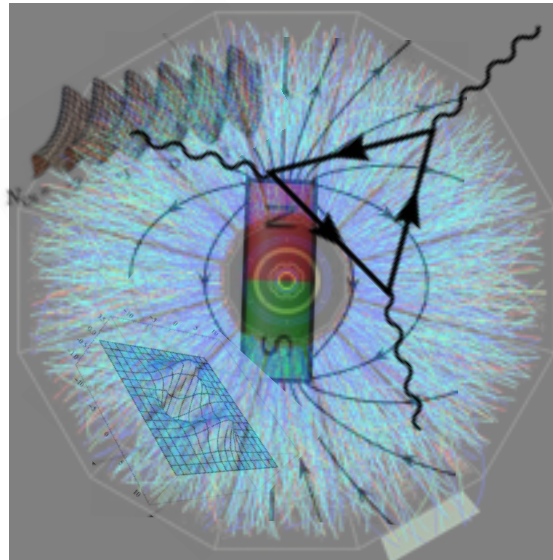


Anomalous Chiral Transport in Heavy Ion Collisions



Jinfeng Liao

Indiana University, Physics Dept. & CEEM

RIKEN BNL Research Center


Research Supported by NSF & DOE



Exciting Progress: See Recent Reviews


Progress in Particle and Nuclear Physics 88 (2016) 1–28

Contents lists available at [ScienceDirect](#)

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Progress in Particle and Nuclear Physics

journal homepage: www.elsevier.com/locate/ppnp




Review

Chiral magnetic and vortical effects in high-energy nuclear collisions—A status report

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^b Department of Physics and RIKEN-BNL Research Center, Brookhaven National Laboratory, Upton, NY 11973-5000, USA
^c Physics Department and Center for Exploration of Energy and Matter, Indiana University, 727 E Third Street, Bloomington, IN 47405, USA
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^e Department of Physics and Astronomy, Wayne State University, 666 W. Hancock, Detroit, MI 48201, USA
^f Department of Physics and Astronomy, University of California, Los Angeles, CA 90095, USA



Prog. Part. Nucl. Phys. 88, 1 (2016) [arXiv:1511.04050 [hep-ph]].

J. Liao, Pramana 84, no. 5, 901 (2015) [arXiv:1401.2500 [hep-ph]].

Chiral Anomaly

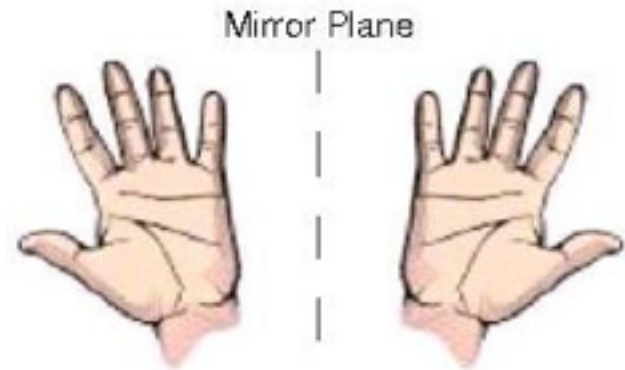
Chiral anomaly is a fundamental aspect of QFT with chiral fermions.

Classical symmetry:

$$\mathcal{L} = i\bar{\Psi}\gamma^\mu\partial_\mu\Psi$$

$$\mathcal{L} \rightarrow i\bar{\Psi}_L\gamma^\mu\partial_\mu\Psi_L + i\bar{\Psi}_R\gamma^\mu\partial_\mu\Psi_R$$

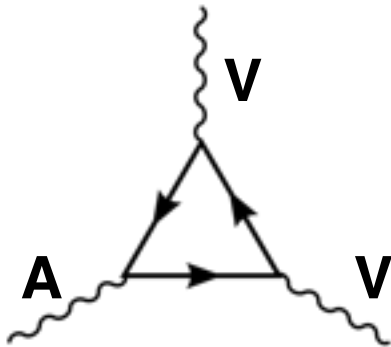
$$\Lambda_A : \Psi \rightarrow e^{i\gamma_5\theta}\Psi$$



Broken at QM level:

$$\partial_\mu J_5^\mu = C_A \vec{E} \cdot \vec{B}$$

$$dQ_5/dt = \int_{\vec{x}} C_A \vec{E} \cdot \vec{B}$$



- * C_A is universal anomaly coefficient
- * Anomaly is intrinsically QUANTUM effect

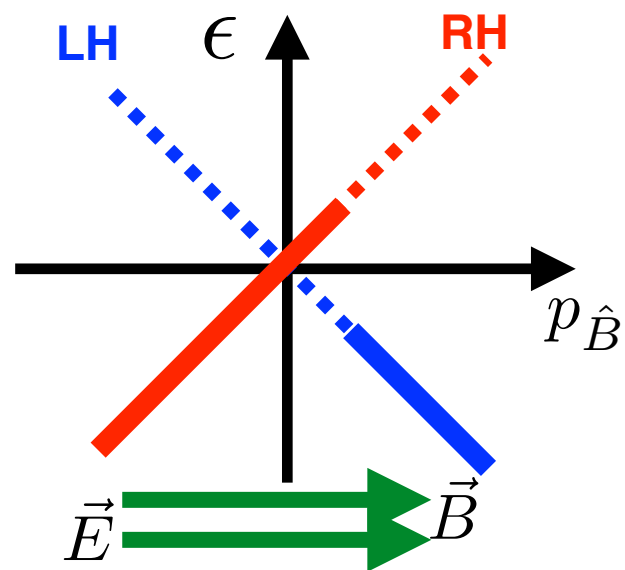
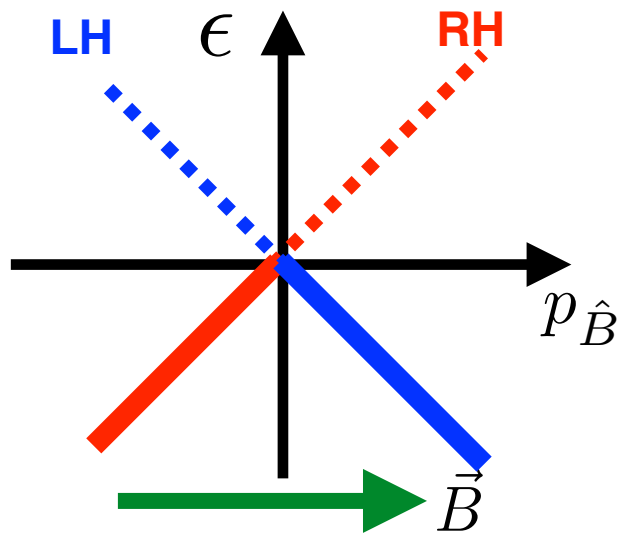
Chiral Anomaly

Chiral anomaly is a fundamental aspect of QFT with chiral fermions.

$$\partial_\mu J_5^\mu = C_A \vec{E} \cdot \vec{B}$$

$$dQ_5/dt = \int_{\vec{x}} C_A \vec{E} \cdot \vec{B}$$

$$J_5^\mu = J_R^\mu - J_L^\mu$$

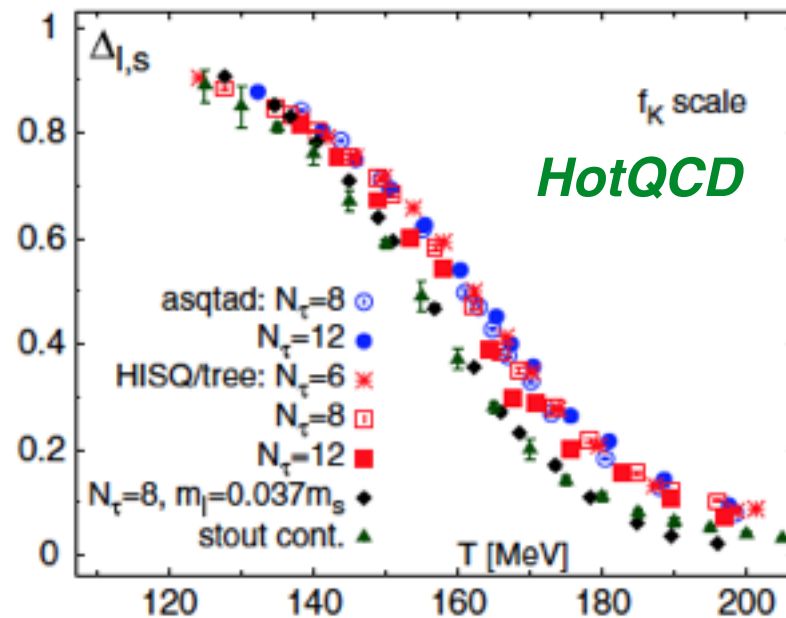


Illustrated with Lowest-Landau-Level (LLL) picture: the LLL is chiral!

Chiral Anomaly in Many-Body System

*Would chiral anomaly, usually considered at microscopic level, manifest itself **MACROSCOPICALLY** in a system of many chiral fermions? If so, how?*

This is a relevant question, for e.g. the quark-gluon plasma, where light quarks have approximate chiral symmetry at high T.



The restored chiral symmetry in quark-gluon plasma (QGP) phase

Anomalous Transport: Chiral Magnetic Effect

** The Chiral Magnetic (CME) is an anomalous transport*

$\vec{J} = \sigma_5 \mu_5 \vec{B}$

*P odd
CP even* →

← *P even
CP odd*

In **NORMAL** environment, this will **NOT** happen.
For this to occur: need a **P- and CP-Odd environment!**

μ_5

A (convenient) way to quantify
IMBALANCE

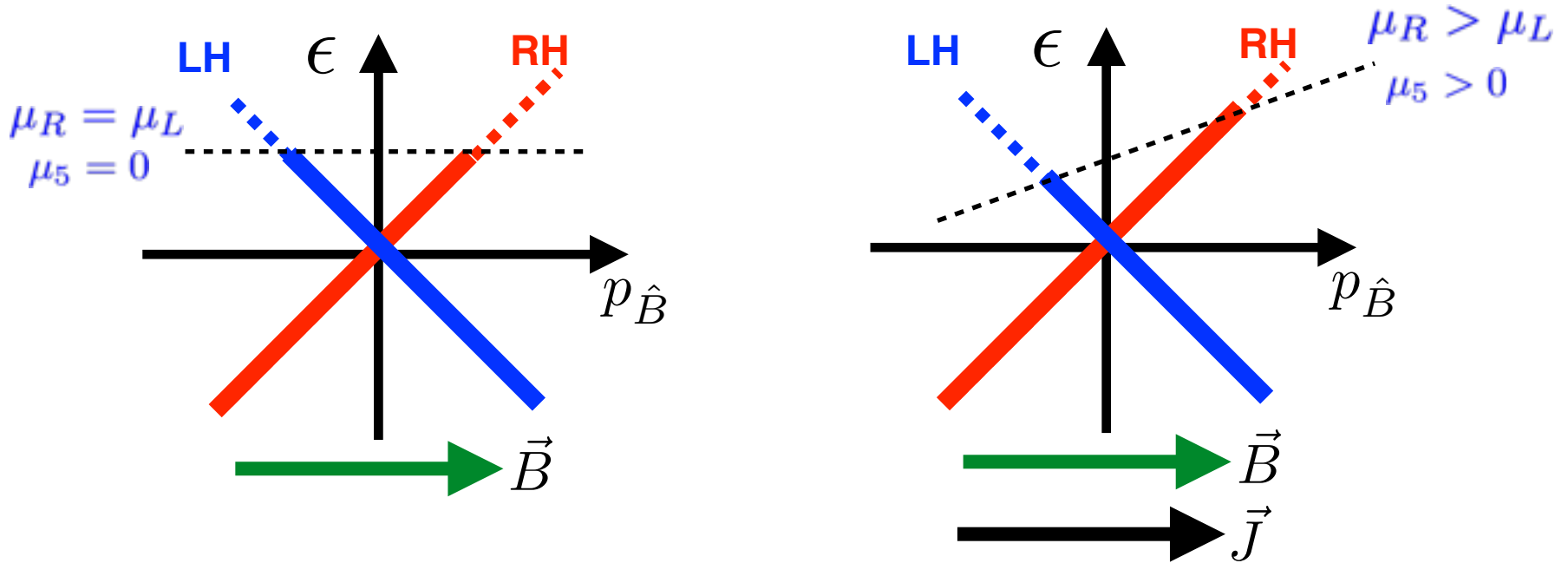
in the numbers of
LH vs RH chiral fermions

→

A CHIRAL QGP!

Such imbalance can be generated through chiral anomaly coupled with topological fluctuations (F-F-dual) of the gluonic sector.

So How Does CME Work?



One may recognize deep connection between CME & anomaly.

$$\partial_{\mu} J_{5}^{\mu} = C_A \vec{E} \cdot \vec{B}$$

$$\vec{J} = \sigma_5 \mu_5 \vec{B}$$

The CME conductivity is

- * fixed entirely by quantum anomaly*
- * universal from weak to strong coupling*
- * T-even, non-dissipative*

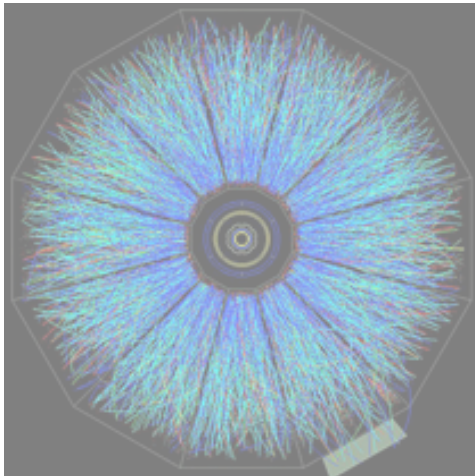
Wrap-up: Emergence in Chiral Matter

*Chiral anomaly:
Basic dynamics of
QFT with chiral fermions*



*Anomalous chiral transport
(Chiral magnetic effect):
Emergent phenomenon
in Chiral Matter:*

Quark-gluon plasma



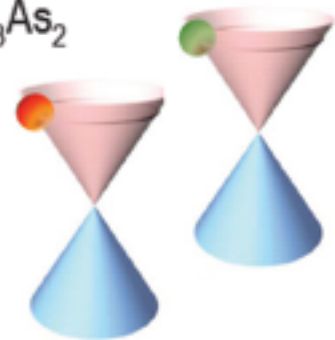
Dirac & Weyl Semimetals



ZrTe₅

Na₃Bi,

Cd₃As₂



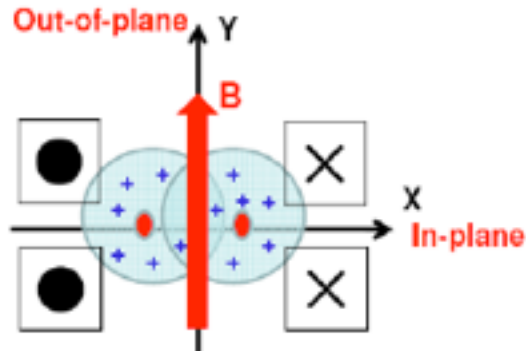
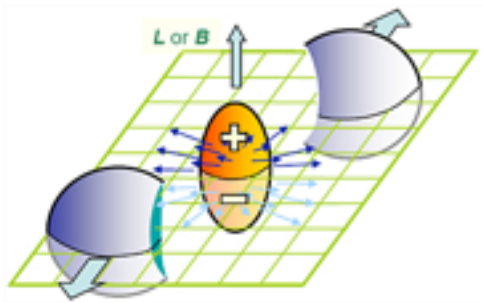
TaAs

NbAs

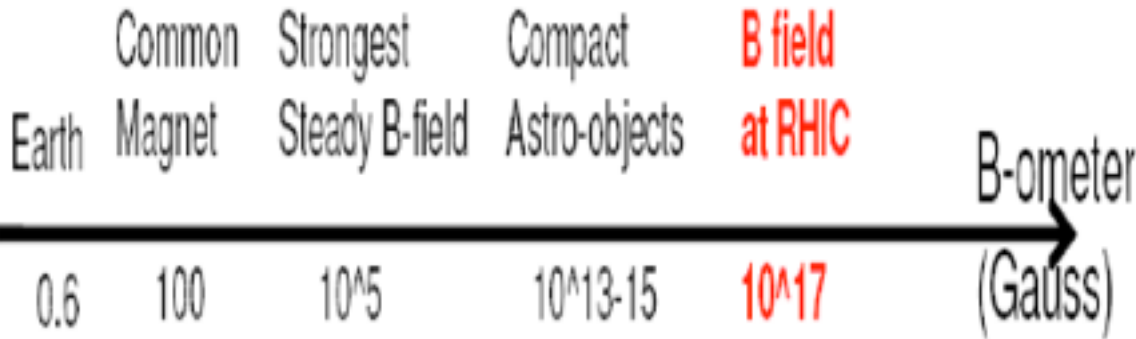
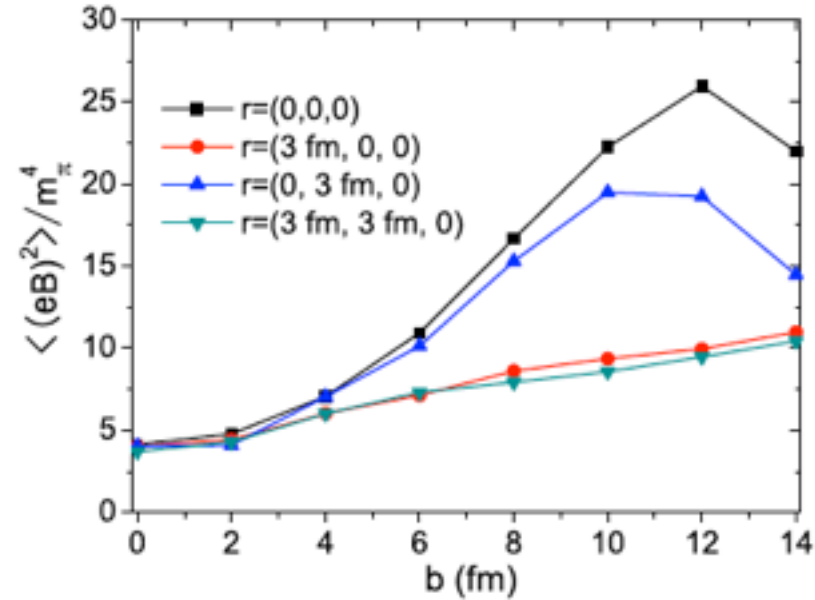
NbP

TaP

Strong EM Fields in Heavy Ion Collisions

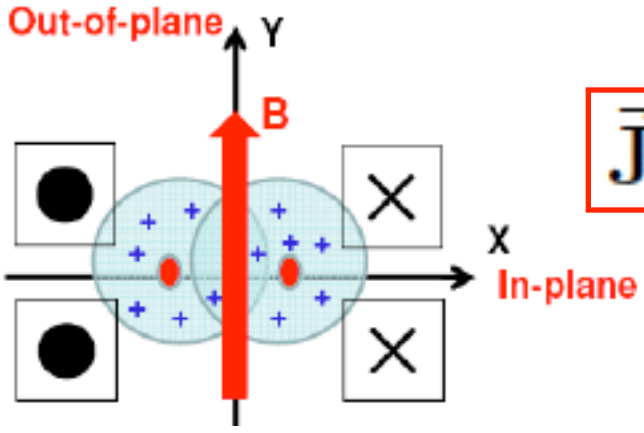


$$E, B \sim \gamma \frac{Z \alpha_{EM}}{R_A^2} \sim 3m_\pi^2$$

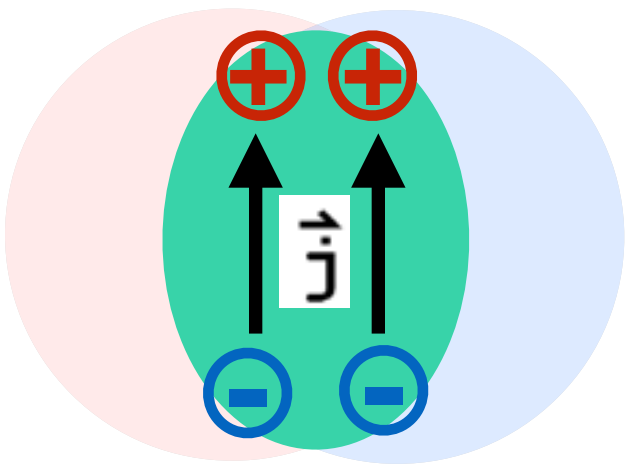
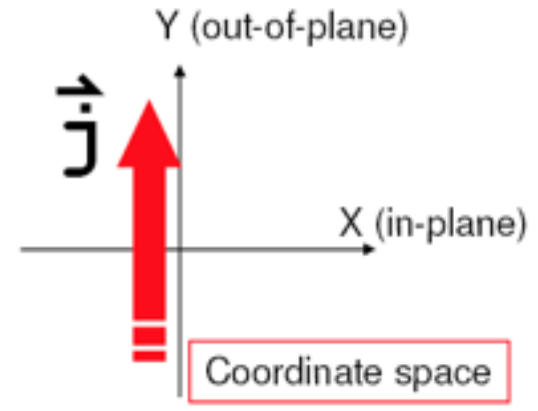


- **Strongest B field (and strong E field as well) naturally arises!**
[Kharzeev, McLerran, Warringa; Skokov, et al; Bzdak-Skokov; Deng-Huang; Błoczyński-Huang-Zhang-Liao; Skokov-McLerran; Tuchin; ...]
- “Out-of-plane” orientation (approximately)

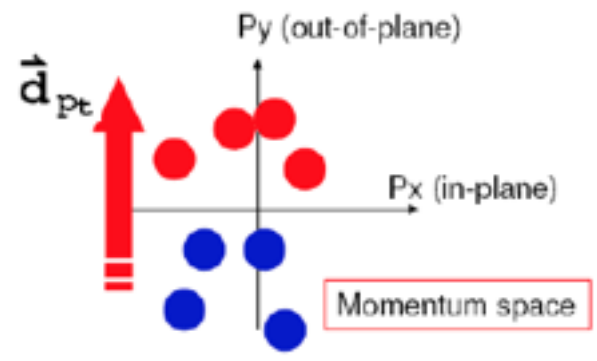
From CME Current to Charge Separation



$$\vec{J} = \sigma_5 \mu_5 \vec{B}$$



*strong radial blast:
position → momentum*



*Charge Separation or
Electric Dipole in Pt Space
(along out-of-plane)*

$$\frac{dN_{\pm}}{d\phi} \propto \dots + a_{\pm} \sin(\phi - \Psi_{RP})$$

$$\langle a_{\pm} \rangle \sim \pm \langle \mu_5 \rangle B$$

[Kharzeev 2004; Kharzeev, McLerran, Warringa, 2008; ...]

Charge Separation Observable

$$\frac{dN_{\pm}}{d\phi} \propto \dots + a_{\pm} \sin(\phi - \Psi_{RP})$$

$$\langle a_{\pm} \rangle \sim \pm \langle \mu_5 \rangle B \rightarrow 0$$

The dipole flips e-by-e and averages to zero (no global P-violation)

[Voloshin, 2004]

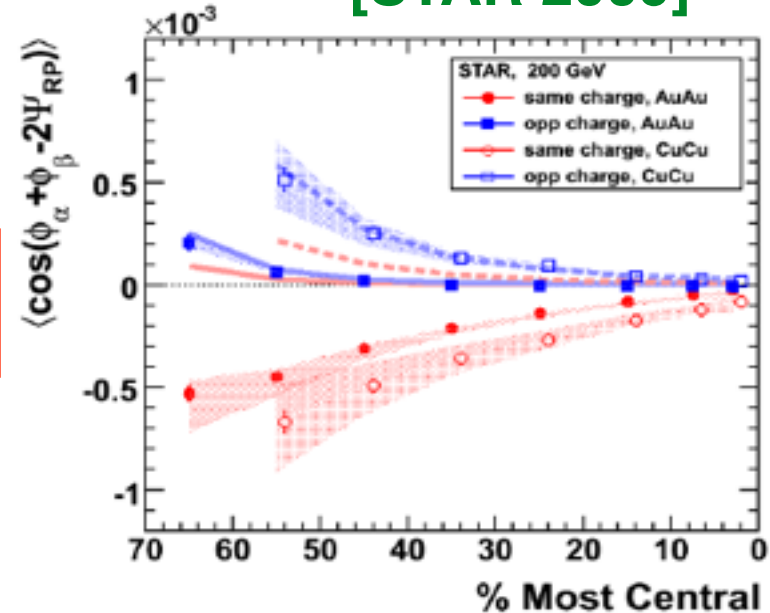
$$\begin{aligned} \gamma &= \langle \cos(\phi_{\alpha} + \phi_{\beta} - 2\psi_{RP}) \rangle \\ &= [\langle v_{1,\alpha} v_{1,\beta} \rangle + B_{in}] - [\langle a_{\alpha} a_{\beta} \rangle + B_{out}] \end{aligned}$$

known to be very small

what we are looking for

The hope was: these two cancel out to be negligible...

[STAR 2009]



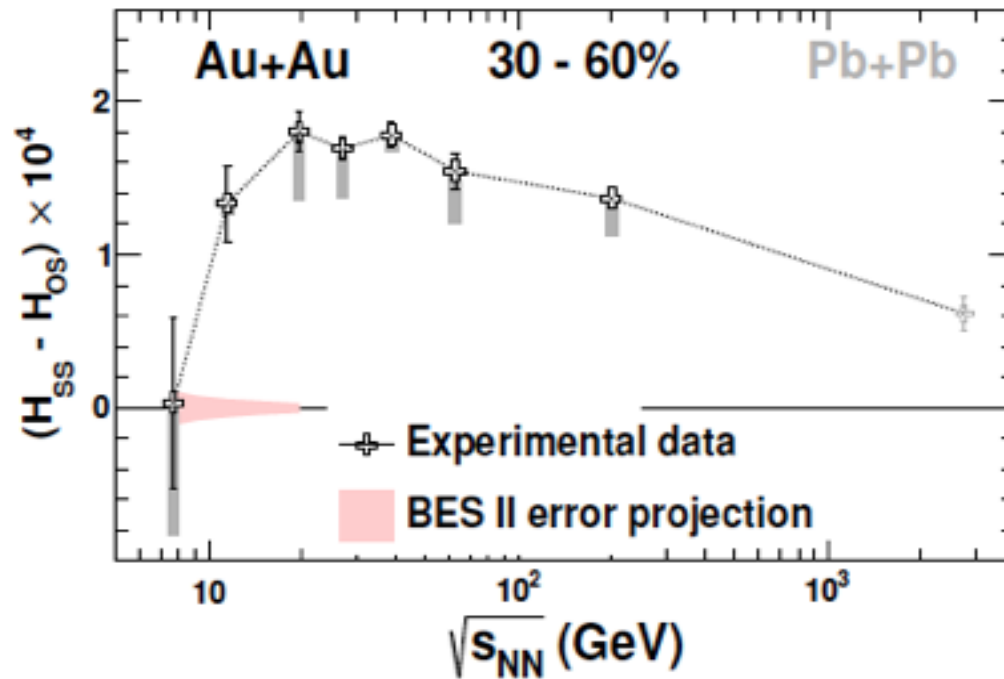
As it was pointed out later, the backgrounds turn out to be NOT negligible...

[Bzdak, Koch, JL, 2009, 2010; Wang; Pratt, ...]

Separation of CME & Flow-Driven Background

$$\begin{aligned} \gamma &= \langle \cos(\phi_\alpha + \phi_\beta - 2\psi_{RP}) \rangle \\ &= [\langle v_{1,\alpha} v_{1,\beta} \rangle + B_{in}] - [\langle a_\alpha a_\beta \rangle + B_{out}] \end{aligned}$$

$$[B_{in} - B_{out}] \sim v_2 \sim \gamma$$



$$H_{CME} \rightarrow 2a_1^2$$

*A big step forward
for the search of
CME (in my view)*

[STAR PRL 2014]

*Making sense of data
in a two-component picture*

$$\begin{aligned} \gamma &\equiv \langle \cos(\phi_1 + \phi_2 - 2\Psi_{RP}) \rangle = \kappa v_2 F - H \\ \delta &\equiv \langle \cos(\phi_1 - \phi_2) \rangle = F + H, \end{aligned}$$

[Bzdak, Koch, JL, 2012;
Blocynski, Huang, Zhang, JL, 2013]

H: “CME Signal”
F: “Flow Driven Background”

Fluid Dynamics That Knows Left & Right

conservation
law:

$$\partial_\mu J^\mu = 0 \longrightarrow \partial_\mu J^\mu = C E^\mu B_\mu$$

constituent
relation:

$$J^\mu = n u^\mu + \nu^\mu$$

$$\partial_\mu s^\mu \geq 0 \quad \nu^\mu = -\sigma T P^{\mu\nu} \partial_\nu \left(\frac{\mu}{T} \right) + \sigma E^\mu + \xi \omega^\mu + \xi_B B^\mu$$

[Son, Surowka, 2009;...]

CVE CME

Chiral Fluid: Microscopic Quantum Anomaly manifests itself as macroscopic hydrodynamic currents!

It provides a hydro framework for simulating anomaly effects. Initial attempts of applying Chiral-Hydro to heavy ion were made. [Hirano, Hirono; Yin, Yee; Hirono, Hirano, Kharzeev; Yin, Liao;...]

[In passing: fluid rotation induces similar effects as magnetic field]

Anomalous-Viscous Fluid Dynamics (AVFD)

[Jiang, Shi, Yin, JL, 2016.]

$$D_\mu J_R^\mu = + \frac{N_c q^2}{4\pi^2} E_\mu B^\mu \quad D_\mu J_L^\mu = - \frac{N_c q^2}{4\pi^2} E_\mu B^\mu$$

$$J_R^\mu = n_R u^\mu + v_R^\mu + \frac{\sigma}{2} E^\mu + \frac{N_c q}{4\pi^2} \mu_R B^\mu$$
$$J_L^\mu = n_L u^\mu + v_L^\mu + \frac{\sigma}{2} E^\mu - \frac{N_c q}{4\pi^2} \mu_L B^\mu \quad \text{CME}$$

$$d v_{R,L}^\mu = (v_{NS}^\mu - v_{R,L}^\mu) / \tau_{rlx}$$

on top of 2+1D VISHNew— OSU Group

$$D_\mu T^{\mu\nu} = 0$$

$$n = 0$$

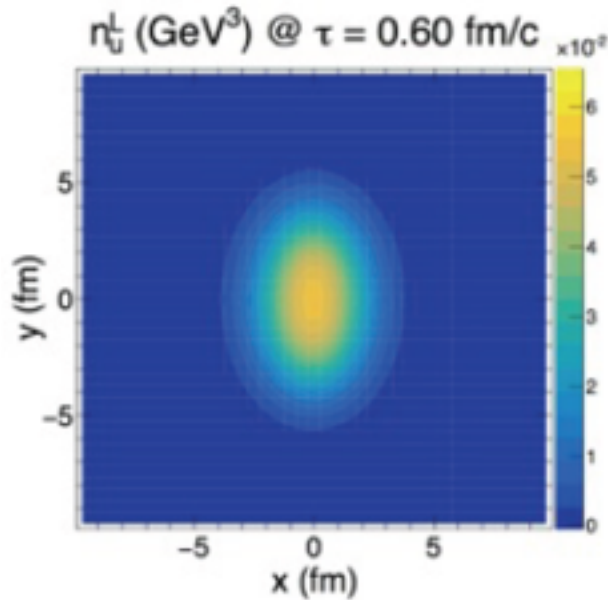


B field + $\mu_A \Rightarrow$ charge separation

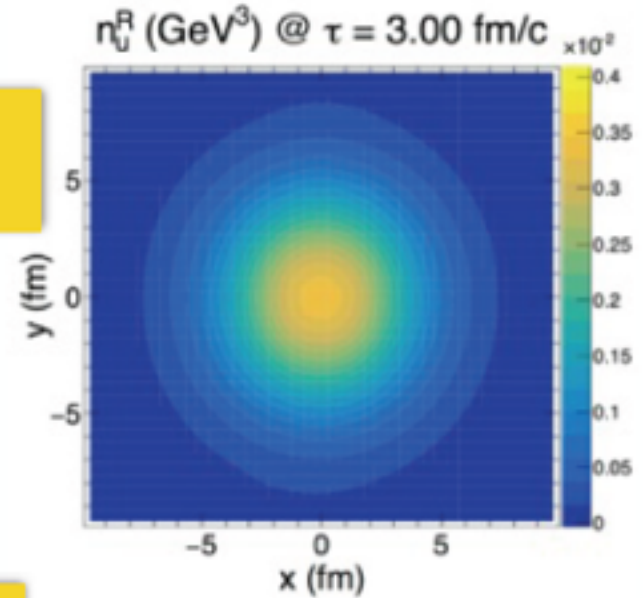
$$dN_\pm/d\phi \propto 1 + 2 a_{1\pm} \sin(\phi - \psi_{RP}) + \dots$$

Anomalous-Viscous Fluid Dynamics (AVFD)

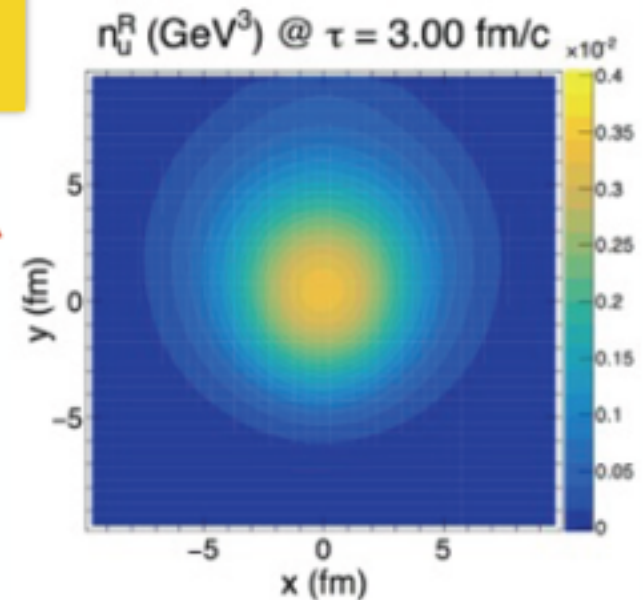
Initial Condition



No B Field

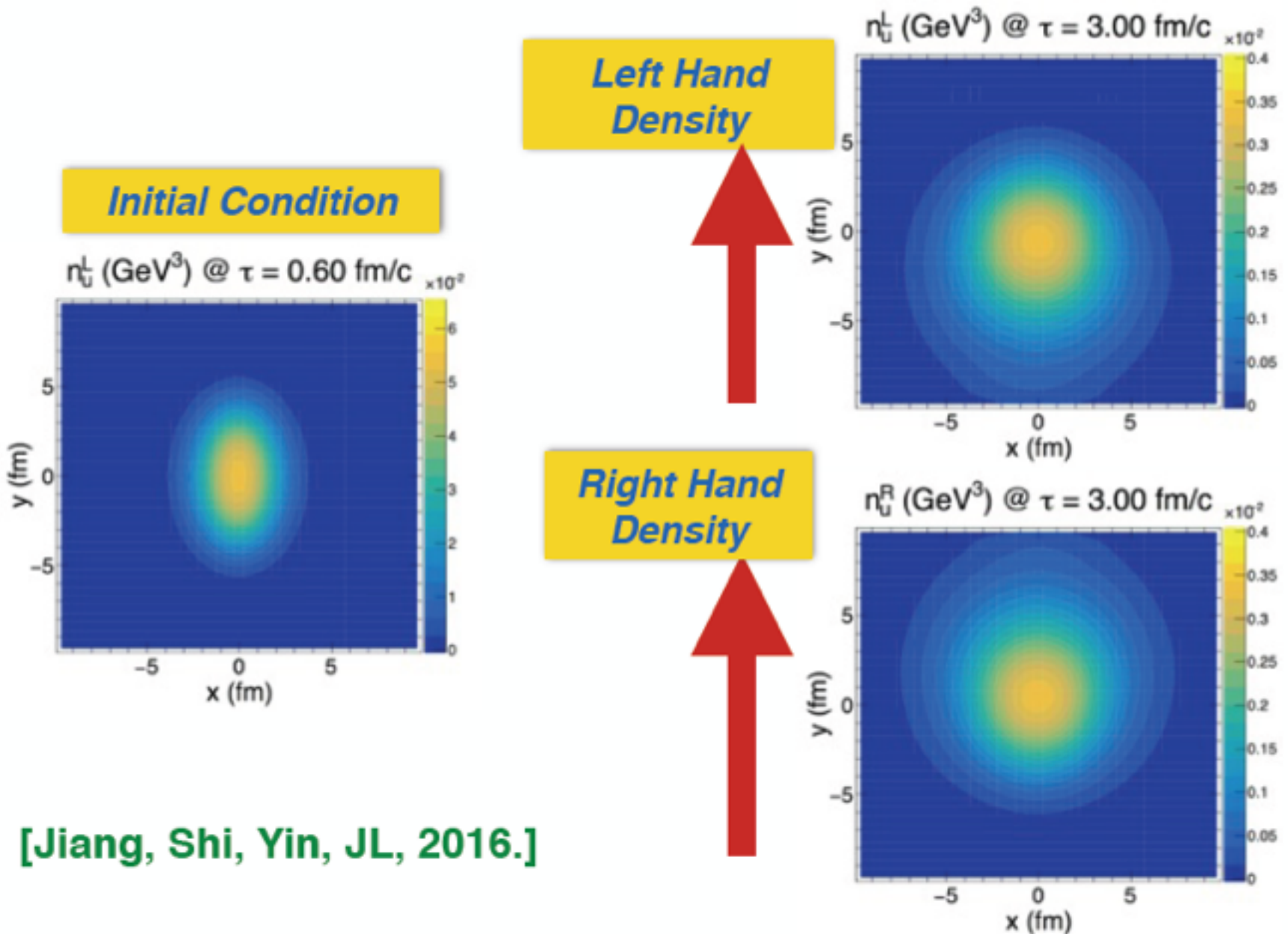


With B Field



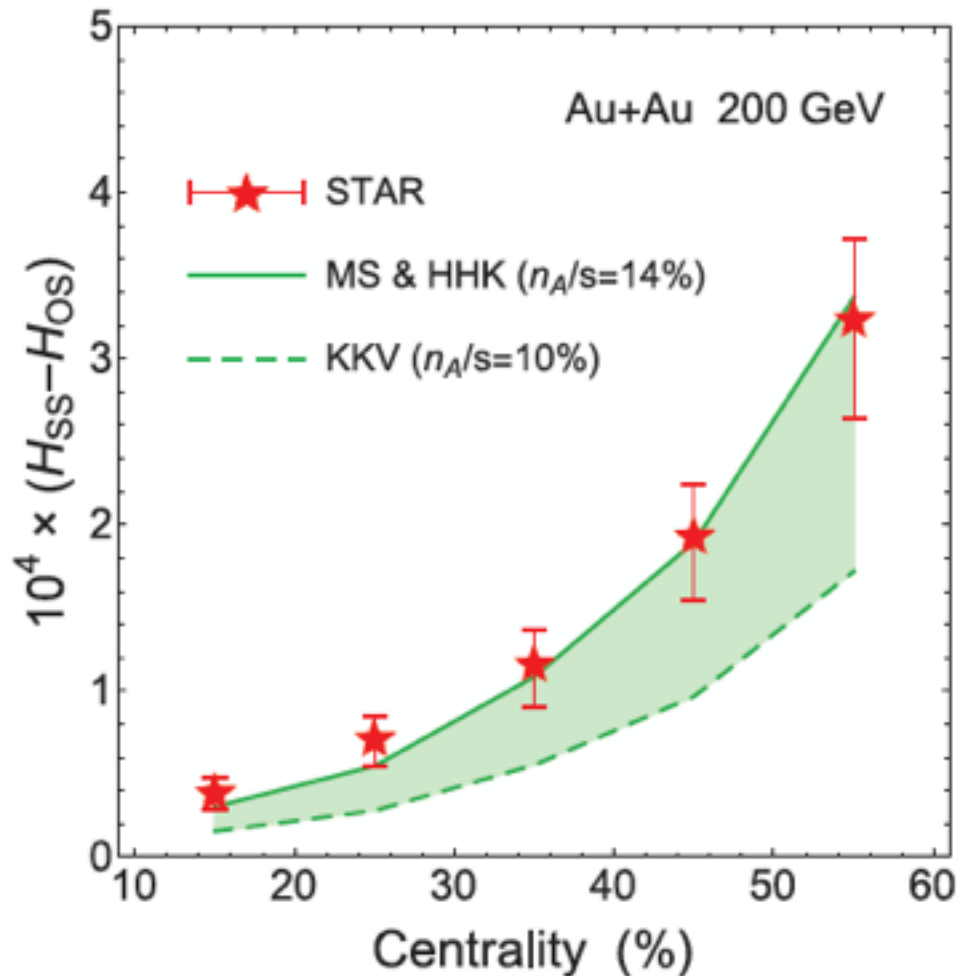
[Jiang, Shi, Yin, JL, 2016.]

Anomalous-Viscous Fluid Dynamics (AVFD)



[Jiang, Shi, Yin, JL, 2016.]

Anomalous-Viscous Fluid Dynamics (AVFD)



$$B = \frac{B_0}{1 + \left(\frac{\tau}{\tau_B}\right)}$$

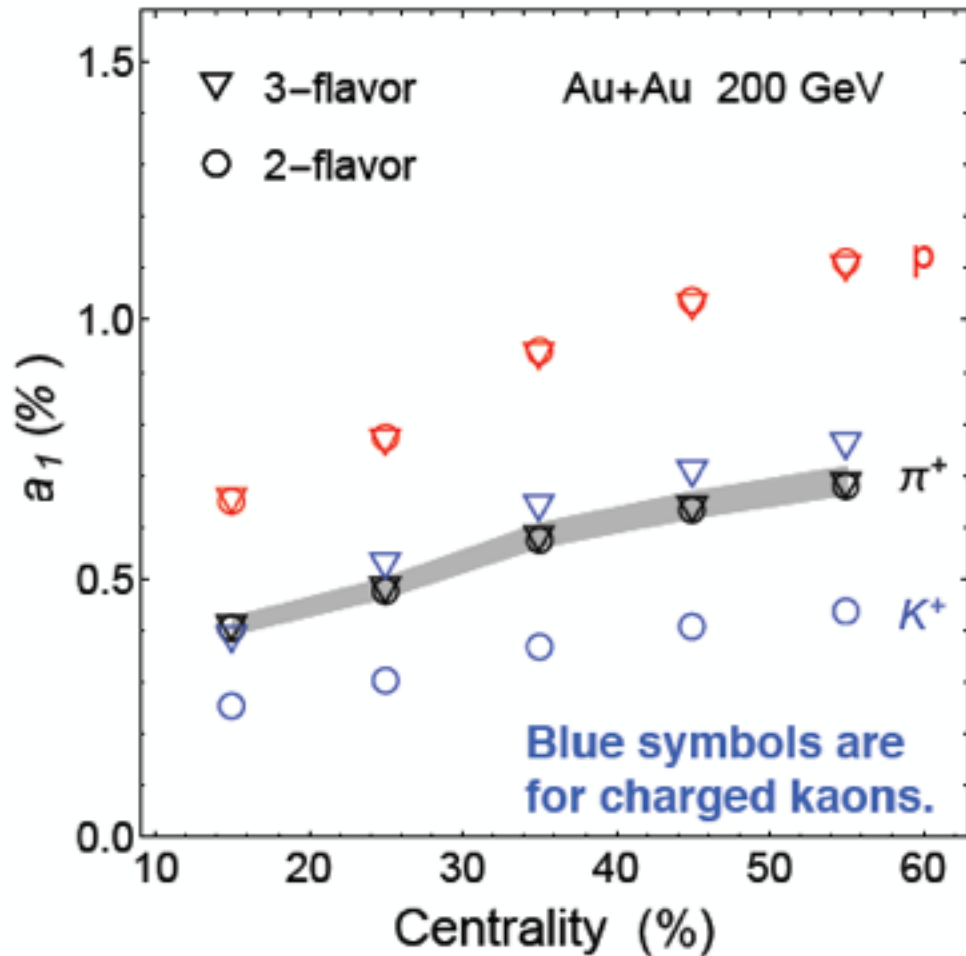
$$\tau_B = 0.6 \text{ fm}/c$$

$$\frac{n_A}{s} \propto \left(\frac{dN}{d\eta}\right)^{-1/3}$$

With realistic initial axial charge density and short magnetic lifetime, the data can be describe well.

[Jiang, Shi, Yin, JL, 2016.]

Is Strangeness Chiral?



Measuring charge separation for Kaons: an exciting opportunity to tell to which extent the strange quarks are chiral!

[Jiang, Shi, Yin, JL, 2016.]

Upcoming Isobaric Collisions (2018@RHIC)

**New Proposal of Isobaric Collisions @ RHIC:
up to 10% variation in B field, thus ~20% shift of CME signal!**

— $^{96}_{40}\text{Zirconium}$ vs $^{96}_{44}\text{Ruthenium}$

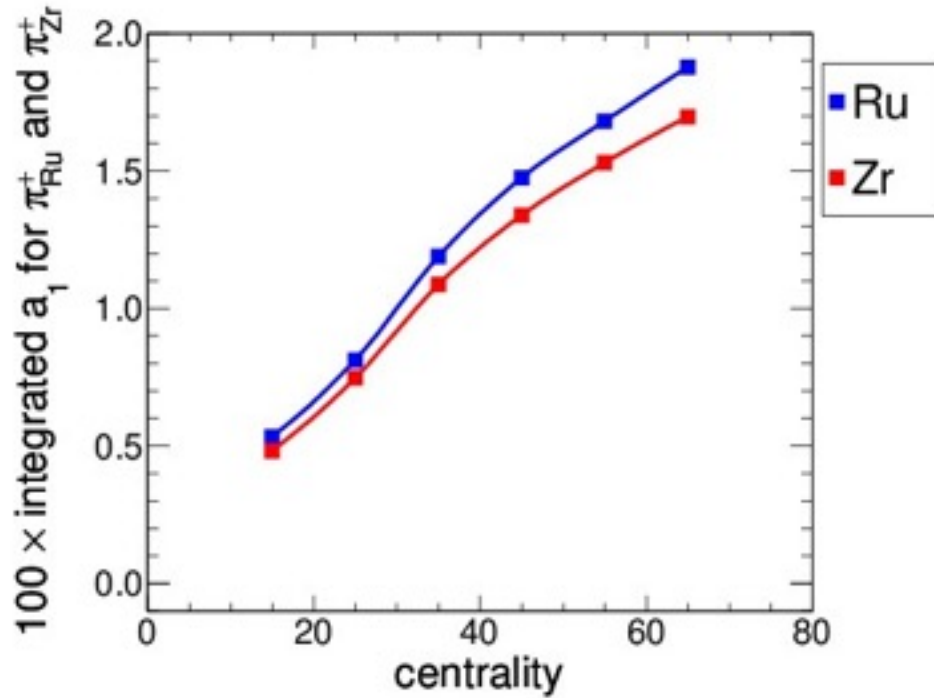


	$^{96}_{44}\text{Ru}+^{96}_{44}\text{Ru}$	vs	$^{96}_{40}\text{Zr}+^{96}_{40}\text{Zr}$
Flow		\leq	
CMW		$>$	
CME		$>$	
CVE		$=$	

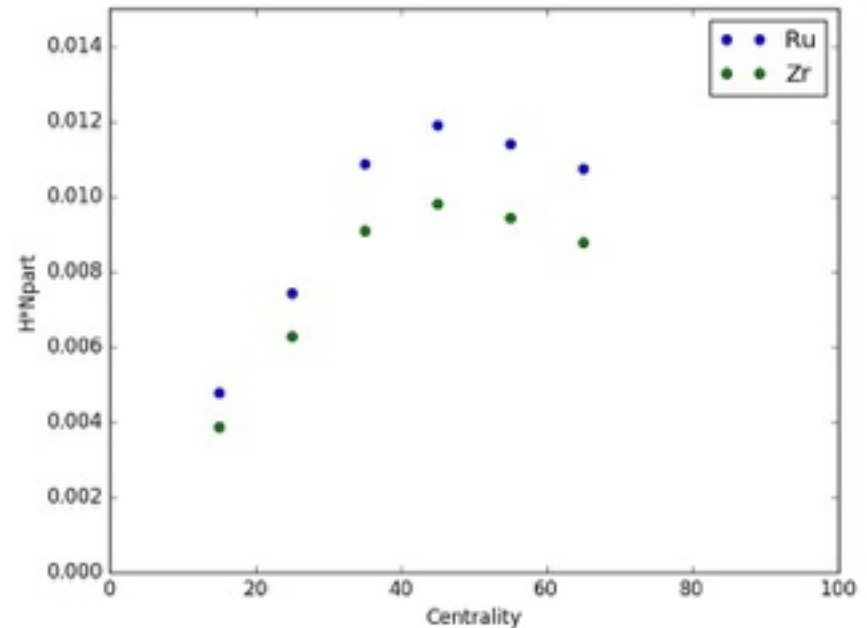
The isobaric collisions will be a crucial test!

[See e.g.: Deng, Huang, Ma, Wang, 1607.04697.]

AVFD Predictions for Isobaric Collisions



[Shi, Lilleskov, Jiang, Liao,
in final preparation.]



Summary

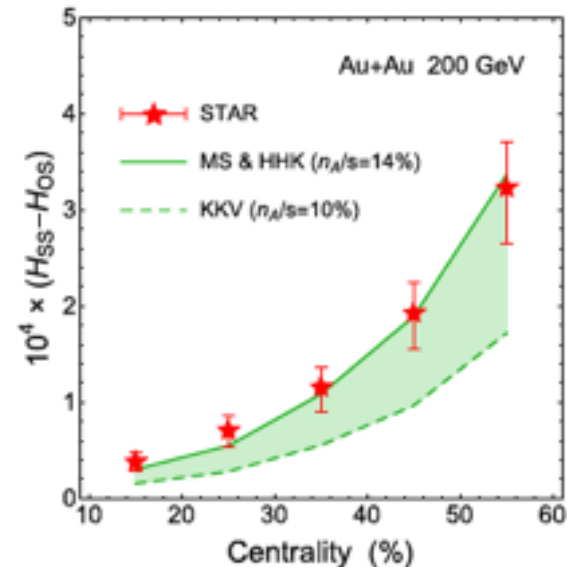
* **Chiral anomaly emerges in chiral matter (e.g. QGP) as anomalous chiral transport: Chiral Magnetic Effect**

* **Quantitative CME from new Anomalous-Viscous Fluid Dynamics simulations: CME-induced charge separation signal could be explained.**

* **Future test: isobaric collisions**

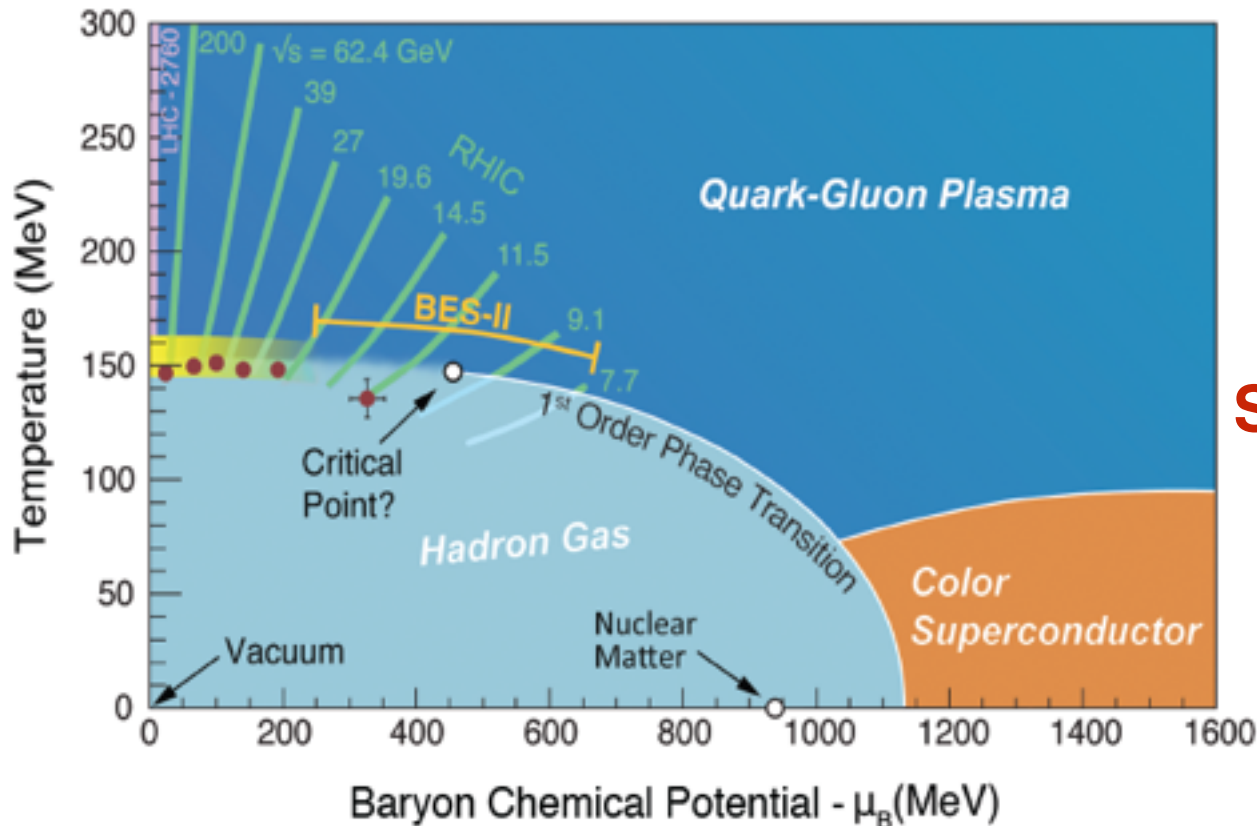
* **Many other interesting anomalous transport phenomena:**

- *Chiral Magnetic Wave [Burnier, Kharzeev, JL, Yee;...]*
- *Chiral Vortical Effect [Kharzeev, Son;...]*
- *Chiral Vortical Wave [Jiang, Huang, JL;...]*
- *Chiral Kinetic Theory [Stephanov, Yin; Son, Yamamoto; ...]*
-



Toward Physics of Beam Energy Scan

- * *Establishing a chiral QGP at higher energy via anomalous chiral effects*
- * *Searching for chiral critical point & 1st-order transition at lower energy*



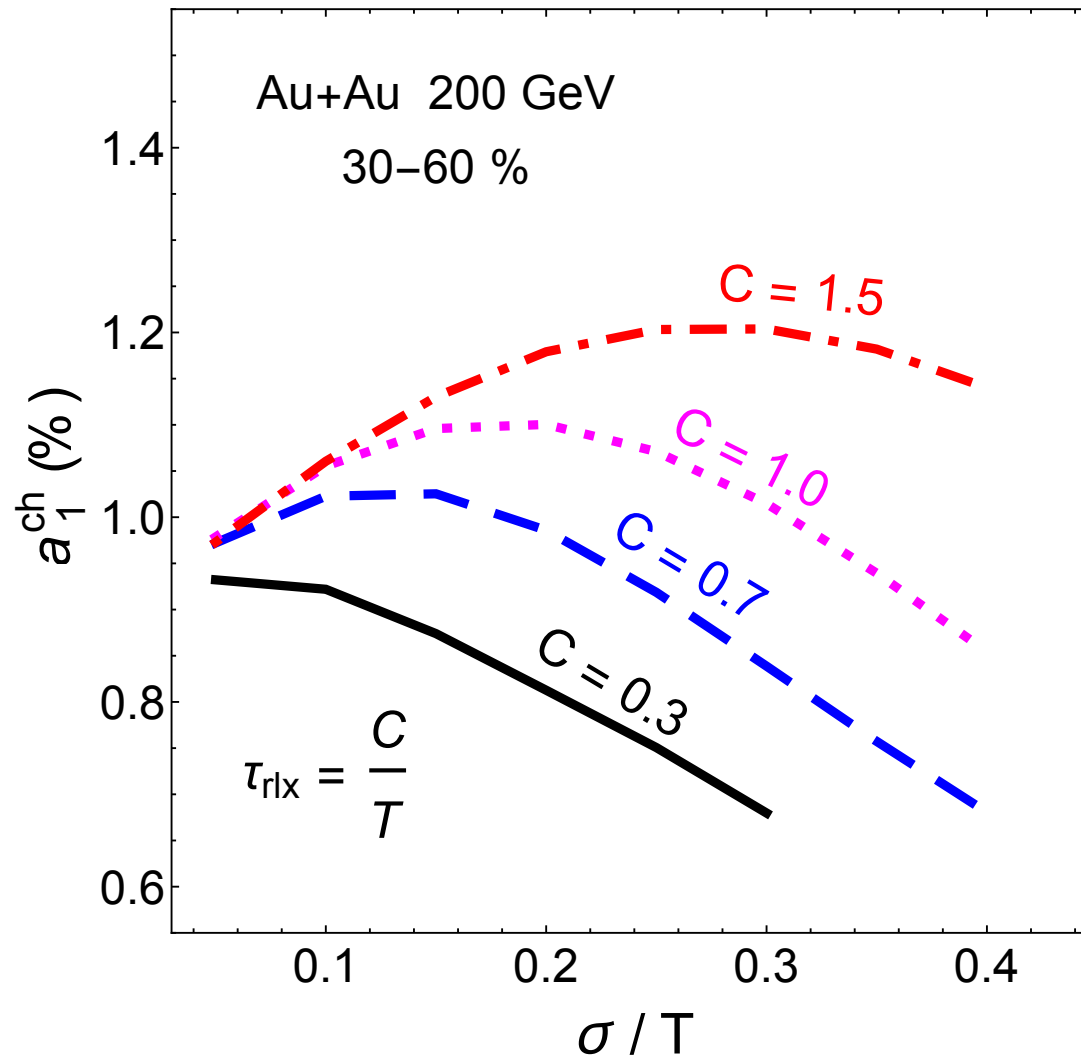
BEST
COLLABORATION

**Stay tuned for news
in the near future!**

***Beam Energy Scan Theory (BEST) Collaboration:
BNL, IU, LBNL, McGill U, Michigan State U, MIT, NCSU, OSU,
Stony Brook U, U Chicago, U Conn, U Huston, UIC***

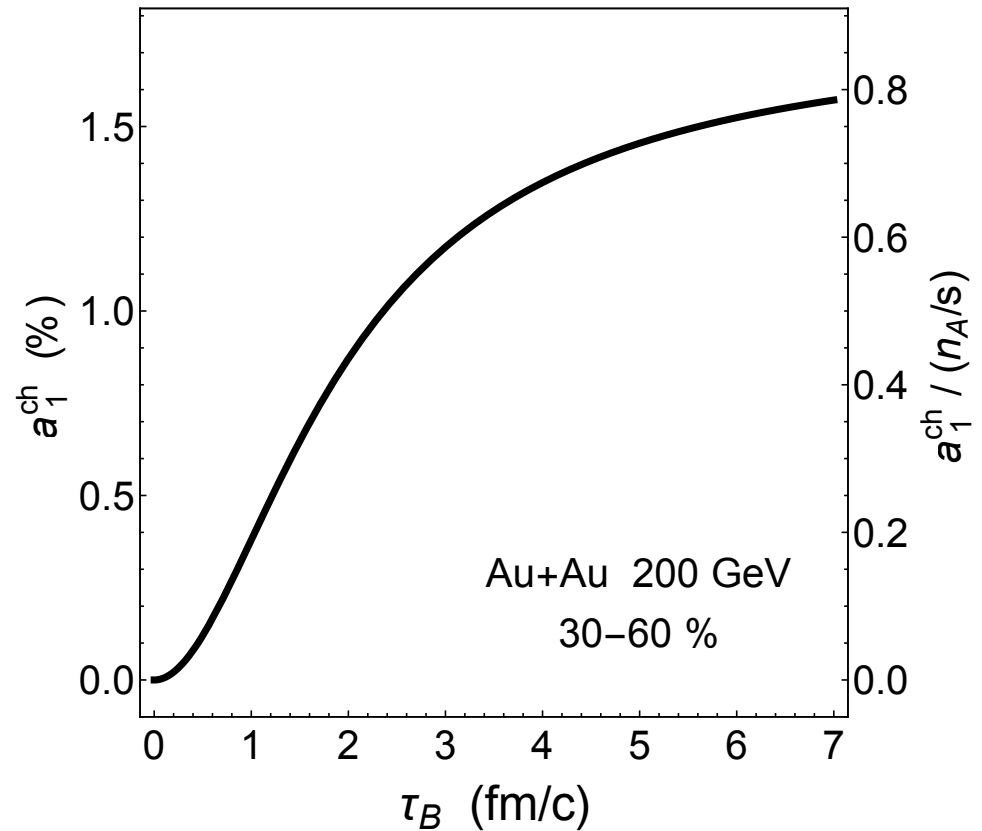
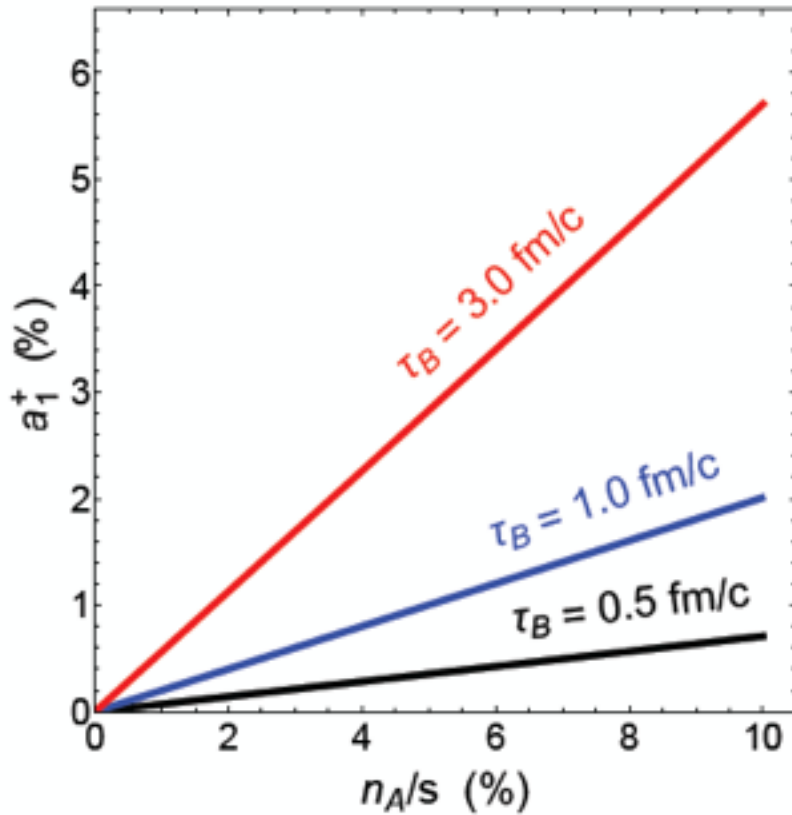
Backup Slides

Anomalous-Viscous Fluid Dynamics (AVFD)



[Jiang, Shi, Yin, JL, 2016.]

Anomalous-Viscous Fluid Dynamics (AVFD)



[Jiang, Shi, Yin, JL, 2016.]

Quantitative Study of Anomalous Transport

Dynamical Evolution

$$\vec{\mathbf{J}} = \sigma_5 \vec{\mathbf{B}},$$

CME

$$\vec{\mathbf{J}} = \frac{1}{\pi^2} \mu_5 \mu \vec{\omega}.$$

CVE

*Initial
Conditions*

*Observable
("Chemistry"):*

partons

→

hadrons

*Driving
Forces*

$$(\partial_0 \pm v_B \partial_{\hat{\mathbf{B}}}) \delta J_{R/L}^0 = 0.$$

$$v_B \equiv \frac{(Qe)B}{(4\pi^2)\chi}$$

CMW

$$(\partial_0 \pm v_\omega \partial_{\hat{\omega}}) \delta J_{R/L}^0 = 0$$

$$v_\omega \equiv \frac{\mu_0 \omega}{(2\pi^2)\chi \mu_0}$$

CVW

*Possible
backgrounds*

Toward Quantitative CME

Physics Letters B 756 (2016) 42–46



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Hydrodynamics with chiral anomaly and charge separation in relativistic heavy ion collisions



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^c RIKEN BNL Research Center, Bldg. 510A, Brookhaven National Laboratory, Upton, NY 11973, USA

[Yi Yin, JL, PLB2016, arXiv:1504.06906]

$$\partial_\mu J^\mu = \partial_\mu (nu^\mu + Q_f C_A \mu_A B^\mu) = 0$$

$$\partial_\mu J_A^\mu = \partial_\mu (n_A u^\mu + Q_f C_A \mu_V B^\mu) = -Q_f^2 e C_A E_\mu B^\mu$$

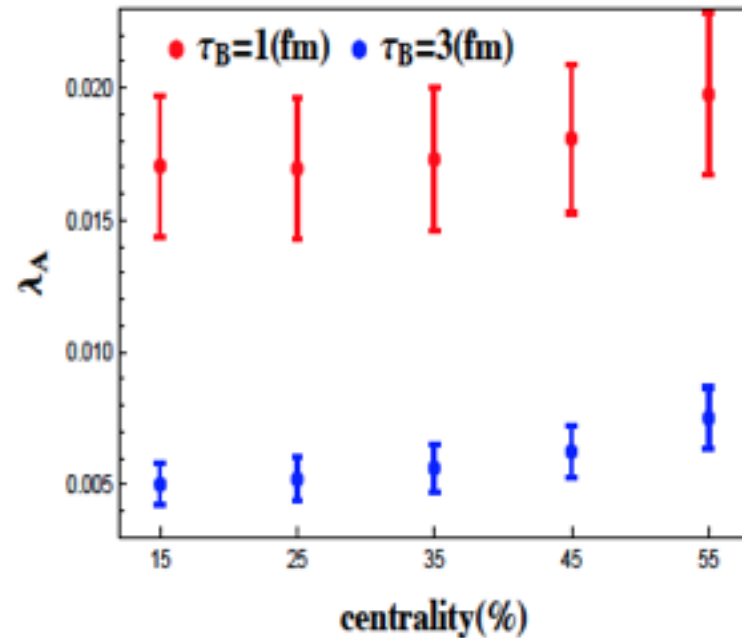
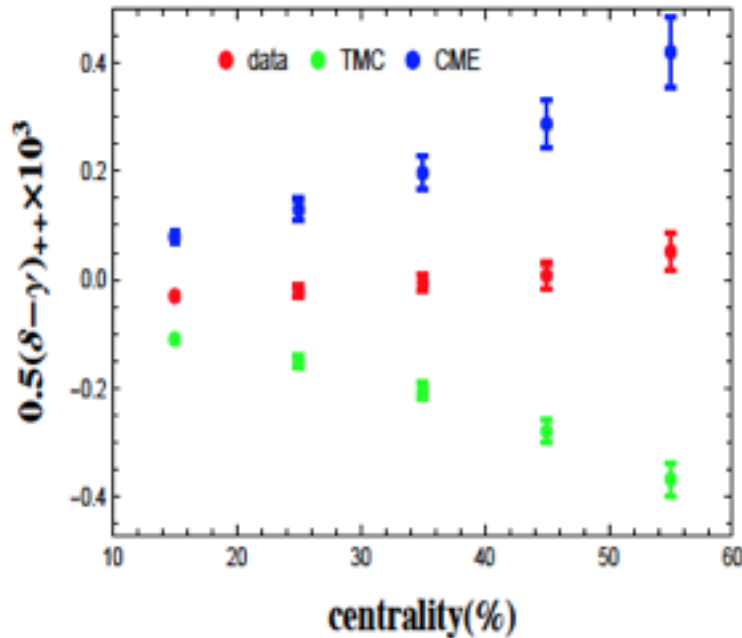
$$\left[\frac{dN^H}{d\phi} \right]_{\text{CME}} \propto [1 + 2Q^H a_1^H \sin(\phi) + \dots]$$

To quantitatively understand, in a viscous and anomalous hydrodynamic framework: how anomaly generates charge separation, and how much?

Quantitative Interpretation of Data

$$\gamma_{\alpha,\beta}^{\text{data}} \simeq \gamma_{\alpha,\beta}^{\text{CME}} + \gamma_{\alpha,\beta}^{\text{TMC}}, \quad \delta_{\alpha,\beta}^{\text{data}} \simeq \delta_{\alpha,\beta}^{\text{CME}} + \delta_{\alpha,\beta}^{\text{TMC}}$$

[Yi Yin, JL, PLB2016,
arXiv:1504.06906]



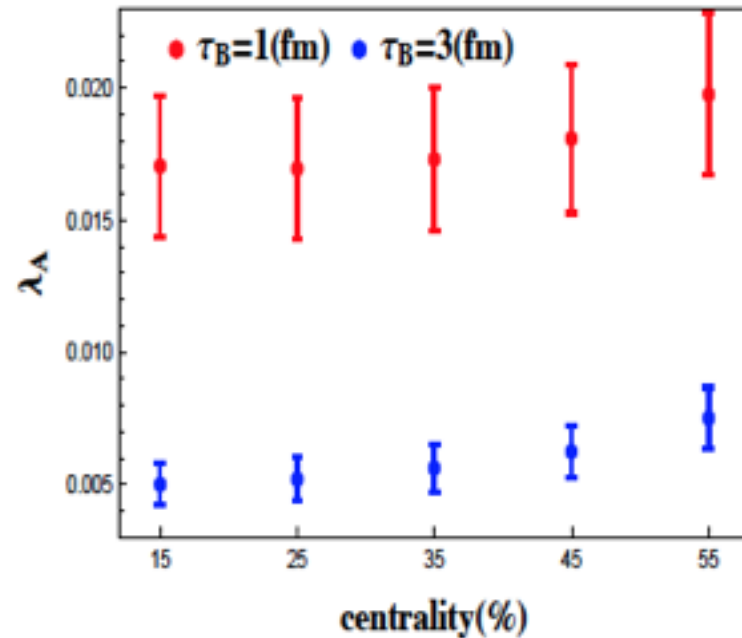
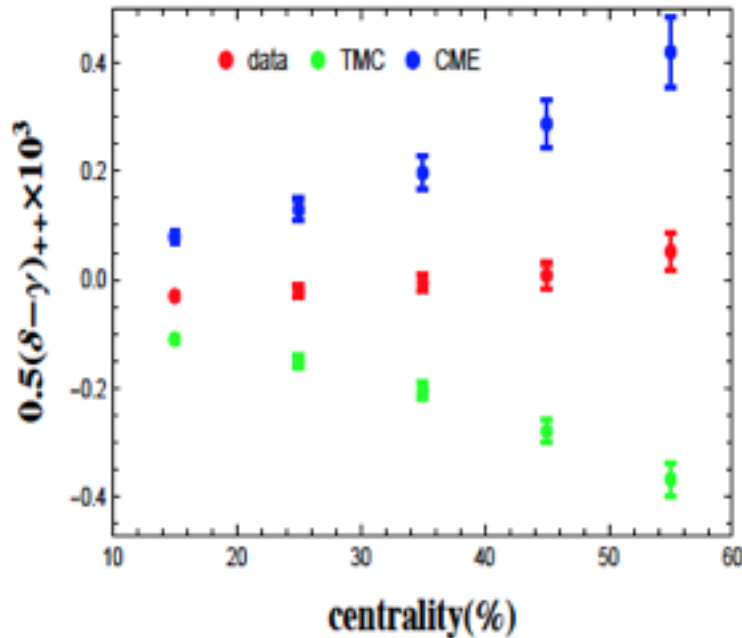
Using the particle spectra from the SAME VISH hydro, we evaluate quantitatively effect from transverse momentum conservation:

$$\delta_{\alpha\beta}^{\text{TMC}} \pm \gamma_{\alpha\beta}^{\text{TMC}} = \frac{[\langle p_{\perp} \rangle_{\alpha} (1 \pm \bar{v}_{2,\alpha})][\langle p_{\perp} \rangle_{\beta} (1 \pm \bar{v}_{2,\beta})]}{N_{\text{TMC}} \langle p_{\perp}^2 \rangle (1 \pm \bar{v}_2)}$$

Quantitative Interpretation of Data

$$\gamma_{\alpha,\beta}^{\text{data}} \simeq \gamma_{\alpha,\beta}^{\text{CME}} + \gamma_{\alpha,\beta}^{\text{TMC}}, \quad \delta_{\alpha,\beta}^{\text{data}} \simeq \delta_{\alpha,\beta}^{\text{CME}} + \delta_{\alpha,\beta}^{\text{TMC}}$$

[Yi Yin, JL, PLB2016,
arXiv:1504.06906]

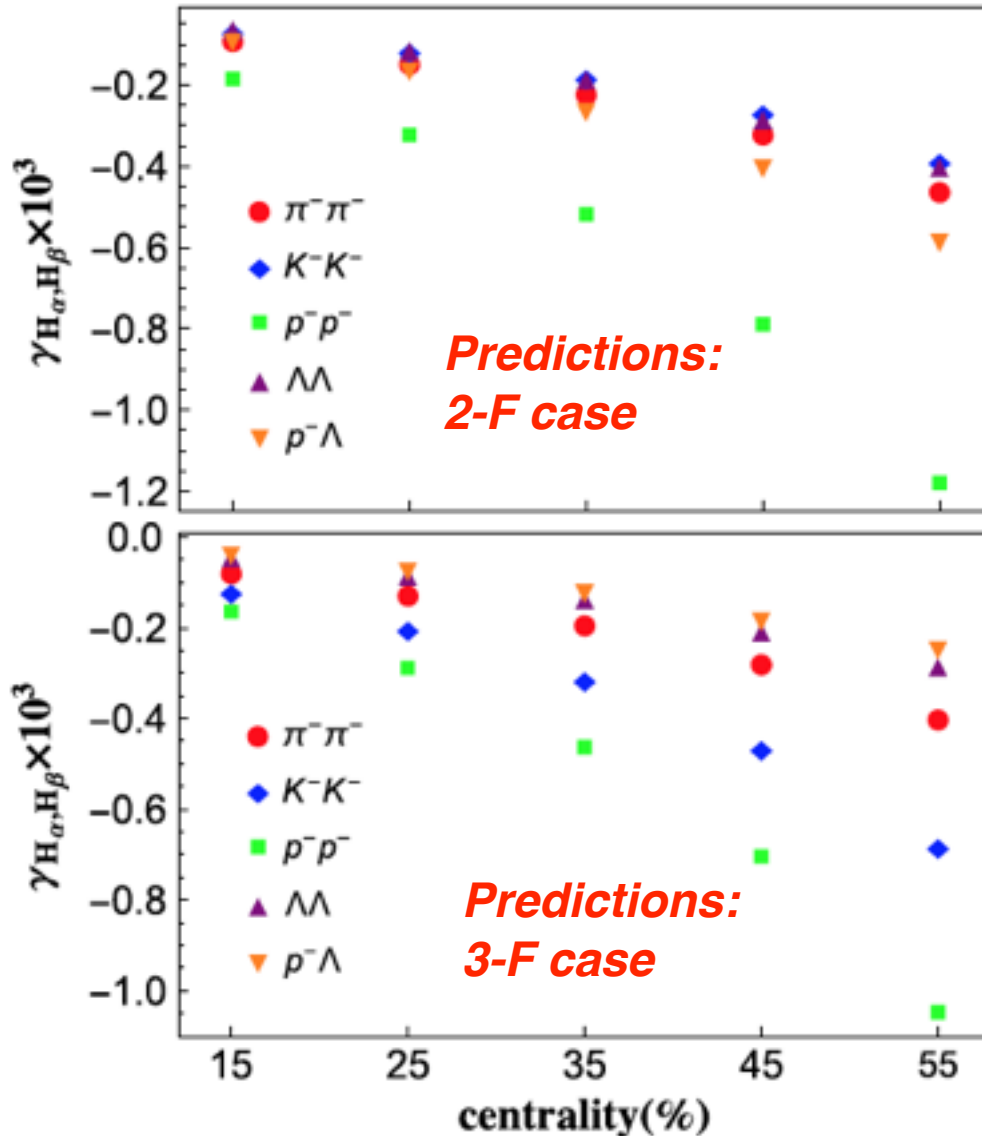


The messages:

- * B field *lifetime* $\sim 1\text{fm}/c$ (or less) is OK!
- * Needed axial charge realistic:
 - \sim percent of initial entropy density, or $n_5 \sim (0.2\text{GeV})^3$!
- * Data could be quantitatively consistent with CME+backgrounds!

Further Predictions for Future Test

[Yi Yin, JL, PLB2016, arXiv:1504.06906]



Anomalous effects:
parton level transport \rightarrow
at freeze-out, combining into
identified hadron observables
in specific patterns:
“chemistry”

*With parameters already
fixed in our computations,
we make predictions for
identified hadron pair
correlations: to be tested!*

*Cautionary remarks:
CME only,
for same charge pair only,
and including TMC only.*