



Max-Planck-Institut für Physik  
(Werner-Heisenberg-Institut)

# Top Quark Mass Measurements with the ATLAS Detector

Andreas Wildauer  
on behalf of the ATLAS Collaboration

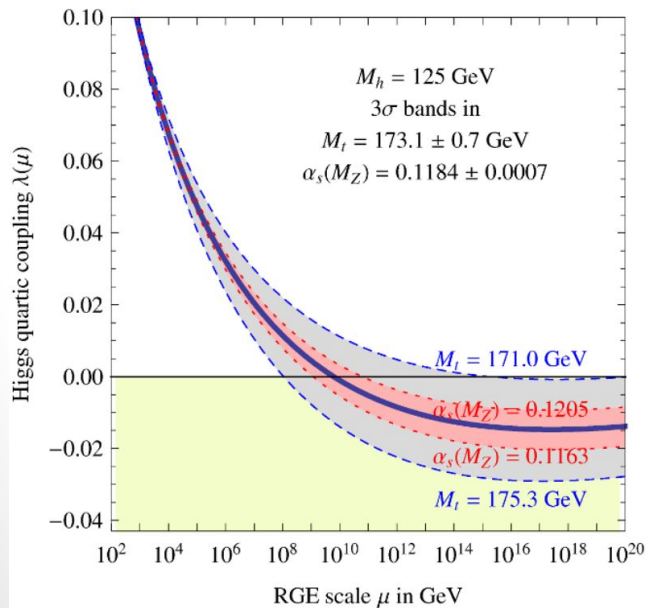
Max-Planck Institut für Physik  
München

38th ICHEP

August 3 - 10, 2016  
Chicago

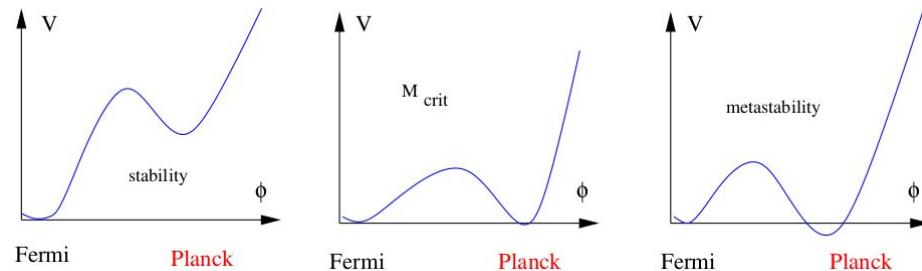
# Top Quark Physics - Introduction

- The top quark is the heaviest known fundamental building block
- Its mass is a free fundamental parameter of the Standard Model (SM)
- World combination 2014 of Tevatron and LHC data
  - $m_{\text{top}} = 173.34 \pm 0.27 \text{ (stat)} \pm 0.71 \text{ (syst)} \text{ GeV}$ , total: 0.6% ([arXiv:1403.4427](https://arxiv.org/abs/1403.4427))
- $m_{\text{top}}$  is an important ingredient for the consistency of the SM
  - especially in conjunction with the mass of the Higgs Boson
  - a low  $m_{\text{Higgs}}$  around 125-130 GeV leads to a stable vacuum if the Higgs quartic coupling  $\lambda$  is small at the Planck scale ( $\sim 10^{19}$  GeV)
  - it depends on  $m_{\text{Higgs}}$  and  $m_{\text{top}}$  at which scale  $\lambda$  becomes small (or negative)



[JHEP 1208 \(2012\) 098](https://arxiv.org/abs/1208.098)

picture from [arXiv:1311.4979](https://arxiv.org/abs/1311.4979)



$$V = \frac{1}{2}\mu^2\Phi^2 + \frac{1}{4}\lambda\Phi^4$$

# Top Quark Mass - Direct Measurements

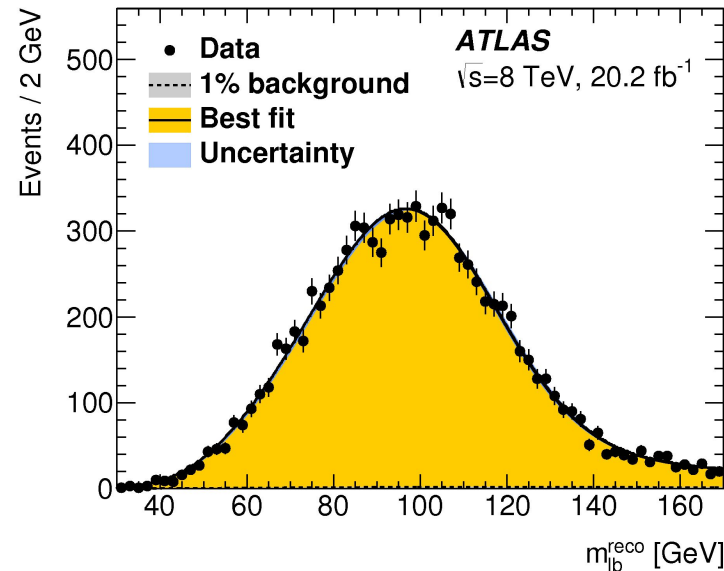
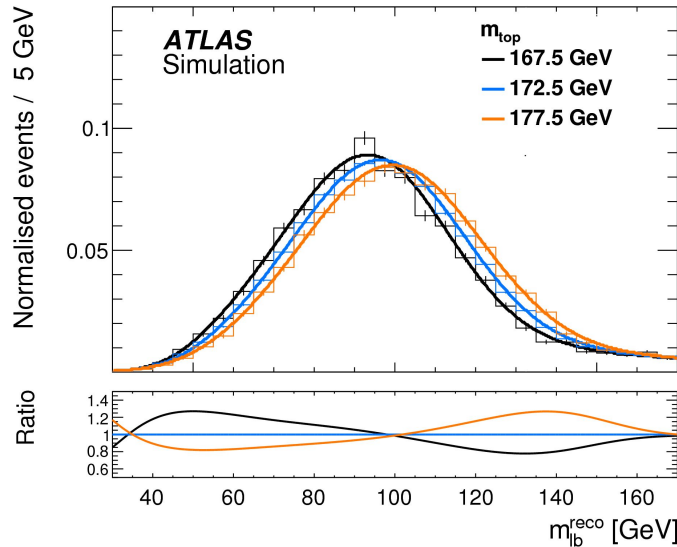
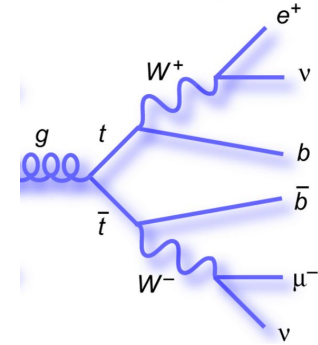
- In ATLAS, direct measurements of the top quark are all performed with the template method
  - Choose a reconstructible quantity which depends on the top quark mass
    - this is the estimator for the top quark mass measurements
  - Construct templates (histograms) with the estimator at various Monte Carlo (MC) input top quark mass values
  - Fit the templates with suitable functions (gauss, landau, novosibirsk, ...)
  - Linearize the parameters of these functions (gauss mean, width, ...) as a function of the Monte Carlo input top mass
  - Perform a combined log likelihood fit to the distribution of the estimator in data and extract the top quark mass
- 
- The measured mass is the one defined in the MC generator
  - Its exact theoretical definition is not yet defined
    - expected to be close to the pole mass (within about 1 GeV)

# Dilepton channel at 8 TeV

[arXiv:1606.02179](https://arxiv.org/abs/1606.02179)



- Low branching ratio  $\sim 4\%$ , very clean: background  $< 1\%$
- Select events where both  $W$ 's decay leptonical ( $e\nu$  or  $\mu\nu$ )
  - Underconstrained final state due to 2 neutrinos
- Partially reconstruct final state and use invariant mass of lepton-b-jet pairs ( $m_{lb}$ ) as top quark mass dependent estimator



$$m_{\text{top}} = 172.99 \pm 0.41 \text{ (stat)} \pm 0.74 \text{ (syst)} \text{ GeV}$$

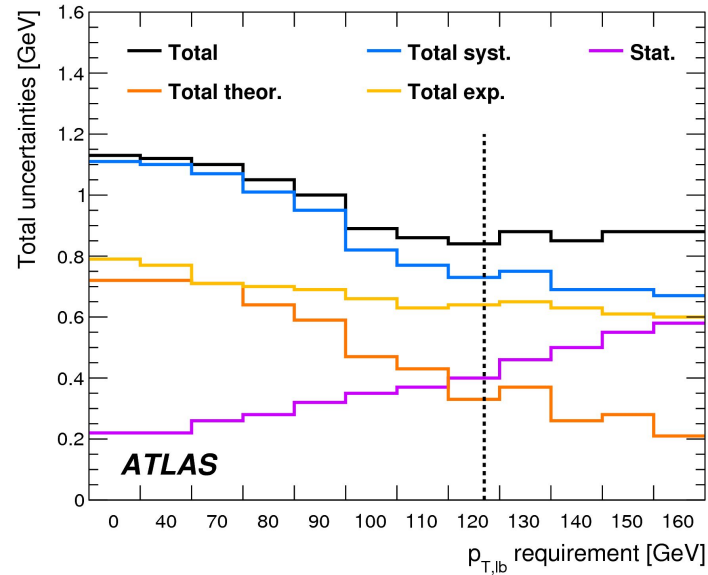
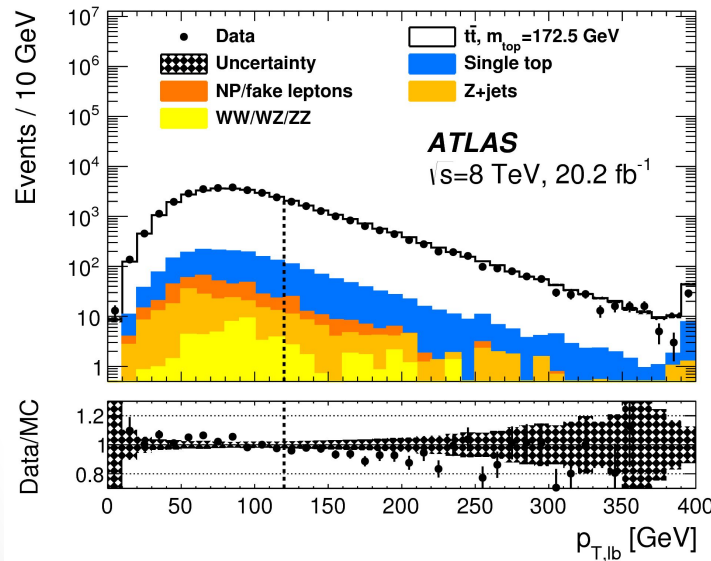
Total Uncertainty:  
 $\pm 0.84 \text{ GeV (0.48\%)}$

- Also measured at  $E_{\text{cm}} = 7 \text{ TeV}$ : [Eur. Phys. J. C \(2015\) 75:330](https://arxiv.org/abs/1508.00011)

# Dilepton channel at 8 TeV



- Optimization of systematic (and statistical) uncertainties
- An additional cut on a minimal average  $p_{T,lb}$  of the two lepton–b-jet pairs
  - increases the fraction of correctly reconstructed top quark pairs
  - reduces the number of unmatched or wrongly reconstructed pairs
- A cleaner event reconstruction leads to reduced systematic uncertainties
  - Minimize total uncertainty by scanning the  $p_{T,lb}$  cut

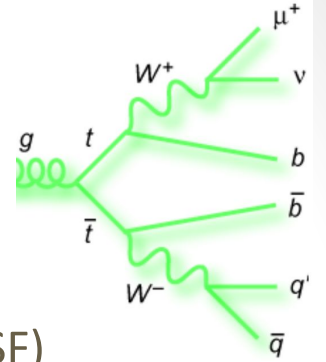


- Most precise measurement in the dilepton channel to date
- Largest uncertainties from (b-)jet energy scales
  - 0.54 and 0.30 GeV

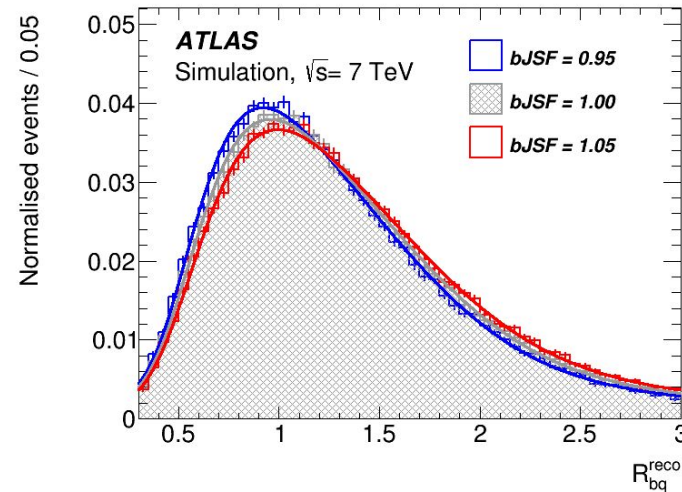
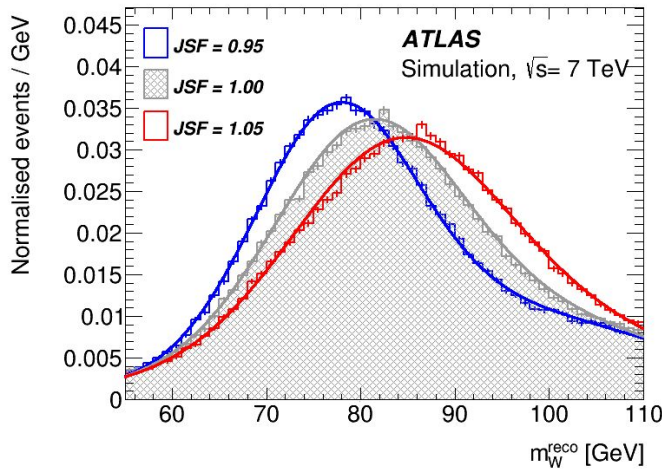


# Lepton + jets channel at 7 TeV [Eur. Phys. J. C \(2015\) 75:330](#)

- Branching ratio  $\sim 30\%$ , clean with background  $O(\text{few } \%)$
- Select events where one  $W$  decays leptonically ( $e\nu$  or  $\mu\nu$ )
- Fully reconstruct final state and apply a 3D template method with  $m_{\text{top}}$ ,  $m_W$  and  $R_{bq}$  as estimators
- In addition to top quark mass, determine a (b-)jet scale factor (JSF)
  - decreases (b-)jet energy scale systematic uncertainties
  - $m_W$  is sensitive estimator to determine JSF
  - The “b to light jet ratio”  $R_{bq}$  is used for bJSF



$$R_{bq}^{\text{reco}} = \frac{\sum p_T^{\text{b-tagged jets}}}{\sum p_T^{\text{untagged jets}}}$$



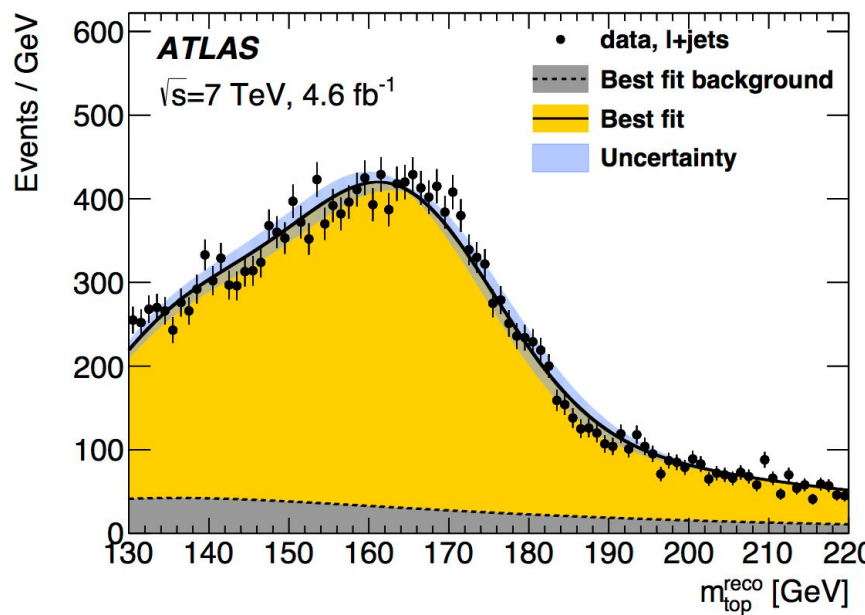
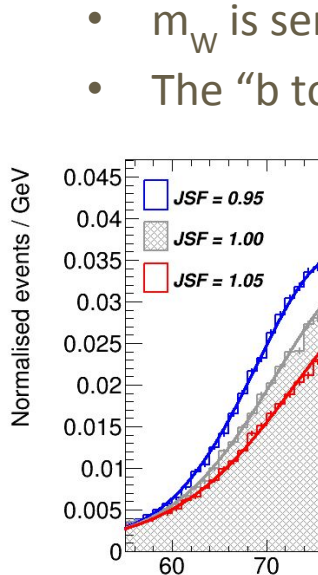
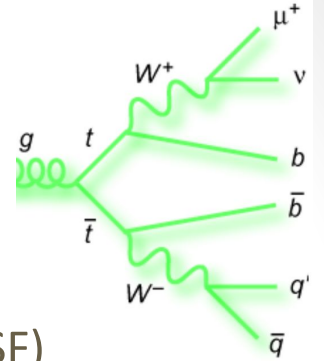
$$m_{\text{top}}^{\ell+\text{jets}} = 172.33 \pm 0.75 (\text{stat} + \text{JSF} + \text{bJSF}) \pm 1.02 (\text{syst}) \text{ GeV}$$

Total Uncertainty:  
 $\pm 1.26 \text{ GeV} (0.73\%)$

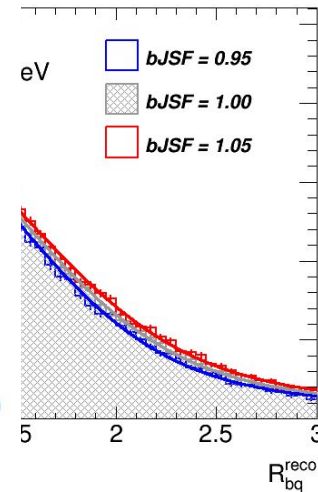
- Uncertainties from (b-)jet energy scales: 0.58 and 0.06 GeV

# Lepton + jets channel at 7 TeV [Eur. Phys. J. C \(2015\) 75:330](#)

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- Select events where one  $W$  decays leptonically ( $e\nu$  or  $\mu\nu$ )
- Fully reconstruct final state and apply a 3D template method with  $m_{\text{top}}$ ,  $m_W$  and  $R_{\text{bq}}$  as top quark mass dependent estimators
- In addition to top quark mass, determine a (b-)jet scale factor (JSF)
  - decreases (b-)jet energy scale systematic uncertainties



$$\frac{\sum p_T^{\text{b-tagged jets}}}{\sum p_T^{\text{untagged jets}}}$$



$$m_{\text{top}}^{\ell+\text{jets}} = 172.33 \pm 0.75 (\text{stat} + \text{JSF} + \text{bJSF}) \pm 1.02 (\text{syst}) \text{ GeV}$$

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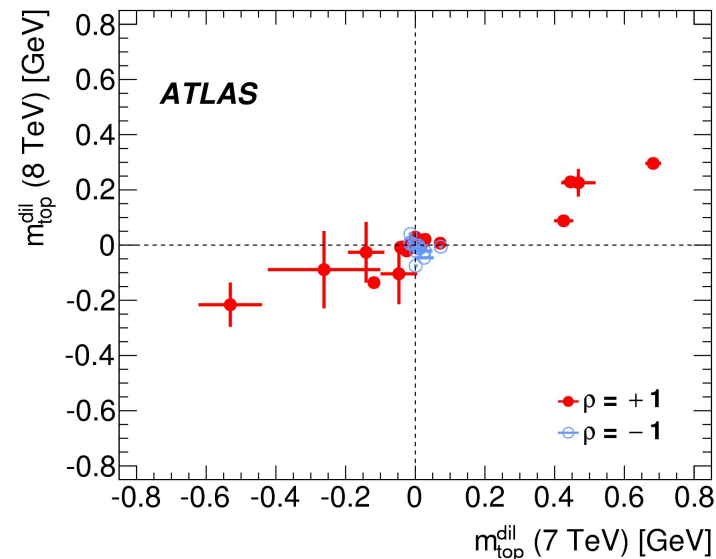
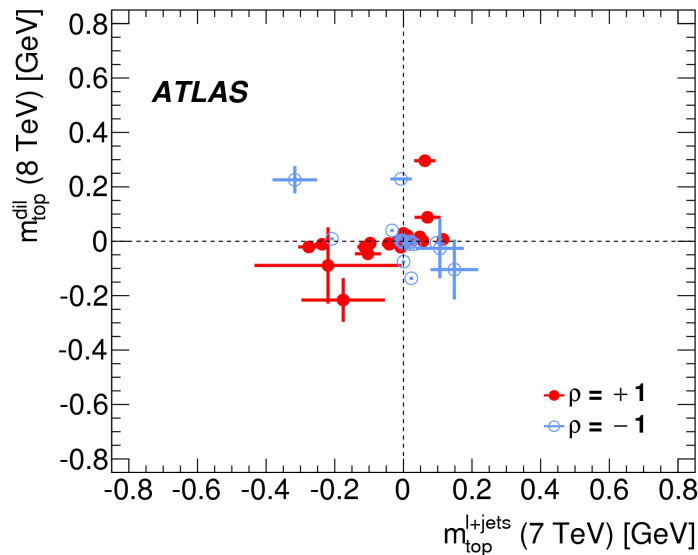
- Uncertainties from (b-)jet energy scales: 0.58 and 0.06 GeV

# Combination 2016

[arXiv:1606.02179](https://arxiv.org/abs/1606.02179)



- Top quark mass measurements in the dilepton channel at  $E_{\text{cm}} = 7\text{-}8\text{ TeV}$  and the lepton+jets channel at  $E_{\text{cm}} = 7\text{ TeV}$  have been combined
- Combination is performed using the “Best Linear Unbiased Estimate” (BLUE) method - [webpage](#)



- The uncertainty components determine the corresponding correlation between the impact on the measurements ( $\pm 1$ )
- Dilepton and lepton + jets analyses use different methods
  - this leads to smaller correlations compared to dilepton at  $E_{\text{cm}} = 7$  and 8 TeV which use identical methods



# Combination 2016

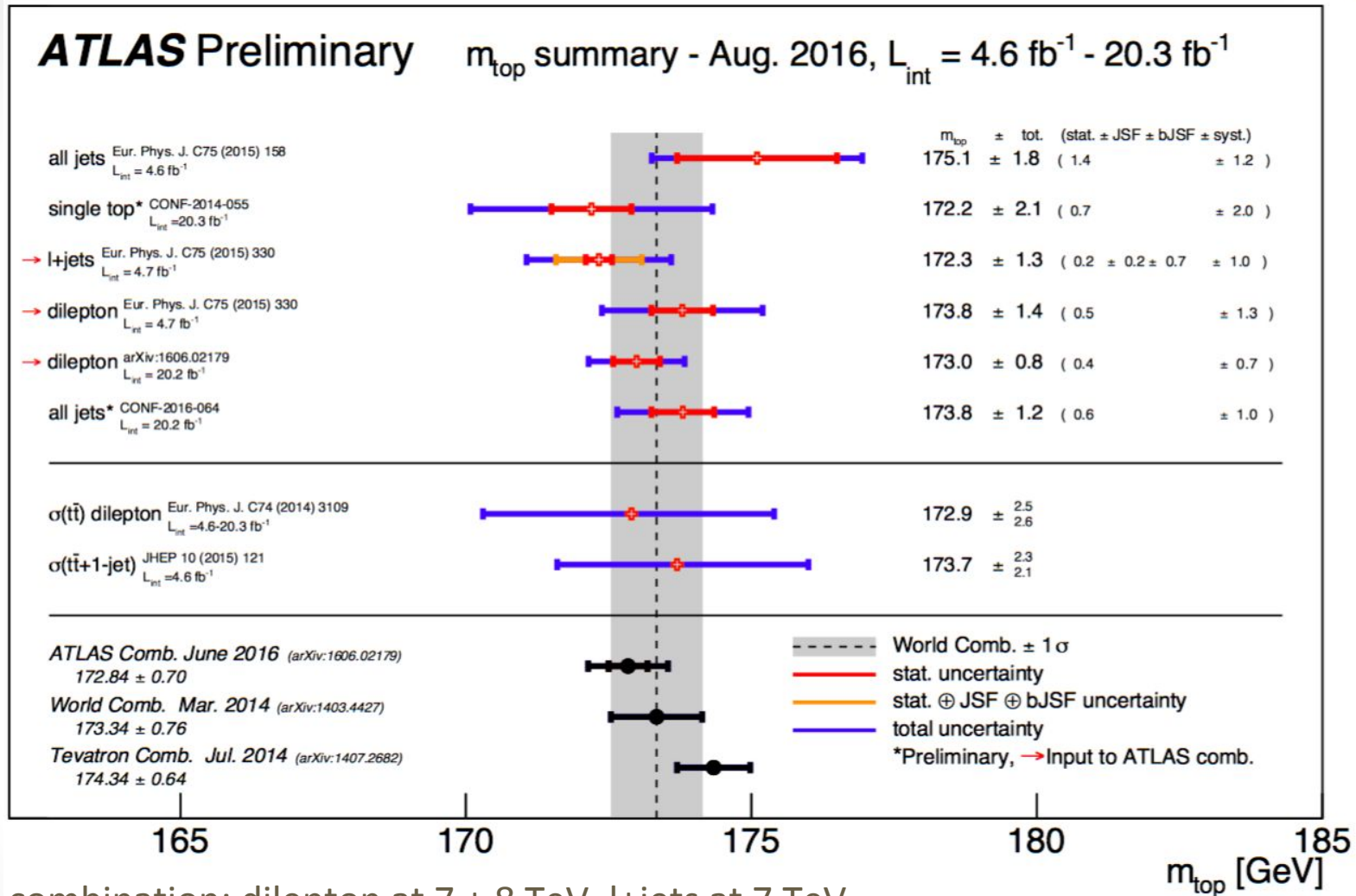


- Table shows the **single input measurements**, the **determined correlations per uncertainty component** and the **result of the respective combinations**
- Combinations:**
  - dilepton and lepton+jets at 7 TeV; dilepton at 7 and 8 TeV; all

	$\sqrt{s} = 7 \text{ TeV}$		$\sqrt{s} = 8 \text{ TeV}$	Correlations			Combinations		
	$m_{\text{top}}^{\ell+\text{jets}}$ [GeV]	$m_{\text{top}}^{\text{dil}}$ [GeV]	$m_{\text{top}}^{\text{dil}}$ [GeV]	$\rho_{01}$	$\rho_{02}$	$\rho_{12}$	$m_{\text{top}}^{7 \text{ TeV}}$ [GeV]	$m_{\text{top}}^{\text{dil}}$ [GeV]	$m_{\text{top}}^{\text{all}}$ [GeV]
Results	172.33	173.79	172.99				172.99	173.04	172.84
Statistics	0.75	0.54	0.41	0	0	0	0.48	0.38	0.34
Method	$0.11 \pm 0.10$	$0.09 \pm 0.07$	$0.05 \pm 0.07$	0	0	0	0.07	0.05	0.05
Signal Monte Carlo generator	$0.22 \pm 0.21$	$0.26 \pm 0.16$	$0.09 \pm 0.14$	+1.00	+1.00	+1.00	0.24	0.10	0.14
Hadronisation	$0.18 \pm 0.12$	$0.53 \pm 0.09$	$0.22 \pm 0.08$	+1.00	+1.00	+1.00	0.34	0.24	0.23
Initial- and final-state QCD radiation	$0.32 \pm 0.06$	$0.47 \pm 0.05$	$0.23 \pm 0.05$	-1.00	-1.00	+1.00	0.04	0.24	0.08
Underlying event	$0.15 \pm 0.07$	$0.05 \pm 0.05$	$0.10 \pm 0.11$	-1.00	-1.00	+1.00	0.06	0.10	0.02
Colour reconnection	$0.11 \pm 0.07$	$0.14 \pm 0.05$	$0.03 \pm 0.11$	-1.00	-1.00	+1.00	0.01	0.03	0.01
Parton distribution function	$0.25 \pm 0.00$	$0.11 \pm 0.00$	$0.05 \pm 0.00$	+0.57	-0.29	+0.03	0.17	0.04	0.08
Background normalisation	$0.10 \pm 0.00$	$0.04 \pm 0.00$	$0.03 \pm 0.00$	+1.00	+0.23	+0.23	0.07	0.03	0.04
$W/Z$ +jets shape	$0.29 \pm 0.00$	$0.00 \pm 0.00$	0	0			0.16	0.00	0.09
Fake leptons shape	$0.05 \pm 0.00$	$0.01 \pm 0.00$	$0.08 \pm 0.00$	+0.23	+0.20	-0.08	0.03	0.07	0.05
Jet energy scale	$0.58 \pm 0.11$	$0.75 \pm 0.08$	$0.54 \pm 0.04$	-0.23	+0.06	+0.35	0.41	0.52	0.41
Relative $b$ -to-light-jet energy scale	$0.06 \pm 0.03$	$0.68 \pm 0.02$	$0.30 \pm 0.01$	+1.00	+1.00	+1.00	0.34	0.32	0.25
Jet energy resolution	$0.22 \pm 0.11$	$0.19 \pm 0.04$	$0.09 \pm 0.03$	-1.00	0	0	0.03	0.08	0.08
Jet reconstruction efficiency	$0.12 \pm 0.00$	$0.07 \pm 0.00$	$0.01 \pm 0.00$	+1.00	+1.00	+1.00	0.10	0.01	0.04
Jet vertex fraction	$0.01 \pm 0.00$	$0.00 \pm 0.00$	$0.02 \pm 0.00$	-1.00	+1.00	-1.00	0.00	0.02	0.02
$b$ -tagging	$0.50 \pm 0.00$	$0.07 \pm 0.00$	$0.03 \pm 0.02$	-0.77	0	0	0.25	0.03	0.15
Leptons	$0.04 \pm 0.00$	$0.13 \pm 0.00$	$0.14 \pm 0.00$	-0.34	-0.52	+0.96	0.05	0.14	0.09
$E_{\text{T}}^{\text{miss}}$	$0.15 \pm 0.04$	$0.04 \pm 0.03$	$0.01 \pm 0.01$	-0.15	+0.25	-0.24	0.08	0.01	0.05
Pile-up	$0.02 \pm 0.01$	$0.01 \pm 0.00$	$0.05 \pm 0.01$	0	0	0	0.01	0.05	0.03
Total systematic uncertainty	$1.03 \pm 0.31$	$1.31 \pm 0.23$	$0.74 \pm 0.25$				0.77	0.74	0.61
Total	$1.27 \pm 0.33$	$1.41 \pm 0.24$	$0.84 \pm 0.25$	-0.07	0.00	0.51	0.91	0.84	0.70

combination: successive reduction of total uncertainty

# Combination - Summary



New combination: dilepton at 7 + 8 TeV, l+jets at 7 TeV

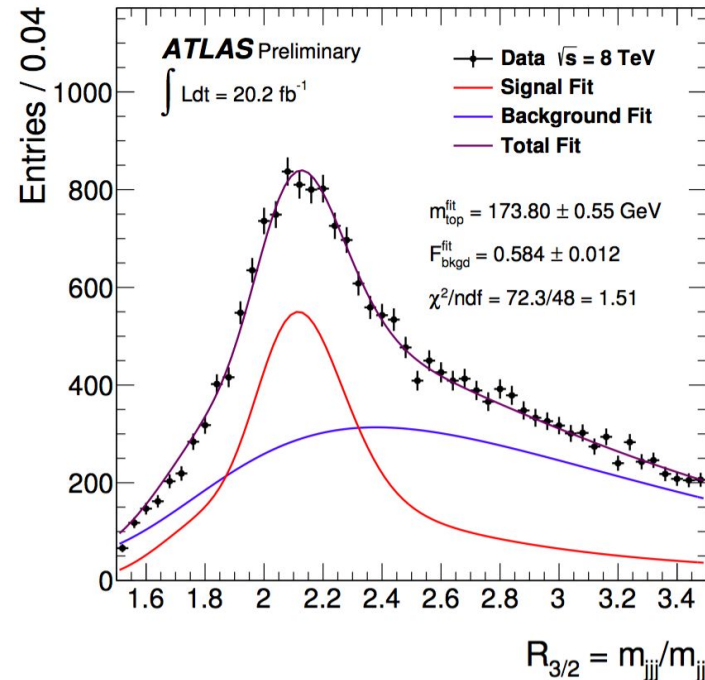
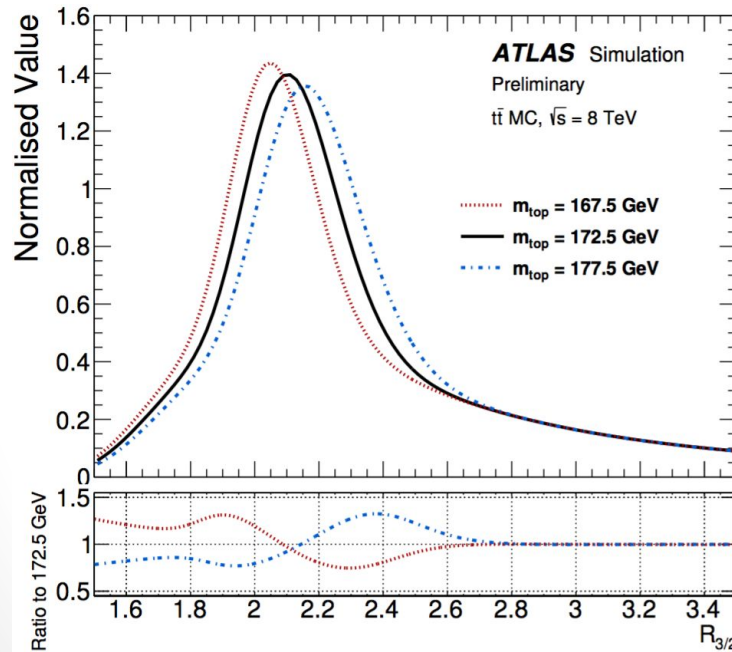
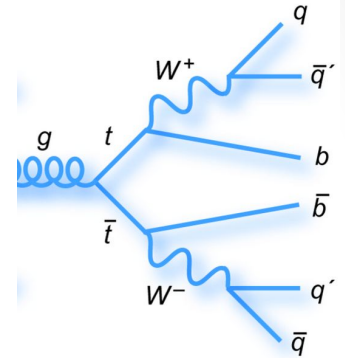
$$m_{\text{top}} = 172.84 \pm 0.34 \text{ (stat)} \pm 0.61 \text{ (syst)} \text{ GeV}$$

Total Uncertainty:  
 $\pm 0.70 \text{ GeV (0.40\%)}$

# All hadronic channel at 8 TeV



- High branching ratio 46%, very large QCD initiated background: ~50%
  - Large background is estimated from data (ABCD method)
- Select events where both W's decay hadronically
  - The final state can be fully reconstructed
- Use  $R_{3/2} = m_{jjj}/m_{jj}$  as top quark mass dependent estimator
  - ratio reduces dependence on jet energy calibration



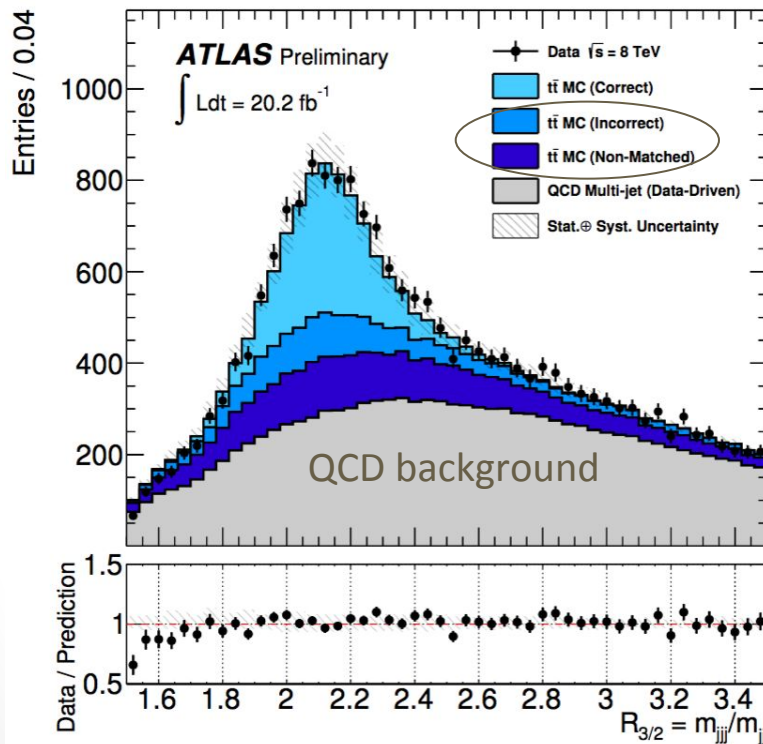
$$m_{top} = 173.80 \pm 0.55 \text{ (stat.)} \pm 1.01 \text{ (syst.) GeV}$$

Total Uncertainty:  
 $\pm 1.15 \text{ GeV (0.7\%)}$

# All hadronic channel at 8 TeV



- Six jets in final state → combinatorial bkg. due to wrong jet parton assignment
  - Reduce combinatorial background by computing  $m_{jj}$  and  $m_{jjj}$  for all permutations and minimising a  $\chi^2$  function



Uncertainty	$\Delta m_{top}$ [ GeV]
Monte Carlo Generator	$0.18 \pm 0.21$
Hadronisation Modelling	$0.64 \pm 0.15$
Parton Distribution Functions	$0.04 \pm 0.00$
Initial/Final-State Radiation	$0.10 \pm 0.28$
Underlying Event	$0.13 \pm 0.16$
Colour Reconnection	$0.12 \pm 0.16$
Template Method Non-Closure	0.06
Signal and Bkgd Parameterisation	0.09
Non All-Hadronic $t\bar{t}$ Contribution	0.06
ABCD vs. ABCDEF	0.16
Trigger Efficiency	$0.08 \pm 0.01$
Pile-Up Reweighting	$0.01 \pm 0.00$
Lepton/ $E_T^{\text{miss}}$ Calibration	$0.02 \pm 0.01$
Overall Flavour Tagging	$0.10 \pm 0.00$
Jet Energy Scale (JES)	$0.60 \pm 0.05$
b-Jet Energy Scale (bJES)	$0.34 \pm 0.02$
Jet Energy Resolution	$0.10 \pm 0.04$
Jet Vertex Fraction	$0.03 \pm 0.01$
Jet Reconstruction Efficiency	$0.00 \pm 0.00$
<b>Total Systematic</b>	<b>1.01</b>
<b>Total Statistical</b>	<b>0.55</b>
<b>Total</b>	<b>1.15</b>

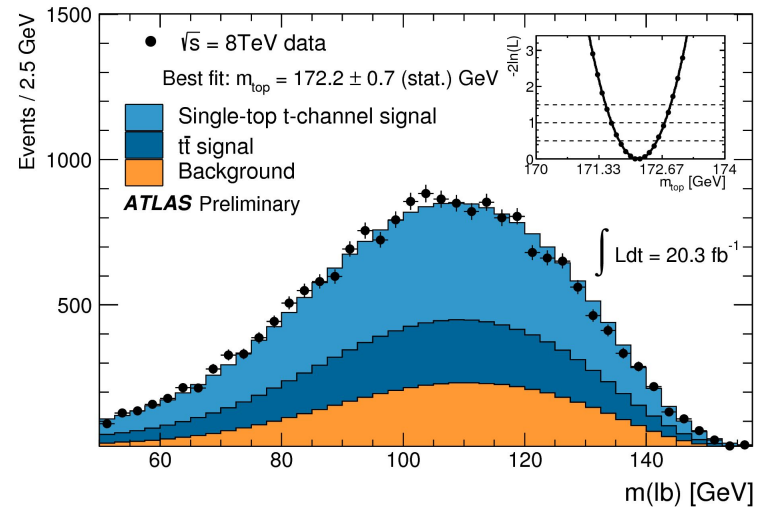
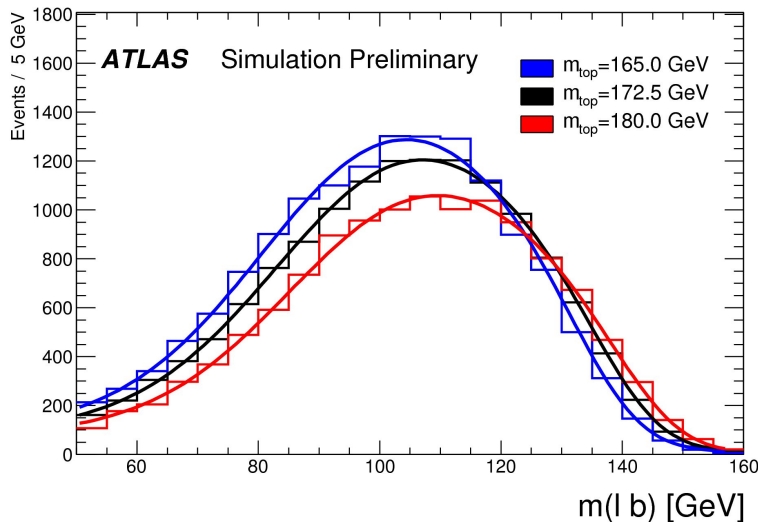
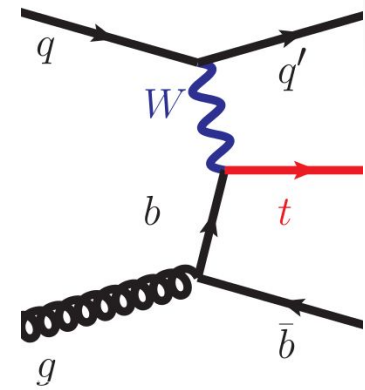
- Largest uncertainties due to jet energy scale and hadronisation



# Single Top t-channel at 8 TeV

ATLAS-CONF-2014-055

- Use single top t-channel to measure top quark mass
- Select events where W decays leptonically ( $e\nu$  or  $\mu\nu$ )
- Main background from top pair production and W + jets
  - Reduce background to <30% by use of neural network
- Use invariant mass of lepton b-jet system as estimator
- Largest uncertainty from
  - jet energy calibration: 1.5 GeV, hadronisation: 0.7 GeV



$$m_{\text{top}} = 172.2 \pm 0.7 (\text{stat.}) \pm 2.0 (\text{syst.}) \text{ GeV}$$

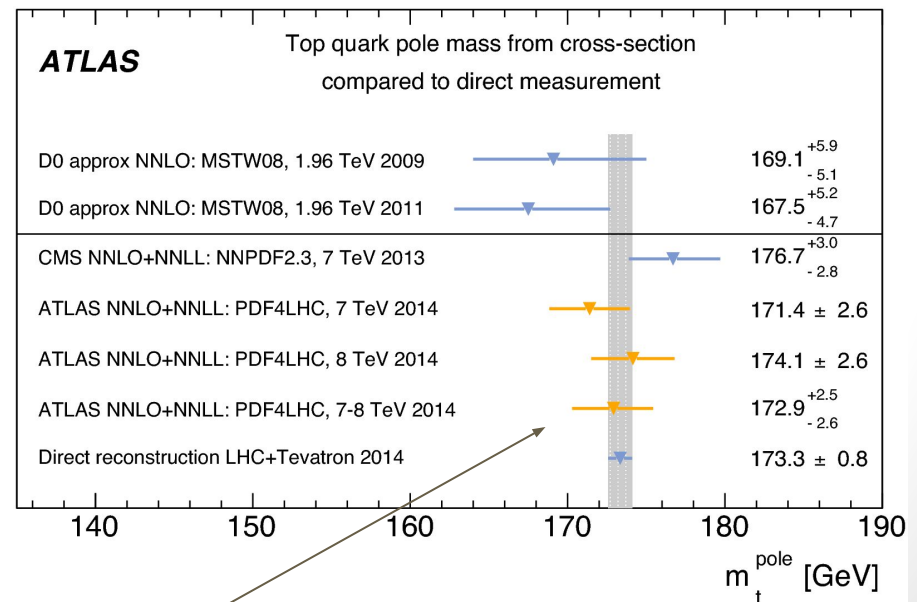
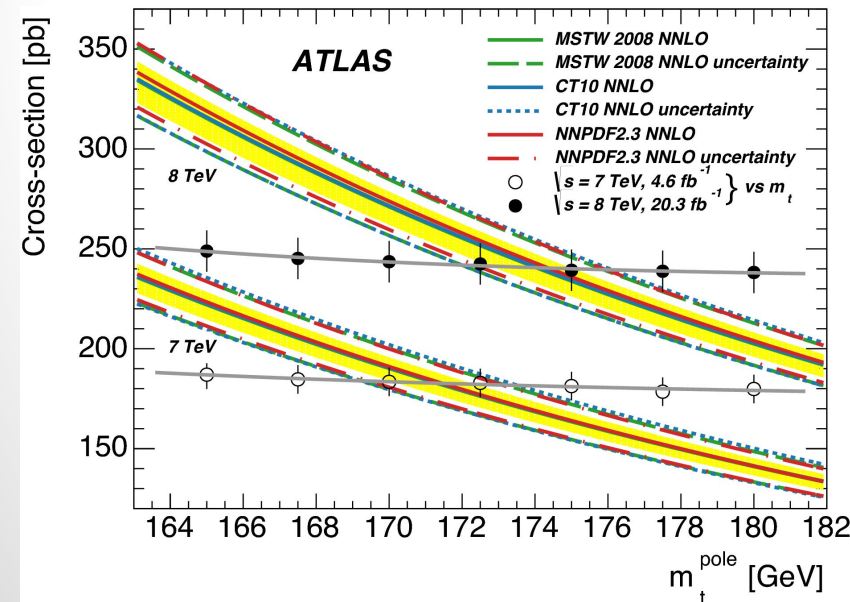
Total Uncertainty:  
 $\pm 2.12 \text{ GeV (1.2\%)}$



# Top Quark Pole Mass via Cross Section

- The top quark pair production cross section depends on the top quark pole mass:  $\sigma_{tt}(m_{t,\text{pole}})$ 
  - measure the cross section and extract the mass
- $\sigma$  is measured in dilepton final state with opposite-charge  $e\mu$  pairs
- Largest systematic uncertainties due to
  - particle distribution function: 1.7 GeV
    - baseline PDF is CT10, with PDF4LHC approach to derive systematic unc.
    - uncertainty could be reduced by using more recent PDF sets
  - uncertainty on integrated luminosity itself: 1.8% (2.8%) at  $E_{\text{cm}} = 7$  (8) TeV
    - leads to 0.7 (1.2) GeV uncertainty on  $m_{\text{top}}$  at  $E_{\text{cm}} = 7$  (8) TeV

[Eur.Phys.J. C74 \(2014\) 3109](#)



error bars include statistical and systematic errors

# Top Quark Pole Mass - tt + 1 jet

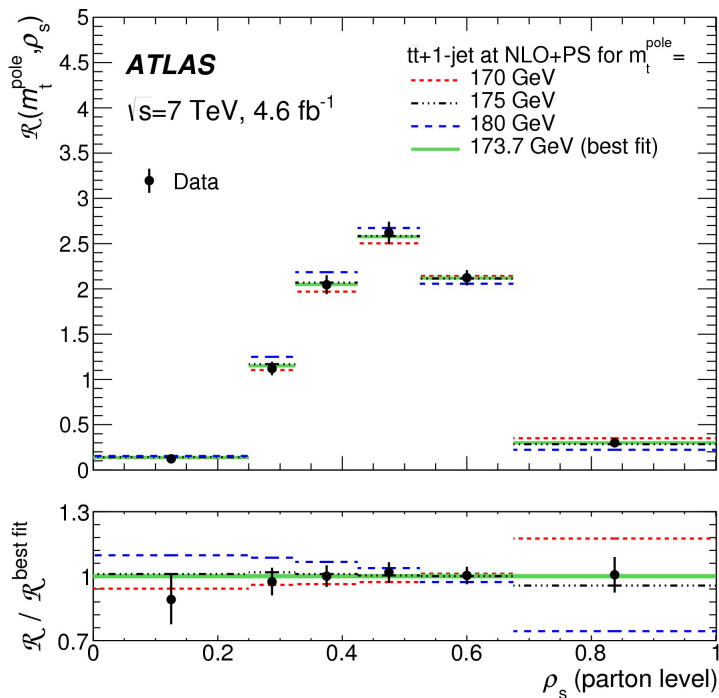
[JHEP 10 \(2015\) 121](#)

- Select top quark pair events in the lepton + jets channel
- Study events of top quark pairs with at least one additional jet
- Normalized differential cross section of tt + 1 jet system

$$\mathcal{R}(m_t^{\text{pole}}, \rho_s) = \frac{1}{\sigma_{t\bar{t}+1\text{-jet}}} \frac{d\sigma_{t\bar{t}+1\text{-jet}}}{d\rho_s}(m_t^{\text{pole}}, \rho_s)$$

$$\rho_s = \frac{2m_0}{\sqrt{s_{t\bar{t}+1\text{-jet}}}}$$

- is sensitive to top quark pole mass



Largest uncertainties from

Statistical: 1.50 GeV

Jet energy scale: 0.96 GeV

Theory (scale variation, PDF): 0.5 - 1.0 GeV

$$m_t^{\text{pole}} = 173.7 \pm 1.5 \text{ (stat.)} \pm 1.4 \text{ (syst.)}_{-0.5}^{+1.0} \text{ (theory) GeV}$$

Total Uncertainty:

$$\pm 2.1 \text{ GeV (2.7\%)}$$

Measurement is

currently

repeated at  $E_{\text{cm}} = 8 \text{ TeV}$

# Summary and Outlook

- The top quark mass is a free parameter of the Standard Model
- Precise measurements of the top quark mass are of great importance for theoretical predictions in conjunction with the Higgs Boson and beyond
- ATLAS has measured the mass at  $E_{\text{cm}} = 8 \text{ TeV}$ 
  - directly in the dilepton and all hadronic top quark pair production channels
  - directly in the single top t-channel
  - indirectly via cross section measurements
- At  $E_{\text{cm}} = 7 \text{ TeV}$ , the top quark mass has been measured in all top quark pair production channels and via cross section measurements
- A few more analyses using Run 1 data are in preparation
- The ATLAS collaboration will continue to perform precise measurements of the top quark mass at  $E_{\text{cm}} = 13 \text{ TeV}$