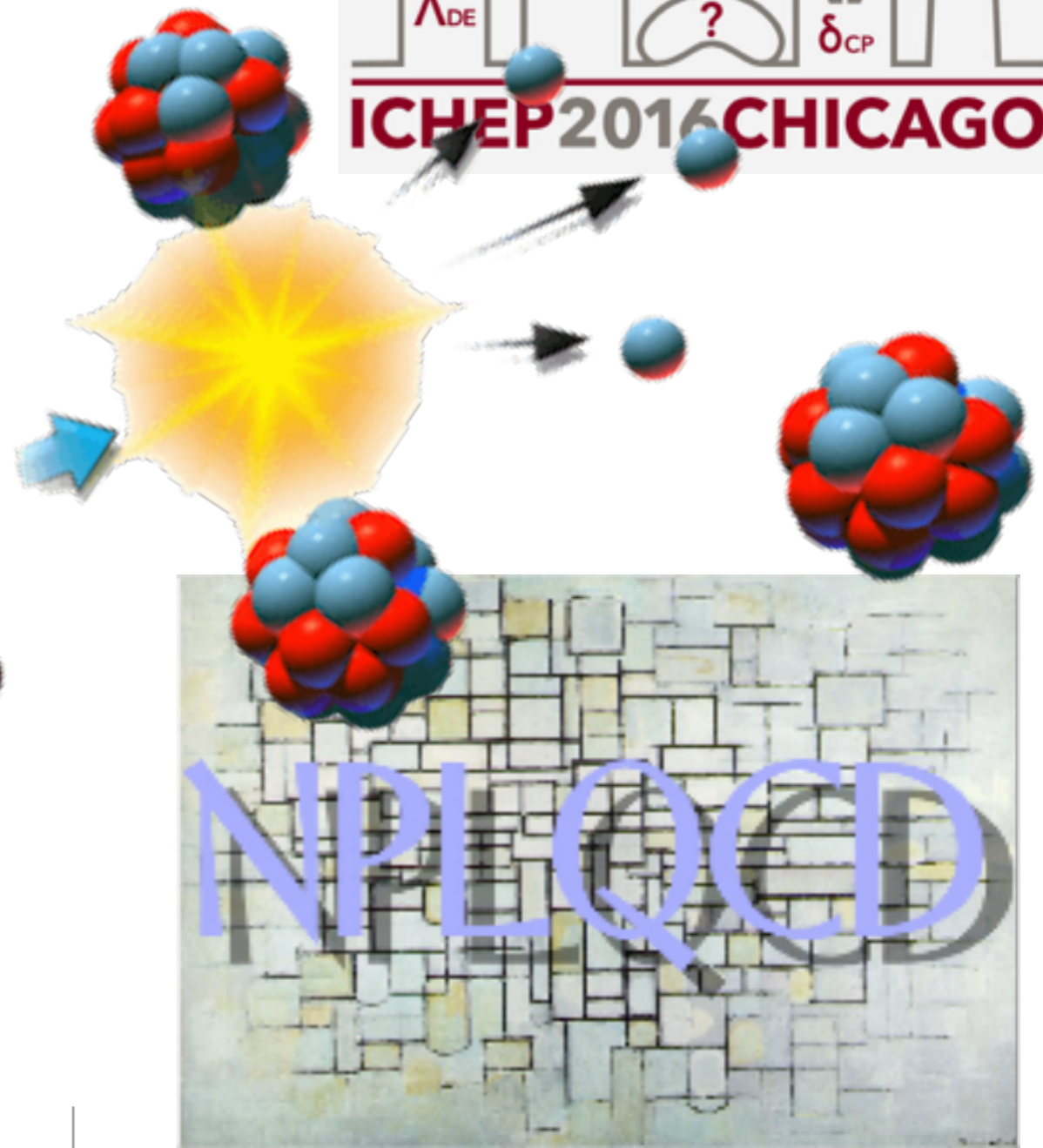
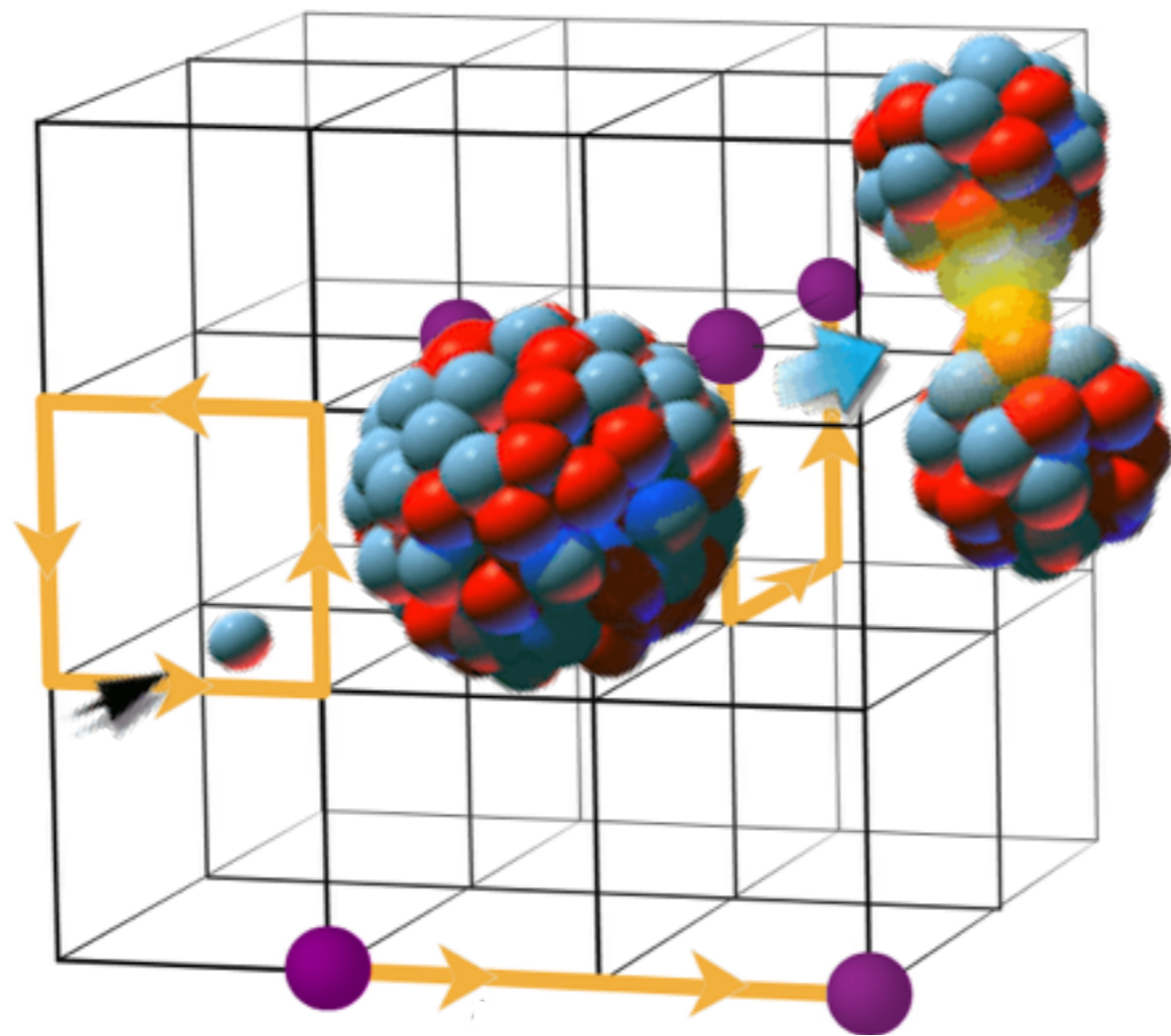


# Axial Current Matrix Elements in Light Nuclei from Lattice QCD



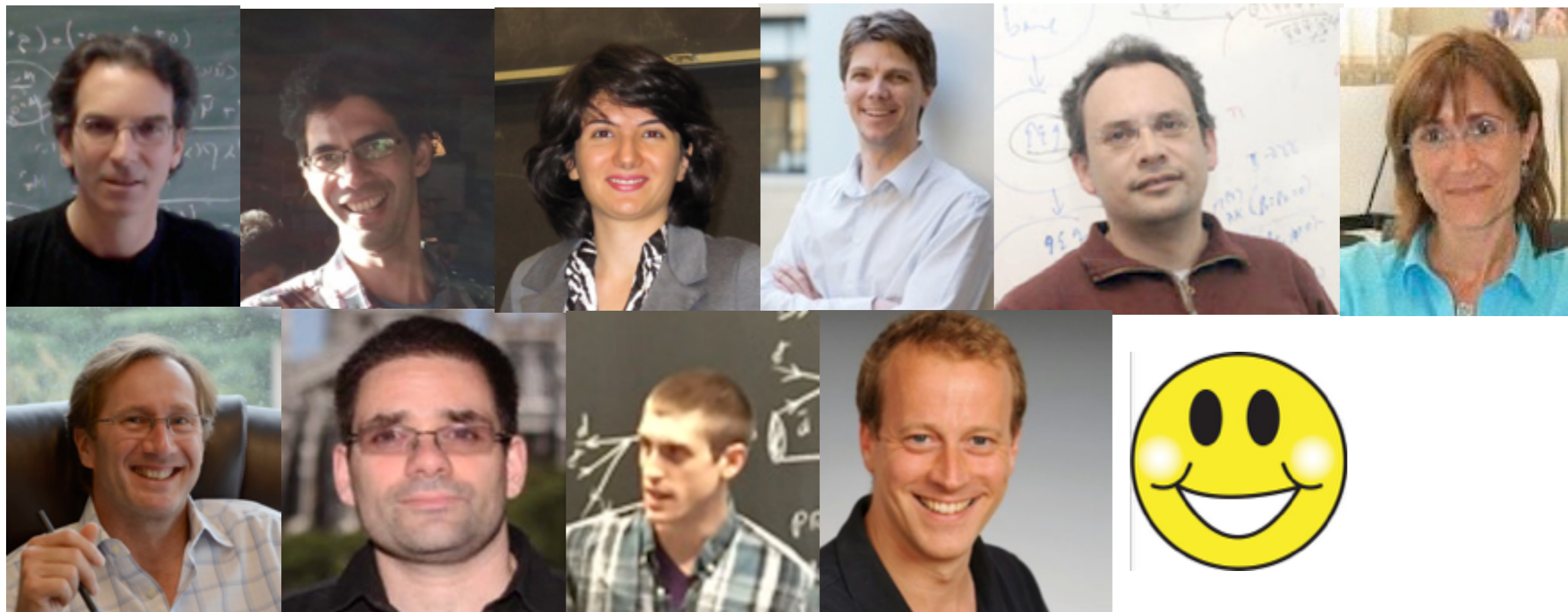
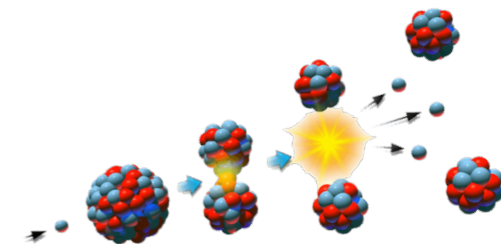
Martin J Savage

on behalf of the NPLQCD Collaboration



INSTITUTE for  
NUCLEAR THEORY



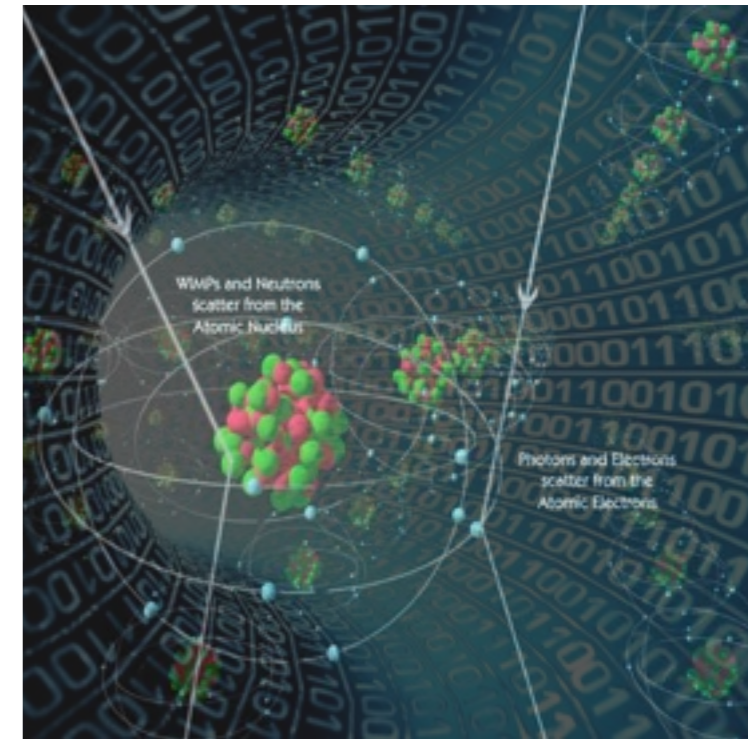
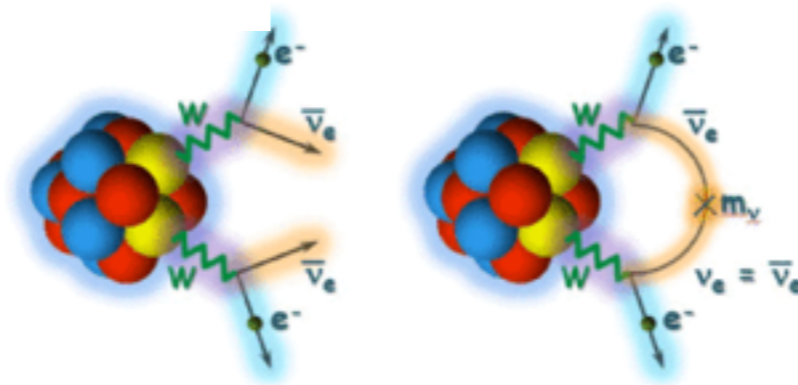
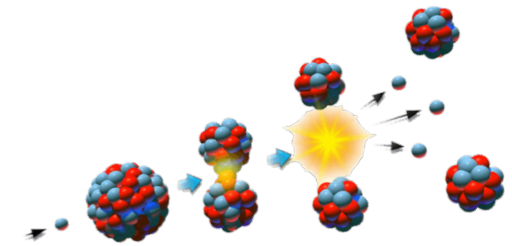


Silas Beane (UW)  
Zohreh Davoudi (MIT)  
Kostas Orginos (WM/JLab)  
Martin Savage (INT)  
Frank Winter (JLab)  
Jonas Wilhelm (Geissen)

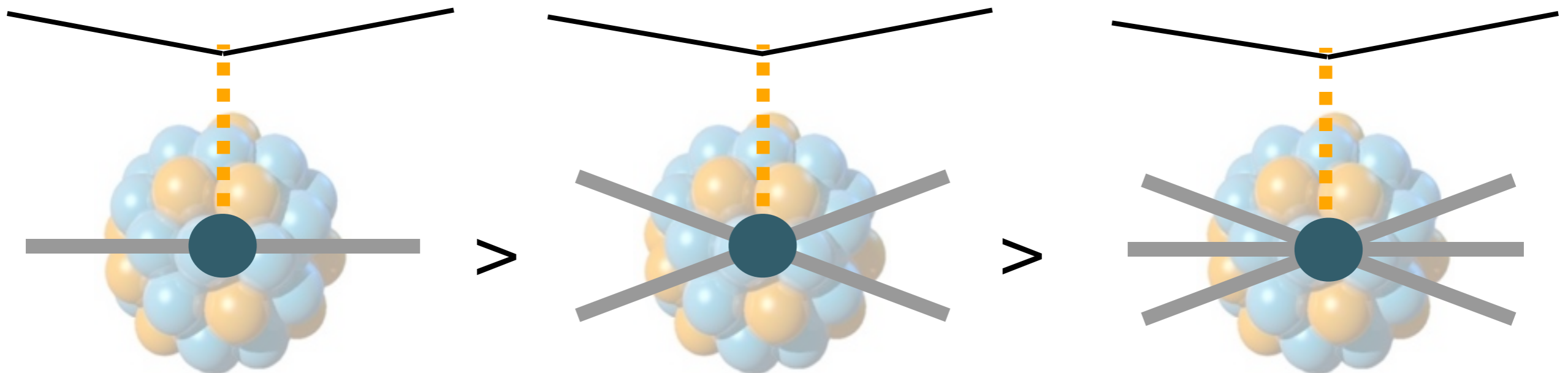
Emmanuel Chang (INT)  
William Detmold (MIT)  
Assumpta Parreno (Barcelona)  
Brian Tiburzi (CCNY/BNL)  
Michael Wagman (UW)

**Past Collaborators**  
Saul Cohen  
Pari Junnarkar  
Huey-Wen Lin  
Aaron Torok  
Tom Luu  
Andre Walker-Loud

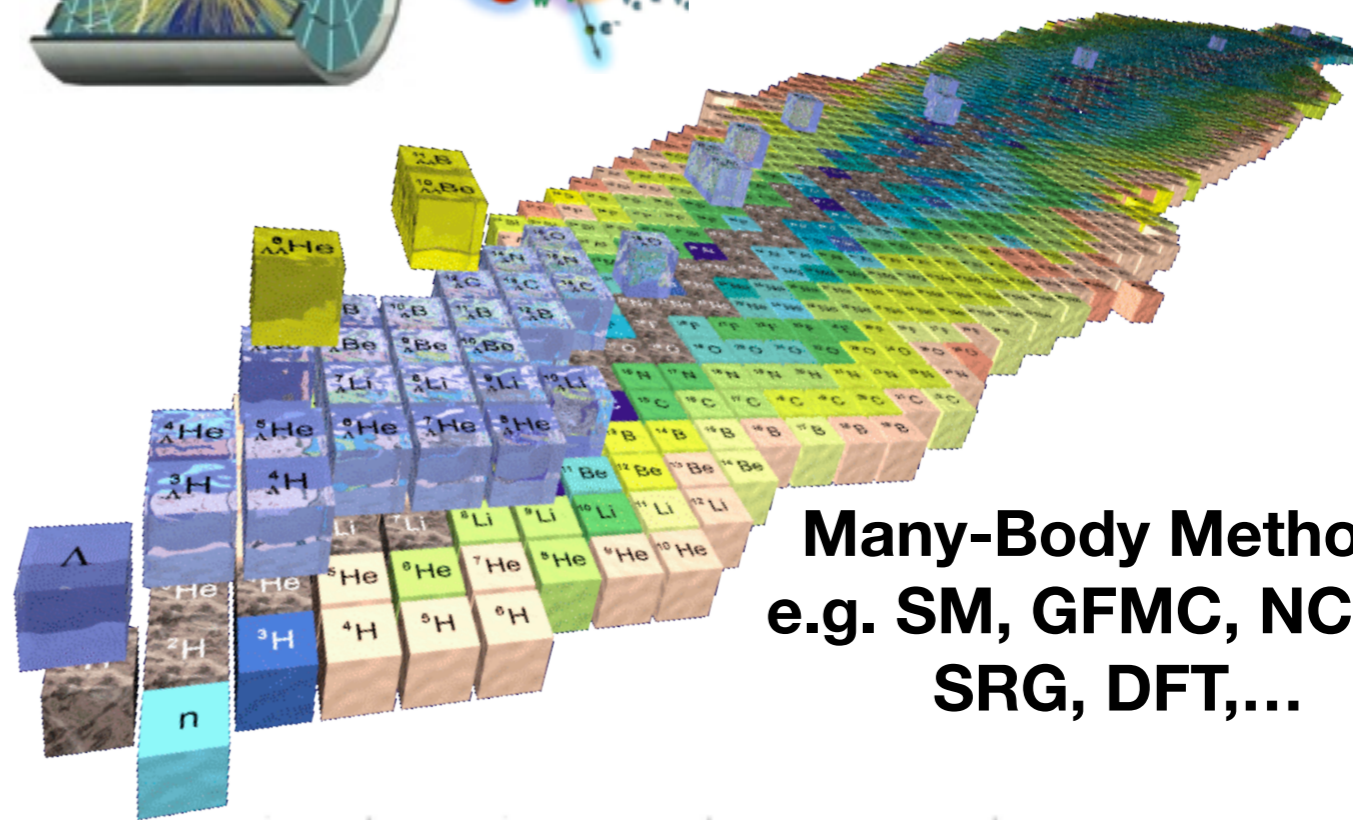
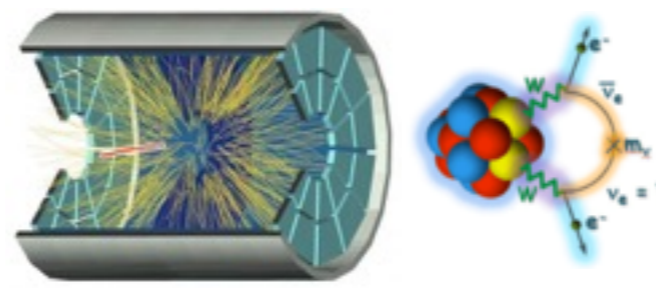
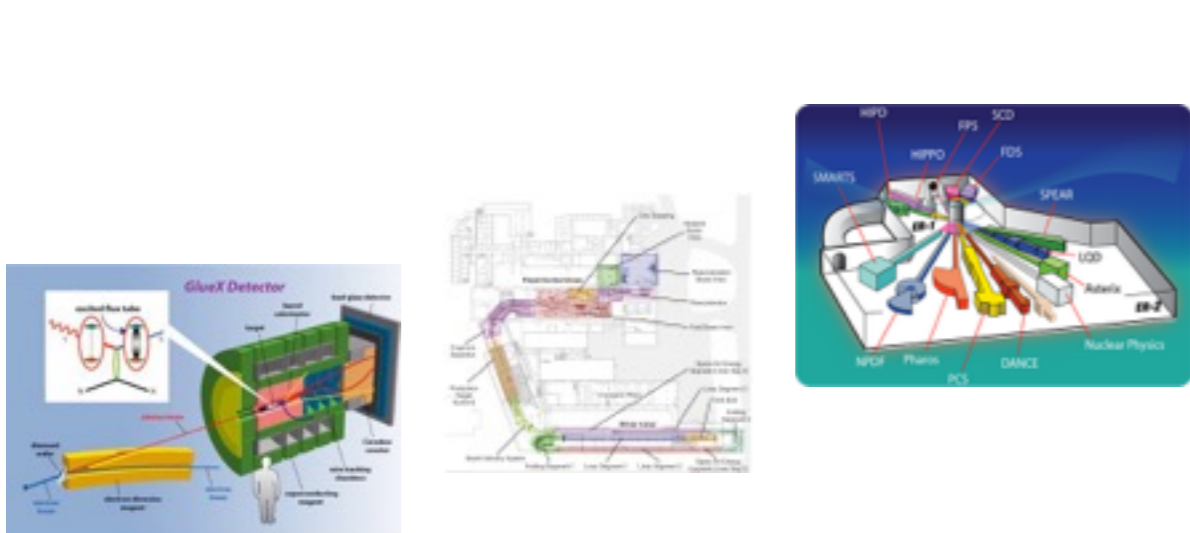
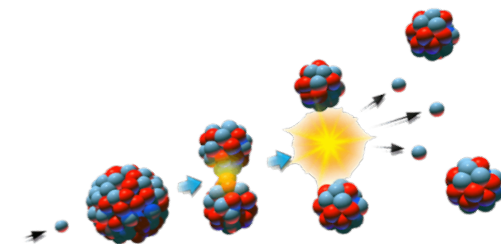
# Nuclear Matrix Elements



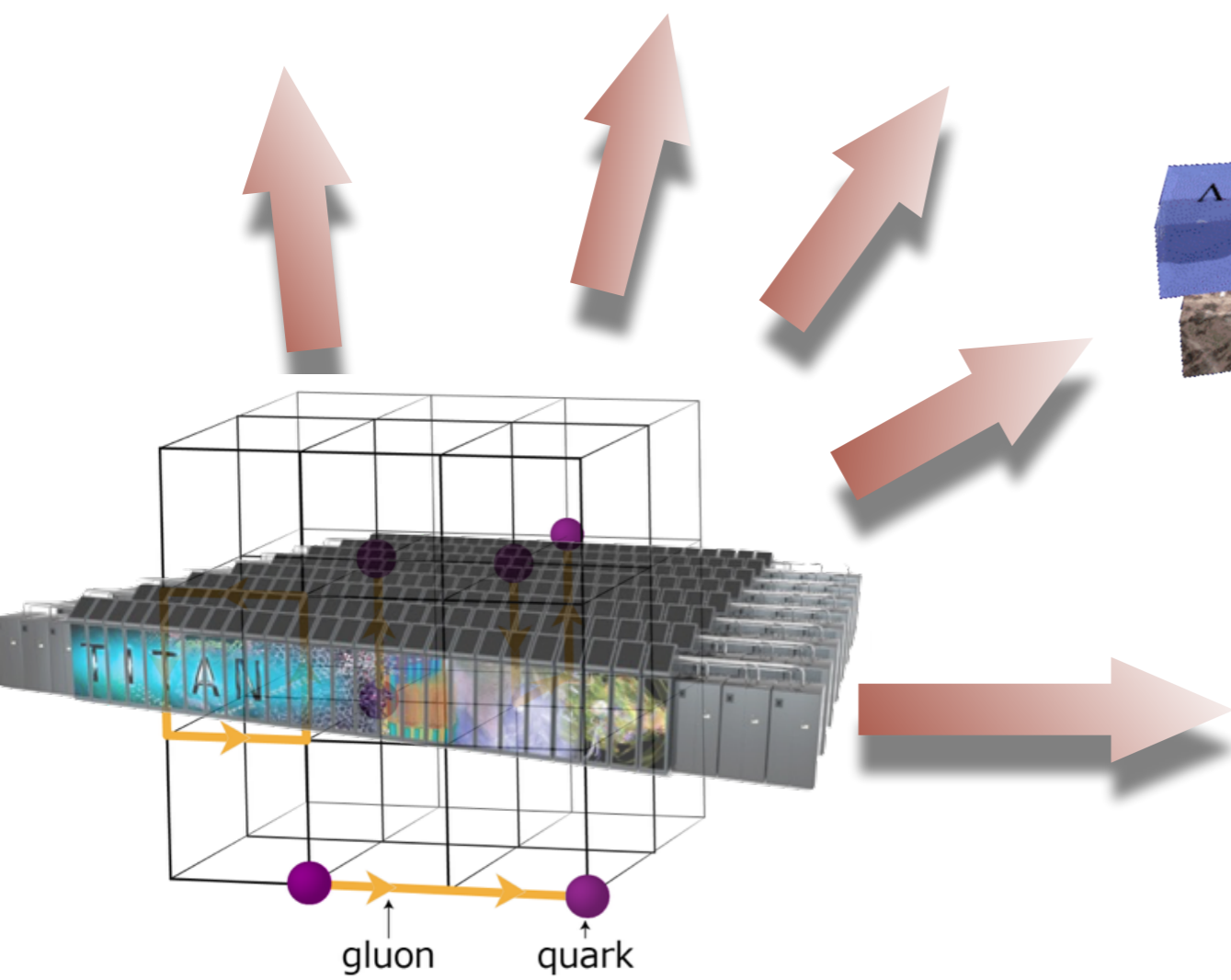
$\nu$ ,  $e$ ,  $\mu$ ,  $X$  - JLab,  $\nu$ -experiments, DUNE, DM, edm, ...



# Low-Energy Nuclear Physics

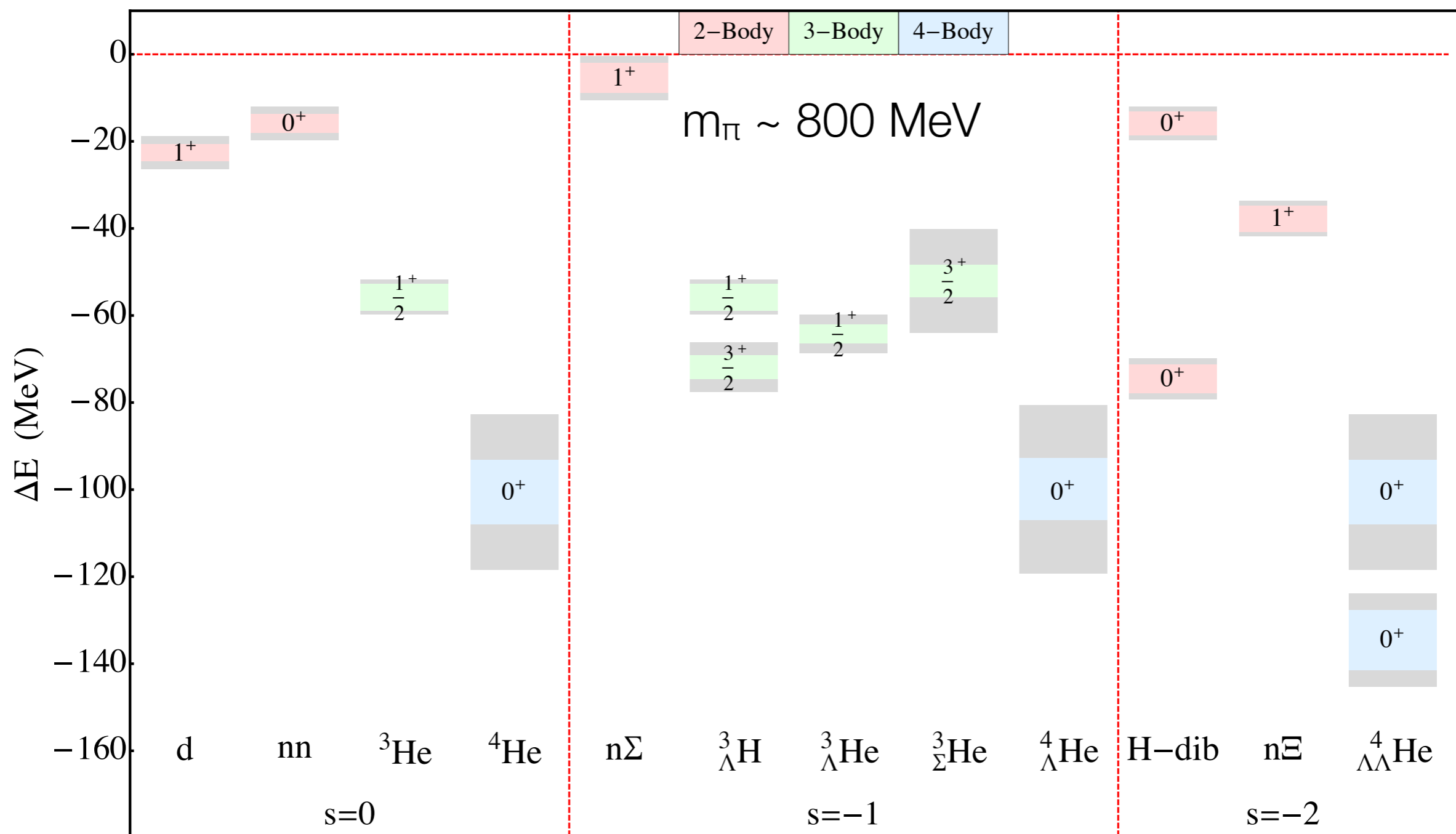
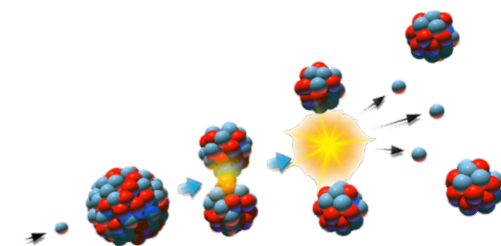


**Many-Body Methods**  
 e.g. SM, GFMC, NCSM,  
 SRG, DFT,...

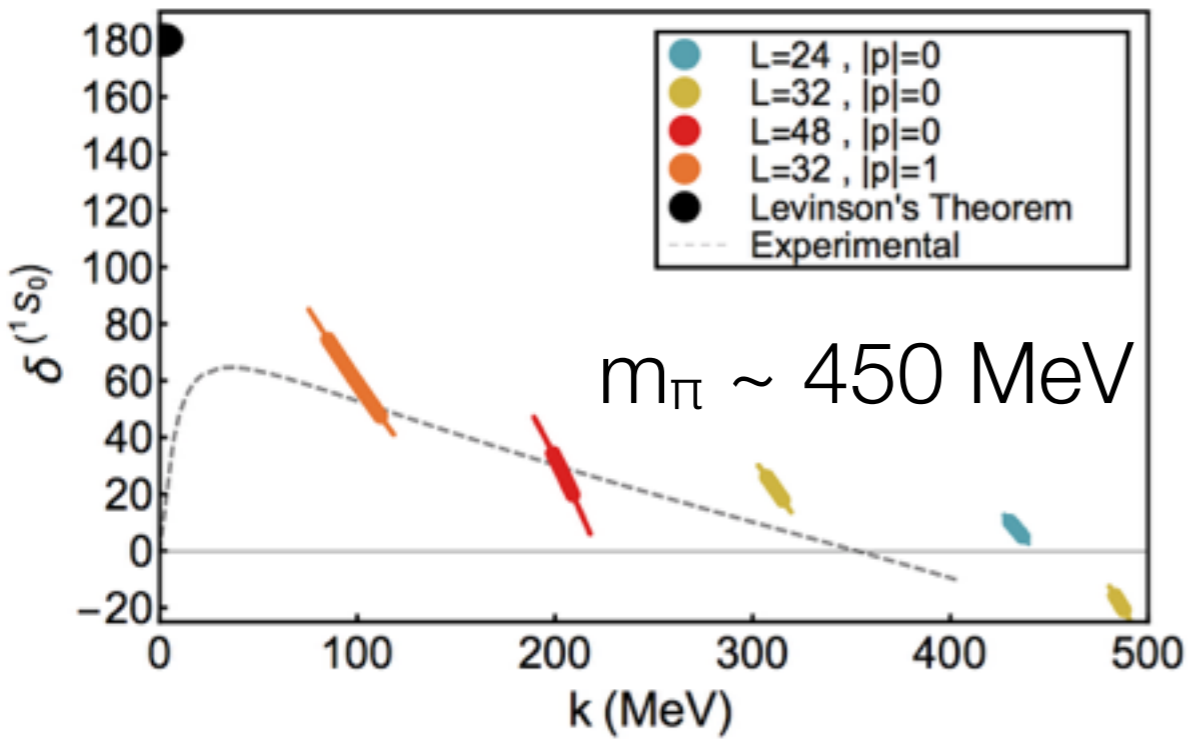
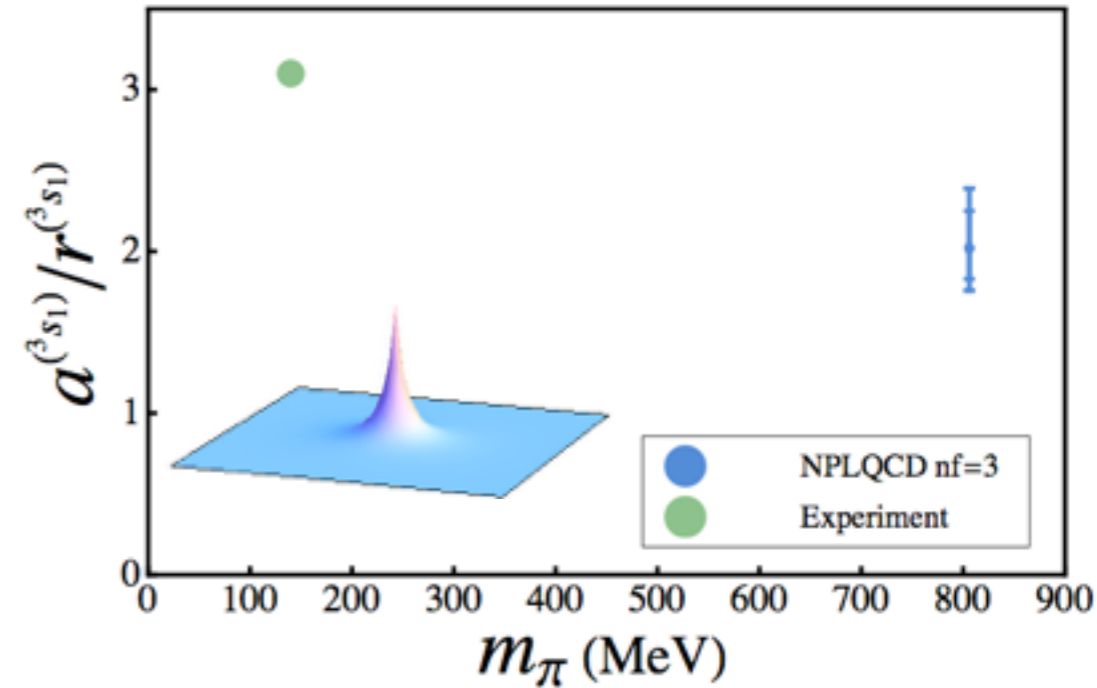
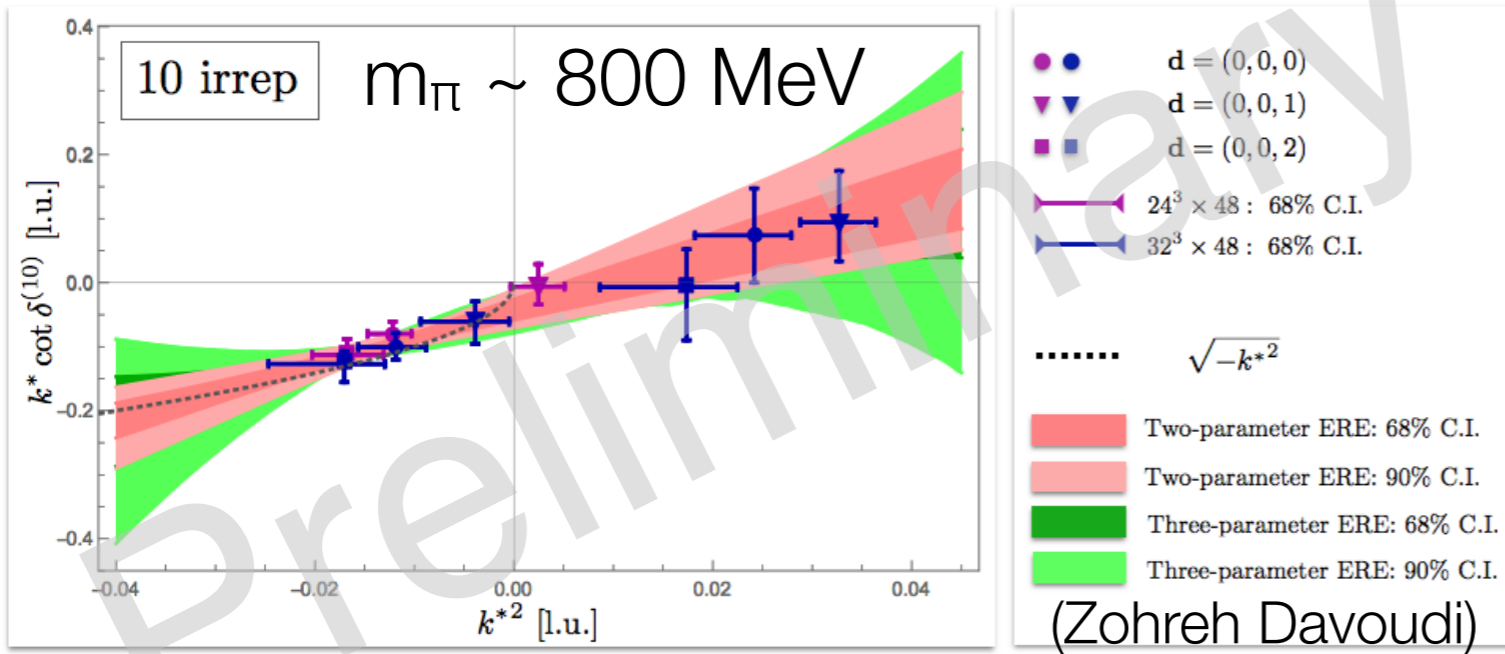
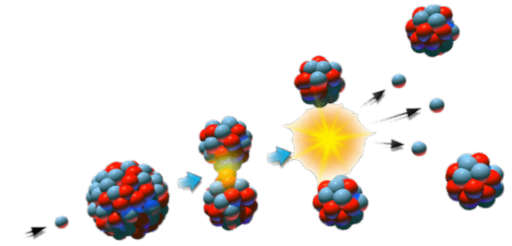


	2N force	3N force	4N force
LO		—	—
NLO		—	—
N <sup>2</sup> LO			—

# Nuclei from QCD

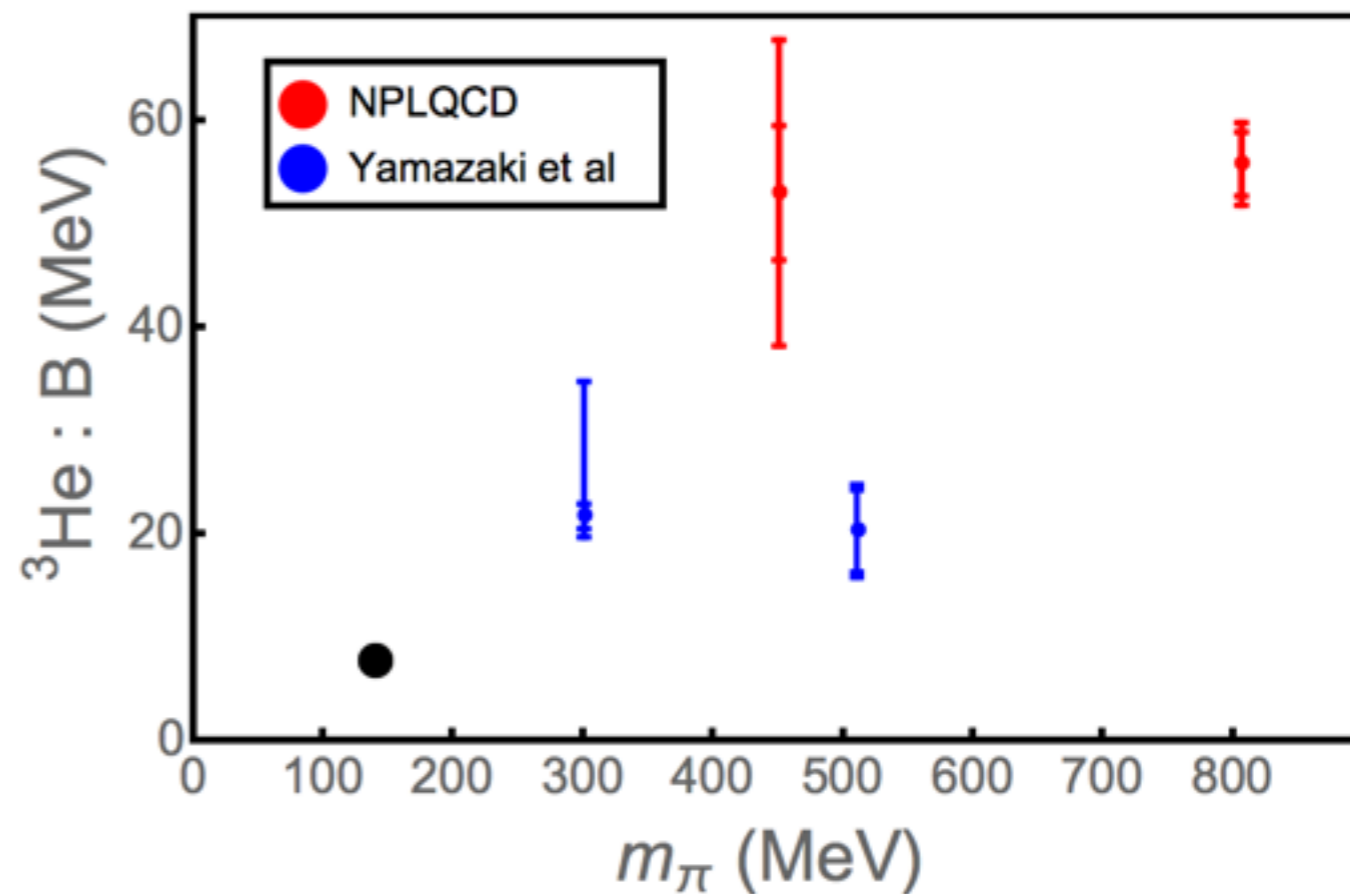
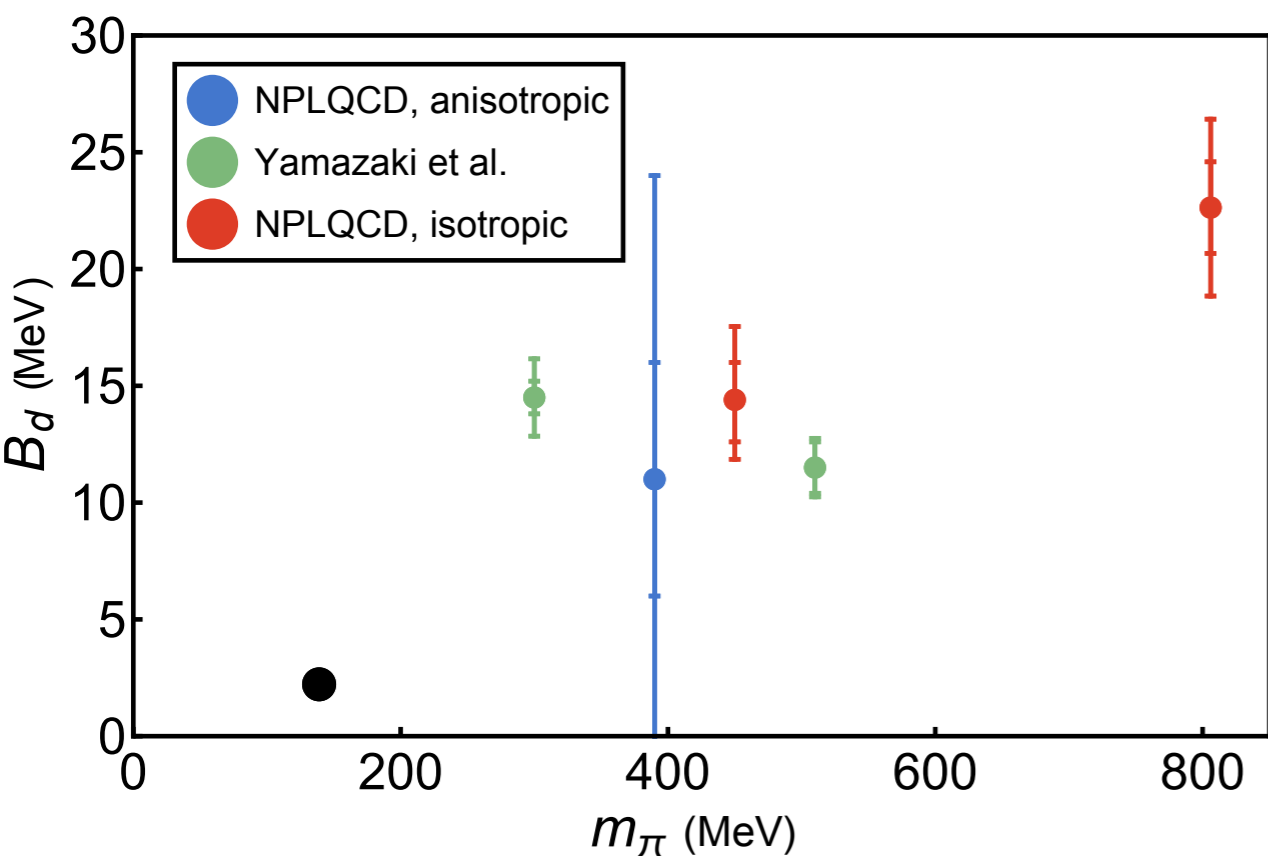
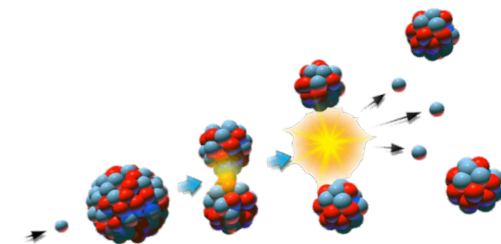


# NN Interactions NPLQCD

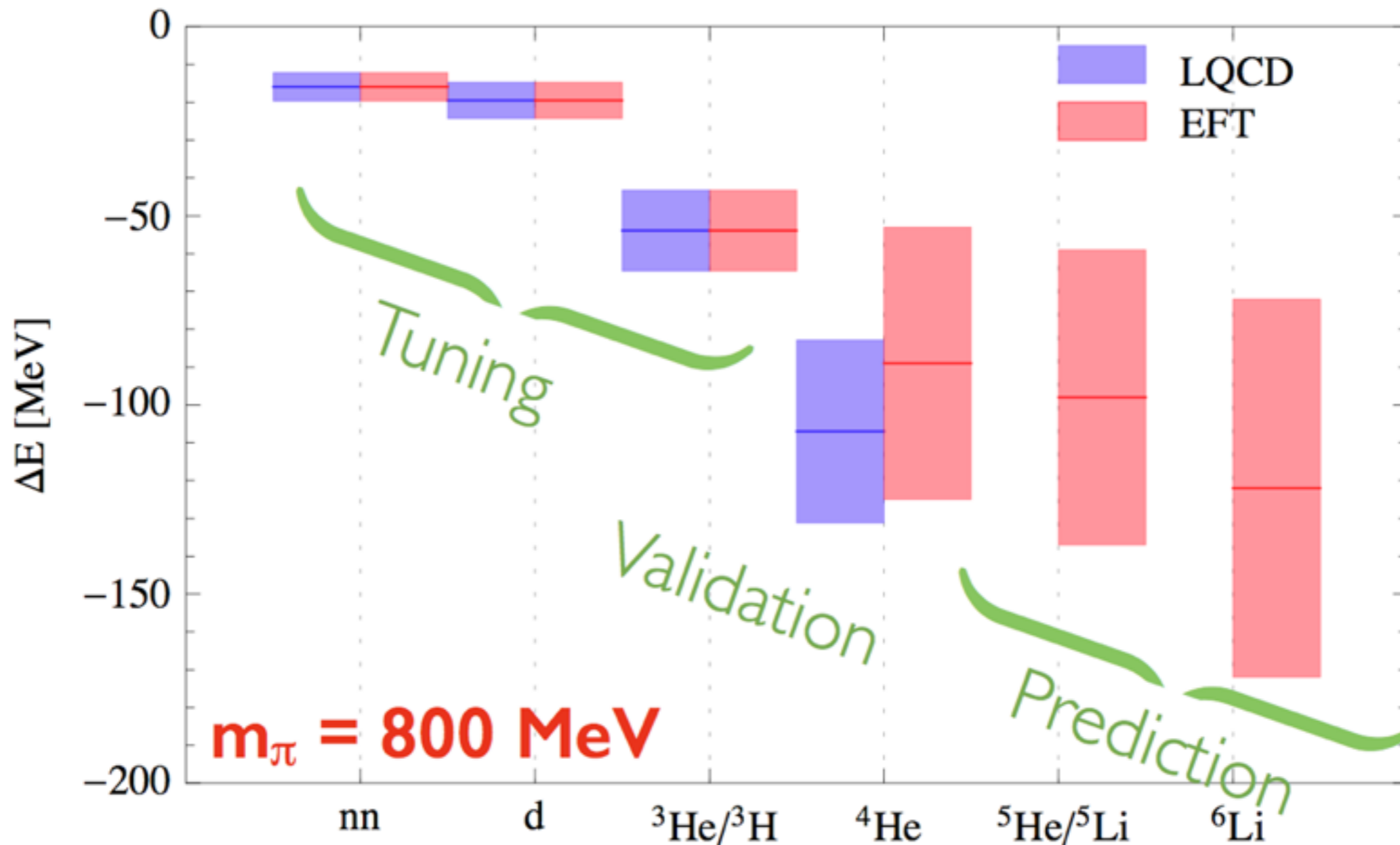
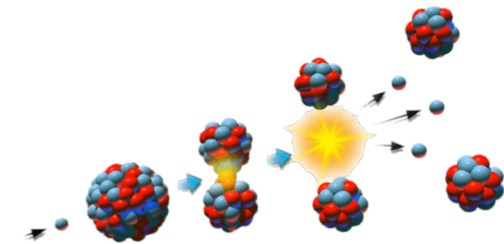


Deuteron appears to be unnatural but not finely-tuned ??  
Generic feature of YM with  $n_f=3$

# Light Nuclei : Quark Mass Effects

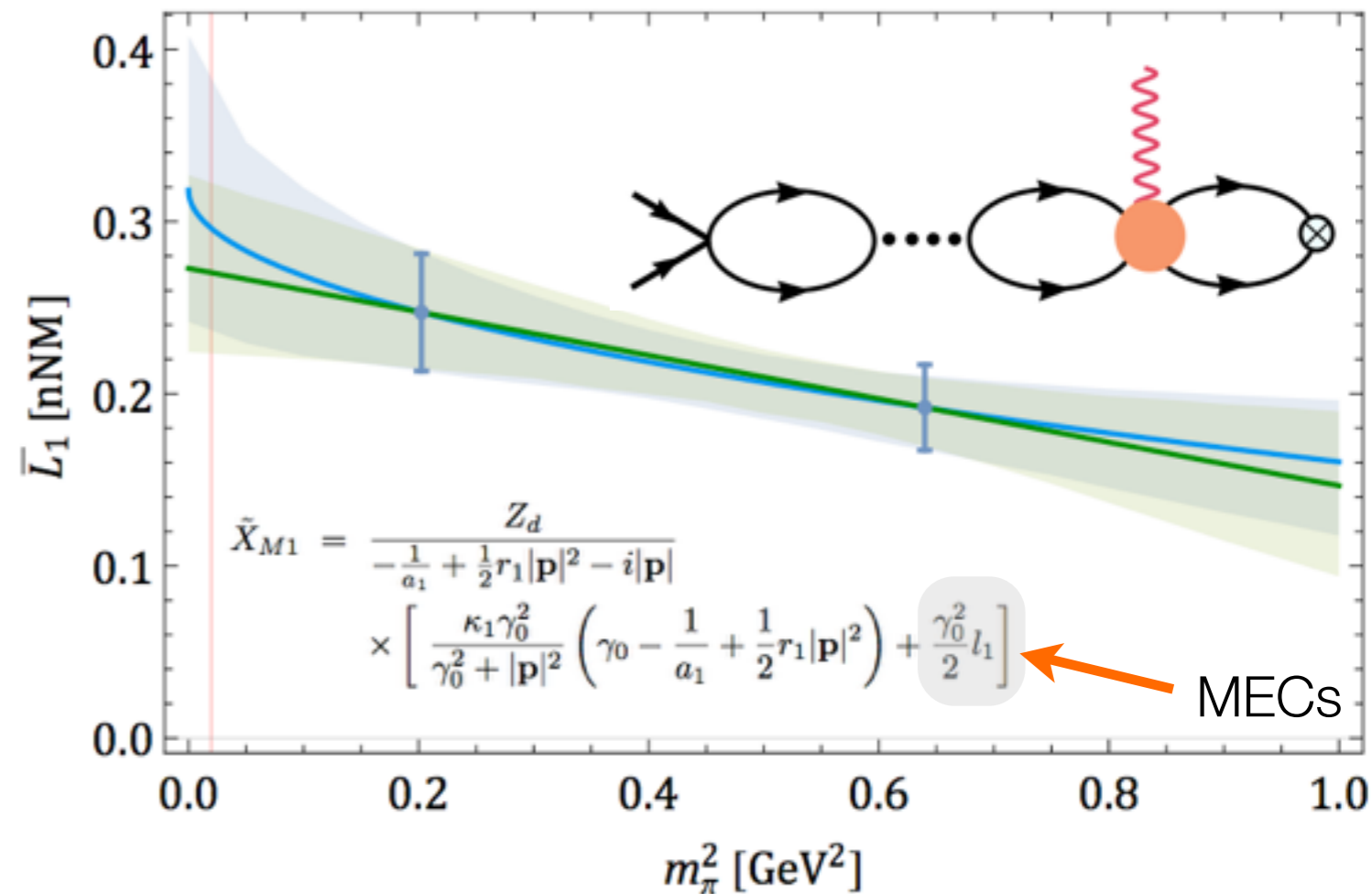
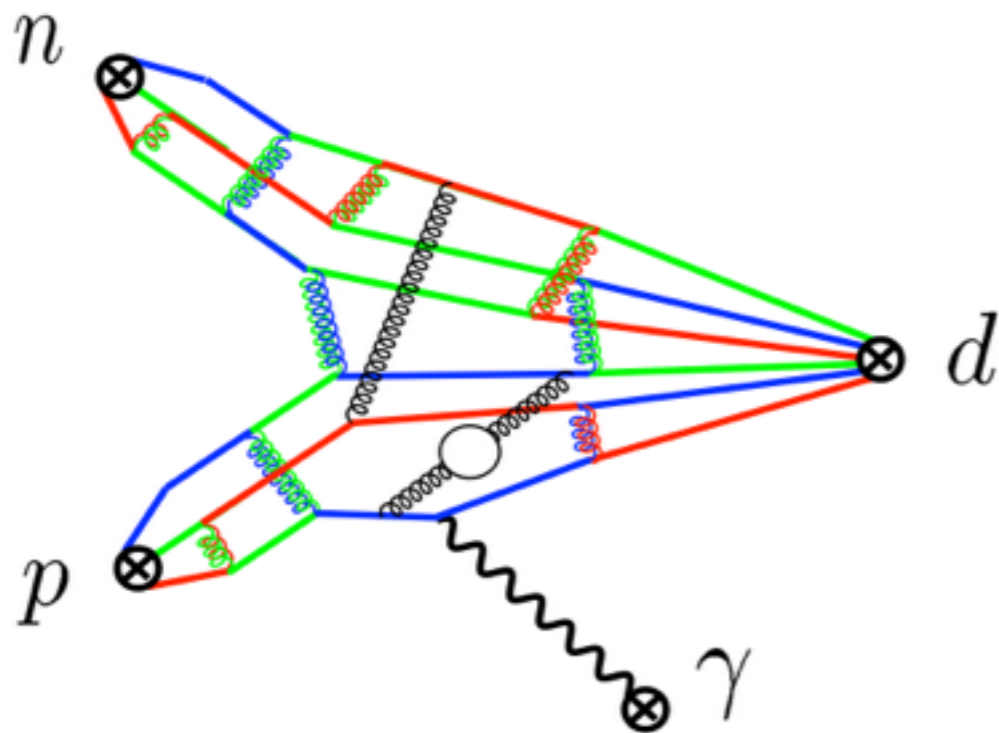
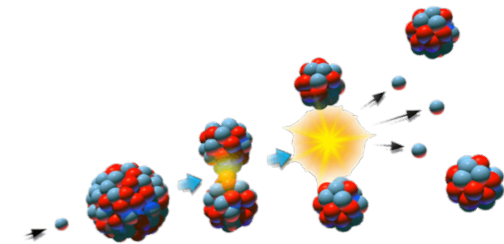
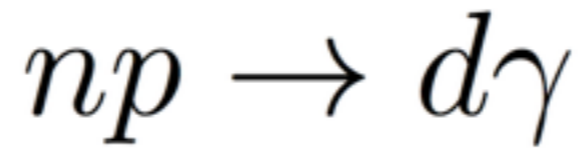


# The Periodic Table as a function of the quark masses



Enhances the scope of the Lattice Calculations

# First Inelastic Nuclear Reaction :



physical point:

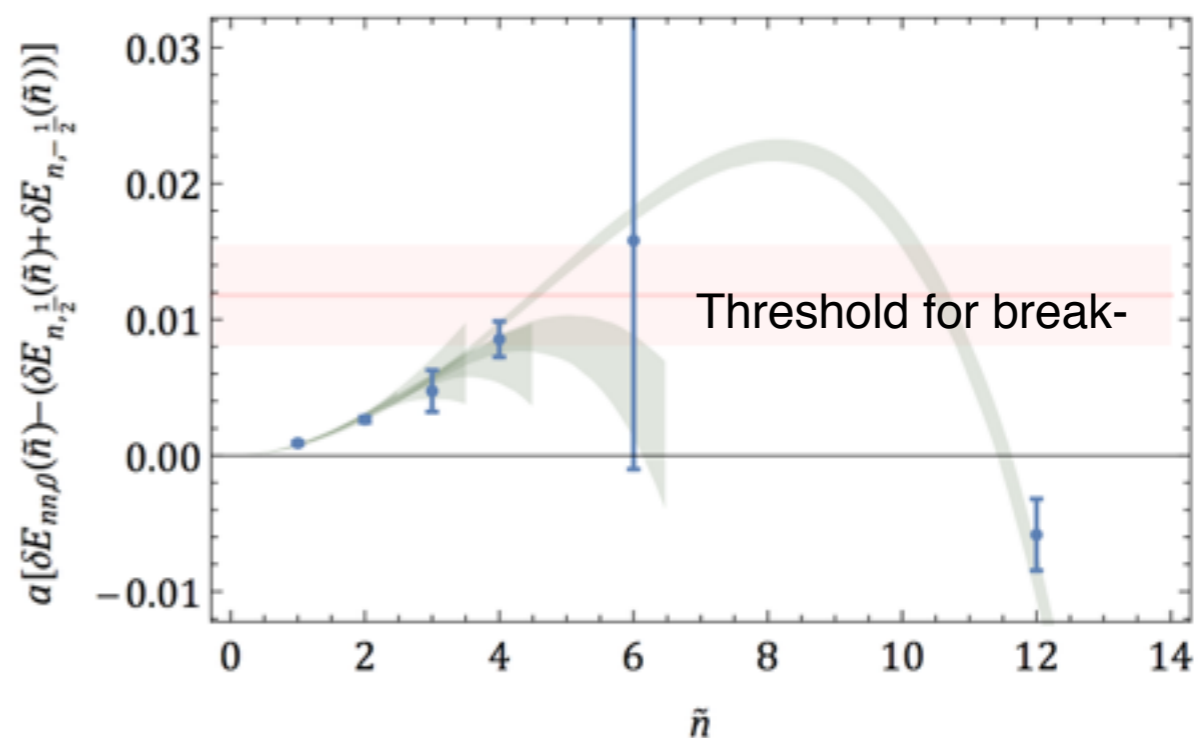
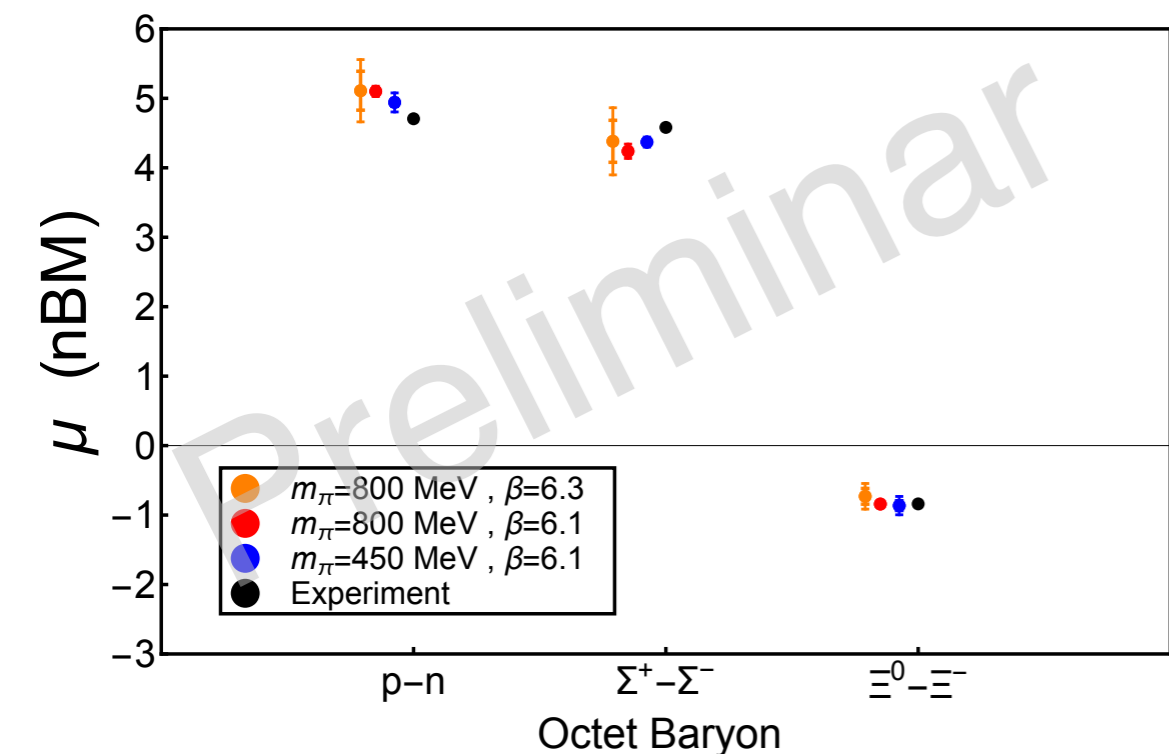
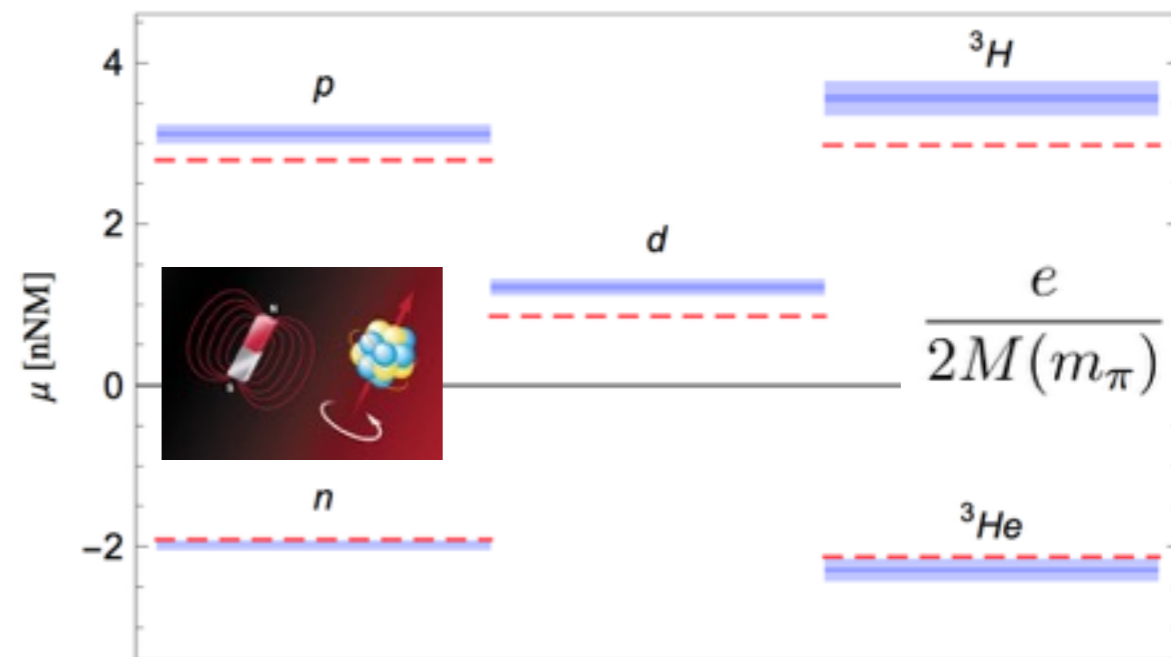
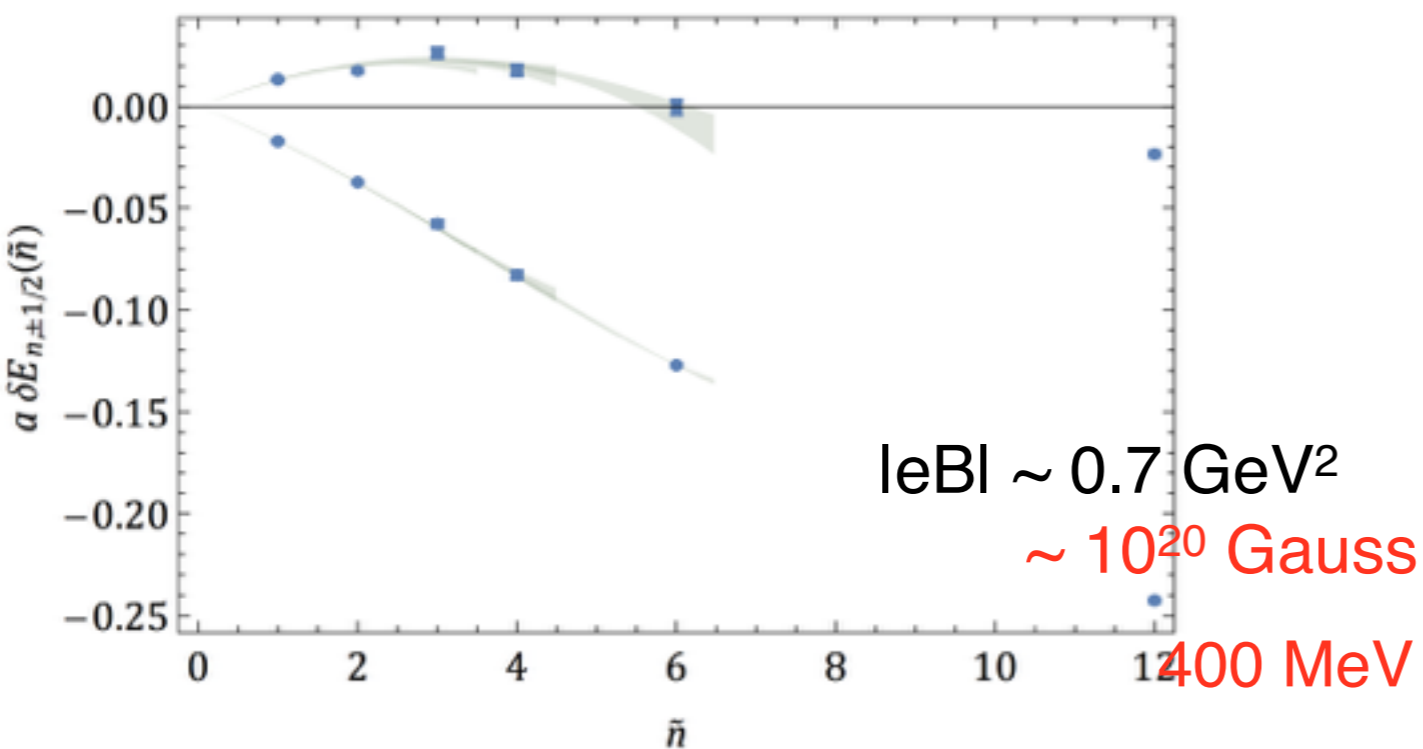
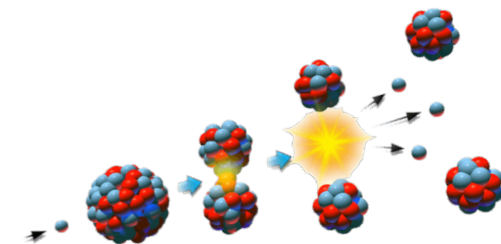
$$\sigma^{\text{LQCD}} = 334.9(5.3) \text{ mb}$$

$$v = 2,200 \text{ m/s}$$

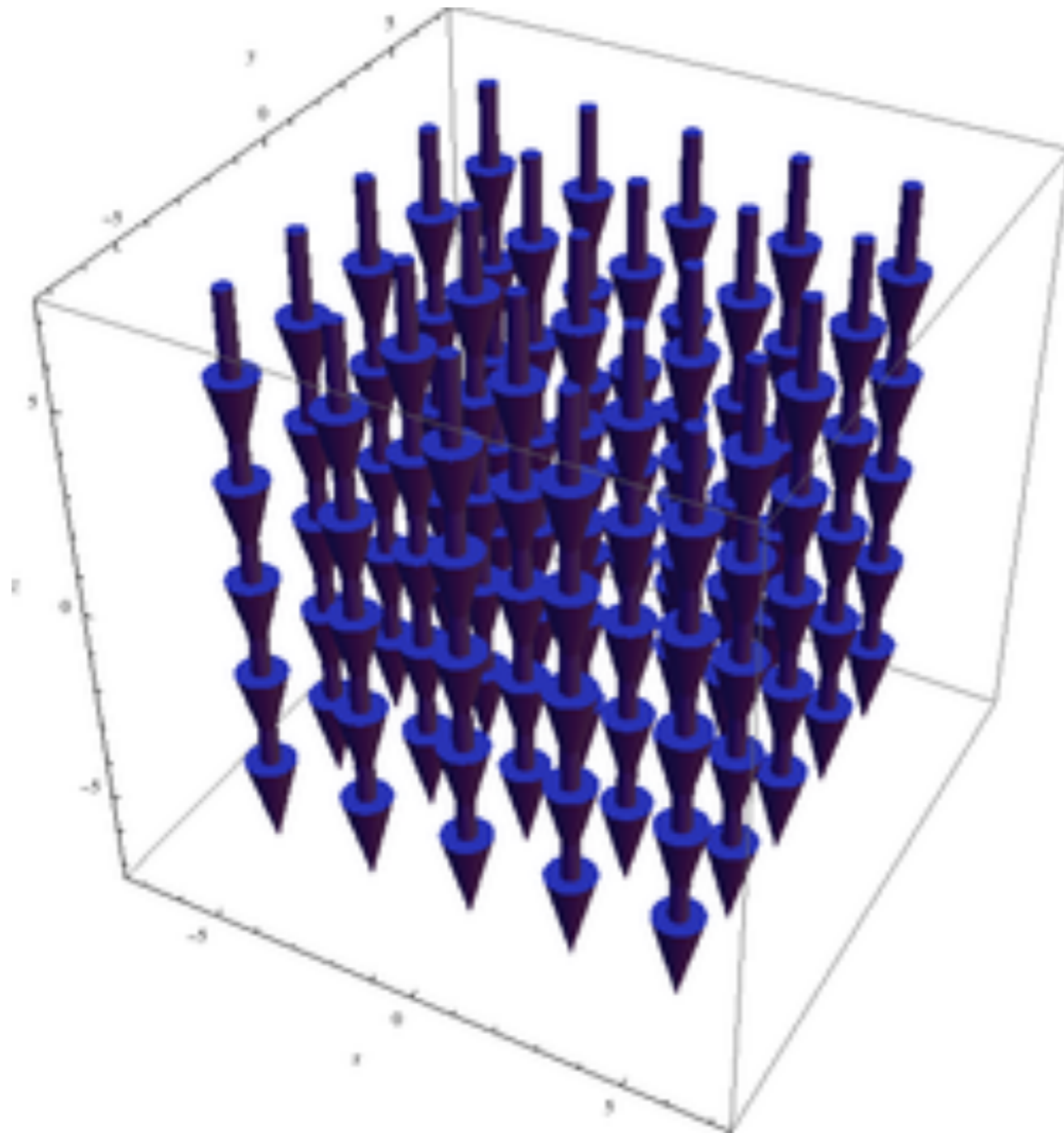
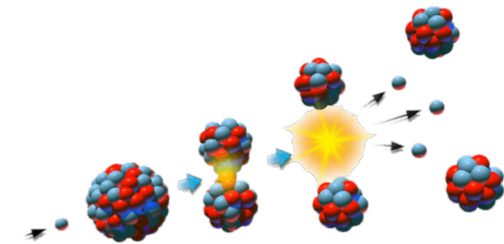
$$\sigma^{\text{expt}} = 334.2(0.5) \text{ mb}$$

[ 306 mb single nucleons alone ]

# Magnetic Moments Neutron Spin States

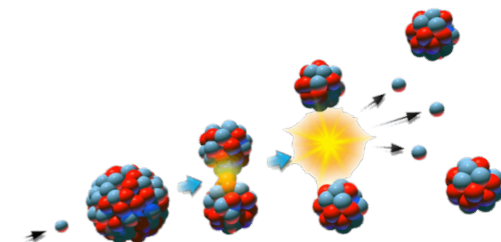


# Axial-Current Matrix Elements



Uniform  
Spacetime Independent  
Axial Background Field  
 $W^{a_{\mu}} \rightarrow W^3_z$

# Axial-Current Matrix Elements

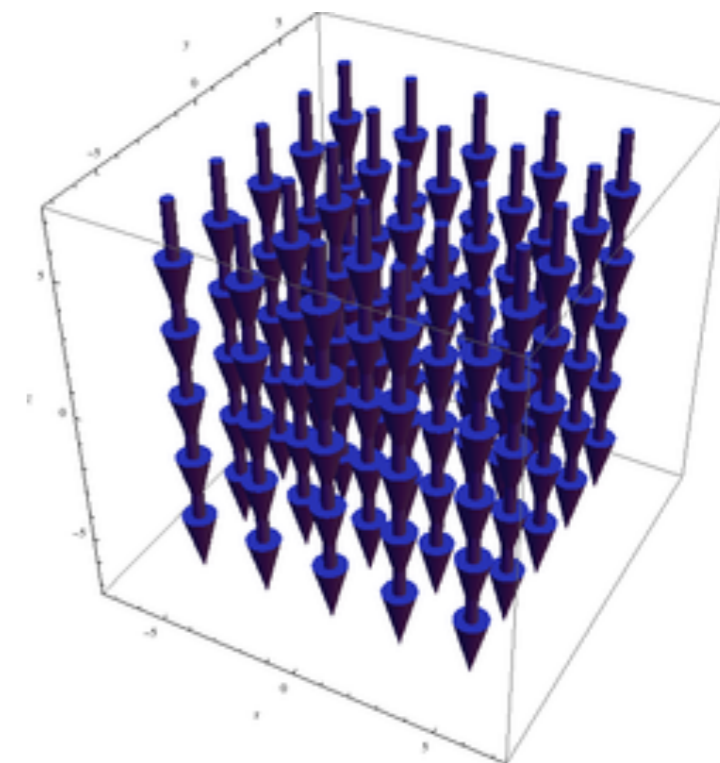


Formalism developed in  
**Electroweak matrix elements in the two nucleon sector from lattice QCD**

William Detmold, MJS  
 Nucl. Phys. A743 (2004) 170-193

quark-level interactions

$$\delta\mathcal{L} = -\frac{1}{2}gW (\bar{u}\gamma^z\gamma_5u - \bar{d}\gamma^z\gamma_5d)$$

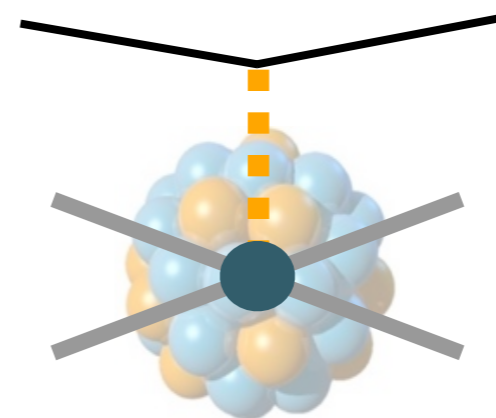
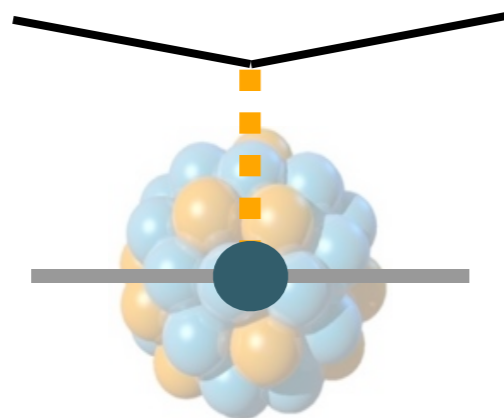


hadronic-level interactions

$$\delta\mathcal{L} = -gW \frac{g_A}{2} N^\dagger \sigma^z \tau^3 N - \frac{gW l_{1,A}}{2M\sqrt{r_1 r_3}} [t_3^\dagger s_3 + \text{h.c.}] + \dots$$

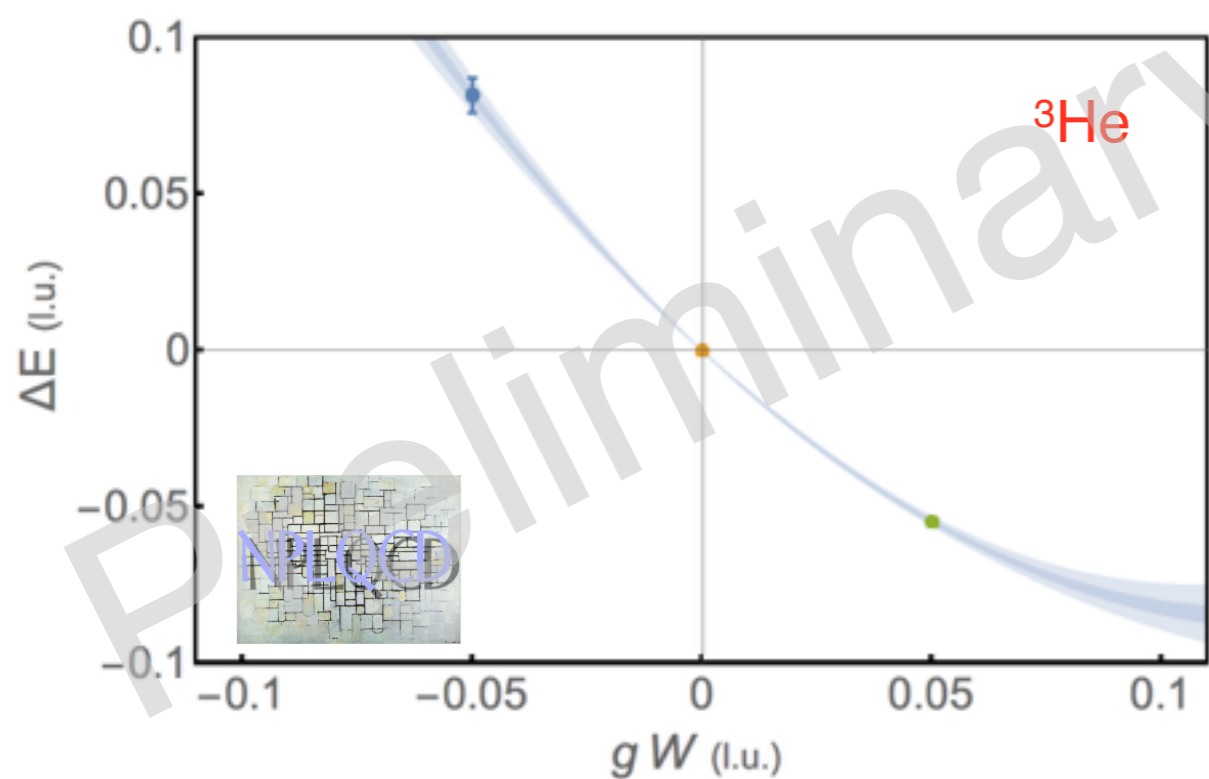
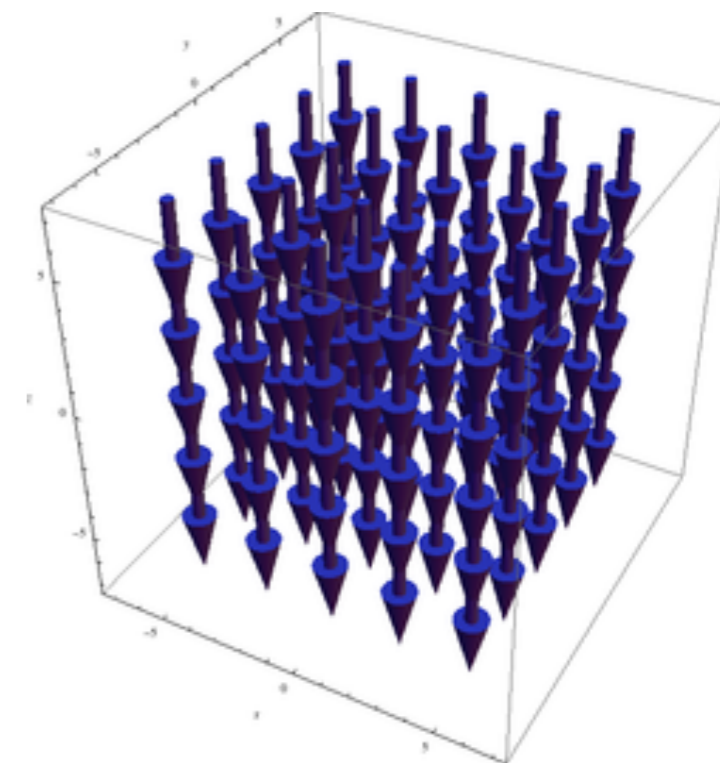
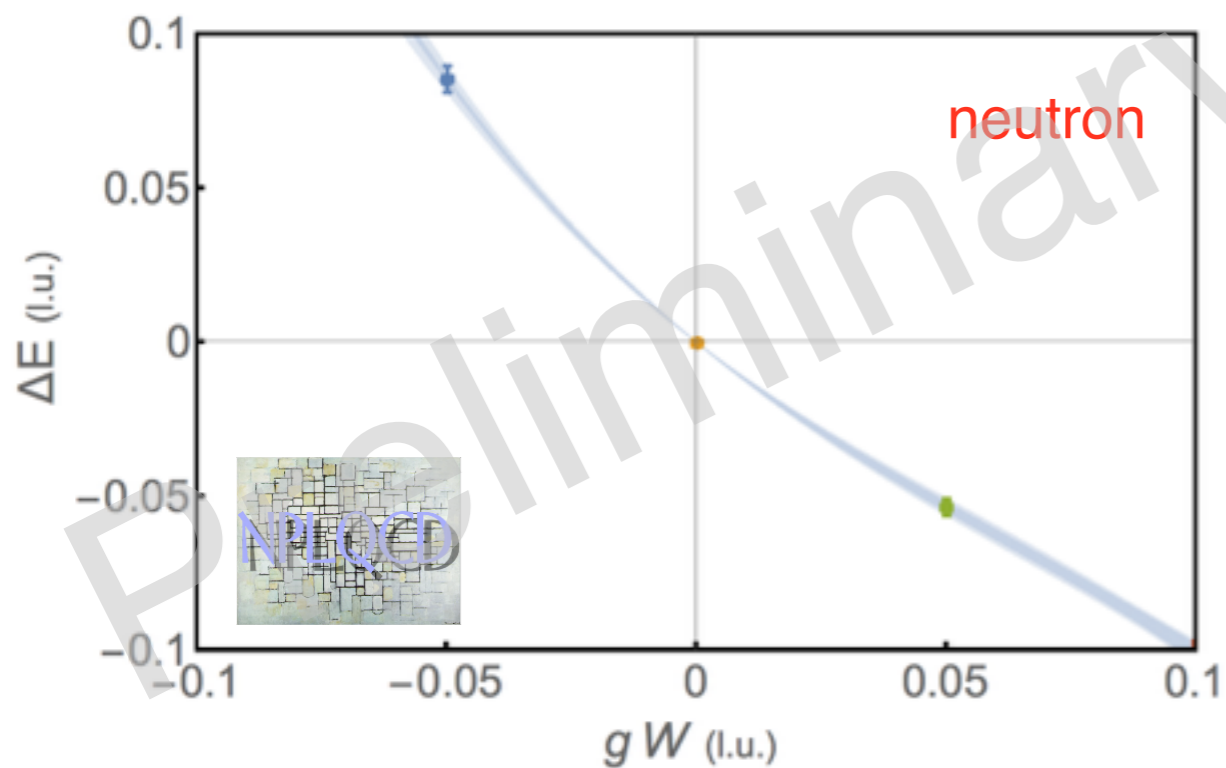
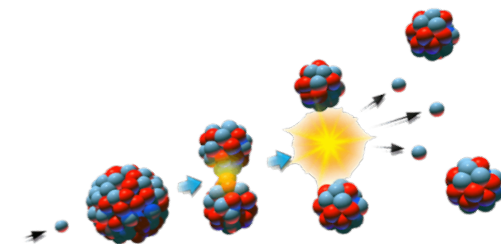
single-nucleon interaction

leading two-nucleon interaction



# Axial-Current Matrix Elements

$M_\pi \sim 800$  MeV



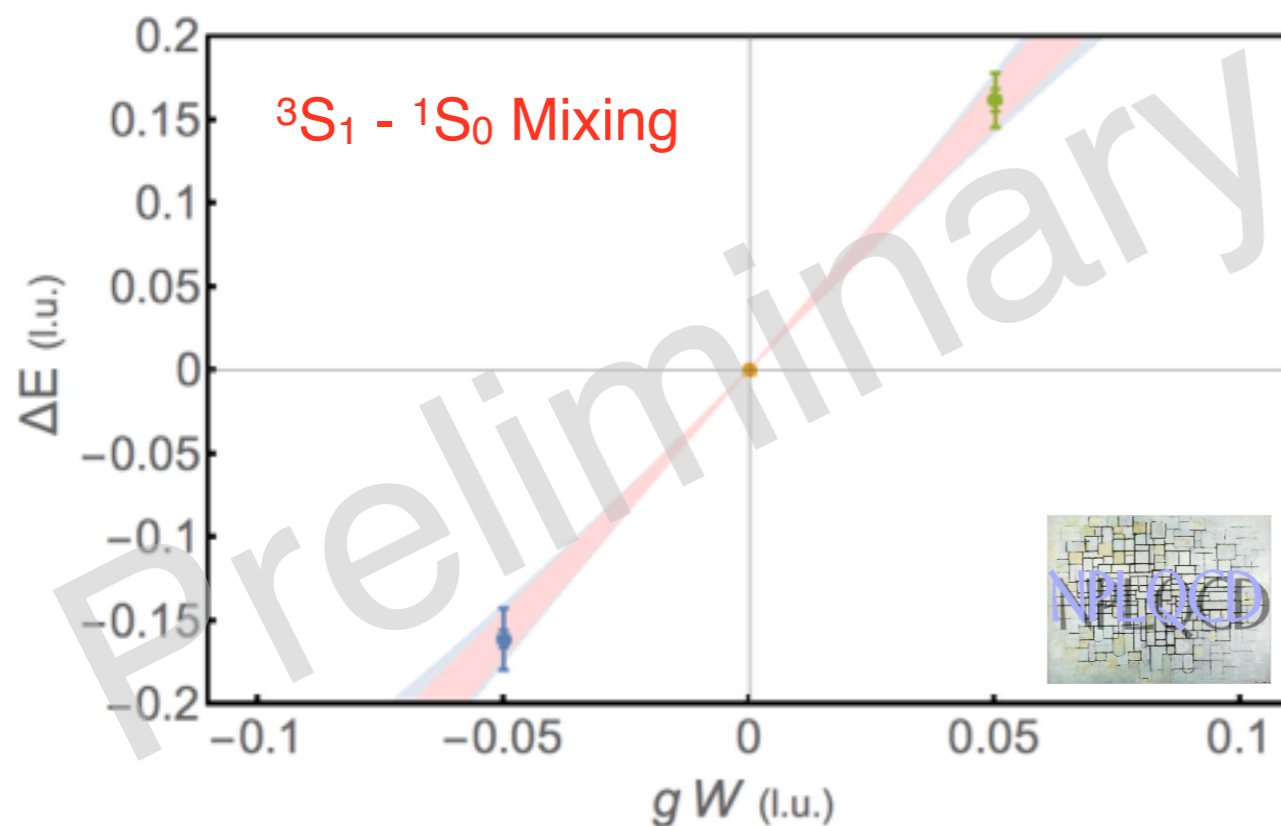
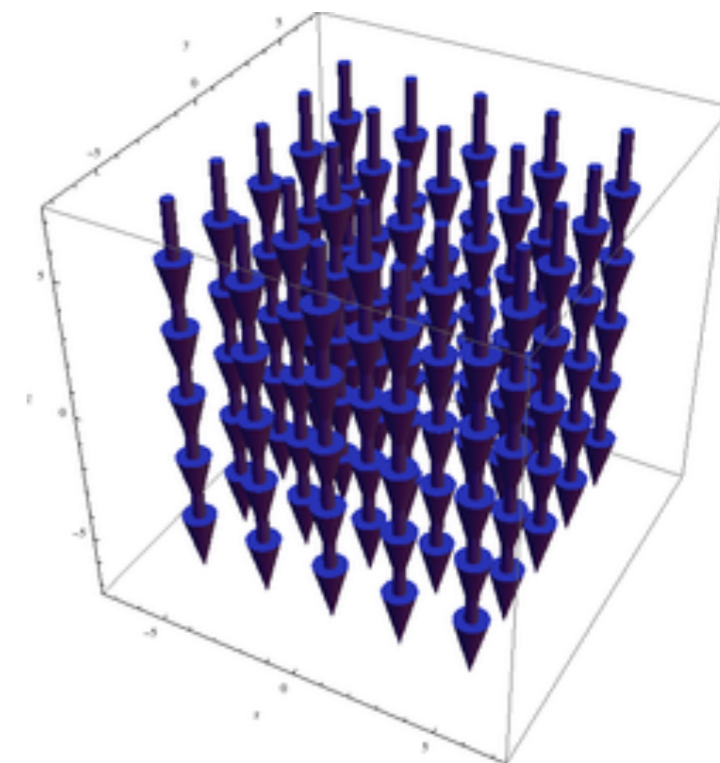
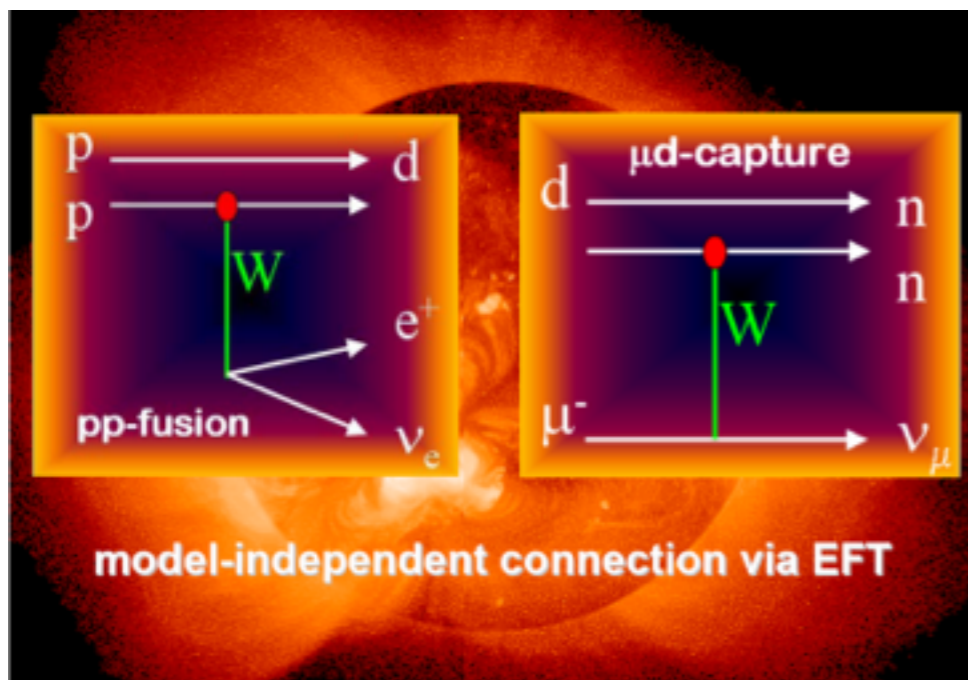
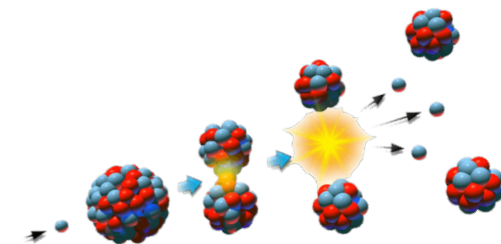
p :  $g_A \sim 1.2$

$^3\text{He}$  :  $g_A \sim 1.2$

Preliminary

# Axial-Current Matrix Elements

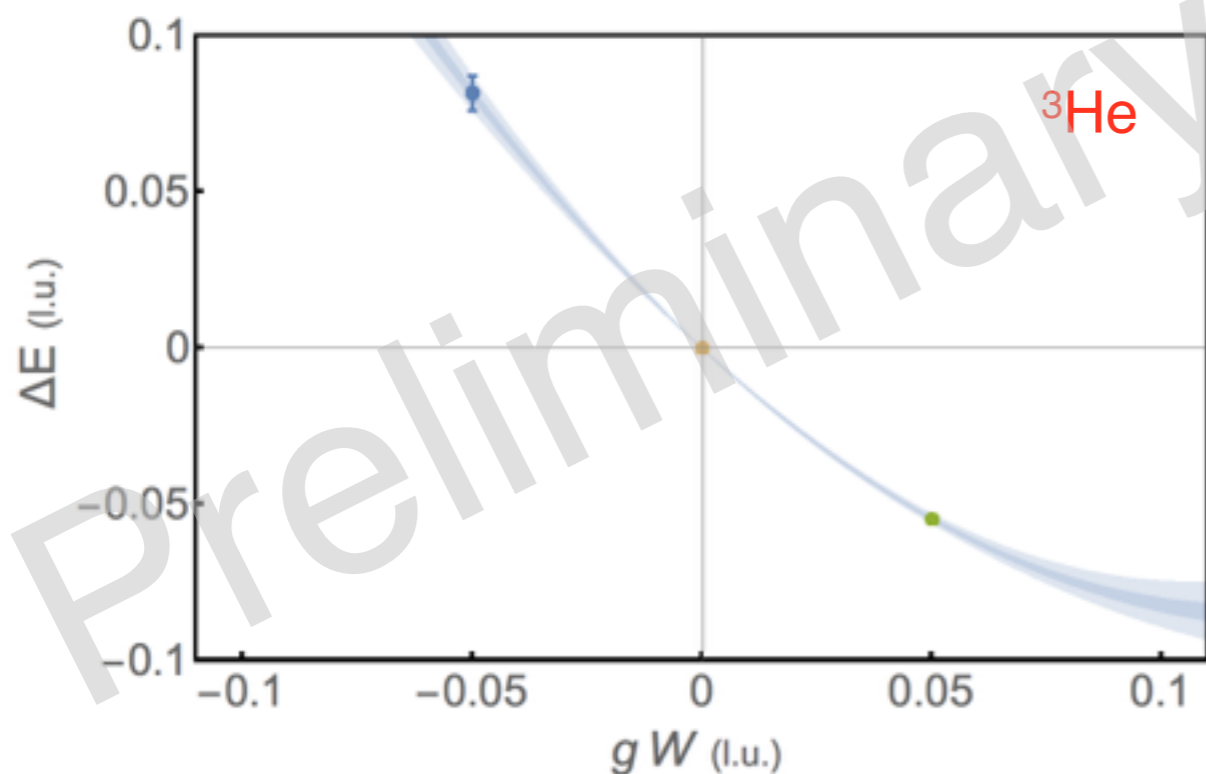
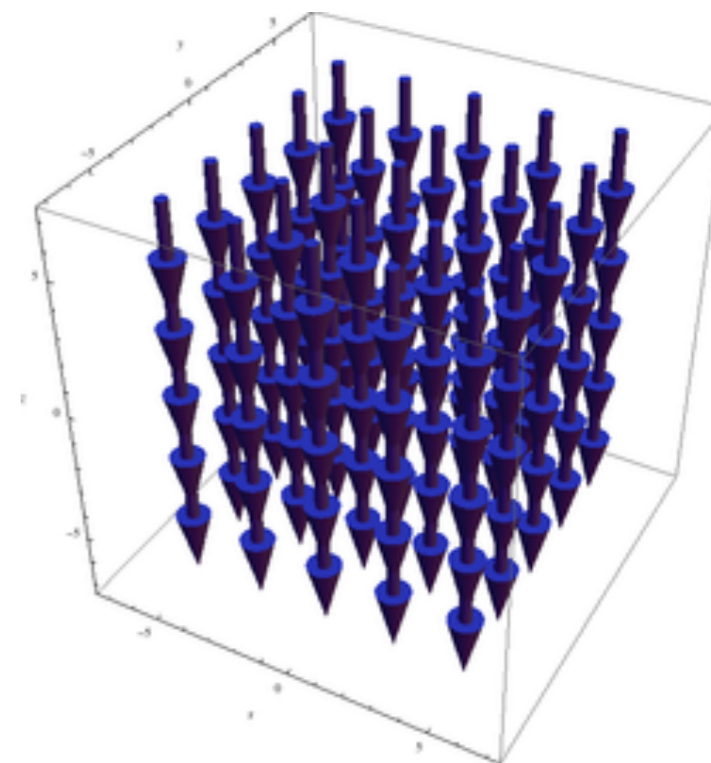
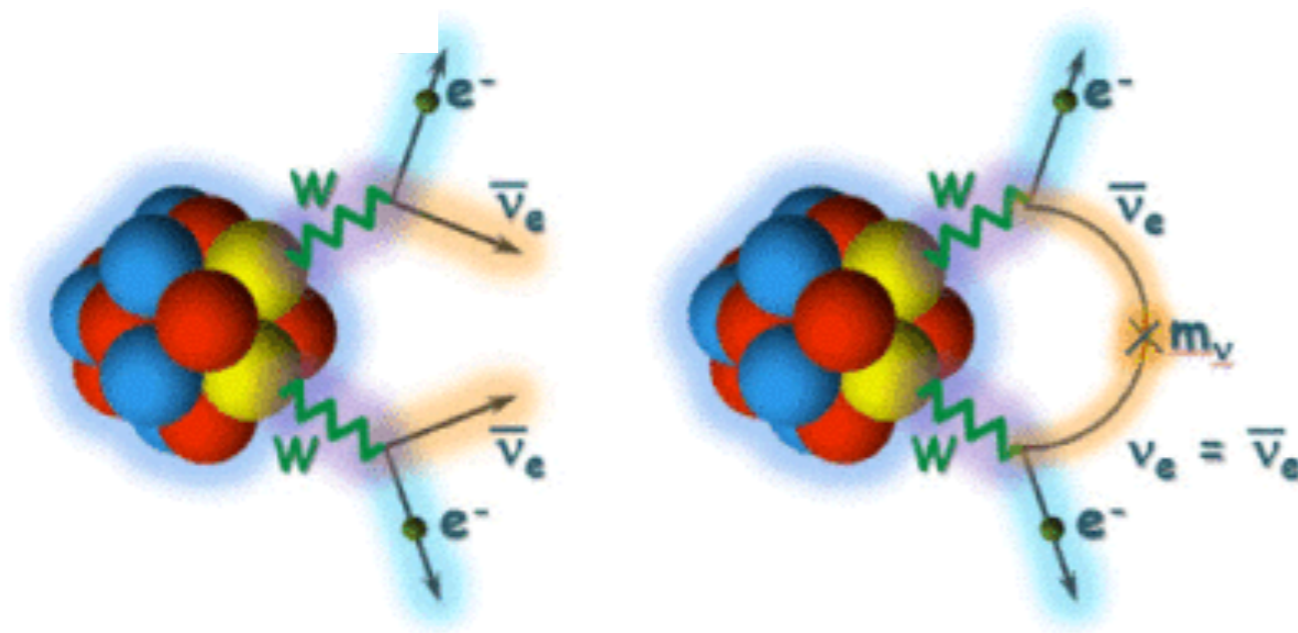
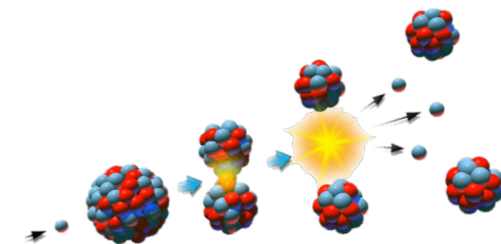
$M_\pi \sim 800 \text{ MeV}$



Extract the correlated two-nucleon interaction with axial field :  $L_{1A}$

(aka - meson-exchange currents)

# Axial Polarizabilities and $0\nu\beta\beta$ -decay rates

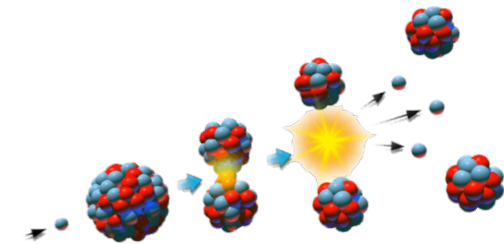


Curvature determined by Axial Polarizabilities.

Long-distance contribution to  $0\nu\beta\beta$ -decay matrix elements



# Summary and Outlook



- Lattice QCD of light nuclei and Interactions is underway
- Background field methods are valuable tools for electroweak and DM matrix elements,
  - e.g. Zohreh Davoudi, William Detmold, Phys.Rev. D92 (2015) no.7, 074506
- Axial current ME's are being calculated in light nuclei
  - refine chiral nuclear forces used in nuclear many-body calculations
- Axial polarizabilities important for  $0\nu\beta\beta$ -decay matrix element calculations



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FIN