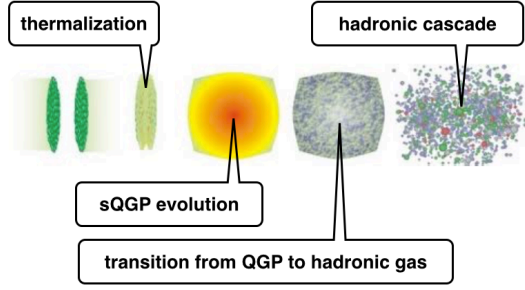


Introduction

Extend the state-of-art hybrid with jets!

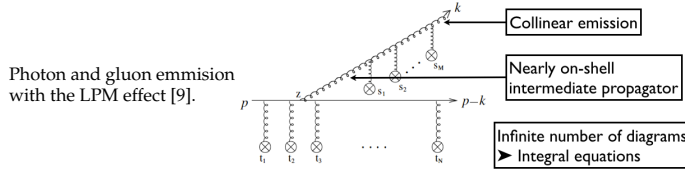
Relativistic heavy ion collision at a glance



What do we need to improve our understanding?
realistic dynamical description

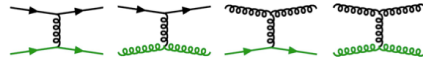
McGill-AMY Formalism in MARTINI

Radiative Energy Loss



Collisional Energy Loss

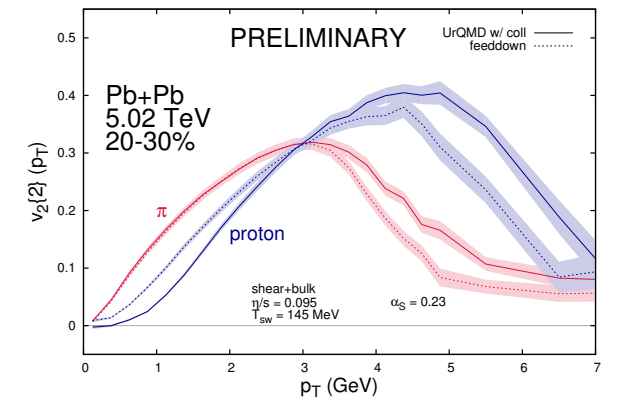
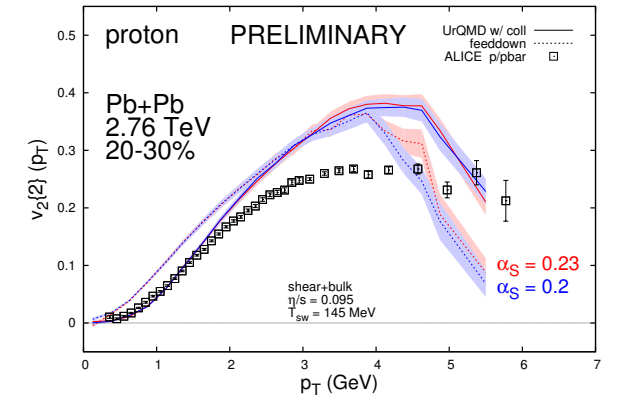
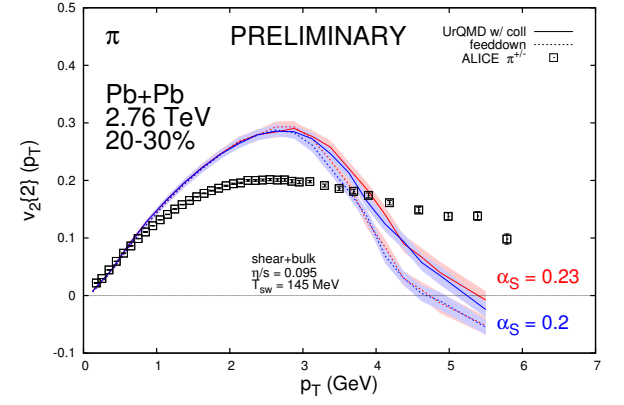
2 → 2 elastic processes between hard and thermal partons [10, 11].



$$\frac{dE}{dt}_{ab} = C_{ab} \pi \alpha_s^2 T^2 \left[\ln \frac{ET}{m_g^2} + D_{ab} \right] \quad (10)$$

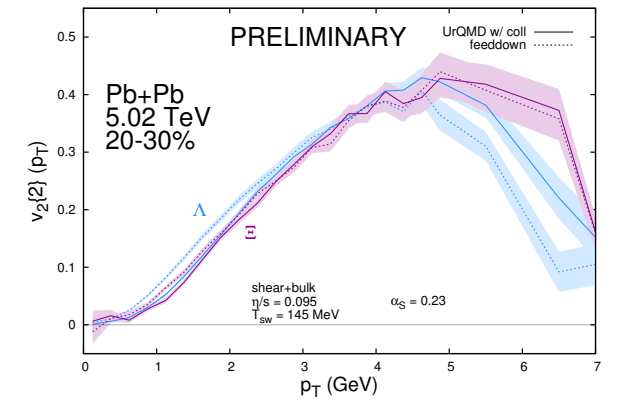
where C_{ab} and D_{ab} are constants that depend on which kind of partons are interacting.

Elliptic flow (PID)



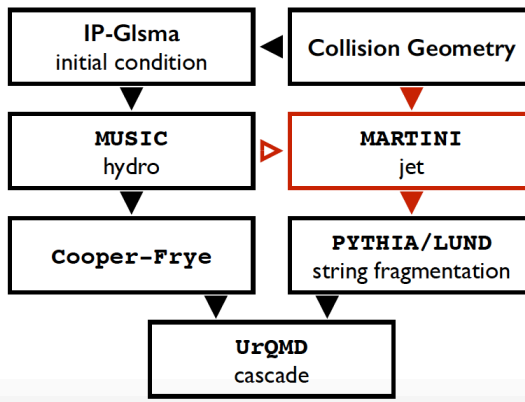
The hadronic re-scattering has significant effects on the elliptic flow in the intermediate p_T range.

The hadronic re-scattering increases $v_2(p_T)$ of identified hadrons in the intermediate p_T range. This can affect the determination of jet-medium interaction in the QGP phase.



Hadronic re-scattering has also relevant effects on the hyperon v_2 .

Overview



Full event generator: includes fluctuations in every stage

IP-Glasma pre-thermalization dynamics

nucleon + partonic fluctuations

In the IP-Glasma picture [1, 2], partons with high x provide color sources for classical Yang-Mills fields. The color gauge field in terms of the path-ordered Wilson line is given by

$$A^i(\mathbf{x}_\perp) = \frac{i}{g} V(\mathbf{x}_\perp) \partial_i V^\dagger(\mathbf{x}_\perp) \quad (1)$$

$$V(\mathbf{x}_\perp) = P \exp \left[-ig \int dx^- \frac{\rho(\mathbf{x}_\perp, x^-)}{\nabla_\perp^2 - m^2} \right] \quad (2)$$

The fluctuation of color charges carried by high- x partons in nuclei are described as

$$\langle \rho^a(x^-, \mathbf{x}_\perp) \rho^b(y^-, \mathbf{y}_\perp) \rangle = g^2 \mu_A^2(\mathbf{x}_\perp) \delta^{ab} \delta(x^- - y^-) \delta^{(2)}(\mathbf{x}_\perp - \mathbf{y}_\perp) \quad (3)$$

where $g^2 \mu$ depends on the transverse position inside the nucleus. These fluctuations are not present in the MC-Glauber model.

MUSIC Hydrodynamics

Second-order viscous hydrodynamics

MUSIC [3] solves 3 + 1D hydrodynamic conservation equations $\partial_\mu T^{\mu\nu}(t, \mathbf{x}) = 0$, along with the equations for the dissipative currents

$$\tau_\Pi \dot{\Pi} + \Pi = -\zeta \theta - \delta_{\Pi\Pi} \Pi \theta + \lambda_{\Pi\pi} \pi^{\mu\nu} \sigma_{\mu\nu} \quad (4)$$

$$\tau_\pi \dot{\pi}^{(\mu\nu)} + \pi^{\mu\nu} = 2\eta \sigma^{\mu\nu} - \delta_{\pi\pi} \pi^{\mu\nu} \theta + \varphi_7 \pi_\alpha^{(\mu} \pi^{\nu)\alpha} - \tau_{\pi\pi} \pi_\alpha^{(\mu} \sigma^{\nu)\alpha} + \lambda_{\pi\Pi} \Pi \sigma^{\mu\nu} \quad (5)$$

The transport coefficients are determined using the relaxation time and 14-moment approximation [4].

Cooper-Frye particlization

Switching from hydro to particles

Hadrons are sampled on the freeze-out hypersurface Σ according to the Cooper-Frye formula [5].

$$\frac{dN}{d^3\mathbf{p}} \Big|_{\text{1-cell}} = \begin{cases} \frac{d}{(2\pi)^3} [f_0(x, \mathbf{p}) + \delta f_{\text{shear}}(x, \mathbf{p}) + \delta f_{\text{bulk}}(x, \mathbf{p})] \frac{p^\mu \Delta_\Sigma \mu}{E_p} & \text{if } f_0 + \delta f_{\text{shear}} + \delta f_{\text{bulk}} > 0 \text{ and } p^\mu \Delta_\Sigma \mu > 0 \\ 0 & \text{otherwise} \end{cases} \quad (6)$$

where f_0 is the local equilibrium distribution function and the bulk [6] and shear [7] viscous corrections are given by

$$\delta f_{\text{shear}} = f_0(1 \pm f_0) \frac{\pi_{\mu\nu} p^\mu p^\nu}{2(\epsilon_0 + P_0) T^2} \quad (7)$$

$$\delta f_{\text{bulk}} = -f_0(1 \pm f_0) \frac{C_{\text{bulk}}}{T} \left[\frac{m^2}{3(p \cdot u)} - \left(\frac{1}{3} - c_s^2 \right) (p \cdot u) \right] \Pi \quad (8)$$

We assume a grand canonical ensemble where particles on each fluid cell are sampled independently.

UrQMD Cascade

Transport approach for dilute hadronic matter

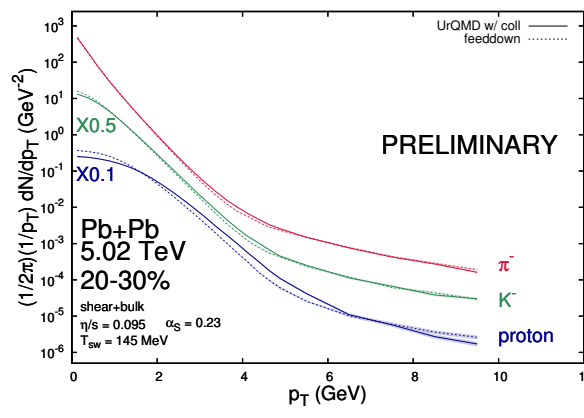
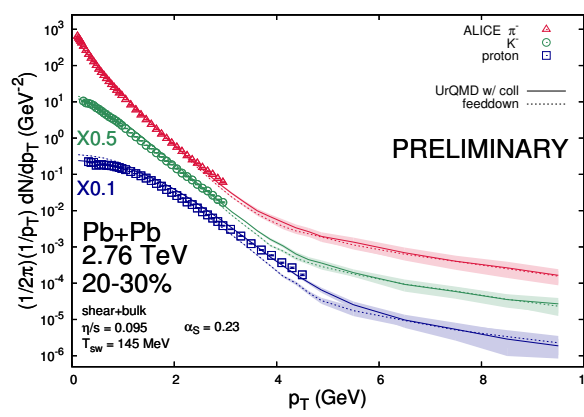
UrQMD (Ultra-relativistic Quantum Molecular Dynamics) [8] is a transport model dealing with the Boltzmann's transport equation

$$p^\mu \frac{\partial f_i}{\partial x^\mu}(t, \mathbf{x}, \mathbf{p}) = C_i[f] \quad (9)$$

by performing scattering (and decay) in an N -body system.

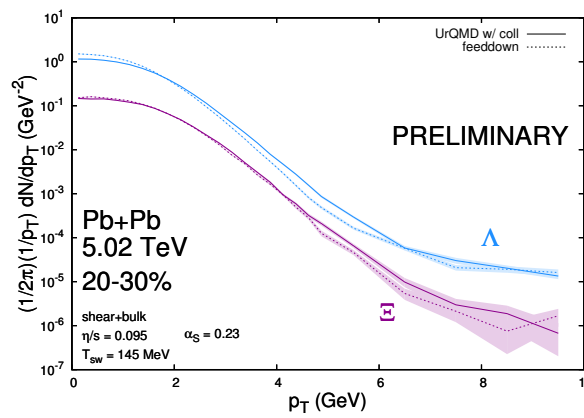
- 55 baryon species and 32 meson species with masses up to 2.25 GeV.
- Cross sections and decay rates based on the experimental data.

p_T spectra (PID)



Hybrid approach can be extended toward higher p_T with jets.

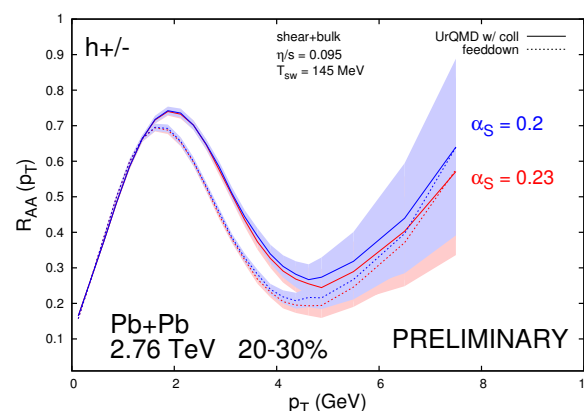
Even though effects on pions and kaons are not significant, protons are largely affected by hadronic re-scattering.



It can be applied for hyperons with higher p_T as well.

The hadronic re-scattering also has a relevant effects for the intermediate p_T range.

Nuclear modification factor



QGP energy loss and hadronic re-scattering have different effects on the particle yields.

While R_{AA} significantly depends on the strong coupling α_S for higher p_T , the hadronic re-scattering has the larger effects in the intermediate p_T range where contributions from the thermal hadrons and minijets are comparable.

Conclusion

1. By combining production and energy-loss of jets in heavy ion collisions, dynamical modelling can be extended to higher p_T .
2. Our hybrid approach is applied for Pb+Pb collisions with $\sqrt{s_{NN}} = 5.02$ TeV and $\sqrt{s_{NN}} = 2.76$ TeV at the LHC.
3. The final state spectra at the intermediate p_T largely depend on the hadronic re-scattering.
→ Energy loss in the hadronic phase needs to be taken into account for understanding of jet-medium interaction.

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