

Λ polarization and spin correlations in a vortical fluid

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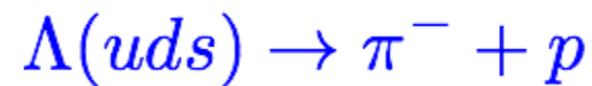
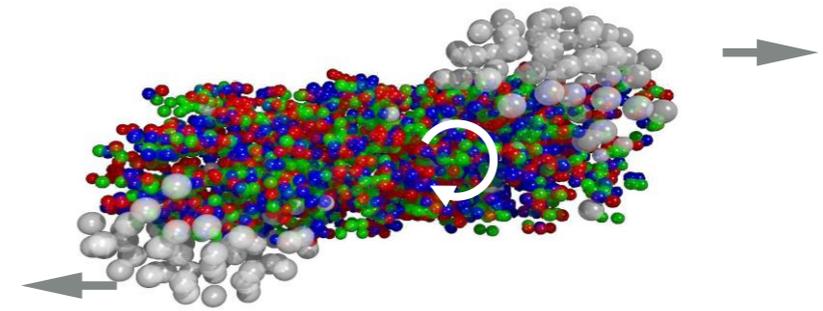
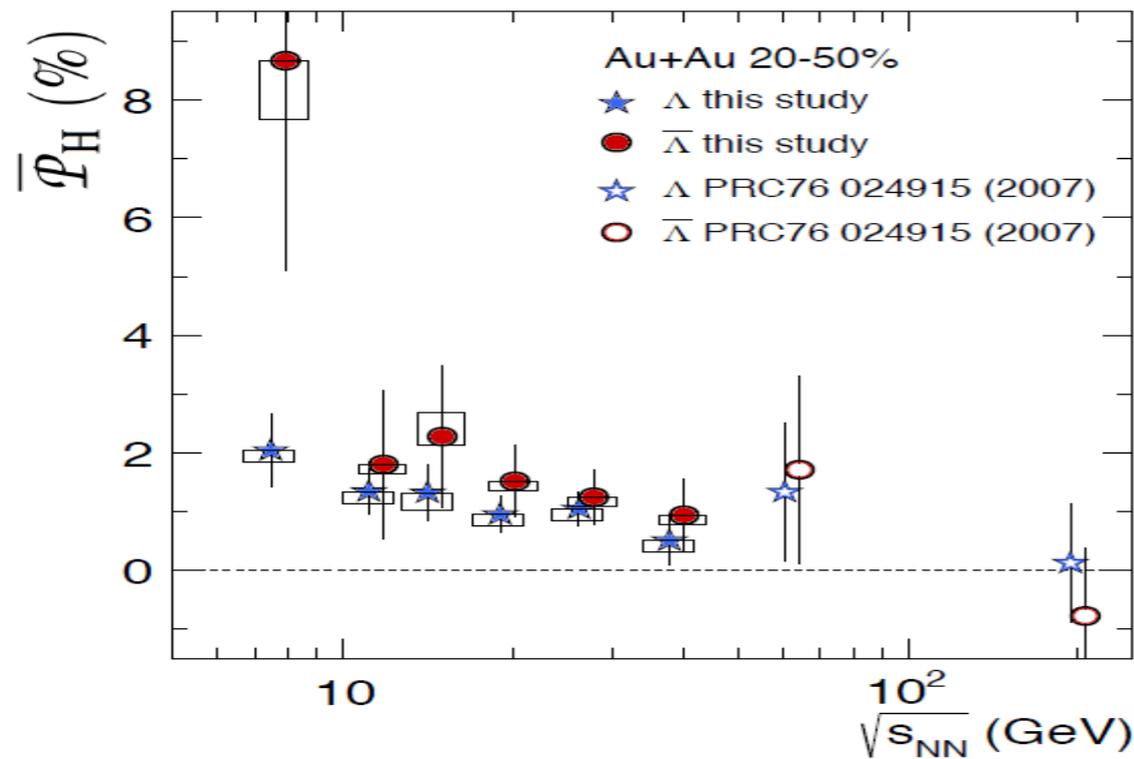
with

H. Petersen, Q. Wang and X.-N Wang

QM2017 @ Chicago



STAR collab., 1701.06657



- self analyzing
- weak decay

- Low energy > high energy

- Bjorken scaling at high energy

- Thermal vorticity

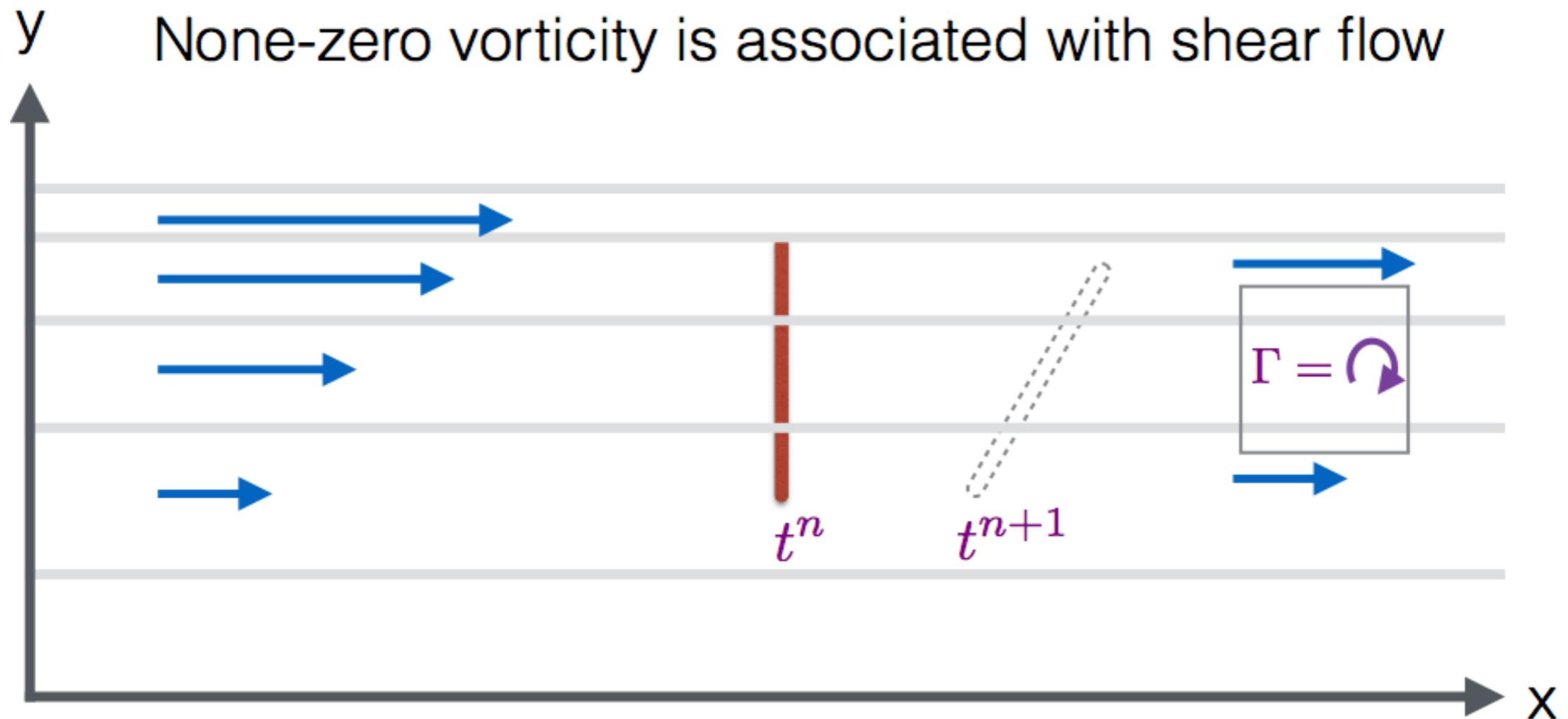
- $\bar{\Lambda} > \Lambda > 0$

- Pauli-blocking

- Spin-Magnetic coupling

Z. T. Liang, X. N. Wang, PRL. 94, 102301(2005), F. Becattini, F. Piccinini, Ann. Phys. 323, 2452 (2008); F. Becattini, F. Piccinini, J. Rizzo, PRC 77, 024906 (2008)

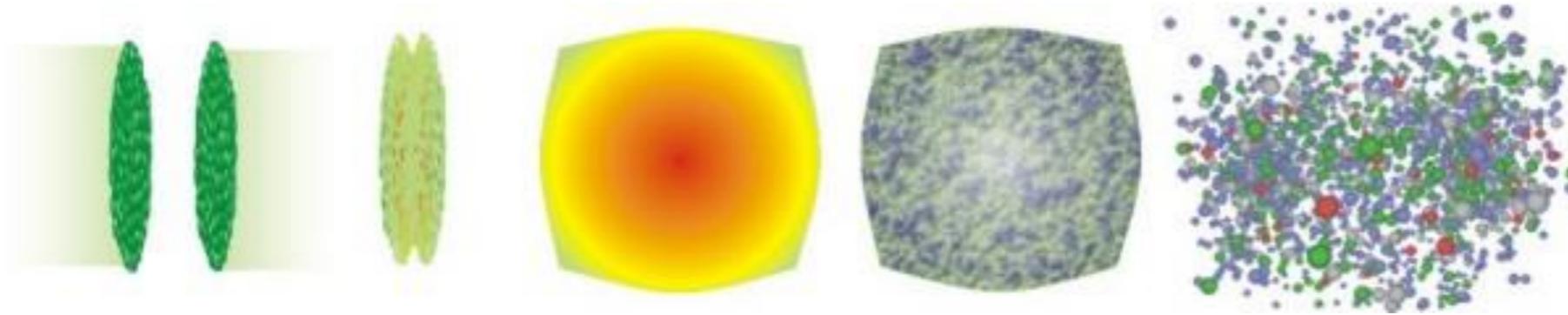
Local vorticity from fluid shear



vorticity:

$$\omega_z = \partial_x v_y - \partial_y v_x$$

circulation:
$$\Gamma = \oint \vec{v} \cdot d\vec{r} = \iint \nabla \times \vec{v} \cdot d\vec{A} = \iint \vec{\omega} \cdot d\vec{A}$$



$$\nabla_{\mu} T^{\mu\nu} = 0 \quad (1)$$

$$\Delta^{\mu\nu\alpha\beta} u^{\lambda} \nabla_{\lambda} \pi_{\alpha\beta} = -\frac{\pi^{\mu\nu} - \pi_{\text{NS}}^{\mu\nu}}{\tau_{\pi}} - \frac{4}{3} \pi^{\mu\nu} \nabla_{\lambda} u^{\lambda} \quad (2)$$

where

$$T^{\mu\nu} = (\varepsilon + P) u^{\mu} u^{\nu} - P g^{\mu\nu} + \pi^{\mu\nu} \quad (3)$$

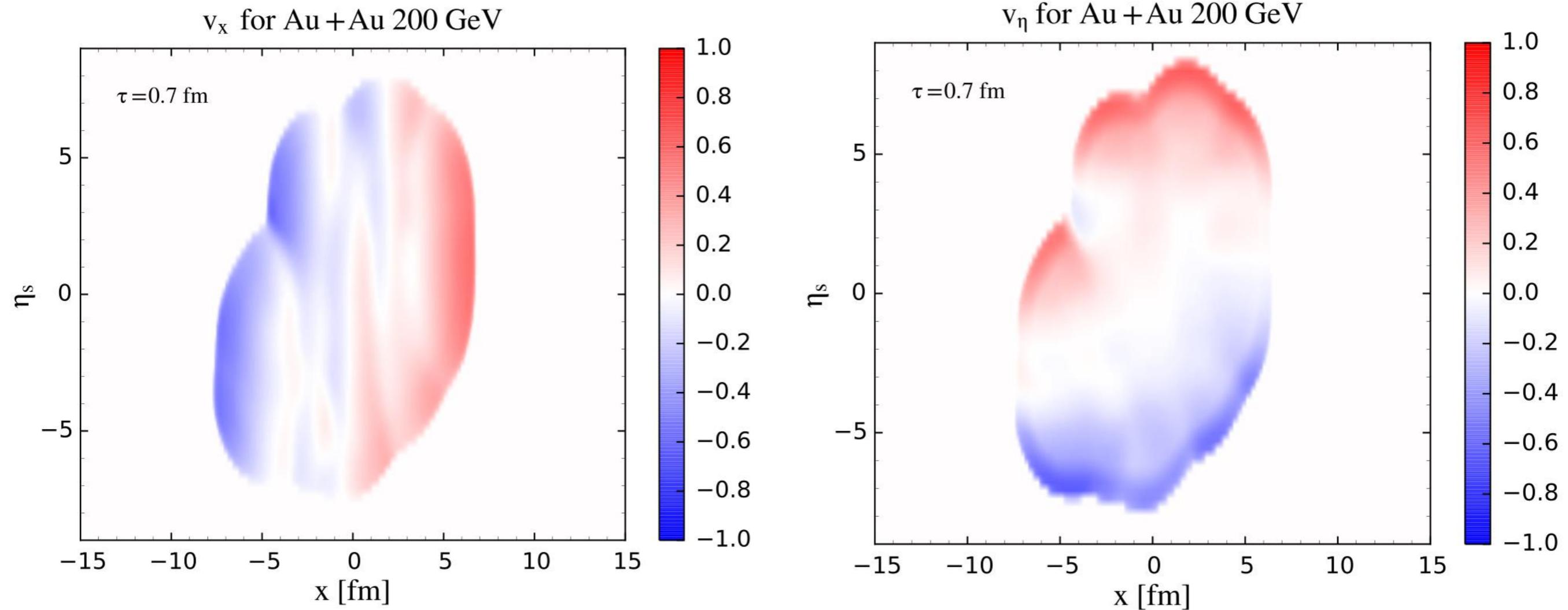
$$\Delta^{\mu\nu\alpha\beta} = \frac{1}{2} (\Delta^{\mu\alpha} \Delta^{\nu\beta} + \Delta^{\nu\alpha} \Delta^{\mu\beta}) - \frac{1}{3} \Delta^{\mu\nu} \Delta^{\alpha\beta} \quad (4)$$

$$\Delta^{\mu\nu} = g^{\mu\nu} - u^{\mu} u^{\nu}, \quad g^{\mu\nu} = \text{diag}(1, -1, -1, -\tau^{-2}) \quad (5)$$

ε and P are the energy density and pressure, u^{μ} is the fluid velocity vector. ∇_{μ} is the covariant derivative.

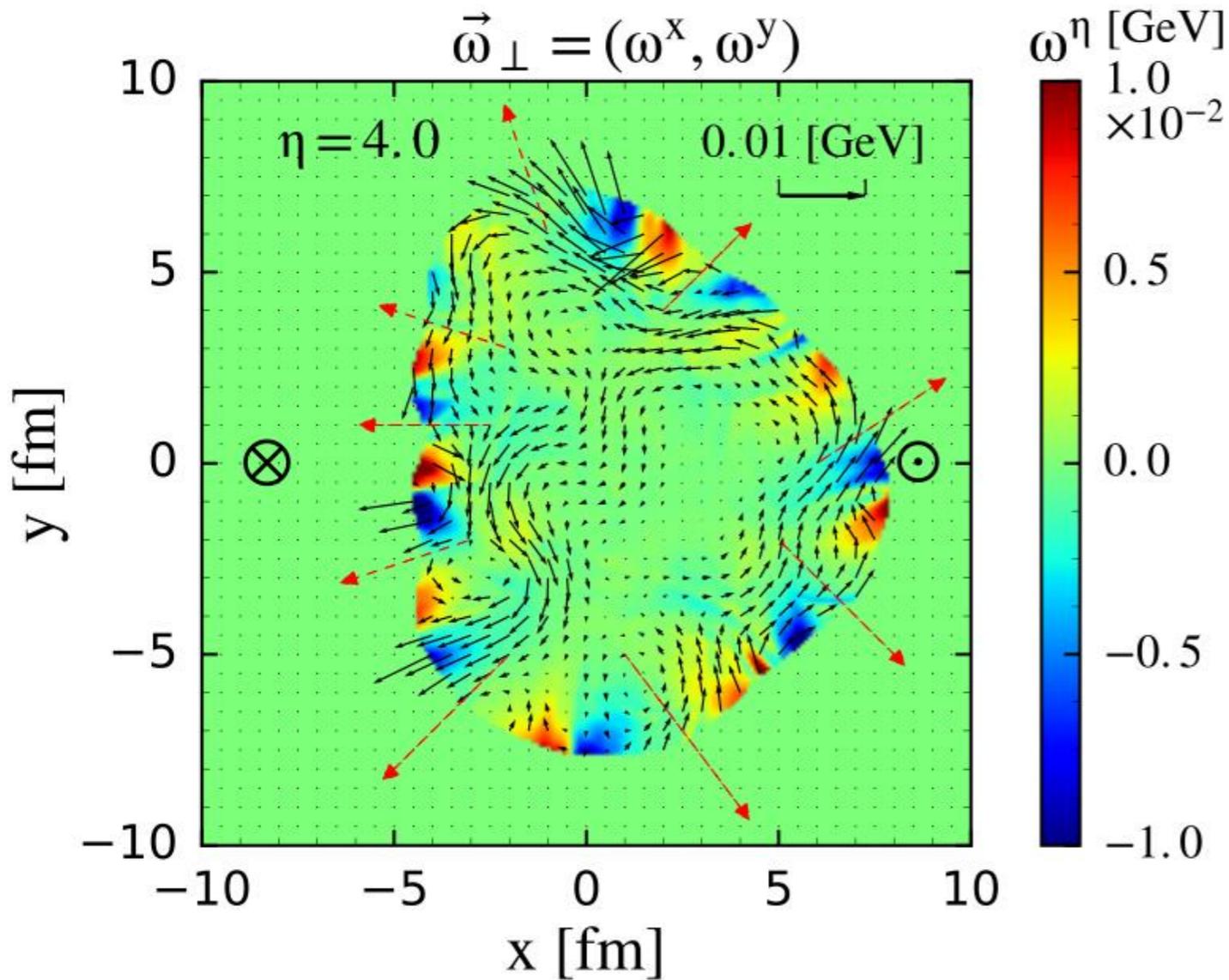
- Constraints: $P = P(\varepsilon)$, $u_{\mu} u^{\mu} = 1$, $u_{\mu} \pi^{\mu\nu} = 0$, $\pi_{\mu}^{\mu} = 0$.

Fluid shear and forward-backward asymmetry



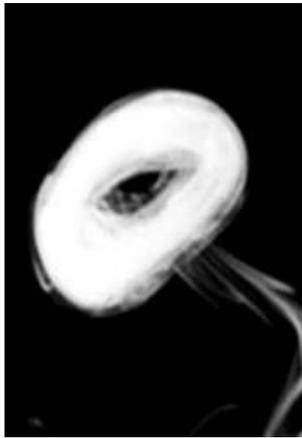
- AMPT initial condition + hydrodynamics
- Start with: $v_x = v_y = v_\eta = 0$ at $\tau = 0.4$ fm

Complex local vorticity structure

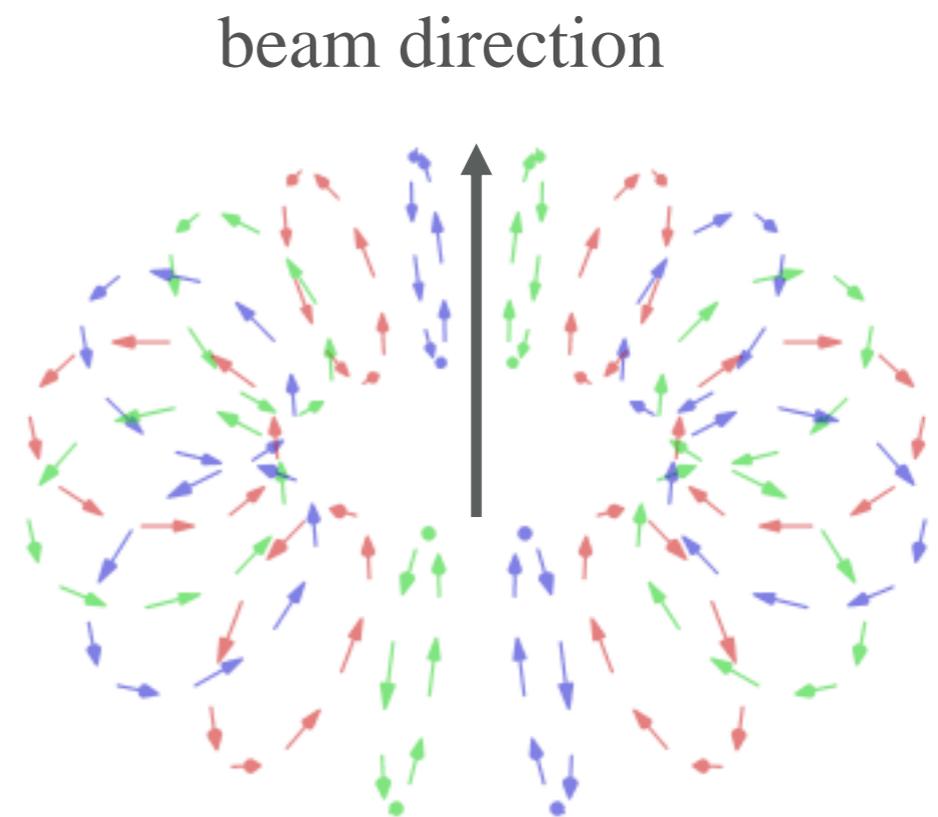


L.G.Pang, H.Petersen, Q.Wang & XNW
PRL 117, 192301 (2016)

- Vortex pair in 2D
- Vortex ring in 3D =
Toroidal (smoke ring)
vortical fluid



- Vortex ring appears in the **longitudinal direction**
- Ridge-like **vortex pairs** in the **transverse plane**.



by Lucas V. Barbosa
from Wiki Pedia

- Polarization at freezeout hypersurface

$$P^\mu \equiv \frac{d\Pi^\mu(p)/d^3p}{dN/d^3p} = \frac{\hbar}{4m} \frac{\int d\Sigma_\alpha p^\alpha \tilde{\Omega}^{\mu\nu} p_\nu n_f (1 - n_f)}{\int d\Sigma_\alpha p^\alpha n_f}$$

where $\tilde{\Omega}^{\mu\nu} = \frac{1}{2} \epsilon^{\mu\nu\rho\sigma} \partial_\rho (u_\sigma/T)$ is the thermal vorticity

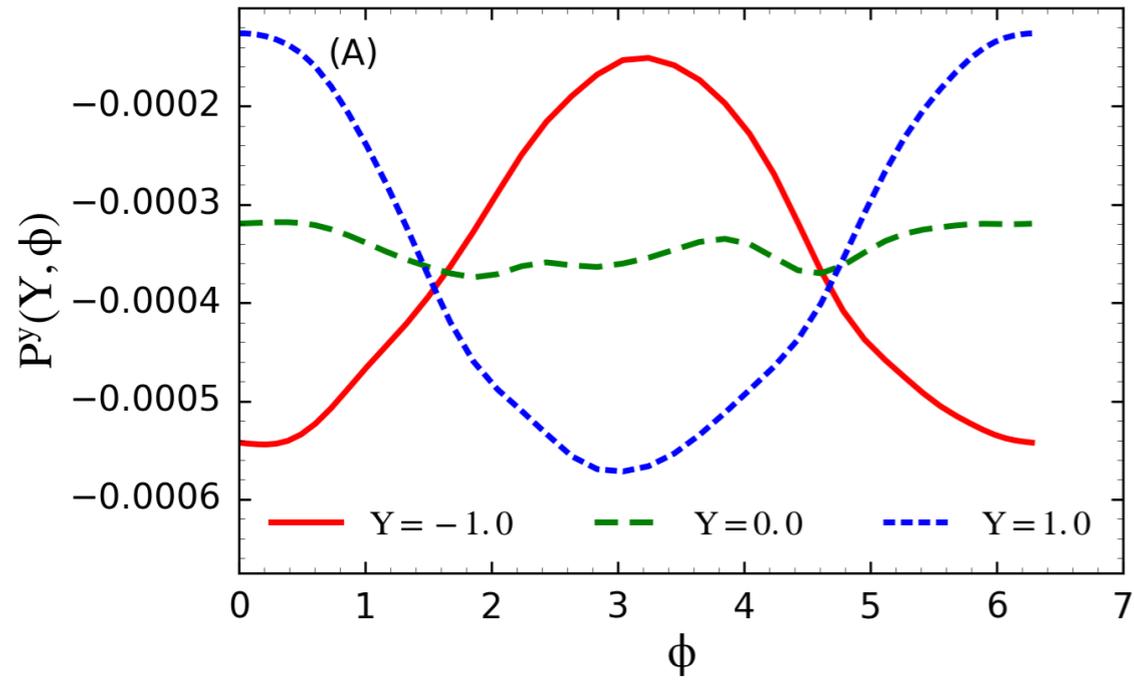
- Spatial distribution of local vorticity is correlated to momentum distribution (pt, rapidity and azimuthal angle) of baryon spin density by strong collective flow.

F. Becattini, et al., Ann. Phys. 338, 32 (2013)

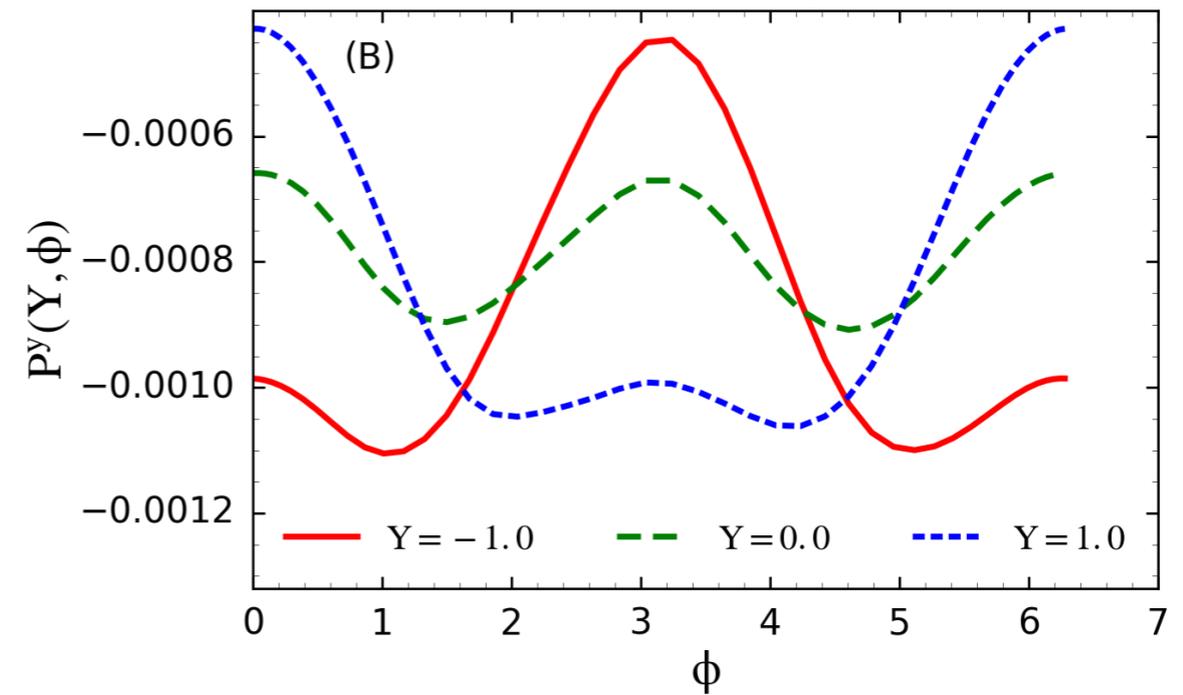
RH. Fang, LG. Pang, Q.Wang & XN.Wang, PRC 94,192301(2016)

Local polarization distributions, 20-30%

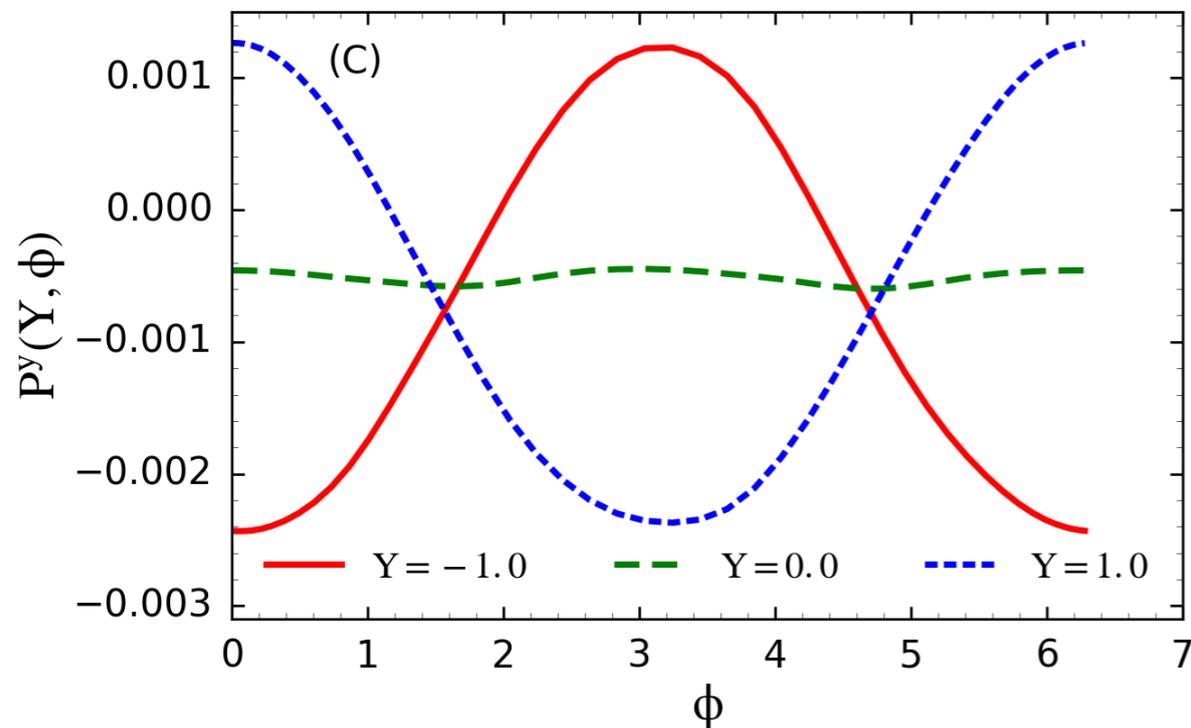
Pb + Pb 2.76 TeV, $\eta_v/s = 0.08$



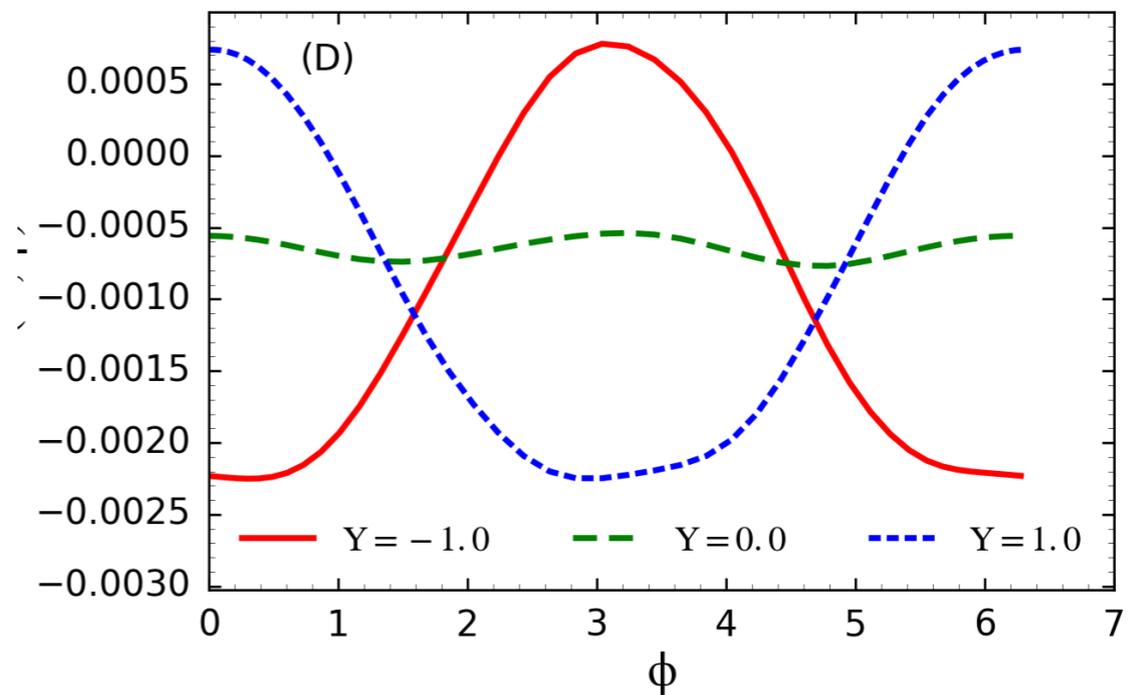
Au + Au 200 GeV, $\eta_v/s = 0.08$



Au + Au 62.4 GeV, $\eta_v/s = 0.08$

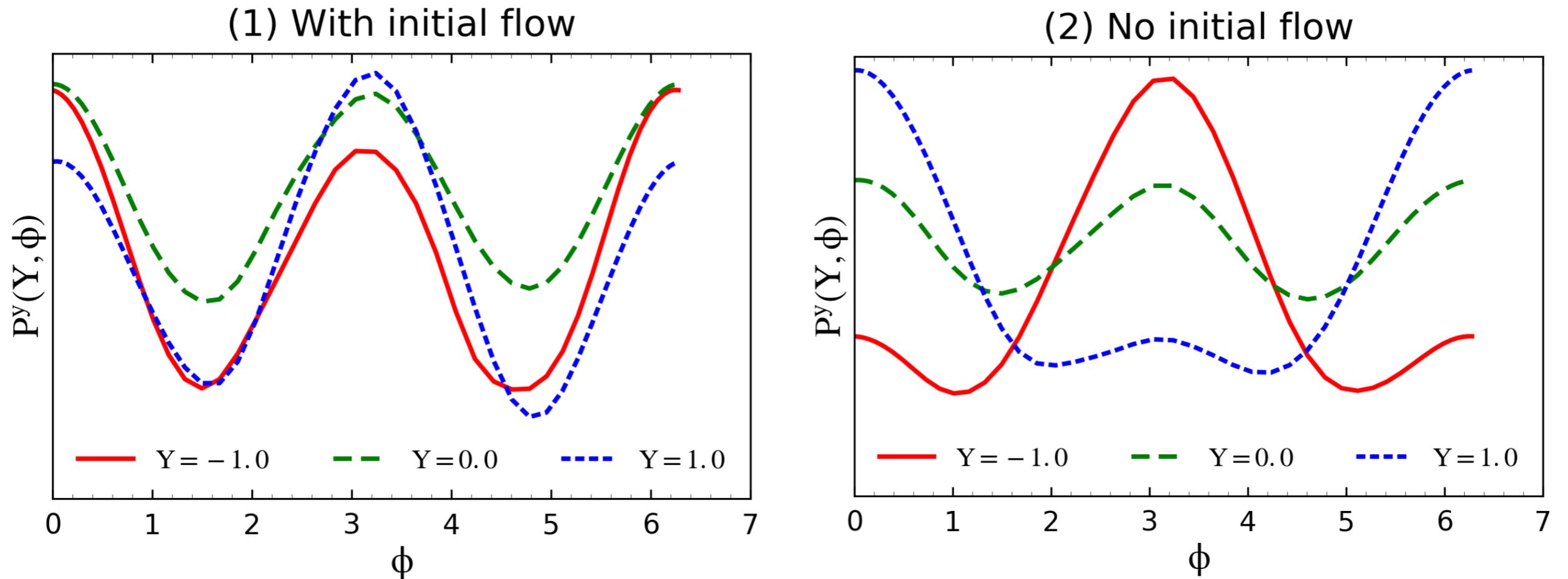


Au + Au 39 GeV, $\eta_v/s = 0.08$



- Local polarization along y direction is
 - Larger for lower beam energies
 - Larger for larger rapidities than mid-rapidity
 - Azimuthal angle distributions are anti-symmetric for forward and backward rapidity
 - For mid-rapidity, $P^y(Y, \phi) \approx P^y(Y, \phi + \pi)$
 - Shifted by global orbital angular momentum

The effect of initial fluid velocity



- $|P^y(Y, \phi) - P^y(Y, \phi + \pi)|$ is much smaller when there is initial fluid velocity
- The effect of asymmetric energy density distribution along x is suppressed by initial flow.

Effect of higher order terms in IS-equations

$$\Delta^{\mu\nu\alpha\beta} u^\lambda \nabla_\lambda \pi_{\alpha\beta} = -\frac{\pi^{\mu\nu} - \eta_v \sigma^{\mu\nu}}{\tau_\pi} - \frac{4}{3} \pi^{\mu\nu} \nabla_\lambda u^\lambda$$

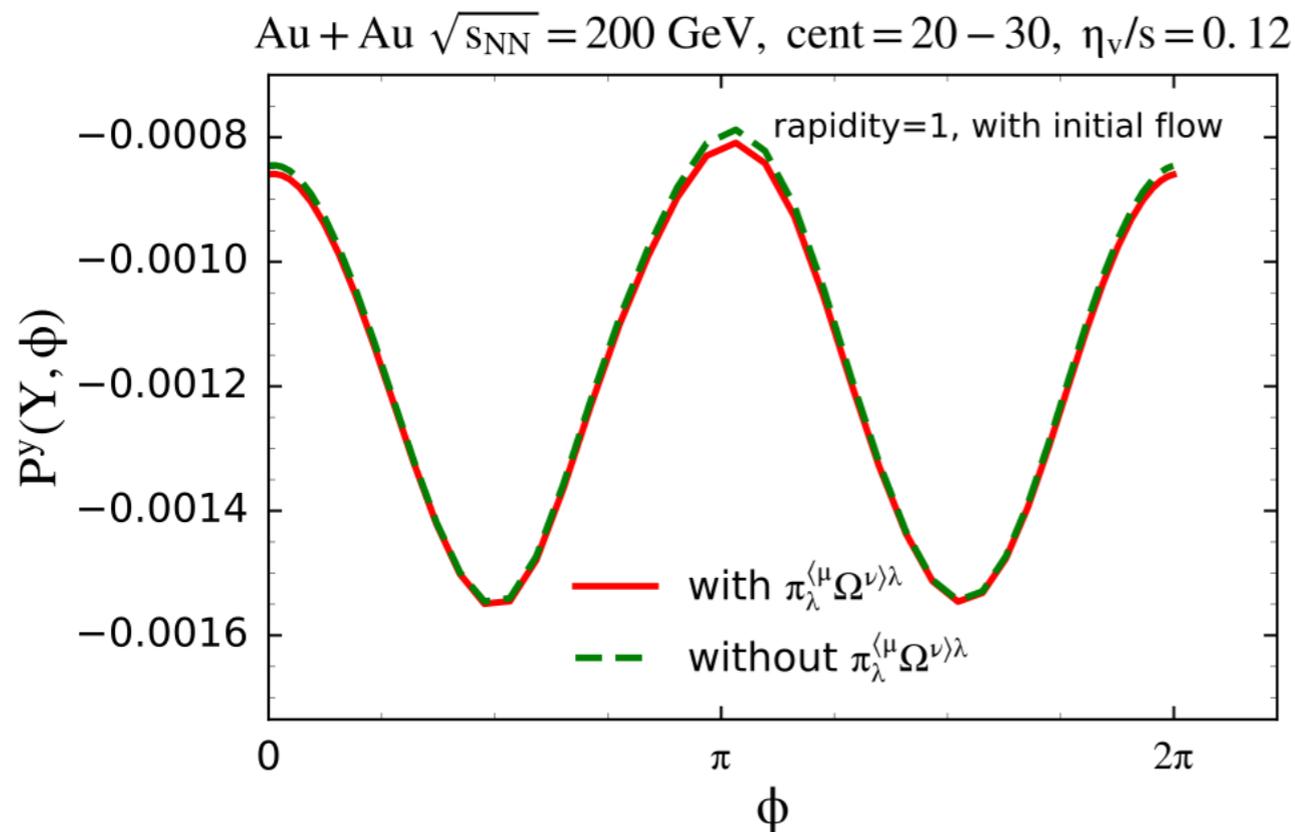
$$+ 2\pi_\lambda^{\langle\mu} \omega^{\nu\rangle\lambda} - \frac{\lambda_3}{\tau_\pi} \omega_\lambda^{\langle\mu} \omega^{\nu\rangle\lambda}$$

where

$$\omega^{\mu\nu} \equiv \frac{1}{2} \Delta^{\mu\alpha} \Delta^{\nu\beta} (\nabla_\alpha u_\beta - \nabla_\beta u_\alpha)$$

$$A^{\langle\mu\nu\rangle} \equiv \Delta^{\mu\nu\alpha\beta} A_{\alpha\beta}$$

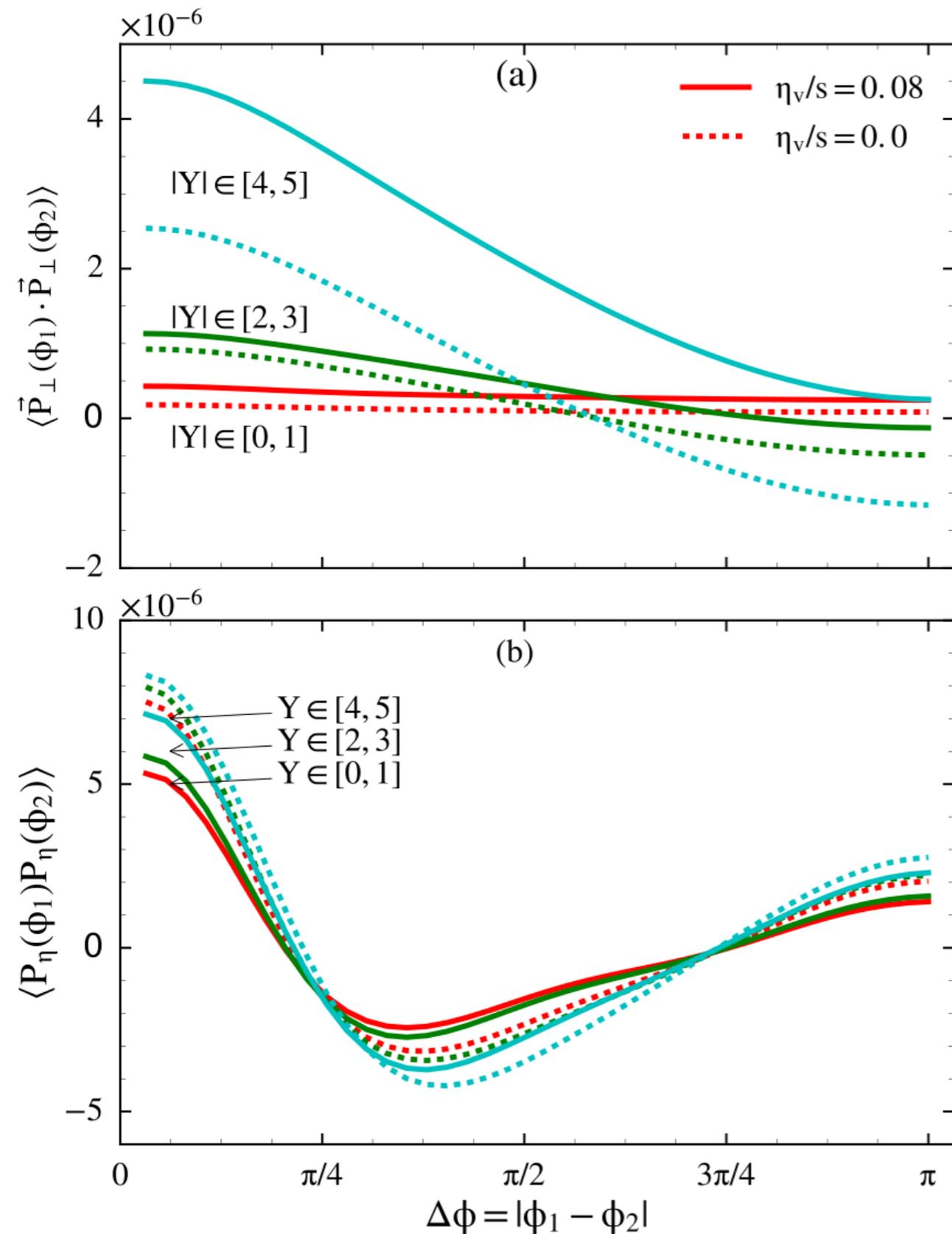
small effect



- Unknown λ_3
- For $\lambda_3 = 1$
- Code is unstable with fluctuating initial conditions

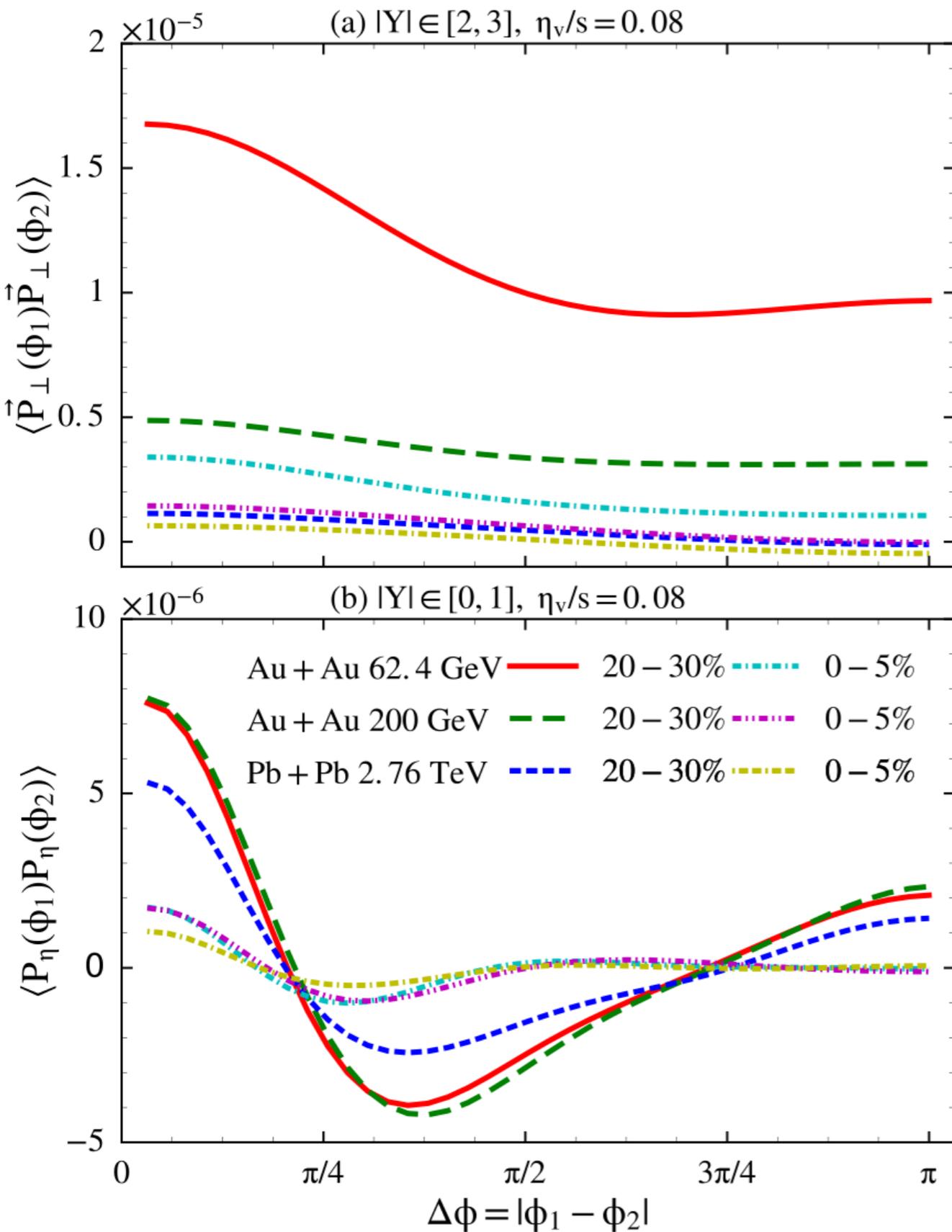
Azimuthal angle correlation of spin distributions

Pb+Pb 2.76 TeV 20-30%



- (a) $\cos(\Delta\phi)$ azimuthal distribution due to local polarization (vortex ring).
- Shear viscosity increases global polarization
- (b) The dependence of longitudinal spin correlation on rapidity is weak

Beam energy and centrality dependence



- (a) Polarization are **stronger** at **lower beam energies** and **peripheral collisions**.
- (b) The longitudinal spin correlation is coupled to the transverse collision geometry
- The beam energy dependence for longitudinal spin is weak.

- **Velocity**: average all particles in cells over 10^6 events

$$\mathbf{v}(x, y, \eta) = \frac{\sum_i \sum_j \mathbf{p}_{ij}}{\sum_i \sum_j E_{ij}}$$

- **Vorticity**: computed from velocity by **finite differential method (FDM)**
 - Non-relativistic vorticity:

$$\boldsymbol{\omega} = \frac{1}{2} \nabla \times \mathbf{v}$$

- Relativistic vorticity:

$$\omega_{\mu\nu} = \frac{1}{2} (\partial_\nu u_\mu - \partial_\mu u_\nu)$$

Spin (pseudo)vector in covariant form

$$S^\mu(x, p) = -\frac{1}{8mT} \epsilon^{\mu\nu\rho\sigma} p_\nu \tilde{\omega}_{\rho\sigma},$$

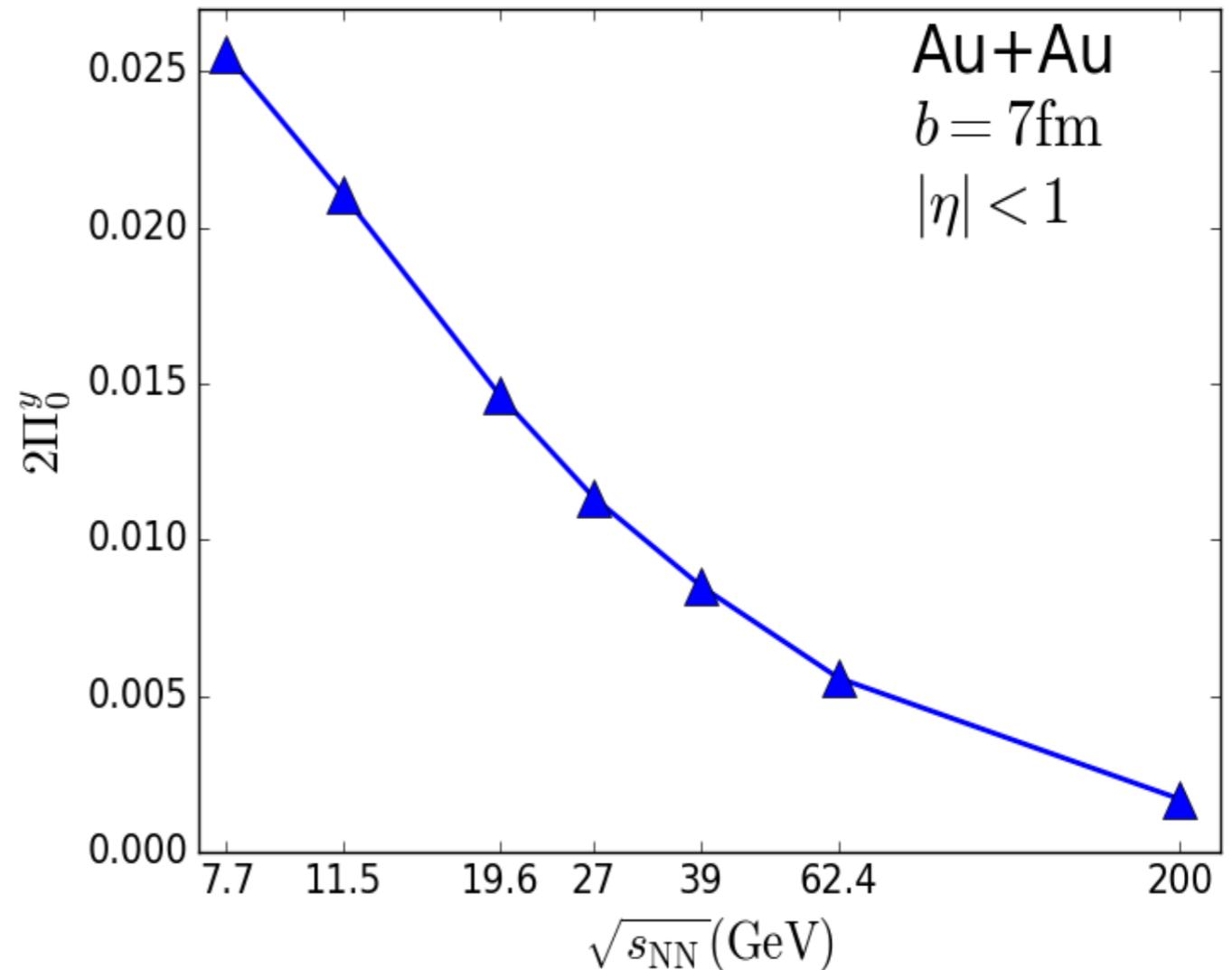
$$\tilde{\omega}_{\mu\nu} = \frac{1}{2} (\partial_\nu u_\mu - \partial_\mu u_\nu).$$

In Lab frame (Λ has momentum)

$$\mathbf{S}_0(x, p) = \mathbf{S} - \frac{\mathbf{p} \cdot \mathbf{S}}{\epsilon(m + \epsilon)} \mathbf{p}.$$

Mean polarization

$$\mathbf{\Pi}_0 = \langle \mathbf{S}_0 \rangle$$



Hui Li, Xia, LGP, Wang, work in progress

- Global polarization
 - Signal is strong at beam energy scan region
 - Possible to estimate the magnitude of magnetic field
 - Small at top RHIC and LHC energy
- Spin correlation
 - Transverse spin distribution/correlation is sensitive to initial fluid velocity.
 - Longitudinal spin correlation survives at LHC energy and mid-rapidity (unique opportunity—strong signal with high statistics)

- Ingredients for quantitative studies
 - **Net baryon density** in initial condition, equation of states and transport coefficients
 - Spin-magnetic coupling, relativistic magneto-hydrodynamics
 - Initial fluid velocity