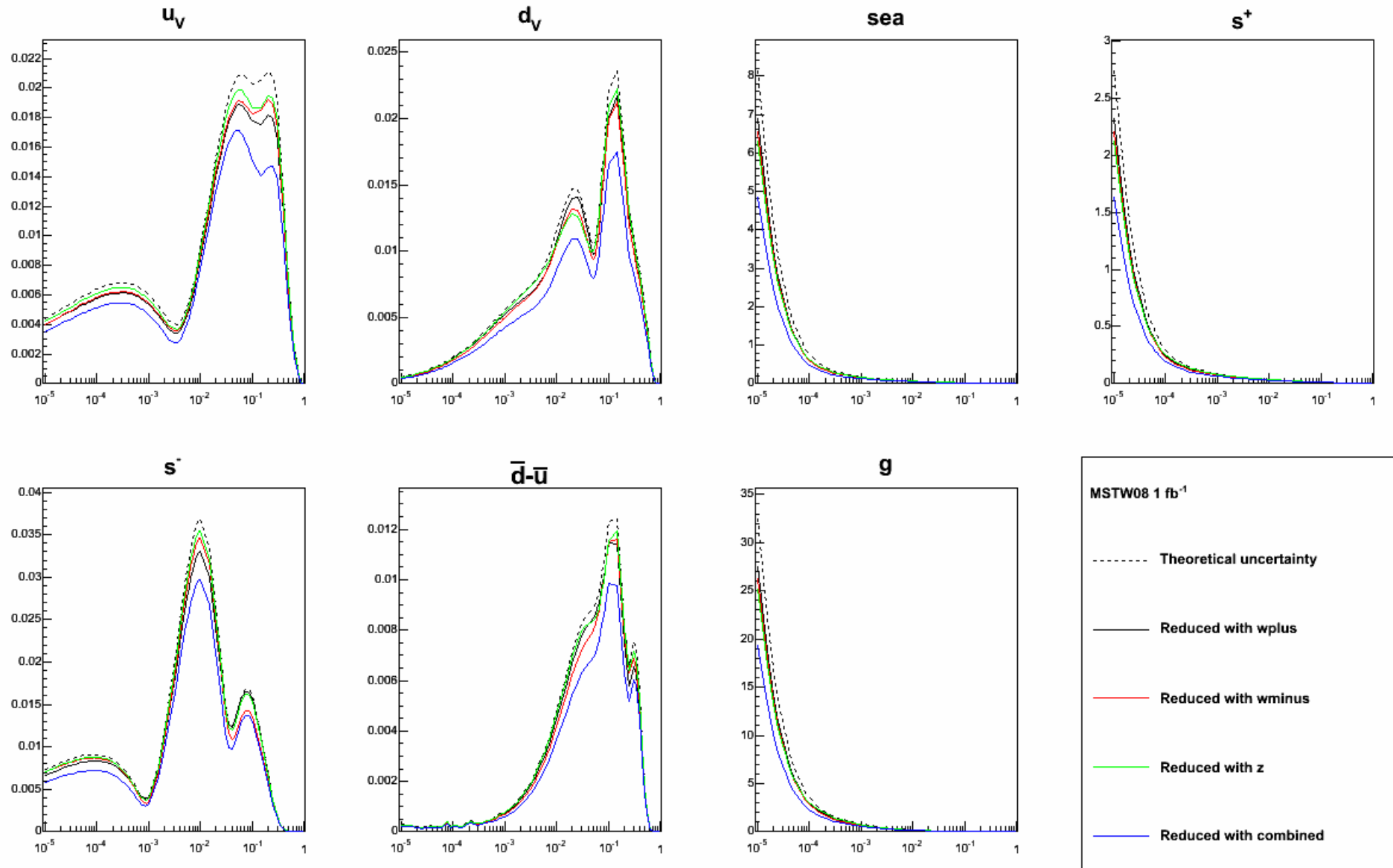
Absolute uncertainty for MSTW08 $Q^2=100 \text{ GeV}^2$



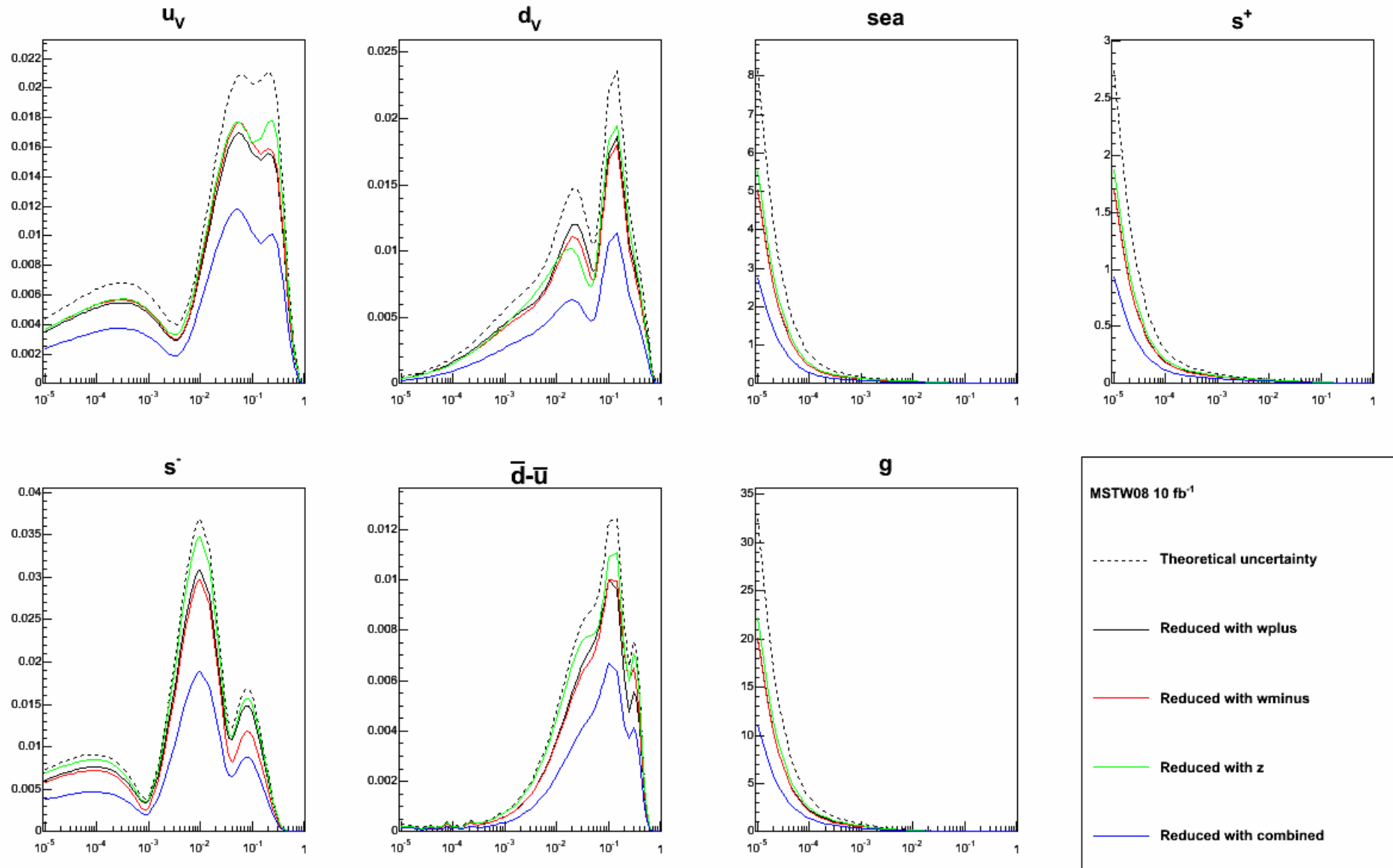
Effect on absolute uncertainty for MSTW08 at $Q^2=100 \text{ GeV}^2$ using **0.1 fb⁻¹** of LHCb data



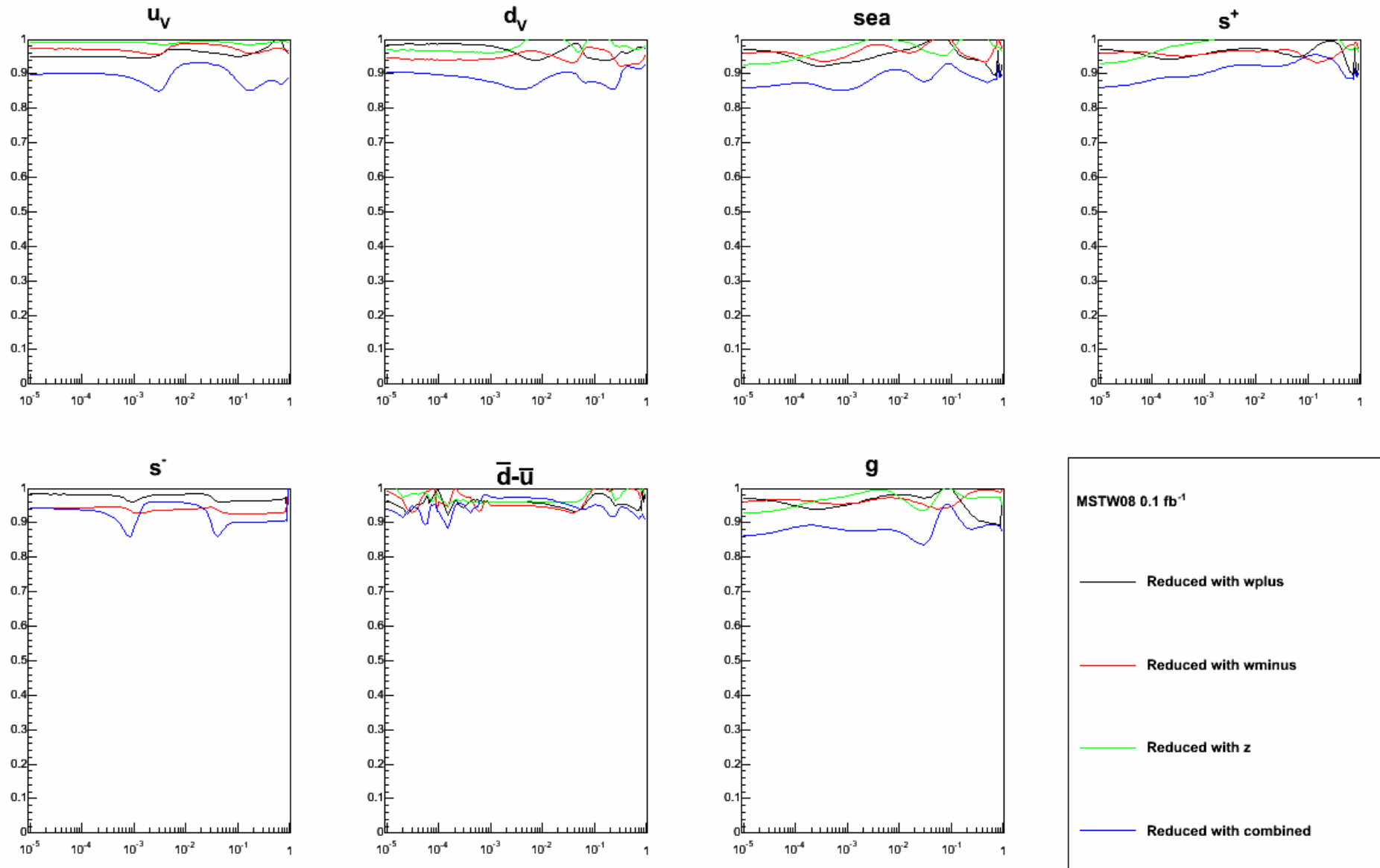
Effect on absolute uncertainty for MSTW08 at $Q^2=100 \text{ GeV}^2$ using **1fb-1** of LHCb data



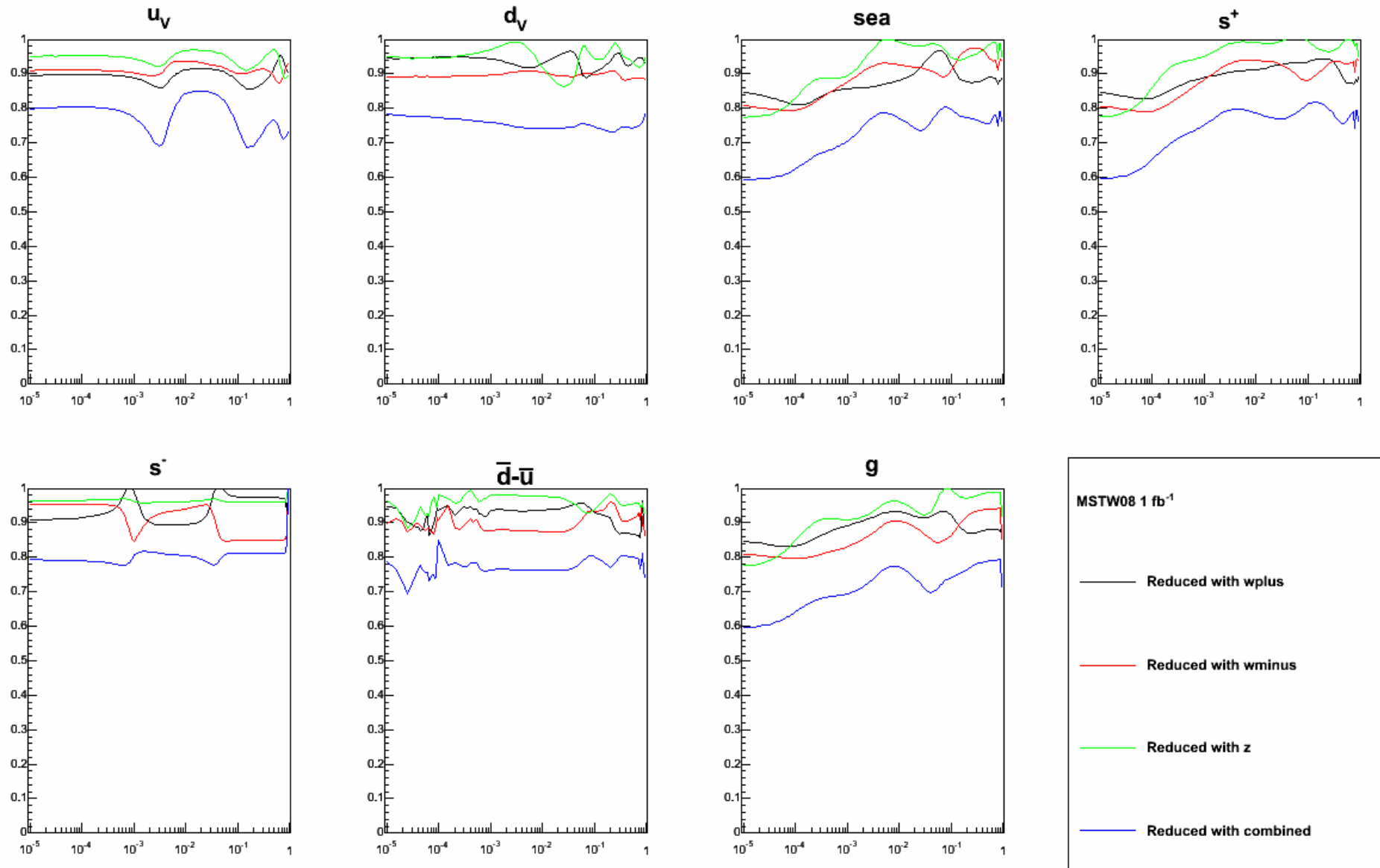
Effect on absolute uncertainty for MSTW08 at $Q^2=100 \text{ GeV}^2$ using **10fb-1** of LHCb data



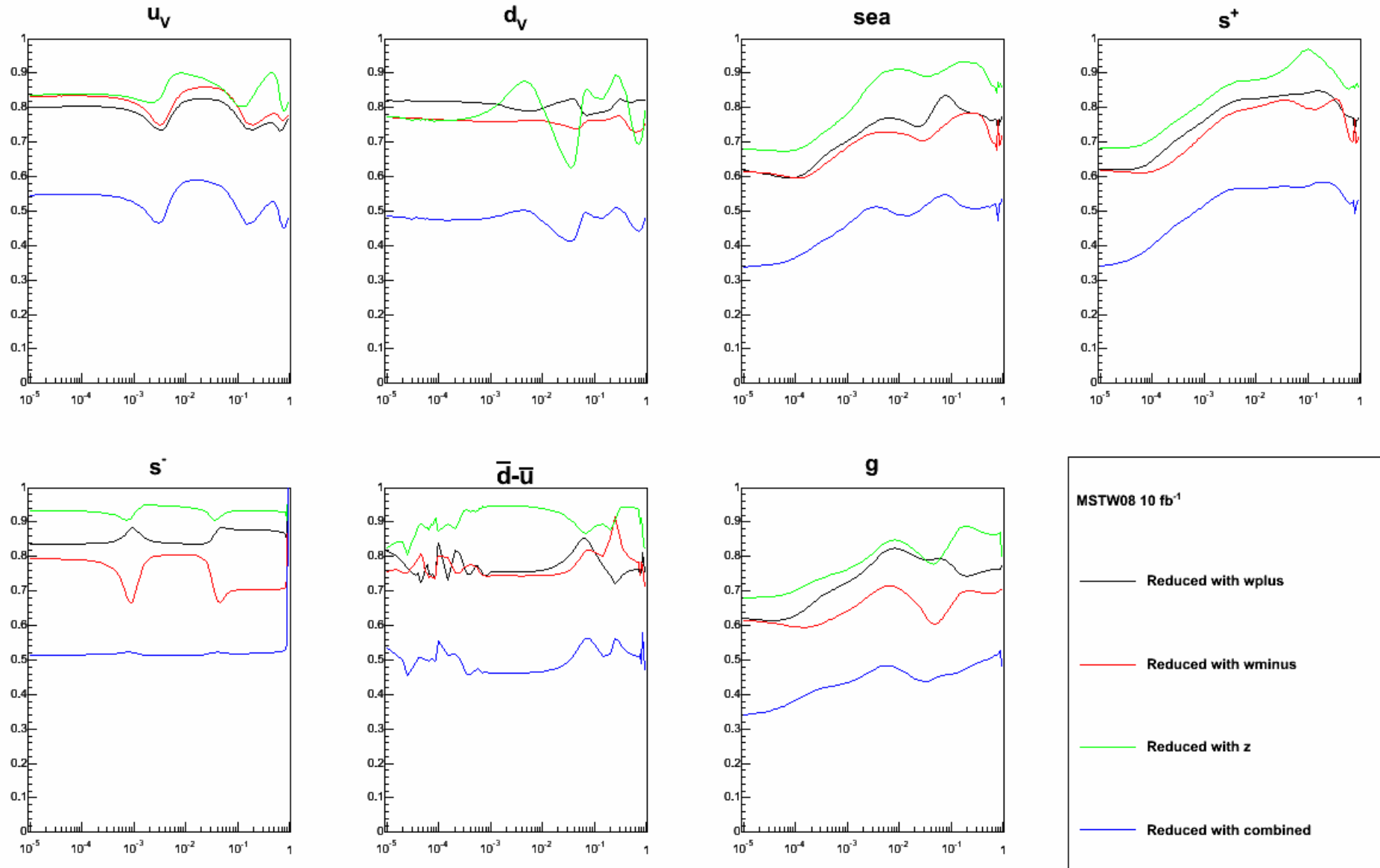
Ratio of uncertainty after fit to before for MSTW08 at $Q^2=100 \text{ GeV}^2$ using **0.1 fb⁻¹** of LHCb data



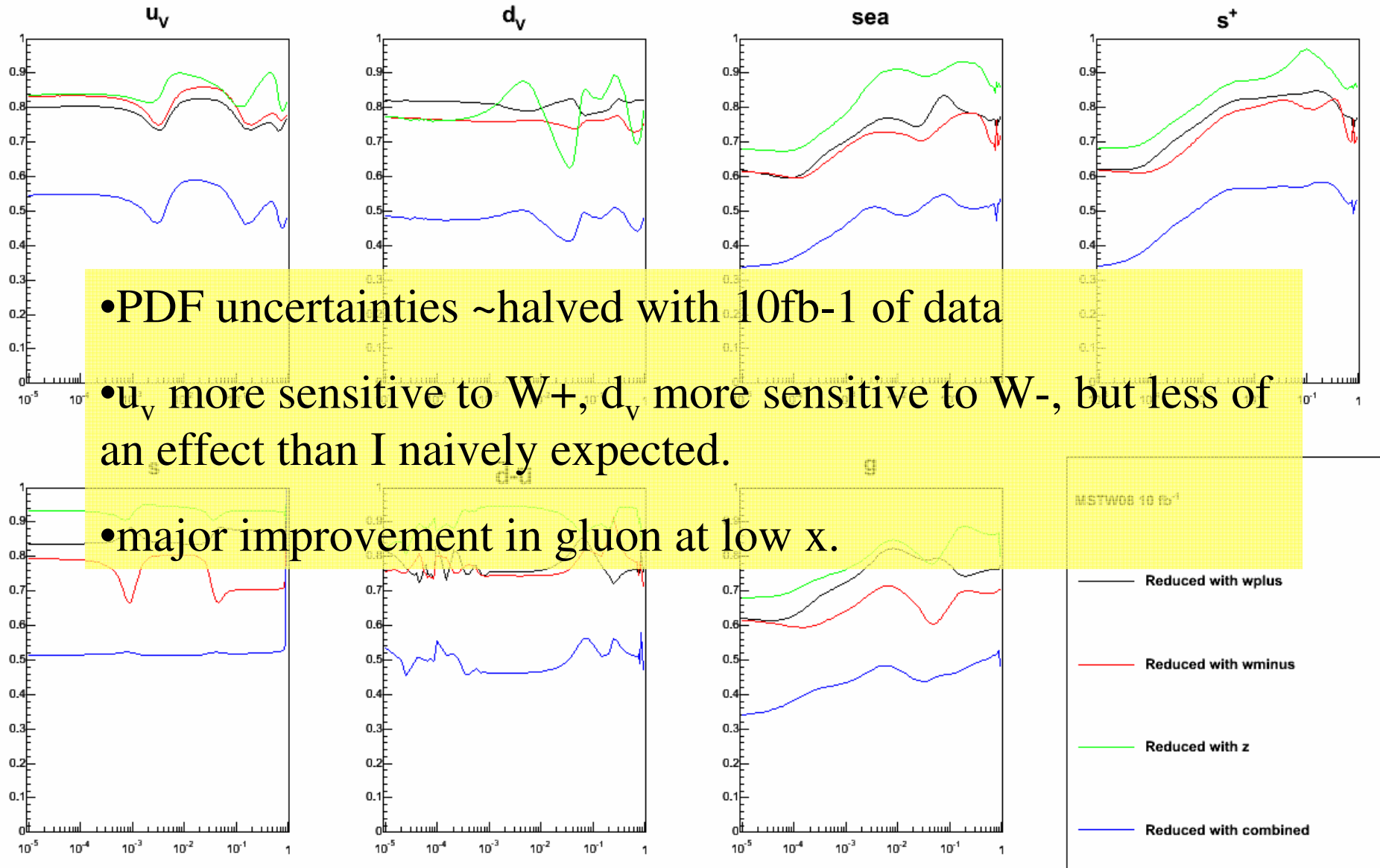
Ratio of uncertainty after fit to before for MSTW08 at $Q^2=100 \text{ GeV}^2$ using **1 fb-1** of LHCb data



Ratio of uncertainty after fit to before for MSTW08 at $Q^2=100 \text{ GeV}^2$ using **10 fb⁻¹** of LHCb data

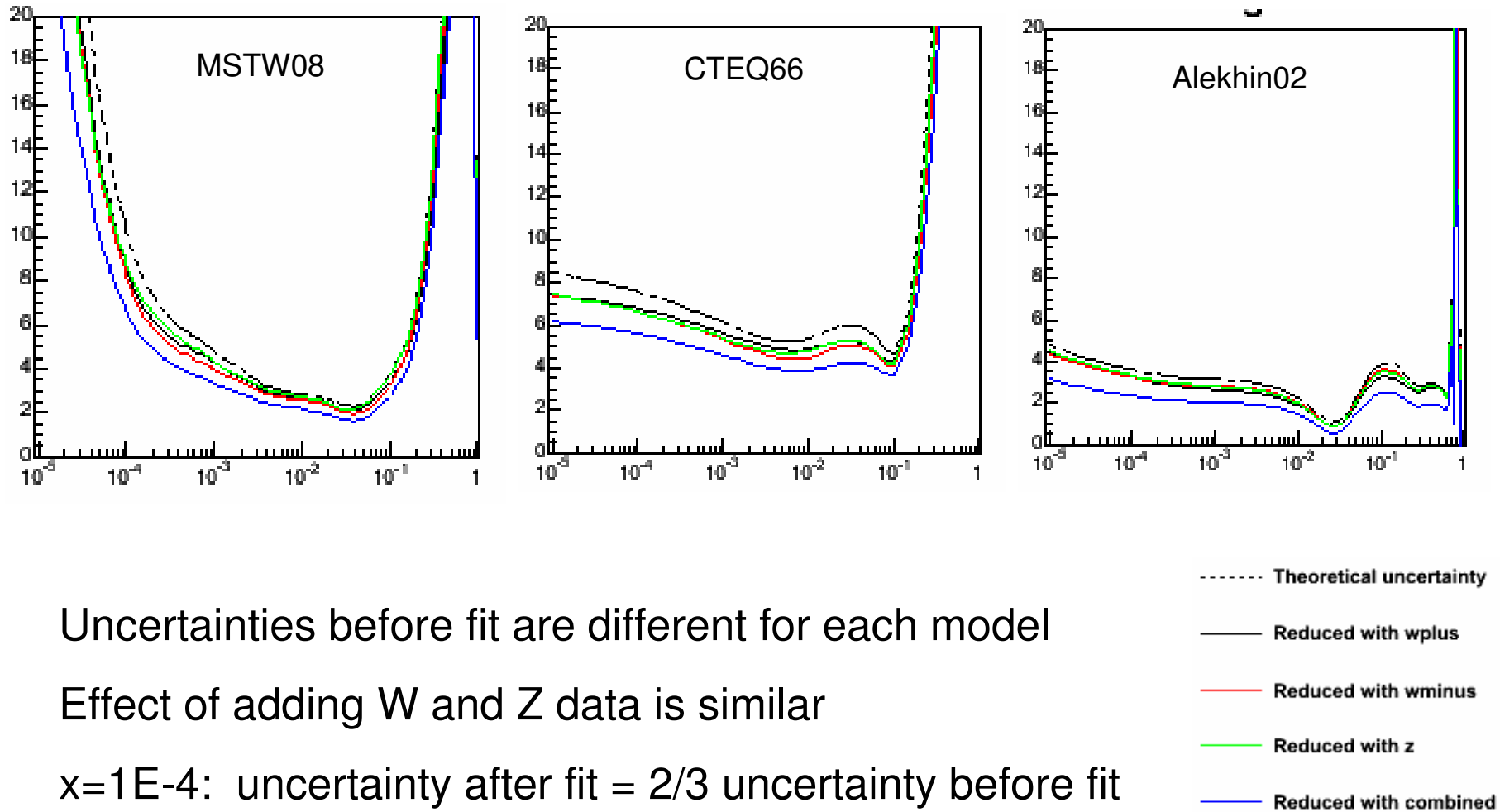


Ratio of uncertainty after fit to before for MSTW08 at $Q^2=100 \text{ GeV}^2$ using **10 fb⁻¹** of LHCb data



First look at
effect on other PDF sets

Effect on gluon PDF with fit to 1fb^{-1} of LHCb data at $Q^2=100\text{ GeV}^2$

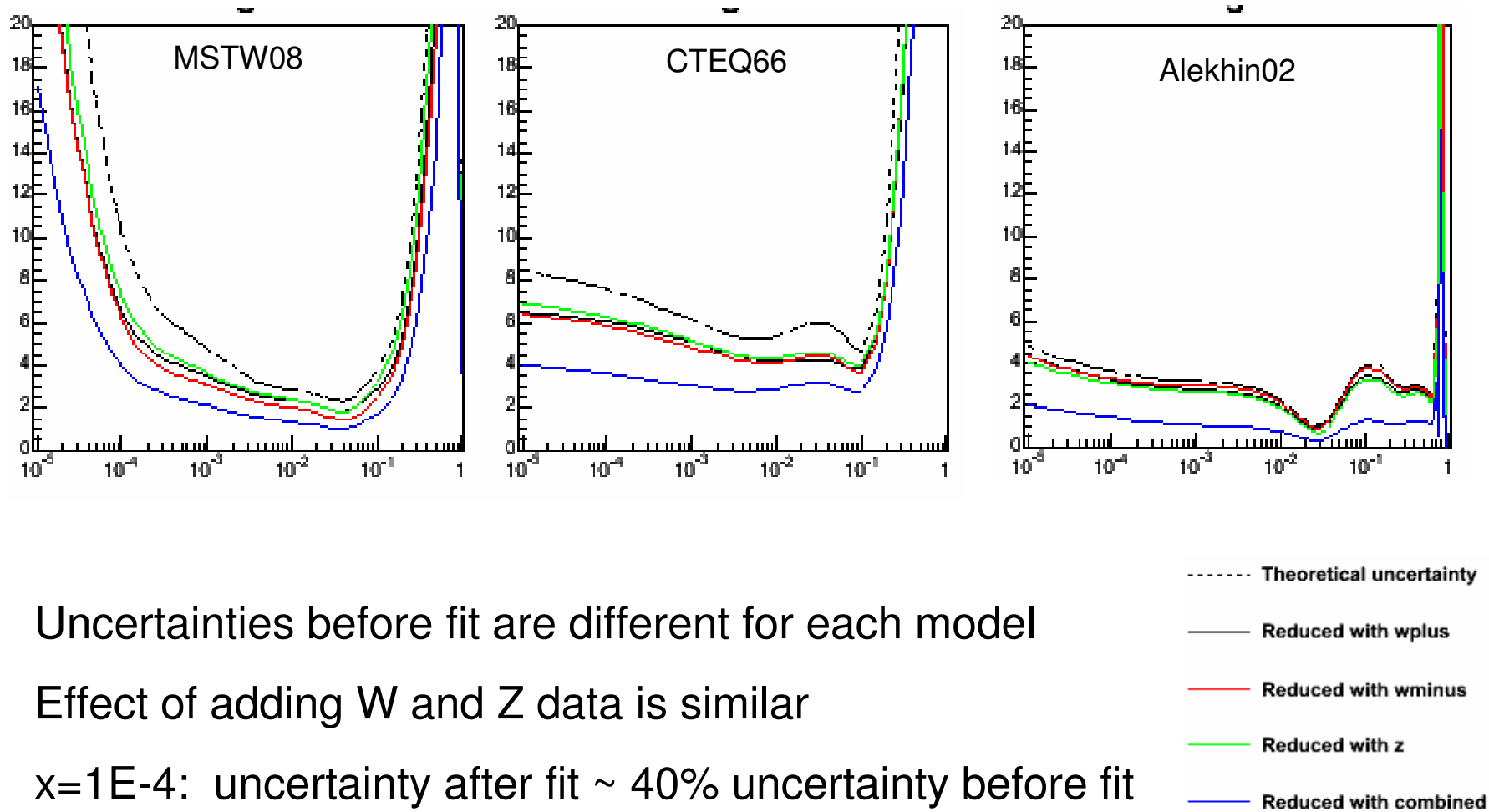


Uncertainties before fit are different for each model

Effect of adding W and Z data is similar

$x=1\text{E-}4$: uncertainty after fit = 2/3 uncertainty before fit

Effect on gluon PDF with fit to 10fb^{-1} of LHCb data at $Q^2=100\text{ GeV}^2$



Future work

- Further cross-check with physics expectations.
- Extend fits to other PDF sets
- Fit to differential distribution for $\gamma^* : \frac{d^2\sigma}{dQ^2 dy}$
(preliminary results show major improvements)