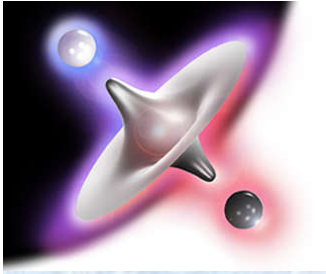


# Antimatter in the Laboratory



Rolf Landua  
CERN

Summer Student Lectures 2006



# Anti-Plan

## Introduction

Einstein, Dirac, Feynman, CPT

## Precision Experiments

Muon magnetic moment ( $g-2$ )  
Antiproton inertial mass

## Antimatter 'Factory'

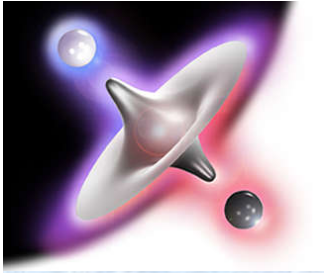
How are antiprotons made?

## Antihydrogen

Short history  
ATHENA and ATRAP  
Making antihydrogen  
Future developments

## Antimatter technology

PET  
Antiproton therapy?  
Rocket propulsion??

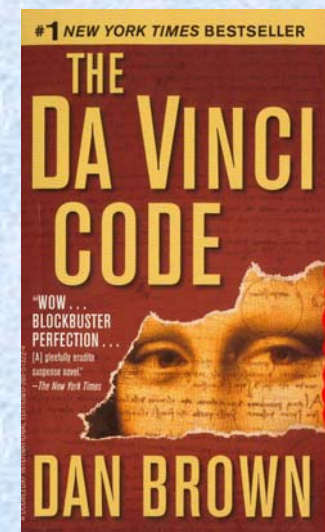


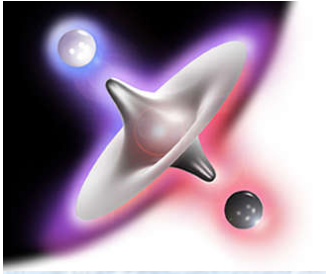
# How antimatter @ CERN \*really\* became famous

1996  
First Antihydrogen Atoms  
Made at LEAR

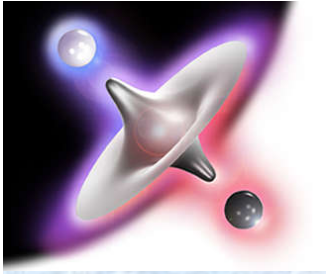


2000  
CERNs 'Antimatter Factory' AD





# I. Introduction



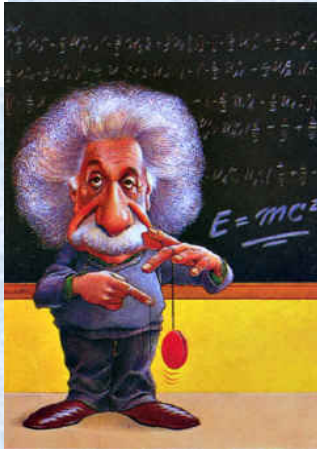
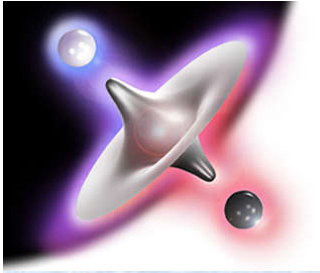
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...the discovery of antimatter was perhaps the biggest jump of all the big jumps in physics in the 20th century.

Werner Heisenberg



# Theory of special relativity



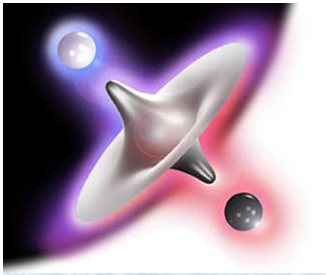
A. Einstein (1905)

$$E=mc^2$$

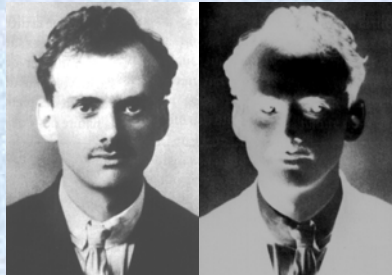
**Mass is condensed energy**

( $c^2$  = exchange rate!)

$$1 \text{ kg} = 9 \cdot 10^{16} \text{ J} = 2.5 \cdot 10^{10} \text{ kWh} = 2.85 \text{ GW} \cdot \text{year}$$



## Relativity + Quantum Theory = Antimatter



Paul A.M. Dirac (1928)

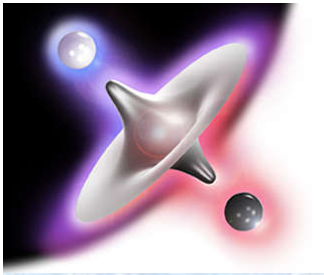
$$(i\gamma^\mu \partial_\mu - m)\psi = 0$$

$$\psi_+ = \begin{pmatrix} 1 \\ 0 \\ 0 \\ 0 \end{pmatrix} \text{ or } \begin{pmatrix} 0 \\ 1 \\ 0 \\ 0 \end{pmatrix} e^{-i m t} \quad \psi_- = \begin{pmatrix} 0 \\ 0 \\ 1 \\ 0 \end{pmatrix} \text{ or } \begin{pmatrix} 0 \\ 0 \\ 0 \\ 1 \end{pmatrix} e^{+i m t}$$

Electron: spin 1/2

Another spin-1/2 particle??

- For  $v \neq 0$ , upper and lower components mix
- 1929: Positive electron = proton ????
- 1931:  $m(e^-) = m(e^+)$  ! Annihilation possible ...



## Positron discovery- why so late ?



C. D. Anderson.  
*Phys. Rev.*, **43**, 491 (1933).

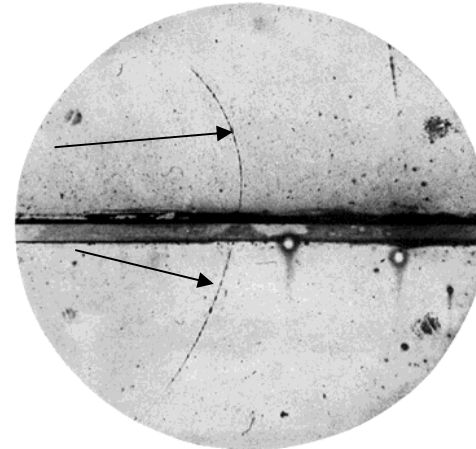


FIG. 1. A 63 million volt positron ( $H_p = 2.1 \times 10^6$  gauss-cm) passing through a 6 mm lead plate and emerging as a 23 million volt positron ( $H_p = 7.5 \times 10^6$  gauss-cm). The length of this latter path is at least ten times greater than the possible length of a proton path of this curvature.

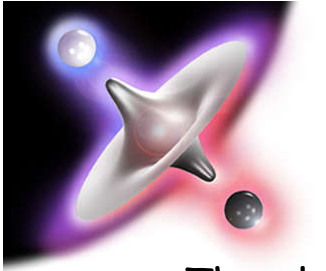
Dirac (1932):

"Why did the experimentalists not see them? **Because they were prejudiced against them.**

The experimentalists ... sometimes saw the opposite curvature, and interpreted the tracks as electrons which happened to be moving into the source, instead of the positively charged particles coming out.

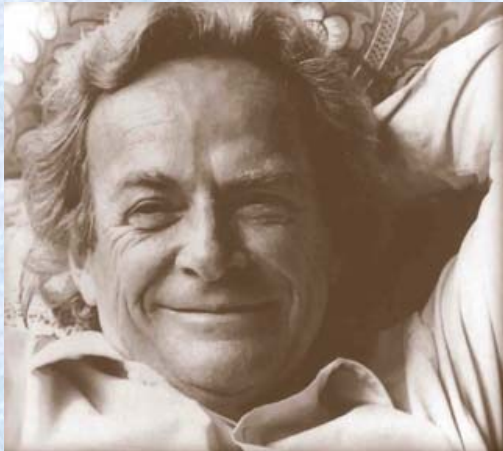
People were so prejudiced against new particles that they never examined the statistics of these particles entering the source to see that there were really too many of them."



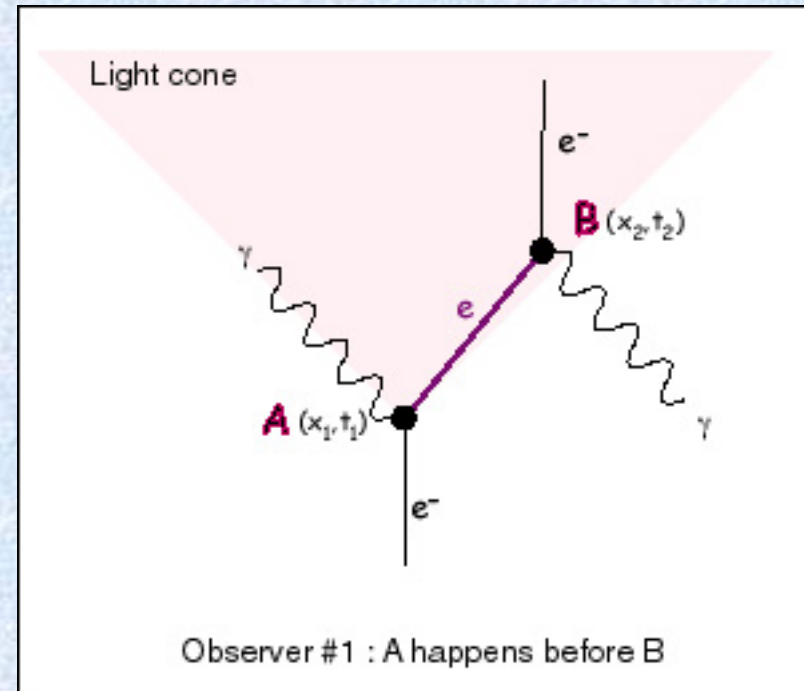


## Antimatter in Quantum Field Theory

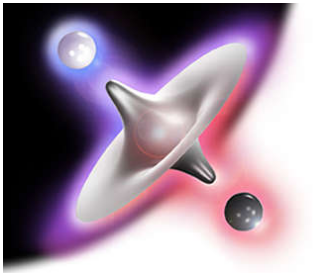
The electron (field) is no longer described by a wave function but an operator that creates and destroys particles. All energies are positive.



R. P. Feynman

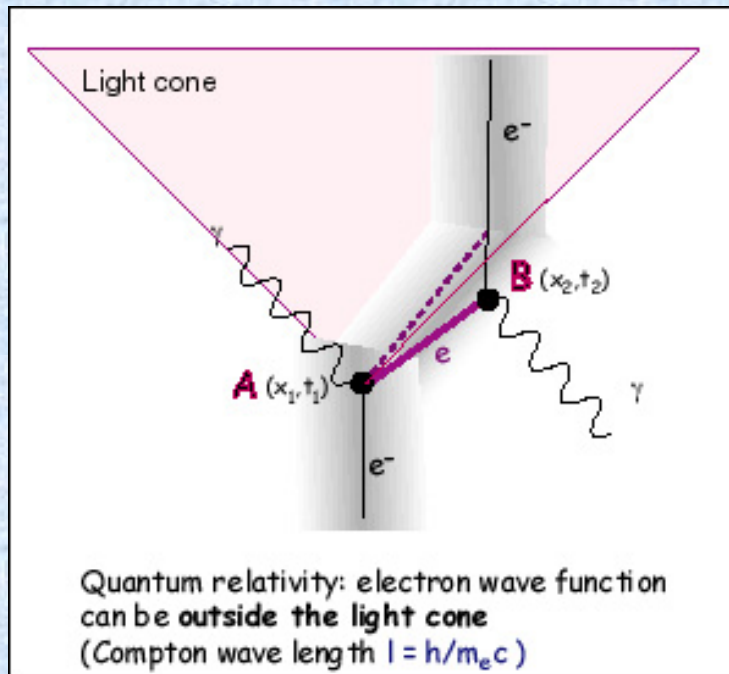


An electron can emit a photon at A, propagate a certain distance, and then absorb another photon at B.

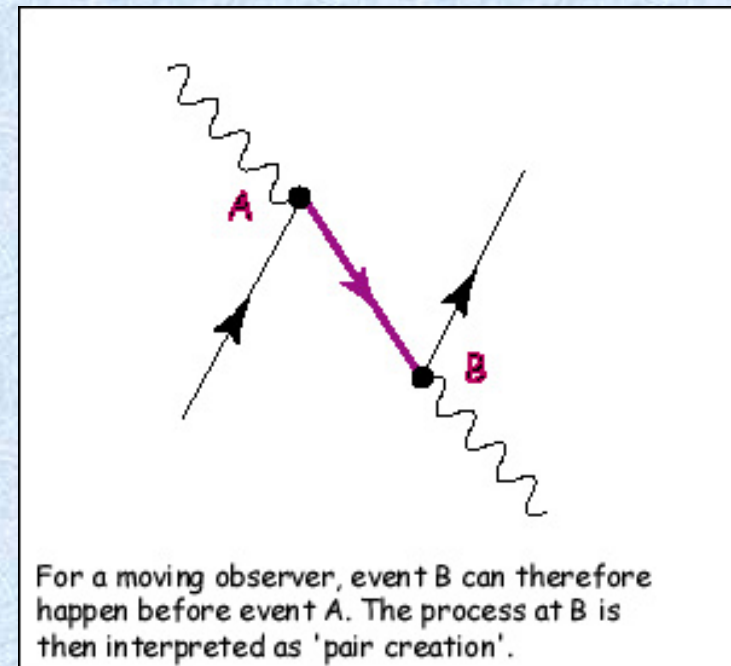
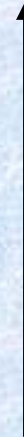


## Why antimatter must exist in quantum theory

Wave function only localized within Compton wave length ( $\lambda \sim 1/m$ ).

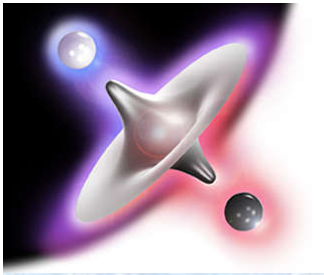


†



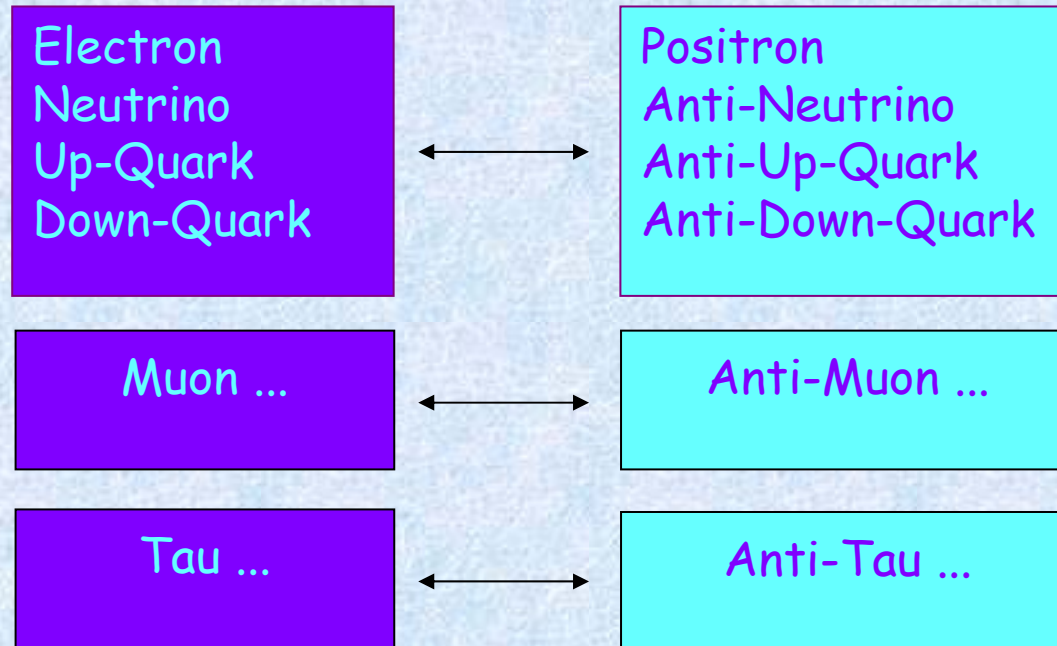
“One observer's electron is the other observer's positron”.

The presence of antiparticles is necessary to restore the **causal structure** to the process seen in another inertial system.



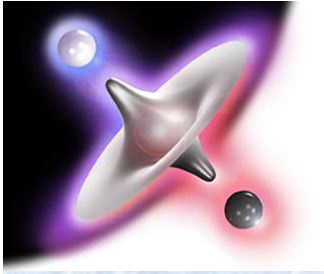
## Therefore:

Every particle has an antiparticle



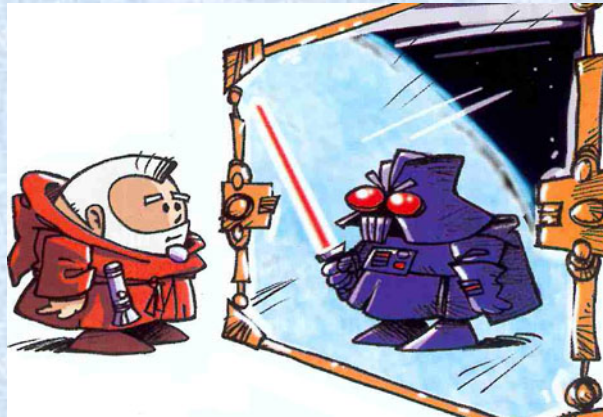
After Dirac, the fundamental spectrum of particles doubled  
In 1973, supersymmetry made a similarly bold prediction ...





# Particles and antiparticles

How can we imagine an 'anti-particle'?



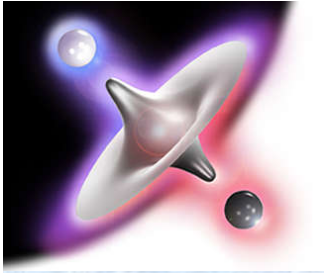
Electron

Positron



Particles and anti-particles are two manifestations of the same underlying, but yet unknown, physical structure (superstrings??).





## CPT Theorem \*

IF :

- |                                  |  |
|----------------------------------|--|
| 1) Locality                      | (no action at a distance)  |
| 2) Lorentz invariance            | (all inertial frames are equivalent)   |
| 3) Causality                     | (no interaction between two space-time points outside each other's light cone) |
| 4) Vacuum is lowest energy state | (spin-statistics connection)   |

Then:

Particles and antiparticles must have

- equal masses
- equal lifetimes
- equal magnitude (opposite sign) of quantum numbers, e.g. charge
- equal energy levels of bound states

\*1955 - Proof of CPT theorem by Pauli (following work by Schwinger and Lüders)



## Why should we test CPT symmetry?

### Dirac's Vision (from his Nobel lecture, 1933)

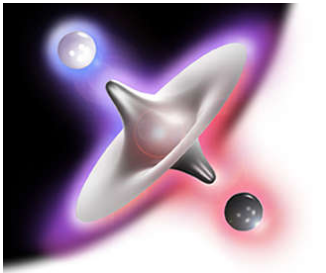
"If we accept the view of complete symmetry between positive and negative electric charge so far as concerns the fundamental laws of Nature, we must regard it rather as an accident that the Earth (and presumably the whole solar system), contains a preponderance of negative electrons and positive protons. It is quite possible that for some of the stars it is the other way about, these stars being built up mainly of positrons and negative protons. In fact, there may be half the stars of each kind. The two kind of stars would both show exactly the same spectra, and there would be no way of distinguishing them by present astronomical methods."

From his Nobel lecture (12 December 1933)



Is CP-violation the reason for cosmological imbalance? May be.

But: CPT theorem is a formidable challenge for experimentalists!  
CPT Violation could give an alternative explanation.



# Antimatter gravitation is not constrained by CPT

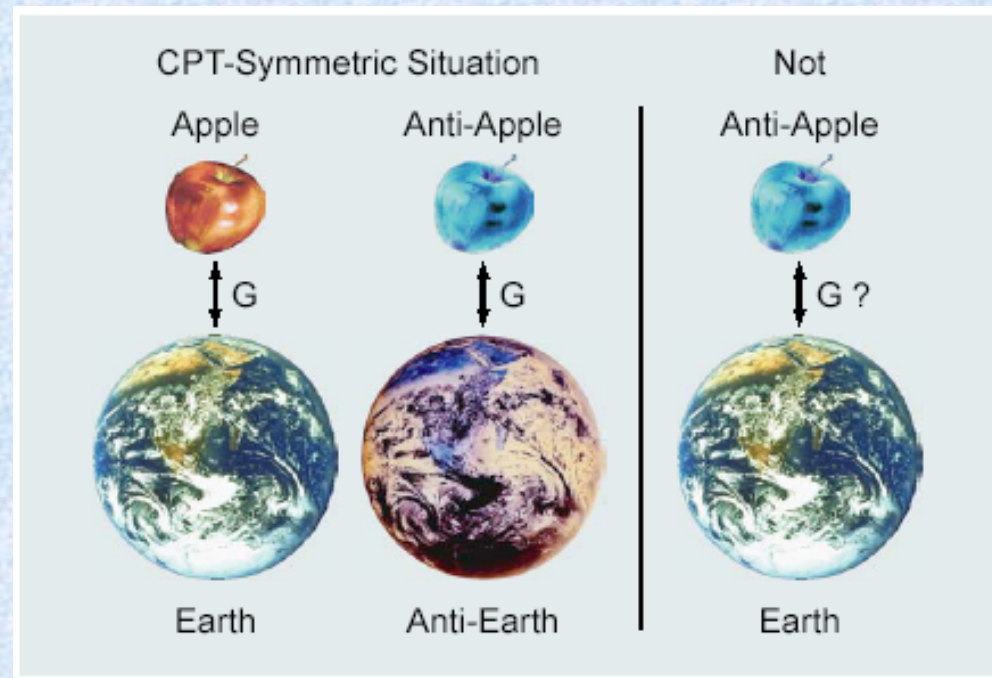
**"Weak" equivalence principle:**

The world-line of a free falling body is independent of its composition or structure

**Gravitational = Inert mass**

**Possible violations:**

- Additional components of gravitational field (baryon number dependent)
- Short-range deviations ( $\ll$  mm) from inverse square-law (e.g. due to extra-dimensions)



Technology in development:

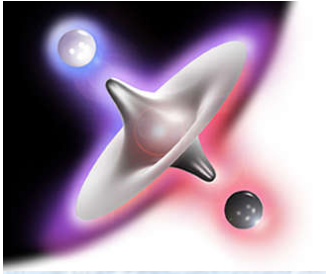


## Measurement of gravitational acceleration by dropping atoms

Achim Peters, Keng Yeow Chung & Steven Chu

Physics Department, Stanford University, Stanford, California 94305-4060, USA

A. Peters et al., Nature 400 (1999) 849

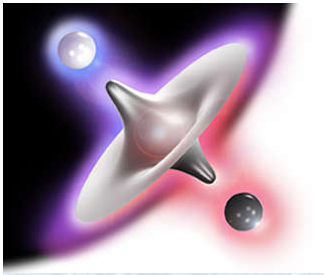


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II.

# PRECISION EXPERIMENTS WITH ANTIMATTER





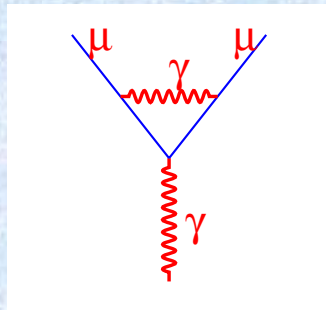
# Muon (and antimuon) magnetic moment

$$\mu_\mu B = g (e/2m) B$$

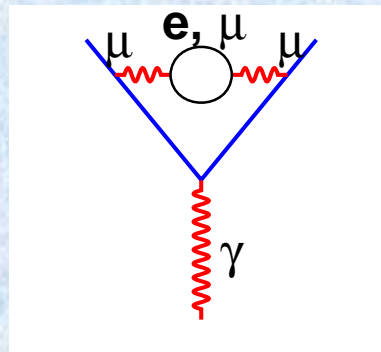
$$\text{Dirac: } g = 2$$

$$\text{QED: } g = 2 (1+a)$$

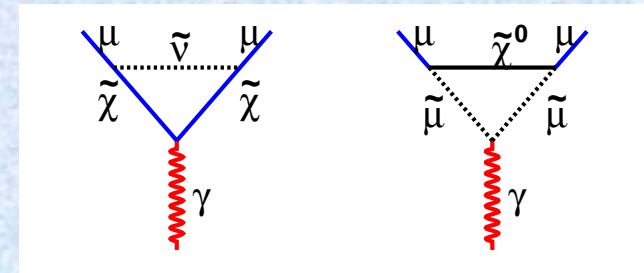
$a$  :



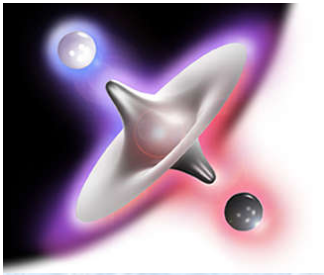
Photons



Leptons  
Quarks

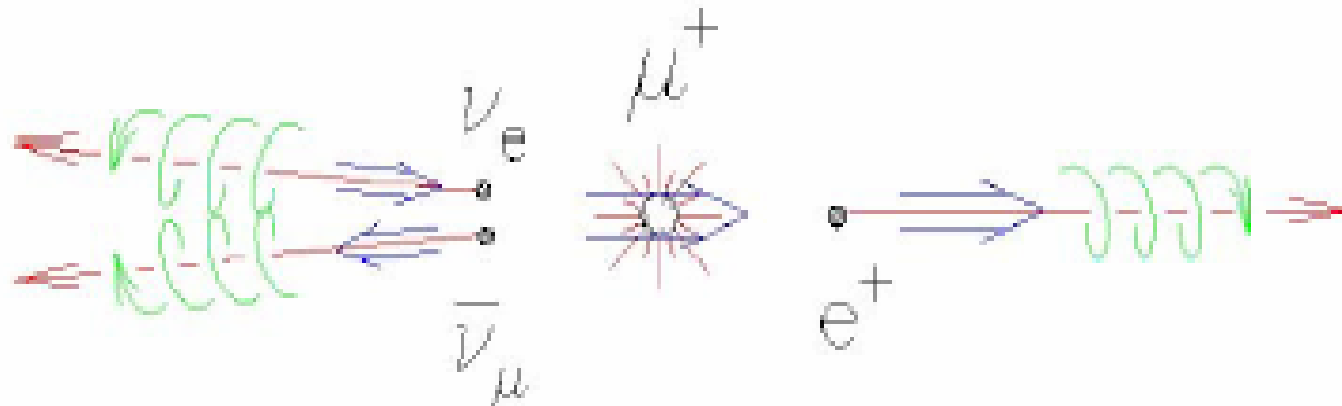


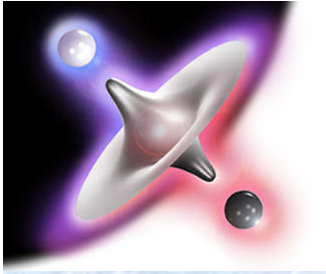
New particles?



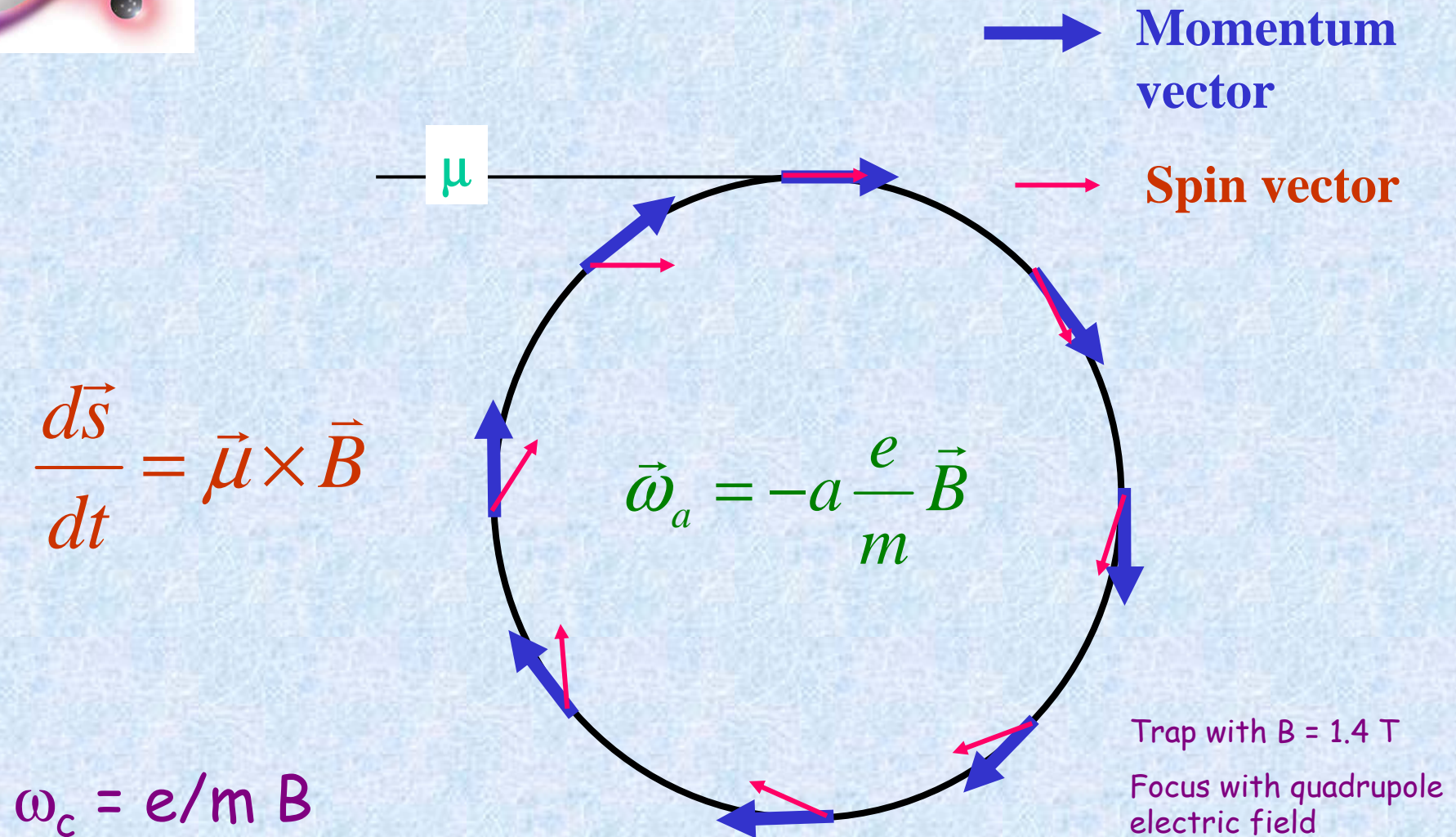
## Muon: born polarized, decaying polarized

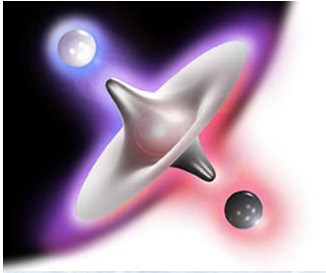
- Muon is born polarized:  $\pi^+ \rightarrow \mu^+ + \nu_\mu$
- Muon shows its polarization when it dies:  $\mu^- \rightarrow e^- + \bar{\nu}_e + \nu_\mu$





# Spin Precession in storage ring

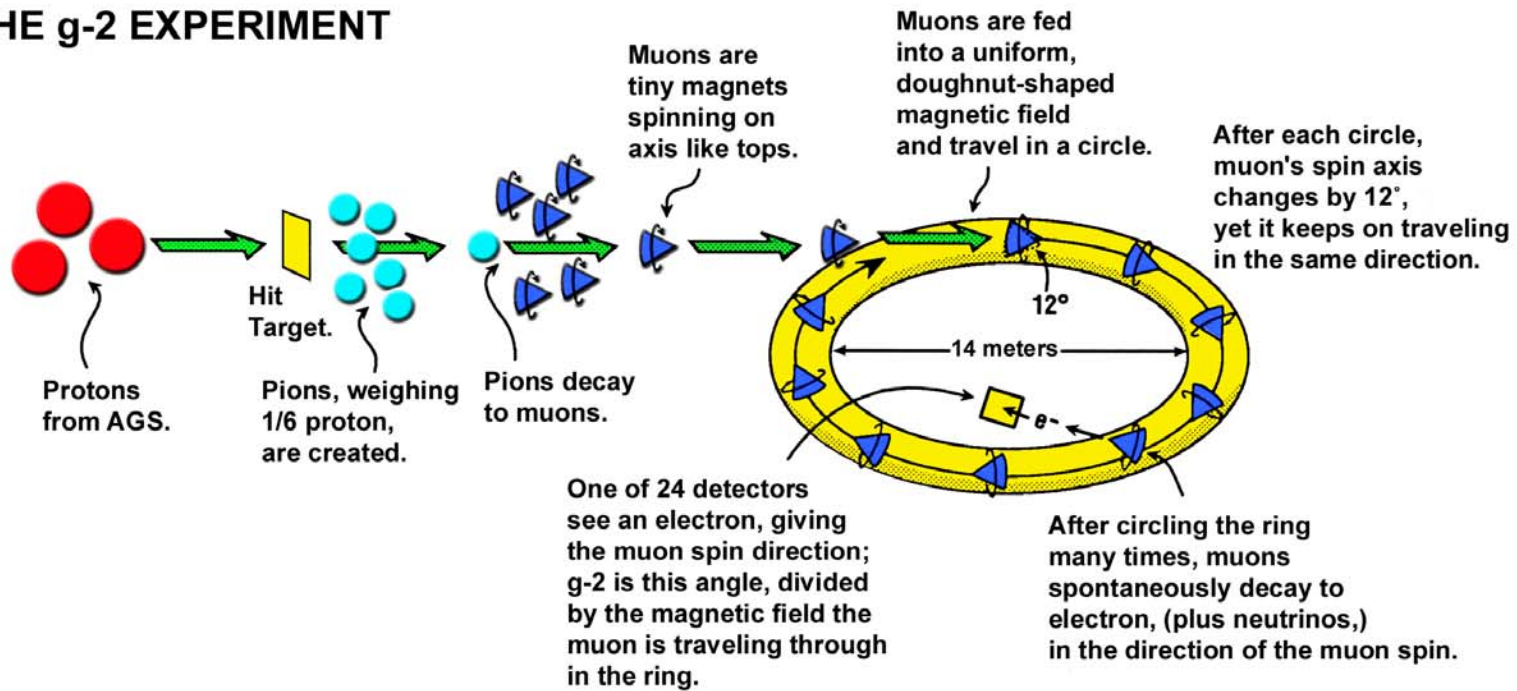




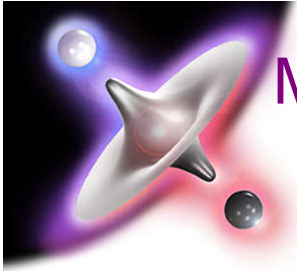
# Principle of experiment

## BNL 821 Brookhaven "g-2"

### LIFE OF A MUON: THE g-2 EXPERIMENT



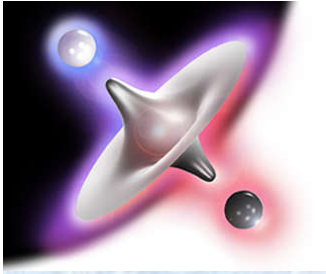




## Muons (antimuons) circulate and decay in storage ring

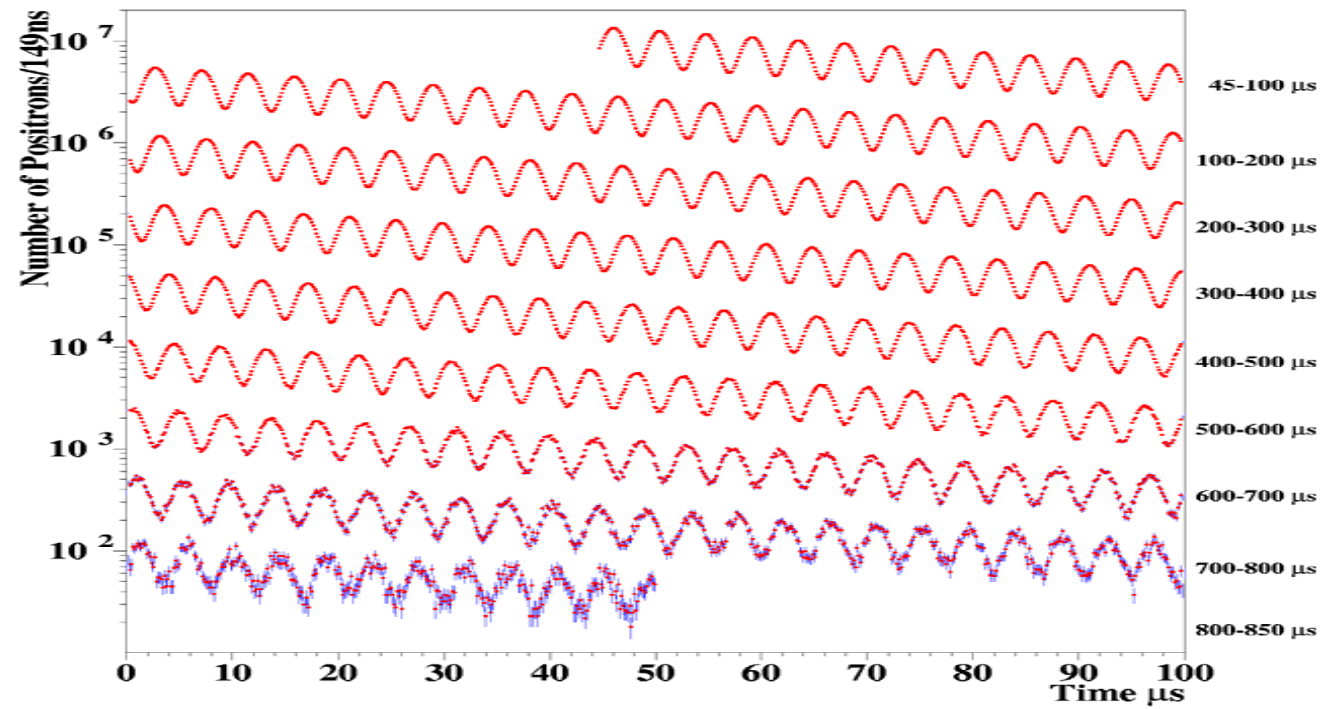
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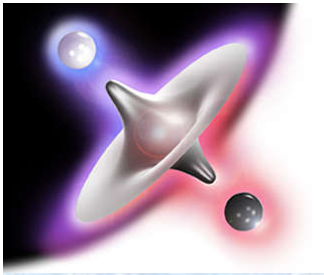
QuickTime™ and a  
TIFF (Uncompressed) decompressor  
are needed to see this picture.



# Electron counting rate from muon decay

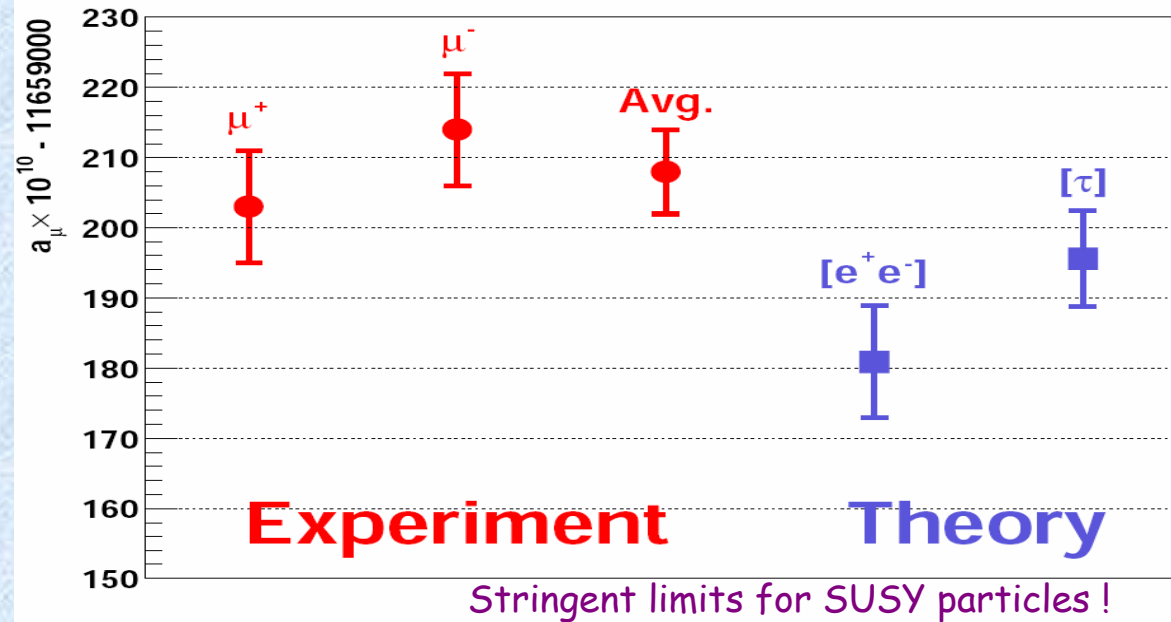
4.5 Billion Positrons with  $E > 2$  GeV





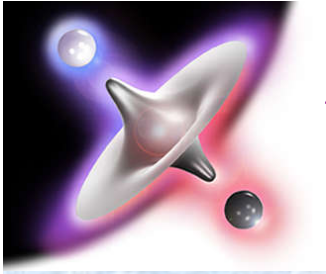
## Results

Experiment vs Theory (for negative muons):



Test of CPT (positive vs negative muons):

$$(g_{\mu^+} - g_{\mu^-}) / g_{av} = (-2.6 \pm 1.6) \times 10^{-8}$$



## A short break to think about precision measurements

---

Precision of a measurement increases with observation time



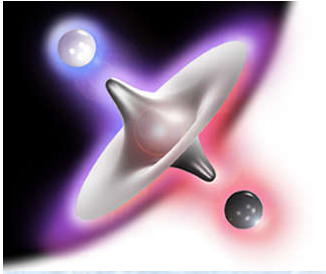
Presence of other particles may decrease precision



Isolate (few) particles and  
observe for long times:

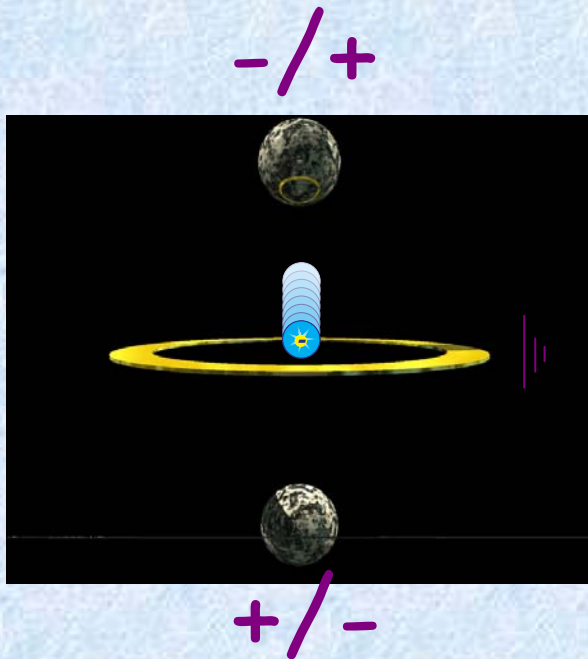
**PARTICLE TRAPS**



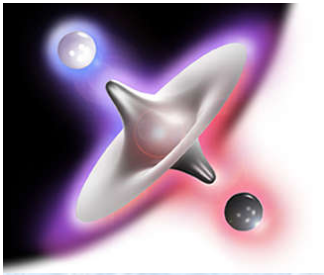


## RF-trap (“Paul trap”)

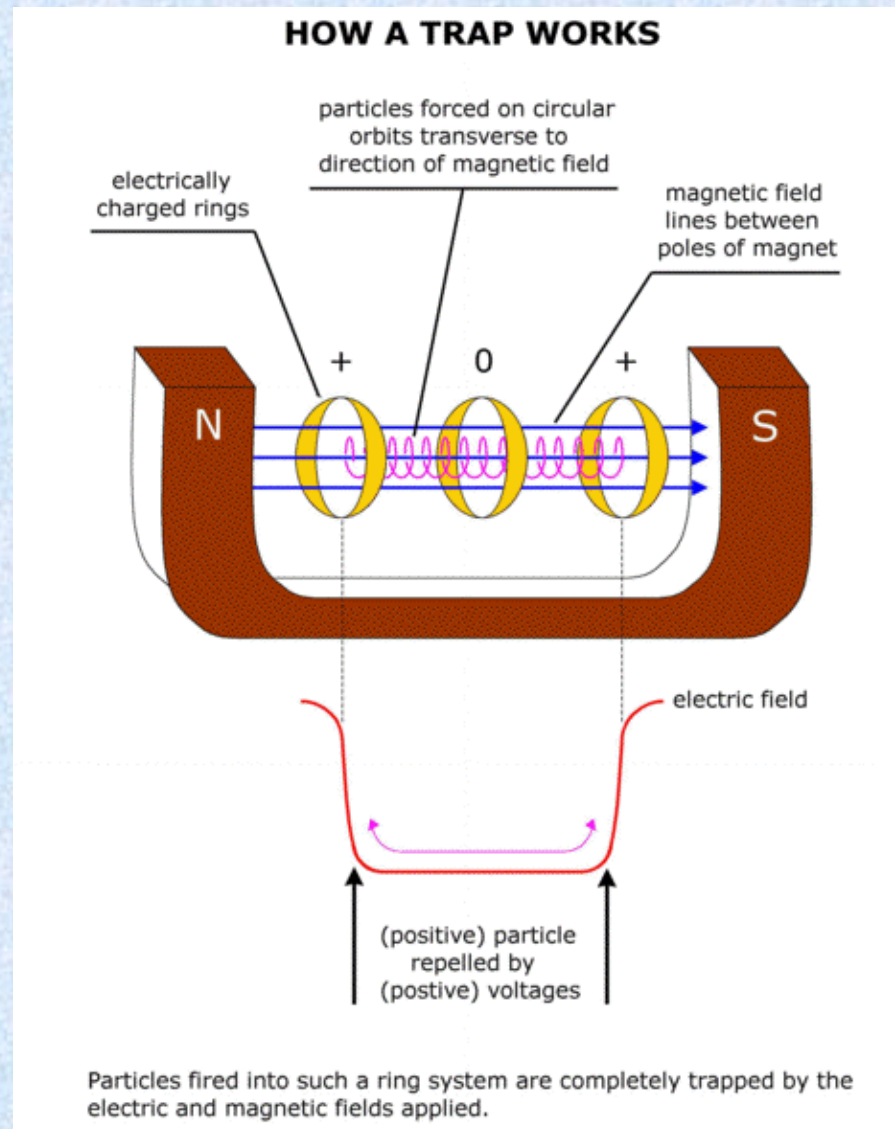
A radio-frequency current on the electrodes maintains an alternating electric field that confines charged particles in a small space.

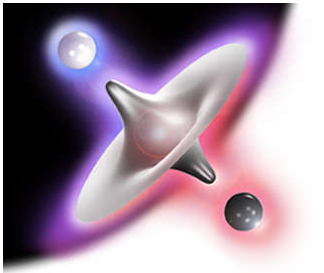


QuickTime™ and a  
H.263 decompressor  
are needed to see this picture.



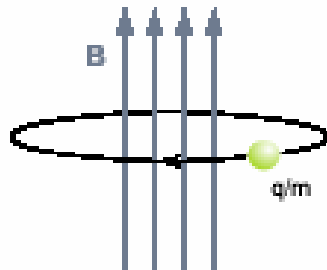
# Magnetic traps





## Special case: Penning trap

Motion of a charged particle in pure magnetic field:

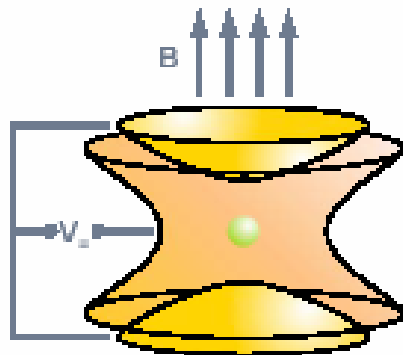


Cyclotron frequency:

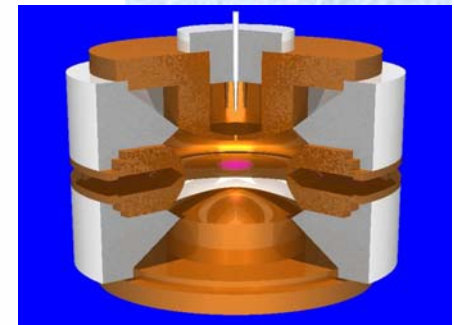
$$f_c = \frac{1}{2\pi} \frac{q}{m} B$$

Penning trap:

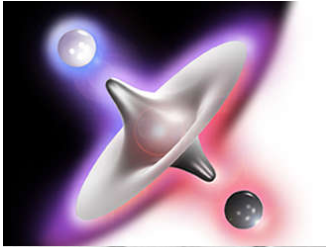
- Strong homogeneous magnetic field
- Weak electric 3D quadrupole field



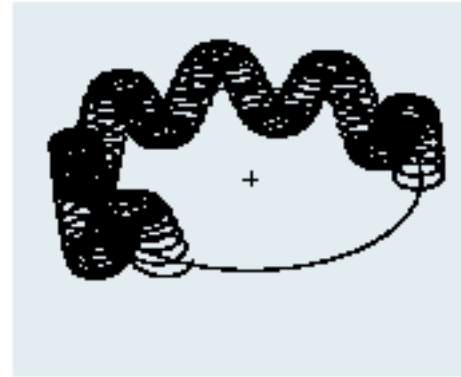
H. G. Dehmelt  
1959



# Antiproton Charge-to-Mass ratio (PS 196, LEAR)



G. Gabrielse



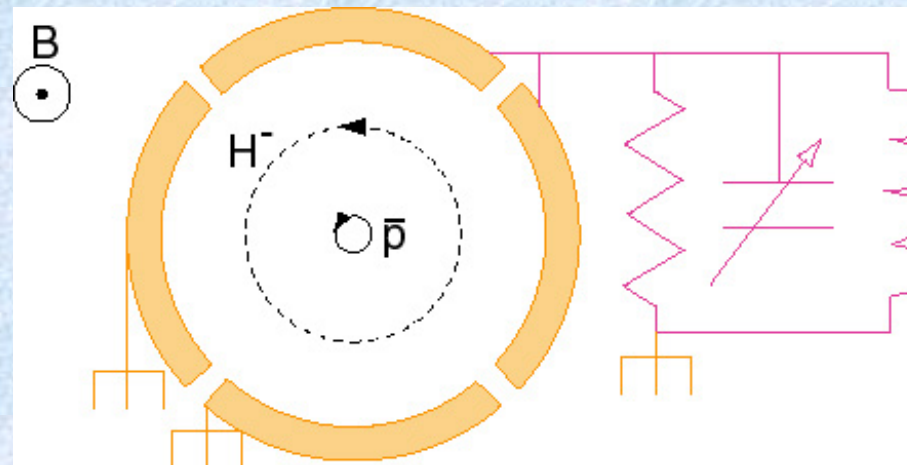
Typical frequencies

$$q = \pm e, B = 3 \text{ T}$$

$$\Rightarrow f_c \approx \text{kHz}$$

$$f_+ \approx 45 \text{ MHz } (p/\bar{p})$$

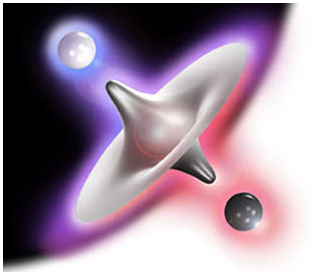
$$f_+ \approx 100 \text{ GHz } (e^\pm)$$



Compare cyclotron frequency of antiprotons and  $H^-$  ions ( $B = 5.3 \text{ T}$ )

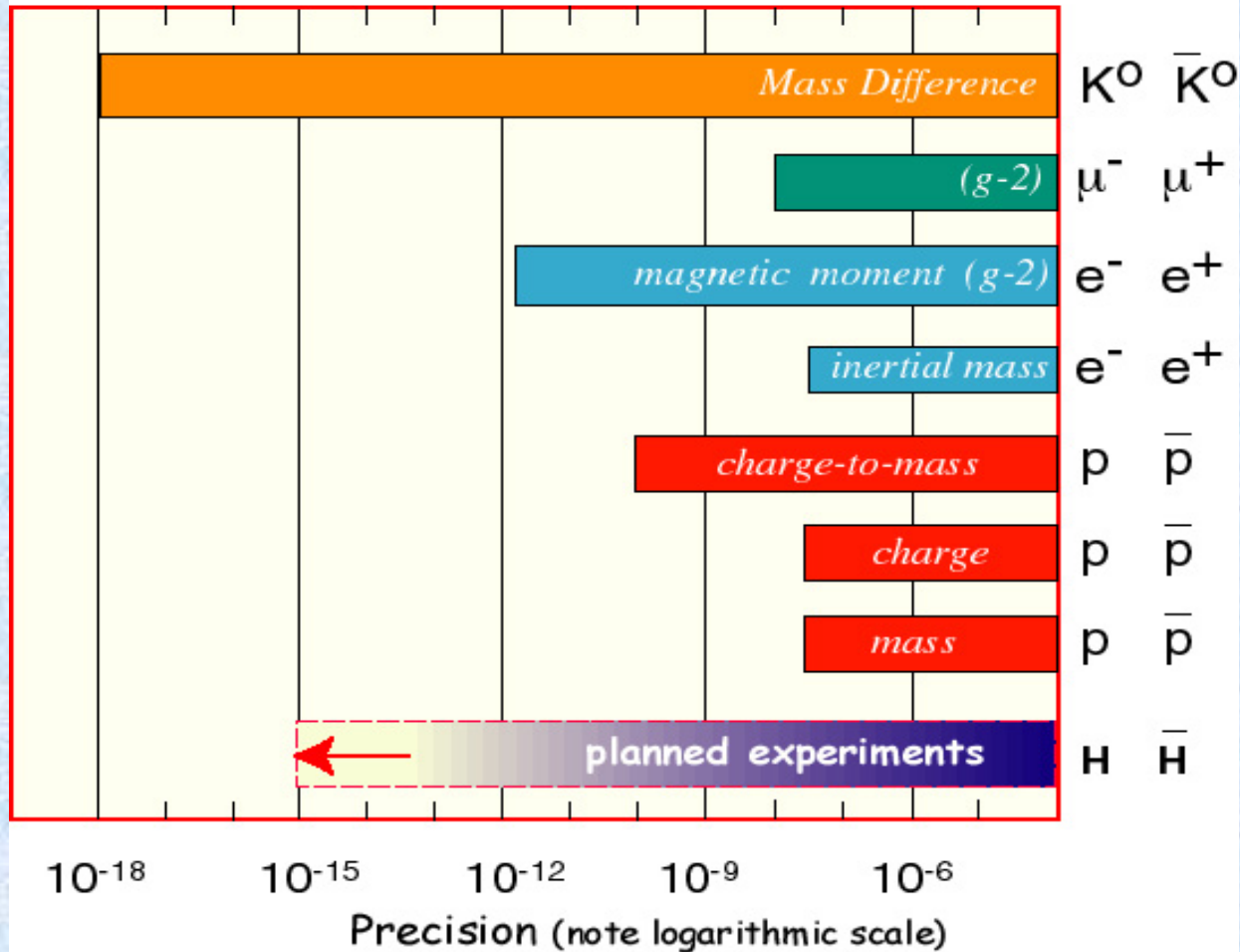
Q/M difference (proton/antiproton) :  $< 9 \times 10^{-11}$

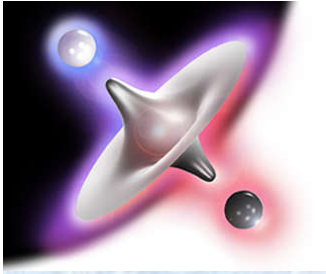




## Summary "Precision Measurements"

### The most precise CPT Tests





## Outlook - Lecture 2

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How do we 'make' antiprotons / antihydrogen ?

To do what?

Antimatter in our daily life?