

Lattice QCD - an **Interacting Hadron Resonance Gas** ?

Entropy density, pressure, entropy, χ_B, Q, S of
interacting HRG = Lattice QCD (WB-data, Borsanyi et al.)



No Phase Transition at $T_c = 155$ MeV of 2+1 Flavor QCD !



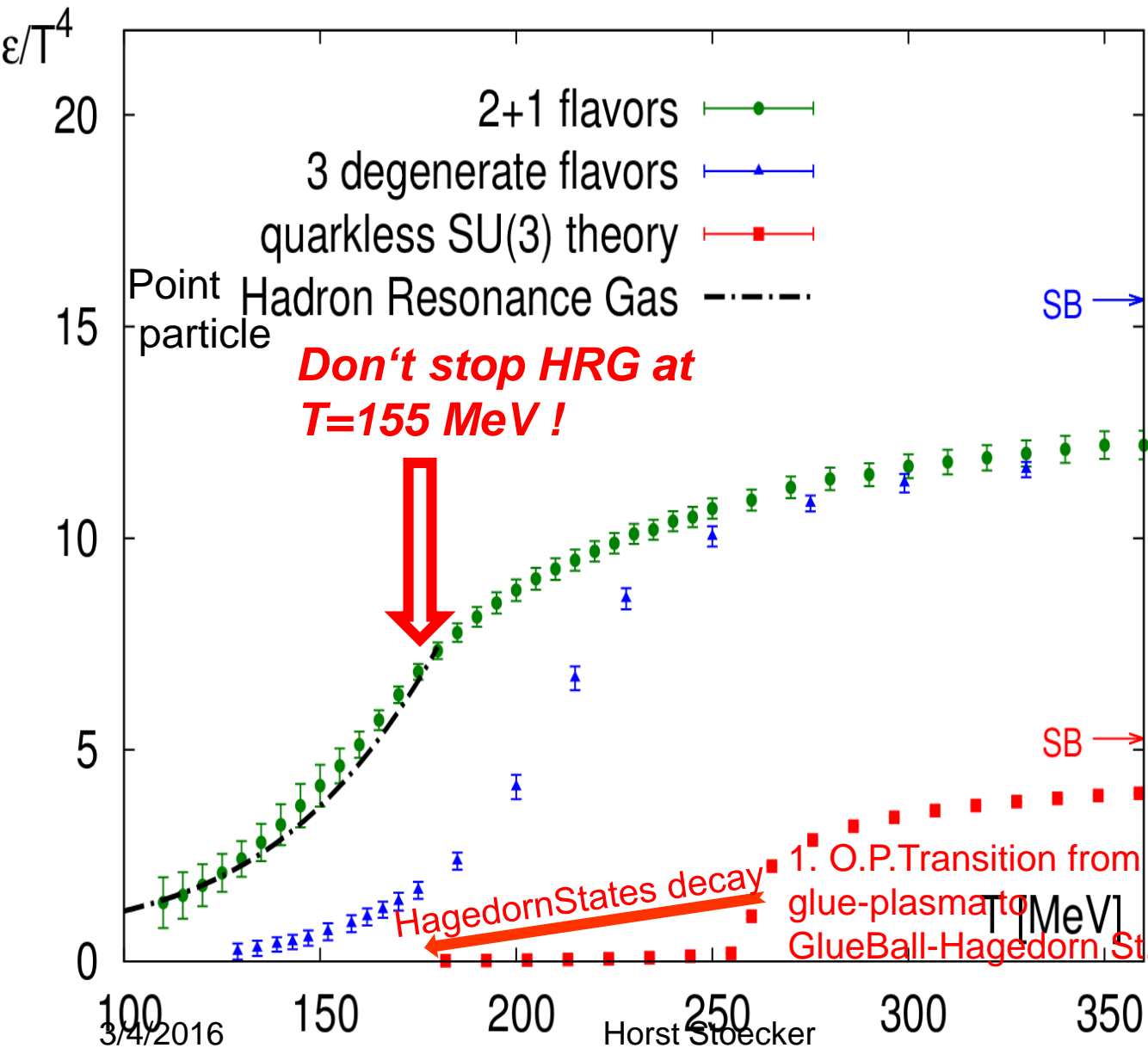
Interact. Hadron Resonance Gas describes lattice QCD well
up to **$T \sim 250$ MeV**, mix w. HTL QGP at higher T



Trace anomaly, interaction measure, nonperturbative effects
the role of 'Hot Hadrons' ?

2+1 flavor Lattice QCD and Pure Yang Mills LGT

Energy density (EoS) **DIFFERENT** for different quark masses



Energy density from Sz. Borsanyi et al. W.B. Wuppertal-Budapest coll. JHEP 1011, 2010, 077; PLB730, 2014, 99

(2+1)- flavor QCD is matched by $N_f = 3, m_{u,d} = m_s$ at $T = 250$ MeV

pure gauge, Yang Mills $T_c = 270$ MeV

Quenched: W.B. coll. JHEP 1207, 2012, 056

Multi-component Eigvol. HRG constrained by lattice QCD data

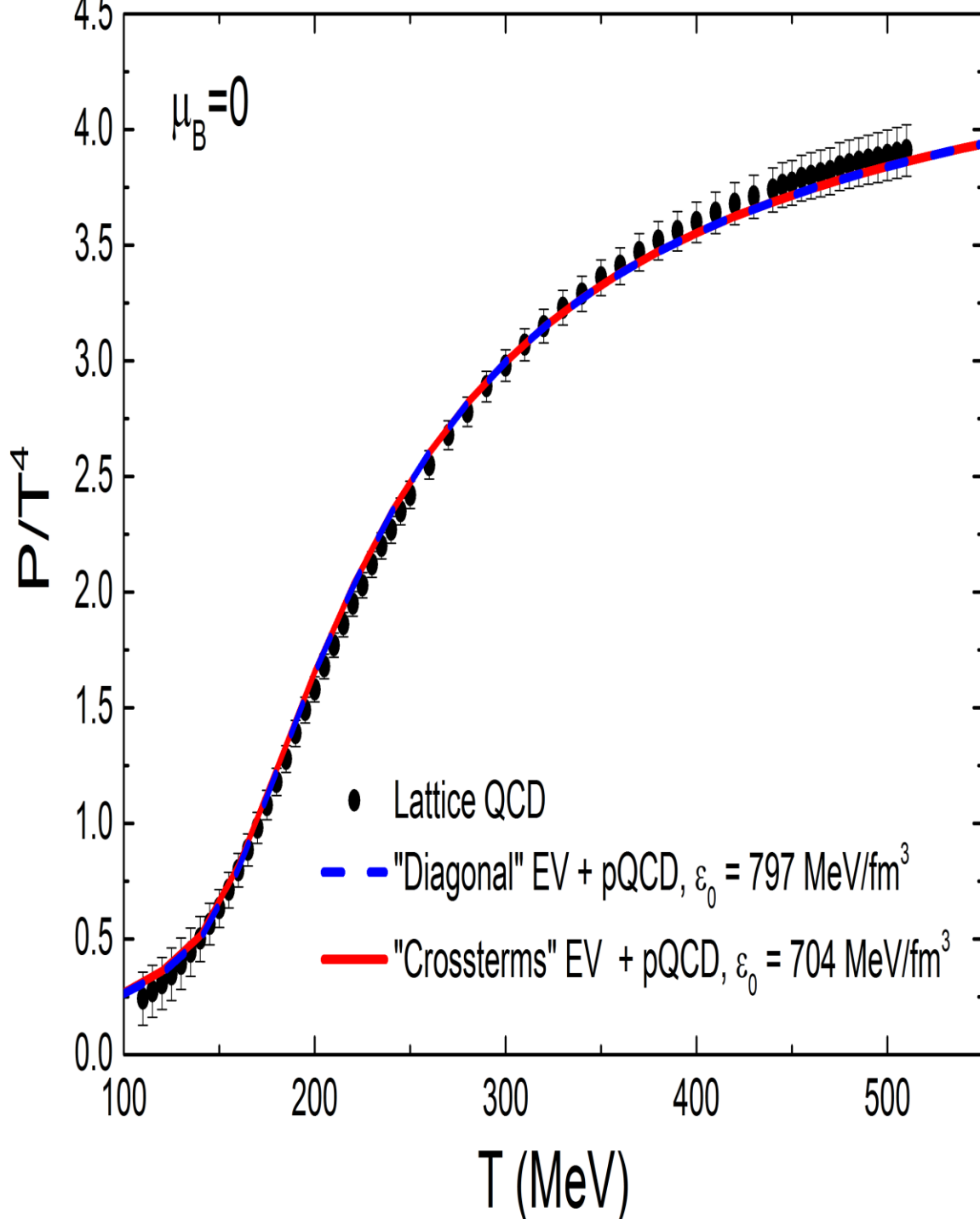
Crossover QCD-EoS matches
HRG at low (T, μ)
+ pert. QCD at high (T, μ)

AKY, Kapusta group
PRC 90024915 (2014)

$$p(T, \mu) = [1 - S(T, \mu)] P_{HRG}(T, \mu) + S(T, \mu) P_{pQCD}(T, \mu)$$

Transition from
EV HRG ($r_i \sim m_i^{1/3}$)
to pQCD
at $T_0 \cong 175$ MeV
via switching function

Fit $T < T_0$ $r_p = 0.43$ fm -
Consistent with lattice



Lattice QCD = Interacting Hadron Resonance Gas ?

PHYSIK

Lattice QCD fit

up to $T \sim 250$ MeV

by *interacting* HRG

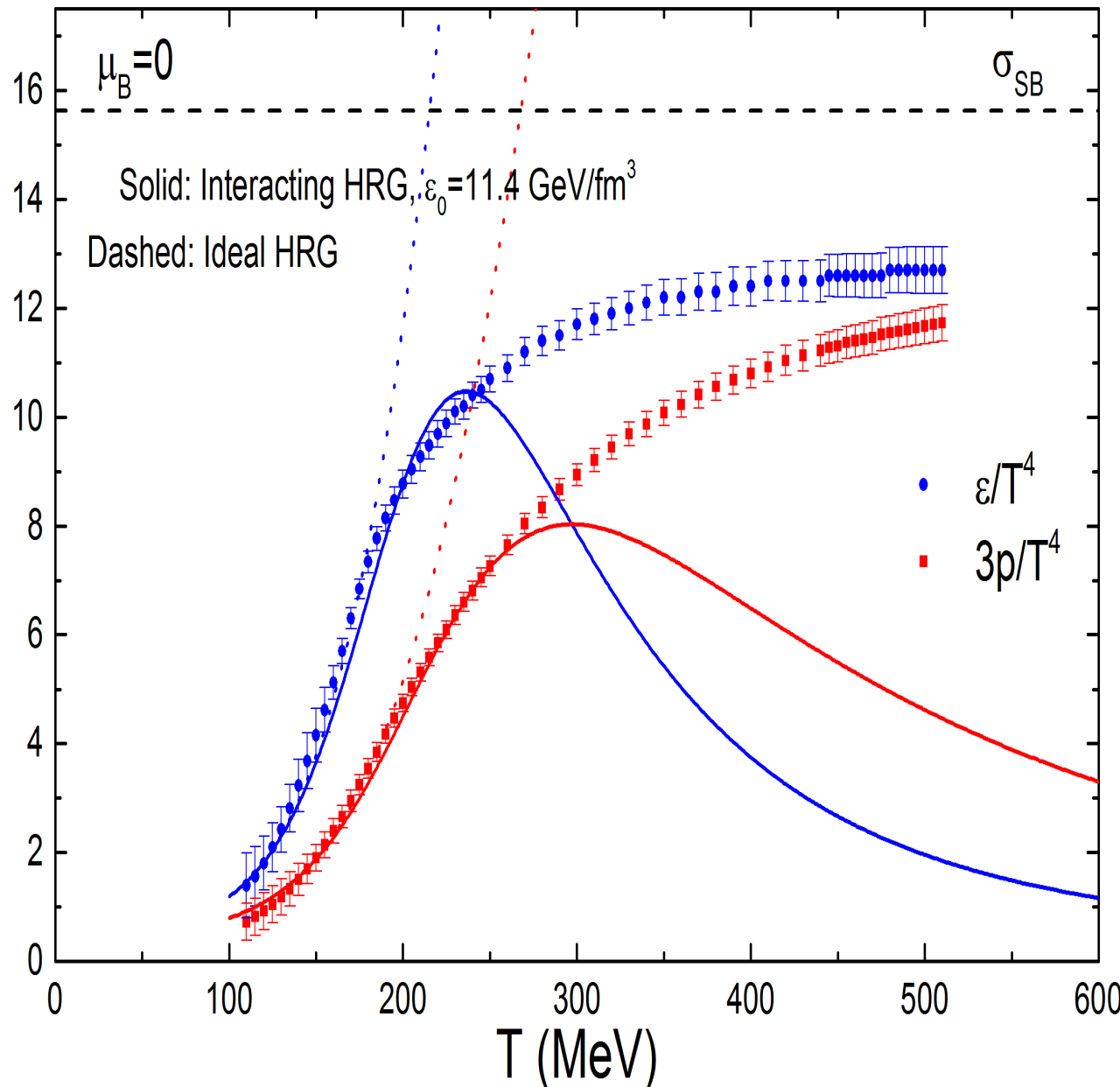
Eigenvolume $v_i = m_i/\varepsilon_0$

“Crossterms” EV model

$$p = \sum_i \frac{T n_i}{1 - \sum_j \tilde{b}_{ji} n_j}$$

$$\tilde{b}_{ij} = \frac{2b_{ii}b_{ij}}{b_{ii} + b_{jj}}$$

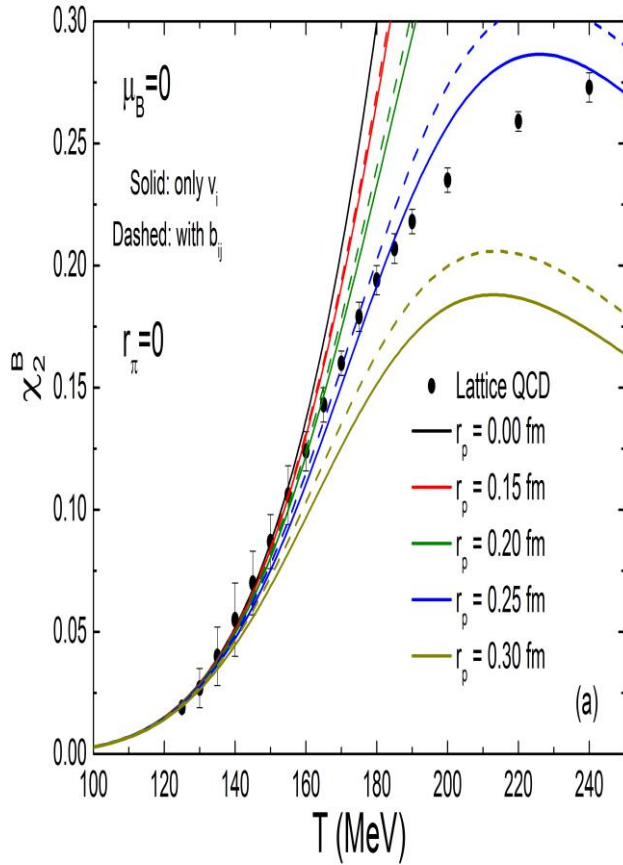
$$b_{ij} = \frac{2}{3} \pi (r_i + r_j)^3$$



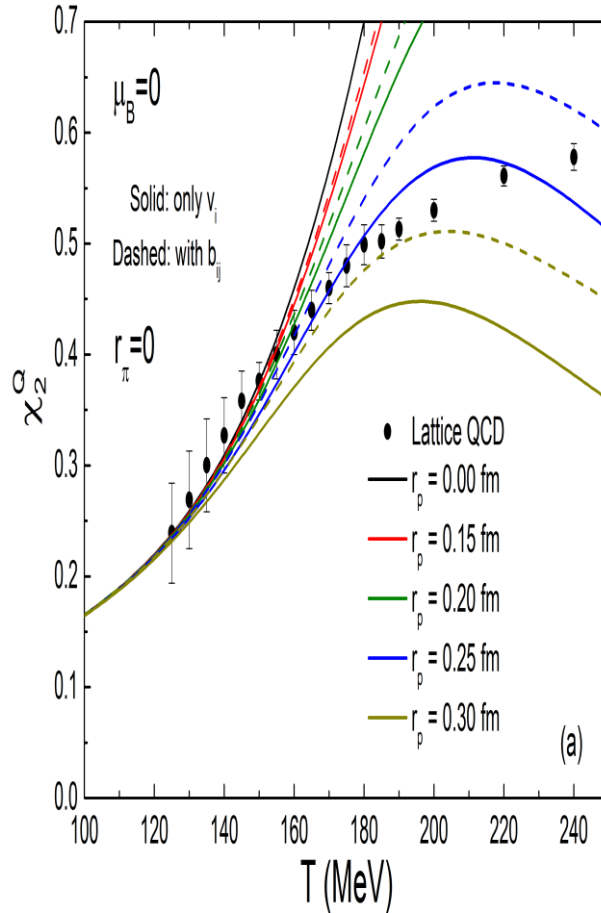
Multi-component bag-eigenvolume HRG vs lattice QCD

Susceptibilities carry information about fine details of the equation of state

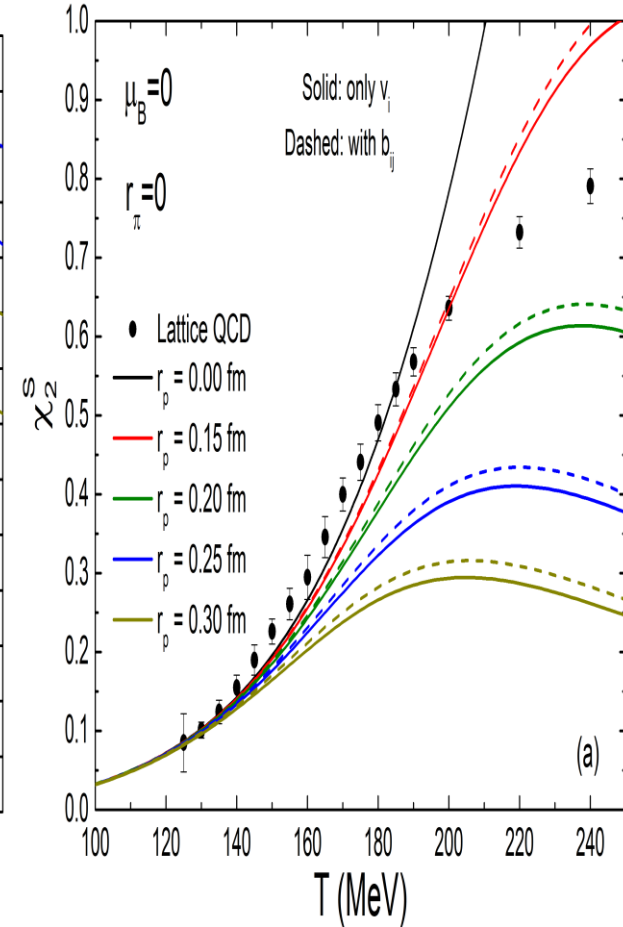
χ_2^B



χ_2^Q



χ_2^S



$r=0$: HRG of point particles
 cannot follow lattice data above $T=160$ MeV
 Finite eigenvolumes of hadron bags:
 dramatic improvement towards lattice data

strange vs non-strange hadrons
 different volumes at same mass?

V. Vovchenko, H.ST

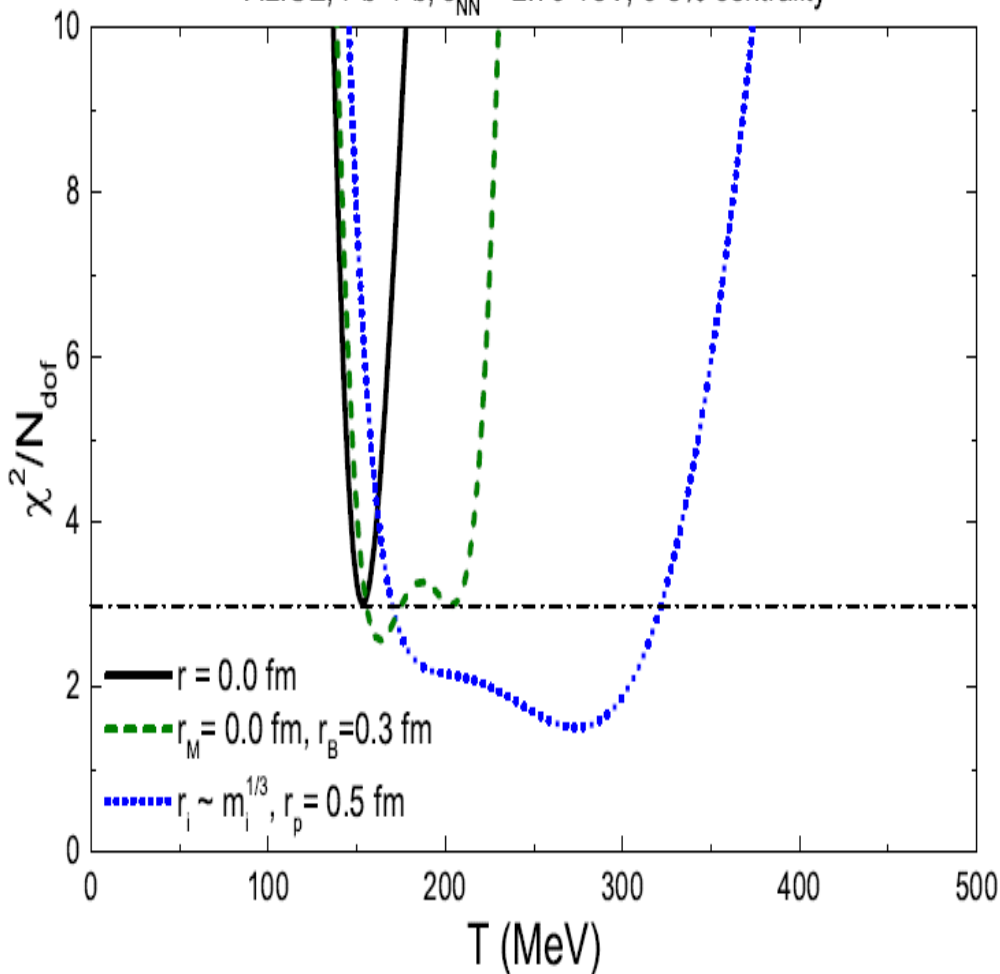
Multi-component Eigenvol. HRG vs ALICE hadron yield data

Two diff. Eigenvolume parametrizations:

AA Point-like mesons, Baryons $r_B = 0.3$ fm

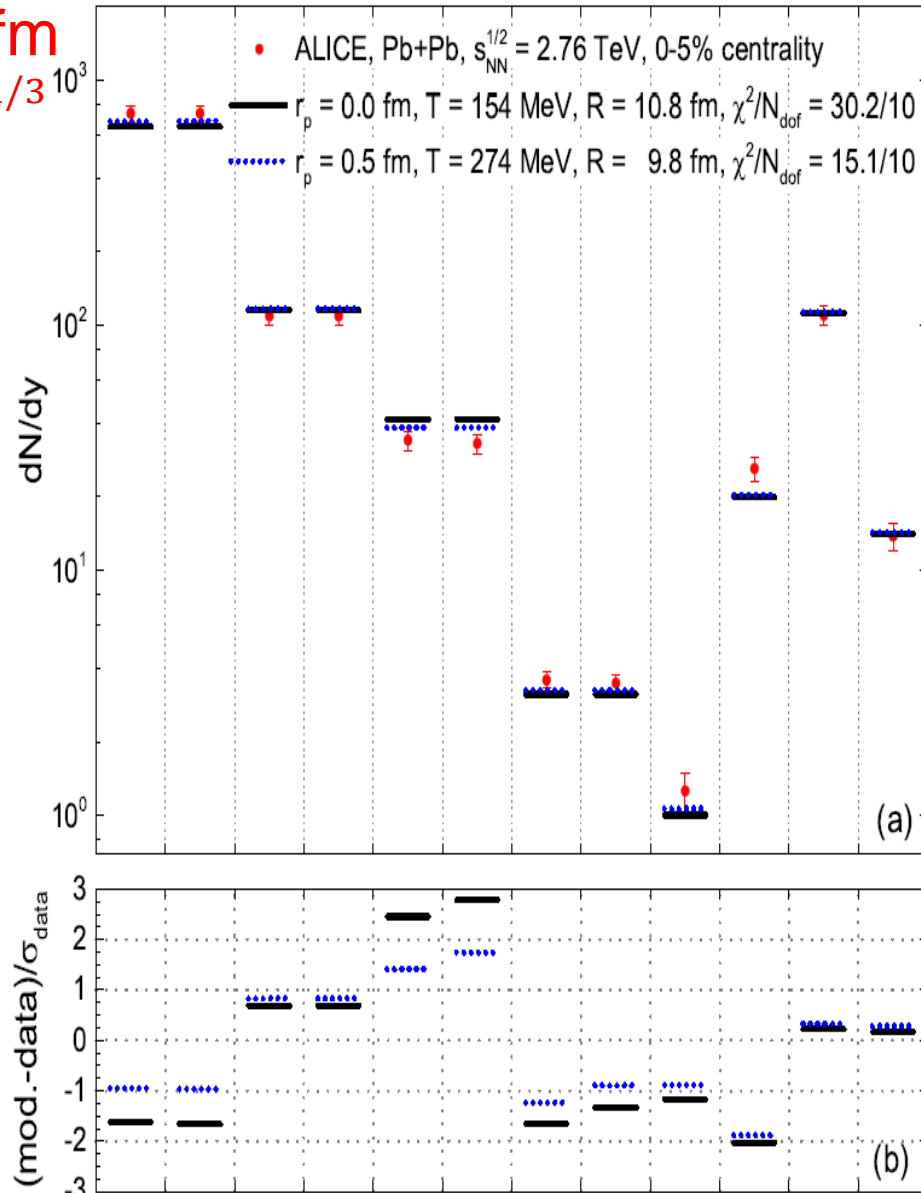
AKY **Baq-model** inspired EV model: $r_i \sim m_i^{1/3}$

ALICE, Pb+Pb, $s_{NN}^{1/2} = 2.76$ TeV, 0-5% centrality



ALICE yield data fit **wide** temperature range
two different eigenvolumes parametrizations

π^+ π^- K^+ K^- p \bar{p} Ξ^- Ξ^+ $\Omega+\bar{\Omega}$ Λ K_S^0 ϕ



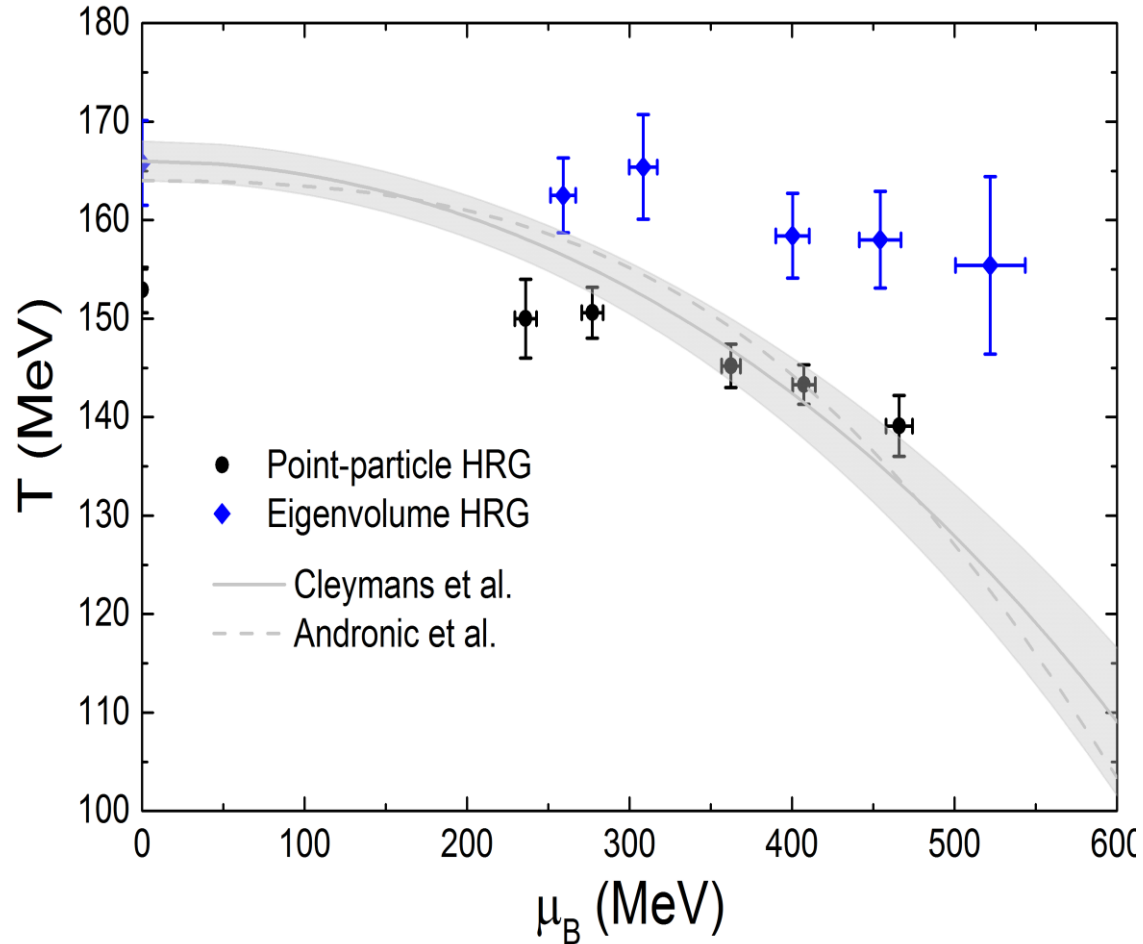
Vovchenko, HST1512.08046 [hep-ph]

Multi-component eigenvol. HRG constrained by lattice data

Crossover QCD-EoS matched by **HRG at low (T, μ)** + **pert. QCD at high (T, μ)**

$$p(T, \mu) = [1 - S(T, \mu)]P_{HRG}(T, \mu) + S(T, \mu)P_{pQCD}(T, \mu)$$

Transition from EV HRG ($r_i \sim m_i^{1/3}$) to pQCD at $T_0 \cong 175$ MeV via **switching function**



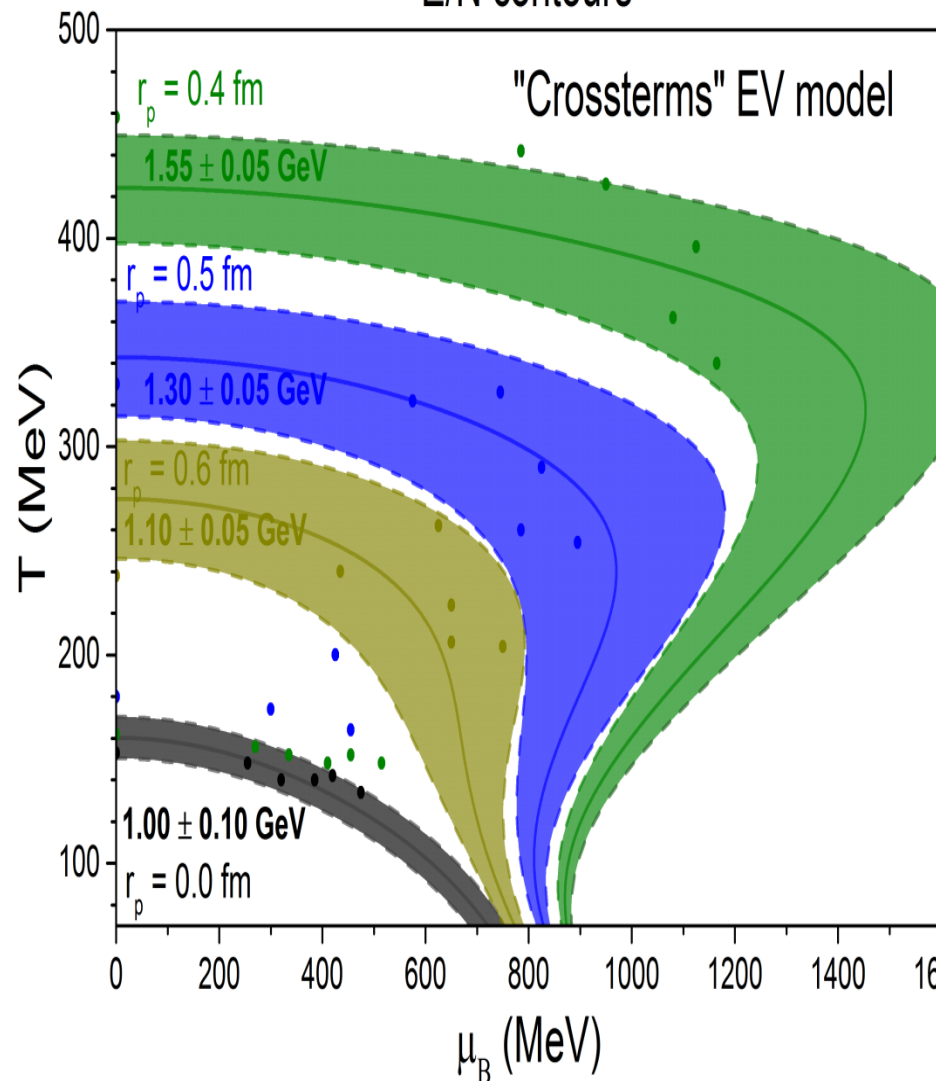
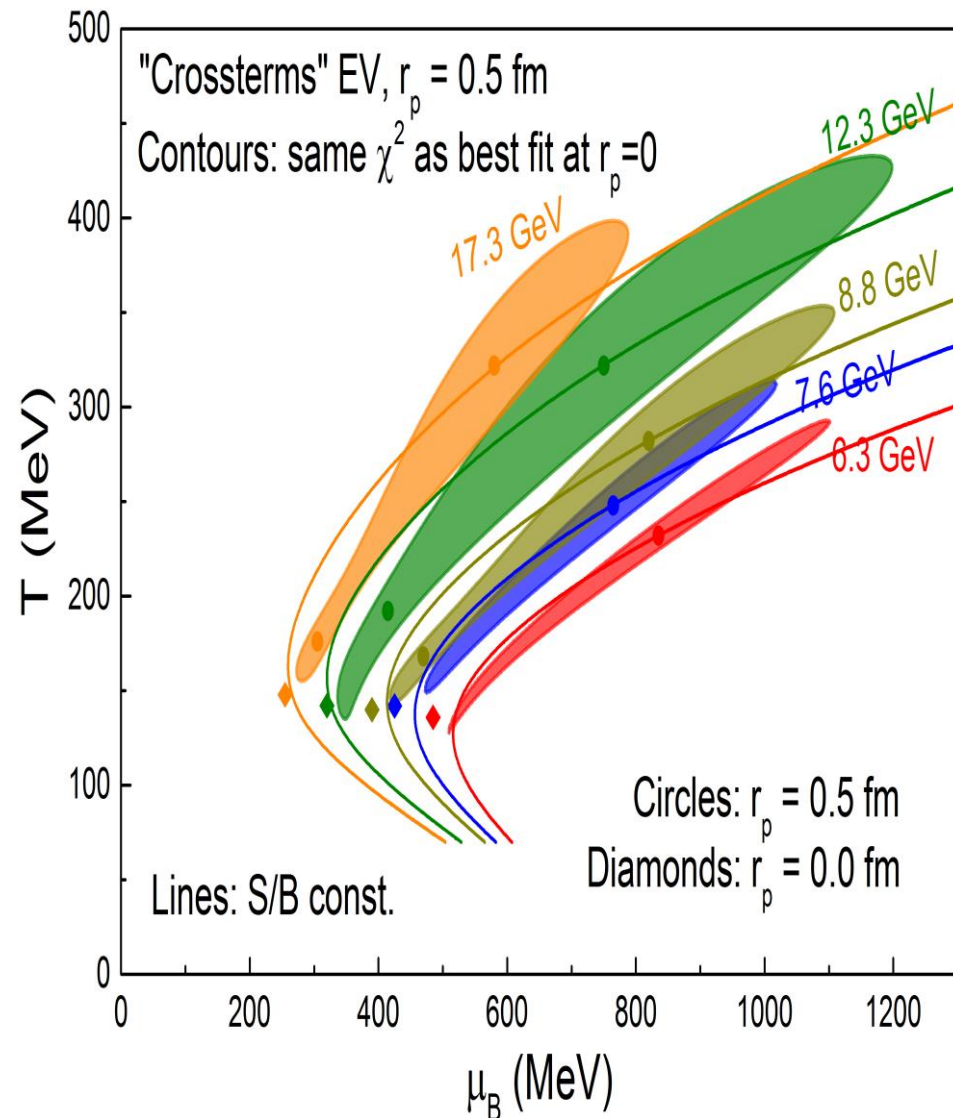
systematically better χ^2 at higher freeze-out T and μ

Fit to yield data at $T < T_0$ with $r_p = 0.43$ fm - Consistent with lattice Vovchenko

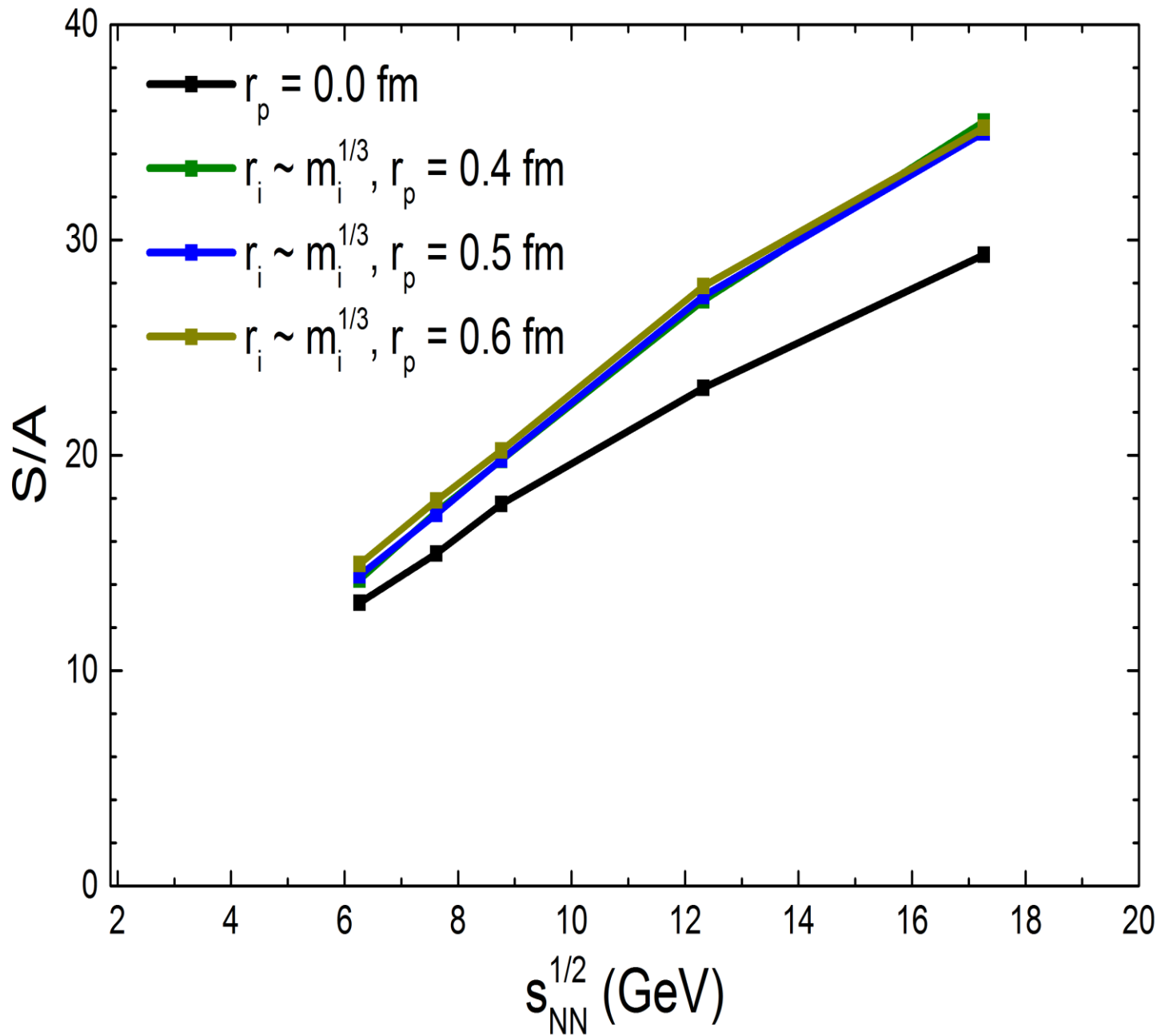
Multi-component eigenvol. HRG vs **NA49** hadron yield data

Bag-model inspired EV model: $r_i \sim m_i^{1/3}$ Vovchenko, HS

E/N contours



freeze-out parameters extraction with int.HRG **does** yield unique S/A fits !



VoVchenko: NA49 data allow measurement of $S/A = \text{const}$ (energy)!

Acknowledgements

Transport: **Zhou, Seizel, Xu, Nara, Pang, Niemi, Biro, C. Greiner...**

Hagedorn: **Beitel, Gallmeister, Vovchenko, Hostler, C. Greiner...**

FIAS: **Schramm, Steinheimer, Struckmeier, Vasak, ...**

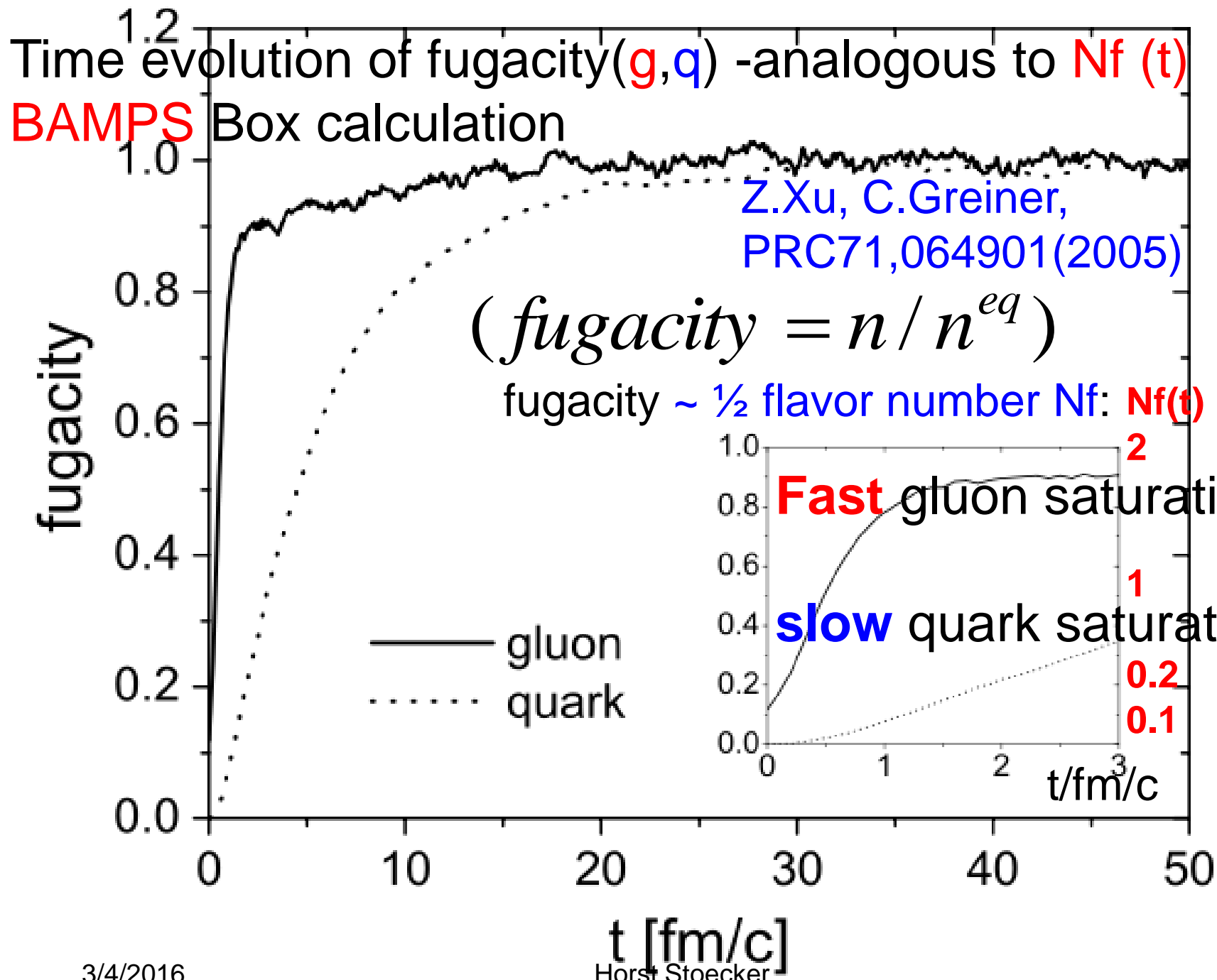
Early phase EM probes : **Vovchenko, Satarov, Gorenstein, Mishustin, Csernai, Raha, Sinha, ...**

Lattice : **Borsanyi, Fodor, Szabo, Karsch, Panero, Philipsen, Ratti**

ALICE: **Giubellino, Harris, Andronic, Bellwied, PBM, Loiz. Masc.**

Signatures for **pure glue => glueball** scenario

New event-class in **high multiplicity pp & pA**
at FAIR*, RHIC and LHC



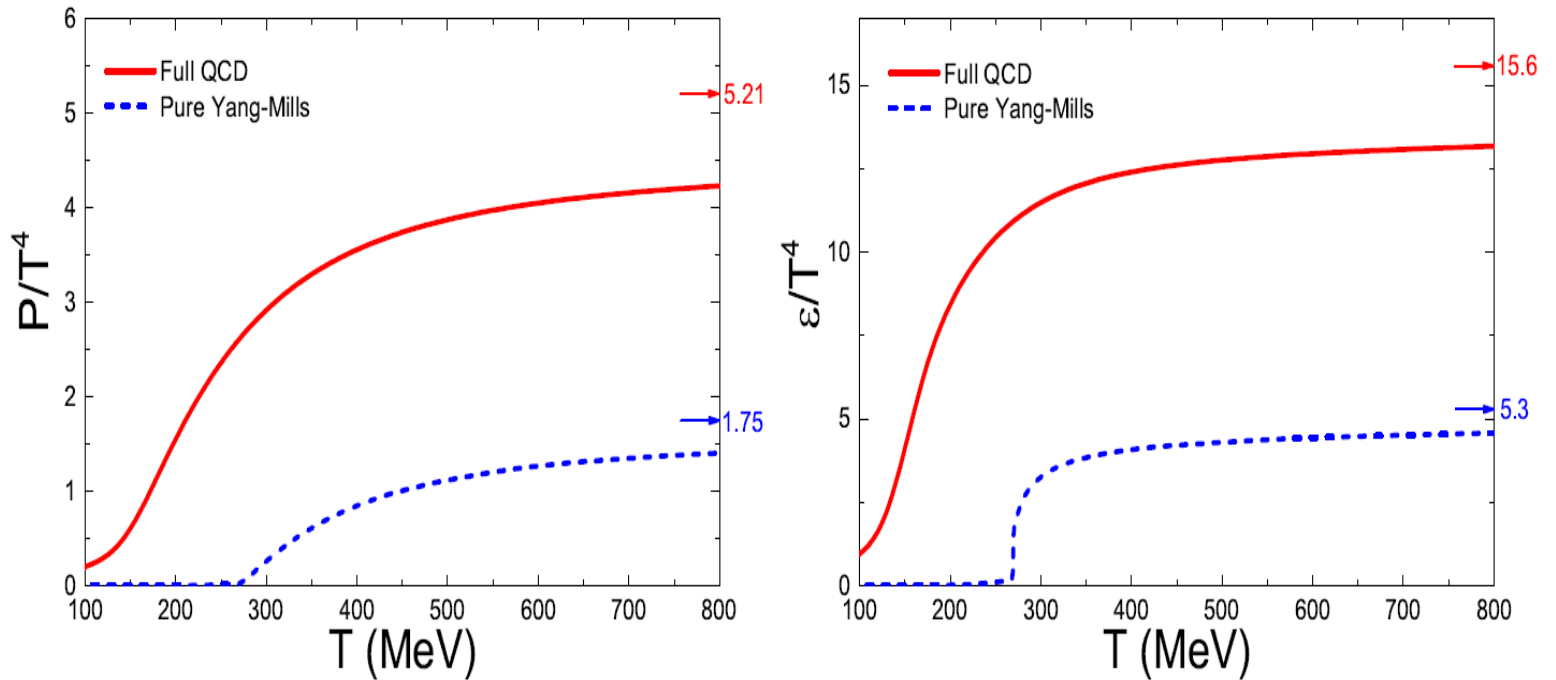
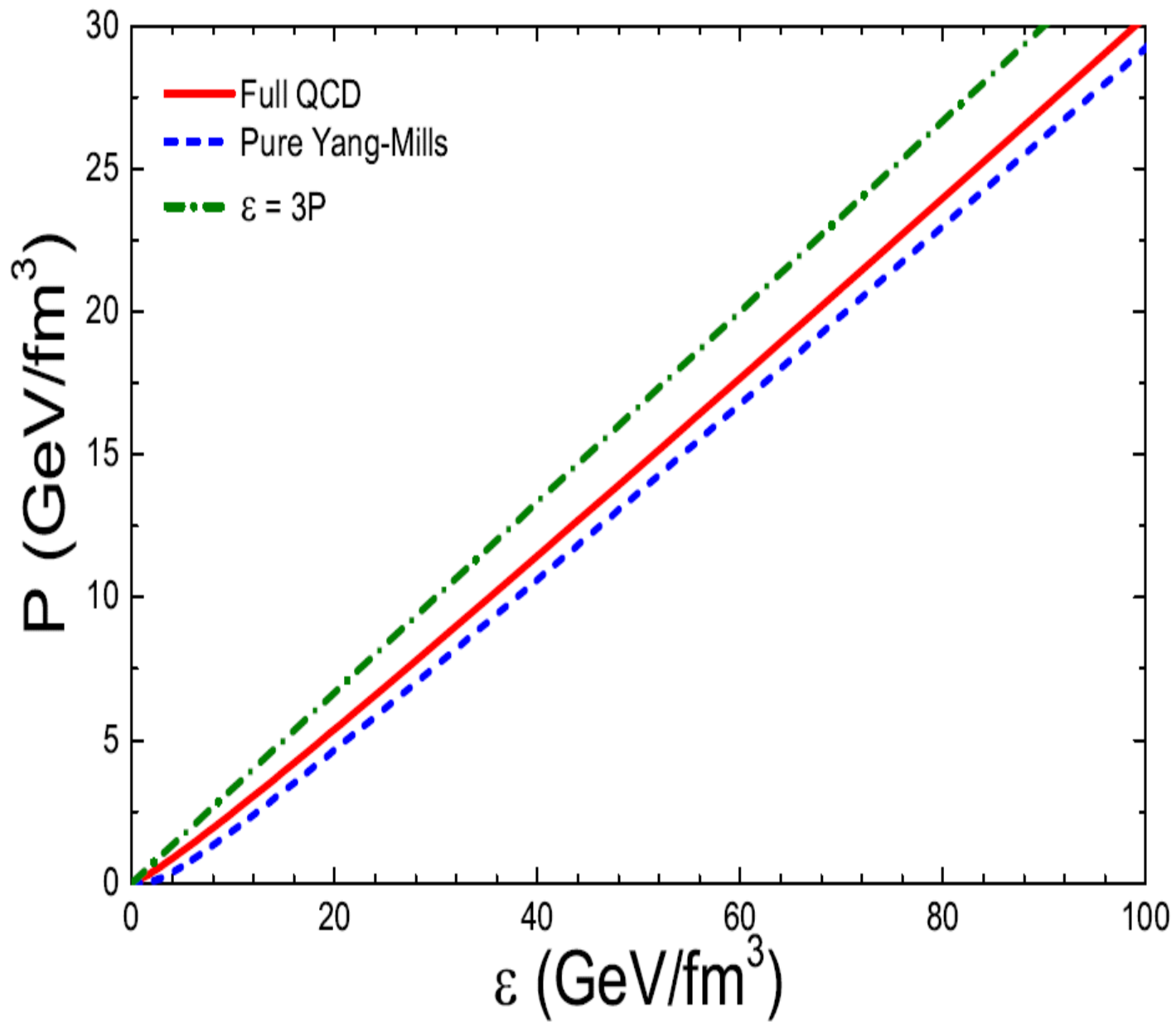
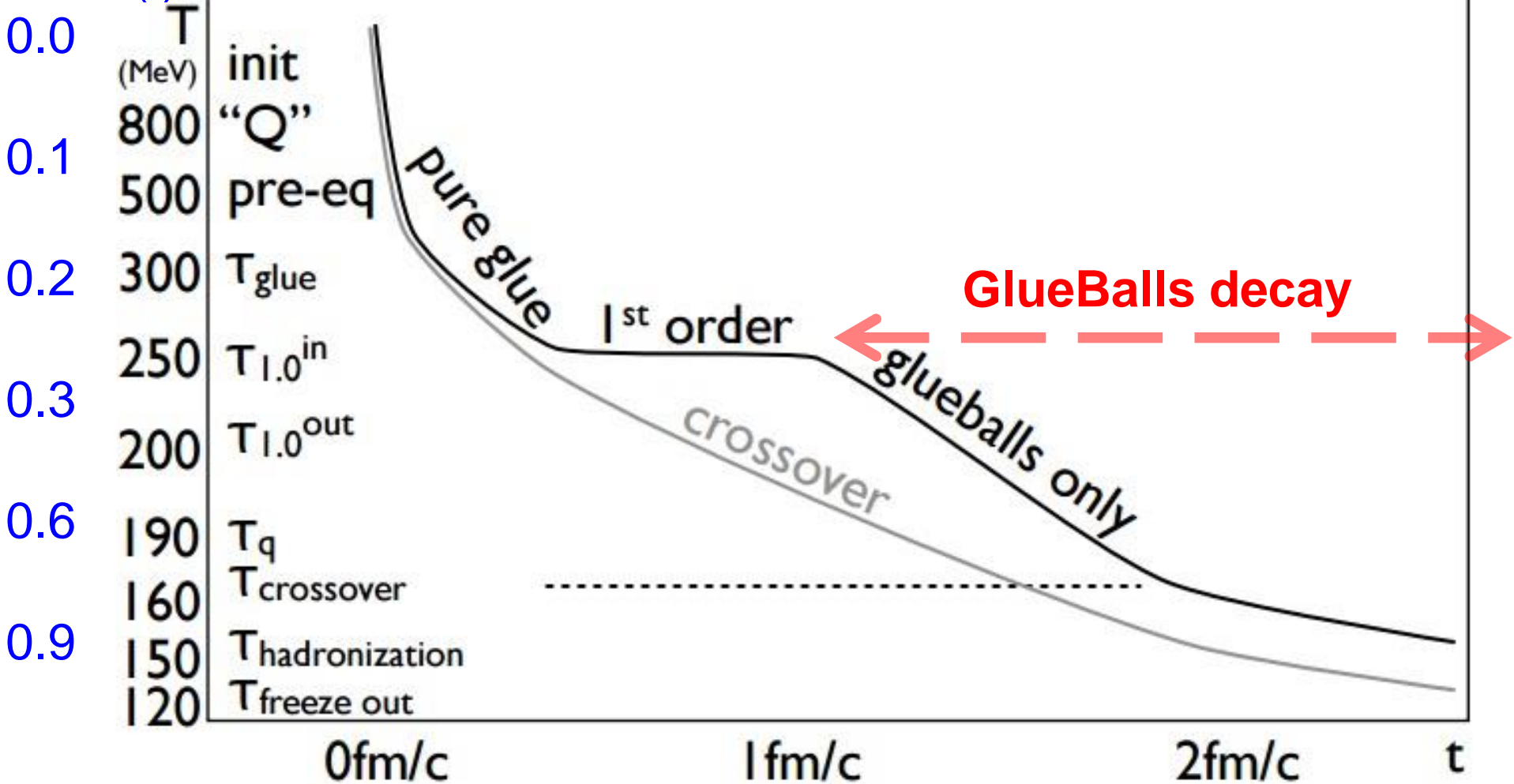


FIG. 1: (Color online) Temperature dependence of the scaled pressure (a) and energy density (b) obtained in lattice QCD calculations of Refs. [28, 31]. The solid and dashed lines correspond to the FQ ($N_f = 2 + 1$) and PG ($N_f = 0$) cases, respectively. The horizontal arrows indicate the asymptotic (Stefan-Boltzmann) values of P/T^4 and ε/T^4 at large temperatures.

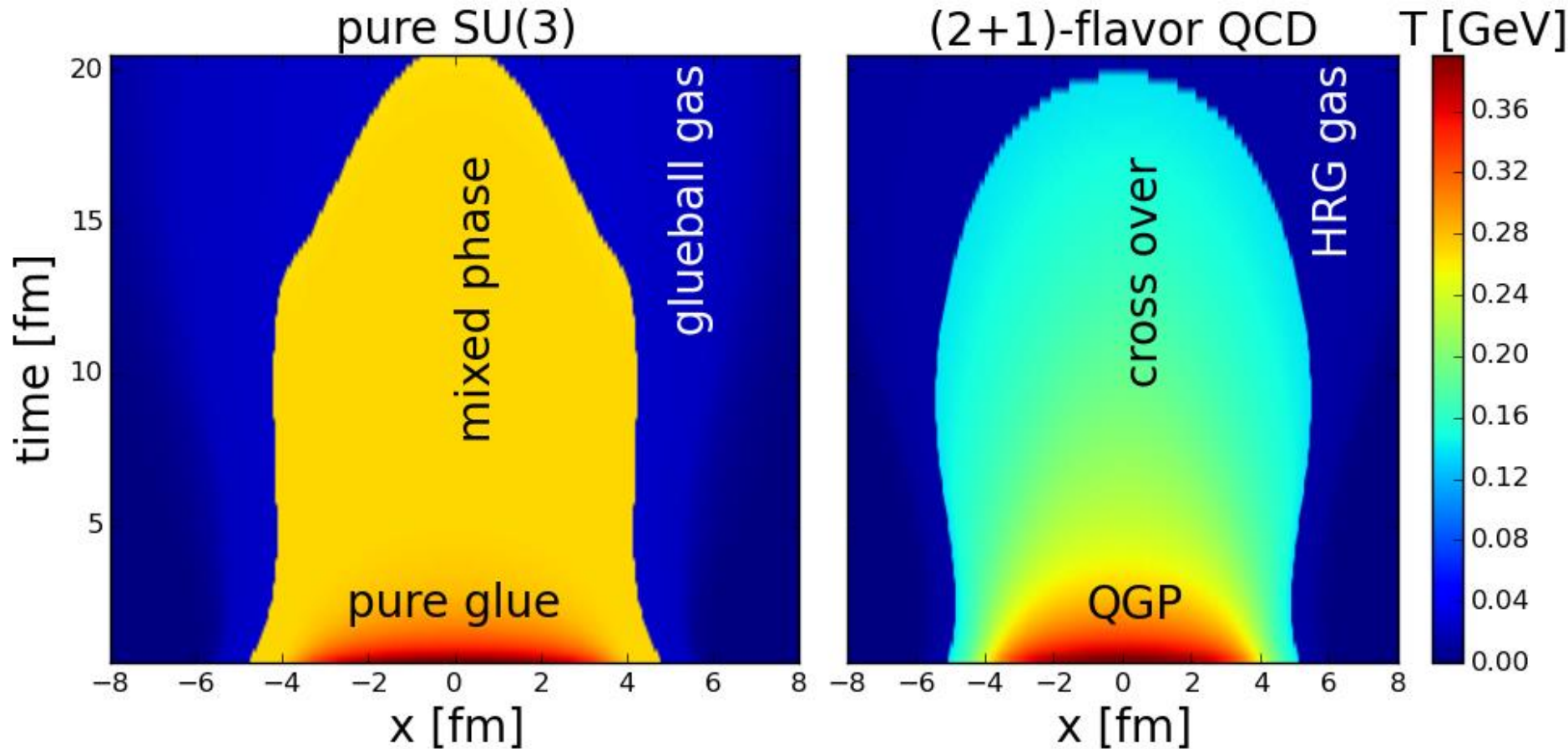


Eff. Nf(t)



Eff. Nf(t): 0 0.1 0.2 0.3 0.6 1.2 ...

Eff. Nf(t) is U.S. – parameter : $N_f = 2+1 \sim \text{fugacity} = 1$



- Energy density smaller than 0.15 GeV is masked as HRG or glueball fluid
- The mixed phase lasts very long with pure SU(3) gauge EOS

Time evolution $T(t)$ of **pp** vs **AA** collisions at RHIC

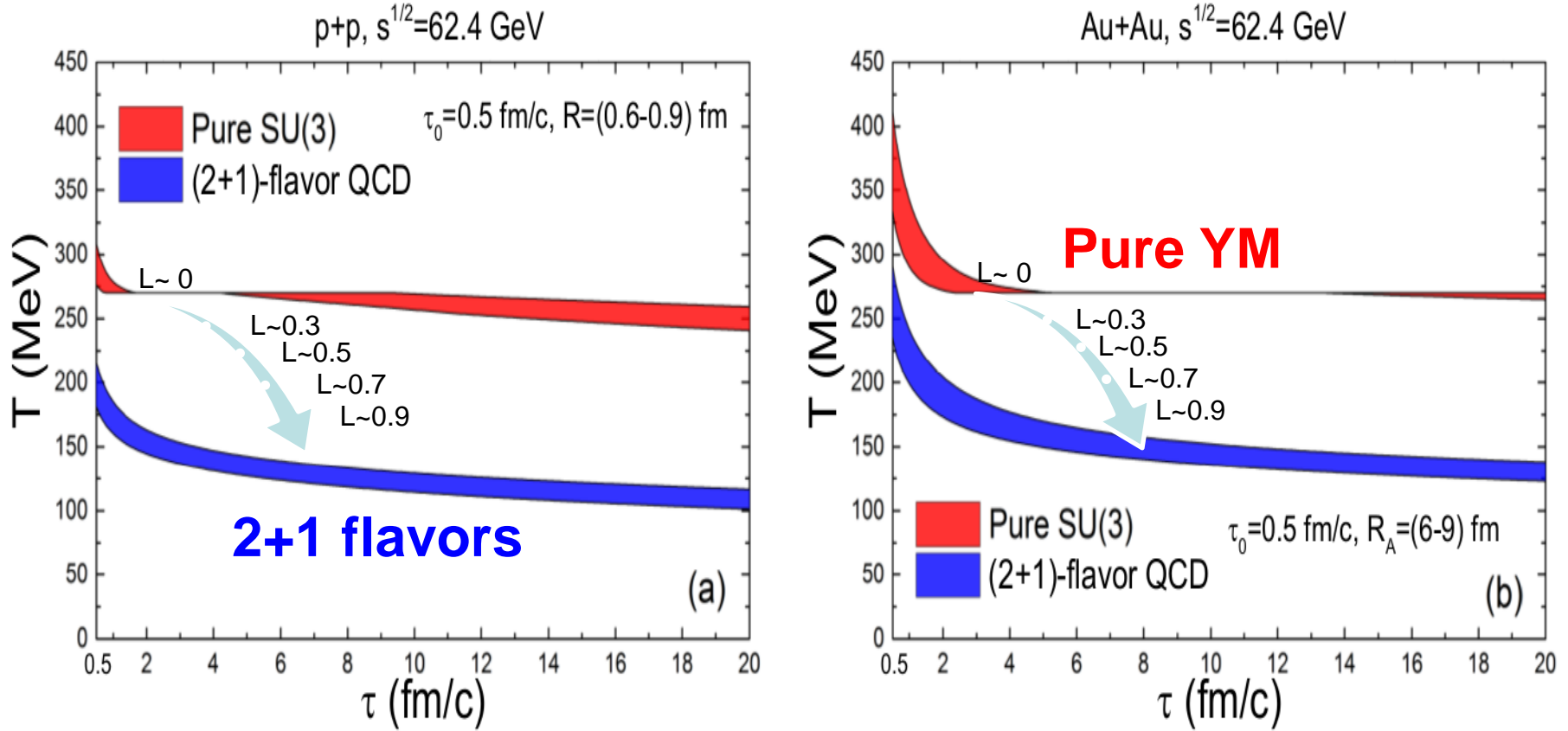


FIG. 3: (Color online) The τ -dependence of the temperature for QGP and pure SU(3) scenarios in (a) $p+p$ and (b) $A+A$ collisions at $\sqrt{s_{NN}} = 62.4$ GeV. The uncertainty bands result from variation of the transverse radius. **V. Vovchenko et al.**

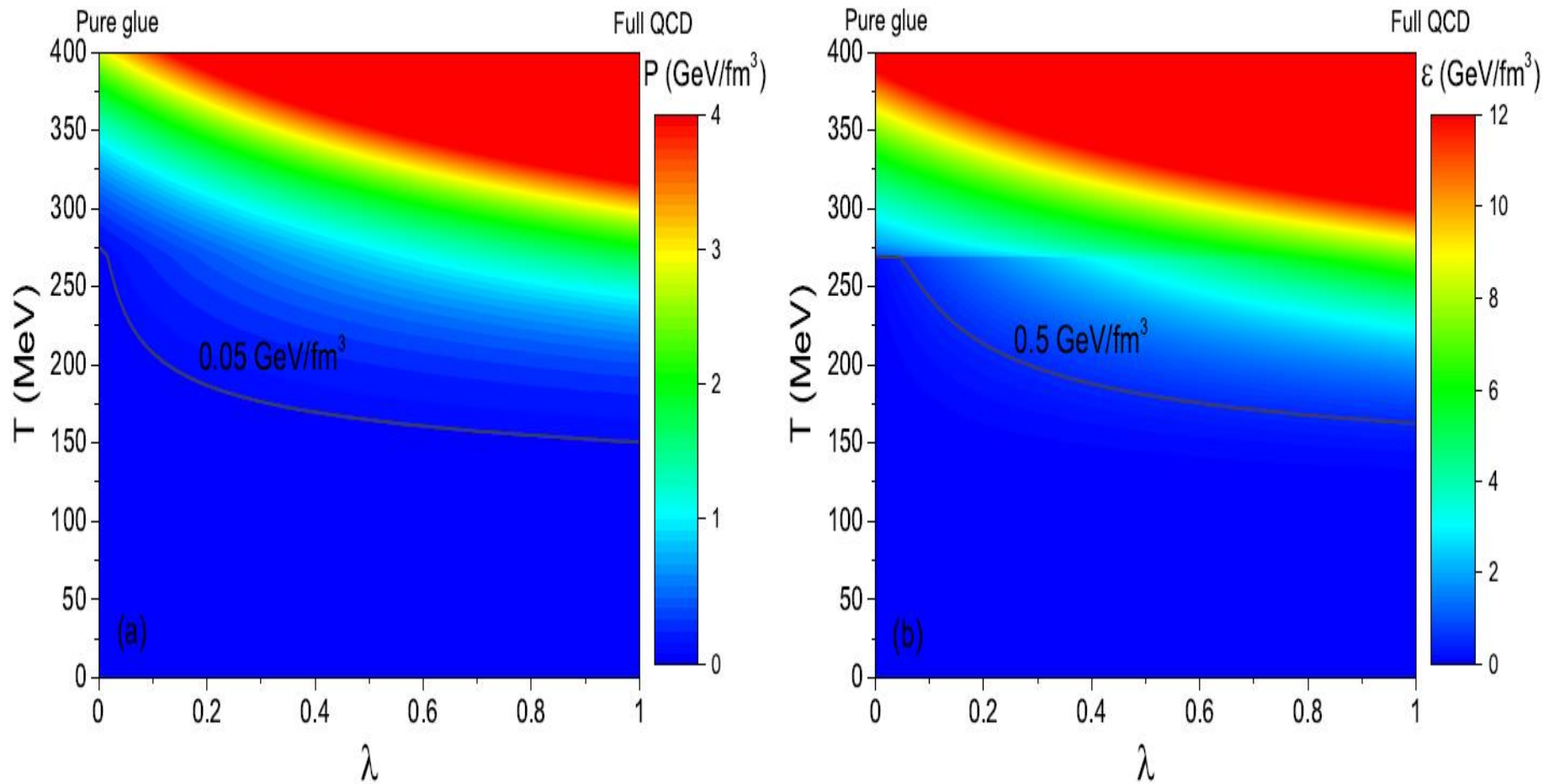


FIG. 3: (Color online) Density plots of pressure (a) and energy density (b) for chemically non-equilibrium QGP calculated from Eqs. (5) and (6). The solid lines show contours $P = 0.05 \text{ GeV}/\text{fm}^3$ (a) and $\varepsilon = 0.5 \text{ GeV}/\text{fm}^3$ (b).

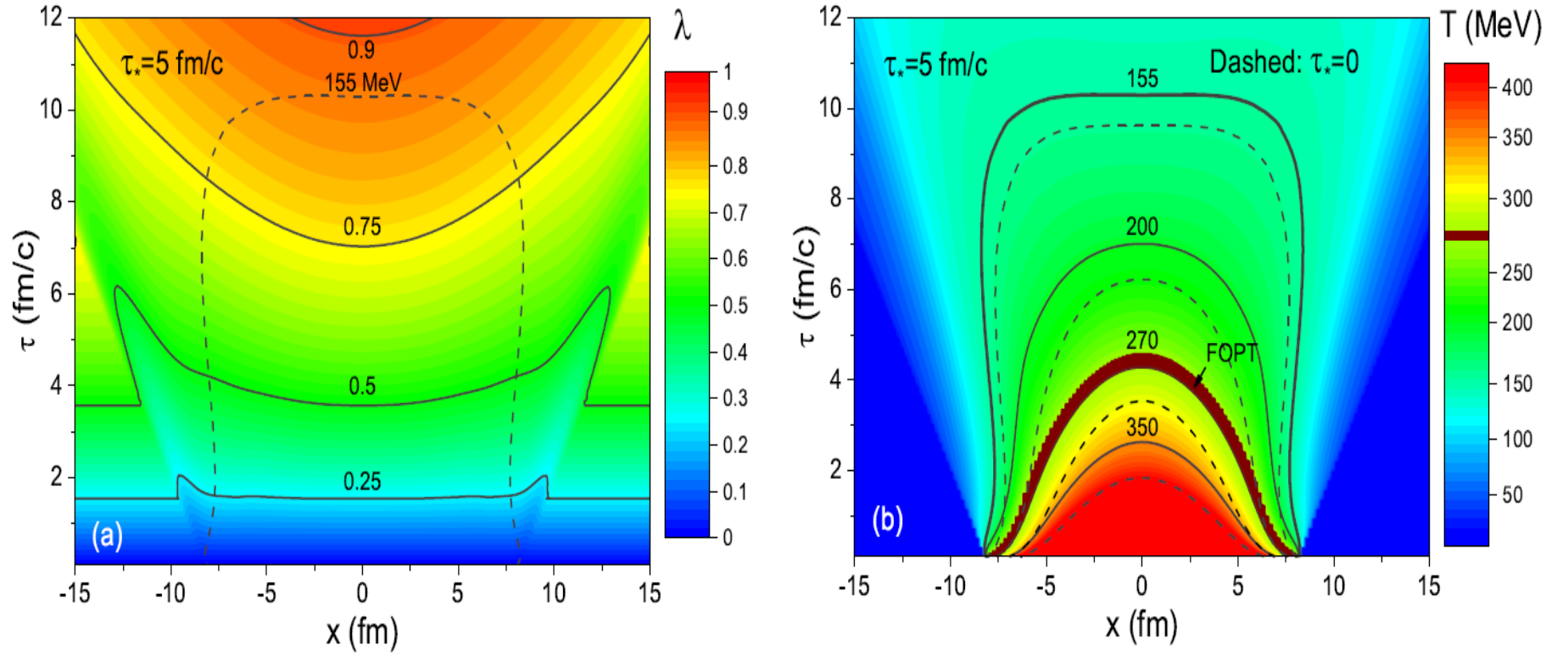


FIG. 4: (Color online) Density plots of the quark fugacity (a) and temperature (b) in the $x - \tau$ plane for the 0–20% most central Pb+Pb collisions at $\sqrt{s_{NN}} = 2.76$ TeV. The solid lines show contours of λ and T (in MeV). The dashed line in (a) corresponds to the isotherm $T = 155$ MeV. The dark region labeled by FOPT corresponds to the mixed-phase region of the first-order phase transition at $T = T_c \simeq 270$ MeV. The dashed lines in (b) are isotherms calculated for equilibrium

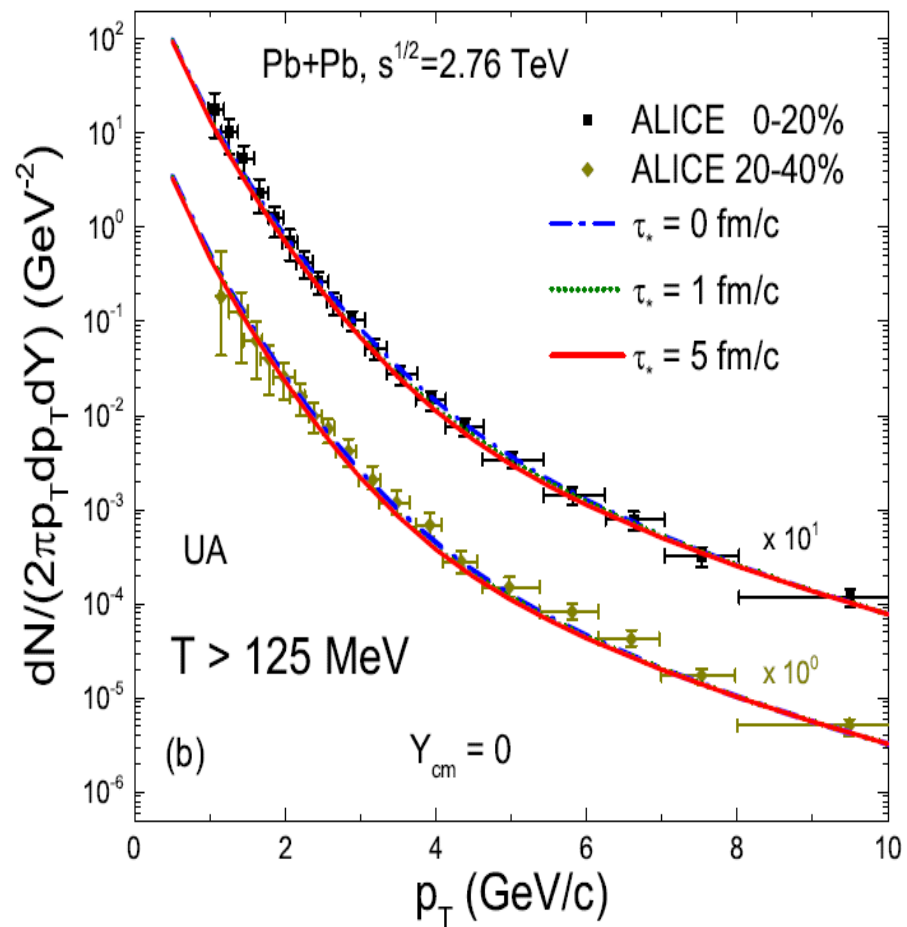
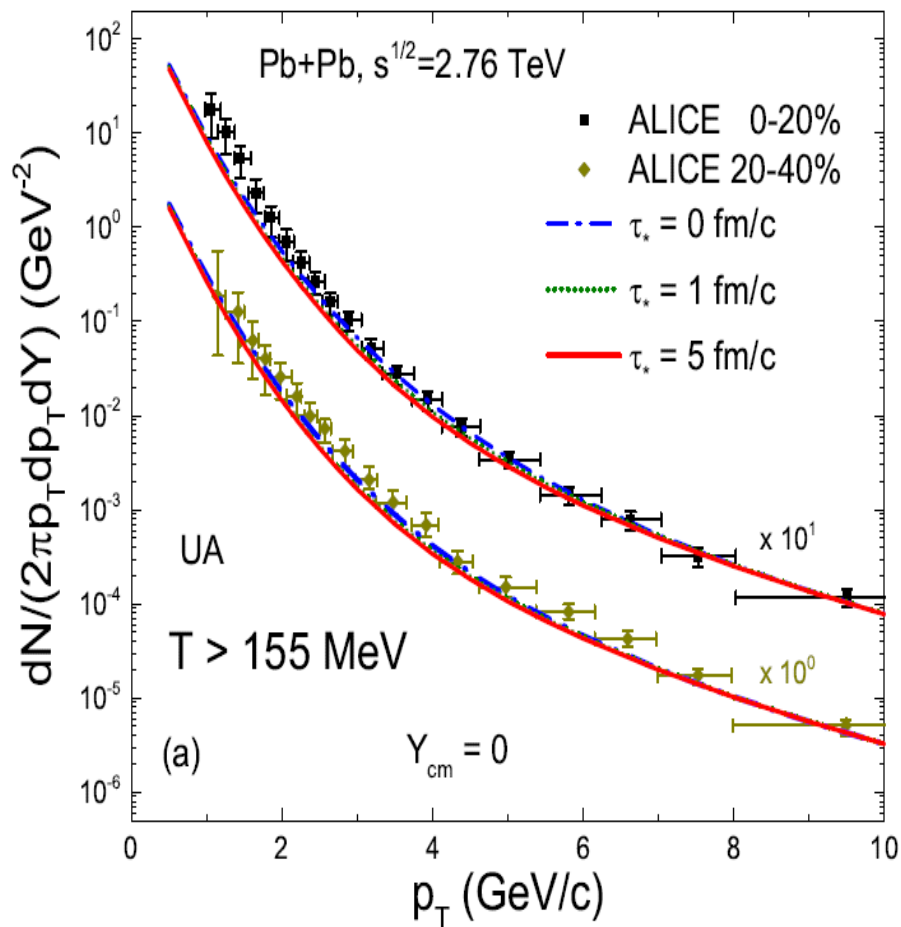


FIG. 8: (Color online) Spectra of direct photons in the 0–20% central Pb+Pb collisions at $\sqrt{s_{NN}} = 2.76$ TeV calculated using Eqs. (13)–(14) with the cutoff temperatures $T_f = 155$ (a) and 125 (b) MeV. The dash-dotted, dotted and solid lines correspond to $\tau_* = 0, 1$ and 5 fm/c, respectively. Dots with error bars show experimental data [42].

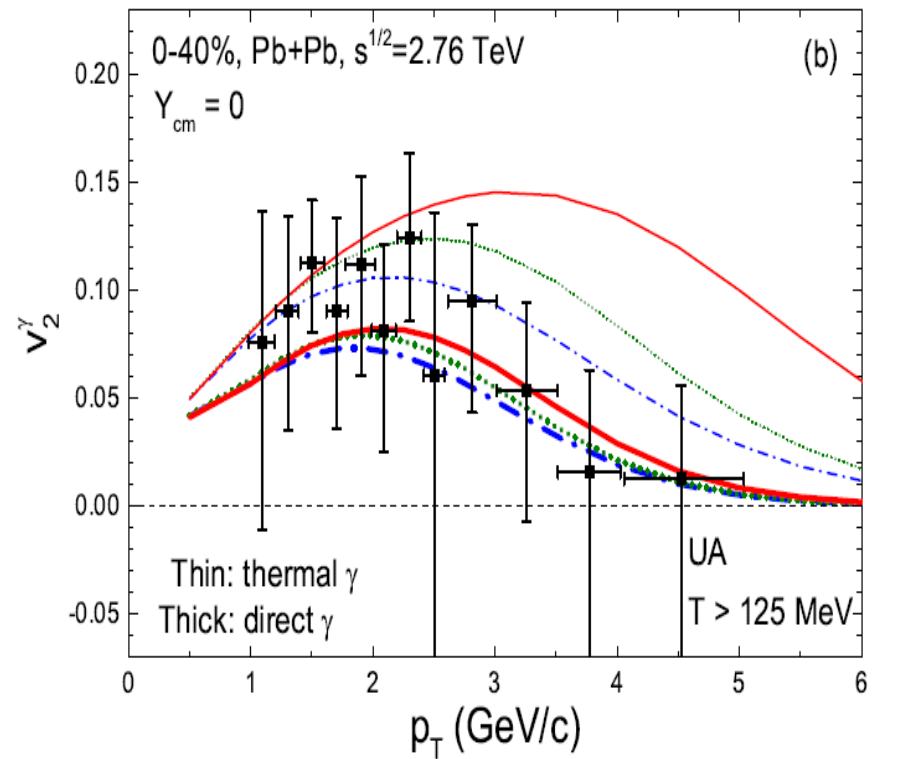
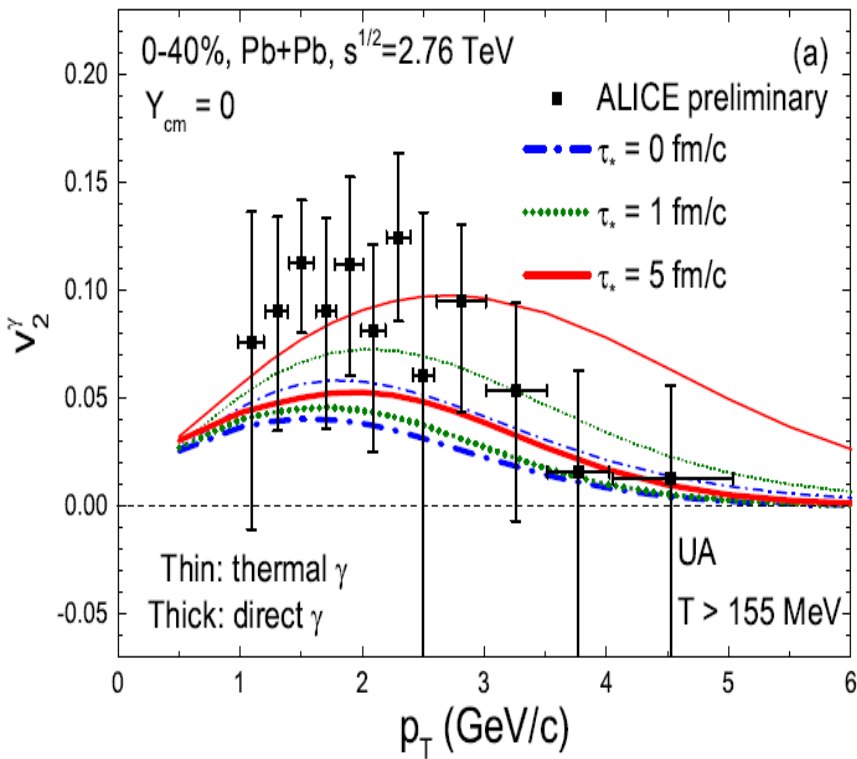


FIG. 9: (Color online) Elliptic flow of direct photons as a function of transverse momentum in the 0–40% central Pb+Pb collisions at $\sqrt{s_{NN}} = 2.76$ TeV calculated with the cutoff temperatures $T_f = 155$ (a) and 125 (b) MeV. The dash-dotted, dotted and solid lines correspond to $\tau_* = 0, 1$ and 5 fm/c, respectively. Thick (thin) curves are calculated with (without) the contribution of prompt photons in Eq. (15). Data are taken from Ref. [39].

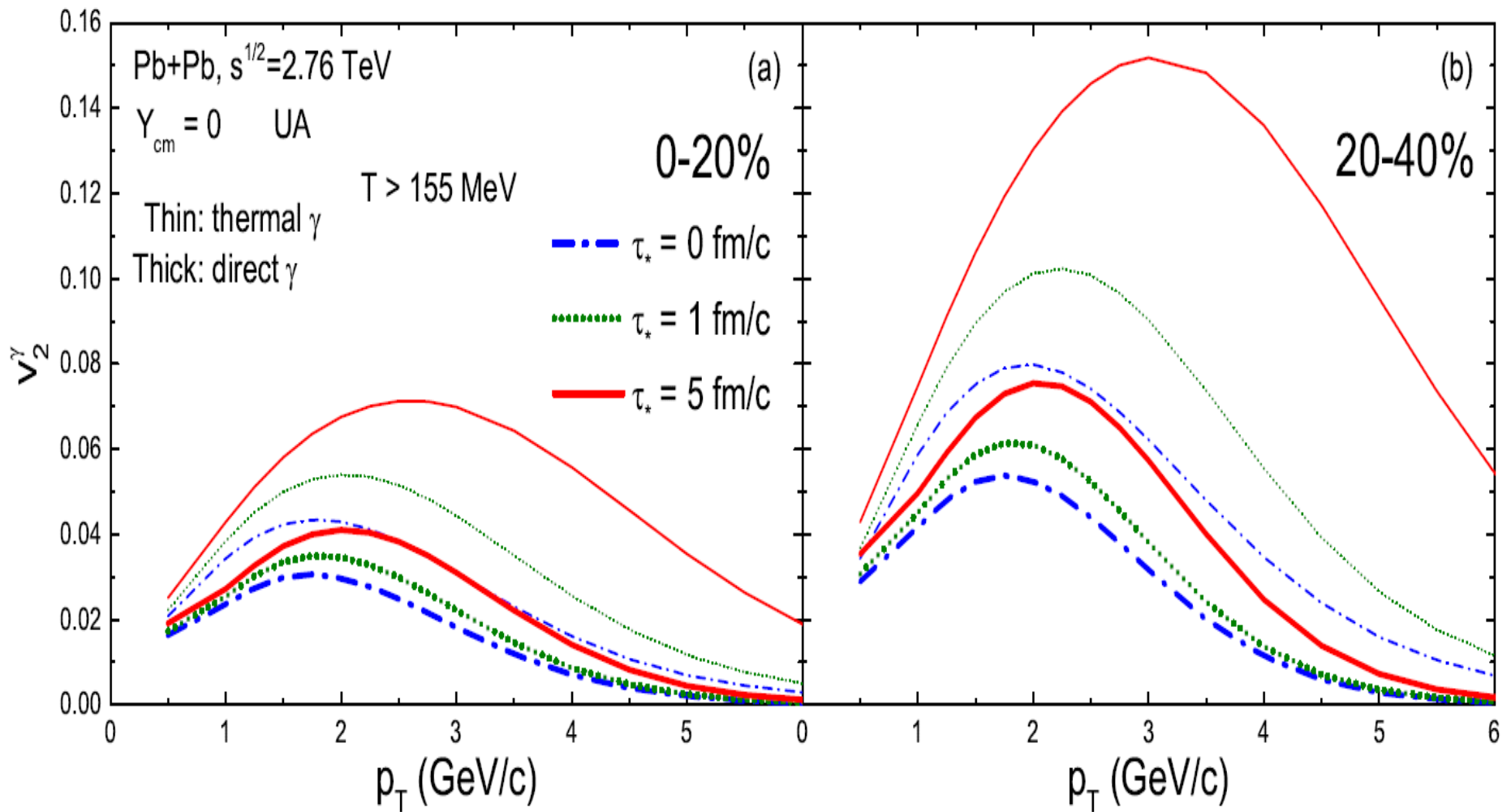


FIG. 10: (Color online) Elliptic flow of the direct (thick lines) and thermal (thin lines) photons for the 0–20% (a) and 20–40% (b) central Pb+Pb collisions at $\sqrt{s_{\text{NN}}} = 2.76$ TeV.

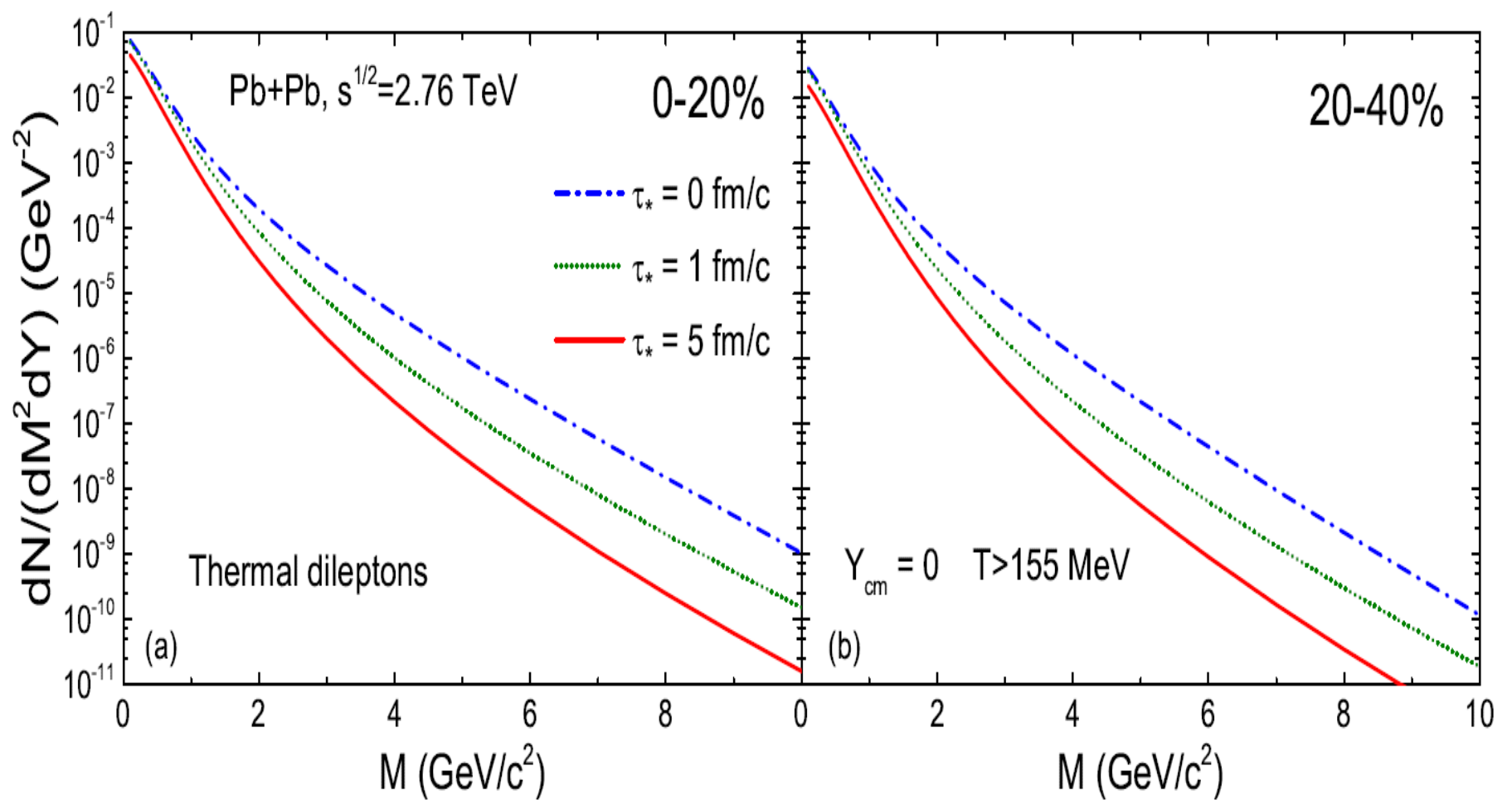


FIG. 11: (Color online) Invariant mass distribution of thermal dileptons in the 0–20% (a) and 20–40% (b) central Pb+Pb collisions at $\sqrt{s_{NN}} = 2.76$ TeV calculated for $\tau_* = 0, 1$ and 5 fm/ c . All results correspond to the cut-off temperature $T_f = 155$ MeV.

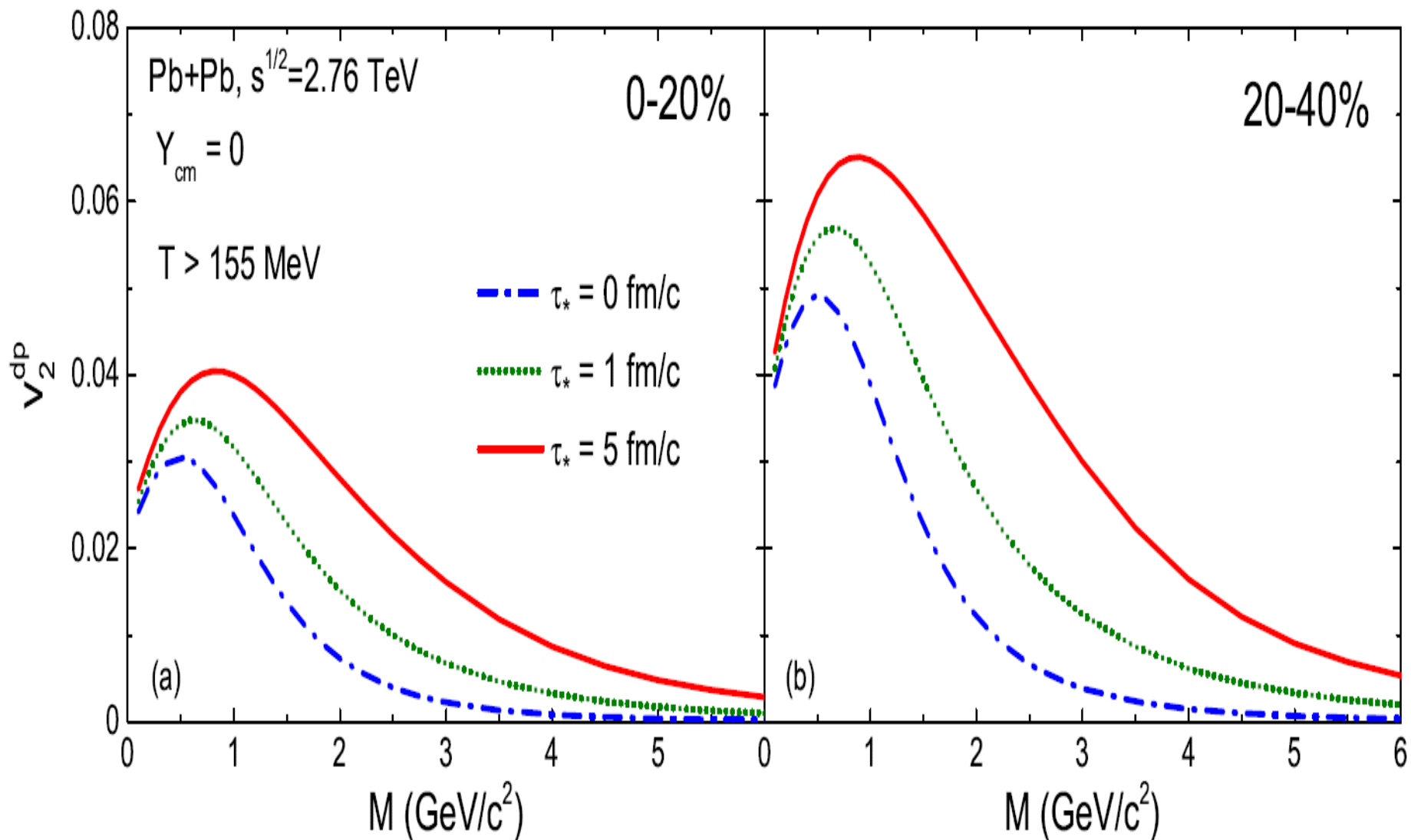
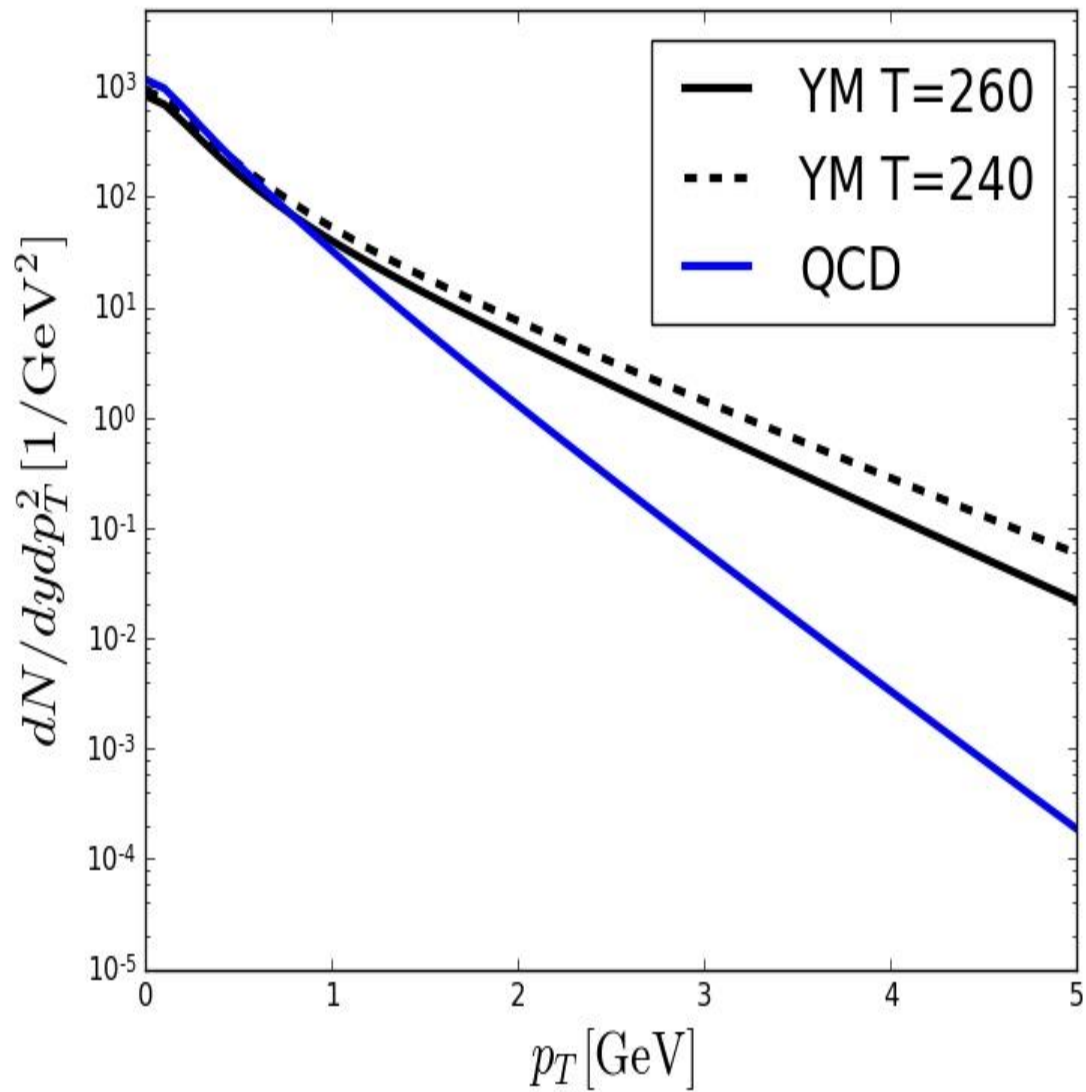
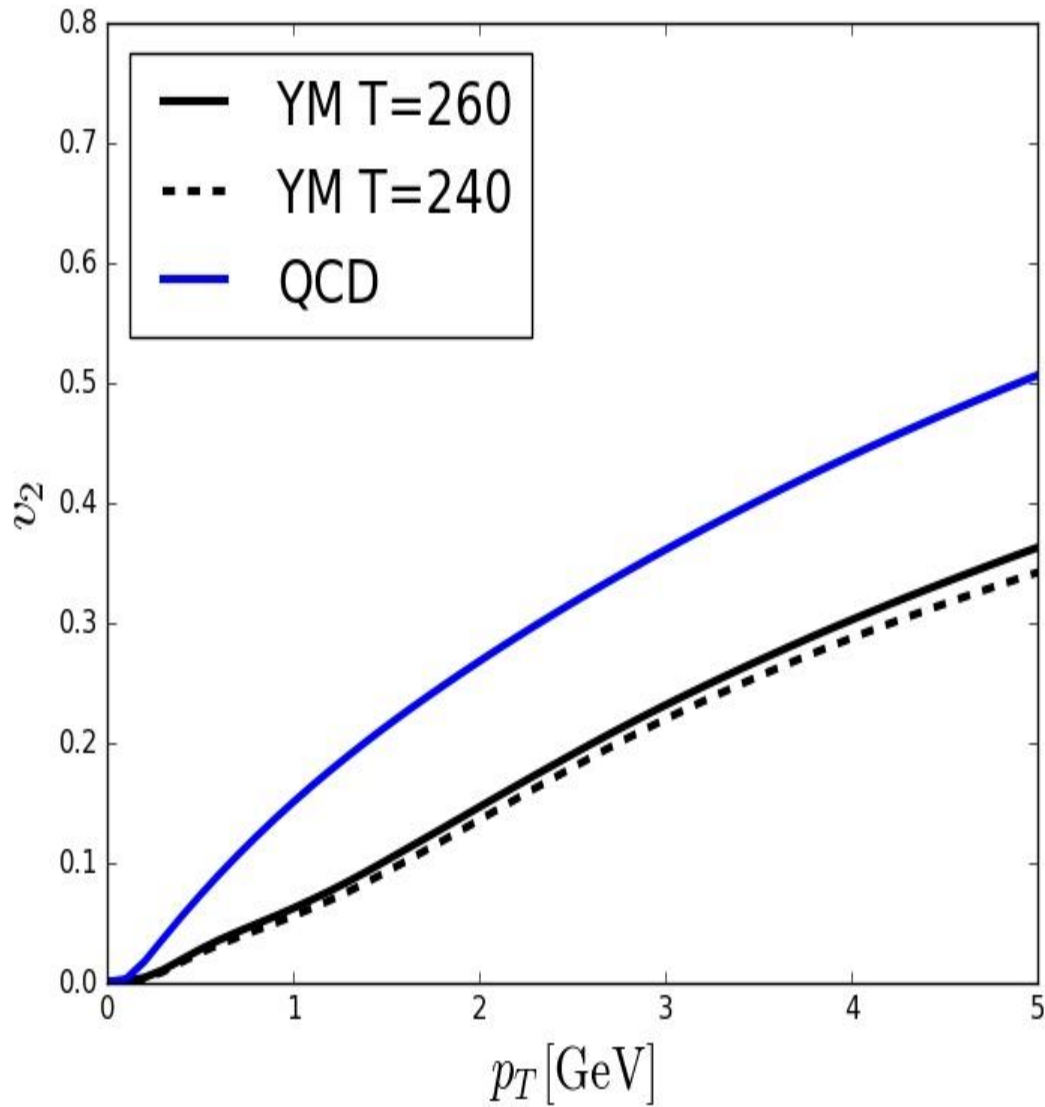


FIG. 12: (Color online) Same as Fig. 11 but for elliptic flow of thermal dileptons.





Identification of Glueballs

Lightest Glueball predicted near two states of same Q.N..

“Over population” Predict 2, see 3 states

Glueballs should decay in a flavor-blind fashion.

$$\pi\pi : K\bar{K} : \eta\eta : \eta'\eta' : \eta\eta' = 3 : 4 : 1 : 1 : 0$$

Production Mechanisms:

Certain are expected to be **Glue-rich**, others are Glue-poor. Where do you see them?

Proton-antiproton

Central Production

J/ψ decays

Observation of **Glueballs** in pp, pA, AA

- violent pp (& AA) collisions
- initial state at LHC:
- Color Glass Condensate
- $t=0.1\text{fm}/c$: glue thermalizes
- **pure glue-plasma** created
- Quenched Lattice $SU(3)_c$:
- **$T_c = 270\text{MeV}$**
- glue plasma \rightarrow **GlueBall fluid**
- 1. Order Phase Transition
- Expansion to critical point
- **$T_{cp} = 240\text{MeV}$** $t \sim 1-2\text{fm}/c$
- **GlueBalls** + Hagedorn States Mix
- more and more quarks produced: **$T_{c.o.} = 155\text{MeV}$** crossover transition
- **Observables** from Columbia plot
- $T > T_{cp}$: **Zero e.m. radiation**
- Measure $T \sim 270\text{MeV}$ Dilepton mass
- T_c : **Flow collapse** as barometer
- T_{cp} : **Critical Scattering (MG, WG)**,
- Kurtosis , # fluctuations
- $T_c \sim 2 * T_{co} \Rightarrow$
- $P_t(pp) \sim 2 * p_t(AA)$
- $M_{\text{GlueBalls}} < 2\text{GeV}$: „**No**“ Baryons
- **$p/\pi \sim 0$** : Yield $p+p\bar{p} \ll$ mesons
- Lightest GlueBall decays:
- - No decays to 2 Omega, no 2 Rho
- Glue Flavor blind !
- **$K/\pi=1$** Yields: Kaons \sim pions

Alternate Scenario: pure gauge matter in pp, pA – AA ?

Initial Color Glass Condensate \Rightarrow Glasma thermalizes
fast equilibration of Gluons, **slow** equil. of quarks
high pressure, entropy **gluon** plasma
 \Rightarrow **fast** hydrodynamic expansion of **gluon** plasma.



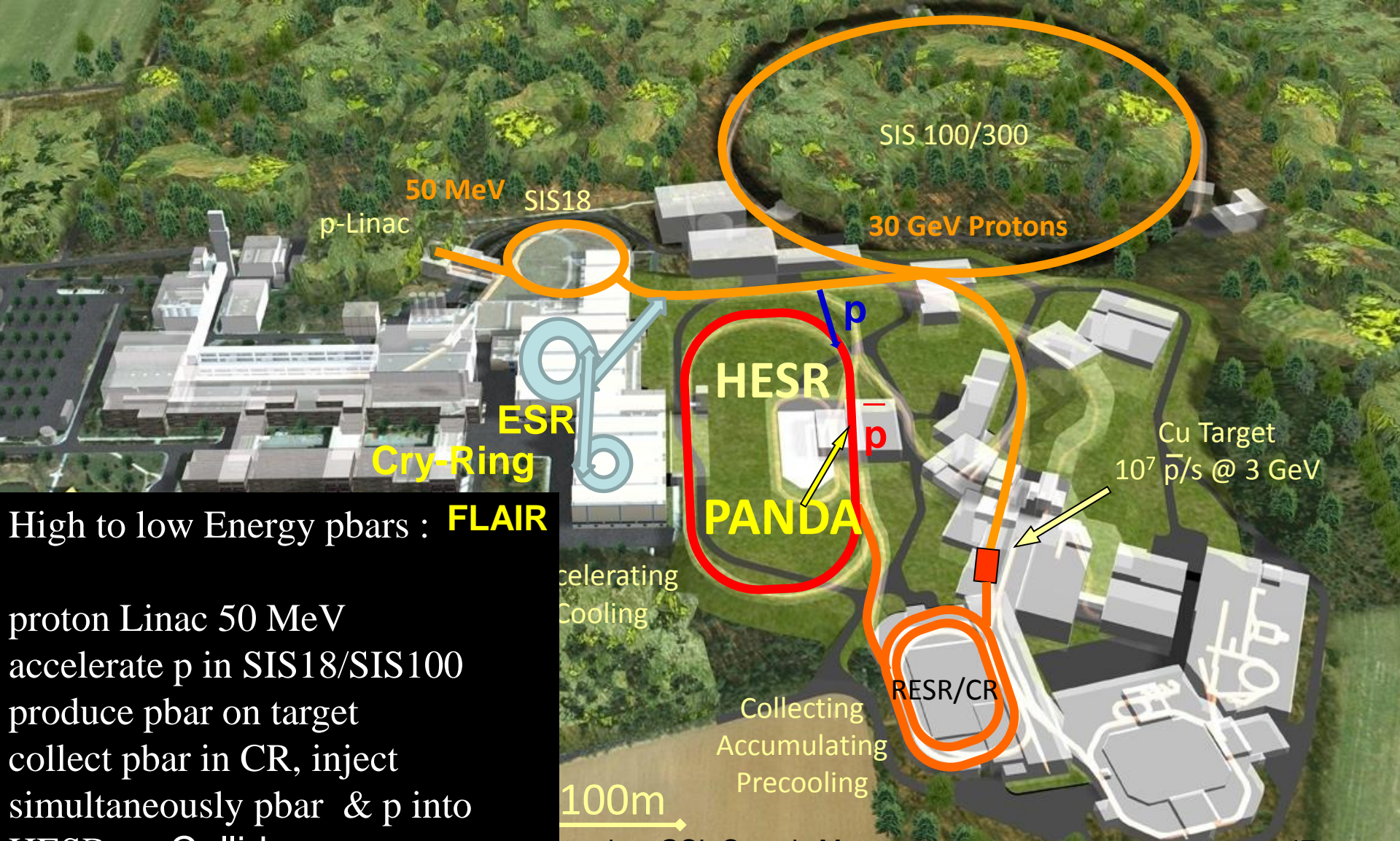
1. Order Phase Transition at $T_c = 270$ MeV of flavorless QCD.



Transition from glue plasma in GlueBall fluid



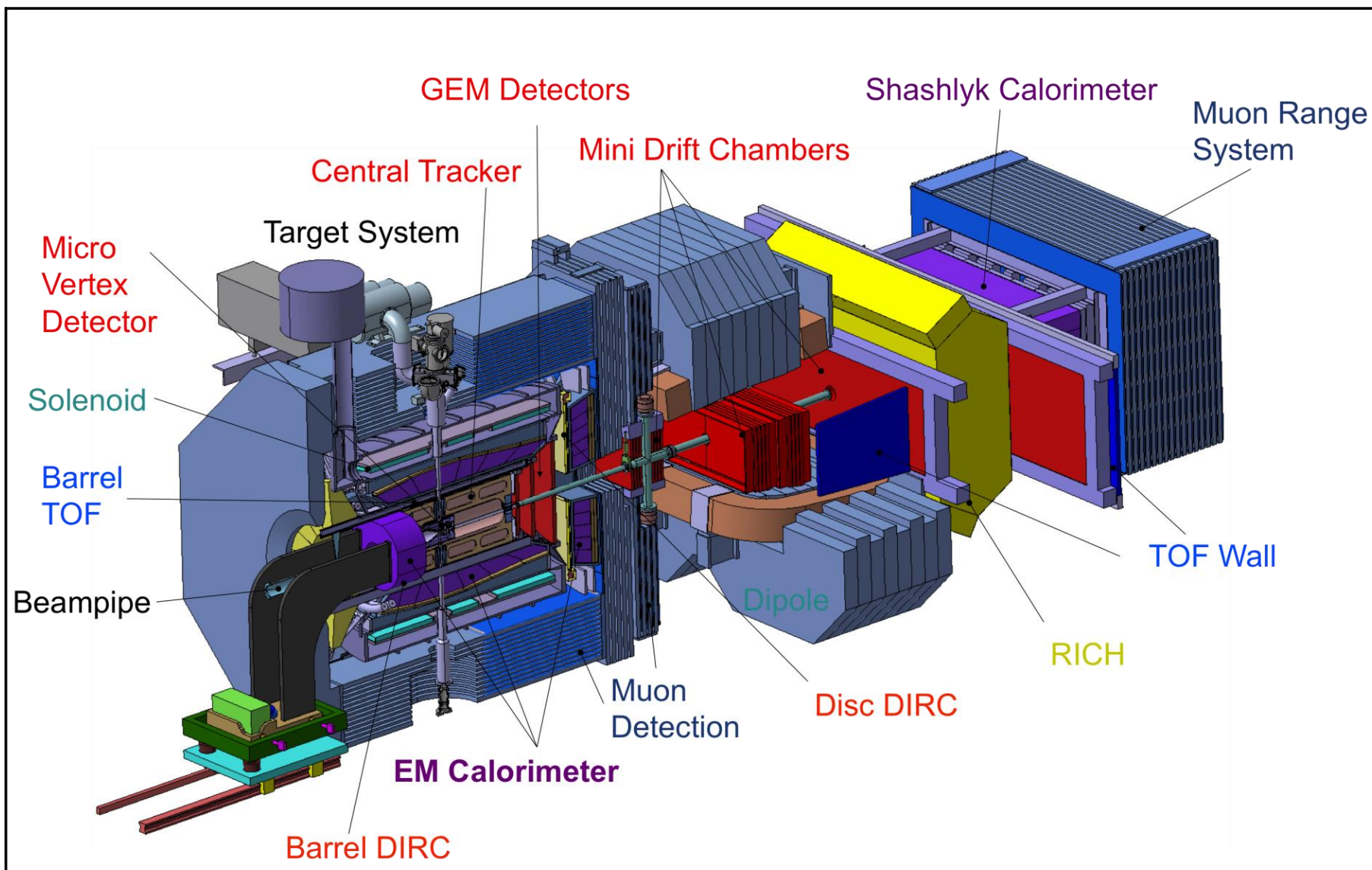
Glueball-Hagedornstates mix with quarks, decay into Hadrons



High to low Energy pbars : **FLAIR**

proton Linac 50 MeV
 accelerate p in SIS18/SIS100
 produce pbar on target
 collect pbar in CR, inject
 simultaneously pbar & p into
 HESR as Collider :
 32 GeV pure glue !

PANDA Detector



PANDA Program: 2 GeV – 5.5 GeV

I: Hadron spectroscopy

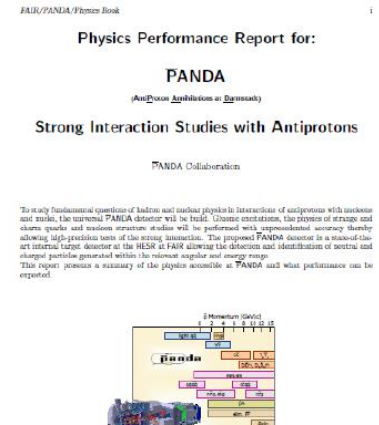
light mesons, baryons, charmonium, open charm,
QCD exotics: **glueballs**, hybrid states, **X,Y,Z**

II: Electromagnetic processes

time like form factors, transition distribution
amplitudes, TMDs, ...

III: Hadronic interactions:

Hyperons, **Hypernuclei**,
In medium-effects



ArXiv:0903.3905

PANDA physics workshop in Uppsala, June 8 – 12, 2015

Frank Meade
2015

X(3872): PANDA vs. Belle II And BES III

Some numbers, considering $J/\psi \pi^+\pi^-$ decay mode only:

- **PANDA**, assume $\sigma(pp \rightarrow X(3872))=50$ nb
statistics ~ 130 (1300) per day on peak for $\mathcal{L}=2 \times 10^{31}$ (10^{32}) $\text{cm}^{-2} \text{s}^{-1}$
efficiency $\sim 50\%$ (4 charged, exclusive)
high boost $R \rightarrow 0.80$ (fixed target) $\rightarrow R \sim 1.05$

mass 350 X(3872)/day

- **Belle**
statistics 820 Y(4260)/day

efficiency 176 Z(3900)/day

small boost $p\gamma=0.45$ (Belle), $p\gamma=0.20$ (Belle II)

mass resolution $\sim 10\text{-}20$ MeV (unfitted)

- **BESIII**

$e^+e^- \rightarrow Y(4260) \rightarrow \gamma X(3872)$ BESIII, Phys. Rev. Lett. 112(2014)092001

≈ 1200 Y(4260) per day ($\sigma \approx 60$ pb, integrated luminosity $\sim 20 \text{ pb}^{-1}/\text{day}$)

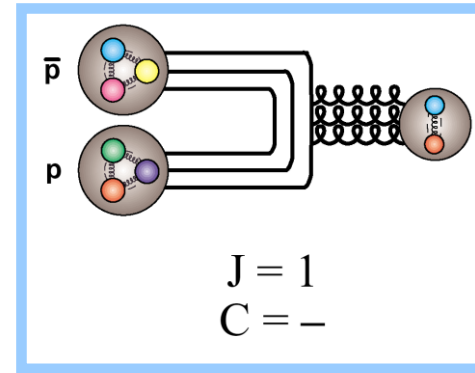
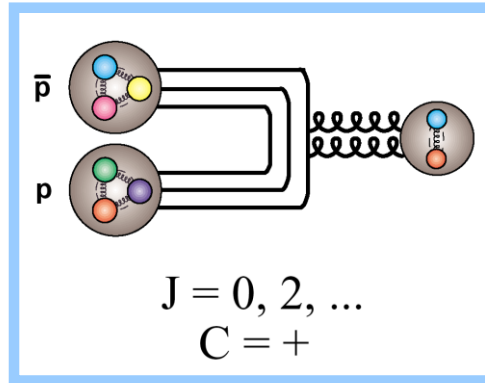
but branching fraction small, only $\approx 0.5\%$ (≈ 20 events in ~ 4 weeks)

rare

PANDA is an X Y Z factory | measurement of X(3872), lineshape!

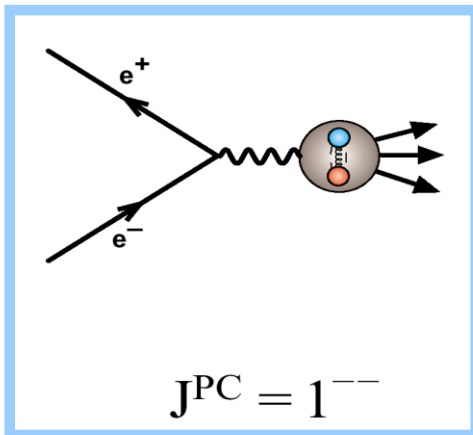
Particle production in $\bar{p}p$ collisions

Formation:



All J^{PC} allowed for $(\bar{q}q)$ accessible in $\bar{p}p$

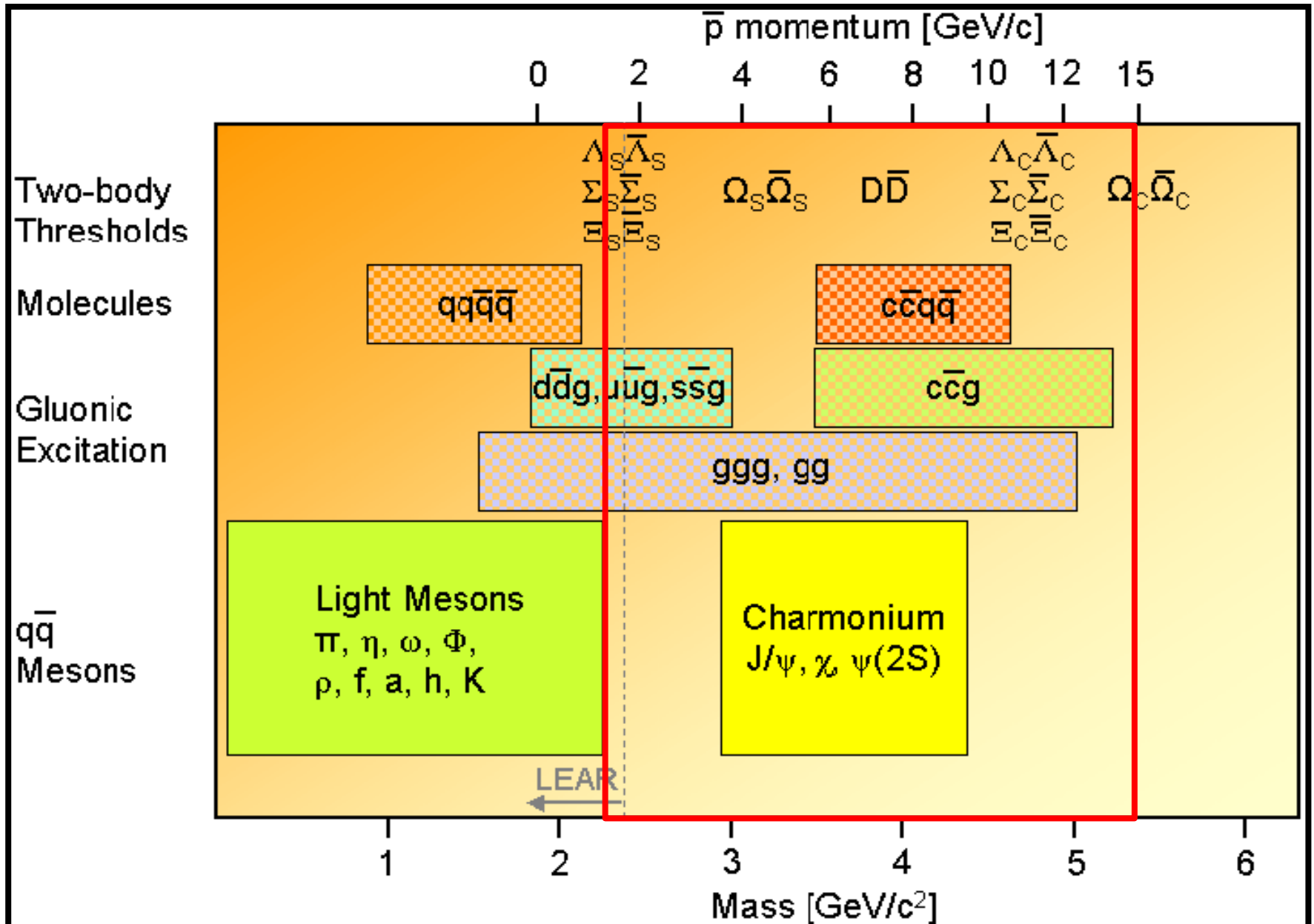
c.f.



Only $J^{PC} = 1^{--}$ allowed in e^+e^-
(to 1st order)

X, Y, Z, Charm-Hybrids, Penta-Quarks, Tetra-quarks, Glue-Balls

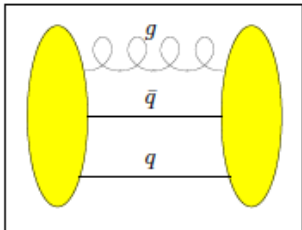
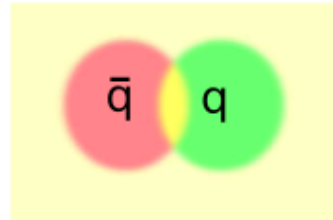
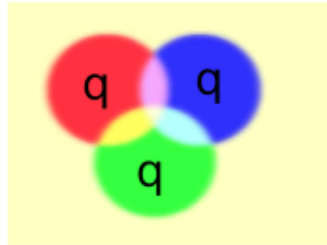
- PANDA explores their properties up to masses ~ 5.5 GeV



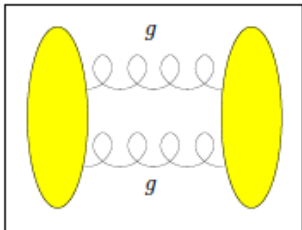
Beyond standard quark configurations

- QCD allows much more than what we have observed:

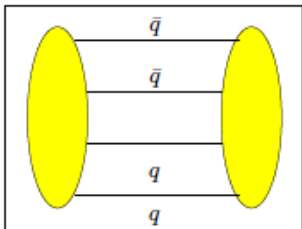
Exotica



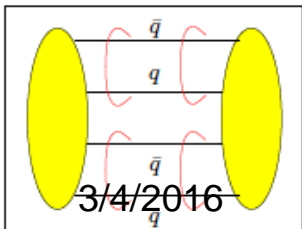
hybrid:
with gluon excitation



glueball:
pure gluon state



4 quark state:
compact 4-quark state



hadronic molecule:
bound state of two mesons

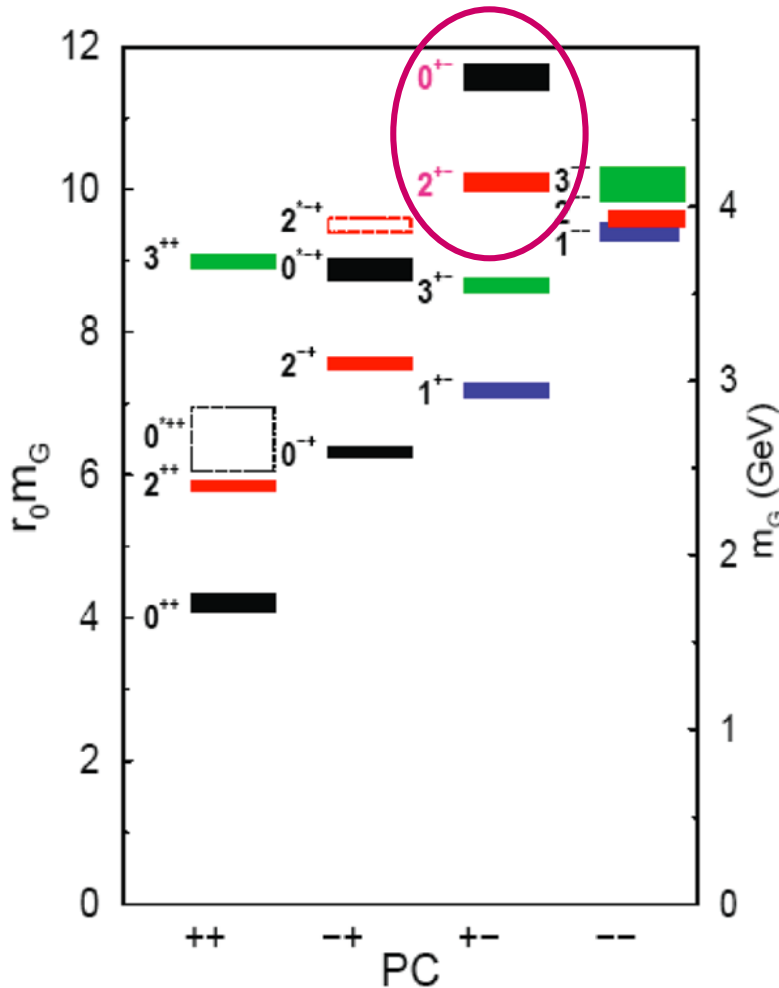
Mesons

} may have J^{PC}
not allowed for
qq

Courtesy C. Hanhart

Lattice QCD vs pure YM: glueballs

Search for Heavy Glueballs



• Charmed Glueballs

- flavour blind decays
 - charmed final states
- only a few charmed mesons around 3 - 4 MeV/c²
 - less mixing

• Exotic glueballs (oddballs), no mixing!

- $m(2^{+-}) = 4140(50)(200)$ MeV
- $m(0^{+-}) = 4740(70)(230)$ MeV
- decay modes $\phi\phi$, $\phi\eta$, $J/\psi\eta$, $J/\psi\phi$
- **Narrow widths predicted**

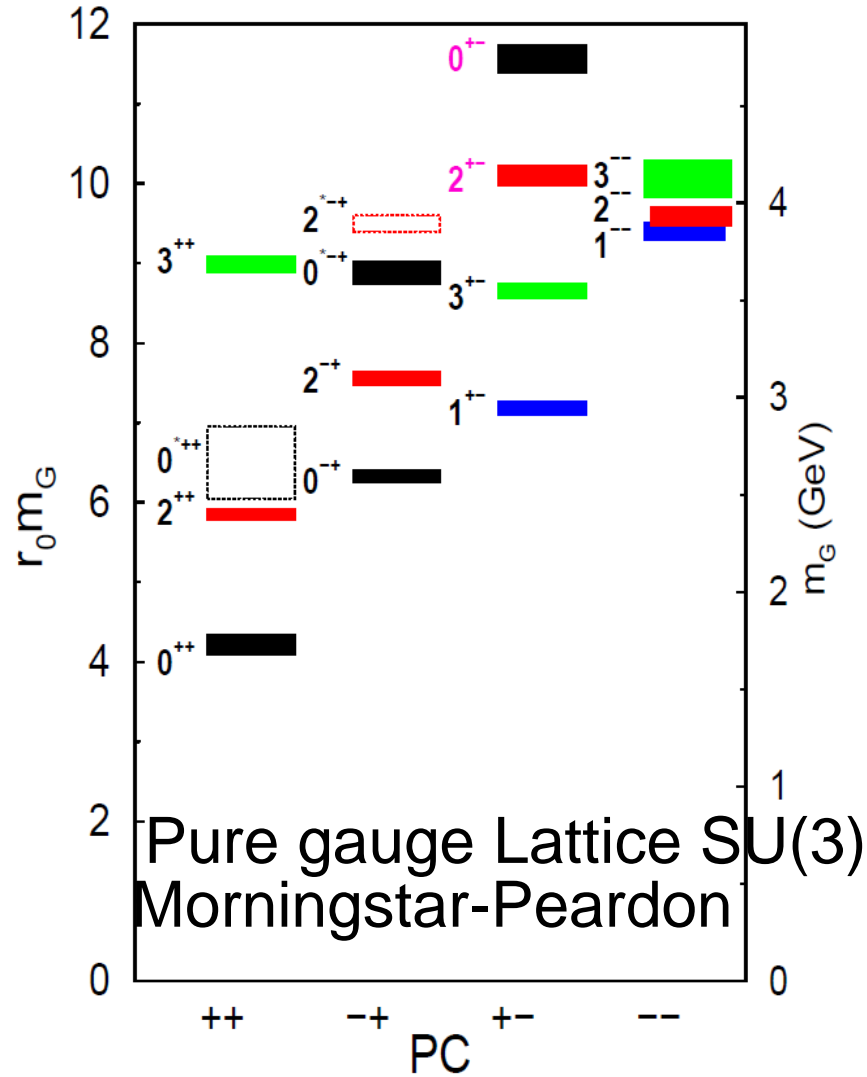
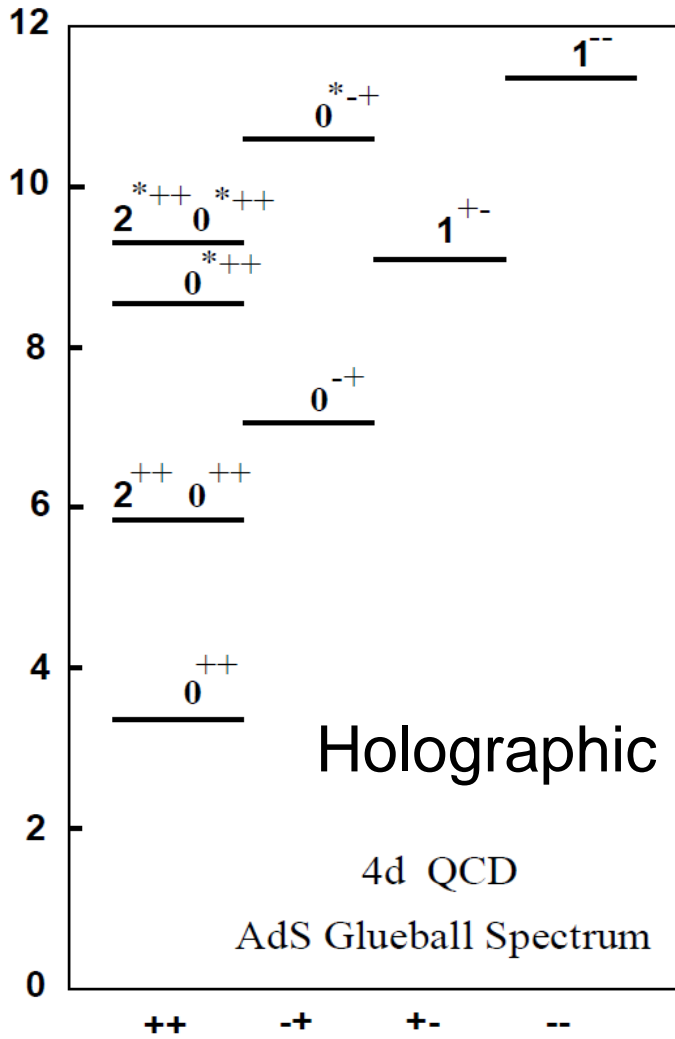
Morningstar & Peardon, PRD60(1999)34509

Morningstar & Peardon, PRD56(1997)4043 **QUENCHED pure gauge** Lattice theory

H. Stoecker, GSI: Cosmic Matter at FCC, LHC, RHIC and FAIR

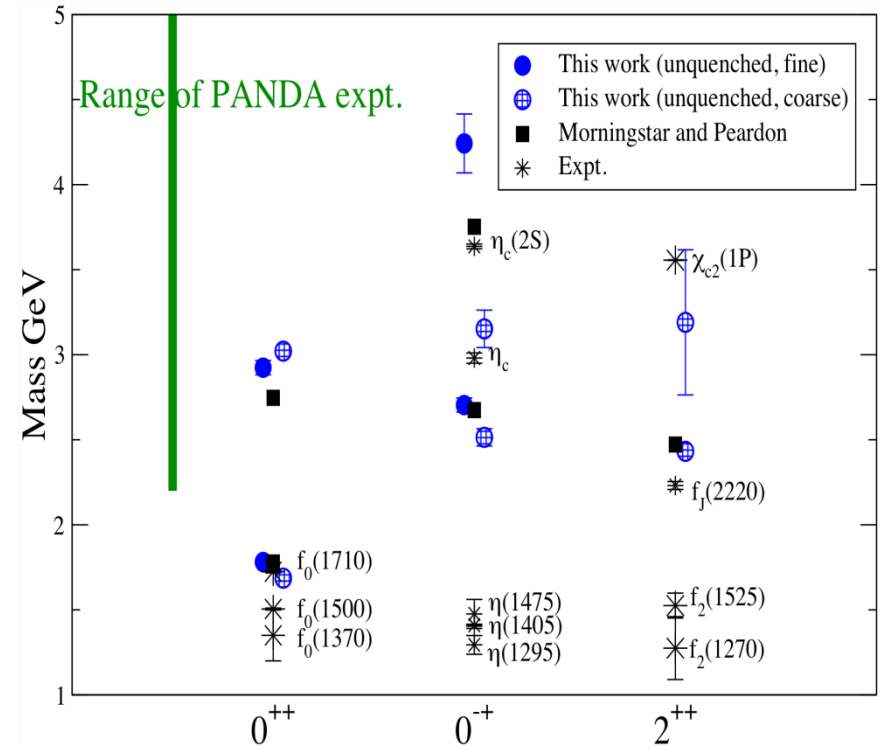
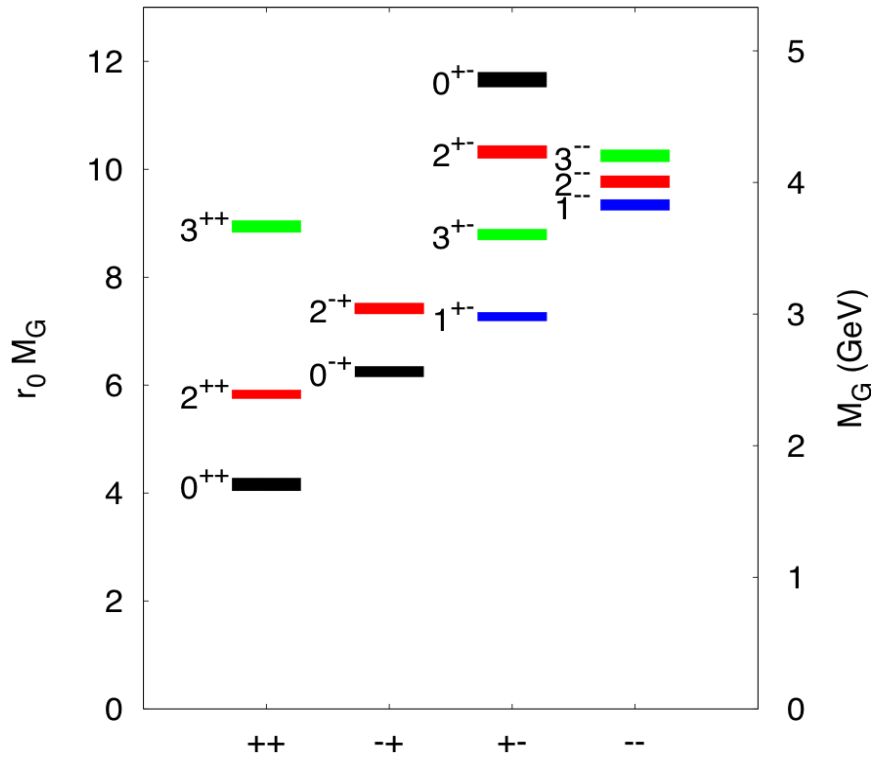
Holographic vs. lattice glueball spectra

Seiji Terashima, YITP, Kyoto, Koji Hashimoto, Riken, Chung-I Tan, Brown, arXiv:0709.2208



Brower-Mathur-Tan, 2000
 $P_\tau = -1$ dropped

Glueball spectrum



Pure YM gauge theory on the lattice:

a hot glue plasma

a 1. Order PhaseTransition,

a warm Glueball Fluid ! ?

The early eighties: predictions of QCD phase structure

1. **two** different phase transitions:

Svetitsky&Yaffe: **F.O.P.T.** in pure gauge YM theory:

“glueplasma – GlueBall fluid” – no quarks!

Pisarski&Wilczek: **chiral massless quarks**

F.O.P.T QGP-Hadrons, but crossing if quark mass nonzero

2. - **two** chemical saturation eq. timescales in RHICs:

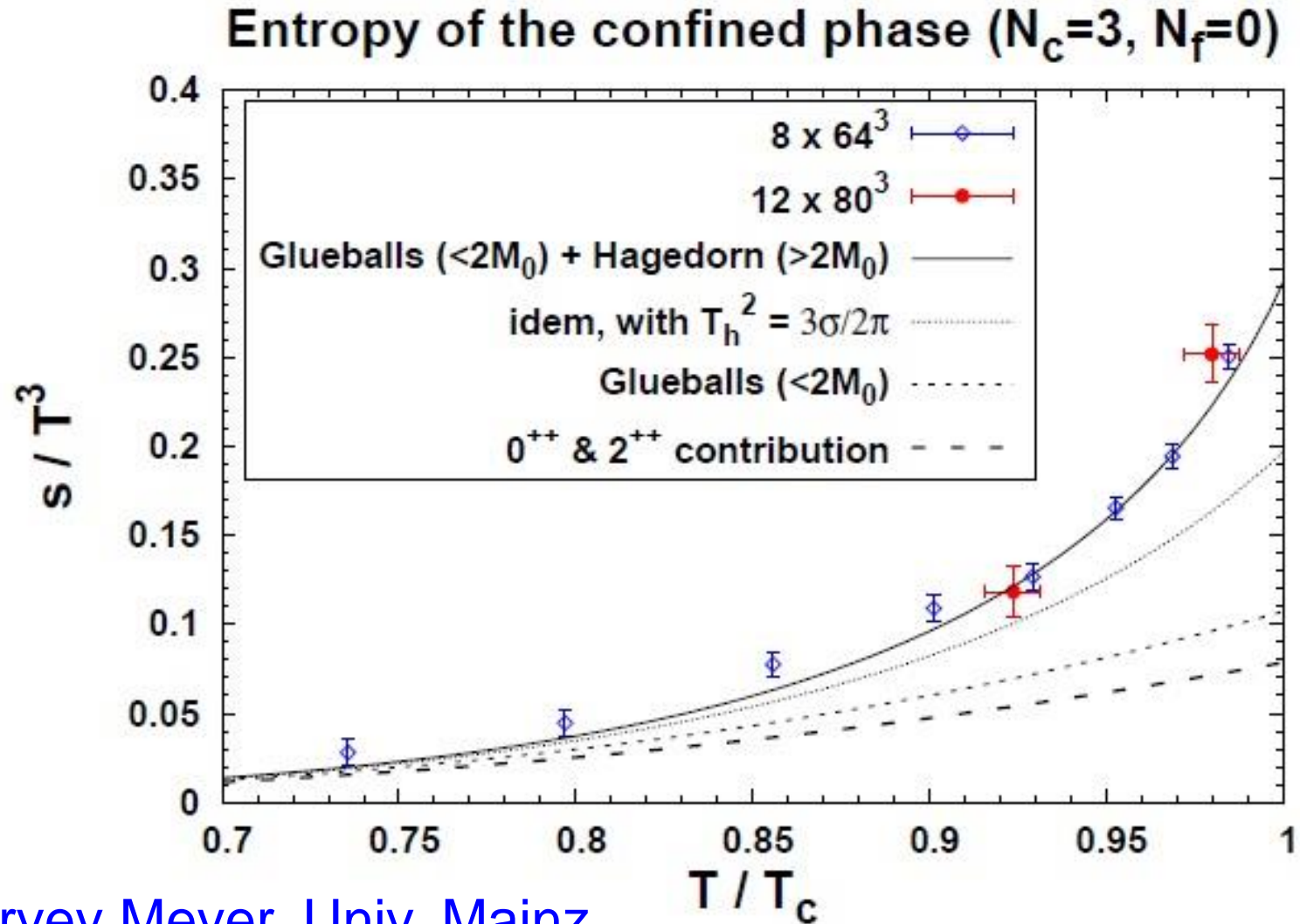
Raha/Sinha; Shuryak; T. Biro, B. Mueller, X.Y. Wang **Transport Theory**

Fast chemical saturation: pure **glue!** But **Slow** saturation: **quarks !**

Search for pure gauge YM F.O.P.T. at early times in colliders?

=> Early pp, pA: **Glue** <=> **GlueBall**: **new QCD phase structure?**

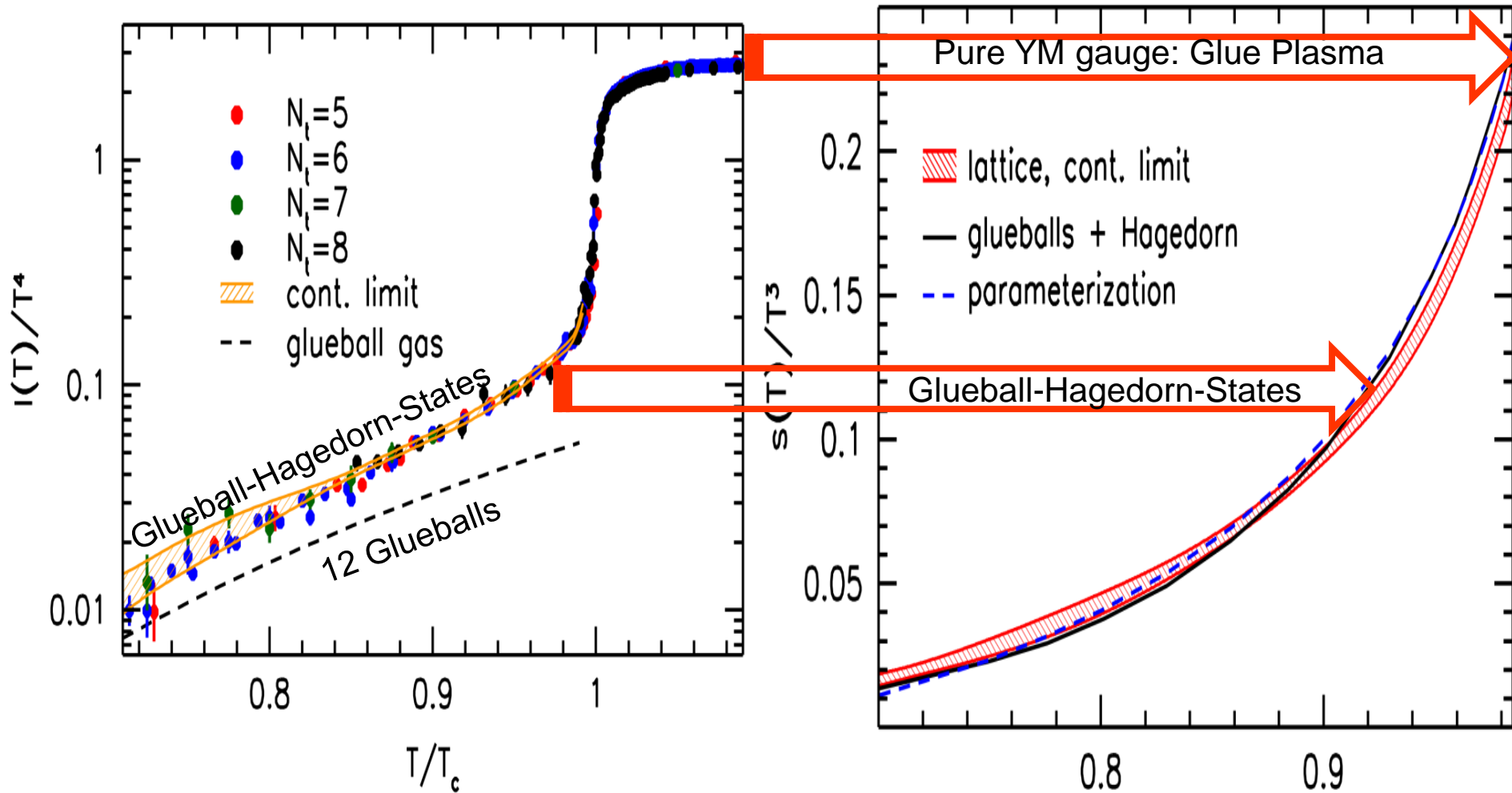
Pure LGT thermal GlueBall-matter observed at RHIC and LHC !?



Harvey Meyer, Univ. Mainz

FIG. 3: The entropy density in units of T^3 for $LT = 8$. We applied a (modest) volume-correction to the $N_t = 12$ data.

Lattice Gauge Thermodynamics of the GlueBall-matter fluid



Wuppertal-Budapest (W.-B.) Collaboration: JHEP 1207 56 ('12)

High precision continuum result for the quenched equation of state. T/T_c

Low temperature behavior and phase transition described by Hagedorn-GlueBall spectrum

W.-B. use 12 **GlueBall** states (Morningstar-Peardon) plus **Hagedorn-GB** towers

(as proposed by Harvey Meyer).

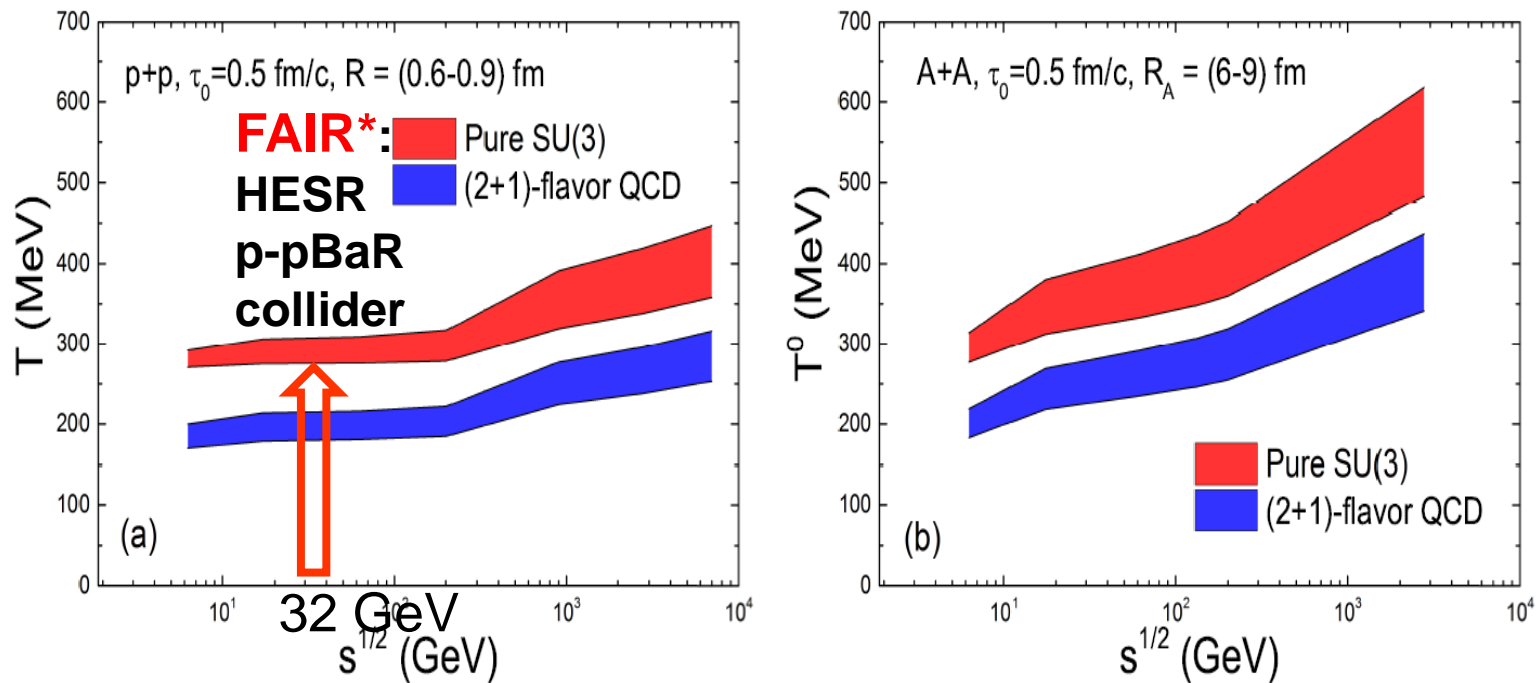
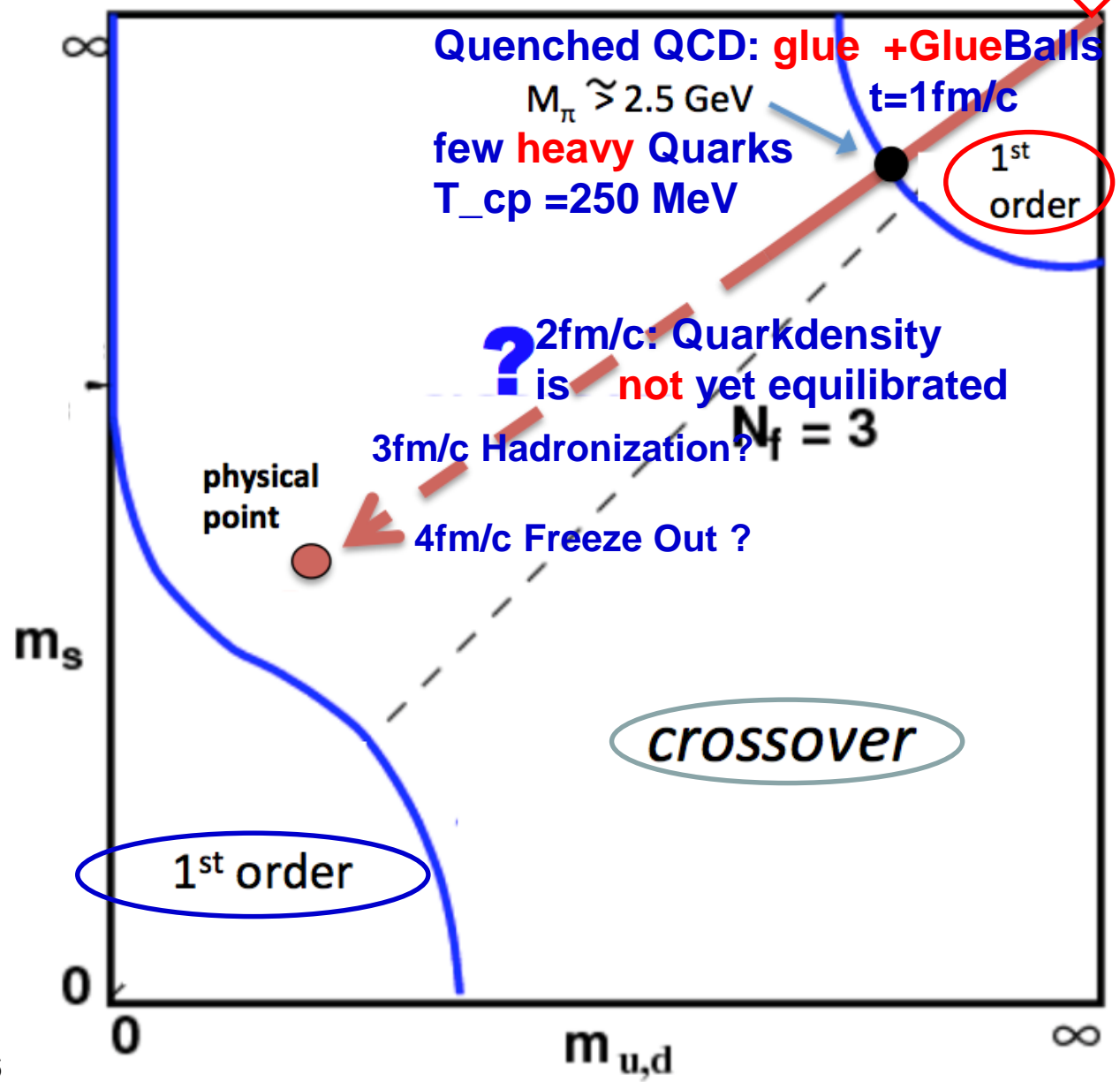


FIG. 6: (Color online) Dependence of the initial temperature T^0 on the collision energy for QGP and pure SU(3) scenarios in (a) p+p and (b) A + A collisions. The uncertainty bands result from variation of the transverse radius.

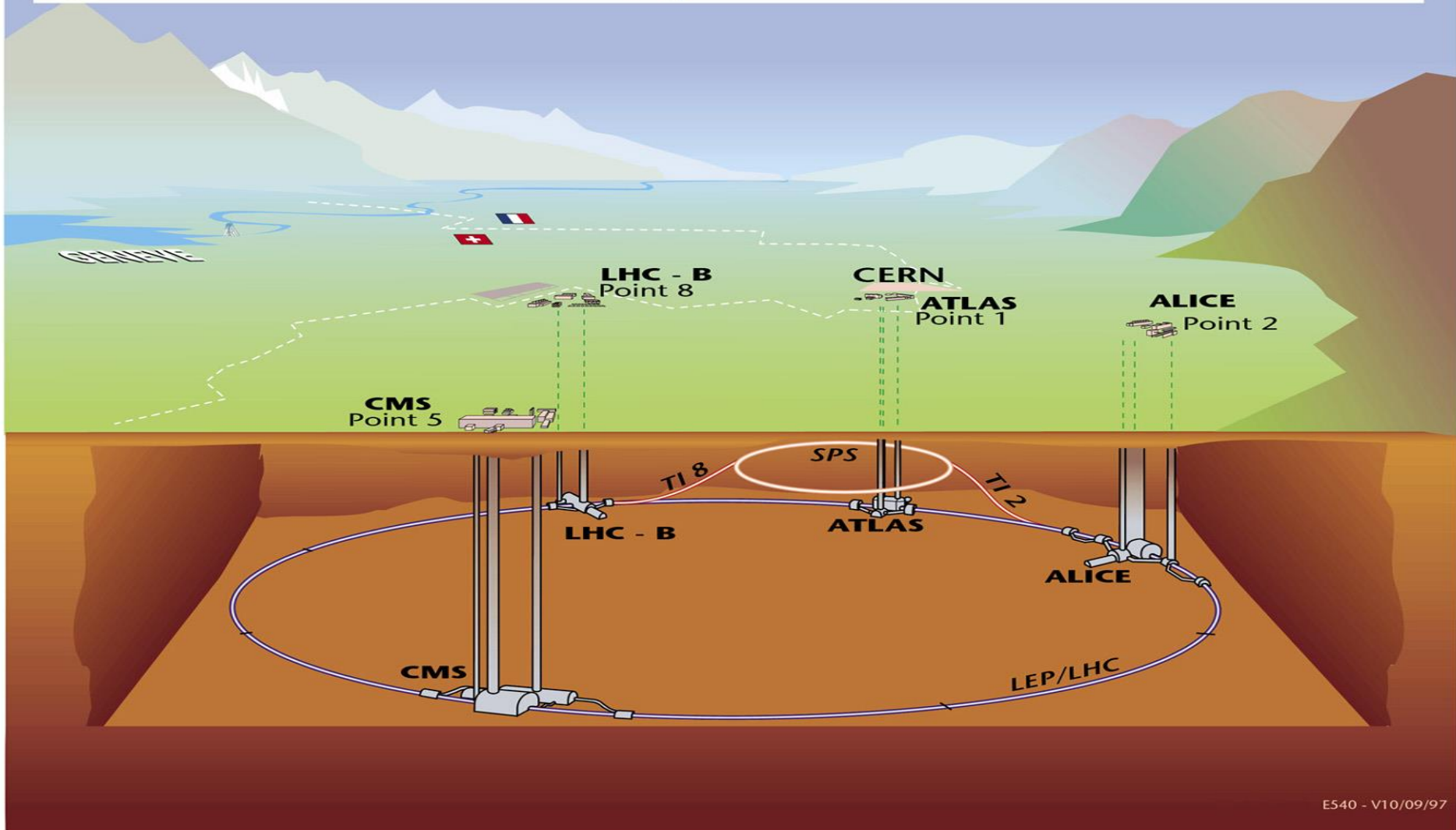
LHC/RHIC/FAIR*: time evol. in pp & AA pure gauge: glue only!
 $t=0.1\text{fm}/c$ No Quarks!



SU(3)_color Lattice Gauge Theory
 Columbia Plot: Order of Phase Transitions

Cosmic **GlueBall-Matter** at CERN LHC and BNL RHIC

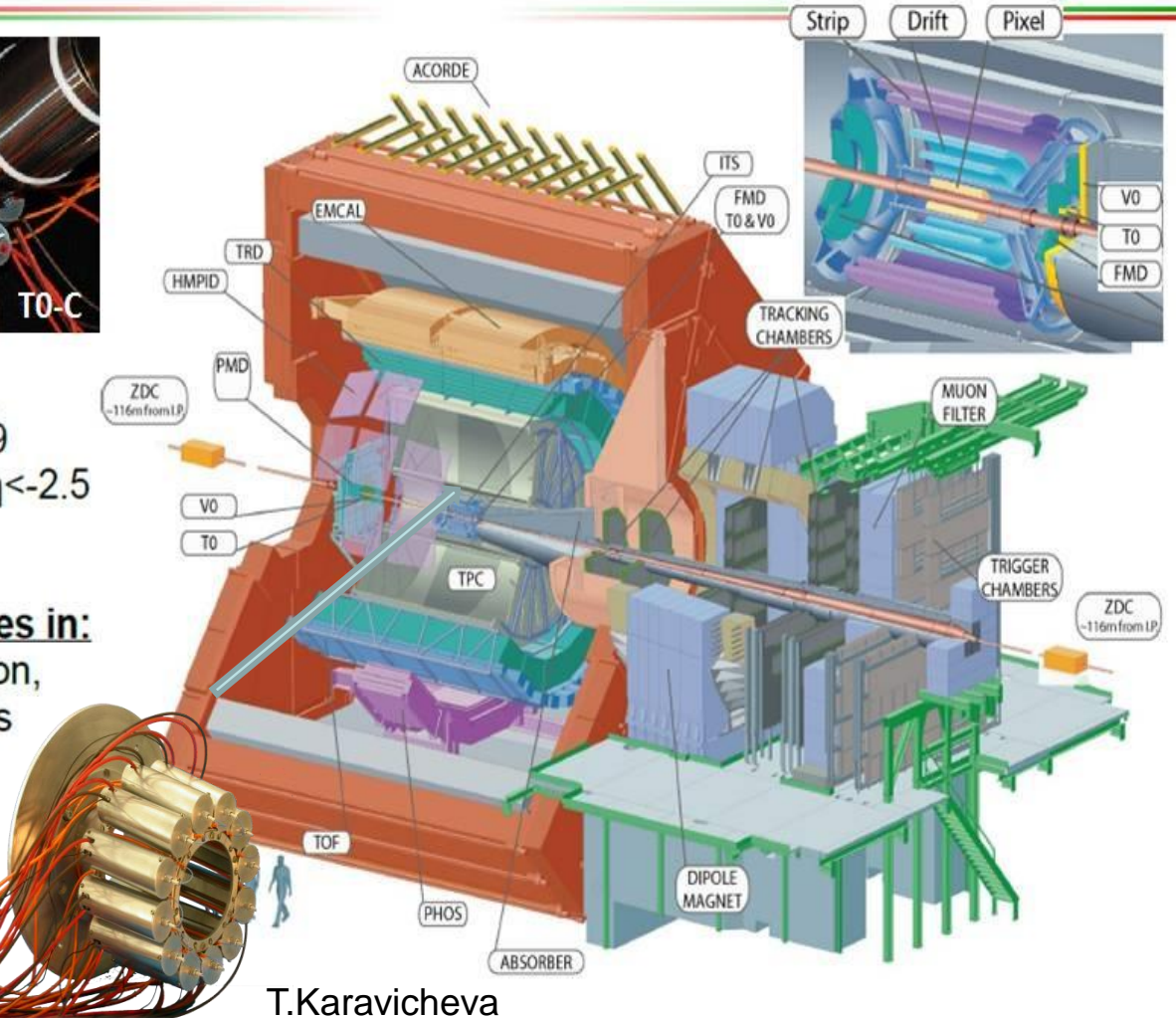
Overall view of the LHC experiments.



Cosmic **GlueBall-Matter** at CERN LHC and BNL RHIC



A Large Ion Collider Experiment



ALICE covers:

- central: $|\eta| < 0.9$
- forward $-4.0 < \eta < -2.5$ regions

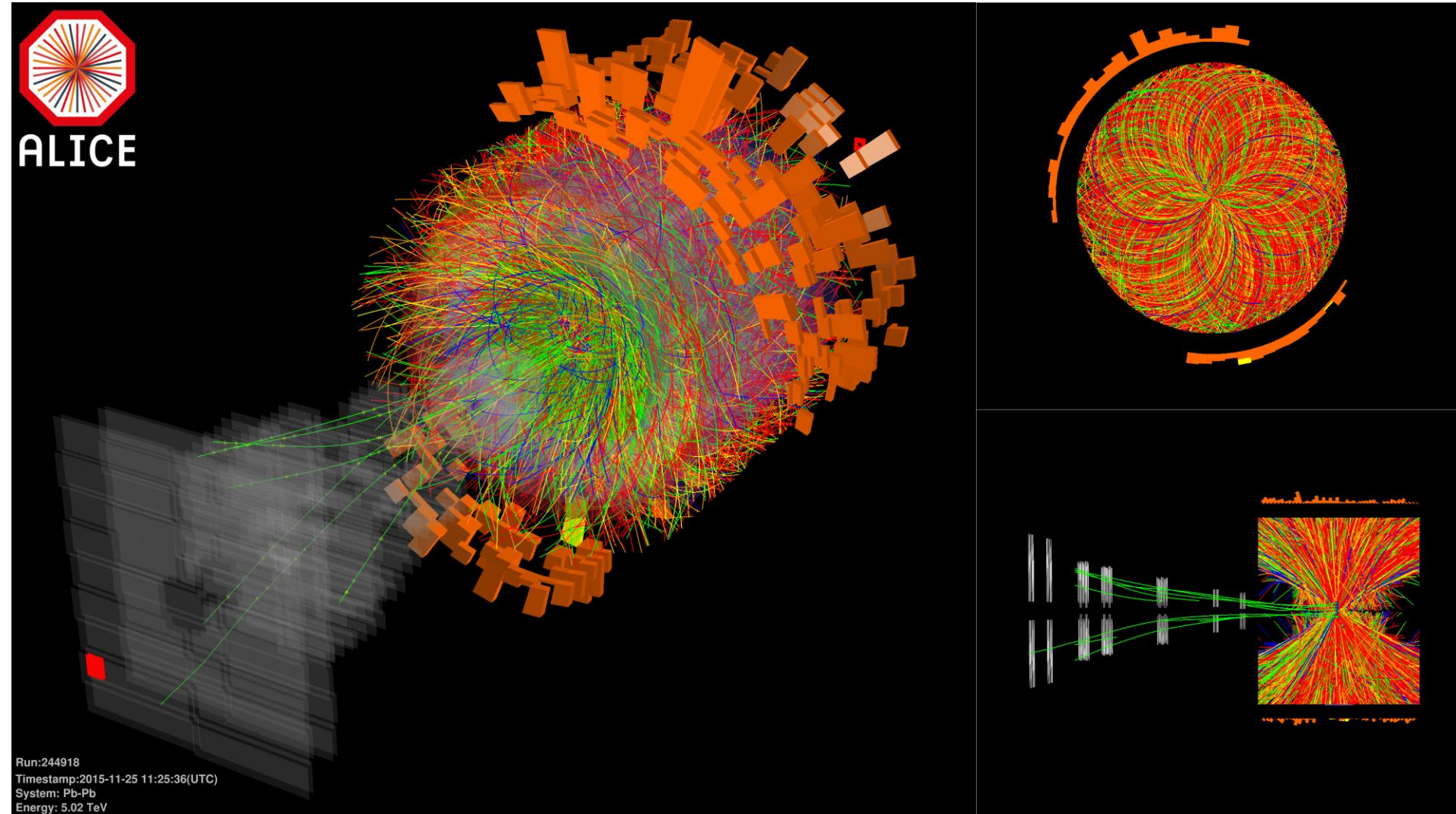
ALICE measures in:

- hadron, electron, muon channels

ALICE @ LHC: Pb-Pb collisions $\sqrt{s_{NN}} = 5.02$ TeV

First Data Nov. 25 LHC design HI luminosity $10^{27} \text{ s}^{-1} \text{ cm}^{-2}$ Dec. 1

Increase of statistics by a factor of 3-10 (centrality, ...)



Extreme computing challenges require power efficient high performance computing data storage & -analysis: Spin-off from Nuclear Physics to Industry & Business

Green Cube at GSI -4- FAIR



**12 MW power consumption, PUE<1.07
T. Kollegger, AIME Big Data, Budapest**

**Nr.1 Green-500: GSI L-CSC Computer Supercomputer Fair, New Orleans, USA
November 2014**



**5.27 Gflops/watt power consumption
with AMD FirePro GPU**

Traditional picture of QCD matter in Heavy Ion Collisions

Initial Color Glass Condensate \Rightarrow Glasma thermalizes
 \Rightarrow fast equilibration of Gluons and Light flavor quarks
high pressure, entropy \Rightarrow hydrodynamic expansion
 \Rightarrow flow v_2 as excellent Barometer: probe of QCD matter.



Hadronization @ $T=155\text{MeV}$: crossing of 2+1 flavor QCD



Hadronic yields and v_2 at RHIC and LHC measured \Rightarrow **FIT !**

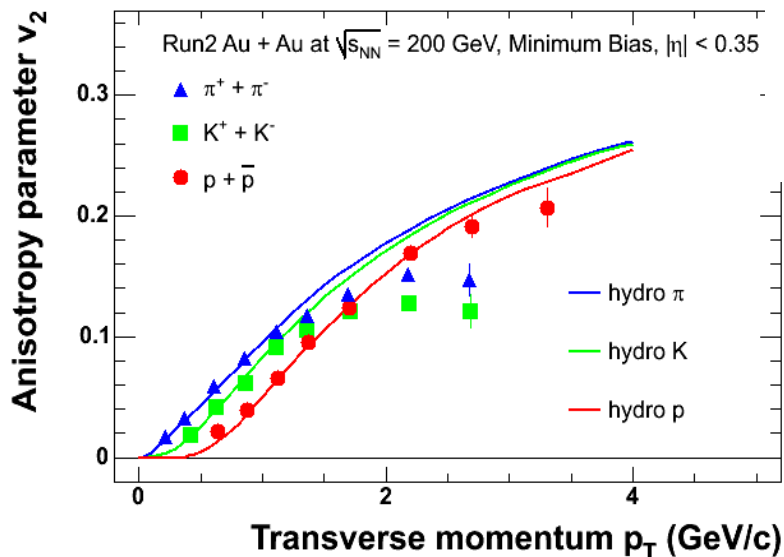
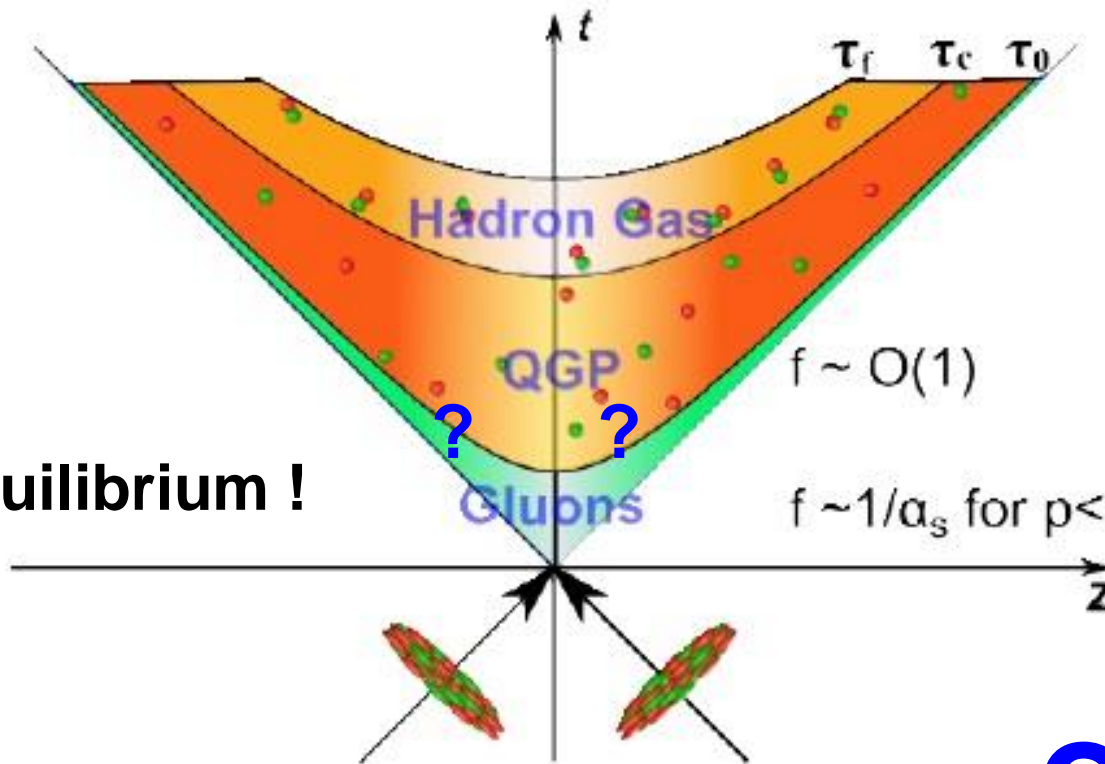


Comparison of v_2 , HRG $T=155\text{ MeV}$, with LHC data
“understanding” of QCD matter and - dynamics

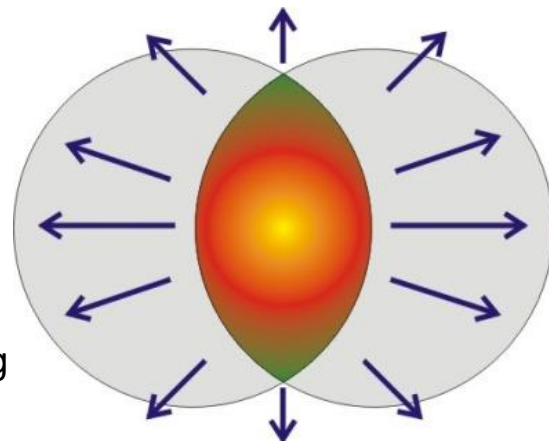
Fast thermalization required for Hydro

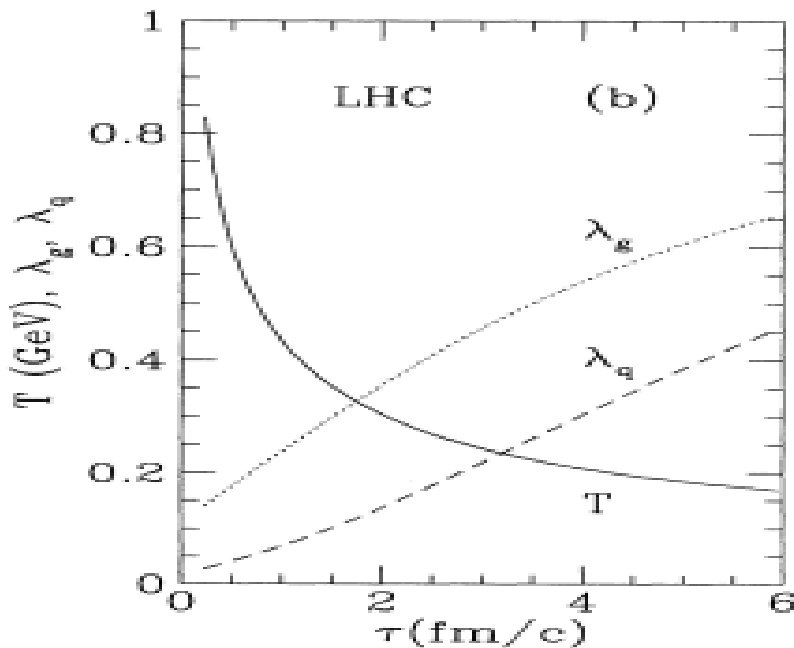
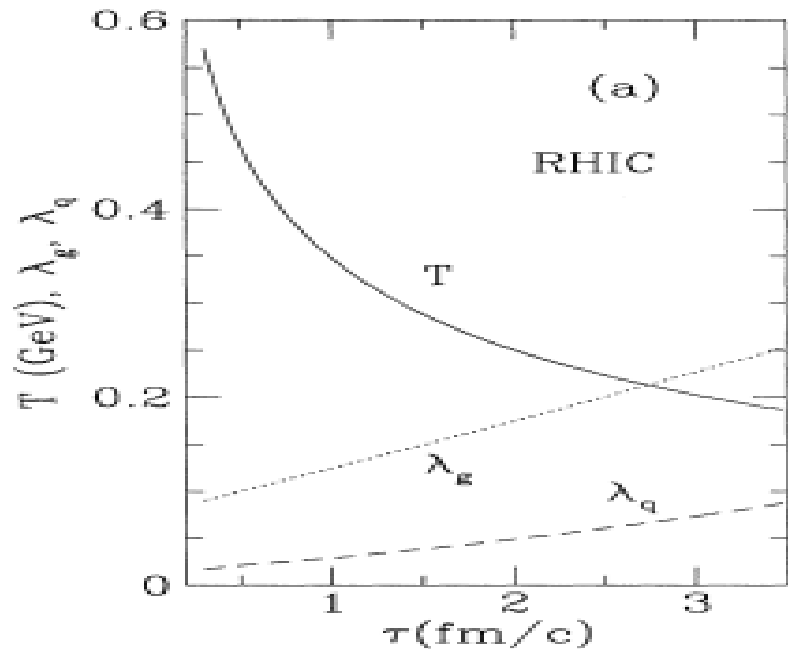
how can a system evolve to thermal equilibrium in such a very short time?

Initially: very far from equilibrium !



2+1QCD Hydro-Onset time < 1 fm/c ?





But:

Time evolution of fugacity

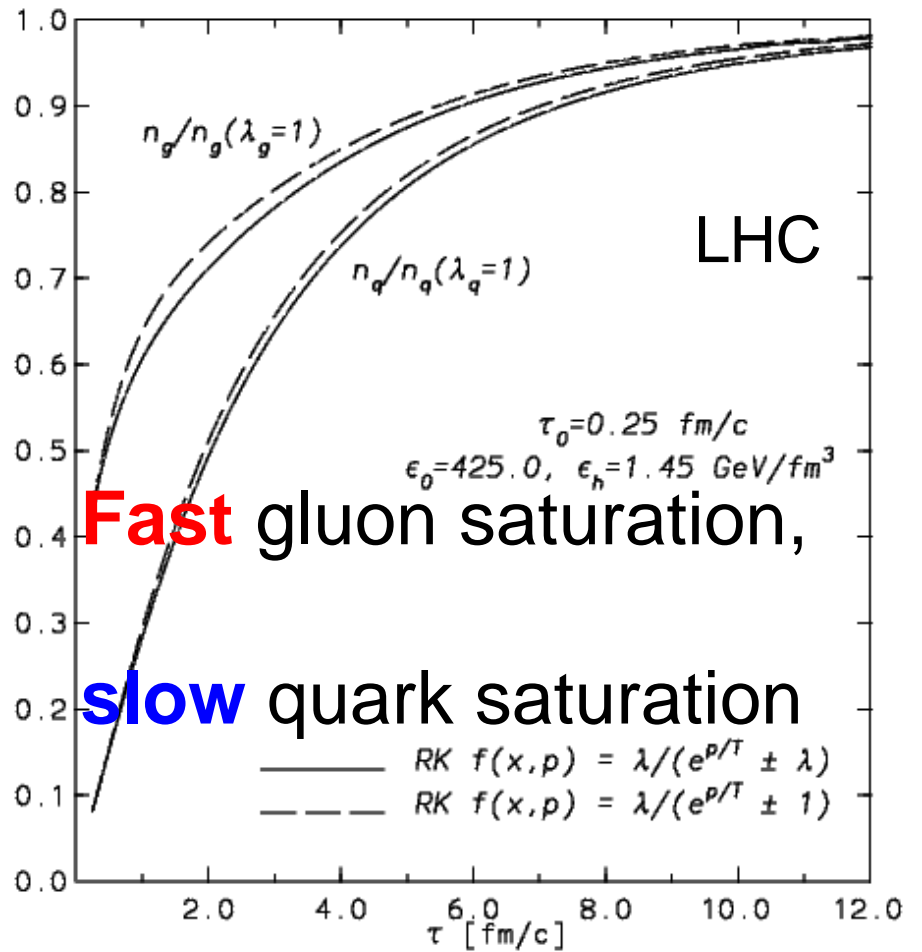
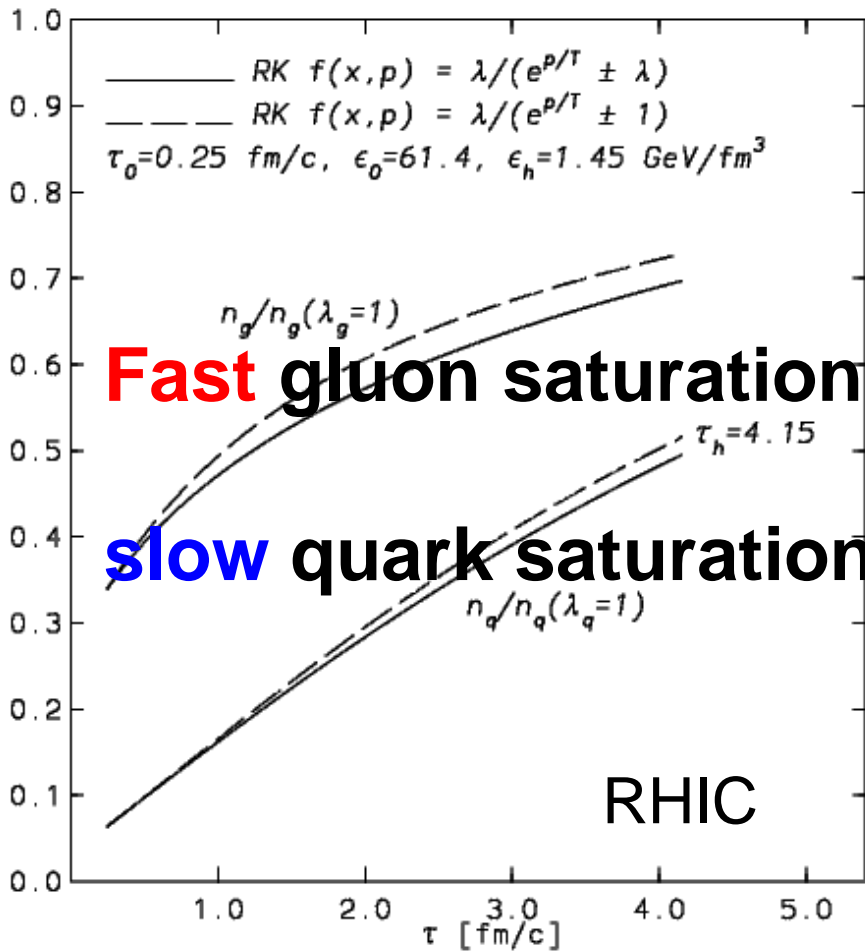
$$\text{fugacity} = n / n^{eq}$$

of gluons and quarks (g, q)
from pQCD-based rate eq.

Fast gluon saturation,

slow quark saturation

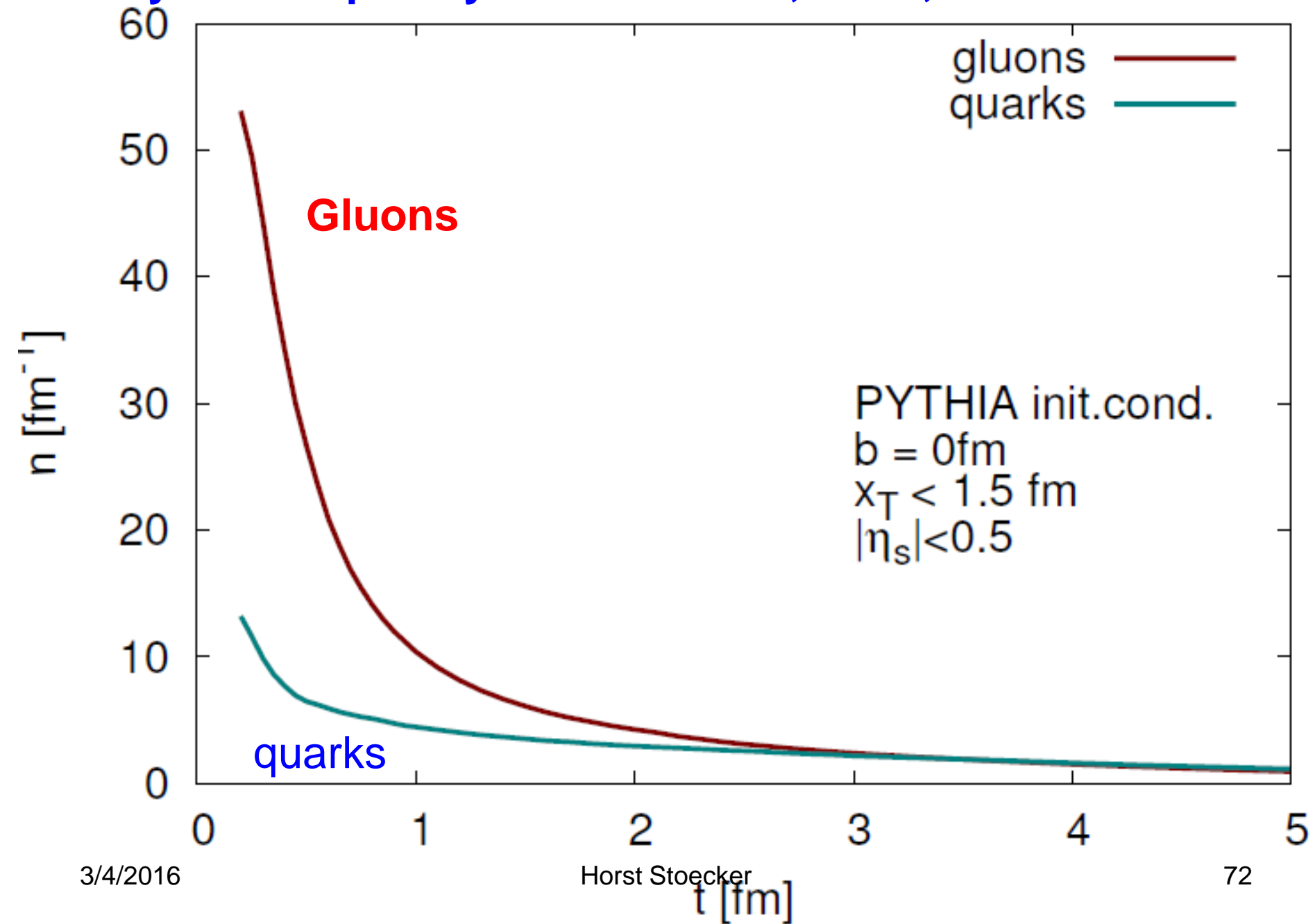
T. S. Biró, B. Mueller, X. N. Wang,
BMW-coll. , PRC48,1275 (1993)
also Kaempfer et al,
also Strickland...



Rate equation calculation

D.M. Elliott, D.H. Rischke, Nucl.Phys. A671,583 (2000)

Gluon yields & quark yields F. Senzel, Z. Xu, C. Greiner BAMPS



Pure YM Glue Matter created at FAIR*, RHIC, LHC ?

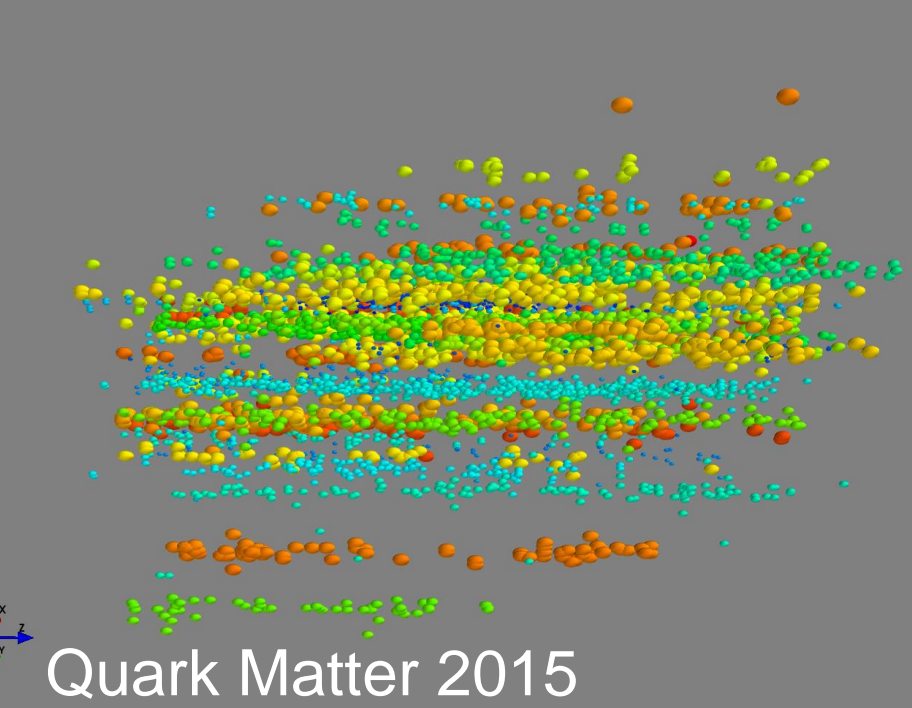
Early proposals for **two** phase transitions and **two timescales** in RHICs:

Svetitsky Yaffe Pisarski Wilczek Raha Sinha Shuryak Biro Kaempfer

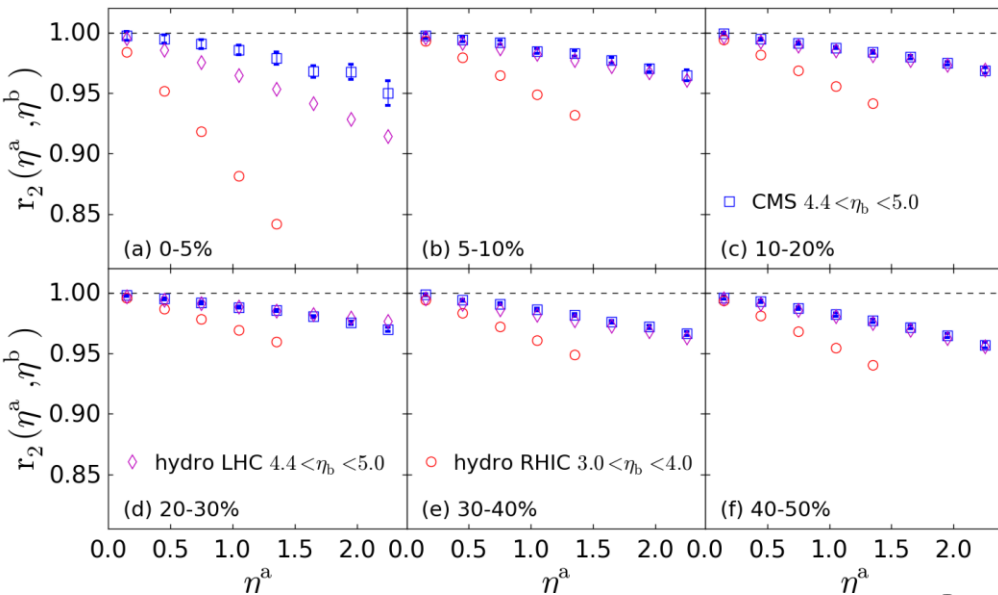
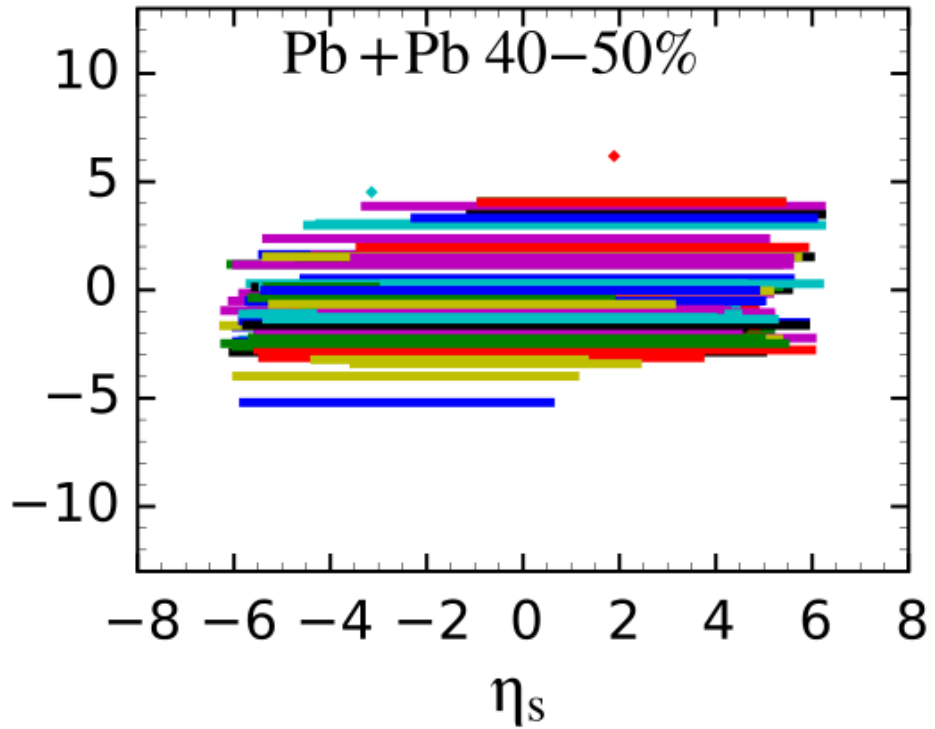
1. **CGC** Gluon Supersaturation – Overoccupied Glue, BEC
2. **Fast** Gluon Equilibration – **slow** quark saturation
3. **Early** 1.Order Phase Trans. in **Yang-Mills gauge** theory
4. **Pure** YM Gauge theory $N_f=0$ -“physical” $N_f=2+1$ QCD $N_f=fct$ of time
5. **Second** Transition Quarks-Hadrons 2+1-QuarkGluonPlasma”**crossing**”
6. **GlueBalls**-HagedornStates, two body sequential **decay cascade**
7. **Hadron** yields, $\langle pt \rangle$ vs. Multiplicity, Flow & **Ridge** in pp, pA, AA
8. **Dileptons**, Photons vs. Multiplicity in pp, pA, AA

Horst Stoecker, Judah M. Eisenberg Prof., ITP & FIAS, Goethe Univ. Frankfurt

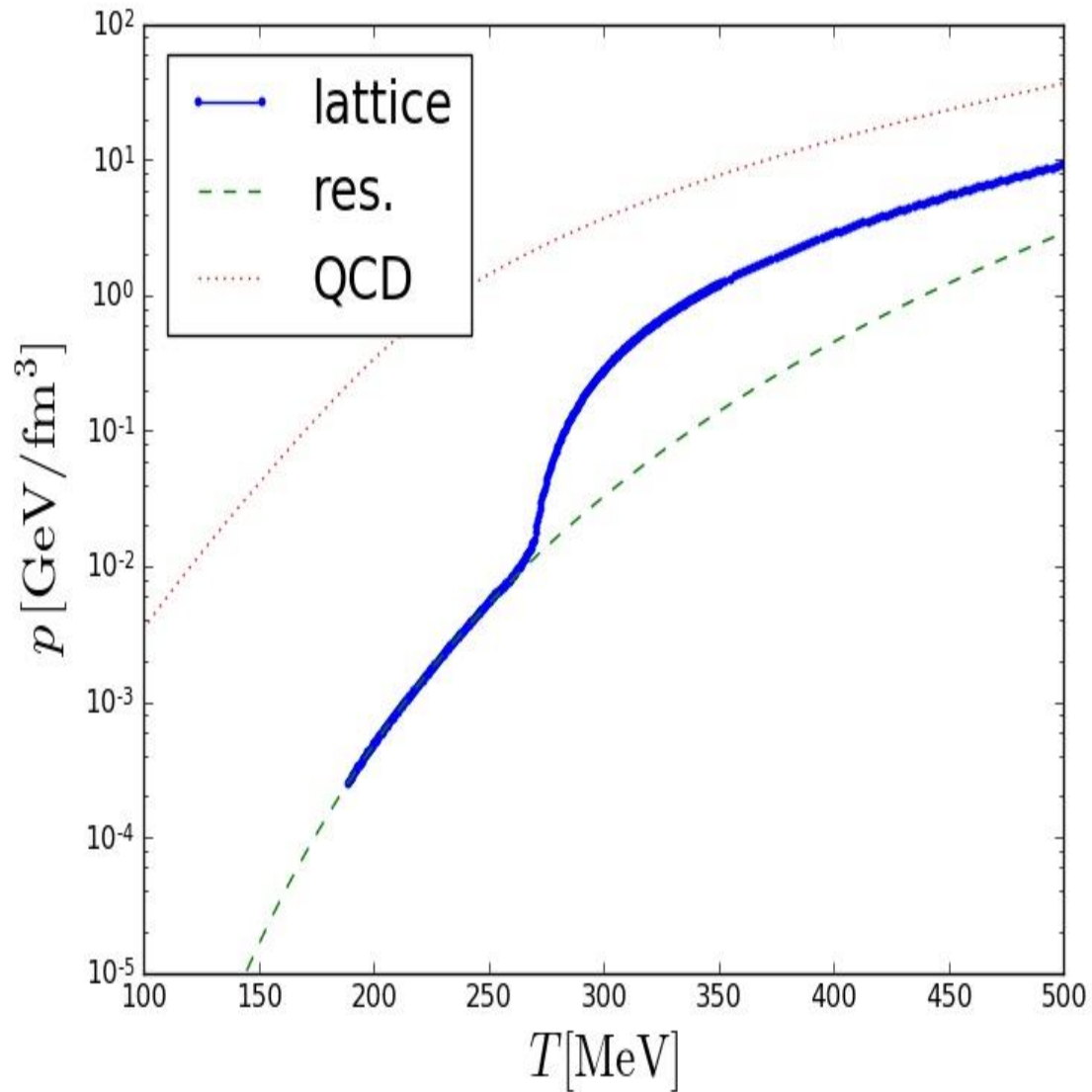
Time evolution of high multiplicity pp AA at RHIC and LHC in pure YM scenario

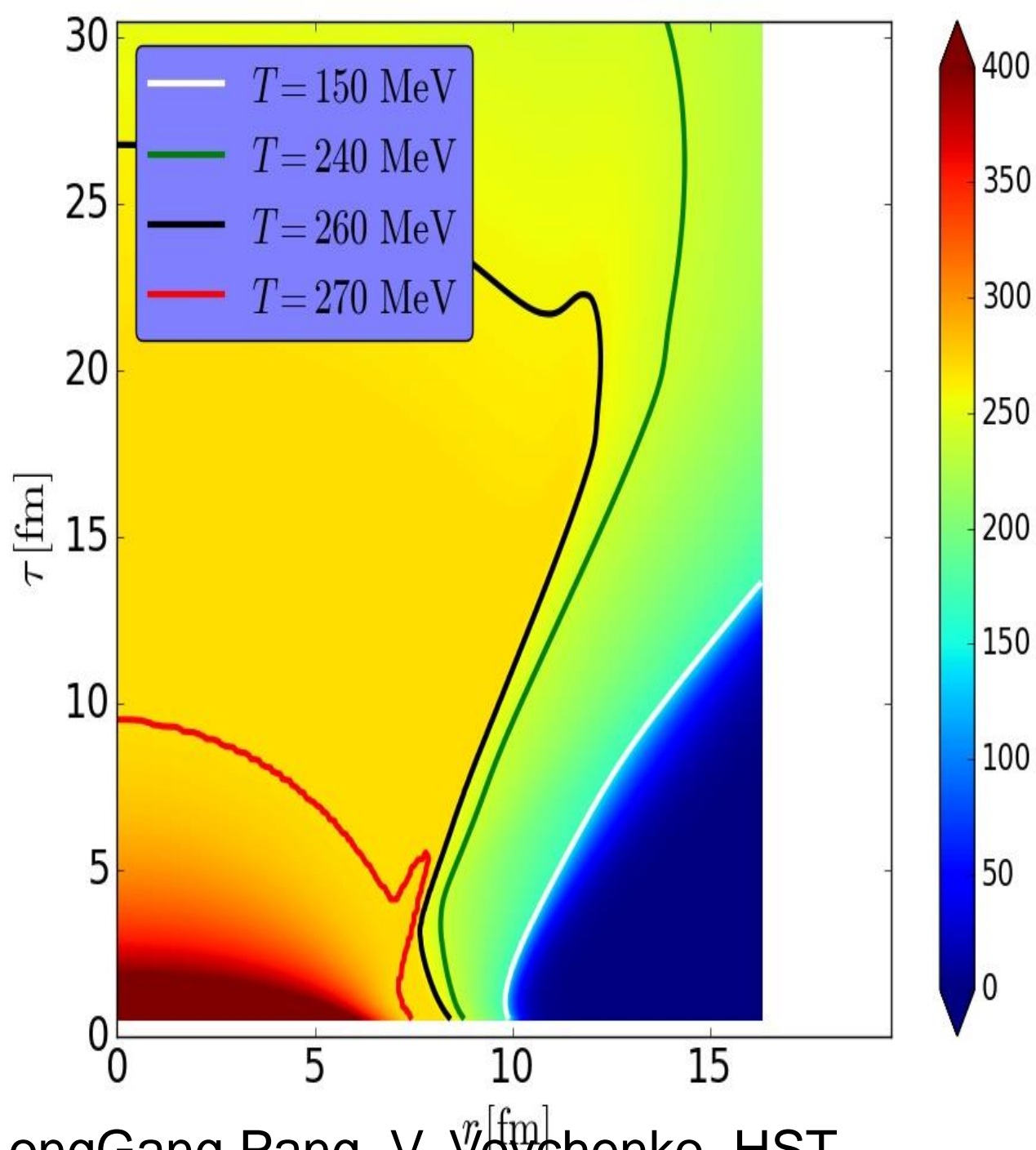


x [fm]

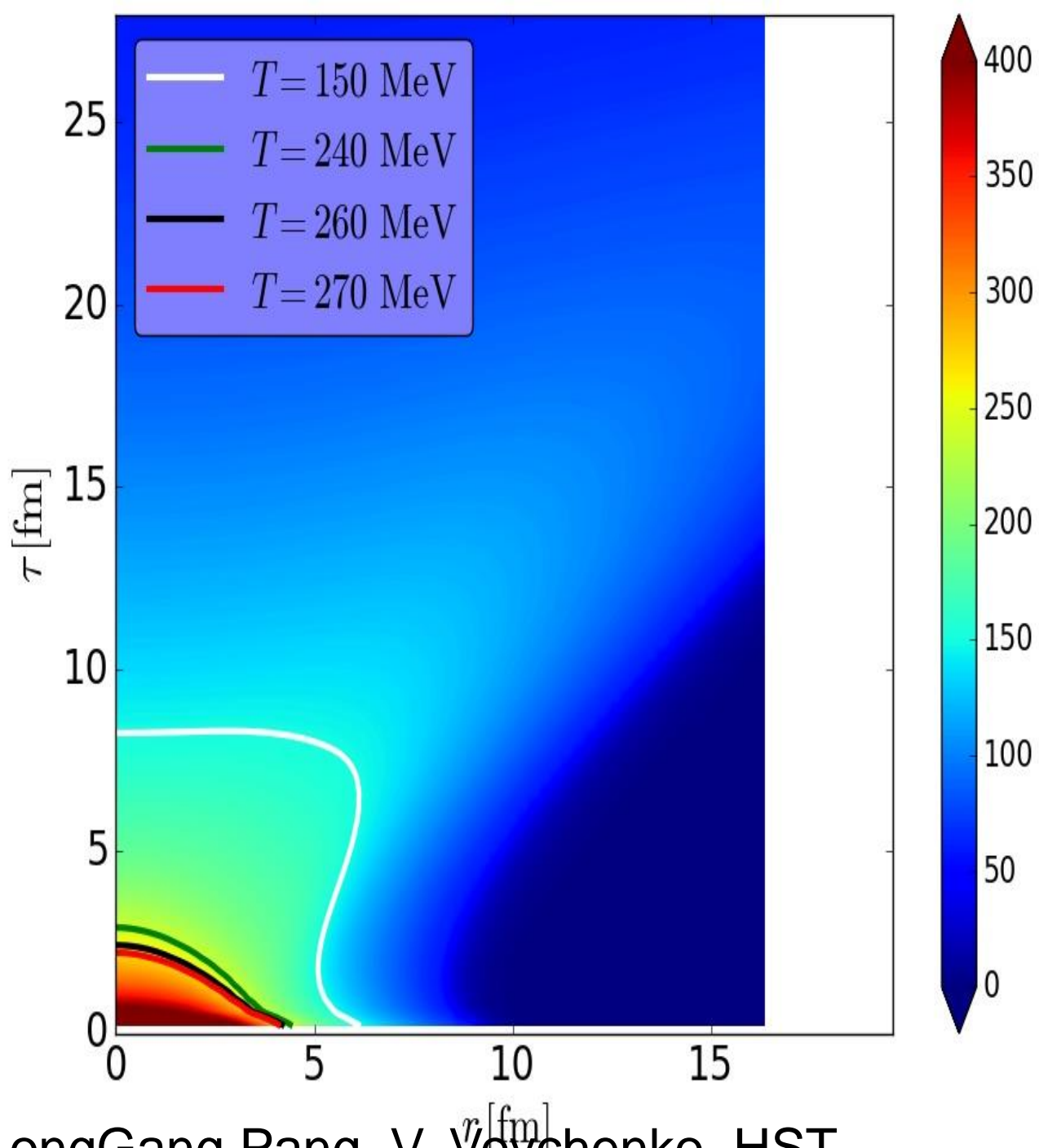


- Event-by-event hydro confirms the de-correlation of anisotropic flow along rapidity
- Brain storms for longitudinal structure of QGP
- Question flow measurements. (Event planes are different with big pseudo-rapidity gap)

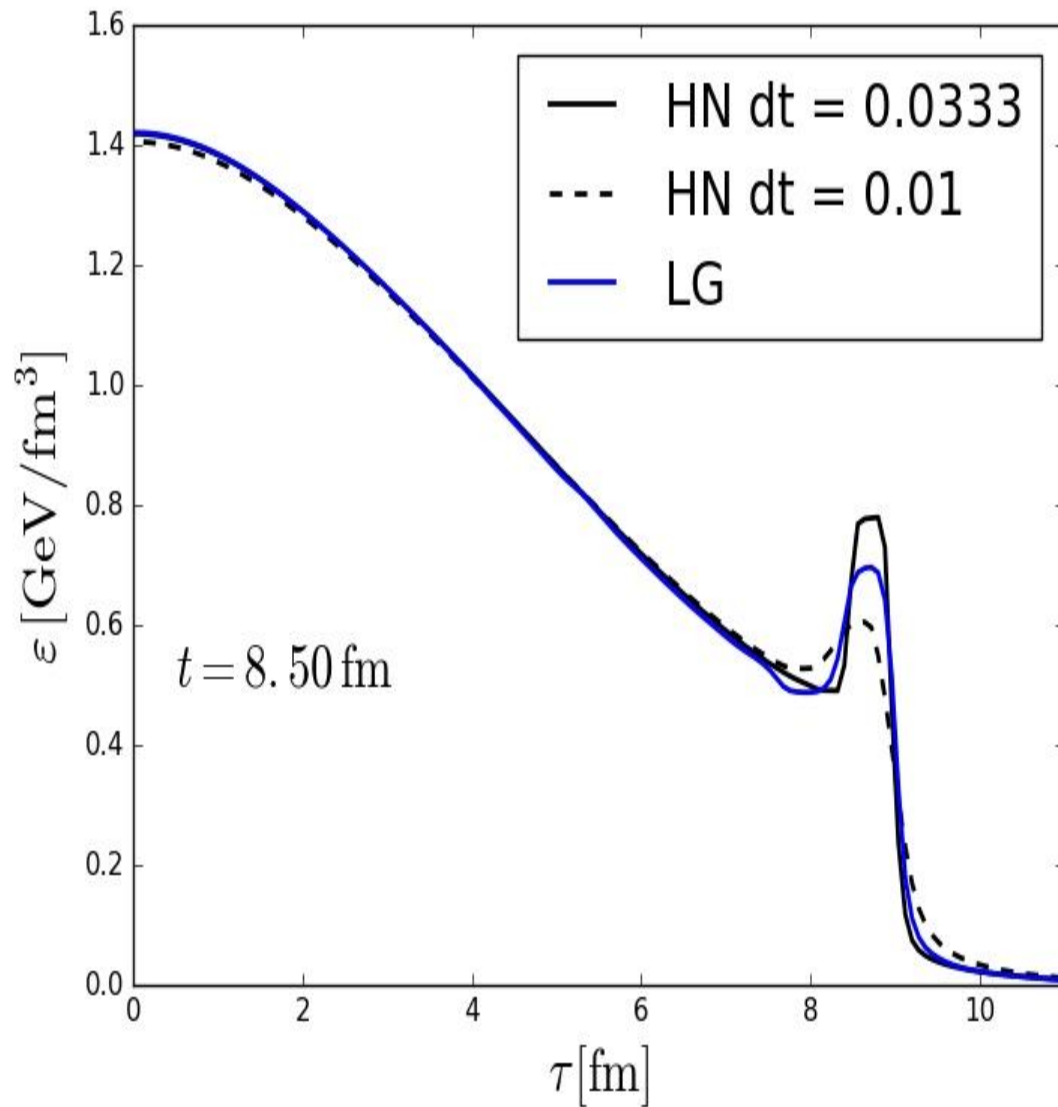


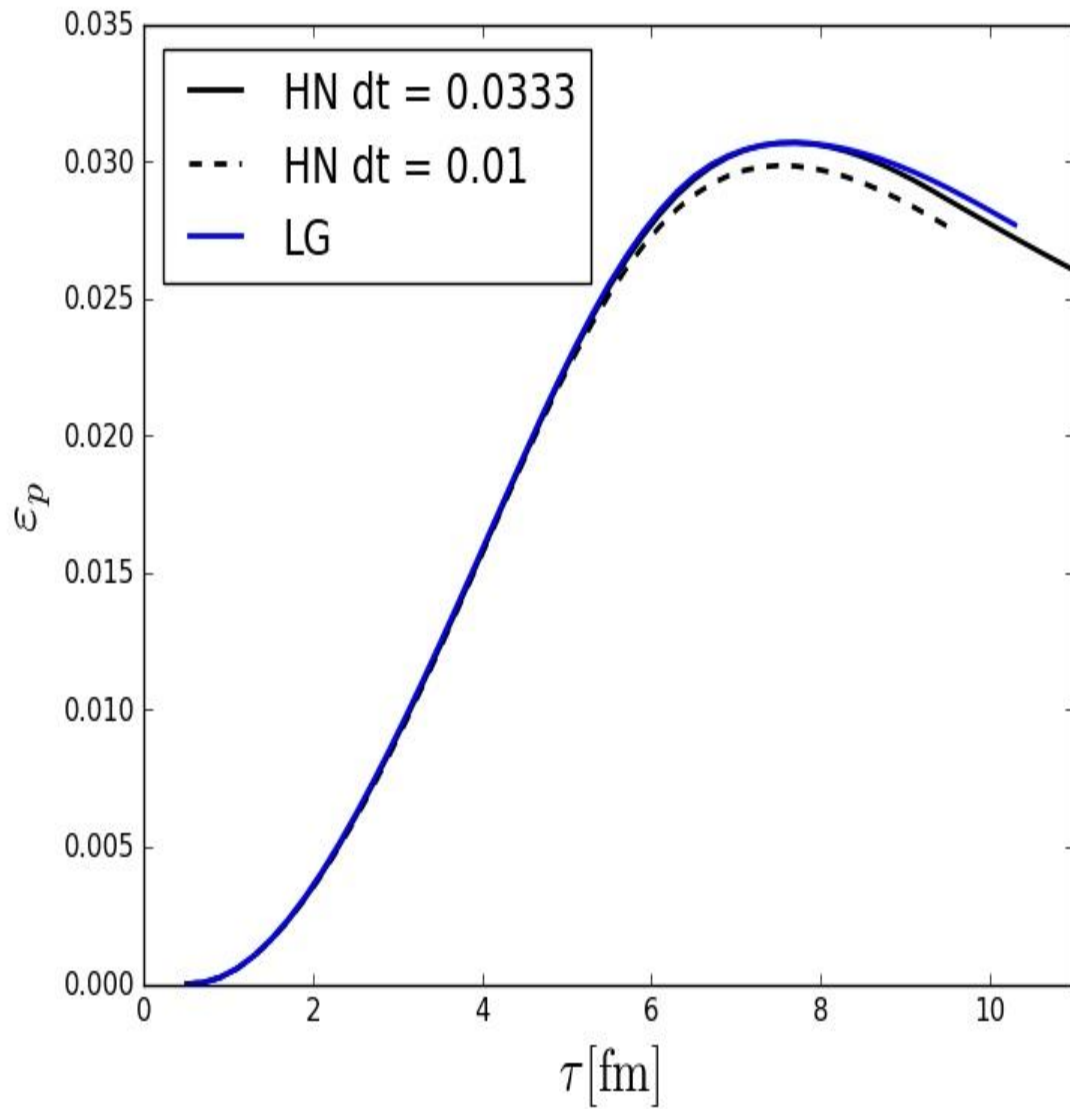


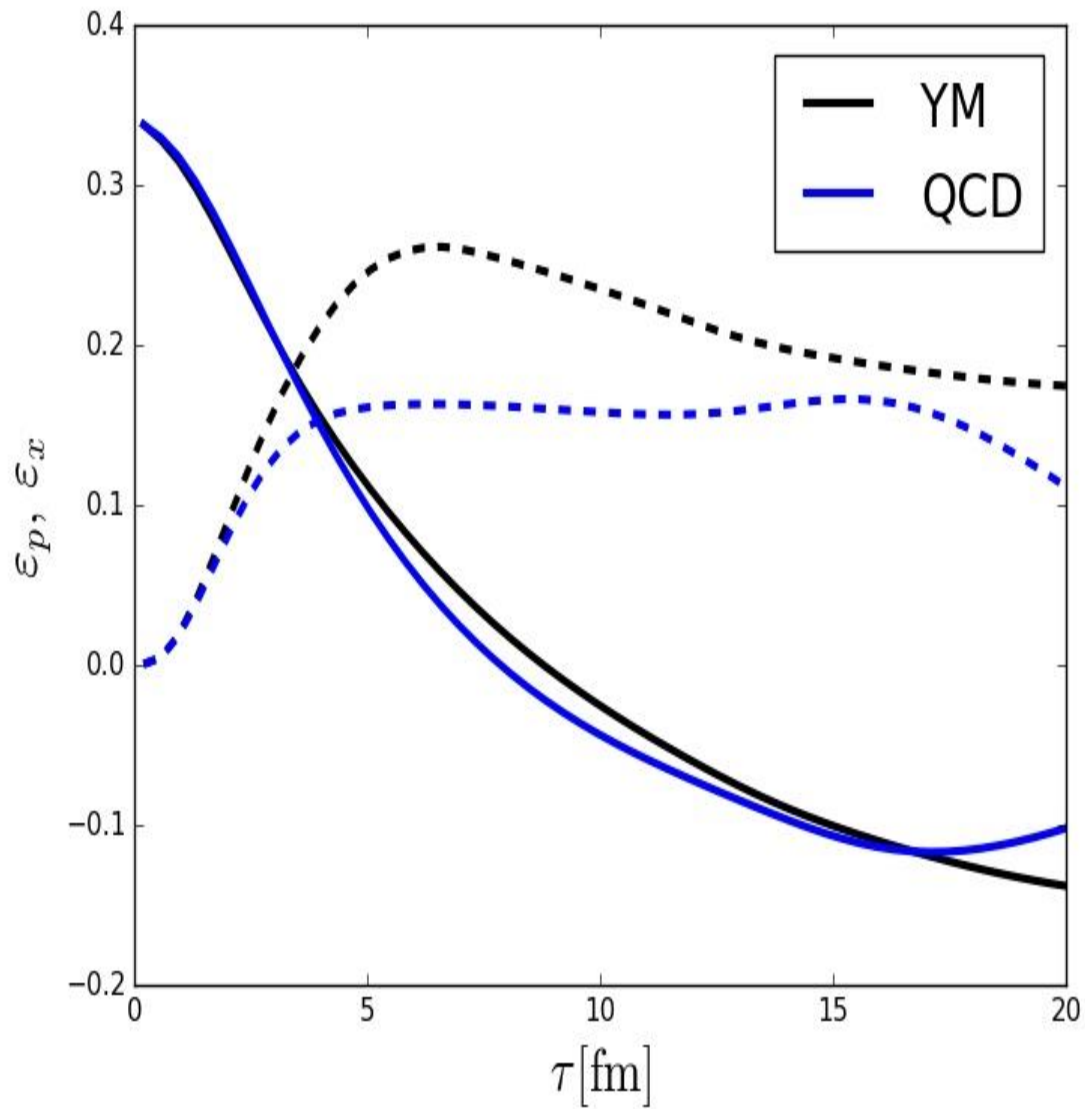
H. Niemi, LongGang Pang, V. Vovchenko, HST

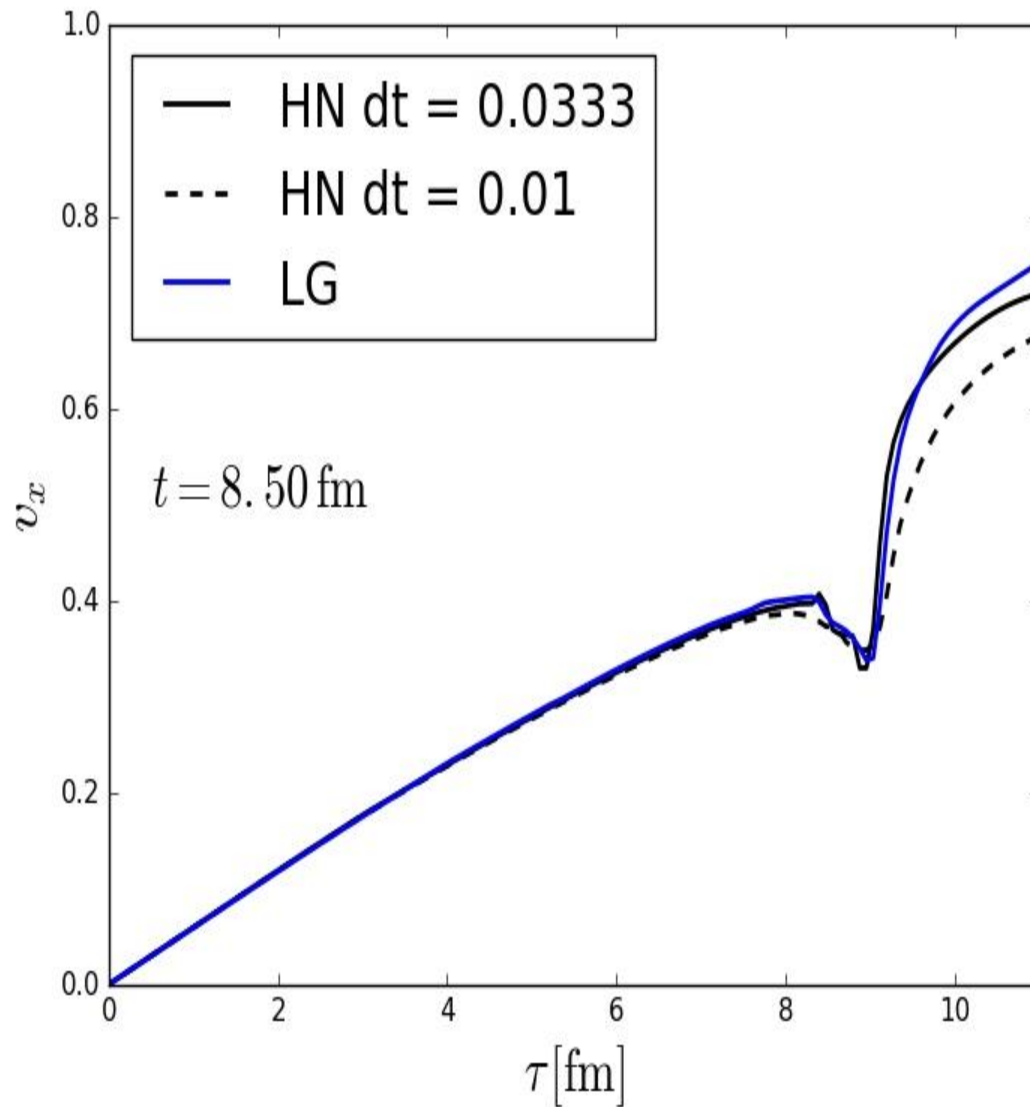


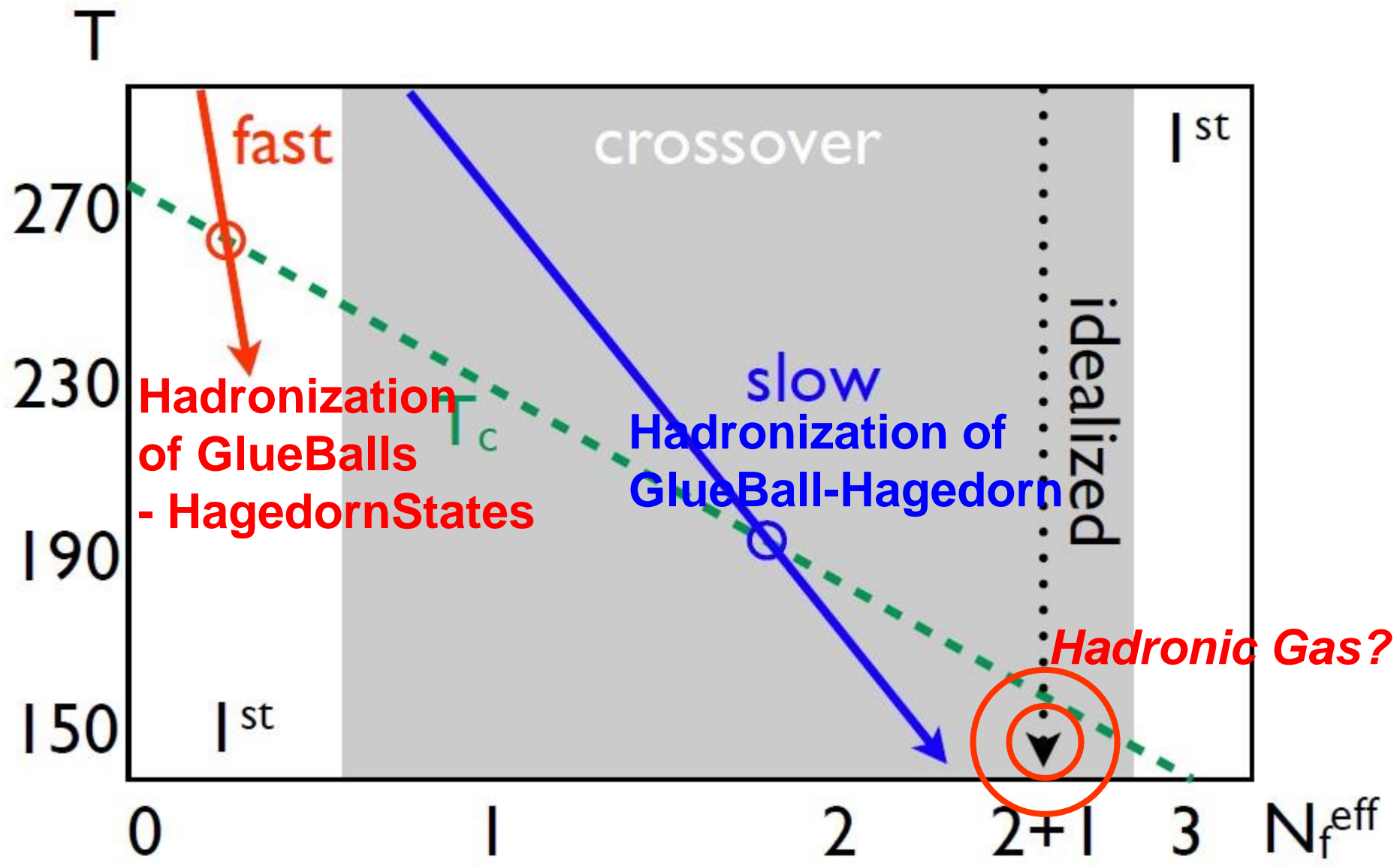
H. Niemi, LongGang Pang, V. Vovchenko, HST





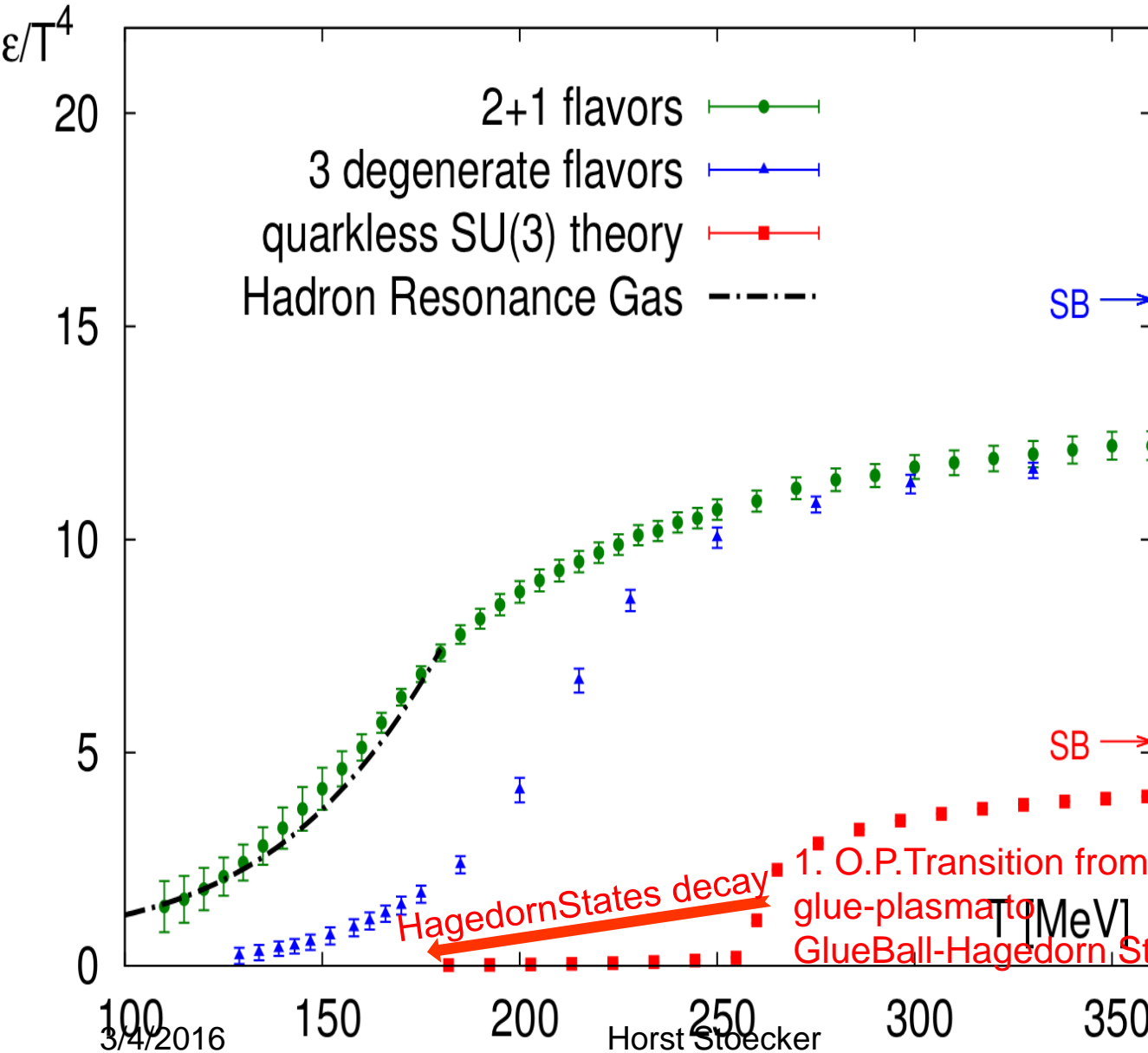






Pure YM LGT vs. 2+1 flavor Lattice QCD

Energy density (EoS) **DIFFERENT** for different quark masses



Energy density from Sz. Borsanyi et al., W.P. Wuppertal-Budapest coll JHEP 1011, 2010,077; PLB730, 2014, 99

“physical point” 2+1
T_c.o. = 155 MeV

N_f = 3, m_u,d = m_s
T_c.o. = 220 MeV

pure gauge YM
T_c = 270 MeV

Quenched: W.B. coll. JHEP 1207, 2012, 056

Multi-component eigenvolume HRG vs lattice QCD

“Diagonal” EV model

$$p = \frac{\sum_i T n_i}{1 - \sum_i v_i n_i} \quad v_i = \frac{16}{3} \pi r^3$$

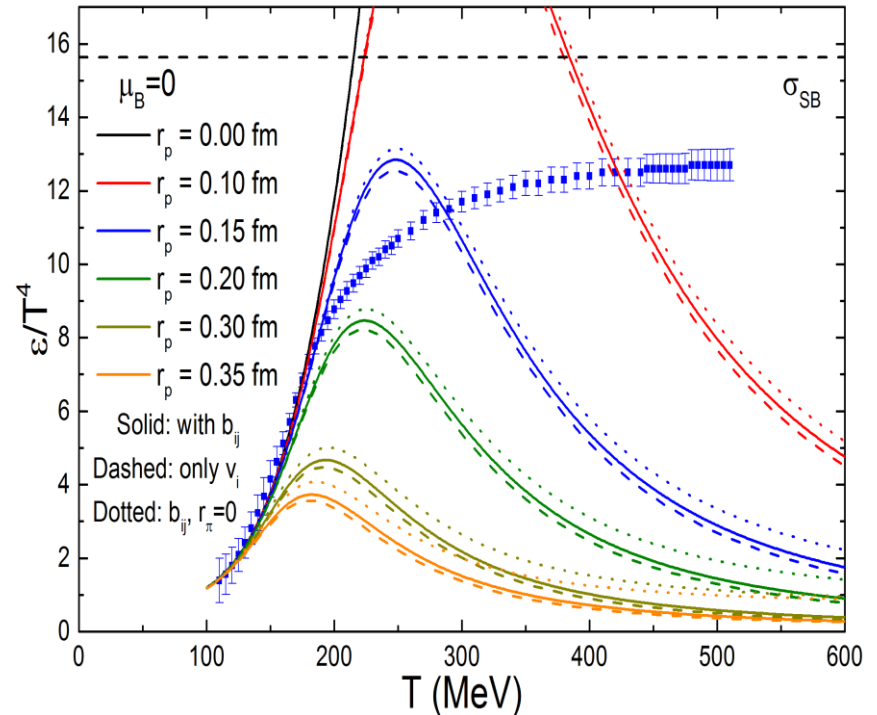
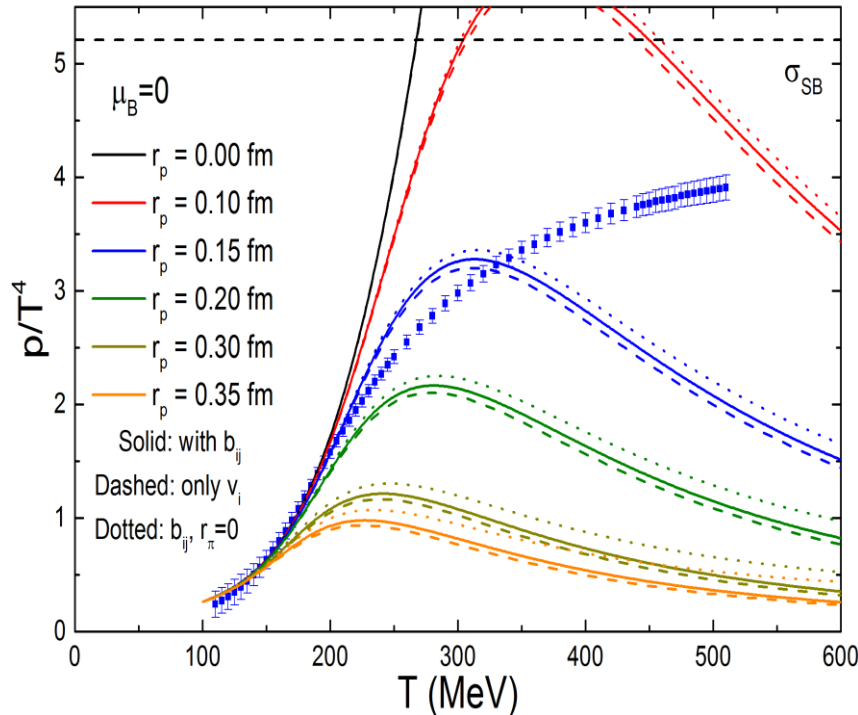
“Crossterms” EV model

$$p = \sum_i \frac{T n_i}{1 - \sum_j \tilde{b}_{ji} n_j} \quad b_{ij} = \frac{2}{3} \pi (r_i + r_j)^3$$

$$\tilde{b}_{ij} = \frac{2 b_{ii} b_{ij}}{b_{ii} + b_{jj}}$$

Bag-model inspired parametrization: $r_i \sim m_i^{1/3}$
 pressure

energy density



Wuppertal-Budapest Lattice data well described by EV HRG

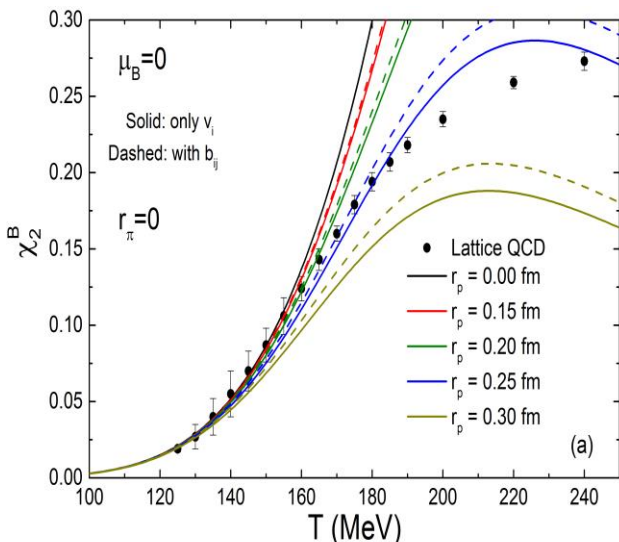
with $r_p = 0.15 - 0.20$ fm up to $T=250$ MeV

V. Vovchenko, HST

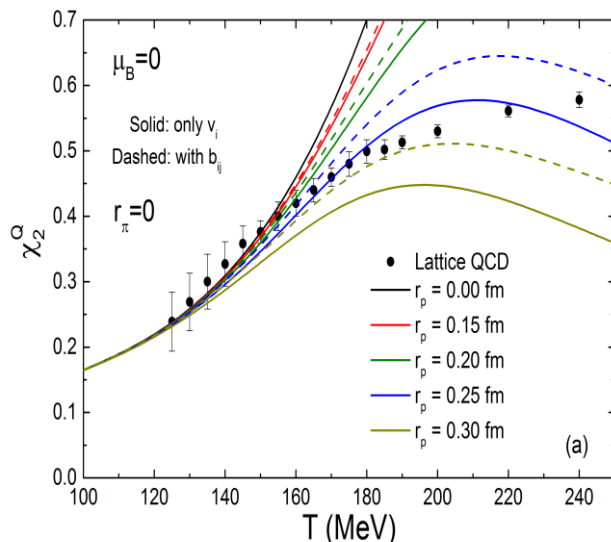
Multi-component bag-eigenvolume HRG vs lattice QCD

Susceptibilities carry information about finer details of the equation of state

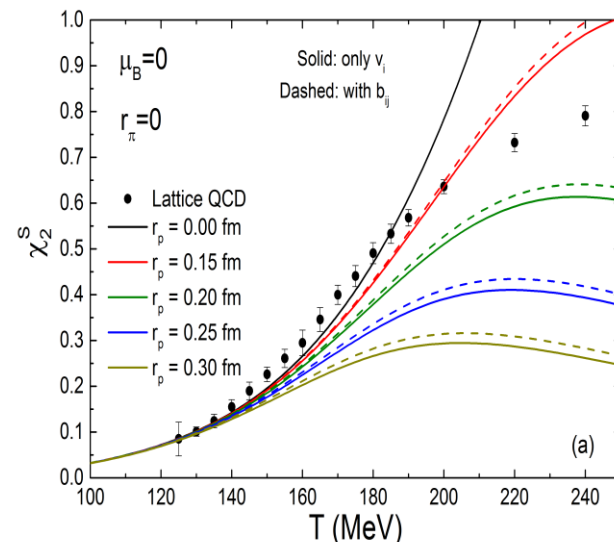
χ_2^B



χ_2^Q



χ_2^S



$r=0$: HRG of point particles
 cannot follow lattice data above $T=160$ MeV
 Finite eigenvolumes of hadron bags:
 dramatic improvement towards lattice data

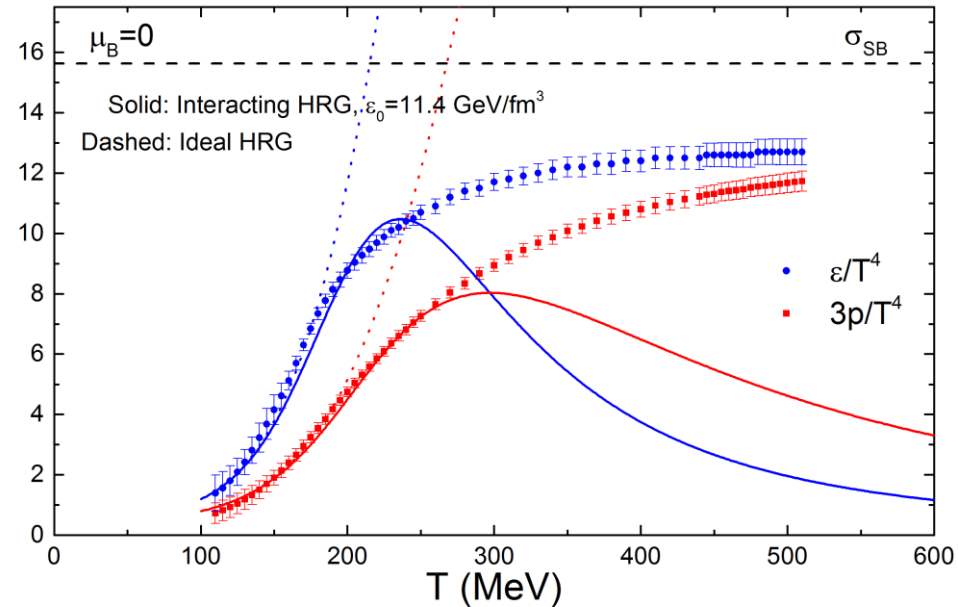
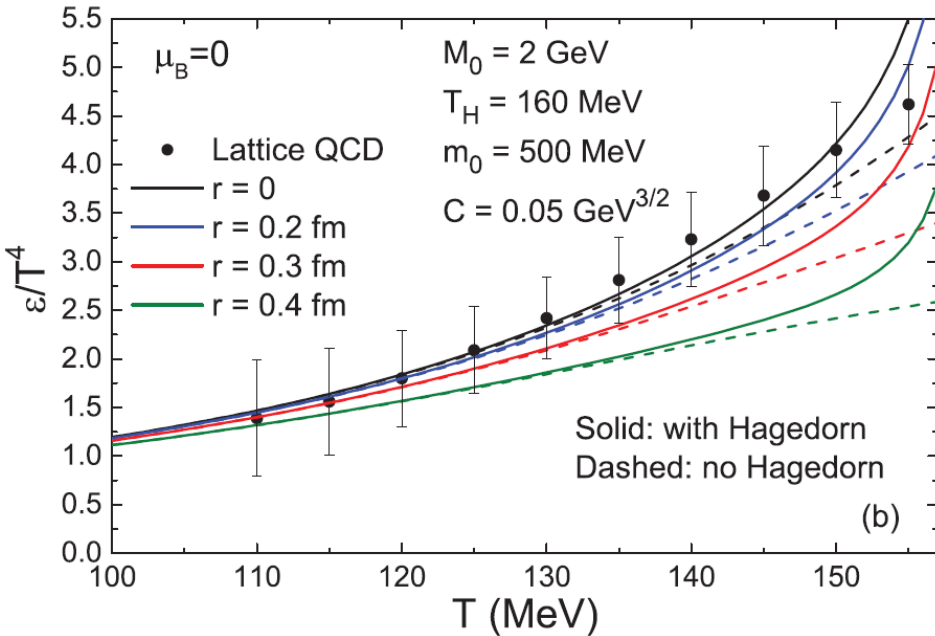
strange vs non-strange hadrons
 - different volumes at same mass?

V. Vovchenko, HST, in preparation

Vovchenko, Anchishkin, Gorenstein PRC 91, 024905 (2015), left rhs: V. Vovchenko, HST work in progress

Eigenvolume ($r = 0.3$ fm)
+ Hagedorn tower ($T_H = 160$ MeV)

Eigenvolume $v_i = m_i/\epsilon_0$



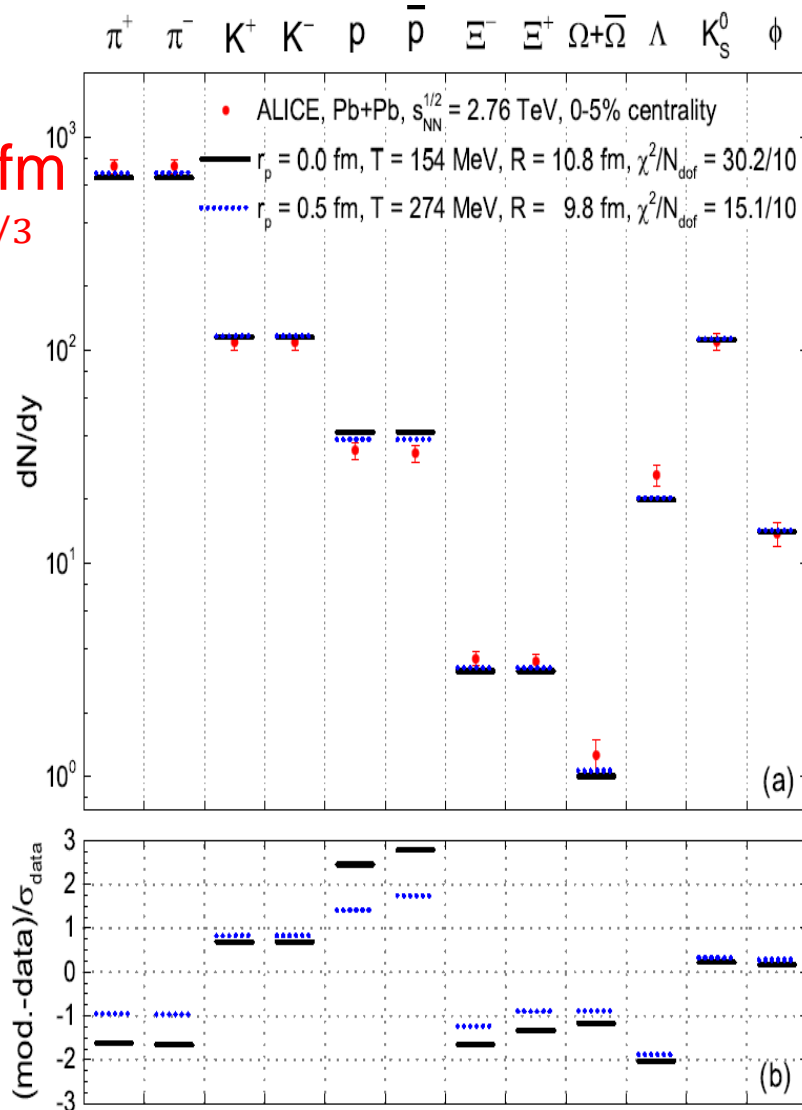
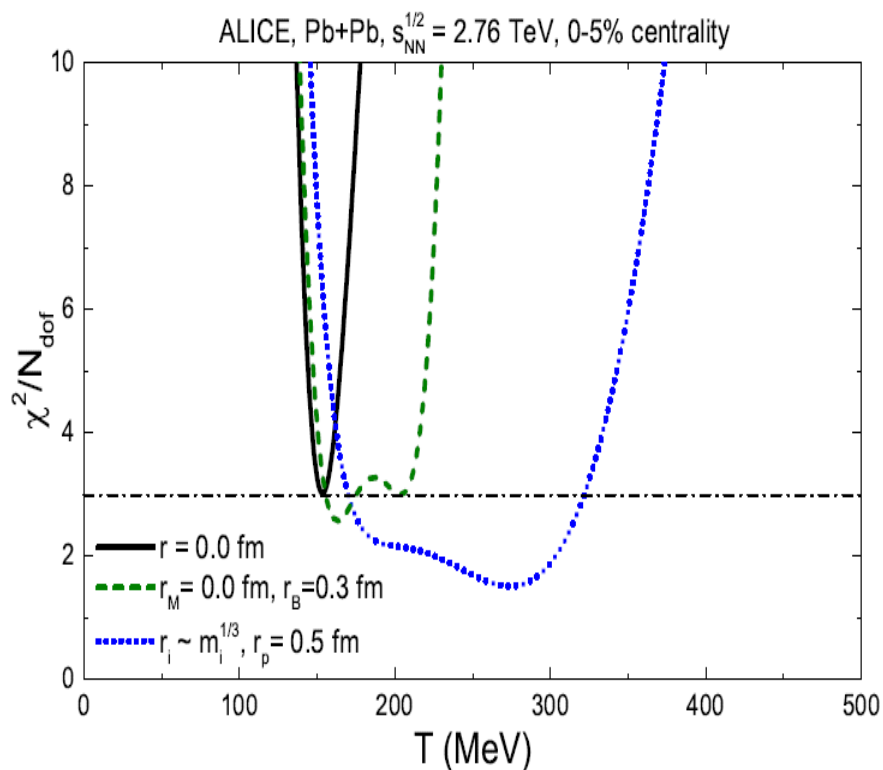
Lattice data clearly require finite eigen-volume of hadrons $v_i = m_i/\epsilon_0$

Lattice data fitted by HRG up to **$T \sim 250$ MeV** - if Eigenvolume is respected

Multi-component eigenvol. HRG vs ALICE hadron yield data

Two eigenvolume parametrizations:

- 1) Point-like mesons, Baryons $r_B = 0.3 \text{ fm}$
- 2) Bag-model inspired EV model: $r_i \sim m_i^{1/3}$



ALICE yield data fit wide temperature range, two different eigenvolumes parametrizations

Multi-component eigenvol. HRG constrained to lattice data

conservative approach: constrain HRG parameters by lattice data

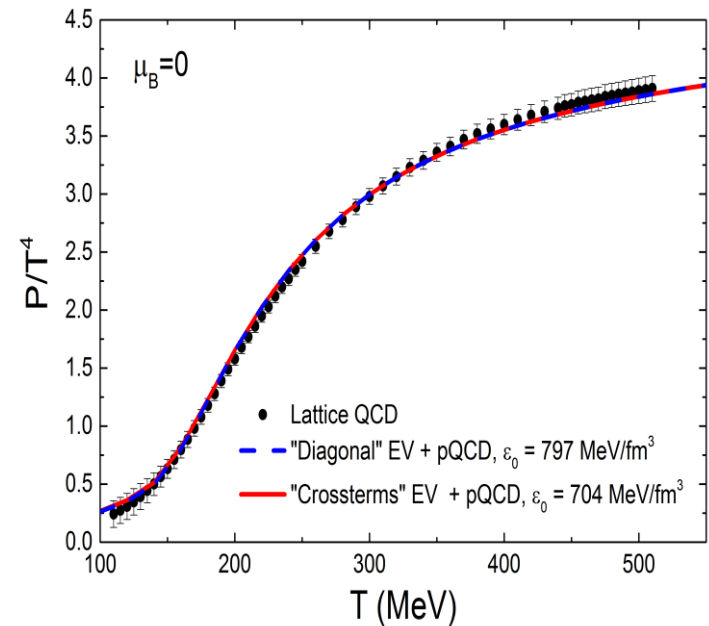
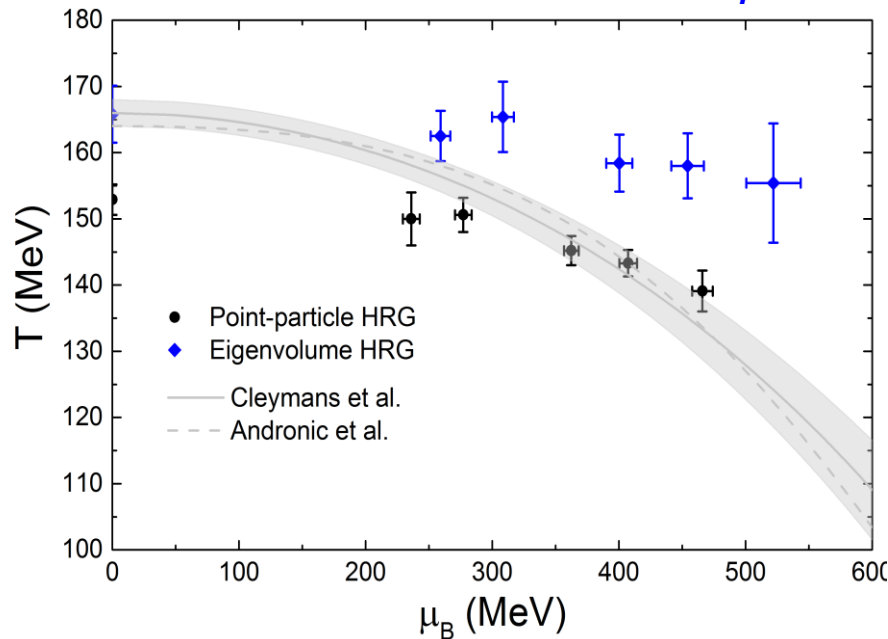
Crossover EoS of QCD: matching HRG low (T, μ) - pert. QCD high (T, μ)

$$p(T, \mu) = [1 - S(T, \mu)]P_{HRG}(T, \mu) + S(T, \mu)P_{pQCD}(T, \mu)$$

Transition from EV HRG ($r_i \sim m_i^{1/3}$) to pQCD at $T_0 \cong 175$ MeV via switching function

Albright, Kapusta, Young, PRC 90, 024915 (2014)

Fit to yield data at $T < T_0$ with $r_p = 0.43$ fm - Consistent with lattice



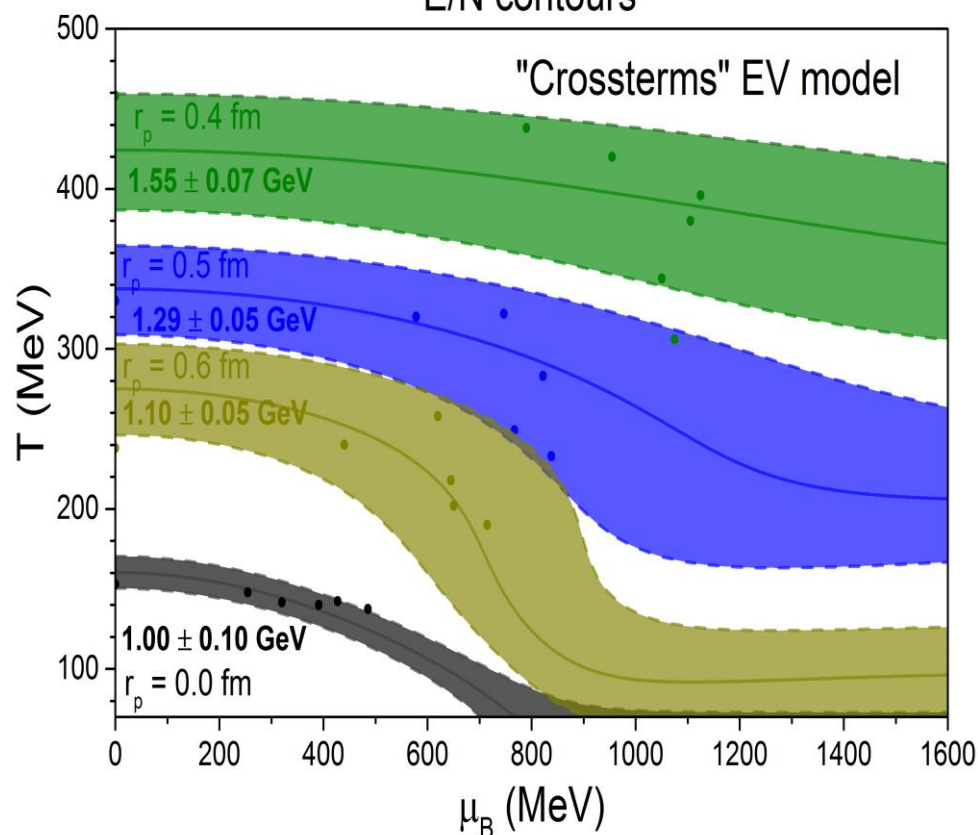
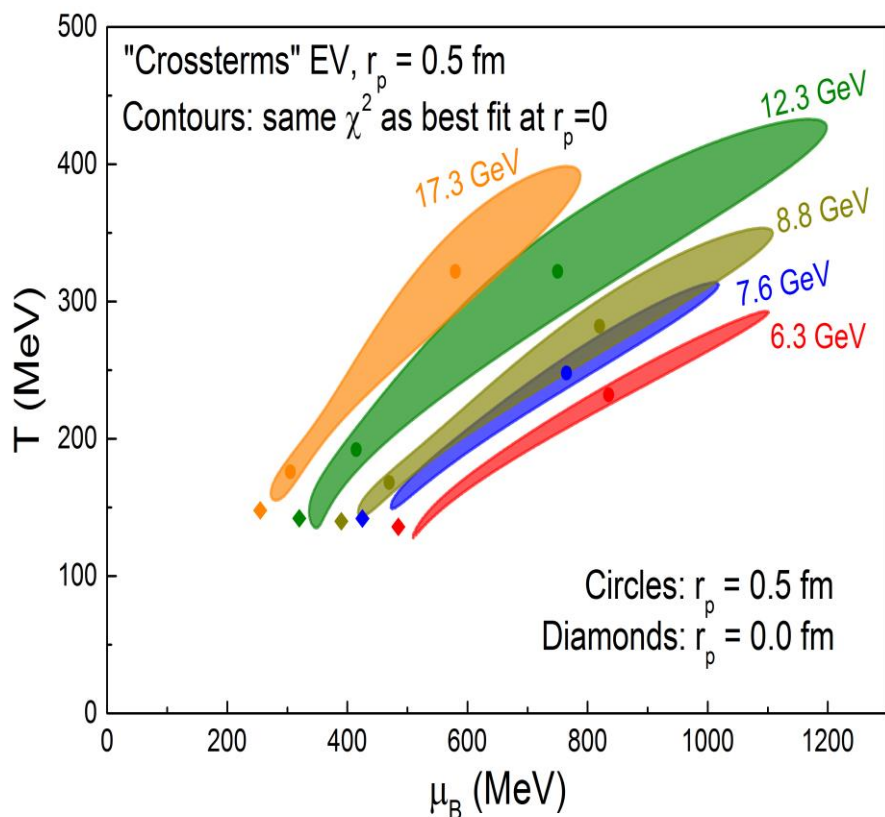
Results: systematically better χ^2 , higher freeze-out T and μ , smaller curvature of freeze-out curve

V. Vovchenko, H. Stoecker, in preparation

Multi-component eigenvol. HRG vs NA49 hadron yield data

Bag-model inspired EV model: $r_i \sim m_i^{1/3}$

E/N contours



Chemical Potentials and Temperatures shows **large uncertainty!**

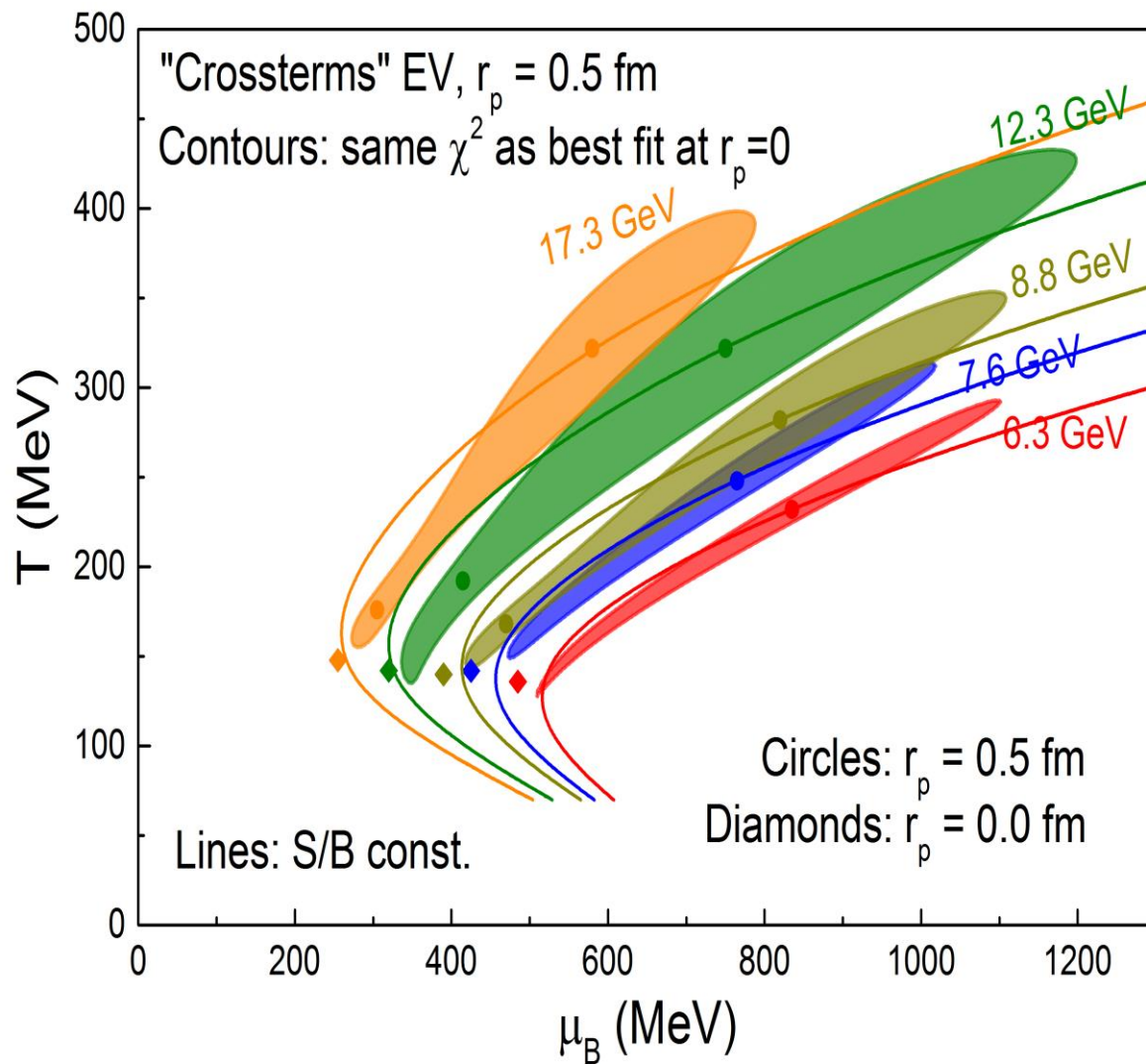
freeze-out criterion **E/N = const. ok**, but 'const.' depends on chosen eigenvolumes

Can freeze-out **T-mu extraction** with HRG

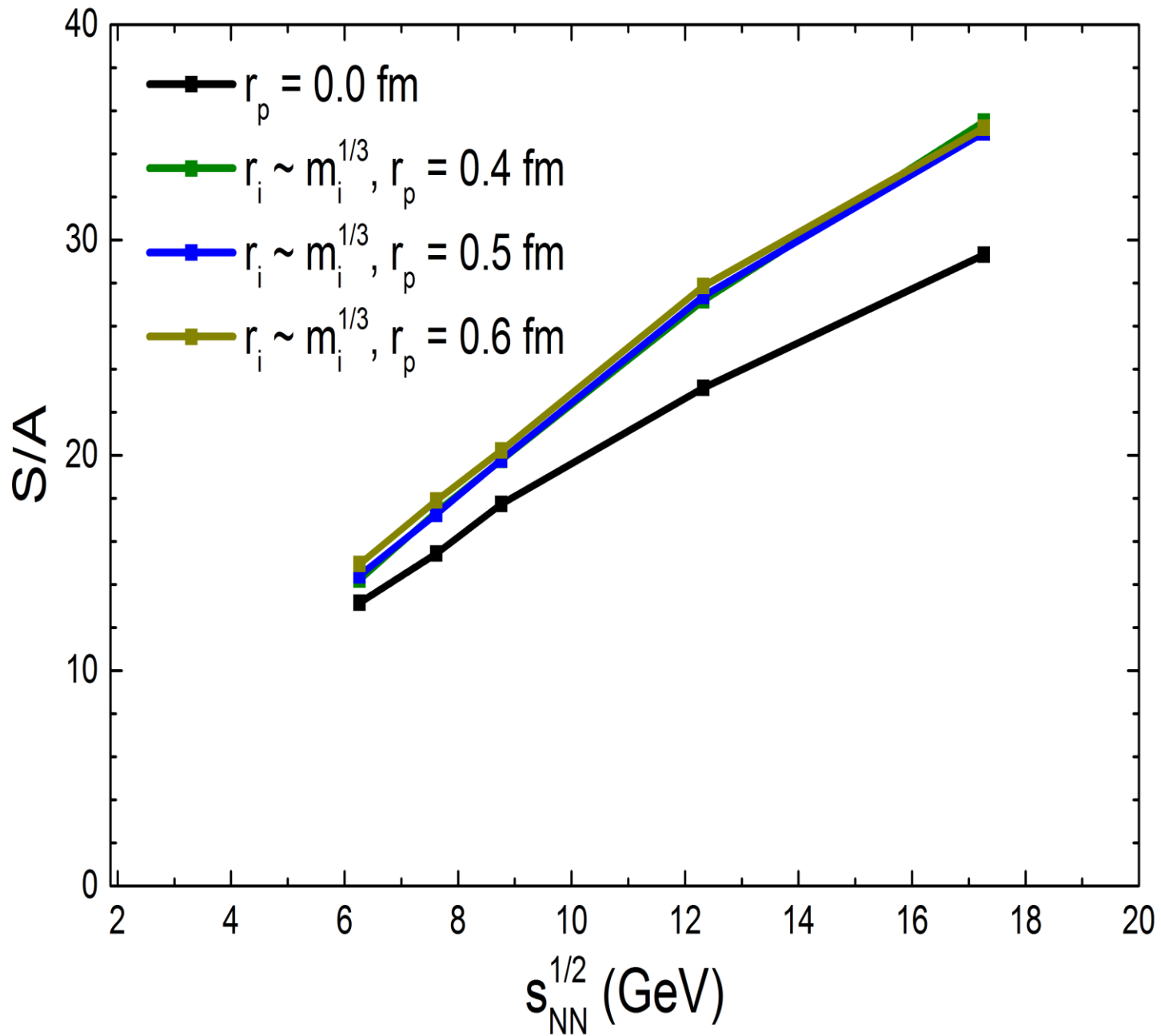
in ISENTROPIC Expansion ever be **reliable?** => **Measure S/A, not T!**

V. Vovchenko, H. Stoecker, in preparation

Multi-component eigenvolume HRG vs NA49 hadron yield data



Wide χ^2 minima regions correspond approximately to isentropic curves



VoVchenko: NA49 data allow measurement of $S/A = \text{const}$ (energy)!

Signatures for **pure glue => glueball** scenario

New event-class in **high multiplicity pp & pA**
at FAIR*, RHIC and LHC

Identification of Glueballs

Lightest Glueball predicted near two states of same Q.N..

“Over population” Predict 2, see 3 states

Glueballs should decay in a flavor-blind fashion.

$$\pi\pi : K\bar{K} : \eta\eta : \eta'\eta' : \eta\eta' = 3 : 4 : 1 : 1 : 0$$

Production Mechanisms:

Certain are expected to be **Glue-rich**, others are Glue-poor. Where do you see them?

Proton-antiproton

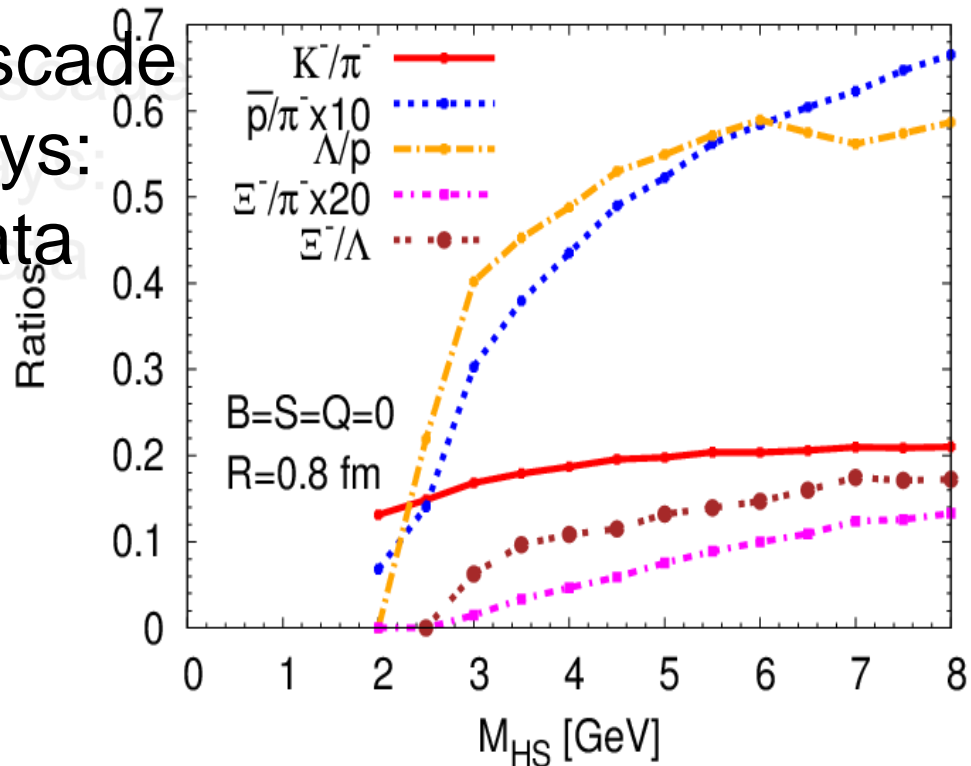
Central Production

J/ψ decays

Hagedorn hadronization: cascade of sequential 2-body decays: yields/ratios vs ALICE data

$$p - p : \sqrt{s_{NN}} = 0.9 \text{ TeV}$$

$$Pb - Pb : \sqrt{s_{NN}} = 2.8 \text{ TeV}$$



data: ALICE @ LHC p-p

	Pb-Pb	4 GeV	8 GeV	
K^-/π^-	0.123(14)	0.149(16)	0.187	0.210
\bar{p}/π^-	0.053(6)	0.045(5)	0.043	0.066
Λ/π^-	0.032(4)	0.036(5)	0.021	0.038
Λ/\bar{p}	0.608(88)	0.78(12)	0.494	0.579
Ξ^-/π^-	0.003(1)	0.0050(6)	0.0023	0.0066
$\Omega^-/\pi^- \cdot 10^{-3}$	—	0.87(17)	0.086	0.560

Alternate Scenario: pure gauge matter in pp, pA – AA ?

Initial Color Glass Condensate \Rightarrow Glasma thermalizes
fast equilibration of Gluons, **slow** equil. of quarks
high pressure, entropy **gluon** plasma
 \Rightarrow **fast** hydrodynamic expansion of **gluon** plasma.



1. Order Phase Transition at $T_c = 270$ MeV of flavorless QCD.



Transition from glue plasma in GlueBall fluid



Glueball-Hagedornstates mix with quarks, decay into Hadrons

Acknowledgements

Transport: **Zhou, Seizel, Xu, Nara, Pang, Niemi, Biro, C. Greiner...**

Hagedorn: **Beitel, Gallmeister, Vovchenko, Hostler, C. Greiner...**

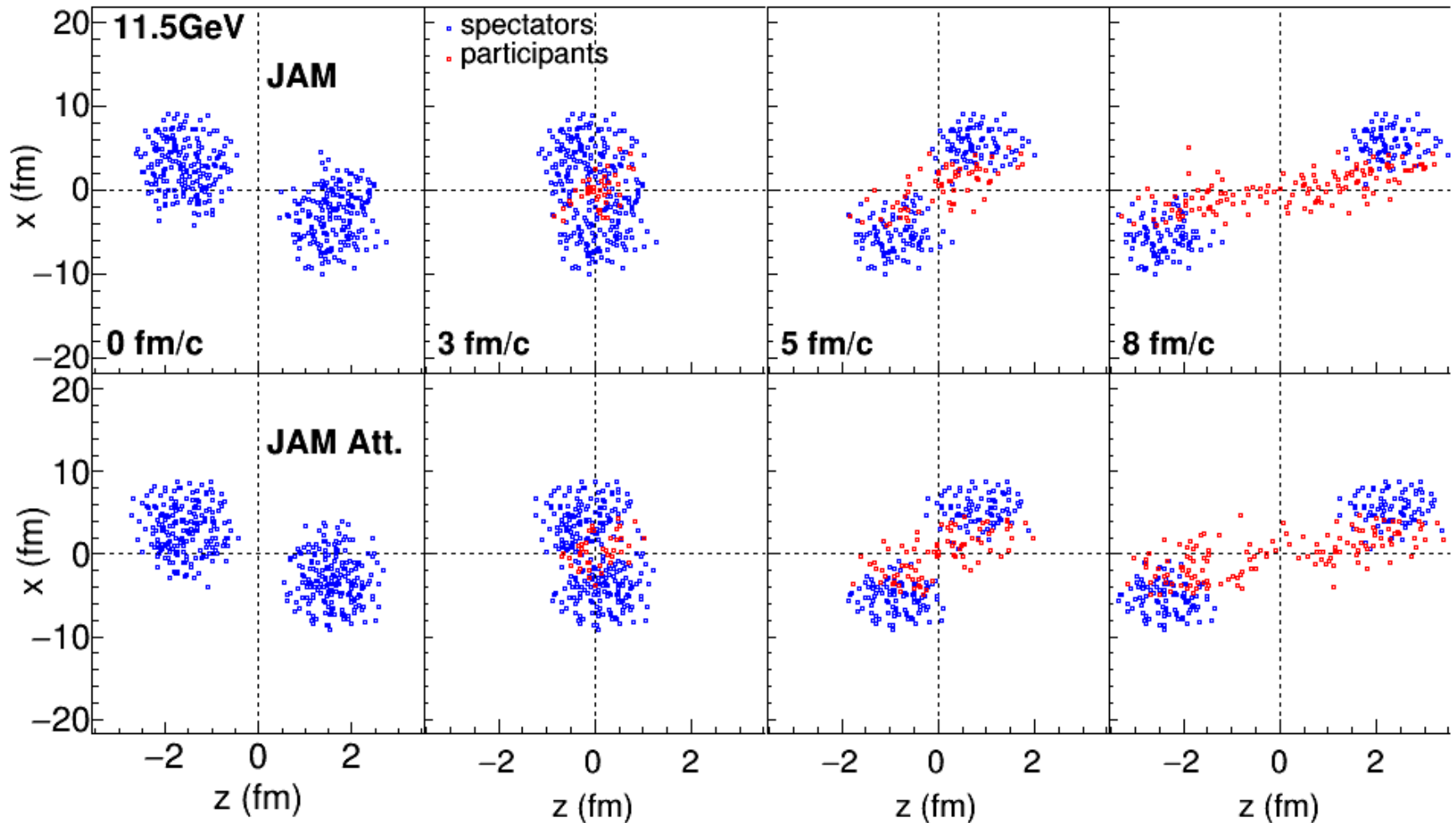
FIAS: **Schramm, Struckmeier, Vasak, ...**

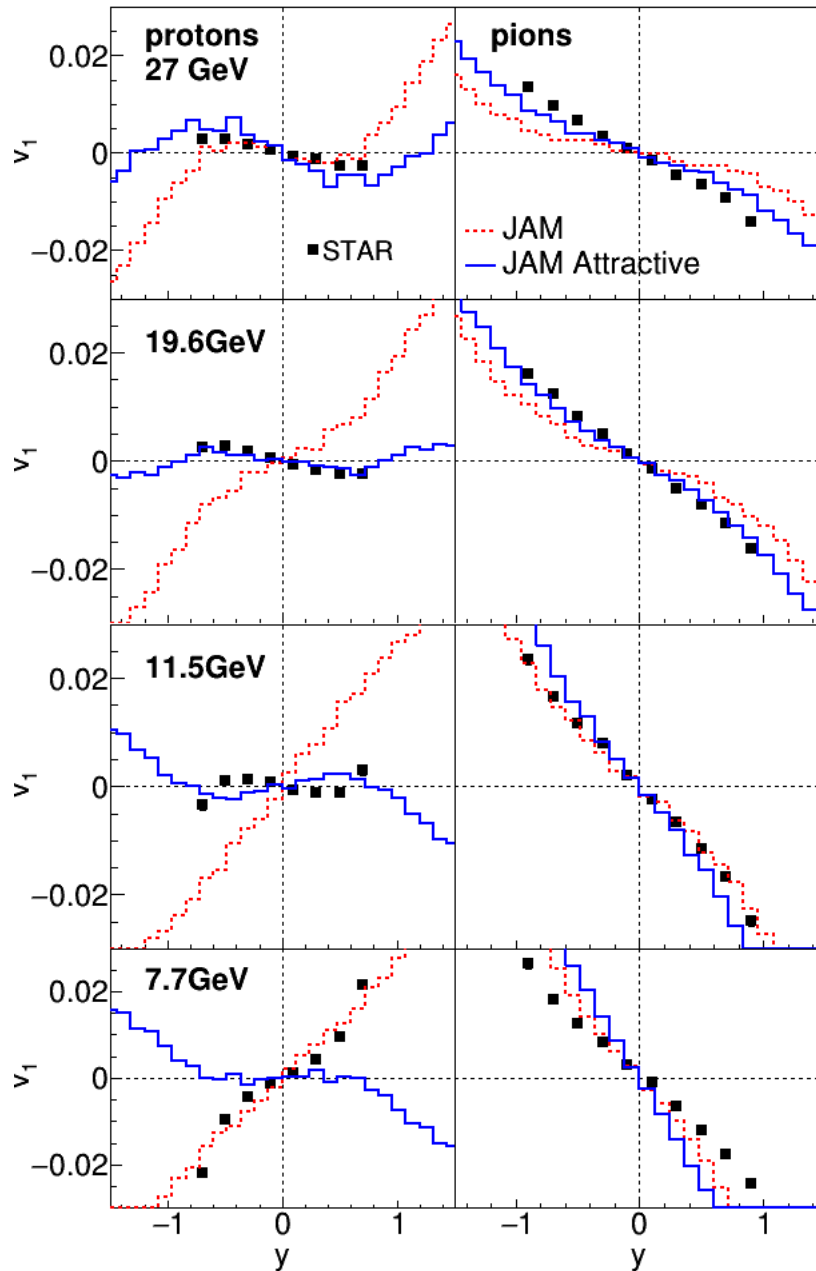
Early phase e-m probes : **Vovchenko, Satarov, Gorenstein, Mishustin, Csernai, Raha, Sinha, ...**

Lattice : **Borsanyi, Fodor, Szabo, Karsch, Panero, Philipsen...**

Experiment: **Giubellino, Harris, Andronic, Oeschler, PBM, Loizids**

Time evolution of density at 11.5GeV





JAM

Akira, Nara & HST

Directed Flow v_1
protons
and pions
STAR data