

1. INTRODUCTION

- ◆ Transport coefficients like shear and bulk viscosity are fundamental properties of thermal QCD.
- ◆ Photons could be an ideal probe to extract these viscosities from experimental results.
- ◆ Calculating viscous corrections boils down to using a general momentum distribution in propagators:

$$n_{B/F}(|p^0|) \rightarrow f_{g/q}(\mathbf{p})$$

E.g. n_B is the Bose-Einstein distribution.

- ◆ Corrections have been calculated for two-to-two scattering diagrams [1], [2].
- ◆ We present a **first calculation of inelastic leading order channels out of thermal equilibrium**. They are just as important as two-to-two channels:
 - Off-shell pair annihilation
 - Quark bremsstrahlung
 - Coherence between different scattering sites (LPM effect)

- ◆ We focus on bulk viscous corrections where

$$f(\mathbf{p}) = f(p).$$

Our calculation applies to any isotropic momentum distribution.

2. FORMALISM

- ◆ In the real time formalism the number of degrees of freedom is doubled. Thus there are four propagators.
- ◆ In the r/a basis the bare propagators for quarks are

$$\begin{aligned} S_{ra}^0 &= S_{\text{ret}}^0 = \text{r} \rightarrow \text{a} \\ S_{ar}^0 &= S_{\text{adv}}^0 = \text{a} \rightarrow \text{r} \\ S_{rr}^0 &= \left(\frac{1}{2} - f_q(\mathbf{p}) \right) [S_{\text{ret}}^0 - S_{\text{adv}}^0] \\ S_{aa}^0 &= 0 \end{aligned}$$

- ◆ We need resummed propagators. In equilibrium one can use the KMS relation to get

$$S_{rr} = \left(\frac{1}{2} - n_F(p^0) \right) [S_{\text{ret}} - S_{\text{adv}}].$$

- ◆ Out of equilibrium we must go beyond the KMS condition and do explicit calculations.

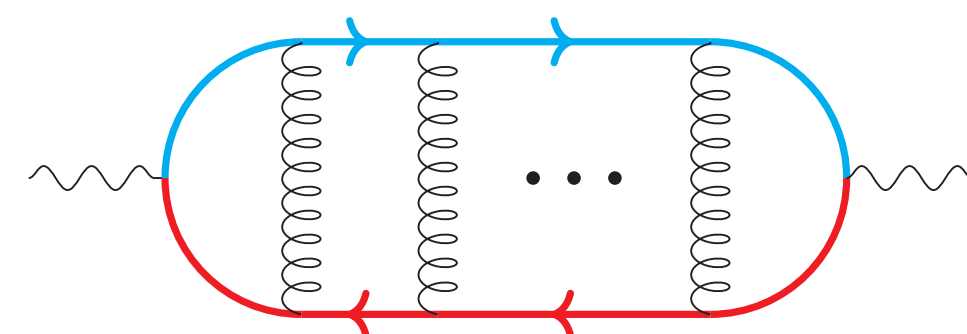
3. THE EQUILIBRIUM CASE

- ◆ Production rate of photons with momentum k is given by

$$k \frac{dR}{d^3k} \sim (i\Pi_{12}^\gamma)^\mu$$

where Π^γ is the photon polarization tensor.

- ◆ The Feynman diagrams for Π_{12}^γ for the inelastic channels are



summed over all number of gluon rungs.

- ◆ Despite multiple vertices the diagrams contribute at leading order in g [3]:

- $1/g$ enhancement for soft gluons, $P \sim gT$, in the rr propagator:

$$n_B(p^0) \sim \frac{T}{p^0} \sim \frac{1}{g}$$

- Pinching poles from hard, on shell quarks:

$$\text{r} \rightarrow \text{a} \leftarrow \text{r} \sim \mathcal{O}\left(\frac{1}{m_\infty^2}, \frac{1}{\Gamma}\right) \sim g^{-2}$$

m_∞^2 is the thermal mass and Γ the thermal decay width.

4. DENSITY OF SOFT GLUONS

- ◆ In a non-equilibrium medium there is also a $1/g$ enhancement from soft gluons:

- ◆ The resummed rr propagator is

$$G_{rr} = \left(\frac{1}{2} + \frac{\Pi_{<}}{\Pi_{>} - \Pi_{<}} \right) (G_{\text{ret}} - G_{\text{adv}})$$

$\Pi_{<}$ and $\Pi_{>}$ are components of the gluon polarization tensor.

- ◆ Leading order diagrams give

$$\frac{\Pi_{<}}{\Pi_{>} - \Pi_{<}} = \Omega \frac{T}{p^0} \sim \frac{\Omega}{g}$$

$\Omega[f]$ describes the resummed occupation number of soft gluons.

- ◆ Extending a sum rule from [4] we get

$$\overline{\text{Q}} \left[\frac{1}{\mathbf{q}_\perp^2} - \frac{1}{\mathbf{q}_\perp^2 + m_D^2} \right]$$

$m_D^2[f]$ is the non-equilibrium Debye mass. It describes screening of chromoelectric fields.

5. DENSITY OF HARD QUARKS

- ◆ In a non-equilibrium medium we also get pinching poles.

- ◆ The resummed rr quark propagator is

$$S_{rr} = \left(\frac{1}{2} + \frac{\Sigma_{<}}{\Sigma_{>} - \Sigma_{<}} \right) [S_{\text{ret}} - S_{\text{adv}}].$$

- ◆ For hard, on-shell quarks the resummed occupation number is

$$F := -\frac{\Sigma_{<}}{\Sigma_{>} - \Sigma_{<}} = \begin{cases} f_q(p), & \text{if } p^0 > 0 \\ 1 - f_q(p), & \text{if } p^0 < 0 \end{cases}$$

Pauli blocking

6. EVALUATING THE CHANNELS

- ◆ To get Π_{12}^γ we must sum sixteen quark four-point functions in the r/a basis.

- ◆ In equilibrium we can use the KMS condition to simplify the sum.

- ◆ Out of equilibrium our formula for S_{rr} makes the sum telescopic. Then

$$\text{P+K} \begin{array}{c} 1 \quad 2 \\ \text{P} \quad 1 \quad 2 \end{array} = -F(P+K) [1 - F(P)] \text{Re} \begin{array}{c} \text{r} \rightarrow \text{a} \\ \text{r} \leftarrow \text{a} \end{array}$$

where

$$\begin{array}{c} \text{r} \rightarrow \text{a} \\ \text{r} \leftarrow \text{a} \end{array} = \begin{array}{c} \text{r} \rightarrow \text{a} \\ \text{r} \leftarrow \text{a} \end{array} + \begin{array}{c} \text{r} \rightarrow \text{ar} \\ \text{r} \leftarrow \text{ar} \end{array} + \dots$$

- ◆ One gets a Boltzmann-like integral equation that must be solved numerically.

7. CONCLUSION

- ◆ Remarkably, the inelastic channels are fully characterized by F and three non-equilibrium constants:

- Ω Density of soft gluons
- m_D^2 Debye mass
- m_∞^2 Thermal mass of quarks

- ◆ Next steps:

- Solve the integral equation.
- Extend to non-isotropic media (relevant for shear viscosity).
- The tools developed can be used for non-equilibrium jet energy loss.

8. REFERENCES

- [1] C. Shen, J.-F. Paquet, U. Heinz, C. Gale, *Phys.Rev.*, vol. C91, p. 014908, 2015 [arXiv:1410.3404]
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- [4] P. Aurenche, F. Gelis, H. Zaraket, *JHEP*, vol. 05, p. 043, 2002 [hep-ph/0204146]