



# 38th INTERNATIONAL CONFERENCE ON HIGH ENERGY PHYSICS

AUGUST 3 - 10, 2016  
CHICAGO

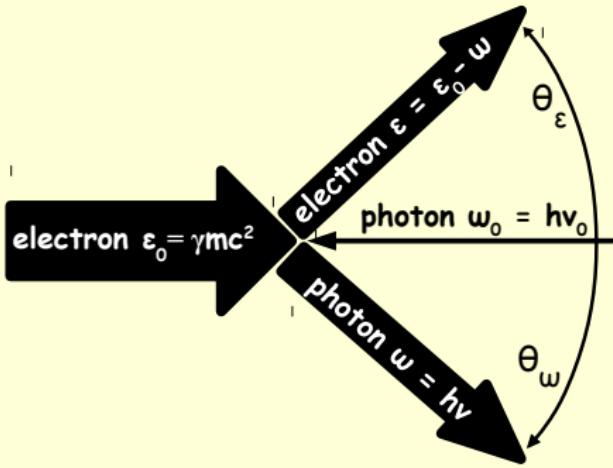
## Review of the laser backscattering as an approach for the electron beam energy measurement

Nickolai Muchnoi

Budker INP, Novosibirsk

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# Inverse Compton Scattering



$$u = \frac{\omega}{\varepsilon} = \frac{\theta_\varepsilon}{\theta_\omega} = \frac{\omega}{\varepsilon_0 - \omega}$$

$$u \in \left[ 0 : \kappa = \frac{4\omega_0\varepsilon_0}{m^2} \right]$$

$$\theta_\omega = \frac{1}{\gamma} \sqrt{\frac{\kappa}{u} - 1}$$

$$\theta_\varepsilon = \frac{4\omega_0}{m} \sqrt{\frac{u}{\kappa} \left( 1 - \frac{u}{\kappa} \right)}$$

Maximum energy of photon ( $u = \kappa$ ,  $\theta_\omega = \theta_\varepsilon = 0$ ):  $\boxed{\omega_{max} = \frac{\varepsilon_0\kappa}{1 + \kappa}}$

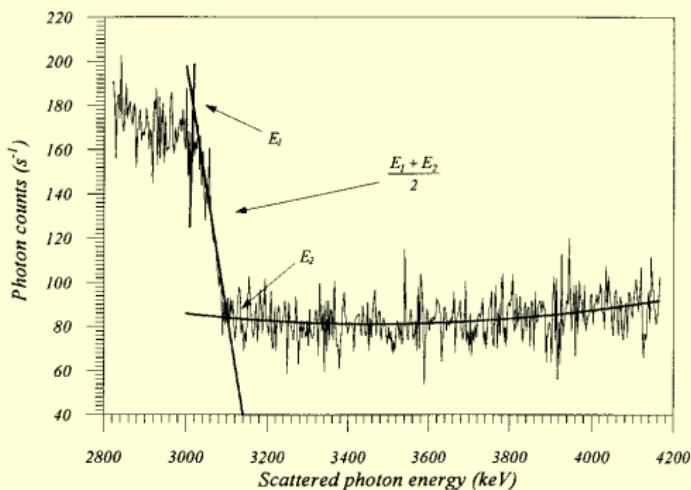
If  $\omega_0$  is a laser photon and we measure  $\omega_{max}$ :

$$\varepsilon_0 = \frac{\omega_{max}}{2} \left( 1 + \sqrt{1 + m^2/\omega_0\omega_{max}} \right) \simeq \frac{m}{2} \sqrt{\frac{\omega_{max}}{\omega_0}}.$$

# Laser backscattering for beam energy calibration

## First experiment in 1996

Taiwan Light Source  
CO<sub>2</sub> laser & HPGe detector



$E = 1305.8 \pm 1.7$  MeV  
Phys. Rev. E v.54 (5) 1996

## STORAGE RINGS

- BESSY-I – 1998
- BESSY-II – 2002
- VEPP-3 – 2008
- NewSUBARU – 2009
- ANKA – 2015

## e<sup>+</sup>/e<sup>-</sup> COLLIDERS

- VEPP-4M – 2005
- BEPC-II – 2010
- VEPP-2000 – 2012

# Accurate energy scale transfer: eV → MeV → GeV

- IR optics: e. g. 10P20 CO<sub>2</sub> laser line  $\omega_0 = 0.117065228$  eV
- $\gamma$ -lines from radioactive isotopes as a good reference for  $\omega_{max}$ :

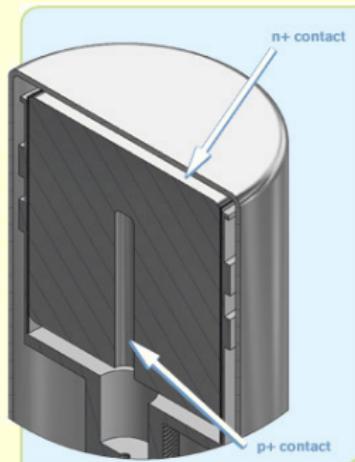
$^{137}\text{Cs}$	$\tau_{1/2} \simeq 30.07$ y	$E_\gamma = 0661.657 \pm 0.003$ keV
$^{60}\text{Co}$	$\tau_{1/2} \simeq 5.27$ y	$E_\gamma = 1173.228 \pm 0.003$ keV
		$E_\gamma = 1332.422 \pm 0.004$ keV
$^{208}\text{Tl}$	$\tau_{1/2} \simeq 3$ m	$E_\gamma = 2614.511 \pm 0.013$ keV
$^{16}\text{O}^*$	$^{232}\text{Pu} \rightarrow \alpha \rightarrow ^{13}\text{C}$	$E_\gamma = 6129.266 \pm 0.054$ keV

- Narrow resonances checkpoints (requires colliding beams)

$\phi$	$1019.461 \pm 0.019$ MeV	PDG - 2014
$J/\psi$	$3096.900 \pm 0.002 \pm 0.006$ MeV	KEDR - 2015
$\psi(2S)$	$3686.099 \pm 0.004 \pm 0.009$ MeV	KEDR - 2015

# Hardware

HPGe coaxial  
detector,  
p-type or n-type



(image: [www.canberra.com](http://www.canberra.com))

Multichannel Analyzer  
ORTEC® DSPEC Pro™



integral nonlinearity

$\pm 250 \text{ ppm}$

[www.ortec-online.com](http://www.ortec-online.com)

Pulse Generator  
BNC PB-5

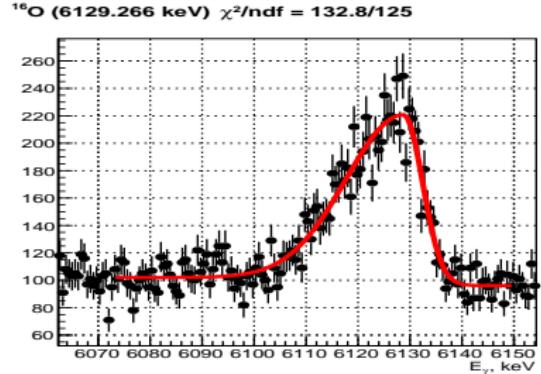
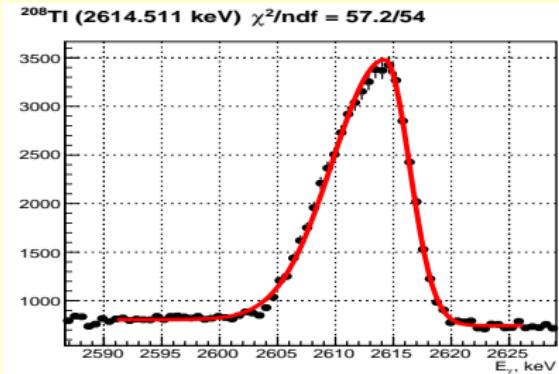
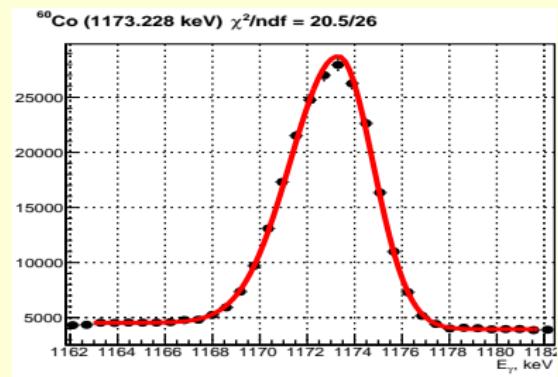
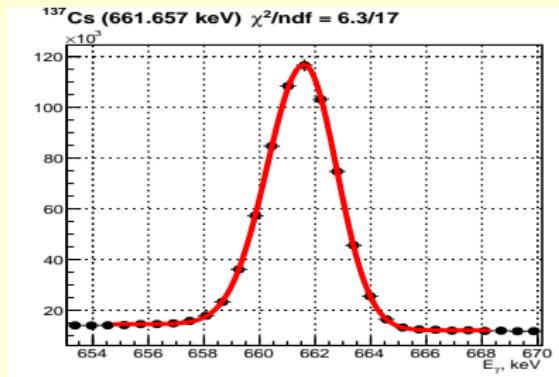


integral nonlinearity

$\pm 15 \text{ ppm}$

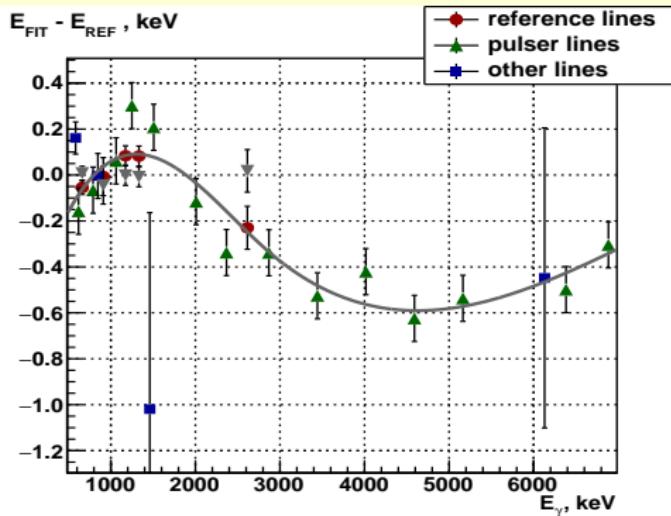
[www.berkeleynucleonics.com](http://www.berkeleynucleonics.com)

# HPGe calibration: photo-peaks fits (BEPC-II 2016)



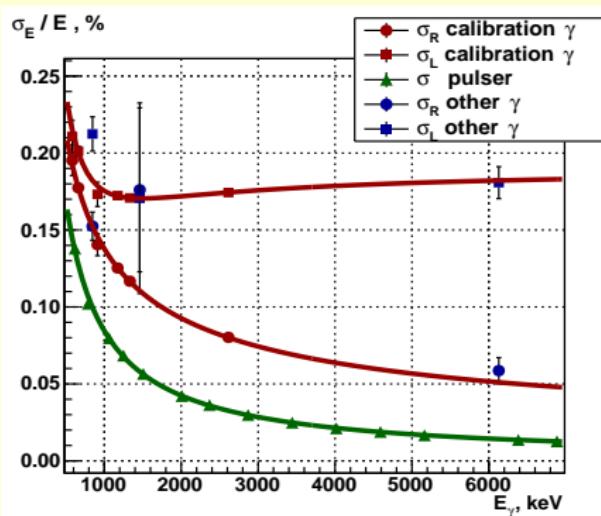
# HPGe energy scale & resolution (BEPC-II 2016)

## Residual Scale Nonlinearity:



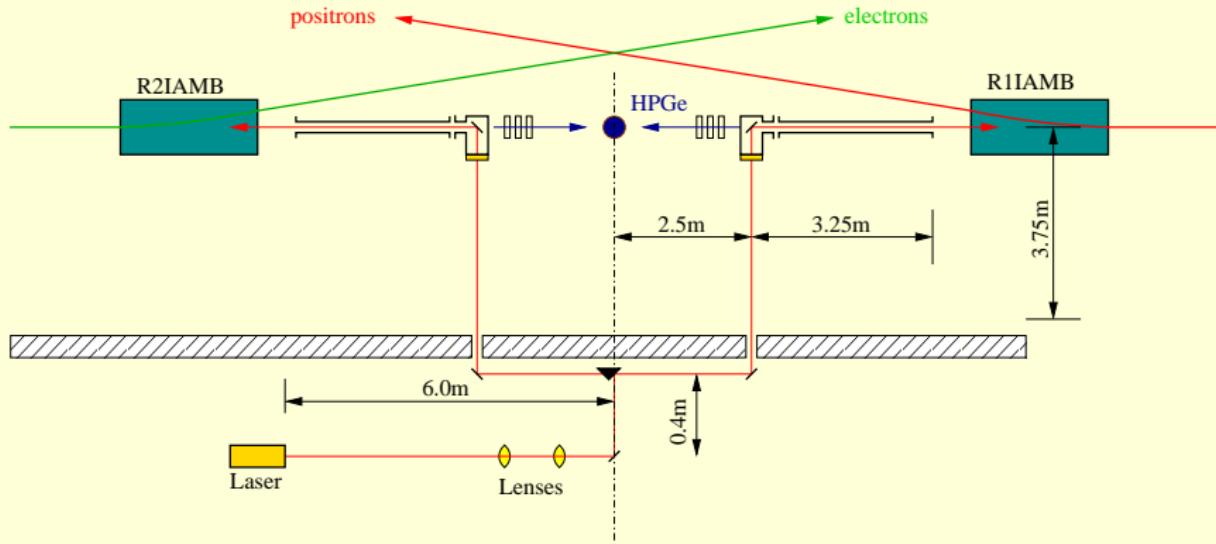
Use of pulser eliminates the MCA nonlinearity down to  $\sim 50$  ppm

## Energy Resolution:



Resolution asymmetry is due to neutron damage of HPGe

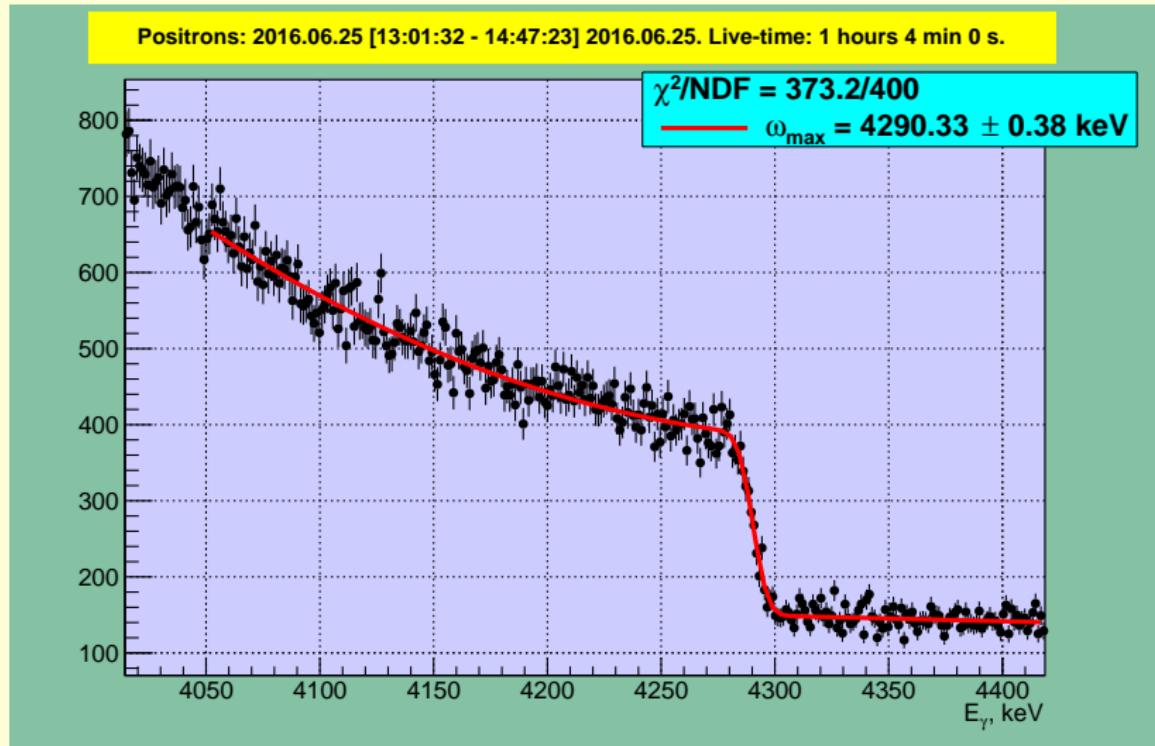
# BEPC-II Beam Energy Measurement System



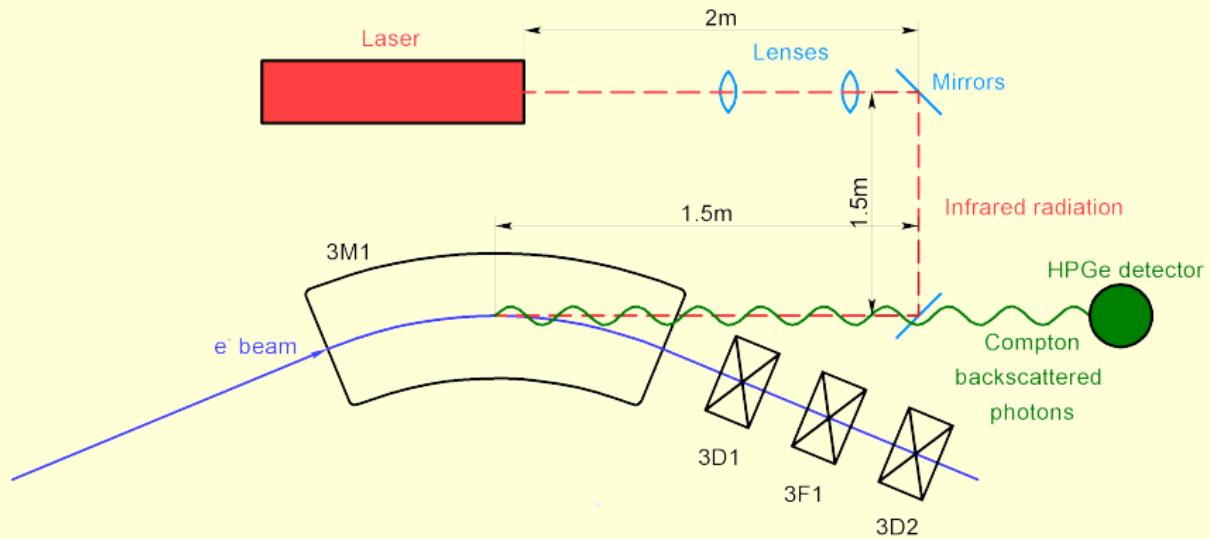
- Size of HPGe detector  $D \simeq 4$  cm
- Distance between HPGe and  $\gamma e^+/\gamma e^-$  scattering area  $L \simeq 8$  m
- Beams orbit angles should be “zero” within  $D/L \simeq \pm 2.5$  mrad

$$m_\tau = 1776.91 \pm 0.12^{+0.10}_{-0.13} \text{ MeV. Phys. Rev. D90 (2014) 012001}$$

# BEPC-II 2016 spectrum edge (example)

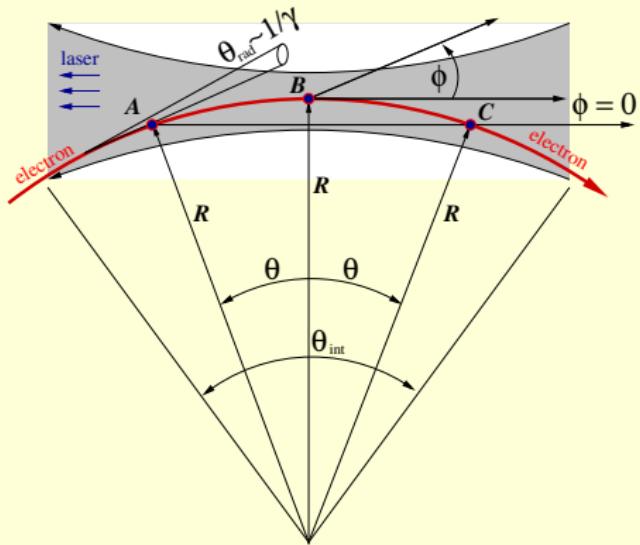


# VEPP-2000 Beam Energy Measurement System



Beam orbit radius in the VEPP-2000 dipole  $R = 140$  cm

Since  $\theta_{int} \gg \theta_{rad}$ , only  $\phi = 0$  case is a matter of interest



$$t_e = \frac{2R\theta}{\beta c}$$

Time for photon  $A \rightarrow C$ :

$$t_\gamma = \frac{2R \sin \theta}{c} \cos \psi$$

Phase shift:

$$\Delta\Phi = 2\pi c \left( \frac{t_e}{\lambda} - \frac{2t_e}{\lambda_0} - \frac{t_\gamma}{\lambda} \right),$$

where  $\lambda_0$  is the laser wavelength.

1 MeV photon has  $\lambda = 1.24 \cdot 10^{-12}$  m. For  $R = 140$  cm,  $E = 1$  GeV,  $\Delta\Phi = 2\pi$  when  $\theta \simeq 0.1/\gamma$  and  $\overline{AC} \simeq 10^{-2}$  cm  $\simeq 10^8 \lambda!$

# Interference of scattered photons / PRL 110 2013 140402

The photon spectrum is:

$$\frac{dN_\gamma}{d\hbar\omega d\psi} \propto \omega^{1/3} \text{Ai}^2(x),$$

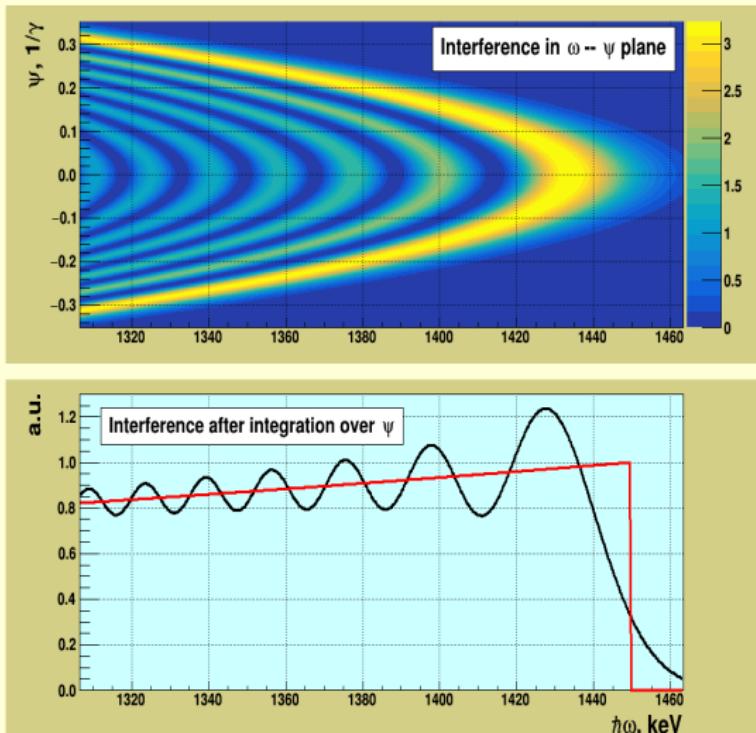
where

$$x = \left[ \frac{\omega R}{2c} \right]^{2/3} \left[ \frac{1}{\gamma^2} - \frac{4\omega_0}{\omega} + \psi^2 \right]$$

and

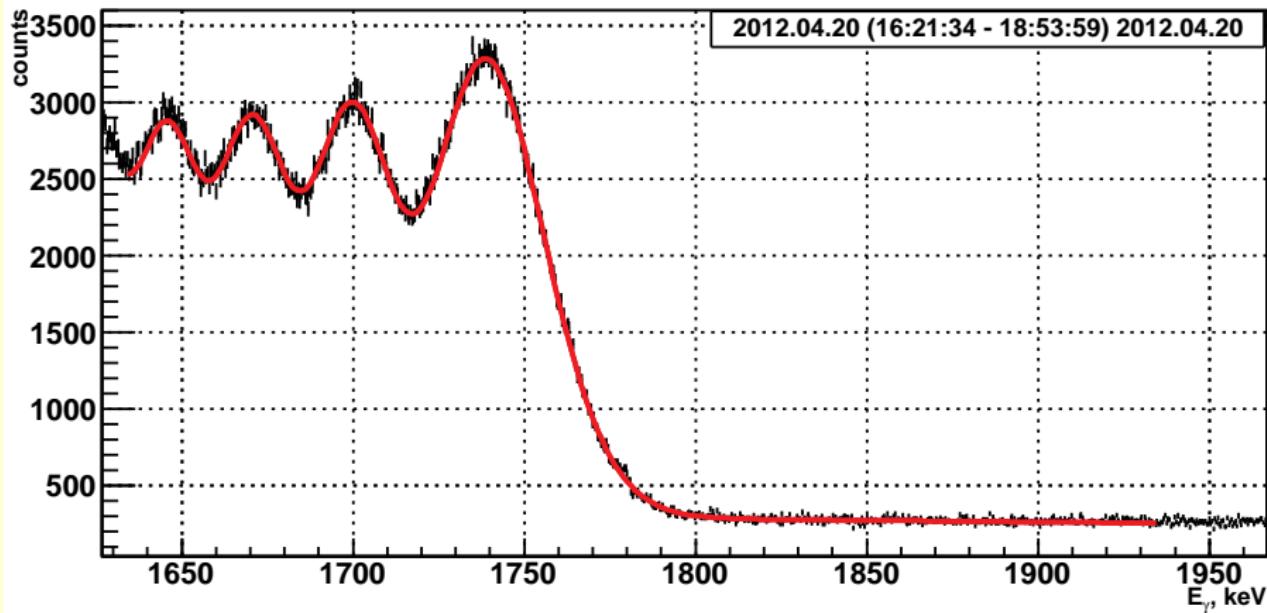
$$\text{Ai}(x) = \frac{1}{\pi} \int_0^\infty \cos \left( xt + \frac{t^3}{3} \right) dt$$

is the Airy function.



$$(\omega_0=0.117 \text{ eV}, E_e = 900 \text{ MeV}, R=140 \text{ cm})$$

# Experimental spectrum & fit / PRL 110 2013 140402

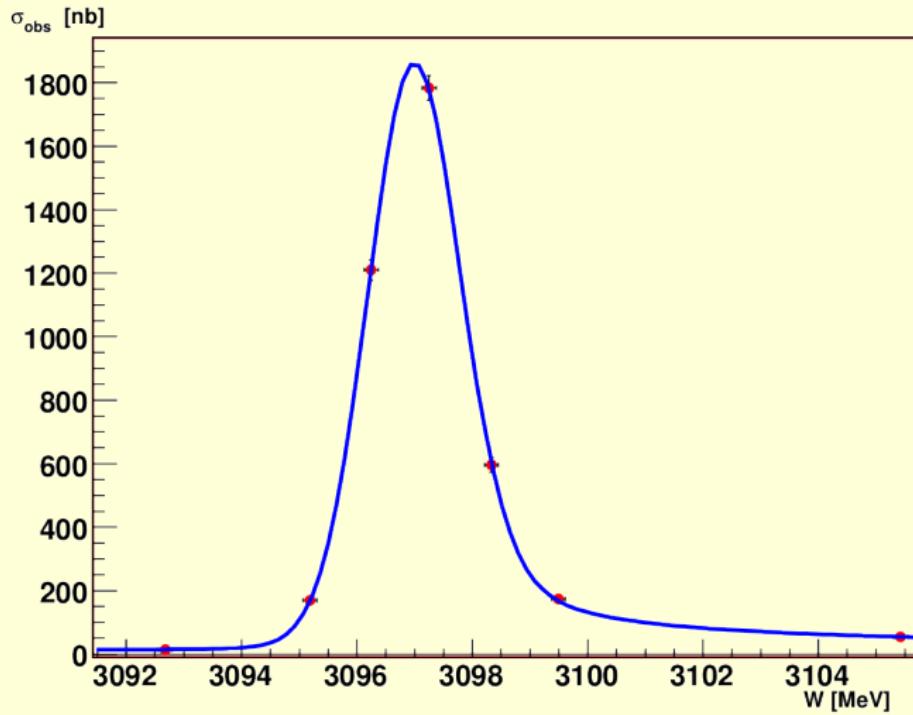


The edge of the energy spectrum with the fit result:

$$\chi^2/NDF = 773.0/745, \text{ Prob.} = 0.231,$$

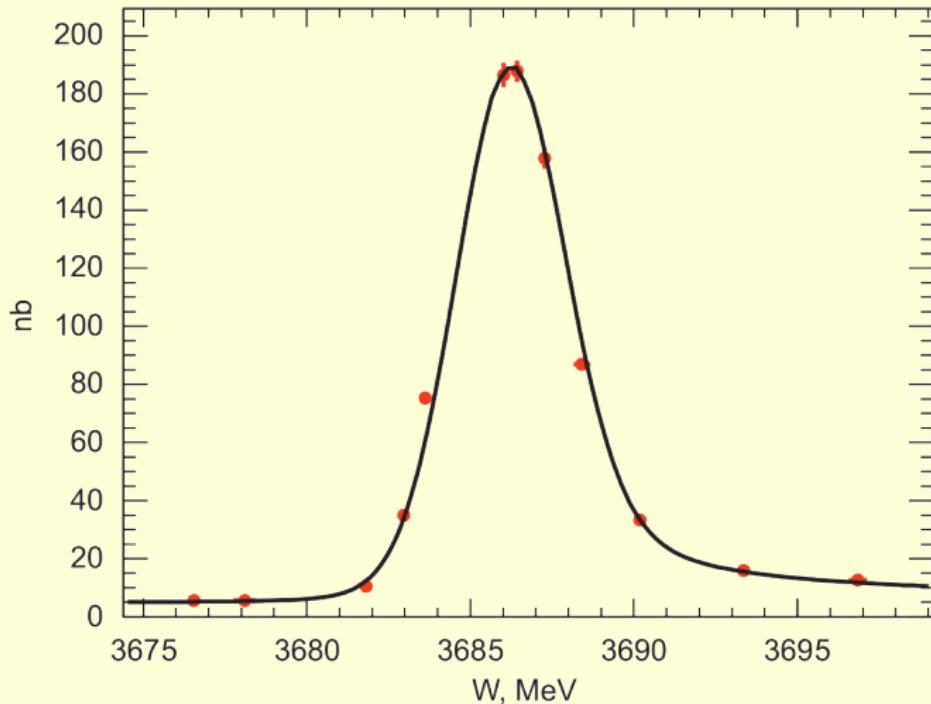
$$E = 993.662 \pm 0.016 \text{ MeV}, B = 2.3880 \pm 0.0044 \text{ T}, \sigma = 810 \pm 40 \text{ keV}.$$

# Cross section $e^+e^- \rightarrow \text{hadrons}$ , KEDR (2010)



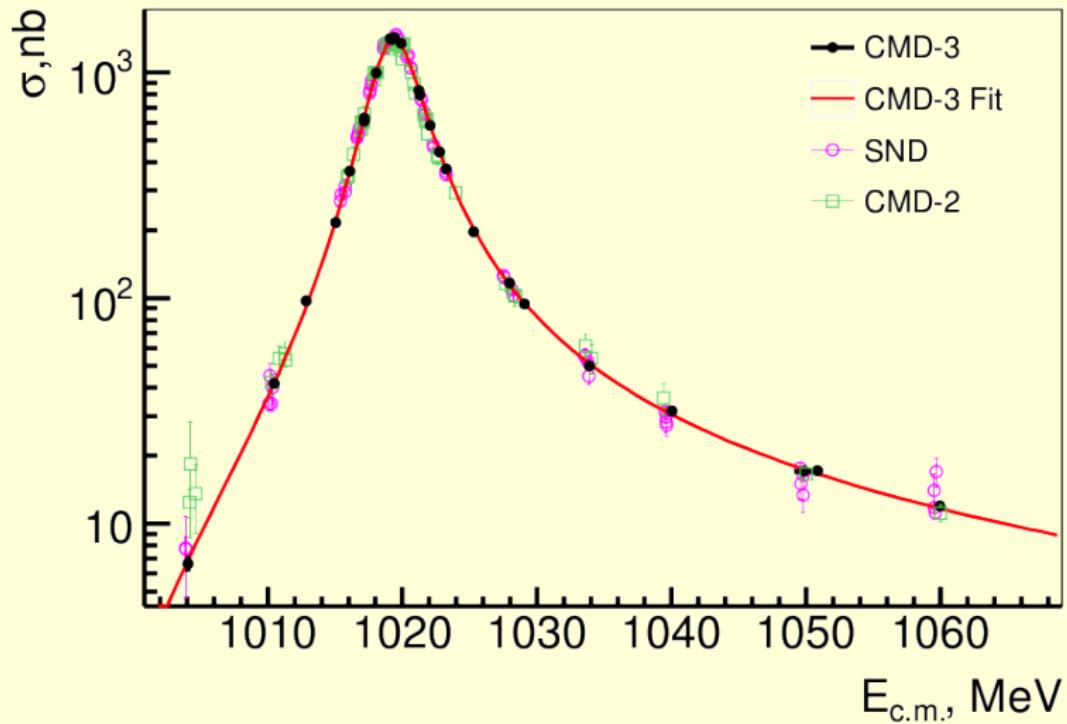
$$m_{J/\psi} - m_{J/\psi}^{PDG} = 1.2 \pm 14.7 \text{ keV}$$

# Cross section $e^+e^- \rightarrow \text{hadrons}$ , BES-III (2011)



$$m_{\psi(2S)} - m_{\psi(2S)}^{PDG} = 1 \pm 72 \text{ keV}$$

# Cross section $e^+e^- \rightarrow K_SK_L$ , CMD-3 (2013)



$$m_\phi - m_\phi^{PDG} = -8 \pm 20 \text{ keV}$$

# Conclusion

- The beam energy measurement systems were implemented successfully at three  $e^+/e^-$  colliders.
- The best accuracy achieved is at the level of  $\Delta E/E \lesssim 5 \cdot 10^{-5}$ .
- High accuracy measurements always requires careful continuous studies of the system performance, calibration, etc.
- There is not enough time to discuss here the extensions of the approach to higher energies. Please refer to my talk “Polarization Free Methods for Beam Energy Calibration.”

THANK YOU!