

` Bridge between Hadrodynamics & HEP' --

Regional CP Asymmetries in Many-Body Final States

Ikaros Bigi (Notre Dame du Lac)

Central points:

- *consistent* parameterization of the CKM matrix
- probe *many-body* final states (FS)
- *connections* between U- vs. V-spin (broken) symmetries
- Penguin *diagrams* vs. Penguin *operators*

crucial:

collaborations of *experimenters* & *theorists* with
judgments

I do *not* give you solutions - I `paint' the progress

We are *not* close to the end of the "road" probing heavy flavor dynamics: we need *much more* than `just' *more data*:

- We have to apply more refined tools & more thinking to make progress.
- There are two different cultures at work between
Hadrodynamics & HEP
- accuracy → precision on different levels
- subtle theoretical tools are `waiting', we have to learn how to apply them
- Quark-hadrons duality - a subtle tool & its limits/violation.
"Duality" is *not* an additional assumption, although often it is `subtle'.

The main points are:

- 3- & 4-body final states of charm & beauty hadrons *not* back-up for information from 2-body ones - the landscapes are very different !
- The best fitted analyses often do *not* give us the best information about the underlying dynamics *i.e., theorists should not be the slaves of the data.* Of course, data are the referees - in the end !

I. Parameterization of CKM Matrix through $O(\lambda^6)$

(A) In smart Wolfenstein parameterization with

$$\lambda \approx 0.225 \text{ with } A, \eta \text{ \& } \rho \sim O(1); A \sim 0.81 = O(1)$$

however:

➤ $\eta \approx 0.34, \rho \approx 0.13 \ll O(1)$

➤ $V_{CKM,Wolf} = \dots + O(\lambda^{4,5,6})$

(B) Needs *consistent* parameteriz. of CKM matrix with more precision! Y.H. Ahn, H-Y. Cheng, S. Oh (2011)

-- $V_{CKM} = \dots + O(\lambda^7)$

-- basically zero CP asymmetries in DCS decays of charm hadrons

-- the *maximal* value of $\sin\phi_1 \sim 0.74$ in the SM

-- correlations etc.

II. Re-scattering & Impact of CPT Invariance

The goal is: measuring CP asymmetries probes existence & even features of **New Dynamics (ND)**, since they can depend only on an amplitude.

$$T(P \rightarrow a) = \exp(i\delta_a) \left[T_a + \sum_{aj \neq a} T_{aj} i T_{aj,a}^{\text{resc}} \right]$$

$$T(P \rightarrow a) = \exp(i\delta_a) \left[T_a^* + \sum_{aj \neq a} T_{aj}^* i T_{aj,a}^{\text{resc}} \right]$$

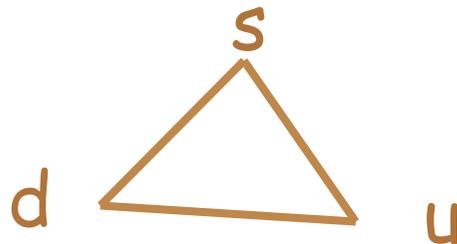
$$\Delta\gamma(a) = |T(P \rightarrow a)|^2 - |T(P \rightarrow a)|^2 = 4 \sum_{aj \neq a} T_{aj,a}^{\text{resc}} \text{Im} T_a^* T_{aj}$$

Without re-scattering direct CP asymmetries cannot happen, even if there are weak phases.

Shifman & Voloshin & collab.; Wolfenstein

(II.1) Connections between U- vs. V-spin symmetries

U- vs. V-spin symmetries were introduced to describe *spectroscopies* of hadrons as subgroups of global SU(3) (by Lipkin ...),
before quarks were seen as real physical states.



The situation changes much with *weak* transition

Lipkin suggested based on U-spin symmetry:

$$\Delta = A_{CP}(B_d \rightarrow K^+\pi^-) / A_{CP}(B_s \rightarrow K^+\pi^-) + BR(B_s \rightarrow K^-\pi^+) / BR(B_d \rightarrow K^+\pi^-) (\tau_d / \tau_s) = 0$$

LHCb, PRL 110 (2013) 221601:

$$A_{CP}(B_s \rightarrow K^-\pi^+) = 0.27 \pm 0.04 \pm 0.01, \quad A_{CP}(B_d \rightarrow K^+\pi^-) = -0.080 \pm 0.007 \pm 0.03$$

$$\Delta_{LHCb} = -0.02 \pm 0.05 \pm 0.04$$

“These results allow a *stringent* test of the validity of the ...”

to get opposite signs in the SM is obvious

? Your job was done by probing *2-body* FS ?

I disagree with two important reasons in different dimensions!

(a) $\Delta_{LHCb} = -0.02 \pm 0.05 \pm 0.04$

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(b) $A_{CP}(B_s \rightarrow K_S K^+ K^-)$? $A_{CP}(B_d \rightarrow K_S K^+ K^-)$? $A_{CP}(B^+ \rightarrow K^+\pi^+\pi^- / K^+ K^+ K^-)$?

$A_{CP}(B_s \rightarrow K^+\pi^-\pi^+\pi^- / K^+ K^- K^+\pi^-)$? $A_{CP}(B_d \rightarrow K^-\pi^+\pi^-\pi^+ / K^- K^+ K^-\pi^+)$? etc.

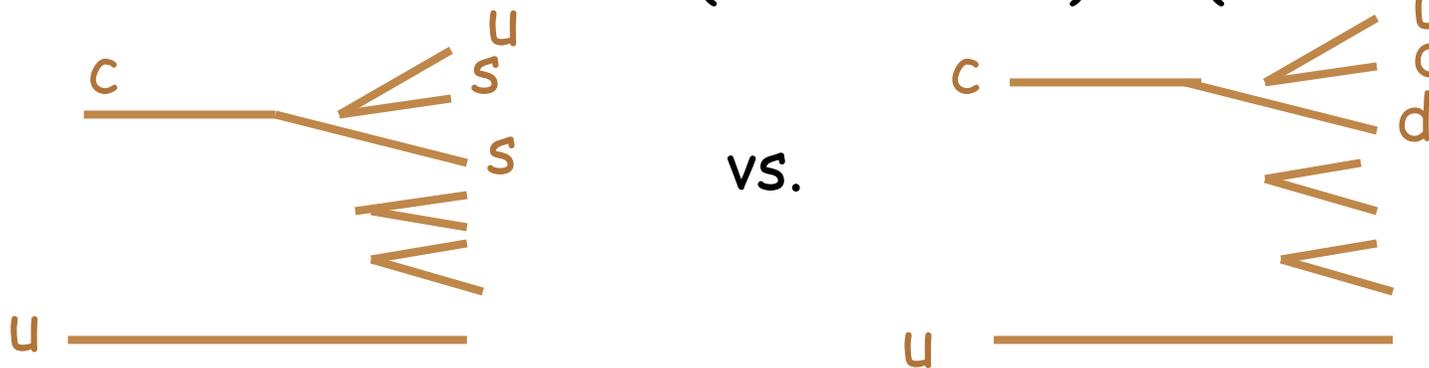
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Well-known examples:

-- $BR(D^0 \rightarrow K^+ K^-) / BR(D^0 \rightarrow \pi^+ \pi^-) \sim 3$



-- on the other hand: $BR(D^0 \rightarrow K^+ K^- \pi^+ \pi^-) / BR(D^0 \rightarrow 2\pi^+ 2\pi^-) \sim 1/3$

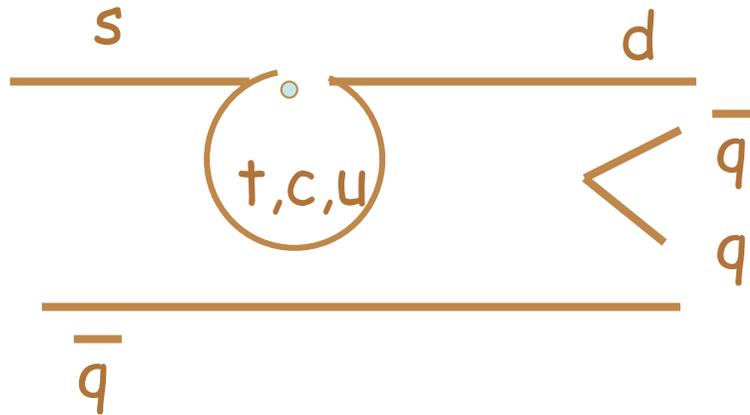


-- next: $BR(D^0 \rightarrow K^+ K^- / K^+ K^- \pi^+ \pi^-) / BR(D^0 \rightarrow \pi^+ \pi^- / 2\pi^+ 2\pi^-) \sim 0.8$

-- impact of many-body FS

(II.2) Impact of Penguin diagrams on CPV?

- the impact of 'penguin' was an important pioneering work of Shifman, Vainshtein, Zakharow 1975; it is based on *local* operators for kaons with mostly two-body FS

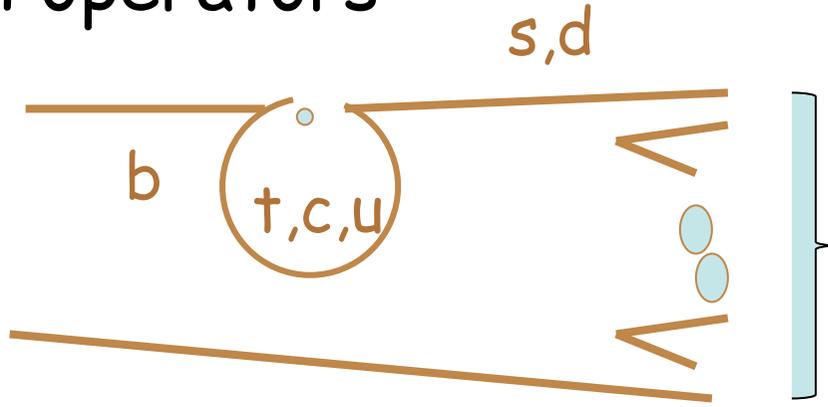


- explain $\Delta I=1/2 \gg \Delta I=3/2$ & direct CPV ε'/ε in $\Delta S=1$ (semi-)quantitatively

- easy part !

ibi: "Mature ND"

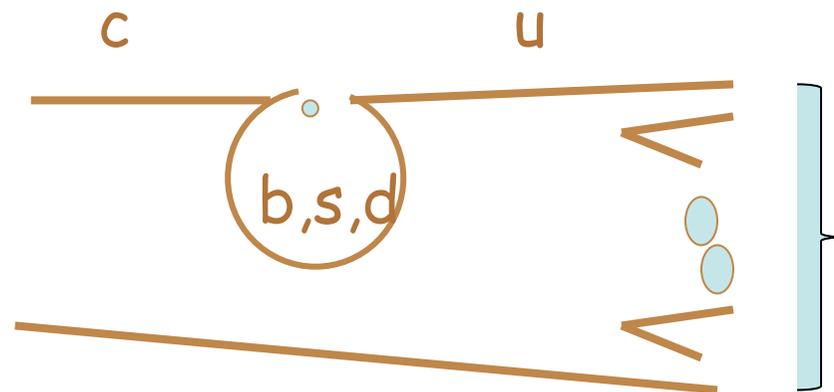
-- Penguin diagrams are fine for suppressed **B decays** about **inclusive** CPV with **hard** FSI to describe with local operators



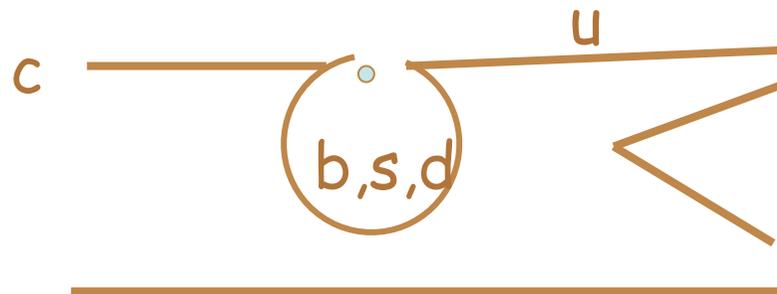
However, *not* about **exclusive** rates & **soft** FSI with hadrons in a **quantitative** way!

In special situations we can use other tools like HQE, LQCD, chiral symmetry, dispersion relations etc. etc.

-- one can draw Penguin diagrams for SCS transitions:



but one can hardly describe D decays (semi-)quantitatively for **inclusive** CPV with local operators, even less about **exclusive** rates & **soft** FSI with hadrons!



` We' have little control over the impact of penguin diagrams in 2-body FS for $\Delta C \neq 0 \neq \Delta B$.

III. 3- & 4-Body FS of CP Asymmetries in B & D

Probing final states with 2 hadrons (including narrow resonances) is not trivial to measure CPV; on the other hand one gets `just' numbers. However 3- & 4-body FS are described in general by two-& more dimensional plots.

☹ Price:

lots of work both for experimenters & theorists

☺ Prize:

find *existence & features* of New Dynamics (ND)!

(III.1) $B^{+/-} \rightarrow K^{+/-}\pi^+\pi^-$ vs. $B^{+/-} \rightarrow K^{+/-}K^+K^-$

Data about rates:

$$\text{BR}(B^+ \rightarrow K^+\pi^+\pi^-) = (5.10 \pm 0.29) \times 10^{-5};$$

$$\text{BR}(B^+ \rightarrow K^+K^+K^-) = (3.37 \pm 0.22) \times 10^{-5};$$

not surprising at all

averaged CP asymmetries for direct ones

$$\Delta A_{CP}(B^+ \rightarrow K^+\pi^+\pi^-) = + 0.032 \pm 0.008 \pm 0.004 \pm 0.007;$$

$$\Delta A_{CP}(B^+ \rightarrow K^+K^+K^-) = - 0.043 \pm 0.009 \pm 0.003 \pm 0.007;$$

it is okay

regional CP asymmetries

$$\Delta A_{CP}(B^+ \rightarrow K^+\pi^+\pi^-)|_{\text{regional}} = + 0.678 \pm 0.078 \pm 0.032 \pm 0.007;$$

$$\Delta A_{CP}(B^+ \rightarrow K^+K^+K^-)|_{\text{regional}} = - 0.226 \pm 0.020 \pm 0.004 \pm 0.007;$$

Very surprising to me due to two connected points:

- the centers of the Dalitz plots are mostly empty
- the differences are so huge!

(III.2) $B^{+/-} \rightarrow \pi^{+/-}\pi^+\pi^-$ vs. $B^{+/-} \rightarrow \pi^{+/-}K^+K^-$

Data about rates:

$$BR(B^+ \rightarrow \pi^+\pi^+\pi^-) = (1.52 \pm 0.14) \times 10^{-5};$$

$$BR(B^+ \rightarrow \pi^+K^+K^-) = (0.50 \pm 0.07) \times 10^{-5};$$

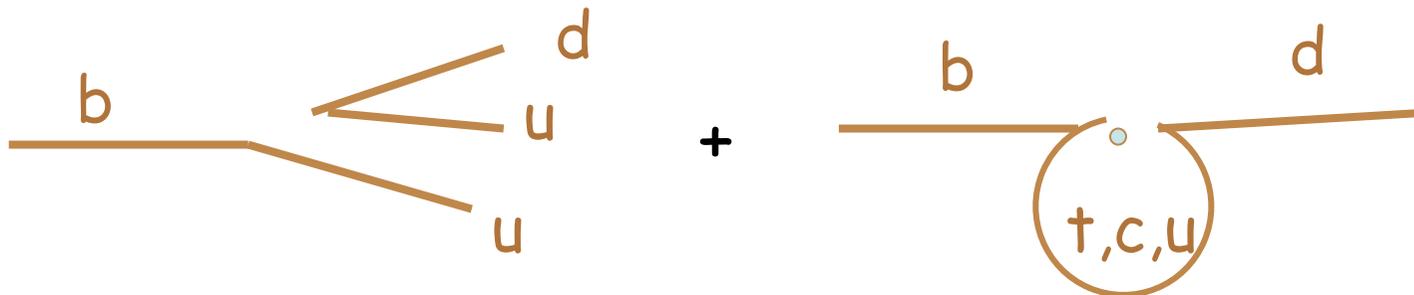
not surprising

averaged CP asymmetries

$$\Delta A_{CP}(B^+ \rightarrow \pi^+\pi^+\pi^-) = + 0.117 \pm 0.021 \pm 0.009 \pm 0.007;$$

$$\Delta A_{CP}(B^+ \rightarrow \pi^+K^+K^-) = - 0.141 \pm 0.040 \pm 0.018 \pm 0.007;$$

surprising: impact of more suppressed penguin diagrams?



(III.2) $B^{+/-} \rightarrow \pi^{+/-}\pi^+\pi^-$ vs. $B^{+/-} \rightarrow \pi^{+/-}K^+K^-$

Data about rates:

$$\text{BR}(B^+ \rightarrow \pi^+\pi^+\pi^-) = (1.52 \pm 0.14) \times 10^{-5};$$

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not surprising

averaged CP asymmetries

$$\Delta A_{\text{CP}}(B^+ \rightarrow \pi^+\pi^+\pi^-) = + 0.117 \pm 0.021 \pm 0.009 \pm 0.007;$$

$$\Delta A_{\text{CP}}(B^+ \rightarrow \pi^+K^+K^-) = - 0.141 \pm 0.040 \pm 0.018 \pm 0.007;$$

surprising: impact of more suppressed penguin diagrams?

regional CP asymmetries

$$\Delta A_{\text{CP}}(B^+ \rightarrow \pi^+\pi^+\pi^-)|_{\text{regional}} = + 0.584 \pm 0.082 \pm 0.027 \pm 0.007;$$

$$\Delta A_{\text{CP}}(B^+ \rightarrow \pi^+K^+K^-)|_{\text{regional}} = - 0.648 \pm 0.070 \pm 0.013 \pm 0.007;$$

Very surprising for me due to two connected points:

- the centers of the Dalitz plots are mostly empty
- the differences are so huge!

(III.4) Outside CPV: $|V_{ub}|_{incl.}$ vs. $|V_{ub}|_{excl.}$

I mention $|V_{ub}|_{incl.}$ vs. $|V_{ub}|_{excl.}$ in an unusual way:
usually one measures $B \rightarrow l \nu \pi$'s to extract the value of
 $|V_{ub}|_{incl.}$, but *not*
 $B^- \rightarrow l^- \nu K^+ K^-, l^- \nu \overline{K^0} \overline{K^0}, l^- \nu K \overline{K} \pi$
 $B^0_d \rightarrow l^+ \nu K_S K^-, l^- \nu K \overline{K} \pi$
based on the item of "duality"

However, "duality" is often subtle:

Local duality does not work, in particular close to thresholds
(it does not work for $|V_{cb}|_{incl.}$ vs. $|V_{cb}|_{excl.}$)

Real $|V_{ub}|_{incl.}$ might be smaller than thought before due
re-scattering!

Test it!

(III.5) 3-body FS of $D^+_{(s)}$

-- CPT invariance in D (& τ) decays is 'practical', since 'few' channels can be combined.

SCS:

$$D^+ \rightarrow \pi^+\pi^-\pi^+ / \pi^+K^-K^+$$

$$D^0 \rightarrow \pi^+\pi^-\pi^0, K^+K^-\pi^0, K_S K^+\pi^-, K_S K^-\pi^+$$

$$D_s^+ \rightarrow K^+\pi^-\pi^+, K^+K^-K^+$$

- no CPV has been found (yet)
- one has to deal with re-scattering; it is not trivial, but crucial; 'paintings diagrams' are not enough.

DCS:

$$D^+ \rightarrow K^+\pi^-\pi^+ / K^+K^-K^+$$

SM ~zero CPV

$$D^0 \rightarrow K^+\pi^-\pi^0 \text{ (the situation with } D^0 \rightarrow K_S \pi^+\pi^-, K_S K^+K^- \text{ is subtle)}$$

$$D_s^+ \rightarrow K^+K^+\pi^-$$

SM ~zero CPV

(III.6) 4-body FS of $D^+_{(s)}$

(III.6.1) General comments

- obviously one first measures T-odd moments of
 $D \rightarrow h_1 h_2 h_3 h_4$ vs. $\overline{D} \rightarrow \overline{h_1} \overline{h_2} \overline{h_3} \overline{h_4}$, namely moments
 $A_T = \langle p_1 \cdot (p_2 \times p_3) \rangle$ and $\overline{A}_T = \langle \overline{p}_1 \cdot (\overline{p}_2 \times \overline{p}_3) \rangle$

FSI can produce $A_T, \overline{A}_T \neq 0$ without CPV - but
 $a_{CPV}^{T\text{-odd}} = (1/2) (A_T - \overline{A}_T)$ establishes CP asymmetry
they give us only numbers

- we cannot stop there, namely to probe
semi-regional CP asymmetries like
- measure the angle ϕ between the planes of $h_1 h_2$ and $h_3 h_4$:
- $$d/d\phi \Gamma(D \rightarrow h_1 h_2 h_3 h_4) = \Gamma_1 \cos^2 \phi + \Gamma_2 \sin^2 \phi + \Gamma_3 \cos \phi \sin \phi$$
- $$d/d\phi \Gamma(\overline{D} \rightarrow \overline{h_1} \overline{h_2} \overline{h_3} \overline{h_4}) = \Gamma_1 \cos^2 \phi + \Gamma_2 \sin^2 \phi - \Gamma_3 \cos \phi \sin \phi$$

(III.6.2) Specific comments *beyond* moments

-- SCS: $D^0 \rightarrow K^+K^-\pi^+\pi^-/2\pi^+2\pi^-$

-- DCS: $D^0 \rightarrow K^+\pi^-\pi^+\pi^-/K^+K^-K^+\pi^-$

-- DCS: $D_s^+ \rightarrow K^+K^+\pi^-\pi^0/K^+K^+\pi^-\eta$

IV. CPV in the decays of charm & beauty baryons

In principle CPV has been found in `our existence';

Back to real world:

- No CPV has been found in the decays of charm & beauty *baryons*!
- It seems there are huge `hunting regions' for LHCb, when one `thinks' about it.

SCS decays:

- CPV in $\Lambda_c^+ \rightarrow \Lambda K^+$; its production rate can be calibrated with $\Lambda_c^+ \rightarrow \Lambda \pi^+$.
- $\Lambda_c^+ \rightarrow p \pi^+ \pi^-, p K^+ K^-$;

DCS decays:

- CPV in $\Lambda_c^+ \rightarrow p K^+ \pi^-$.

CPV in $\Delta B=1$: probe Dalitz plots independent of production

- $\Lambda_b^0 \rightarrow p \pi^-, \Lambda K^+ \pi^-$;
- $\Lambda_b^0 \rightarrow p K^-, \Lambda \pi^+ \pi^-, \Lambda K^+ K^-$;
- $\Lambda_b^0 \rightarrow p \pi^- \pi^+ \pi^-, p \pi^- K^+ K^-$;

V. Summary of Indirect Searching for New Dynamics (ND) in 3- & 4-Body Final States

the goal is to find ND - like a criminal case where you did *not* see two witnesses at the crime.

-- accuracy -> precision !

-- No golden test of flavor dynamics you have to rely on a series of several arguments with *correlations* !

➤ Need detailed analyses of *3- & 4-body final states* including CPV - despite the large start-up work!

-- The best fitted analyses often do *not* give us the best information about the underlying dynamics

i.e., theorists should *not* be the *slaves of the data*

Of course, data are the referees - in the end !

Quote of Marinus

(~468 AD student of Proklos, known Neoplatonist Philosopher):

“ *Only being good is one thing -*

but good doing it is the other one! “

One example of different cultures to get a `team':
“dispersion relations”

“Bridge between Hadrodynamics & HEP”
or
“Lot of Water still Passing under the Bridge”