

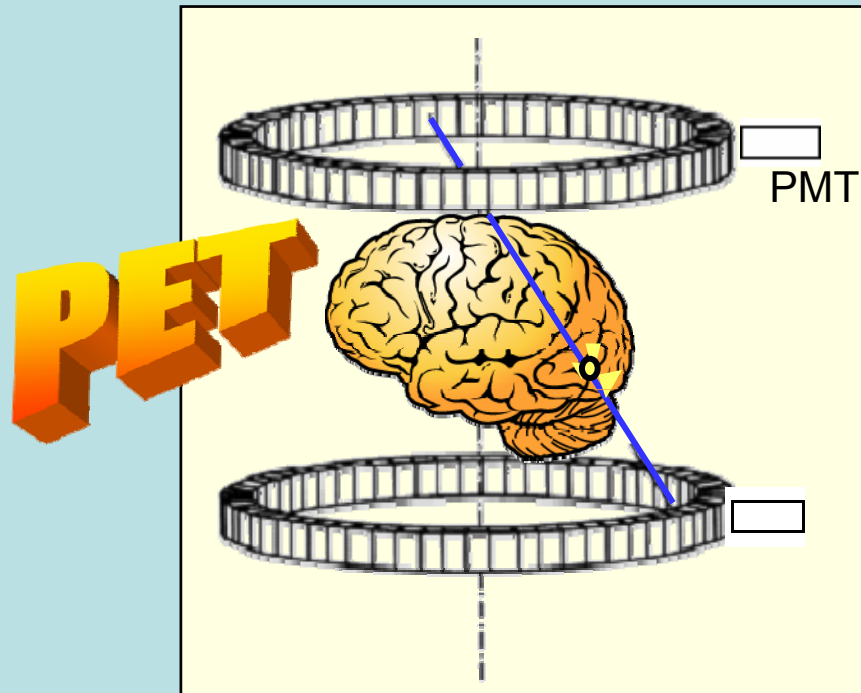
Scintillation studies for
The Axial 3-D PET Concept
HPD-PET project
implemented by Wave Length Shifter
Strip Hodoscope



R. De Leo
INFN, Sezione di Bari, I-70122 Bari, Italy

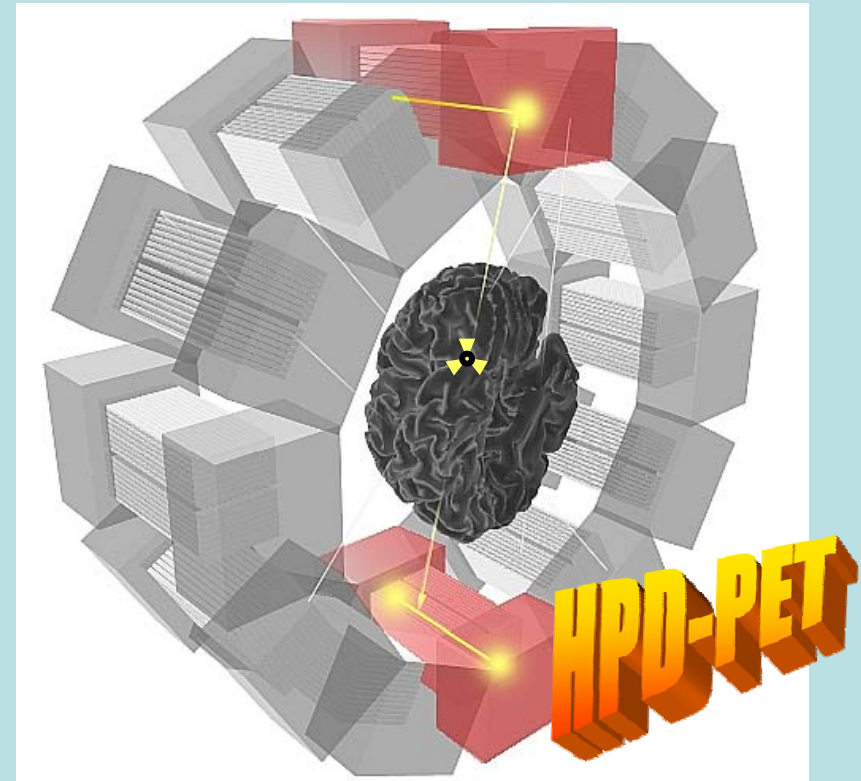
The 3D PET cameras

Standard **radial PET** concept



Many rings of
crystal-photodetector blocks
radially displaced
 $L_c = 1.5-3\text{cm}$

the **axial HPD-PET** concept



Arrays of long ($L_c \sim 10-20\text{ cm}$) crystal bars
read out at both sides by segmented HPDs

Concept made possible by CERN development of rectangular segmented 5" HPDs
with integrated self-triggering electronics

ADVANTAGES OF THE AXIAL HPD-PET CONCEPT

High Granularity → exact reconstruction of the γ interaction point (no parallax error)

- x,y from fired scintillator
 $\sigma(x,y) = 3.2 \text{ mm}/\sqrt{12} = 0.92 \text{ mm}$
 $\Delta x, \Delta y$ (FWHM) = 2.2 mm
- z (DOI) from the ratio of the photoelectrons detected at the two crystal ends
 $\sigma(z)$ linked to the scint. choice

Reduced # of photodet., scint., electr.

→ (12 module PET: only 24 HPDs)

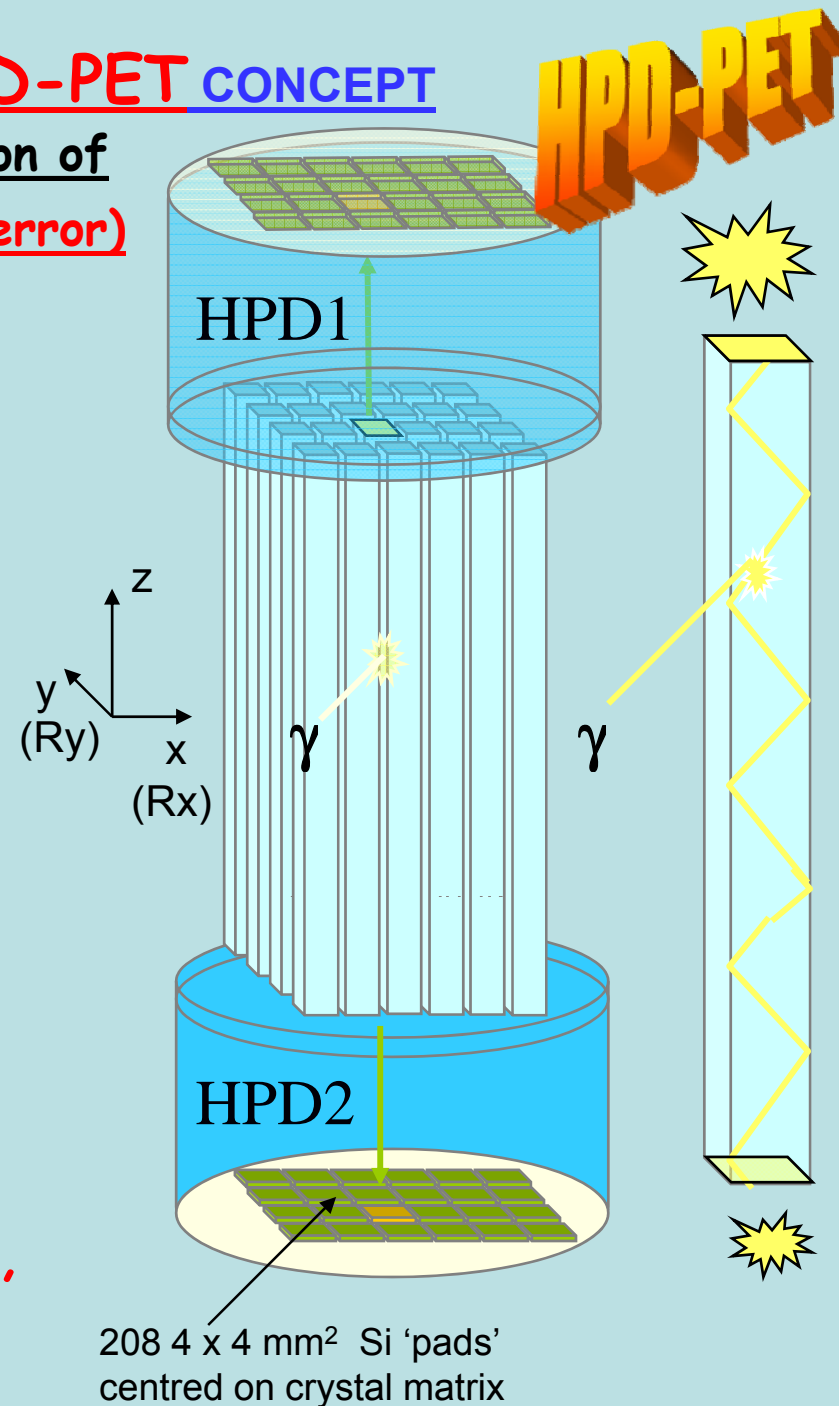
No limit to module radial dimension

→ higher efficiency

Double scatt. events in one module
(Compton-photoel) reconstruction

→ higher efficiency

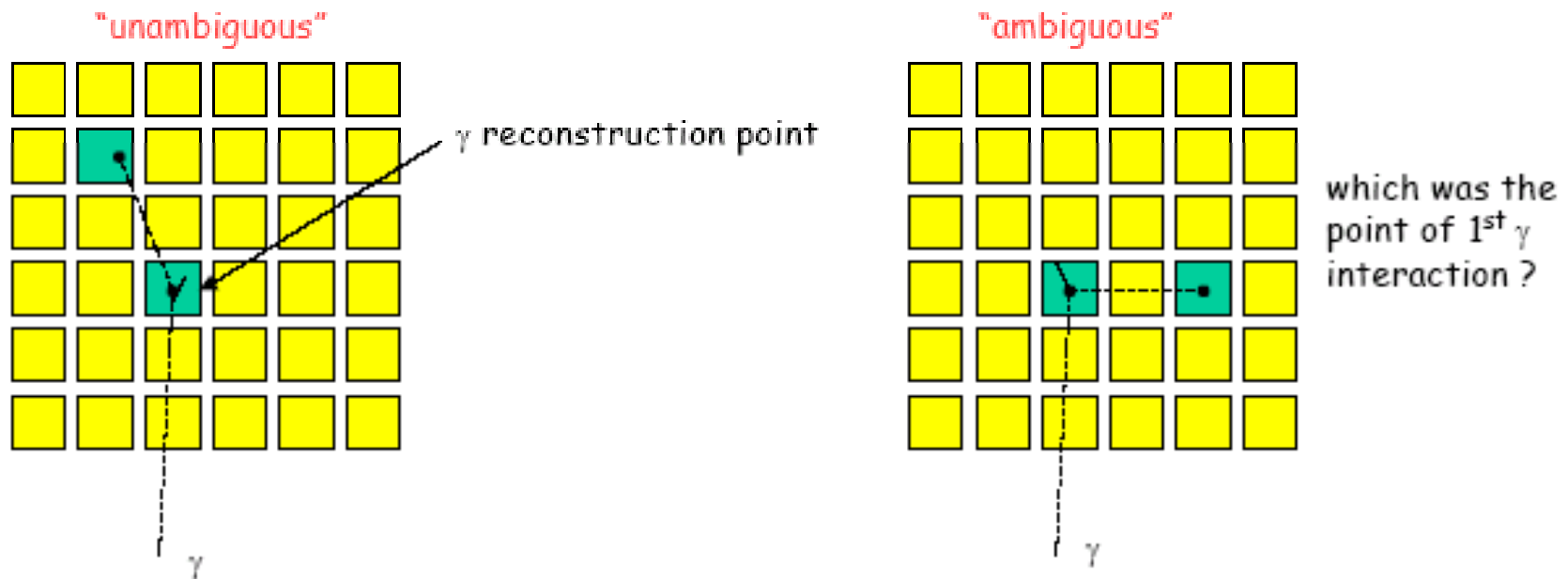
J. Séguinot et al., *Nuovo Cimento C*,
29 (2006)429-463



2) ADVANTAGES OF THE AXIAL HPD-PET CONCEPT

possibility to reconstruct the int. point of part of γ 's that suffers a double (Compton + photoelectric) event in the same module

COMPTON + PHOTOELECTRIC events-



- Select only events in which Compton scattering happens in forward hemisphere
- Restrict to Compton angle $10^\circ \leq \theta \leq 60^\circ$
- Ask for energy deposit in first interaction $E \leq 170$ keV

~ 25% Compton events (50 keV [energy cut] < E < 170 keV) followed by a photoelectric one in the same module can unambiguously be reconstructed

→ detection efficiency increases but spatial resolution worsens

Inorganic Scintillation crystals

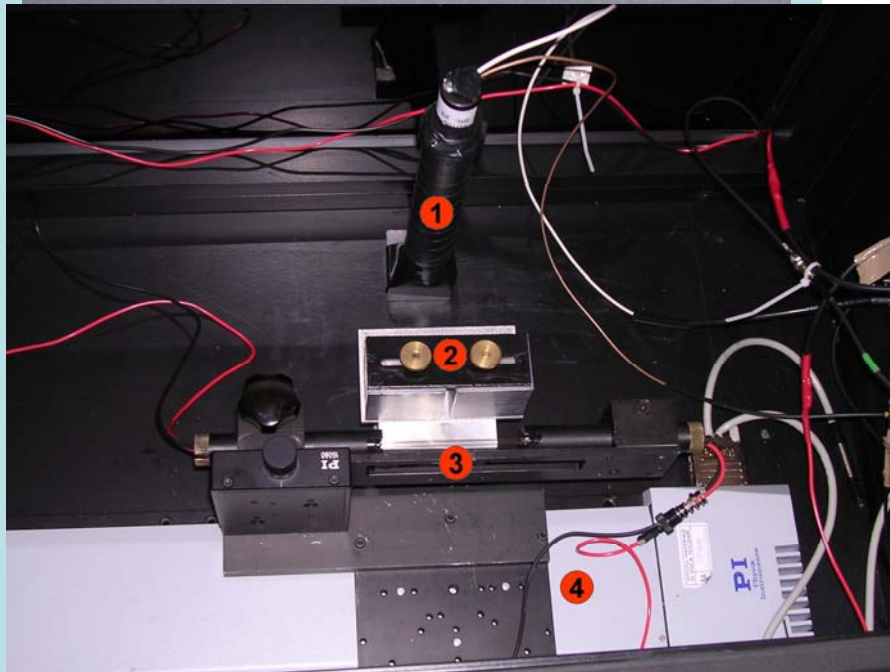
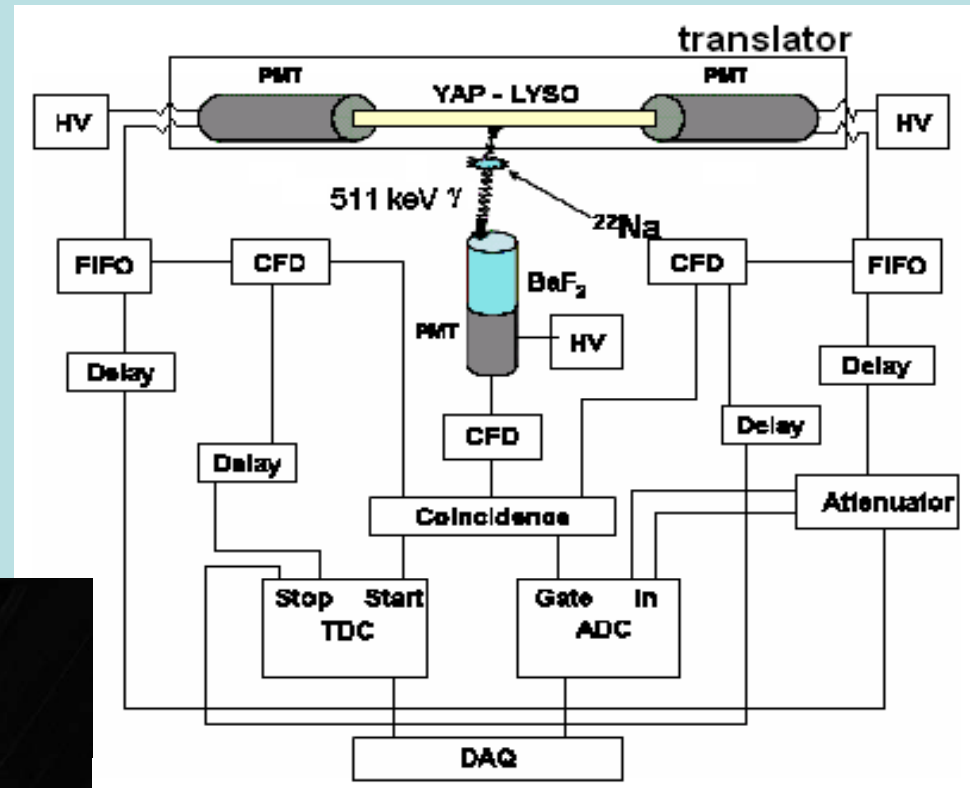
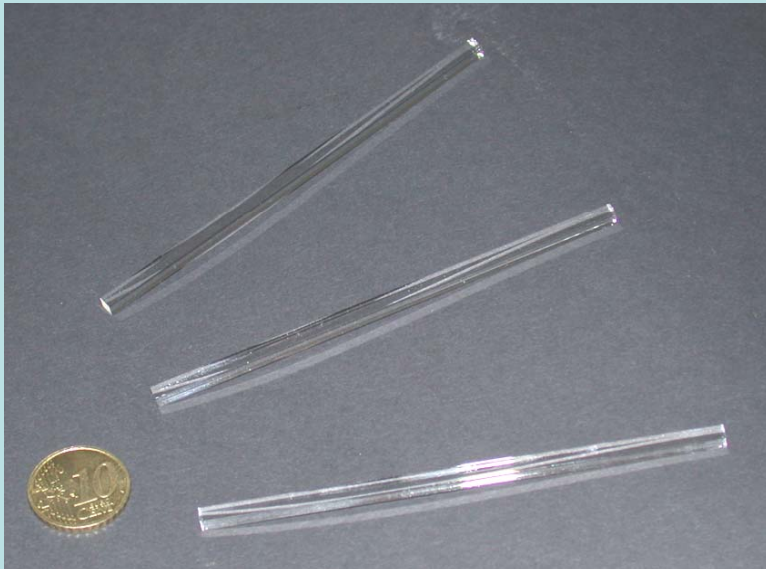
- Criteria to be taken into account: light yield, absorption length, photo fraction, self absorption, decay time, availability, machinability, price.

	YAP:Ce	LSO:Ce	LuAP:Ce	LaBr₃:Ce	BGO
Density ρ (g/cm ³)	5.55	7.4	8.34	5.3	7.13
Effective atomic charge Z	32	66	65	46.9	75
Scintillation light output (photons / MeV)	18000	23000	~10000	~61000	~9000
wavelength λ_{\max} of max. emission (nm)	370	420	370	356	480
Refractive index n at λ_{\max}	1.94	1.82	1.95	~1.88	~2.15
Bulk light abs. length λ_{bulk} (cm) at λ_{\max}	~20	~40			
Principal decay time (ns)	27	40	18	30+5	300
Mean γ atten. length λ_a at 511keV (mm)	22.4	11.5	10.5	~20	~11.6
Photo fraction at 511 keV (%)	4,5	32.5	30.5	15	41.5
Energy resolution (FWHM) at 663 keV	4.5	8		2.9	



LSO (LYSO) is the most interesting crystal scintillator :
fast (40 ns), short att. length (~12mm) at 511keV, high photofraction (32%),
not hygroscopic, but high energy resolution (8% FWHM)

PROOF of the HPD-PET CONCEPT with YAP and LYSO crystals and PMTs



- 1 BaF₂ (used with a ²²Na source)
- 2 Pb collimator Pb + source
- 3 YAP (Preciosa Co)
LYSO (Photonic Materials)
(3.2 x 3.2 x 100 mm³)
PMT H3164-10 (Φ=8mm, 1250 V)
- 4 linear translator M-511(Phys.Instrum.)

Lc, λ_{eff} , No: KEY PARAMETERS OF THE HPD-PET CONCEPT

HPD-PET

- **Lc**: crystal length
- λ_{eff} : attenuation length of scint. photons

$$1/\lambda_{\text{eff}} = 1/(\lambda_{\text{bulk}} * \cos \theta) + c'/(c_{\text{abs}})$$
- **No**: light yield, p.e.'s (511keV γ) in a Lc~0 crystal
 (n_{ph}/keV, sci.ph.transport, q.e. & wind. of photodet.)

$\sigma_z, \sigma_E/E, \sigma_t$: (only statistical)

$$N_1 = \frac{N_0}{2} \exp\left(\frac{-z}{\lambda_{\text{eff}}}\right), \quad N_2 = \frac{N_0}{2} \exp\left(\frac{-(L_c - z)}{\lambda_{\text{eff}}}\right), \quad N_{pe}(z) = N_1 + N_2.$$

$$z = \frac{1}{2} \left(\lambda_{\text{eff}} \ln \frac{N_1}{N_2} + L_c \right), \quad \sigma_z = \frac{\sqrt{ENF} \lambda_{\text{eff}}}{\sqrt{2N_0}} \left(\exp \frac{z}{\lambda_{\text{eff}}} + \exp \frac{L_c - z}{\lambda_{\text{eff}}} \right)^{1/2},$$

$$\frac{\sigma_E}{E} = \sqrt{\frac{ENF}{N_{pe}}} \oplus \text{Rint}, \quad \sigma_T = \frac{c}{\sqrt{N_{pe}}},$$

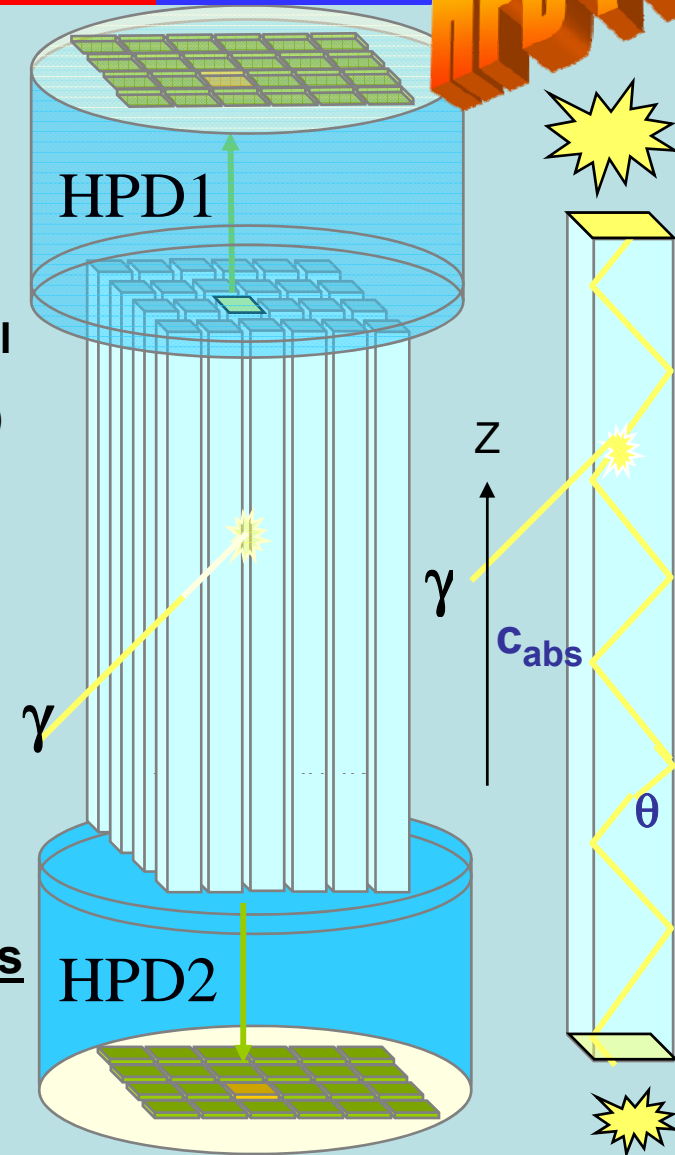
a) crystal axial length (Lc) worsens all resolutions

limit of Lc: 10 ~ 15 cm

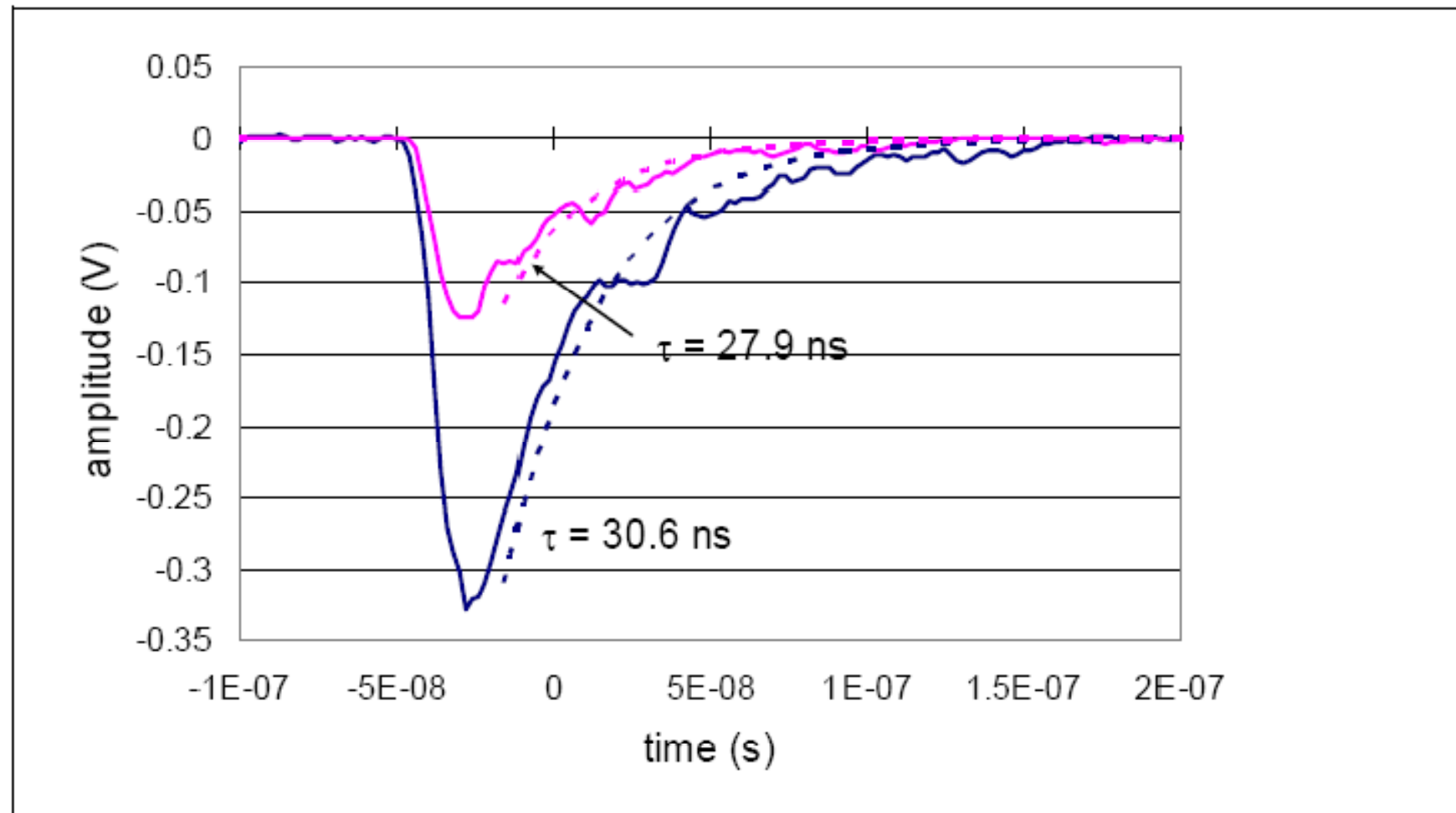
b) light yield (No) improves all resolutions

c) contrasting effects of λ_{eff} on σ_z & $\sigma_E/E, \sigma_t$

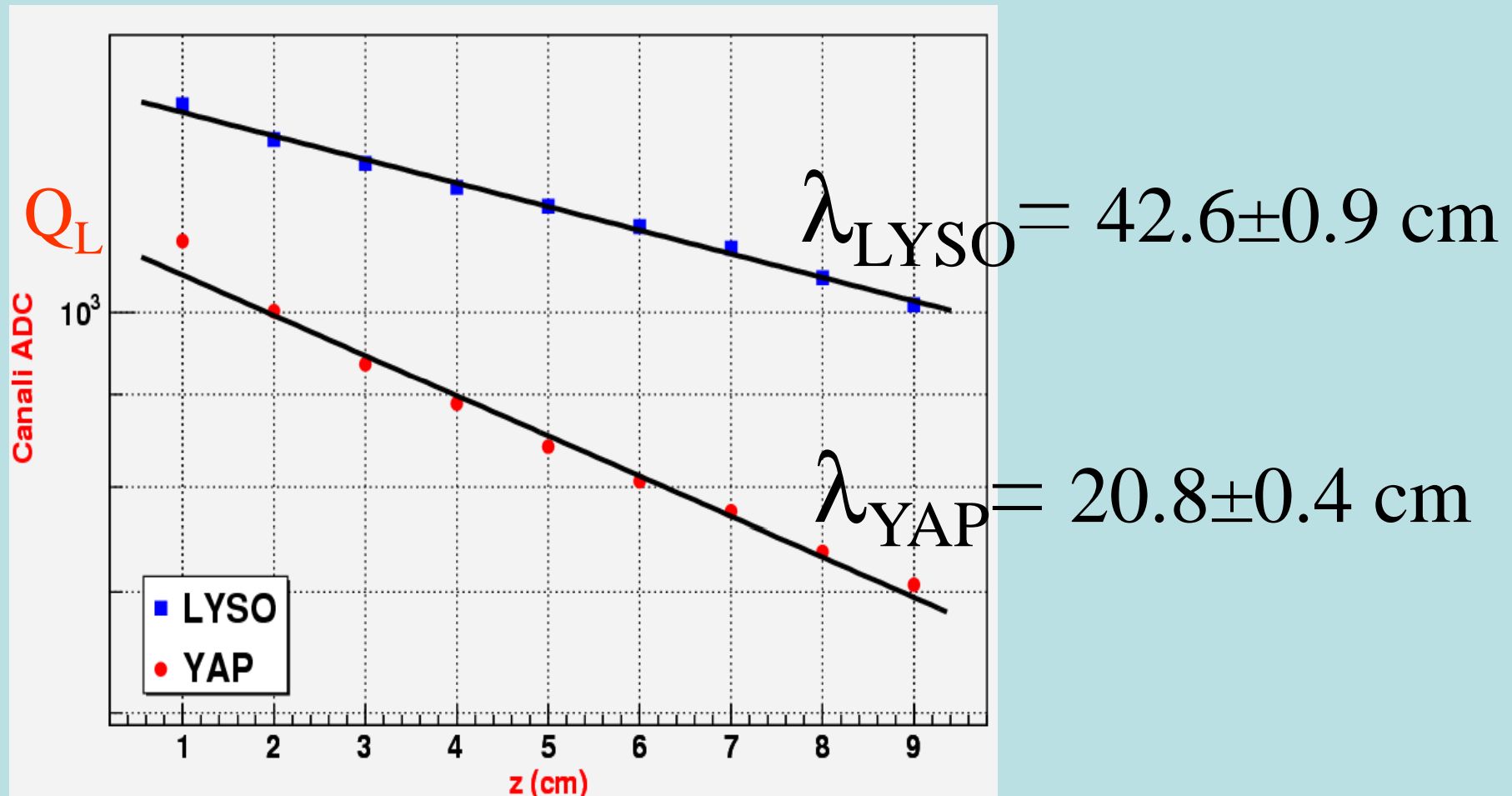
→ optimize λ_{eff} value by wrapping or coating the crystal lateral surface



Typical pulses from LYSO bars



λ_{eff} in polished 3x3x100 mm³ YAP-LYSO

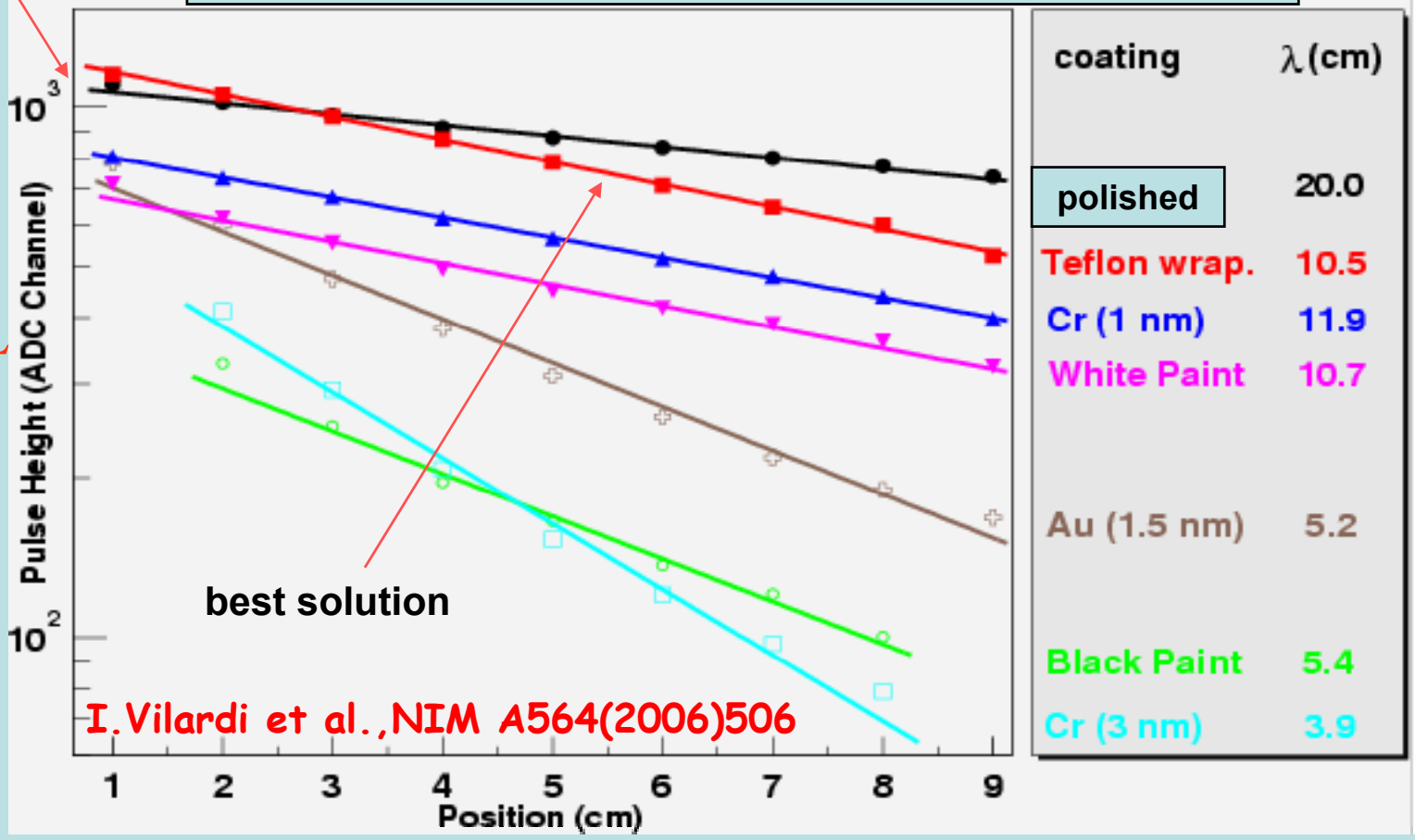


- LYSO more transparent (higher λ_{eff}) than YAP
- too high λ -eff values (poor σ_z) both for LYSO and YAP

Crystal wrappings or metal-coatings
change light attenuation length of a YAP ($3.2 \times 3.2 \times 100 \text{ mm}^3$)

No/2

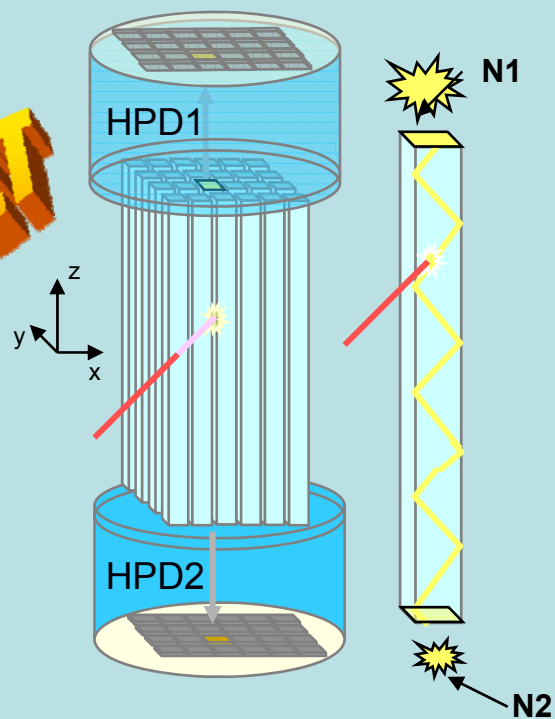
Q_L



I. Vilardi et al., NIM A564(2006)506

- at $z=0$ $Q(\text{teflon}) > Q(\text{polished})$: slight increase of No
- $\lambda(\text{polished}) / \lambda(\text{teflon}) = 1.9$
- possibility to tune λ -eff value with metal coatings
- metal coating reduces No

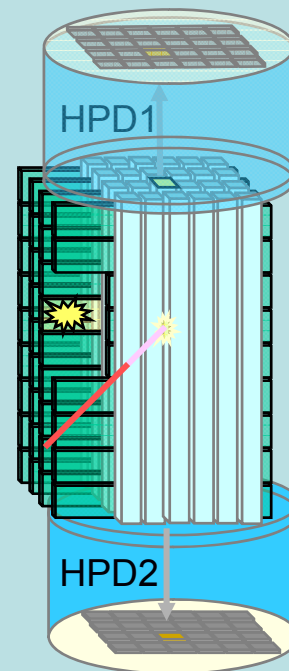
HPD-PET



HPD-PET concept

crystal	$\lambda_{\text{eff}}(\text{cm})$	$\sigma_z(\text{mm})$	σ_E/E (%)
YAP polish	21	10	4
YAP coated	8	4	6
LYSO polish	42	18	7
LYSO coated	8	5	10

WLS-HPD-PET



New WLS-HPD-PET concept

(proposed by D.Schinzal)

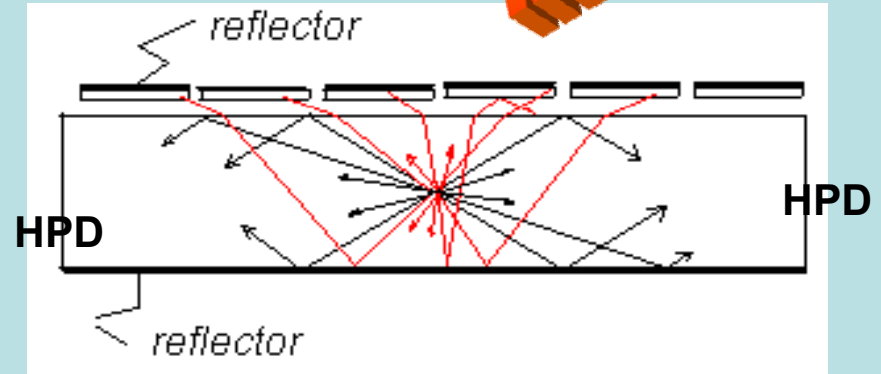
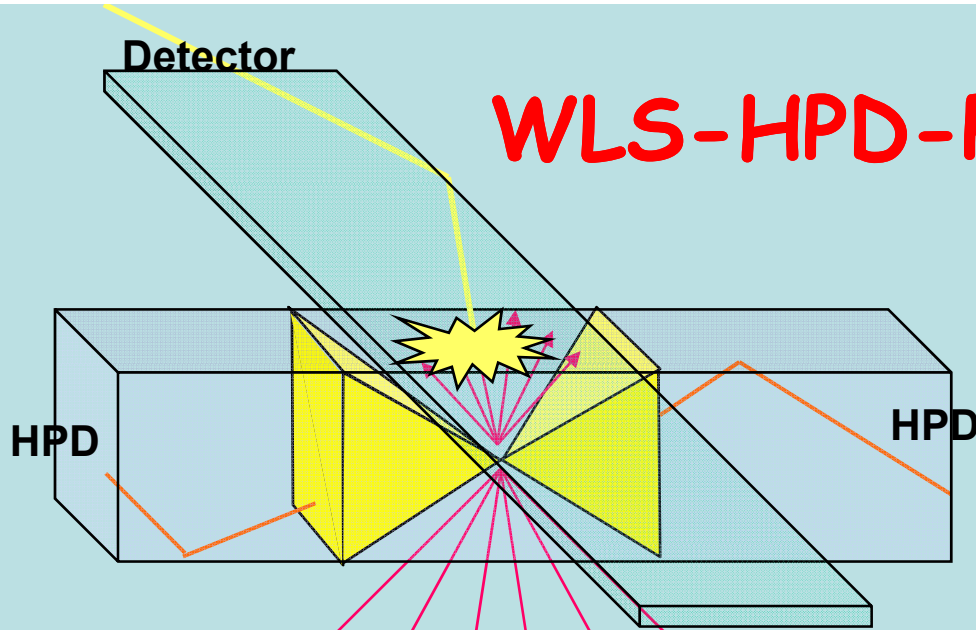
WLS strip width $w = 3 \text{ mm}$, $\sigma_z \leq w/\sqrt{12} = 0.9 \text{ mm}$

$\lambda_{\text{eff}}(\text{cm})$	$\sigma_z(\text{mm})$	σ_E/E (%)
21	1	4
42	1	7

A. Braem et al., NIM A580(2007)1513

WLS-HPD-PET concept

WLS-HPD-PET



$$N_{pe} = Y \cdot \frac{d\Omega}{4\pi} \cdot \frac{1}{4} \cdot \epsilon_{fluor} \cdot \epsilon_{trans} \cdot \epsilon_{det}$$

$$Y = 32000 / \text{MeV} \quad (\text{LYSO})$$

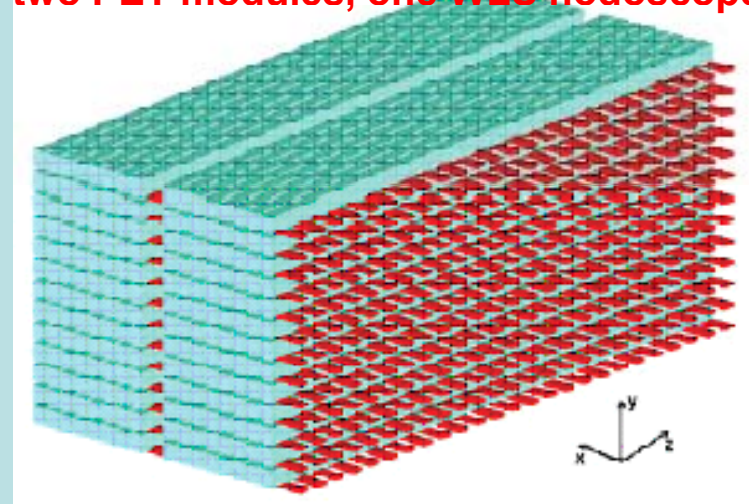
$$\epsilon_{fluor} = 0.8$$

$$\epsilon_{trans} = 0.5$$

$$\epsilon_{det} = 0.15 \quad (@ 490 \text{ nm})$$

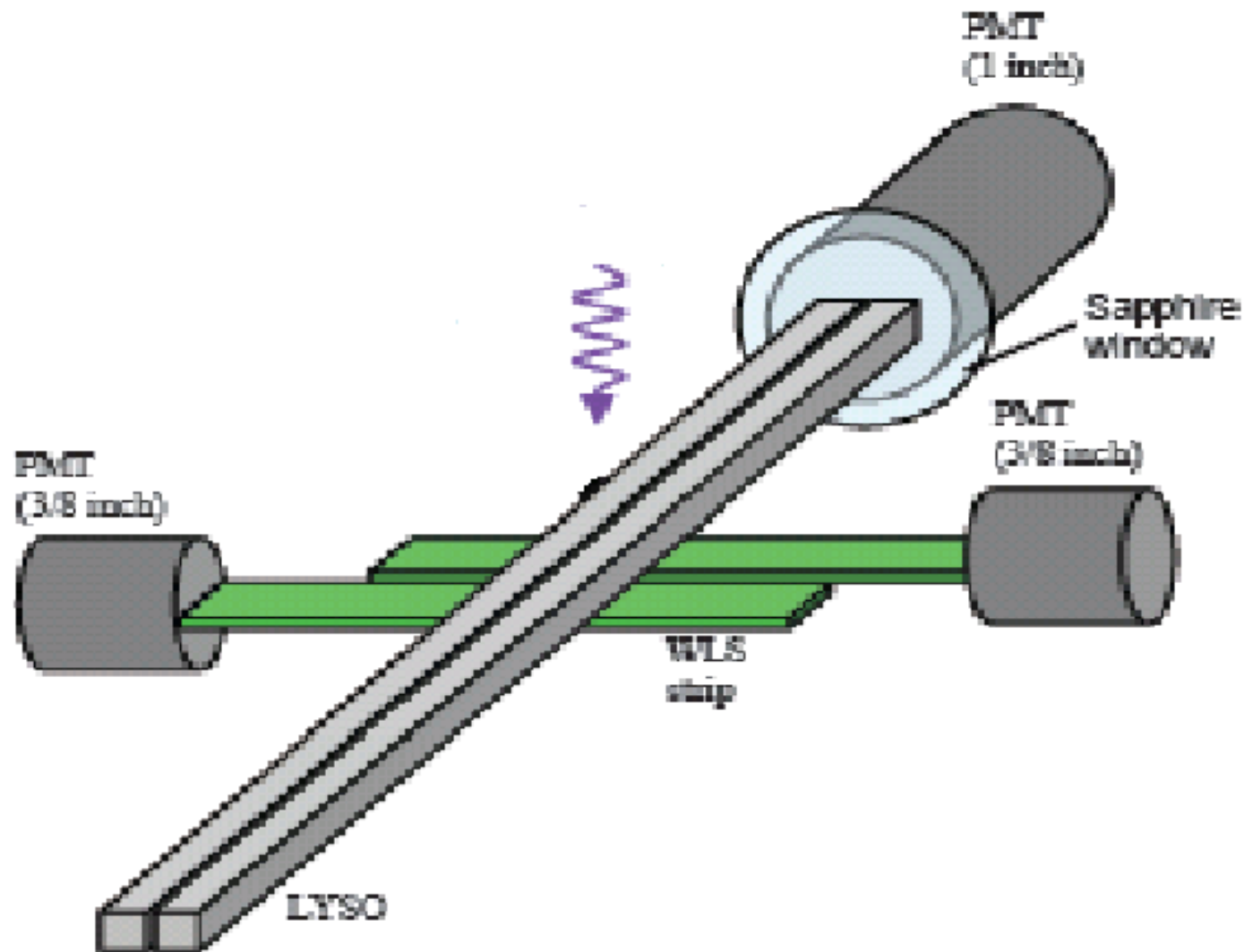
$$N_{pe} = 46 \quad (@ 511 \text{ keV}) \quad \rightarrow \quad \boxed{\epsilon_{\gamma} \approx 1}$$

two PET modules, one WLS hodoscope

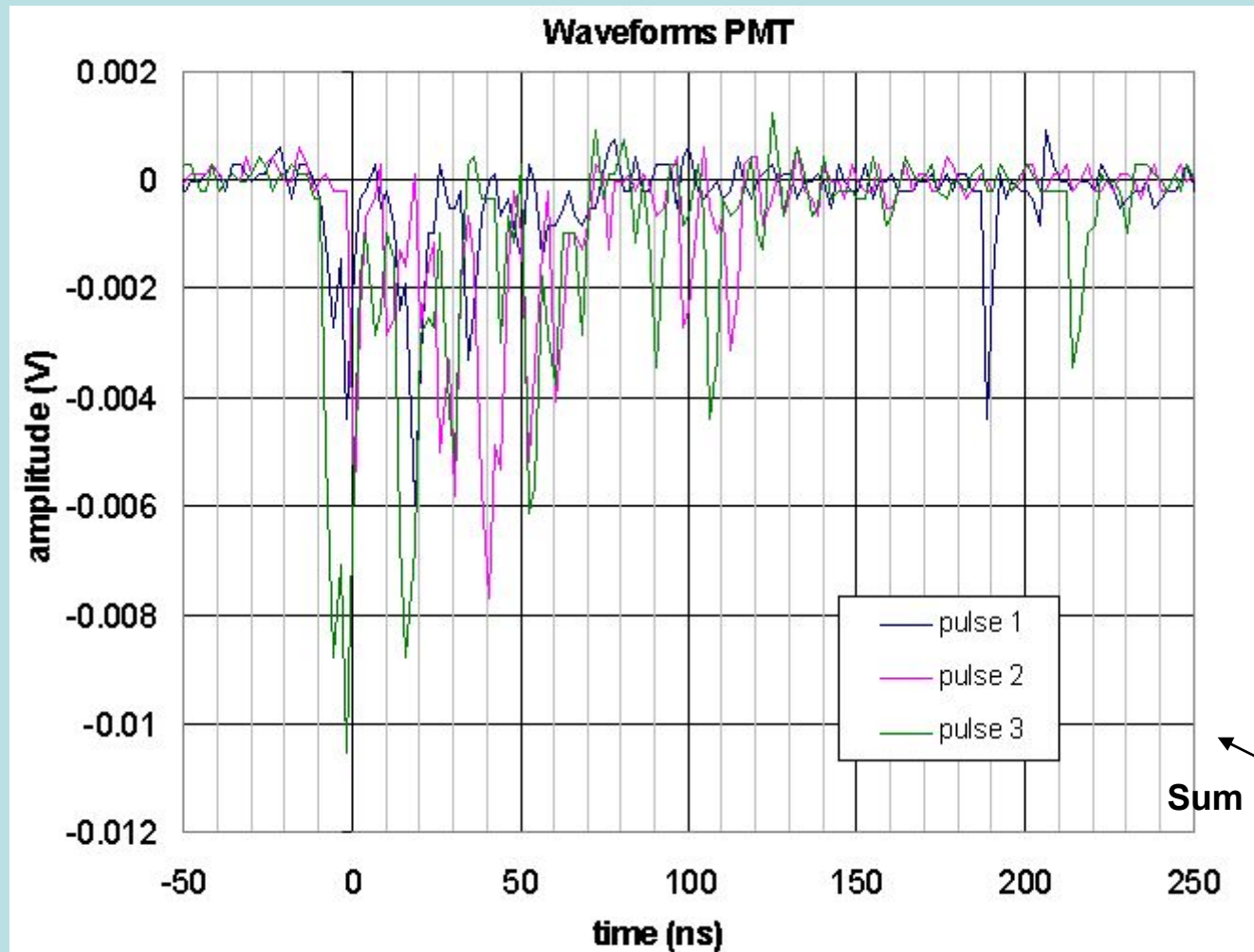


SETUP for WLS-HPD-PET Test

LYSO + 2WLS readout by PMTs



Typical pulses from WLS strips bars

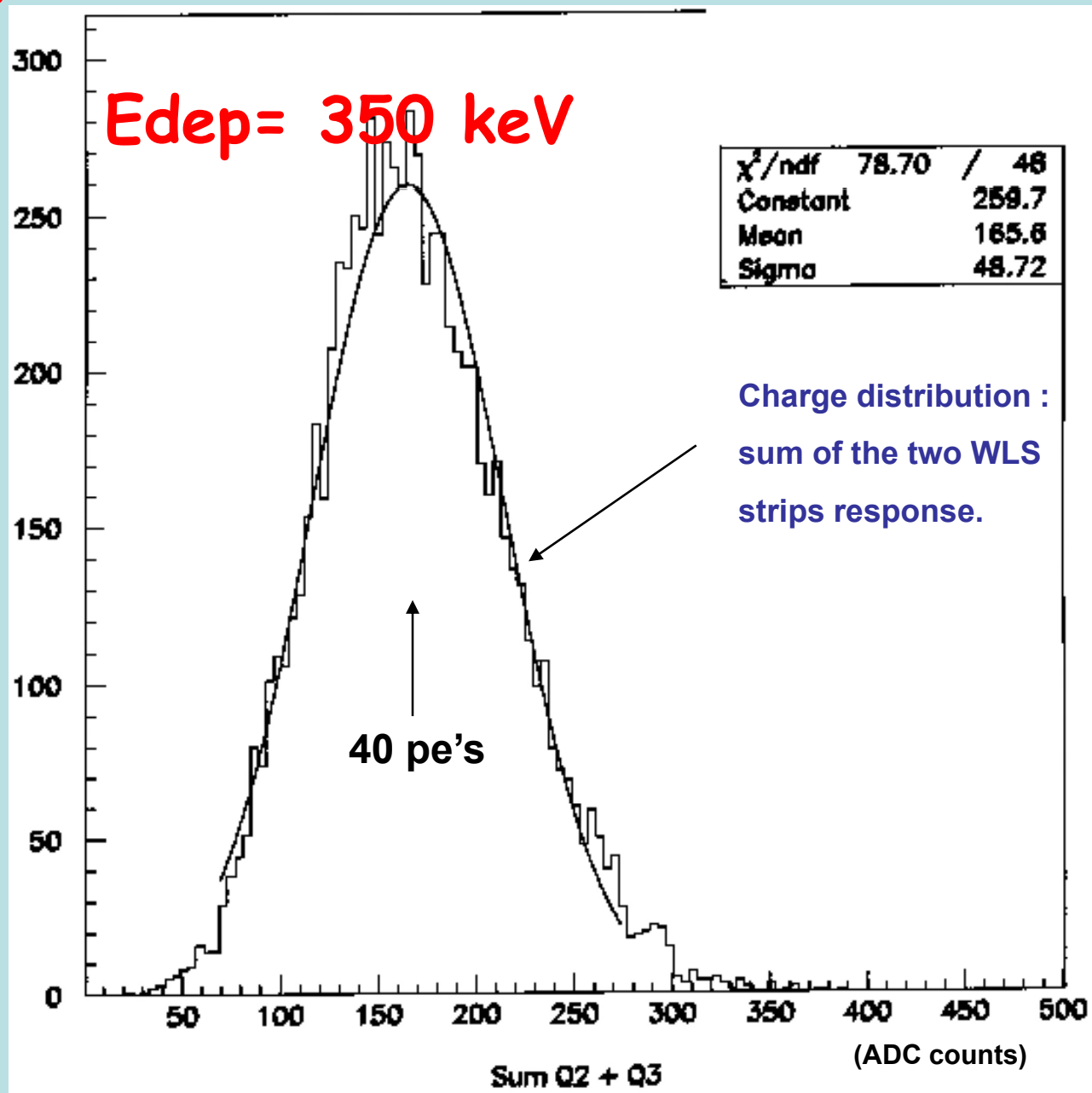


$$\tau_{\text{WLS}} = 10 \text{ ns}$$

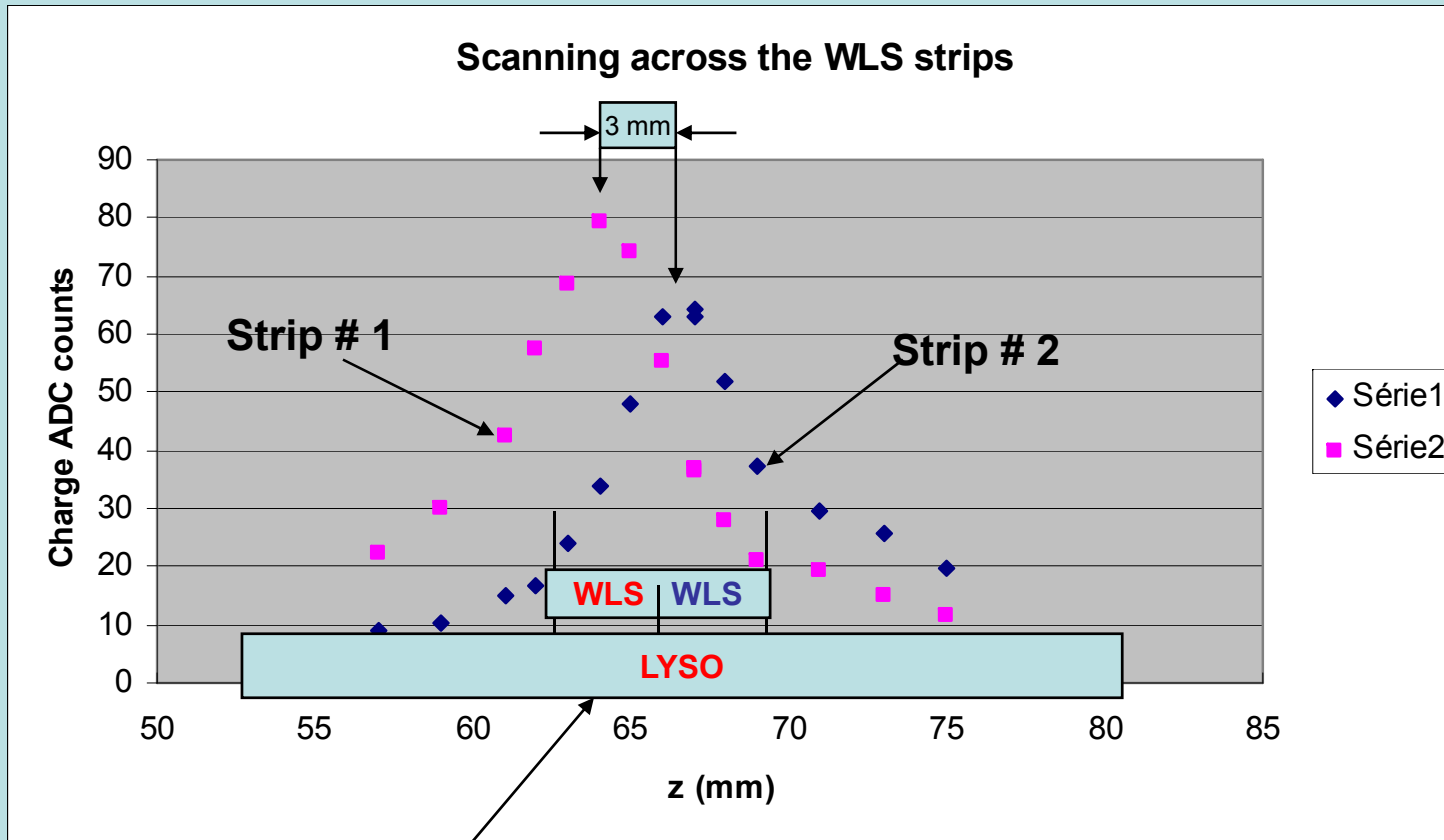
$$\tau_{\text{LYSO}} = 30 \text{ ns}$$

Sum of channels 1 and 2

charge distribution of the sum of two WLS



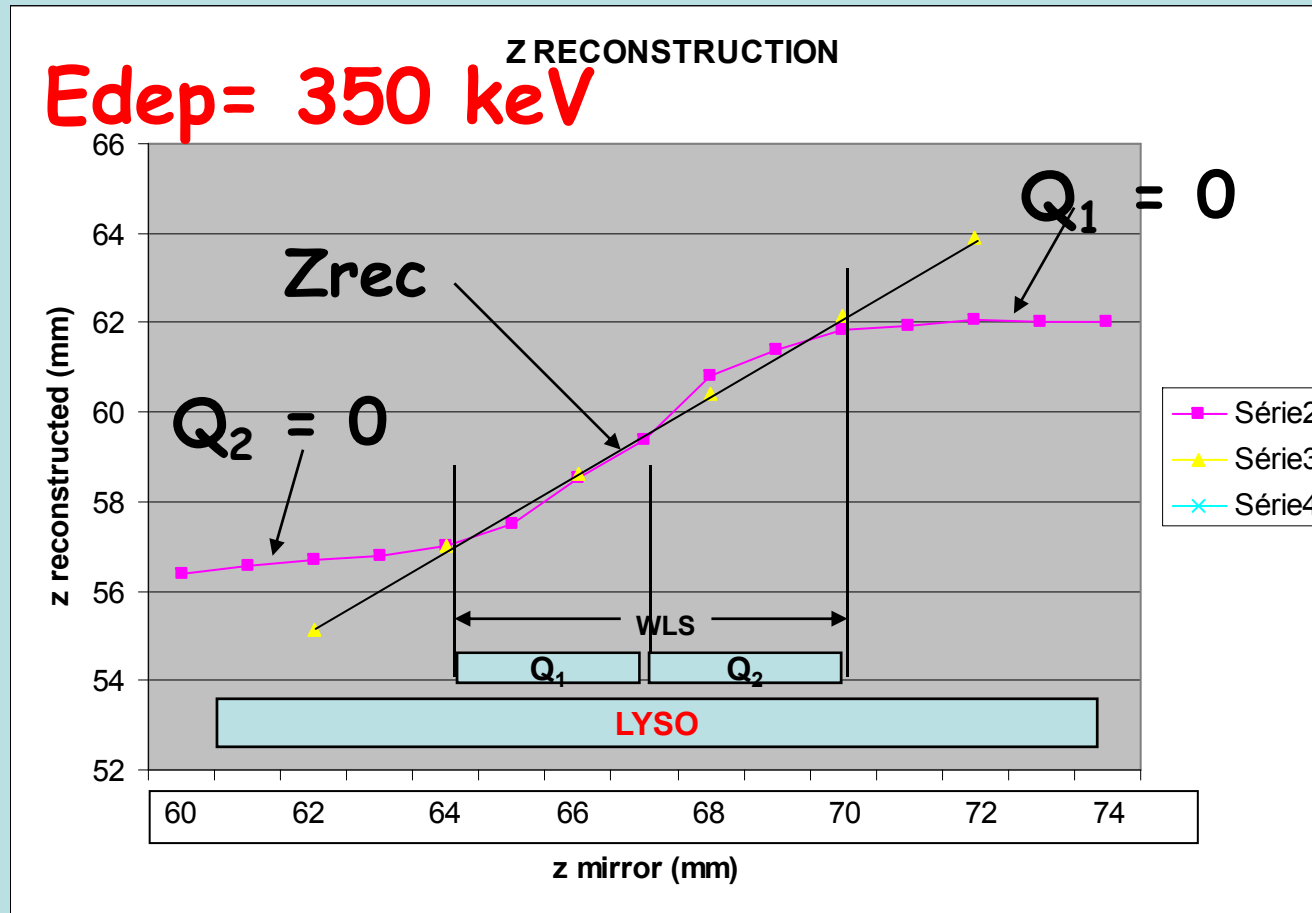
charges on 2 LYSO bars



at $z = 64$ mm (centre of strip #1)

65% of charge on strip #1, 35% on strip#2

Scintillation position (DoI) reconstruction

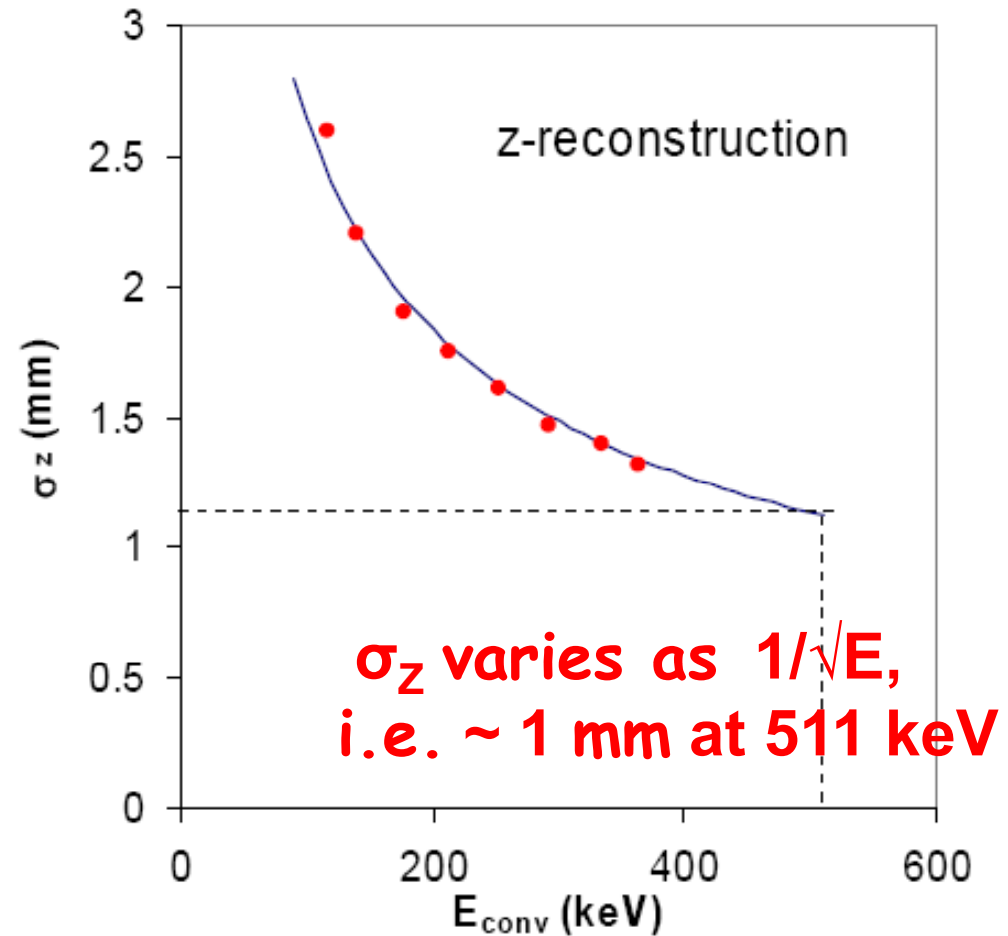
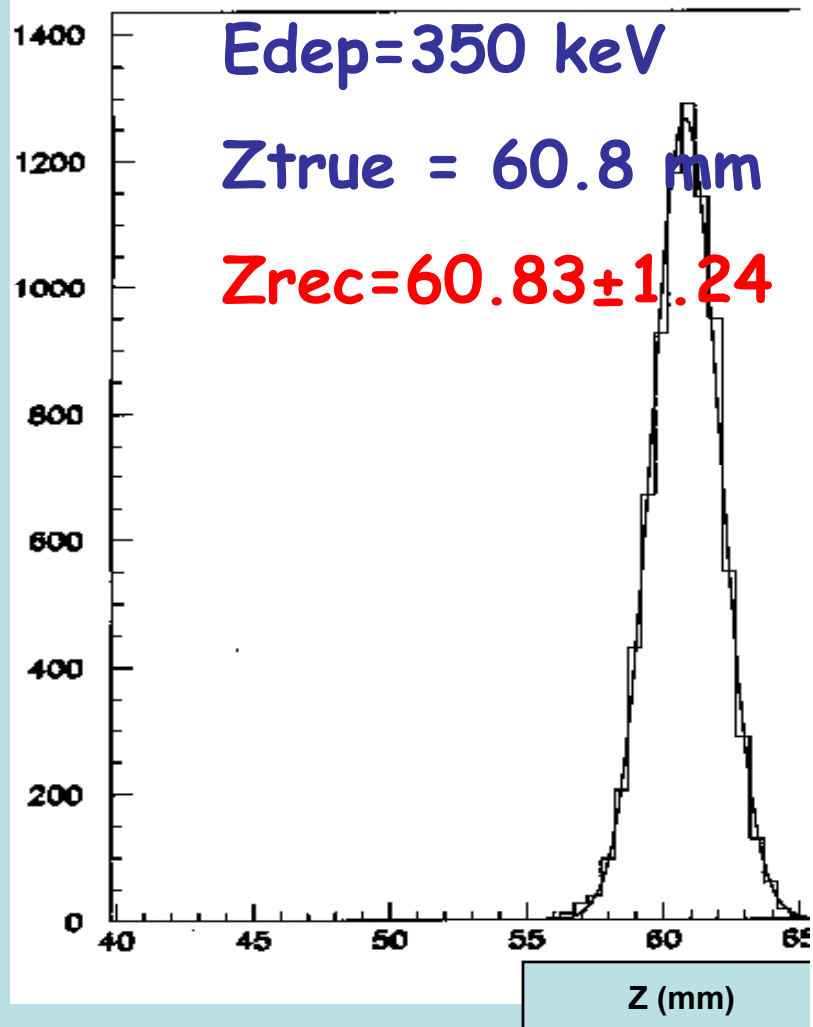


$$Z_{rec} = c + m (Q_2 - Q_1) / (Q_2 + Q_1)$$

$m = 0.9$ (# 1) is due to a different det. eff. of the two WLS strips.

$c = \text{constant}$

Zrec distribution from two WLS charges



From our publication in Il Nuovo Cimento Vol. 29 C,N. 4

FWHM values

Comparison of reconstruction resolution (FWHM values): HRRT data vs. HPD-PET simulation. In the simulations a crystal length of 150 mm was assumed. All values correspond to the central plane ($z=0$).

	Transaxial resolution $R_x (= R_y)$ (mm)		Axial resolution R_z (mm)		Mean volumetric resolution $R_V = R_x \times R_y \times R_z$ (mm ³)
	x=0; y=0	x=100; y=0	x=0; y=0	x=100; y=0	
HRRT data, span 9	2.35	2.75	2.5	3.6	20
IIRRT data, span 3	2.35	2.75	2.5	2.8	18
HPD-PET LSO	1.85	2.35	5.78	6.33	26
HPD-PET LaBr ₃	1.59	2.13	3.43	3.57	11.8

WLS-HPD-PET LYSO ~ 2.2 ~ 2.2

2.1

~ 9 mm³



This is ~ physical limit
due to positron range and
gamma acolinearity