

# Production of heavy Higgs bosons and decay into top quarks at the LHC

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in collaboration with

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based on [PhysRevD.93.034032/ arXiv:1511.05584](#)



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- **2012: Discovery of the Higgs** [ATLAS, Phys. Lett. B716 (2012) 1; CMS, Phys. Lett. B716 (2012) 30]  
→ at least 1 type of scalar elementary particle exists in nature
- Are there other types of spin-0 bosons (different masses, pseudoscalars)? For example: another Higgs-doublet → 2HDM, SUSY
- Heavy Higgs bosons are experimentally less constrained than additional light Higgs bosons
- high mass and Yukawa coupling  $\sim m_f \rightarrow$  study resonance in the  $t\bar{t}$  decay channel

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# 2-Higgs-Doublet Model (2HDM) in a nutshell

- $$\Phi_1 = \begin{pmatrix} \xi_1^+ \\ \frac{1}{\sqrt{2}}(v_1 + \phi_1 + i\chi_1) \end{pmatrix}, \quad \Phi_2 = \begin{pmatrix} \xi_2^+ \\ \frac{1}{\sqrt{2}}(v_2 + \phi_2 + i\chi_2) \end{pmatrix}$$

CP conserving case

CP violating case

$$\begin{aligned} h &= -\phi_1 \sin \alpha + \phi_2 \cos \alpha \\ H &= \phi_1 \cos \alpha + \phi_2 \sin \alpha \\ A &= -\chi_1 \sin \beta + \chi_2 \cos \beta \end{aligned} \quad \begin{pmatrix} \phi_1 \\ \phi_2 \\ \phi_3 \end{pmatrix} = R(\alpha_1, \alpha_2, \alpha_3) \begin{pmatrix} \phi_1 \\ \phi_2 \\ A \end{pmatrix}$$

$$H^+ = -\xi_1^+ \sin \beta + \xi_2^+ \cos \beta$$

- $$\tan \beta = \frac{v_2}{v_1}$$

- top-Yukawa coupling:  $\mathcal{L}_{\text{Yuk},t} = -\frac{m_t}{v} \sum_j \bar{t}(a_{jt} - ib_{jt}\gamma_5)t\phi_j$
- reduced Yukawa couplings  $a_t, b_t$  depend on  $\alpha$  or  $\alpha_1, \alpha_2, \alpha_3$  and  $\beta$
- use flavour conserving **type-II 2HDM** ( $d_R, \ell_R$  couple to  $\Phi_1$ ,  $u_R$  couple to  $\Phi_2$ ) because of strong exp. constraints on FCNC

for details see, e.g.: [Branco, Ferreira, Lavoura, Rebelo, Sher, Silva, arXiv:1106.0034]

# 2HDM-Type-II Scenarios

## CP-conserving scenario I and II

study:  $\tan\beta = 0.7$ ,  $\alpha = \beta - \frac{\pi}{2}$

	$h$	$H$	$A$
$a_t$	1	1.43	0
$b_t$	0	0	1.43
$f_{VV}$	1	0	0
$m(\text{I})$ [GeV]	125	<b>550</b>	<b>510</b>
$\Gamma(\text{I})$ [GeV]	0.004	34.56	49.28
$m(\text{II})$ [GeV]	125	<b>550</b>	<b>700</b>
$\Gamma(\text{II})$ [GeV]	0.004	34.49	75.28

## CP-violating scenario III

study:  $\tan\beta = 0.7, \alpha_1 = \beta,$

$$\alpha_2 = \frac{\pi}{15}, \alpha_3 = \frac{\pi}{4}$$

	$\phi_1$	$\phi_2$	$\phi_3$
$a_t$	<b>0.98</b>	0.86	-1.16
$b_t$	<b>0.30</b>	0.99	0.99
$f_{VV}$	<b>0.98</b>	-0.15	-0.15
$m(\text{III})$ [GeV]	125	<b>500</b>	<b>800</b>
$\Gamma(\text{III})$ [GeV]	0.004	36.55	128.16

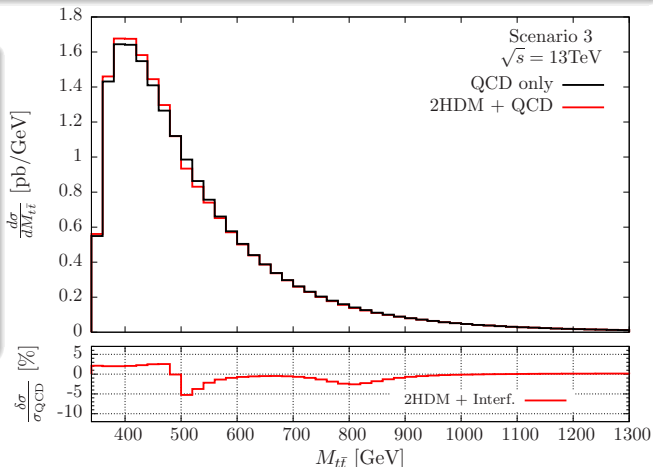
- $h, \phi_1$  SM-like (by construction, so-called “alignment limit”)
- H,A-Yukawa coupling to  $t$  quark  $a_t, b_t = \cot\beta = 1.43 \Rightarrow$  enhanced
- H,A-Yukawa coupling to  $b$  quark  $a_b, b_b = \tan\beta \Rightarrow$  suppressed  $\rightarrow$  save to neglect
- $f_{VV}$ : coupling to vector bosons
- $m$ : free parameter;  $\Gamma$  fixed by mass and couplings
- CPC-case I: mass degenerate; CPC-case II: mass non-degenerate

## QCD contribution

$$\mathcal{A}_{\text{QCD}} = \text{[tree-level gluon exchange]} + \text{[gluon loop]} + \text{[gluon loop]} + \text{[gluon loop]}$$

## (pseudo-)scalar contribution

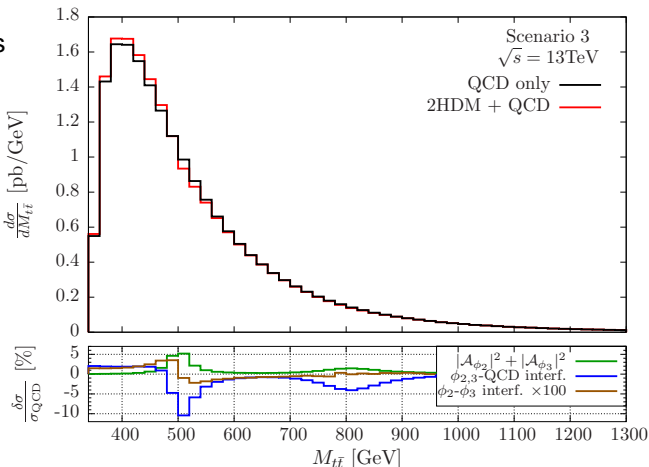
$$\mathcal{A}_{\phi_j} = \text{[gluon loop]} \rightarrow \phi_j \rightarrow \text{[quark lines]}$$





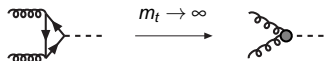
# Different Contributions to the Leading Order

- effect of 2HDM most prominent in the **resonant region**
- **interference with QCD** very important
- interference effects between different CPV scalars negligible
- How large are the contributions from the NLO QCD corrections?



# Next-to-Leading Order – Heavy Top-Quark Limit

- LO is already a 1-loop calculation  $\Rightarrow$  NLO requires a 2-loop calculation
- use effective  $gg\phi$  vertex:



$$\mathcal{L}_{\text{eff}} = (f_S G_{\mu\nu}^a G_a^{\mu\nu} + f_P \epsilon_{\mu\nu\rho\sigma} G_a^{\mu\nu} G_a^{\rho\sigma}) \phi$$

- effective theory : leading order in the  $1/m_t$  expansion of the  $gg\phi$  vertex
- take higher orders of  $1/m_t$  into account by **using K-factor** [Krämer, Laenen, Spira 1996]

$$\sigma_{\text{NLO}}^{\text{approx}} = \frac{\sigma_{\text{NLO}}^{\text{eff}}}{\sigma_{\text{LO}}^{\text{eff}}} \sigma_{\text{LO}}^{\text{full}}$$

- good approximation for  $pp \rightarrow HX$   
Assumption: also valid for  $|pp \rightarrow \phi \rightarrow t\bar{t}|^2$
- no K-factor for QCD-interference

LO: significant heavy Higgs contributions only in resonance region



NLO: restrict the calculation to the resonance region

- ⇒ extract resonance/pole contribution by applying **soft gluon approximation**
- ⇒ **non-factorizing contributions** from real and virtual corrections **cancel exactly** in soft gluon approximation [Fadin et al. '94, Melnikov et al. '96, Beenakker et al. '97, Dittmaier et al. 2014]

# NLO Results - Inclusive Cross Section

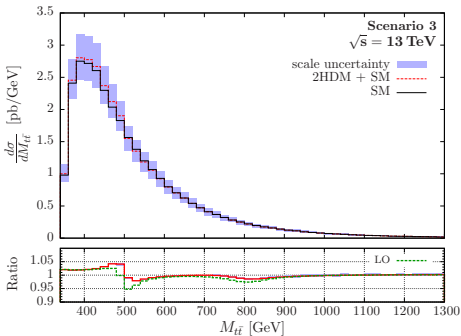
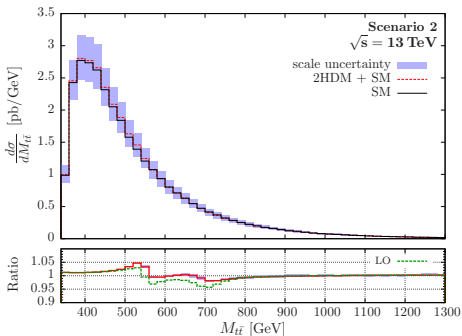
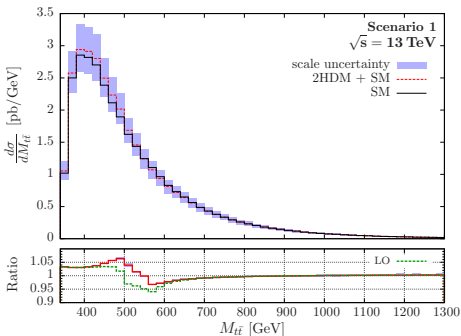
	Scenario 1	Scenario 2	Scenario 3
$\mu_0$ [GeV]	265	312.5	325
$\sigma_{\text{QCDW}}$ [pb]	$643.22^{+81.23}_{-77.71}$	$624.25^{+80.98}_{-76.19}$	$619.56^{+81.05}_{-75.72}$
$\sigma_{2\text{HDM}}$ [pb]	$13.59^{+1.85}_{-1.64}$	$7.4^{+0.77}_{-0.78}$	$7.21^{+0.81}_{-0.77}$
$\sigma_{2\text{HDM}}/\sigma_{\text{QCDW}}$ [%]	2.1	1.2	1.2

$$\mu_0 = \mu_R = \mu_F = \frac{m_2 + m_3}{4}$$

$$\mu \text{ variation: } \mu = \frac{\mu_0}{2}, \mu_0, 2\mu_0$$

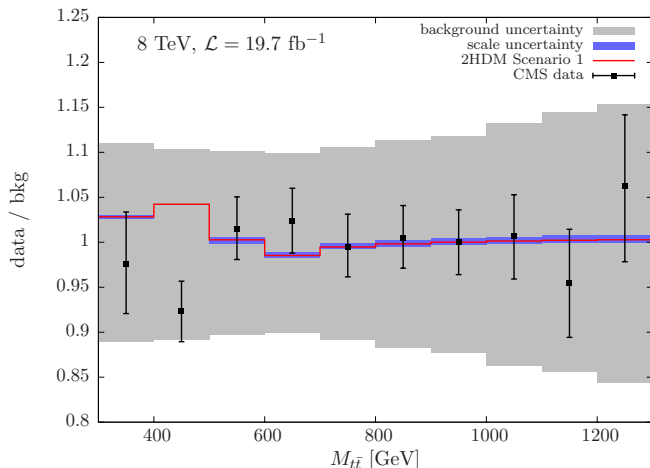
inclusive cross section shows only **little sensitivity** to heavy Higgs contribution  
(not yet constrained by measurement:  $\delta\sigma_{\tilde{t}\tilde{t}}^{\text{exp}} \sim 5\%$ )

⇒ study more sensitive observables



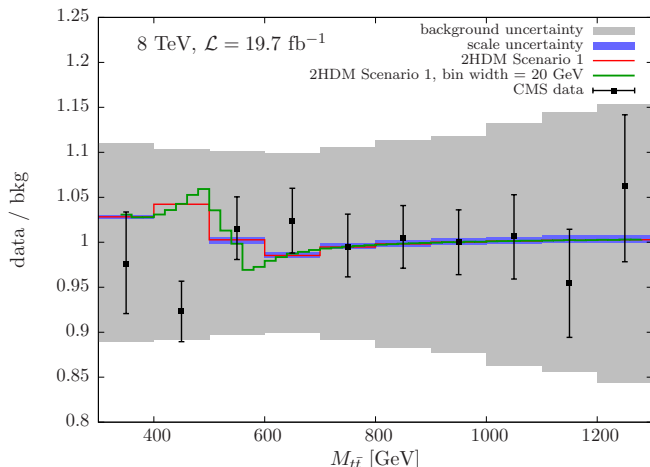
- heavy Higgs NLO corrections **small w.r.t. to QCD background**
- heavy Higgs NLO corrections **important w.r.t. the heavy Higgs LO**
- **strongest effect in the mass degenerate case** where resonances overlap

# Comparison with CMS [arXiv:1309.2030]



scenario 1 cannot be excluded by this measurement  
because of background uncertainty

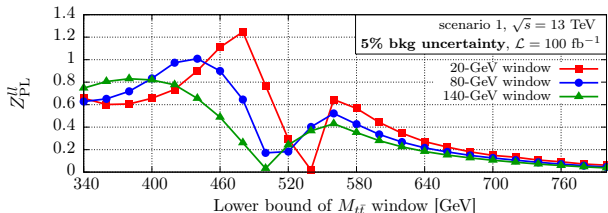
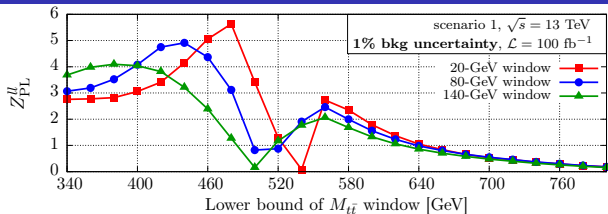
# Comparison with CMS [arXiv:1309.2030]



How to avoid **peak-dip cancellation** and find resonance experimentally?

- use smaller  $M_{t\bar{t}}$  bins: new ATLAS analysis (also incl. interference)  
see talk by Danilo Enoque Ferreira De Lima on Saturday in BSM session
- here: use sliding  $M_{t\bar{t}}$  window

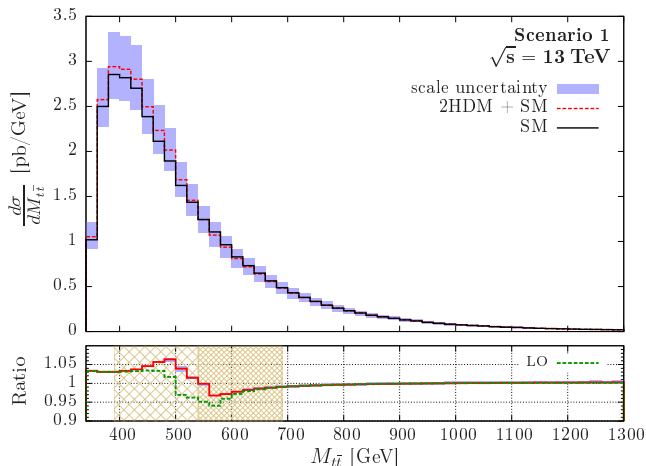
# Signal Significance @NLO



- estimate significance from  $N_s$  and  $N_b$  in different  $M_{t\bar{t}}$  windows
- smaller **bin width**  $\rightarrow$  significance  $Z_{PL}$  larger
- smaller **background uncertainty**  $\rightarrow$  significance  $Z_{PL}$  larger
- precision measurements crucial

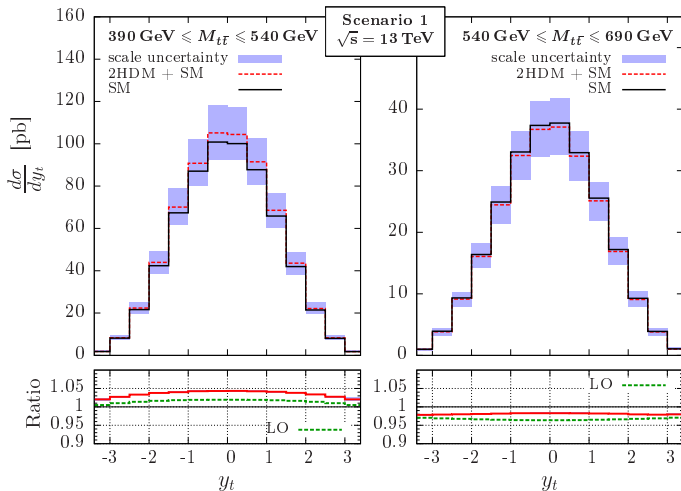


# NLO Results – Applied Cuts



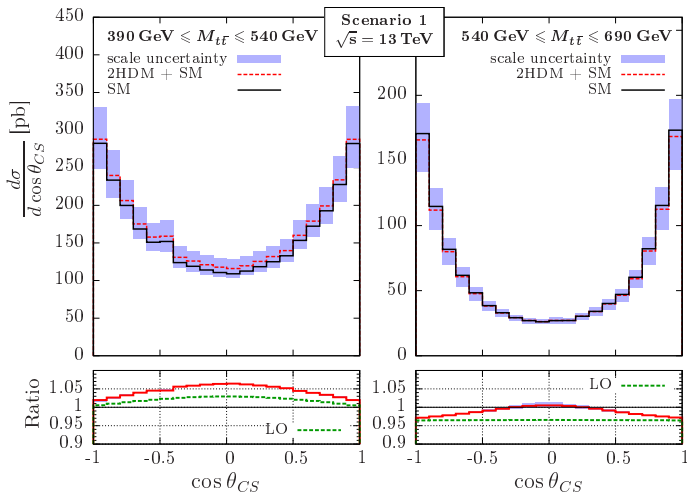
- Note: approximation valid only in resonance region
- avoid peak-dip cancellation in other observables, e.g.  $y_t$ ,  $\cos\theta_{CS}$  by applying cuts below and above the resonance to estimate maximal effect

# Results - Rapidity Distribution $y_t$



- NLO slightly increases effect above the resonance in the central region  
 $\Rightarrow$  **highest sensitivity in central region**
- NLO decreases effect below the resonance

# Results - Cosine of Collins Soper Angle $\cos\theta_{CS}$



- $\theta_{CS}$  defined in  $t\bar{t}$  ZMF (@LO same as scattering angle)
- largest effects in central region:  $\sim 7\%$  in lower  $M_{t\bar{t}}$  bin

# Results - Spin Dependent Observables

Try to increase signal/background ratio by analysing spin dependent observables, e.g. **spin correlations**

$$C_{aa} = -4 \langle (\mathbf{S}_t \cdot \hat{\mathbf{a}}) (\mathbf{S}_{\bar{t}} \cdot \hat{\mathbf{a}}) \rangle$$

$\mathbf{S}_t$  and  $\mathbf{S}_{\bar{t}}$  are the spin operators of  $t$  and  $\bar{t}$ , respectively

choosing three different axes

$$\hat{\mathbf{a}} = \{\hat{\mathbf{k}}, \hat{\mathbf{n}}, \hat{\mathbf{r}}\}$$

$\hat{\mathbf{k}}$ : direction of top quark in  $t\bar{t}$  ZMF,  $\hat{\mathbf{n}}, \hat{\mathbf{r}}$  directions perpendicular to  $\hat{\mathbf{k}}$

correlations have direct interpretation as **expectation values of angular distributions**, e.g. in the leptonic decay of  $t\bar{t}$

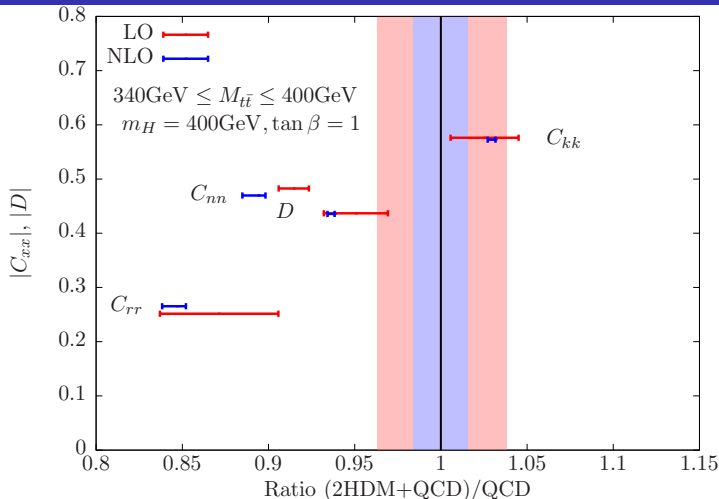
$$C_{kk} \sim \langle \cos \theta_+ \cos \theta_- \rangle$$

$\theta_{\pm}$ : angle between  $\ell^{\pm}$  and  $t$  ( $\bar{t}$ ) in the  $t$  ( $\bar{t}$ ) rest frame

Form  $C_{aa}$  construct **opening angle correlation**:

$$D = \langle \mathbf{S}_t \cdot \mathbf{S}_{\bar{t}} \rangle = -\frac{1}{3} (C_{kk} + C_{nn} + C_{rr})$$

# Results - Spin Correlations @NLO



- model: scalar heavy Higgs boson,  $m_H = 400$  GeV, SM Yukawa couplings
- chosen  $M_{\tilde{t}\tilde{t}}$  cut to enhance signal/background ratio
- $C_{rr}$  shows strongest effect (Sig./Bkg. ratio  $\sim 15\%$ )
- compare with Sig./Bkg. ratio of cross section in the same  $M_{\tilde{t}\tilde{t}}$  bin:  $\sim 4\%$

- heavy Higgs-QCD interference must be taken into account
- NLO effect large w.r.t. Higgs-only cross section but small w.r.t. QCD background
- NLO effects from heavy Higgs bosons can be enhanced by appropriate  $M_{\tilde{t}\tilde{t}}$  cuts
- $m_\phi$  unknown  $\rightarrow$  scan  $M_{\tilde{t}\tilde{t}}$  to avoid cancellation from peak-dip structure
- strong significance in  $d\sigma/dM_{\tilde{t}\tilde{t}}$  only achievable by reducing background uncertainty
- $\frac{d\sigma}{d\cos\theta_{CS}}$  is most sensitive observables among the spin independent observables studied so far
- spin correlations with an additional cut on  $M_{\tilde{t}\tilde{t}}$  have higher sensitivity than spin independent observables

Thank you for your attention!

# Additional Material



## 2-Higgs-Doublet Model (2HDM) – Yukawa Couplings

$$\mathcal{L}_{\Phi, \text{Yuk}} \supset -\bar{Q}_L [(\lambda_1^d \Phi_1 + \lambda_2^d \Phi_2) d_R + (\lambda_1^u \tilde{\Phi}_1 + \lambda_2^u \tilde{\Phi}_2) u_R] + \text{h.c.}$$

$$\tilde{\Phi}_i = i\tau_2 \Phi_i^*$$

Flavour conserving 2HDMs:

Type	$u_R$	$d_R$	$\ell_R$
I	$\Phi_2$	$\Phi_2$	$\Phi_2$
II	$\Phi_2$	$\Phi_1$	$\Phi_1$
Lepton-specific (X)	$\Phi_2$	$\Phi_2$	$\Phi_1$
Flipped (Y)	$\Phi_2$	$\Phi_1$	$\Phi_2$

$\mathcal{L}_{\text{Yuk}}$  in terms of Higgs mass eigenstates  $\phi_j$ :

$$\mathcal{L}_{\text{Yuk}} \supset -\sum_j \left[ \frac{m_u}{v} \bar{u} (a_{ju} - ib_{ju} \gamma_5) u + \frac{m_d}{v} \bar{d} (a_{jd} - ib_{jd} \gamma_5) d \right] \phi_j$$

$$a_{ju} = \frac{R_{j2}}{\sin \beta}, \quad b_{ju} = R_{j3} \cot \beta, \quad a_{jd} = \frac{R_{j1}}{\cos \beta}, \quad b_{jd} = R_{j3} \tan \beta, \quad v = \sqrt{v_1^2 + v_2^2}$$

## 2-Higgs-Doublet Model (2HDM) – Gauge Couplings

Higgs-Gauge couplings are derived from  $\mathcal{L}_{\Phi,\text{kin}}$

$$\begin{aligned}\mathcal{L}_{\Phi,\text{kin}} &= (D_\mu \Phi_1)^\dagger (D^\mu \Phi_1) + (D_\mu \Phi_2)^\dagger (D^\mu \Phi_2) \\ &= \mathcal{L}_{VV\Phi} + \mathcal{L}_{VV\Phi\Phi} + \mathcal{L}_{WZ\Phi\Phi} + \mathcal{L}_{W\gamma\Phi\Phi} + \mathcal{L}_{Z\Phi\Phi} + \mathcal{L}_{W\Phi\Phi} + \mathcal{L}_{\gamma\Phi\Phi}\end{aligned}$$

relevant terms for decay width

$$\begin{aligned}\mathcal{L}_{VV\Phi} &= f_{VV\phi_i} \left( \frac{2m_W^2}{v} W_\mu^+ W^{-\mu} + \frac{m_Z^2}{v} Z_\mu Z^\mu \right) \phi_i \\ \mathcal{L}_{Z\Phi\Phi} &= \frac{m_Z}{v} f_{Z\phi_j\phi_k} (\phi_j \overleftrightarrow{\partial}_\mu \phi_k) Z^\mu\end{aligned}$$

with

$$\begin{aligned}f_{VV\phi_i} &= R_{i1} \cos \beta + R_{i2} \sin \beta \\ f_{Z\phi_j\phi_k} &= (R_{i2} R_{j3} - R_{i3} R_{j2}) \cos \beta + (R_{i3} R_{j1} - R_{i1} R_{j3}) \sin \beta\end{aligned}$$

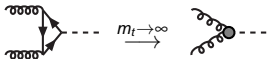
# Next-to-Leading Order – Effective $gg\phi$ Vertex

LO is already a 1-loop calculation

$\Rightarrow$  NLO is a 2-loop calculation

Use effective  $gg\phi$  vertex:

$$\mathcal{L}_{\text{eff}} = (f_S G_{\mu\nu}^a G_a^{\mu\nu} + f_P \varepsilon_{\mu\nu\rho\sigma} G_a^{\mu\nu} G_a^{\rho\sigma}) \phi$$



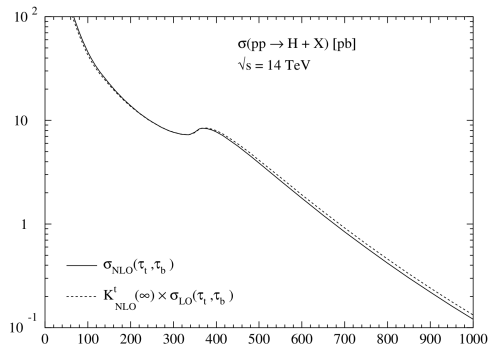
Effective theory : leading order in the  $1/m_t$  expansion of the  $gg\phi$  vertex

$\rightarrow$  take higher orders of  $1/m_t$  into account by using K-factor

[Krämer, Laenen, Spira 1996]

$$\sigma_{\text{NLO}}^{\text{approx}} = \frac{\sigma_{\text{NLO}}^{\text{eff}}}{\sigma_{\text{LO}}^{\text{eff}}} \sigma_{\text{LO}}^{\text{full}}$$

Good approximation for Higgs production:

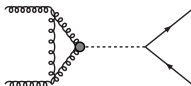


- major part of NLO QCD corrections originates from soft/collinear gluons which do not resolve the effective coupling
- here we assume that this is true for the process  $pp \rightarrow \phi \rightarrow t\bar{t}$  as well

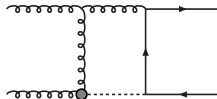
# Next-to-Leading Order – Soft Gluon Approximation

- Seen in LO: significant contributions from the extended Higgs sector to  $t\bar{t}$  production only in resonance region
- at NLO: restrict the calculation to the resonance region

a) factorizing contributions, e.g.



b) non-factorizing contributions, e.g.



- extract pole contribution by soft gluon approximation

$$\xrightarrow{l \rightarrow 0} \sim \frac{1}{s - m_\phi^2 + i\Gamma_\phi m_\phi}$$

⇒ non-factorizing contributions from real and virtual corrections cancel

$$\left( \text{Diagram 1} \right) \left( \text{Diagram 2} \right)^* + \left( \text{Diagram 3} \right) \left( \text{Diagram 4} \right)^* \Big|_{\text{soft-gluon approx.}} = 0$$

## Leading Order Matrix Elements

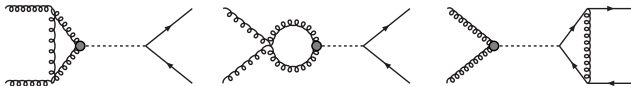
$$\begin{aligned} |\overline{\mathcal{M}}_\phi|^2 &= \frac{s^3 m_t^3}{2C_{FV}^2} \left\{ (|\tilde{f}_{S_2}|^2 + 4|\tilde{f}_{P_2}|^2)(a_{2t}^2 \beta_t^2 + b_{2t}^2) + (|\tilde{f}_{S_3}|^2 + 4|\tilde{f}_{P_3}|^2)(a_{3t}^2 \beta_t^2 + b_{3t}^2) \right. \\ &\quad \left. + 2(\operatorname{Re}[\tilde{f}_{S_2} \tilde{f}_{S_3}^*] + \operatorname{Re}[\tilde{f}_{P_2} \tilde{f}_{P_3}^*])(a_{2t} a_{3t} \beta_t^2 + b_{2t} b_{3t}) \right\} \\ 2\overline{\operatorname{Re}[\mathcal{A}_\phi \mathcal{A}_{\text{QCD}}^*]} &= -\frac{4\pi\alpha_s m_t^2 s}{C_A C_{FV}(1 - \beta^2 z^2)} \left\{ (a_{2t} \beta_t^2 \operatorname{Re}[\tilde{f}_{S_2}] - 2b_{2t} \operatorname{Re}[\tilde{f}_{P_2}]) \right. \\ &\quad \left. + (a_{3t} \beta_t^2 \operatorname{Re}[\tilde{f}_{S_3}] - 2b_{3t} \operatorname{Re}[\tilde{f}_{P_3}]) \right\} \end{aligned}$$

# Resonant Contributions

The resonant contributions can be divided into

## 1. Factorizing Diagrams

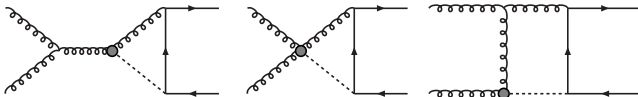
→ scalar propagator as coefficient; divide into scalar prod. and decay



(simpler to calculate, known from literature)

## 2. Non-Factorizing Diagrams

→ scalar propagator in loop; no division into scalar prod. and decay possible

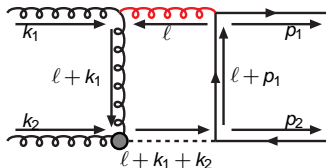


How to extract pole contribution  $\frac{1}{s - m_\phi^2 + i\Gamma_\phi m_\phi}$  ?

⇒ **soft-gluon approximation**

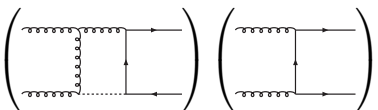
# Soft-Gluon Approximation

Example: Box Diagram



$$\xrightarrow{l \rightarrow 0} \sim \frac{1}{\hat{s} - m_\phi^2 + i\Gamma_\phi m_\phi} + \text{non-resonant terms}$$

# Soft-Gluon Approximation

Example for Virtual Correction:  \*

neglect loop momenta in the numerator  $\rightarrow$  scalar integral:

$$\int \frac{d^4 \ell}{(2\pi)^4} \frac{1}{(\ell^2 + i\epsilon)((\ell + k_1)^2 + i\epsilon)((\ell + k_1 + k_2)^2 - m_\phi^2 + i\Gamma_\phi m_\phi)((\ell + p_1)^2 - m_t^2 + i\epsilon)}$$

neglect  $\ell^2$  terms in the denominator where possible

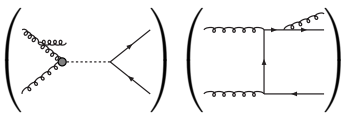
$$\int \frac{d^4 \ell}{(2\pi)^4} \frac{1}{(\ell^2 + i\epsilon)(2\ell k_1 + i\epsilon)(2\ell(k_1 + k_2) + \hat{s} - m_\phi^2 + i\Gamma_\phi m_\phi)(2\ell p_1 + i\epsilon)}$$

perform contour integration

$$\begin{aligned} & -i \int \frac{d^3 \ell}{(2\pi)^3} \frac{1}{2|\vec{\ell}| \left[ -2|\vec{\ell}|k_1^0 + 2\vec{\ell}\vec{k}_1 + i\epsilon \right] \left[ -2|\vec{\ell}|(k_1^0 + k_2^0) + 2\vec{\ell}(\vec{k}_1 + \vec{k}_2) + \hat{s} - m_\phi^2 + i\Gamma_\phi m_\phi \right] \left[ -2|\vec{\ell}|p_1^0 + 2\vec{\ell}\vec{p}_1 + i\epsilon \right]} \\ & = +i \int \frac{d^3 \ell}{(2\pi)^3} \frac{1}{2\ell^0 \left[ -2\ell k_1 + i\epsilon \right] \left[ -2\ell(k_1 + k_2) + \hat{s} - m_\phi^2 + i\Gamma_\phi m_\phi \right] \left[ 2\ell p_1 - i\epsilon \right]}; \quad \ell^0 = |\vec{\ell}| \end{aligned}$$



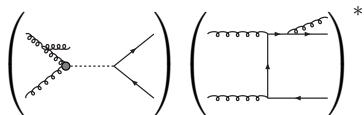
# Soft-Gluon Approximation

Example Real Correction: 

$$\rightarrow -i \int \frac{d^3 q}{(2\pi)^3 2q^0} \frac{1}{[-2qk_1 + i\epsilon] [-2q(k_1 + k_2) + \hat{s} - m_\phi^2 + i\Gamma_\phi m_\phi] [2qp_1 - i\epsilon]}$$

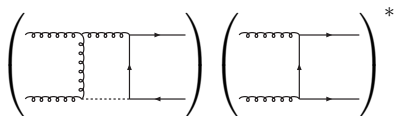
$$q^0 = |\vec{q}|$$

# Soft-Gluon Approximation



$$\rightarrow -i \int \frac{d^3 q}{(2\pi)^3 2q^0} \frac{1}{[-2qk_1 + i\epsilon] [-2q(k_1 + k_2) + \hat{s} - m_\phi^2 + i\Gamma_\phi m_\phi] [2qp_1 - i\epsilon]}$$

$$q^0 = |\vec{q}|$$

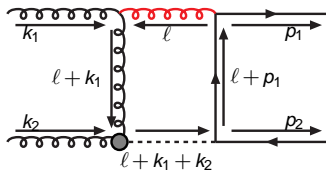


$$\rightarrow +i \int \frac{d^3 \ell}{(2\pi)^3 2\ell^0} \frac{1}{[-2\ell k_1 + i\epsilon] [-2\ell(k_1 + k_2) + \hat{s} - m_\phi^2 + i\Gamma_\phi m_\phi] [2\ell p_1 - i\epsilon]}$$

$$\ell^0 = |\vec{\ell}|$$

# Soft-Gluon Approximation

Example: Box Diagram



$$\xrightarrow{\ell \rightarrow 0} \sim \frac{1}{\hat{s} - m_\phi^2 + i\Gamma_\phi m_\phi} + \text{non-resonant terms}$$

$$\left( \text{Diagram 1} \right) \left( \text{Diagram 2} \right)^* + \left( \text{Diagram 3} \right) \left( \text{Diagram 4} \right)^* \Big|_{\text{soft-gluon approx.}} = 0$$

The equation shows four diagrams in parentheses, with the second and fourth having an asterisk. Diagram 1 is a box diagram with a red gluon line on the top-left vertex. Diagram 2 is a box diagram with a red gluon line on the top-right vertex. Diagram 3 is a diagram with a red gluon line on the top-left vertex and a dashed line connecting it to a vertex with two outgoing lines. Diagram 4 is a box diagram with a red gluon line on the top-right vertex. The entire expression is evaluated in the soft-gluon approximation, resulting in zero.

non-factorizing virtual corrections cancel with real corrections from initial and final state radiation in the soft-gluon approximation

(known effect from: [Beenakker, Chapovsky, Berends '97])

- only valid if observable is inclusive enough

# Results – Inclusive Cross Section (LO & NLO)

			$\sigma_{\text{LO}}^{\phi}$	$\sigma_{\text{NLO}}^{\phi}$	$K^{\phi}$	$\sigma_{\text{LO}}^{\phi+\text{QCD}}$	$\sigma_{\text{NLO}}^{\phi+\text{QCD}}$	$K^{\phi+\text{QCD}}$
I	8 TeV	w/o int	2.03	4.11	2.02	123.63	195.96	1.59
		w int	0.65	3.58	5.51	122.25	195.44	1.60
	13 TeV	w/o int	7.34	14.90	2.03	411.84	652.76	1.58
		w int	1.55	11.57	7.46	406.05	649.42	1.60
II	8 TeV	w/o int	0.79	1.56	1.97	115.05	187.25	1.63
		w int	0.52	1.91	3.67	114.79	187.59	1.63
	13 TeV	w/o int	3.05	6.03	1.98	385.65	624.94	1.62
		w int	1.41	6.33	4.49	384.01	625.24	1.63
III	8 TeV	w/o int	1.30	2.72	2.09	113.91	186.95	1.64
		w int	0.67	2.72	4.06	113.28	186.94	1.65
	13 TeV	w/o int	4.74	9.89	2.09	382.36	624.33	1.63
		w int	1.88	8.92	4.74	379.50	623.35	1.64

# Heavy Higgs Widths

	Scenario 1		Scenario 2		Scenario 3	
	$\Gamma_2$ [GeV]	$\Gamma_3$ [GeV]	$\Gamma_2$ [GeV]	$\Gamma_3$ [GeV]	$\Gamma_2$ [GeV]	$\Gamma_3$ eV]
$\phi_j \rightarrow tt$	34.48	49.15	34.41	71.97	32.31	85.05
$\phi_j \rightarrow VV$	0	0	0	0	1.12	5.11
$\phi_j \rightarrow \phi_1 Z$	0	0	0	0	0.65	3.24
$\phi_j \rightarrow \phi_2 Z$	0	0	0	3.14	0	31.28
$\phi_j \rightarrow \phi_1 \phi_1$	0	0	0	0	2.38	3.00
$\phi_j \rightarrow \phi_1 \phi_2$	0	0	0	0	0	0.31
$\phi_j \rightarrow gg$	0.08	0.13	0.08	0.17	0.08	0.17
Total	34.56	49.28	34.49	75.28	36.55	128.16