



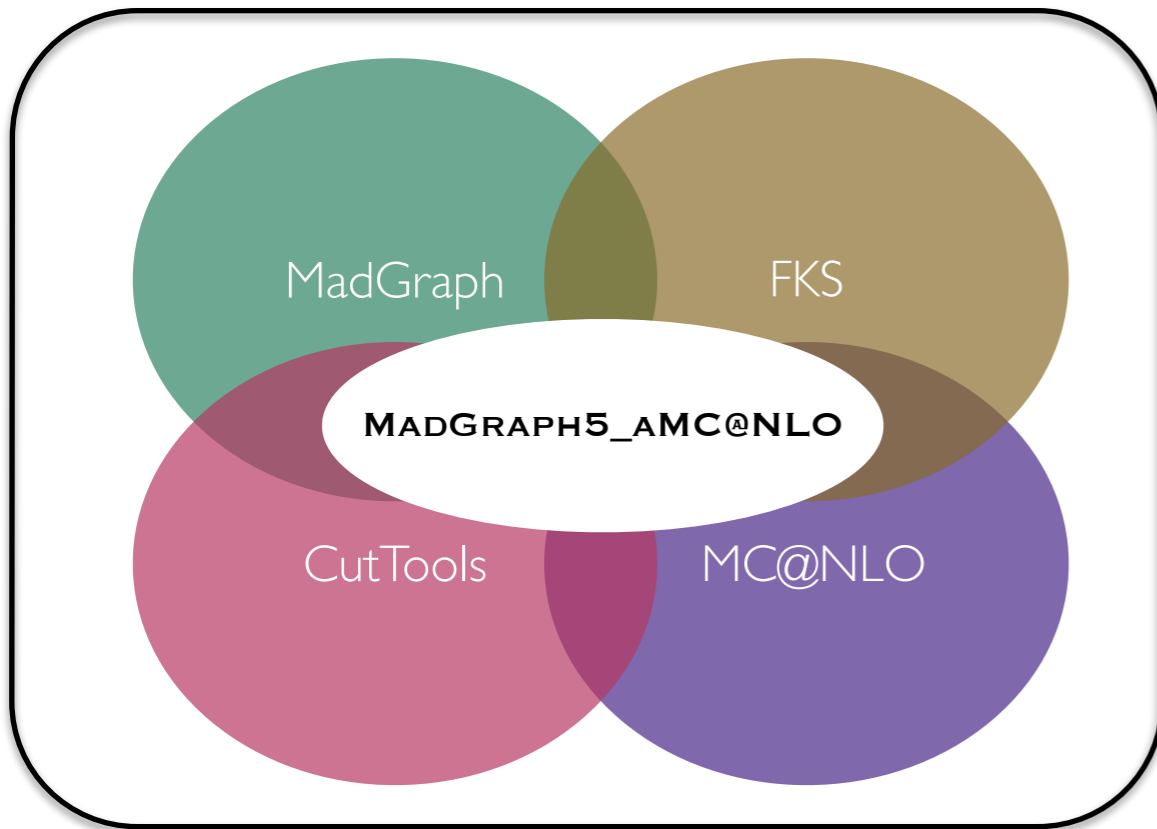
Loop-induced and rare processes @ 100 TeV

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IPPP/Durham

in collaboration with P. Torrielli and V. Hirschi
based on 1407.1623
1507.00020

- rare processes
 - enhancement from 8 TeV to 100 TeV
 - cross-sections @100TeV
- loop-induced processes
 - method and validation
 - cross-sections @100TeV
 - examples

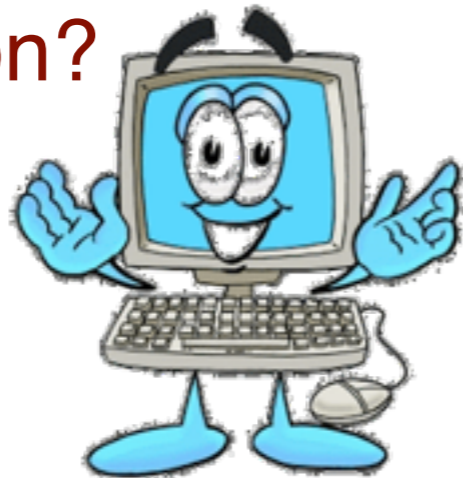
- Important to have the cross-section for a large sample of (SM) processes
 - ➔ allow to decide which one can be study
 - ➔ important for BSM searches
- We have the tools (@NLO)



- automated NLO
- MC@NLO method
- using FKS subtraction
- using OPP method

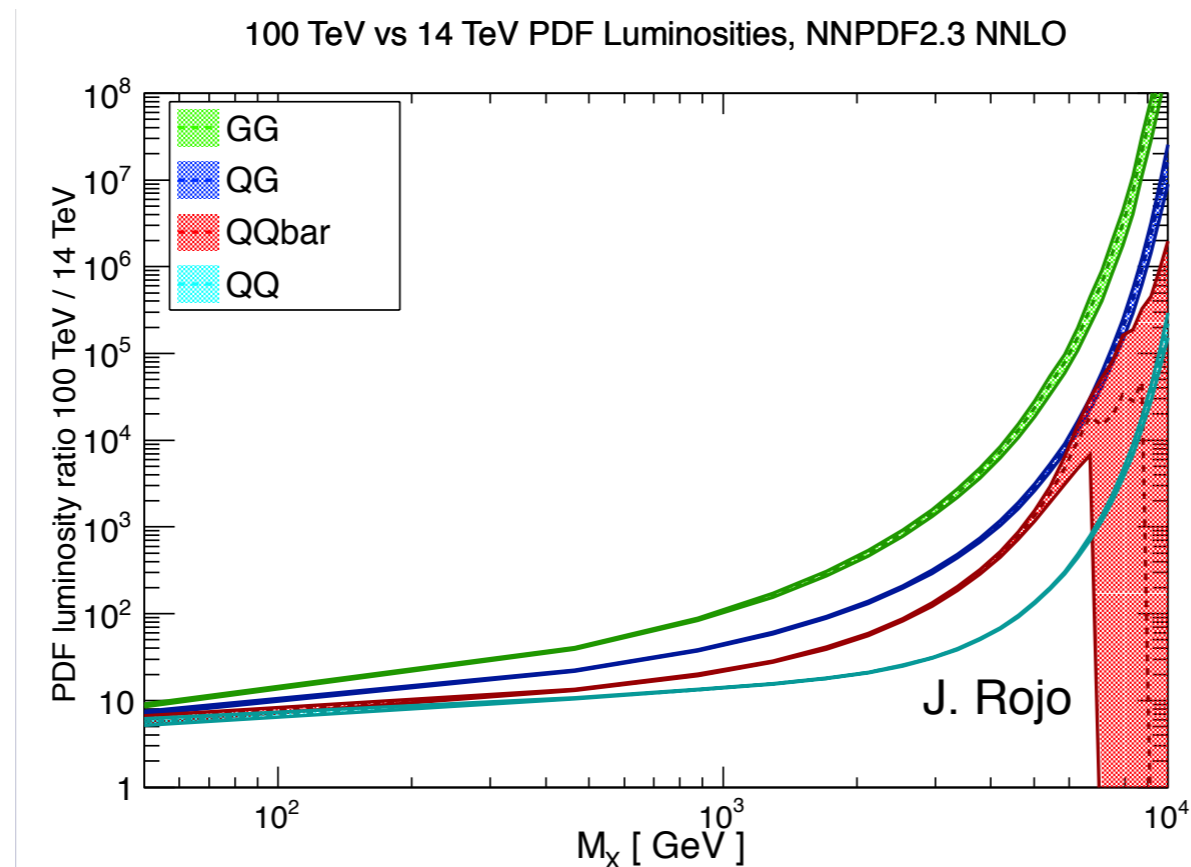
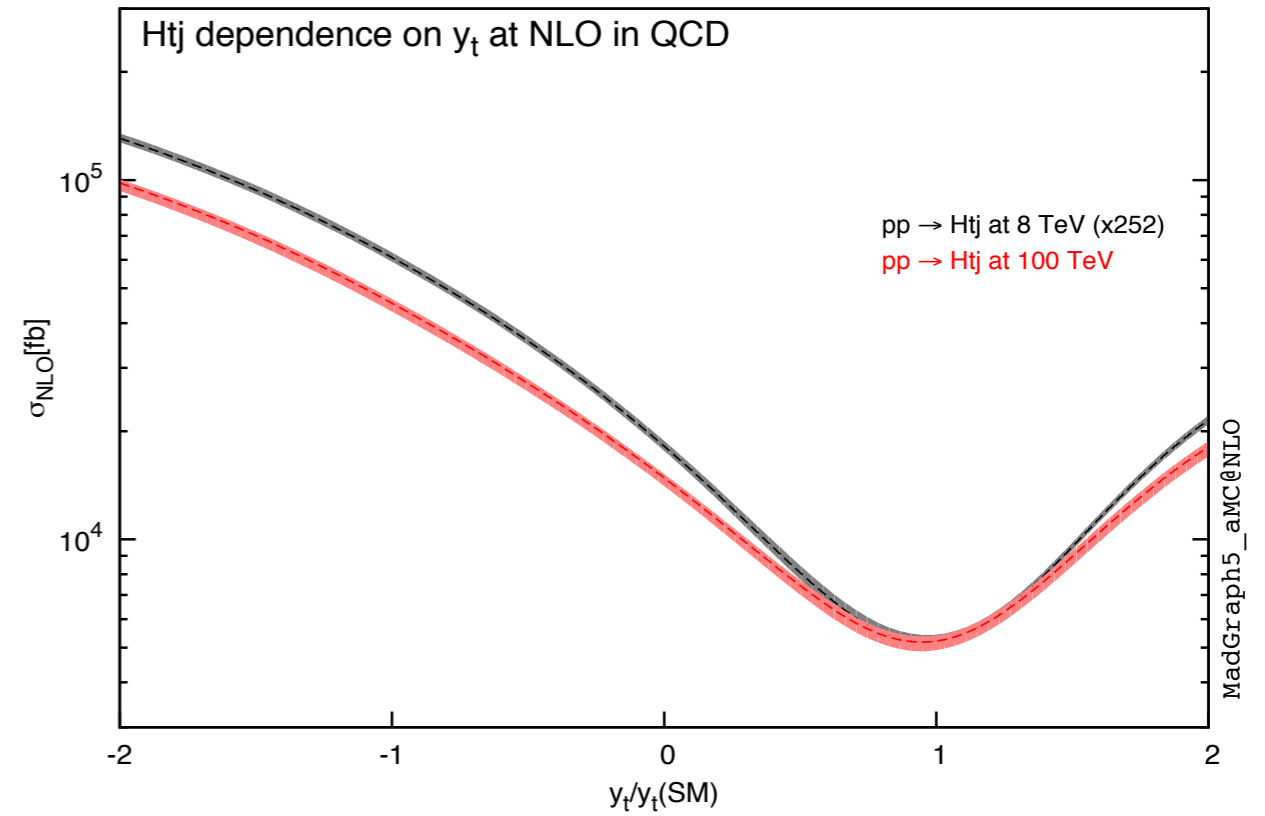
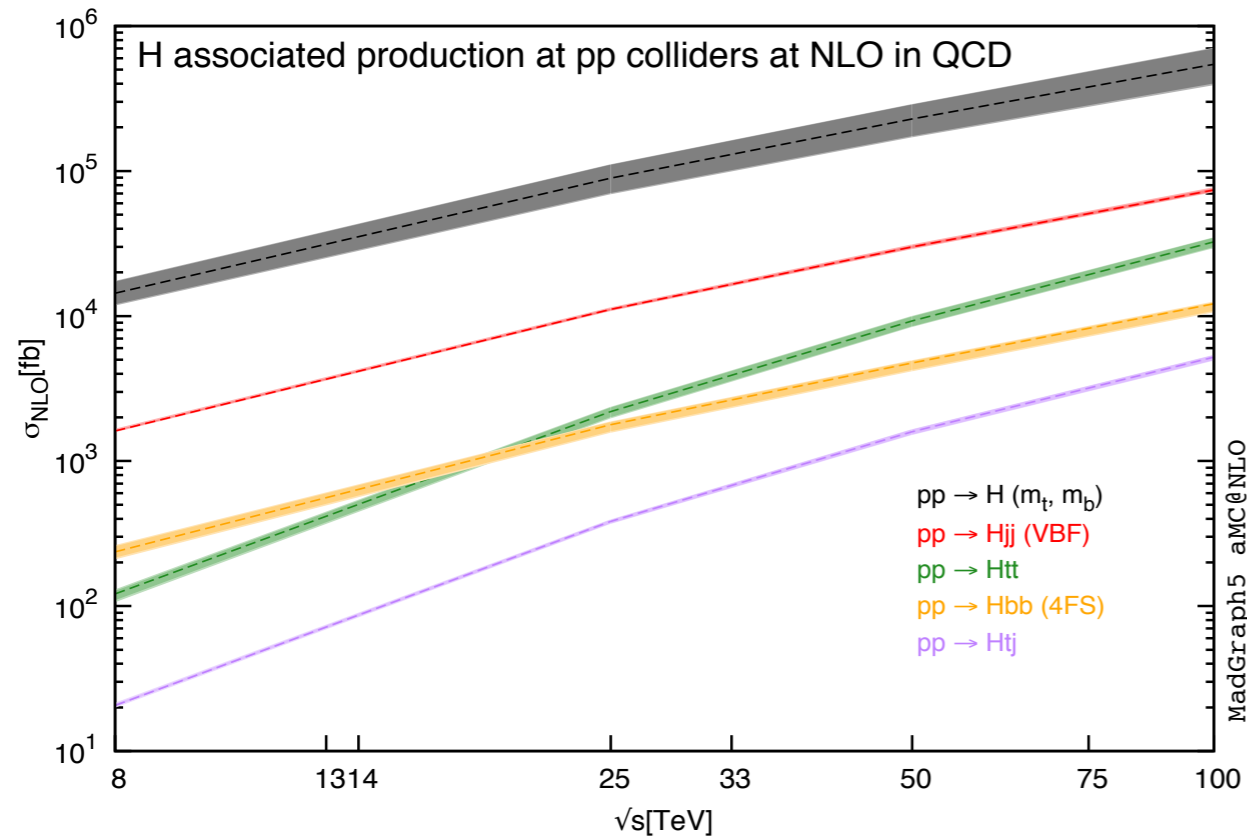
Why Automation?

- time
- robust
- easy

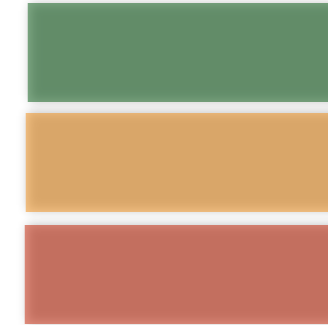


Why NLO?

- reliable prediction of cross-section
- reduction of theoretical uncertainty



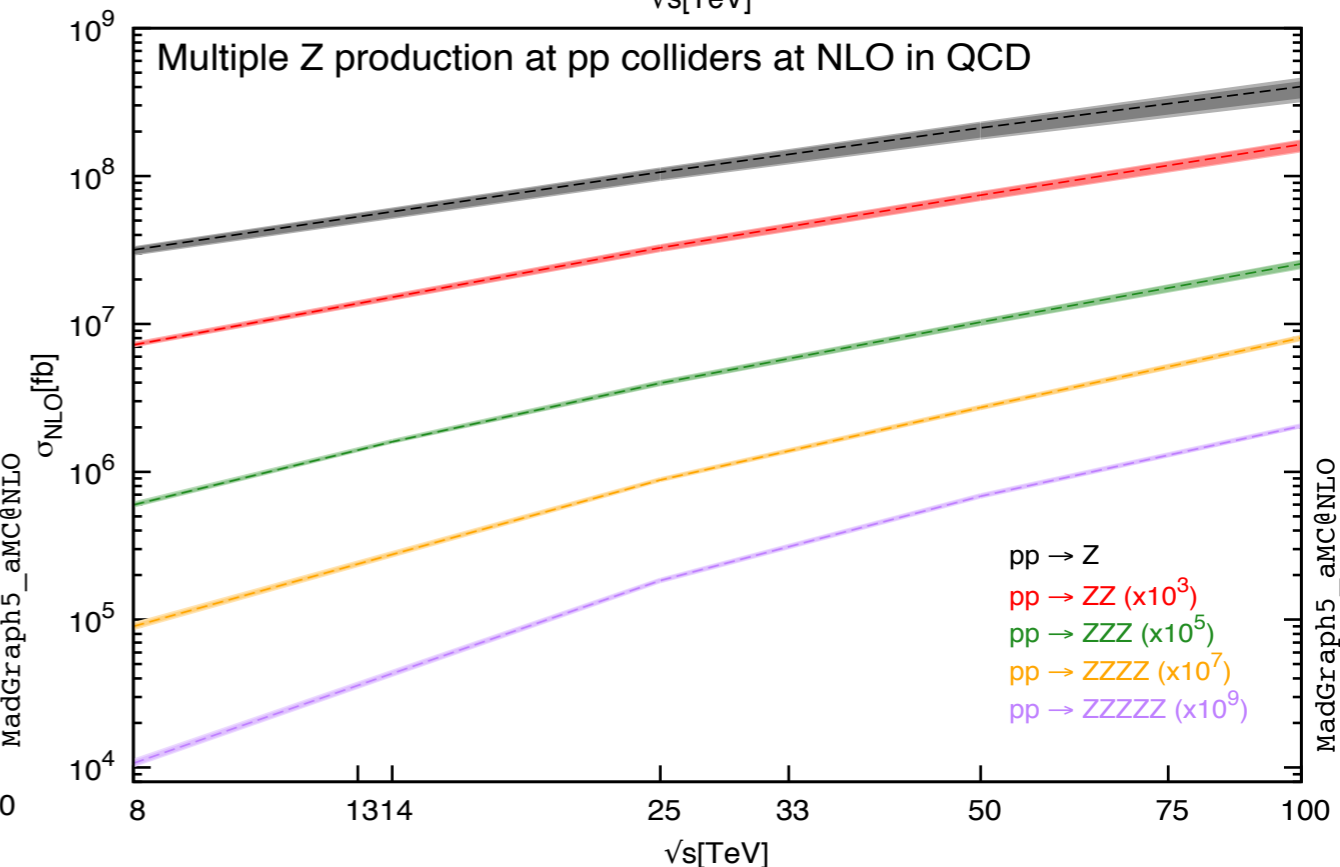
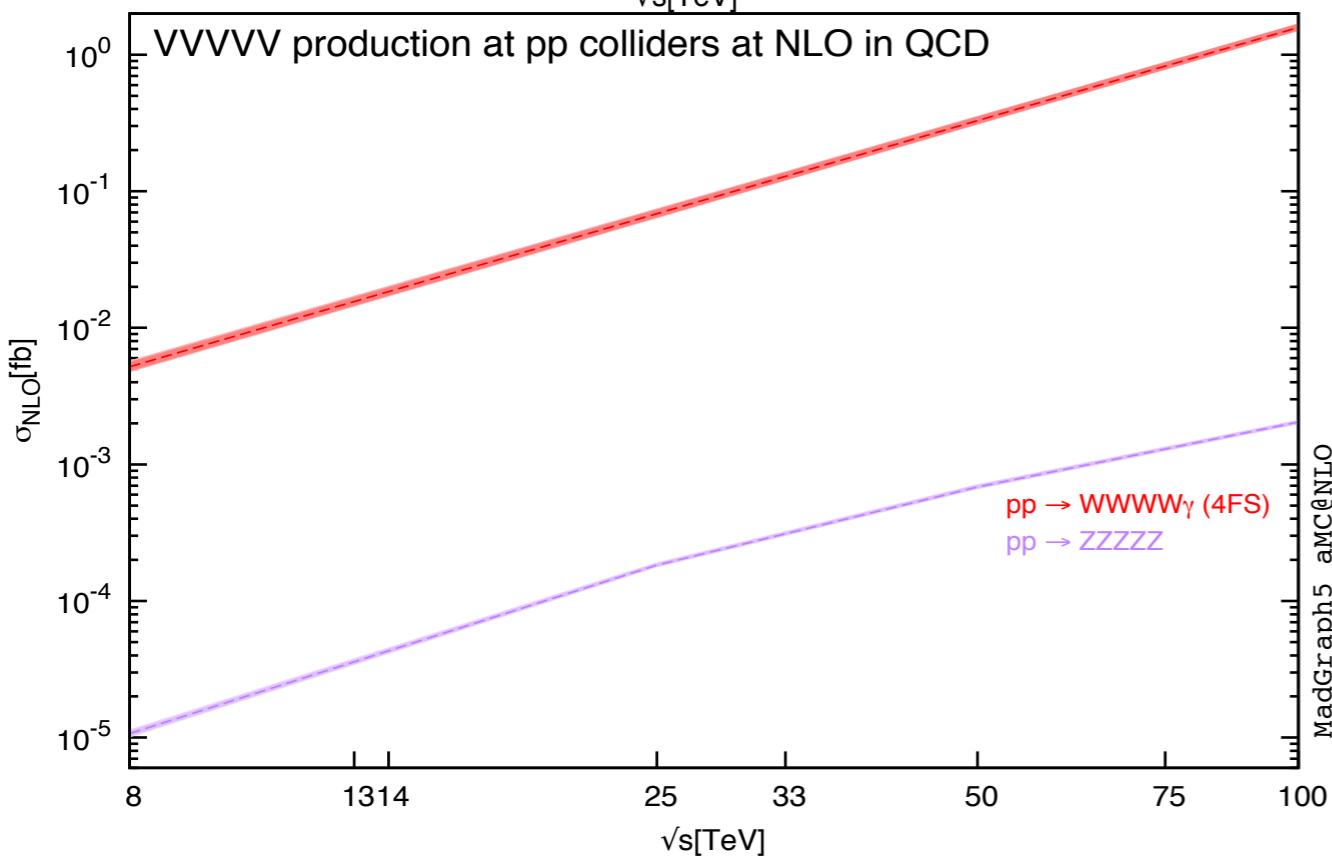
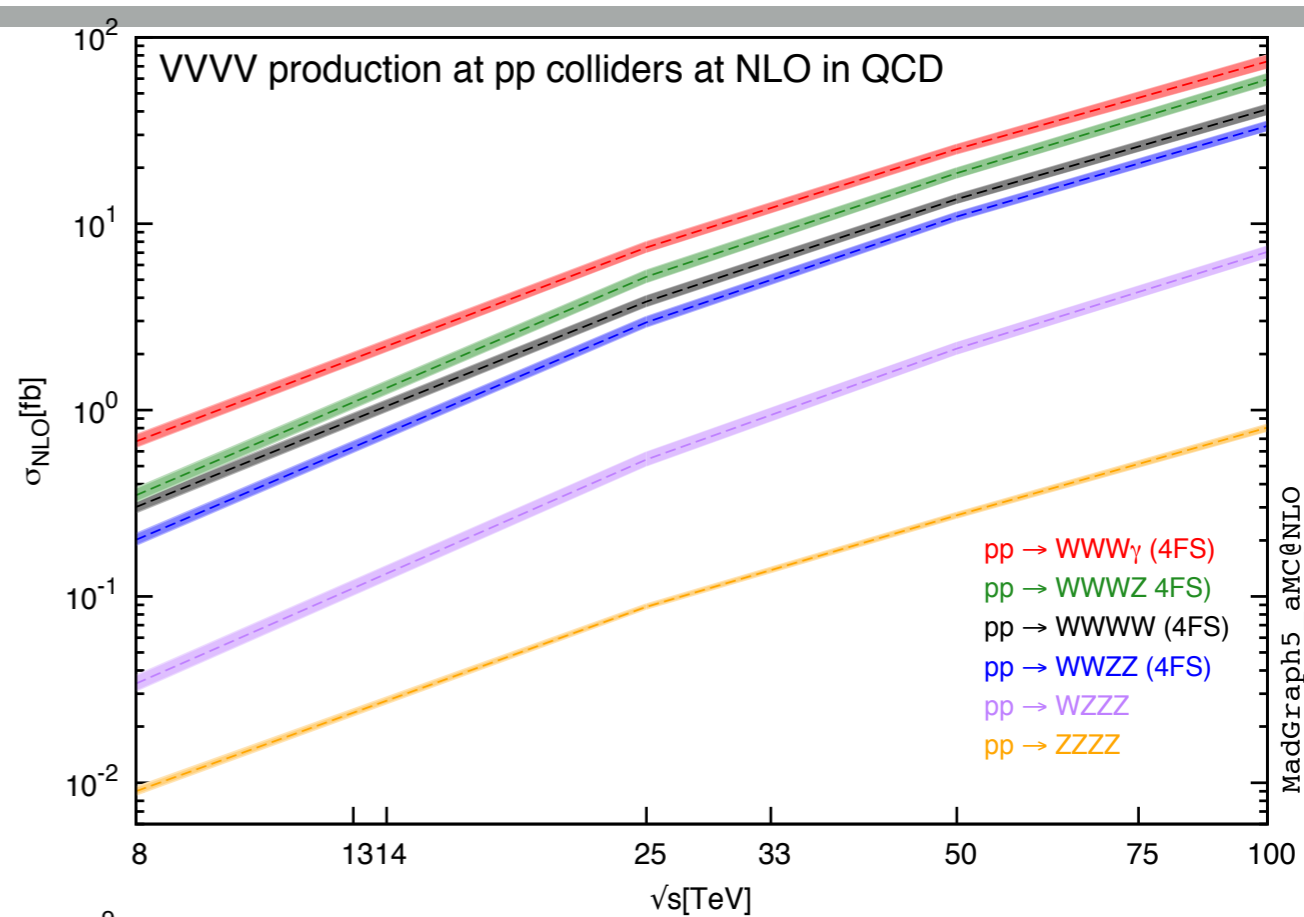
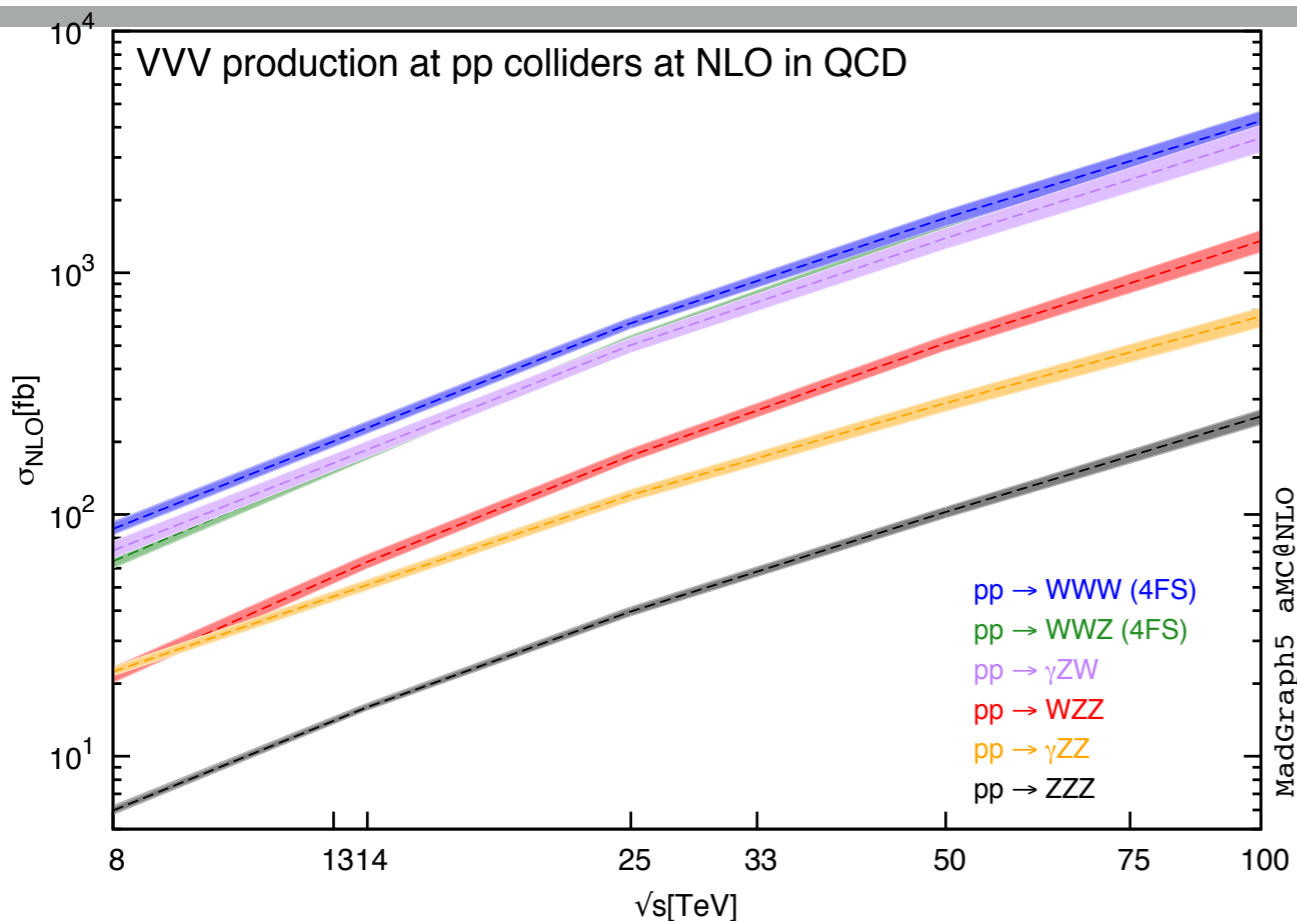
Process	$\sigma_{\text{NLO}}(8 \text{ TeV})$ [fb]	$\sigma_{\text{NLO}}(100 \text{ TeV})$ [fb]	ρ
$pp \rightarrow H(m_t, m_b)$	$1.44 \cdot 10^4$ $^{+20\% +1\%}_{-16\% -2\%}$	$5.46 \cdot 10^5$ $^{+28\% +2\%}_{-27\% -2\%}$	38
$pp \rightarrow Hjj$ (VBF)	$1.61 \cdot 10^3$ $^{+1\% +2\%}_{-0\% -2\%}$	$7.40 \cdot 10^4$ $^{+3\% +2\%}_{-2\% -1\%}$	46
$pp \rightarrow Ht\bar{t}$	$1.21 \cdot 10^2$ $^{+5\% +3\%}_{-9\% -3\%}$	$3.25 \cdot 10^4$ $^{+7\% +1\%}_{-8\% -1\%}$	269
$pp \rightarrow Hb\bar{b}$ (4FS)	$2.37 \cdot 10^2$ $^{+9\% +2\%}_{-9\% -2\%}$	$1.21 \cdot 10^4$ $^{+2\% +2\%}_{-10\% -2\%}$	51
$pp \rightarrow Htj$	$2.07 \cdot 10^1$ $^{+2\% +2\%}_{-1\% -2\%}$	$5.21 \cdot 10^3$ $^{+3\% +1\%}_{-5\% -1\%}$	252
$pp \rightarrow HW^\pm$	$7.31 \cdot 10^2$ $^{+2\% +2\%}_{-1\% -2\%}$	$1.54 \cdot 10^4$ $^{+5\% +2\%}_{-8\% -2\%}$	21
$pp \rightarrow HZ$	$3.87 \cdot 10^2$ $^{+2\% +2\%}_{-1\% -2\%}$	$8.82 \cdot 10^3$ $^{+4\% +2\%}_{-8\% -2\%}$	23
$pp \rightarrow HW^+W^-$ (4FS)	$4.62 \cdot 10^0$ $^{+3\% +2\%}_{-2\% -2\%}$	$1.68 \cdot 10^2$ $^{+5\% +2\%}_{-6\% -1\%}$	36
$pp \rightarrow HZW^\pm$	$2.17 \cdot 10^0$ $^{+4\% +2\%}_{-4\% -2\%}$	$9.94 \cdot 10^1$ $^{+6\% +2\%}_{-7\% -1\%}$	46
$pp \rightarrow HW^\pm\gamma$	$2.36 \cdot 10^0$ $^{+3\% +2\%}_{-3\% -2\%}$	$7.75 \cdot 10^1$ $^{+7\% +2\%}_{-8\% -1\%}$	33
$pp \rightarrow HZ\gamma$	$1.54 \cdot 10^0$ $^{+3\% +2\%}_{-2\% -2\%}$	$4.29 \cdot 10^1$ $^{+5\% +2\%}_{-7\% -2\%}$	28
$pp \rightarrow HZZ$	$1.10 \cdot 10^0$ $^{+2\% +2\%}_{-2\% -2\%}$	$4.20 \cdot 10^1$ $^{+4\% +2\%}_{-6\% -1\%}$	38
$pp \rightarrow HW^\pm j$	$3.18 \cdot 10^2$ $^{+4\% +2\%}_{-4\% -1\%}$	$1.07 \cdot 10^4$ $^{+2\% +2\%}_{-7\% -1\%}$	34
$pp \rightarrow HW^\pm jj$	$6.06 \cdot 10^1$ $^{+6\% +1\%}_{-8\% -1\%}$	$4.90 \cdot 10^3$ $^{+2\% +1\%}_{-6\% -1\%}$	81
$pp \rightarrow HZj$	$1.71 \cdot 10^2$ $^{+4\% +1\%}_{-4\% -1\%}$	$6.31 \cdot 10^3$ $^{+2\% +2\%}_{-7\% -1\%}$	37
$pp \rightarrow HZjj$	$3.50 \cdot 10^1$ $^{+7\% +1\%}_{-10\% -1\%}$	$2.81 \cdot 10^3$ $^{+2\% +1\%}_{-5\% -1\%}$	80



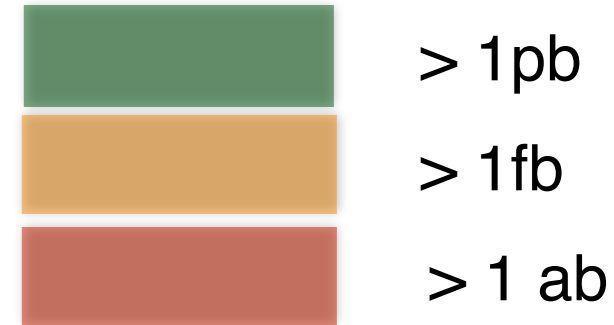
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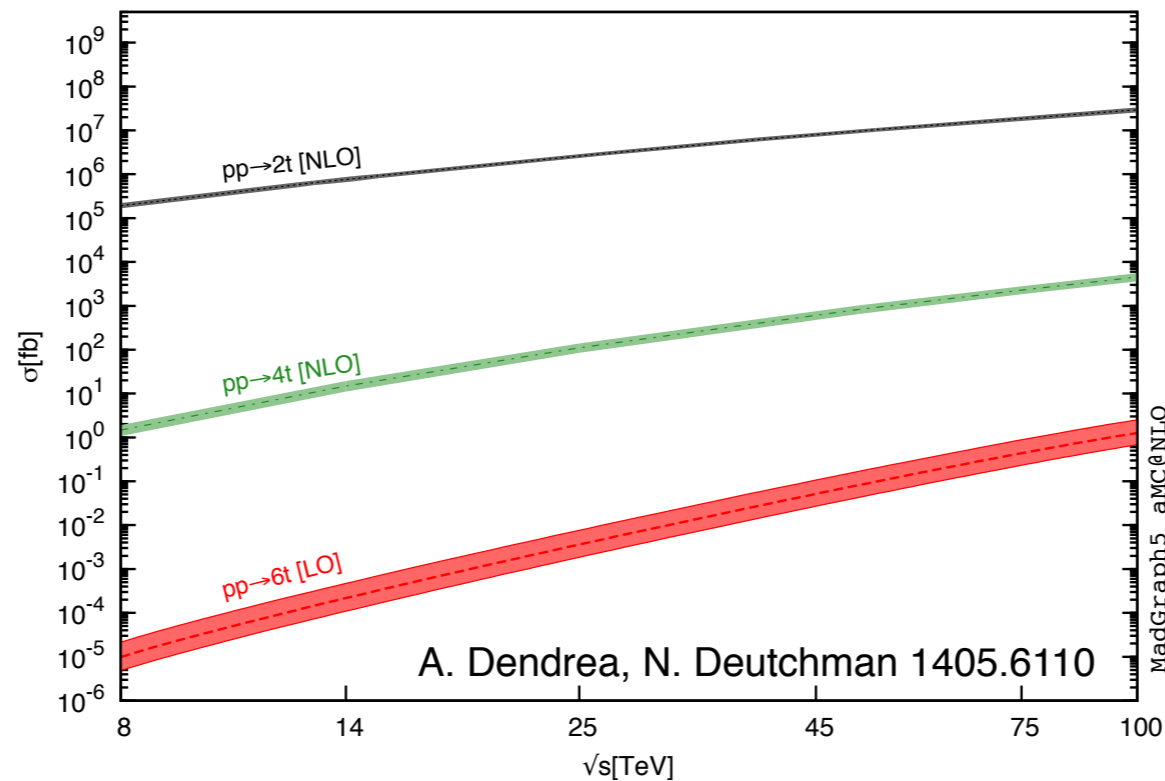
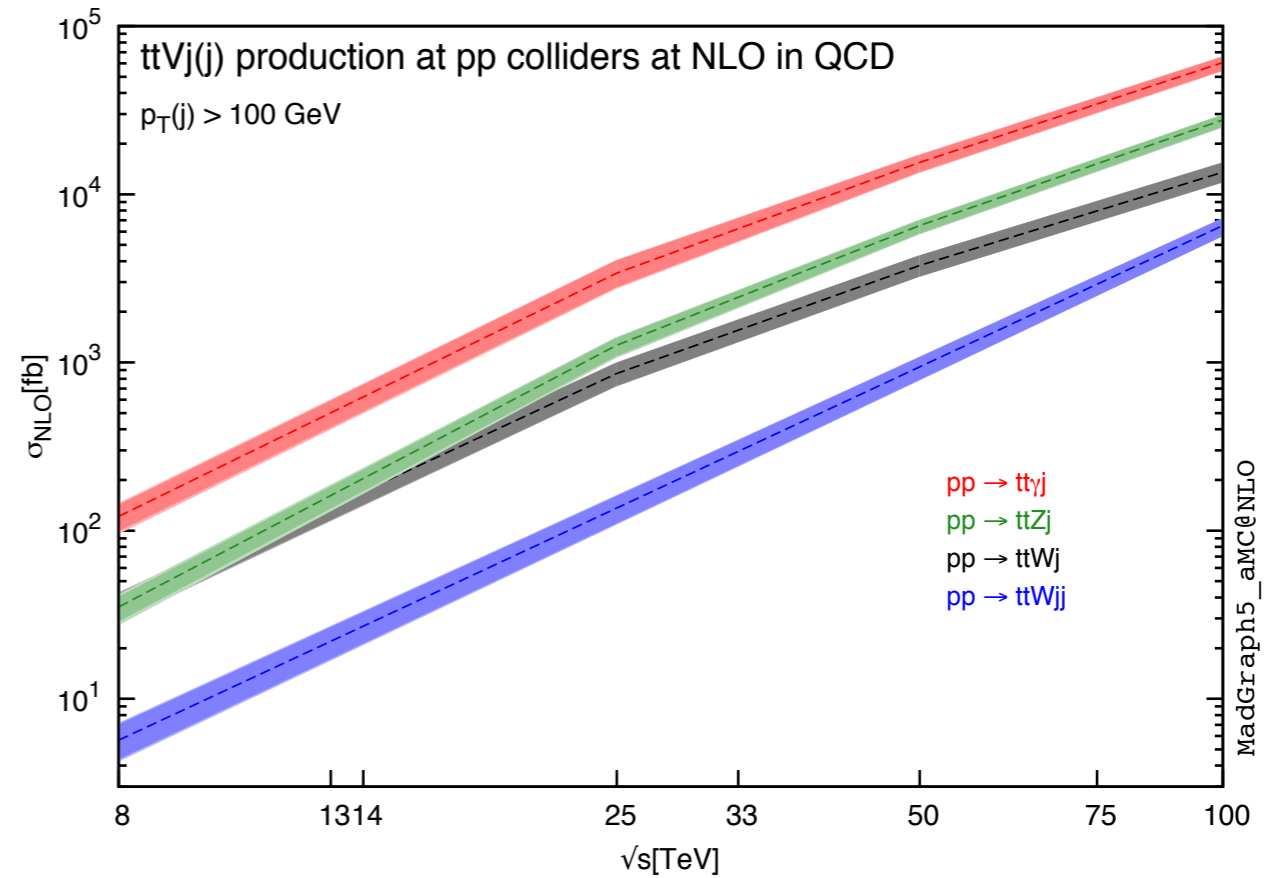
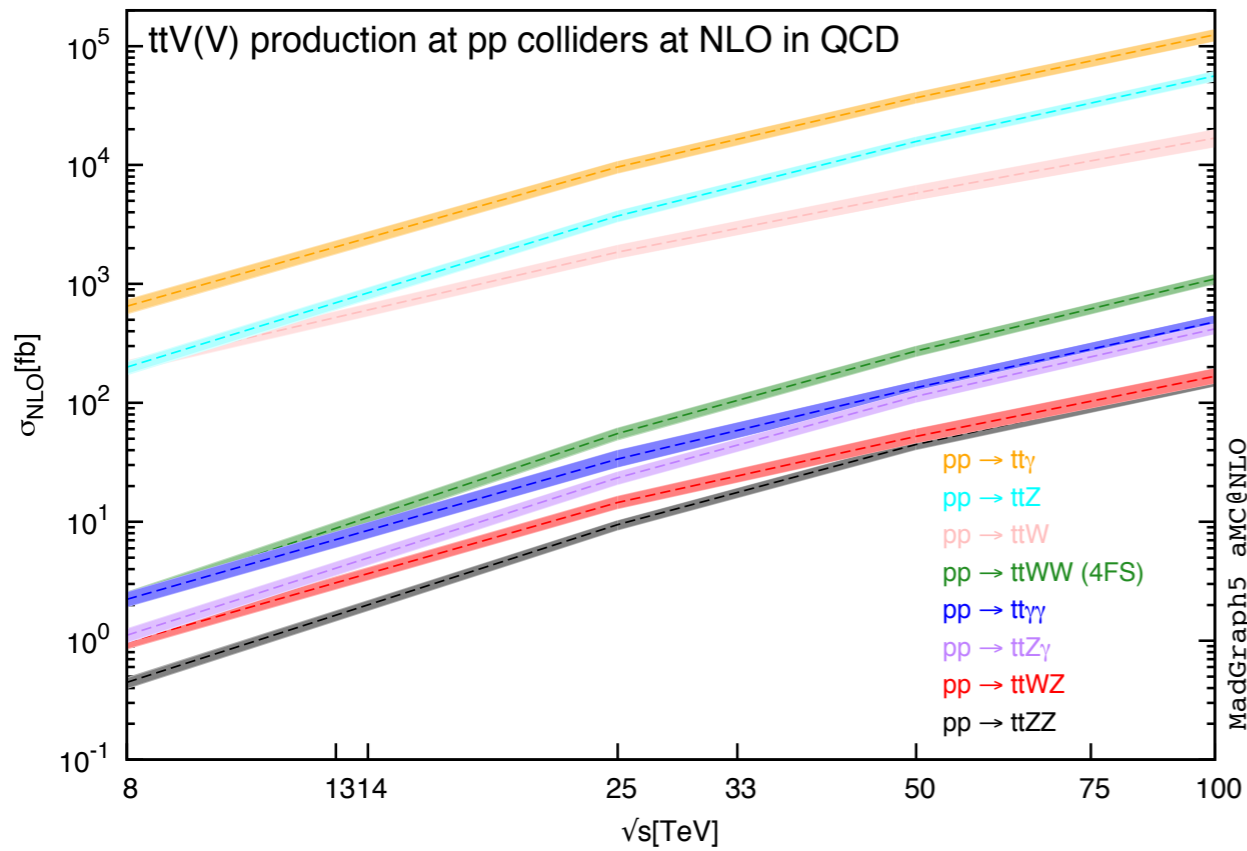
> 1 fb

> 1 ab

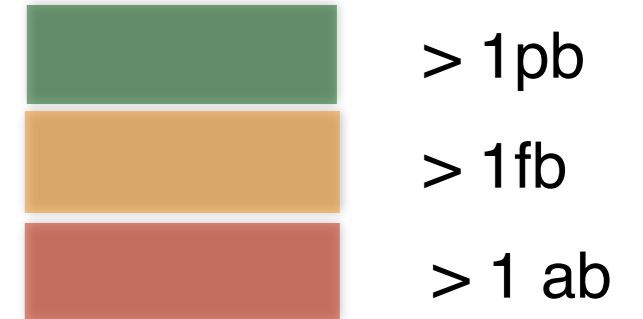


Process		$\sigma_{\text{NLO}}(8 \text{ TeV})$ [fb]	$\sigma_{\text{NLO}}(100 \text{ TeV})$ [fb]	ρ
$pp \rightarrow$	$W^+W^-W^\pm$ (4FS)	$8.73 \cdot 10^1$ $^{+6\%}_{-4\%}$ $^{+2\%}_{-2\%}$	$4.25 \cdot 10^3$ $^{+9\%}_{-9\%}$ $^{+1\%}_{-1\%}$	49
$pp \rightarrow$	W^+W^-Z (4FS)	$6.41 \cdot 10^1$ $^{+7\%}_{-5\%}$ $^{+2\%}_{-2\%}$	$4.01 \cdot 10^3$ $^{+9\%}_{-9\%}$ $^{+1\%}_{-1\%}$	63
$pp \rightarrow$	$\gamma W^\pm Z$	$7.11 \cdot 10^1$ $^{+8\%}_{-7\%}$ $^{+2\%}_{-1\%}$	$3.61 \cdot 10^3$ $^{+12\%}_{-12\%}$ $^{+1\%}_{-1\%}$	51
$pp \rightarrow$	$W^\pm ZZ$	$2.16 \cdot 10^1$ $^{+7\%}_{-6\%}$ $^{+2\%}_{-2\%}$	$1.36 \cdot 10^3$ $^{+10\%}_{-10\%}$ $^{+1\%}_{-1\%}$	63
$pp \rightarrow$	γZZ	$2.24 \cdot 10^1$ $^{+4\%}_{-3\%}$ $^{+2\%}_{-2\%}$	$6.62 \cdot 10^2$ $^{+8\%}_{-9\%}$ $^{+2\%}_{-1\%}$	30
$pp \rightarrow$	ZZZ	$5.97 \cdot 10^0$ $^{+3\%}_{-3\%}$ $^{+2\%}_{-2\%}$	$2.55 \cdot 10^2$ $^{+5\%}_{-7\%}$ $^{+2\%}_{-1\%}$	43
$pp \rightarrow$	$W^+W^-W^\pm\gamma$ (4FS)	$6.78 \cdot 10^{-1}$ $^{+8\%}_{-6\%}$ $^{+2\%}_{-2\%}$	$7.42 \cdot 10^1$ $^{+8\%}_{-8\%}$ $^{+1\%}_{-1\%}$	109
$pp \rightarrow$	$W^+W^-W^\pm Z$ (4FS)	$3.48 \cdot 10^{-1}$ $^{+8\%}_{-7\%}$ $^{+2\%}_{-2\%}$	$5.95 \cdot 10^1$ $^{+7\%}_{-7\%}$ $^{+1\%}_{-1\%}$	171
$pp \rightarrow$	$W^+W^-W^+W^-$ (4FS)	$3.01 \cdot 10^{-1}$ $^{+7\%}_{-6\%}$ $^{+2\%}_{-2\%}$	$4.11 \cdot 10^1$ $^{+7\%}_{-6\%}$ $^{+1\%}_{-1\%}$	137
$pp \rightarrow$	W^+W^-ZZ (4FS)	$2.01 \cdot 10^{-1}$ $^{+7\%}_{-6\%}$ $^{+2\%}_{-2\%}$	$3.34 \cdot 10^1$ $^{+6\%}_{-6\%}$ $^{+1\%}_{-1\%}$	166
$pp \rightarrow$	$W^\pm ZZZ$	$3.40 \cdot 10^{-2}$ $^{+10\%}_{-8\%}$ $^{+2\%}_{-2\%}$	$7.06 \cdot 10^0$ $^{+8\%}_{-7\%}$ $^{+1\%}_{-1\%}$	208
$pp \rightarrow$	$ZZZZ$	$8.72 \cdot 10^{-3}$ $^{+4\%}_{-4\%}$ $^{+3\%}_{-2\%}$	$8.05 \cdot 10^{-1}$ $^{+4\%}_{-4\%}$ $^{+2\%}_{-1\%}$	92
$pp \rightarrow$	$W^+W^-W^+W^-\gamma$ (4FS)	$5.18 \cdot 10^{-3}$ $^{+8\%}_{-7\%}$ $^{+3\%}_{-2\%}$	$1.58 \cdot 10^0$ $^{+6\%}_{-5\%}$ $^{+1\%}_{-1\%}$	305
$pp \rightarrow$	$ZZZZZ$	$1.07 \cdot 10^{-5}$ $^{+5\%}_{-4\%}$ $^{+3\%}_{-2\%}$	$2.04 \cdot 10^{-3}$ $^{+3\%}_{-3\%}$ $^{+2\%}_{-1\%}$	191

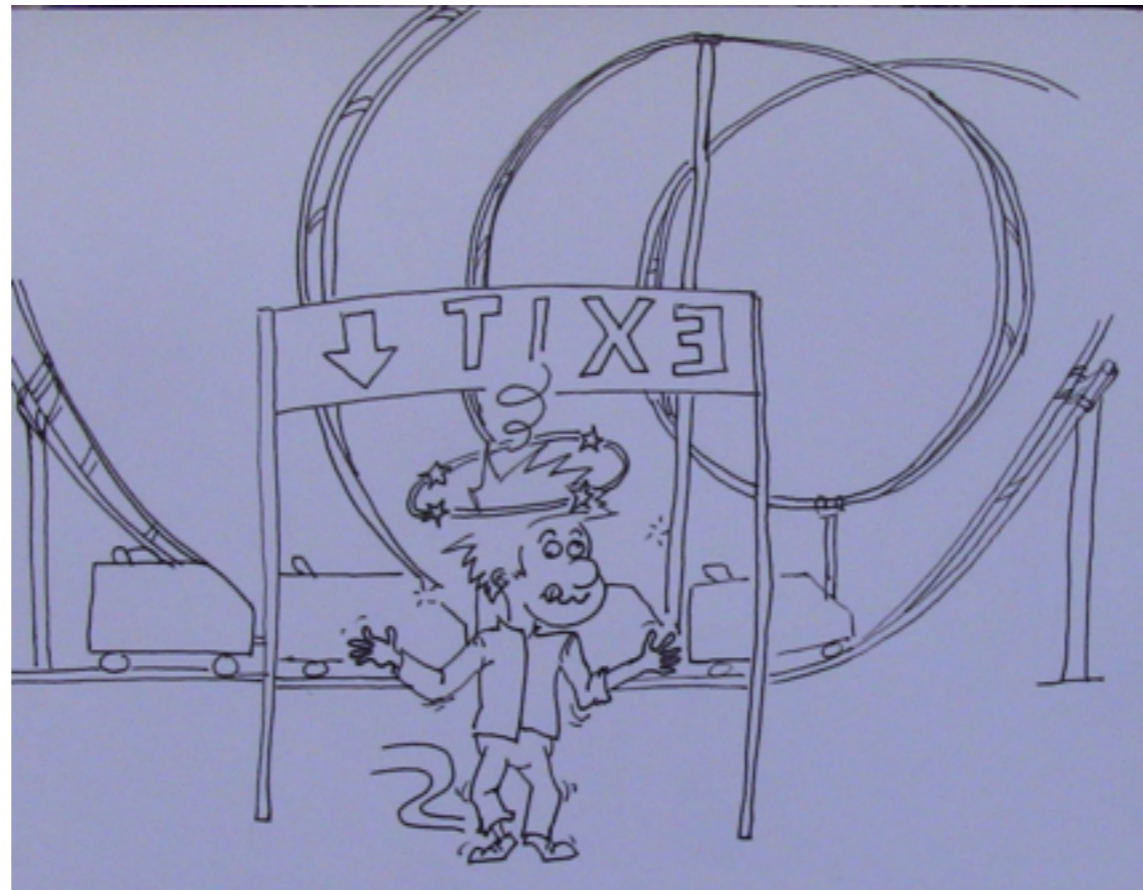




Process	$\sigma_{\text{NLO}}(8 \text{ TeV})$ [fb]	$\sigma_{\text{NLO}}(100 \text{ TeV})$ [fb]	ρ
$pp \rightarrow t\bar{t}\gamma$	$6.50 \cdot 10^2$ $^{+12\%}_{-13\%}$ $^{+2\%}_{-2\%}$	$1.24 \cdot 10^5$ $^{+11\%}_{-11\%}$ $^{+1\%}_{-1\%}$	192
$pp \rightarrow t\bar{t}Z$	$1.99 \cdot 10^2$ $^{+10\%}_{-12\%}$ $^{+3\%}_{-3\%}$	$5.63 \cdot 10^4$ $^{+9\%}_{-10\%}$ $^{+1\%}_{-1\%}$	282
$pp \rightarrow t\bar{t}W^\pm$	$2.05 \cdot 10^2$ $^{+9\%}_{-10\%}$ $^{+2\%}_{-2\%}$	$1.68 \cdot 10^4$ $^{+18\%}_{-16\%}$ $^{+1\%}_{-1\%}$	82
$pp \rightarrow t\bar{t}\gamma j$	$1.22 \cdot 10^2$ $^{+17\%}_{-18\%}$ $^{+3\%}_{-3\%}$	$6.07 \cdot 10^4$ $^{+8\%}_{-10\%}$ $^{+1\%}_{-1\%}$	498
$pp \rightarrow t\bar{t}Z j$	$3.51 \cdot 10^1$ $^{+15\%}_{-18\%}$ $^{+4\%}_{-4\%}$	$2.77 \cdot 10^4$ $^{+7\%}_{-9\%}$ $^{+1\%}_{-1\%}$	789
$pp \rightarrow t\bar{t}W^\pm j$	$3.59 \cdot 10^1$ $^{+18\%}_{-18\%}$ $^{+2\%}_{-2\%}$	$1.36 \cdot 10^4$ $^{+14\%}_{-13\%}$ $^{+1\%}_{-1\%}$	379
$pp \rightarrow t\bar{t}W^\pm jj$	$5.67 \cdot 10^0$ $^{+24\%}_{-23\%}$ $^{+3\%}_{-2\%}$	$6.52 \cdot 10^3$ $^{+11\%}_{-14\%}$ $^{+1\%}_{-1\%}$	1150
$pp \rightarrow t\bar{t}W^+W^-$ (4FS)	$2.27 \cdot 10^0$ $^{+11\%}_{-13\%}$ $^{+3\%}_{-3\%}$	$1.10 \cdot 10^3$ $^{+9\%}_{-9\%}$ $^{+1\%}_{-1\%}$	486
$pp \rightarrow t\bar{t}\gamma\gamma$	$2.23 \cdot 10^0$ $^{+14\%}_{-13\%}$ $^{+2\%}_{-1\%}$	$4.81 \cdot 10^2$ $^{+13\%}_{-11\%}$ $^{+1\%}_{-1\%}$	216
$pp \rightarrow t\bar{t}Z\gamma$	$1.11 \cdot 10^0$ $^{+12\%}_{-13\%}$ $^{+2\%}_{-2\%}$	$4.20 \cdot 10^2$ $^{+10\%}_{-9\%}$ $^{+1\%}_{-1\%}$	378
$pp \rightarrow t\bar{t}W^\pm Z$	$9.71 \cdot 10^{-1}$ $^{+10\%}_{-11\%}$ $^{+3\%}_{-2\%}$	$1.68 \cdot 10^2$ $^{+16\%}_{-13\%}$ $^{+1\%}_{-1\%}$	173
$pp \rightarrow t\bar{t}ZZ$	$4.47 \cdot 10^{-1}$ $^{+8\%}_{-10\%}$ $^{+3\%}_{-2\%}$	$1.58 \cdot 10^2$ $^{+15\%}_{-12\%}$ $^{+1\%}_{-1\%}$	353



- loop-induced processes
 - ➔ method and validation
 - ➔ cross-sections @100TeV
 - ➔ examples



Why?

- main production mechanism for Higgs & Higgs associated processes
- contribution for NNLO computation
- correction to shape of observables

Difficulties?

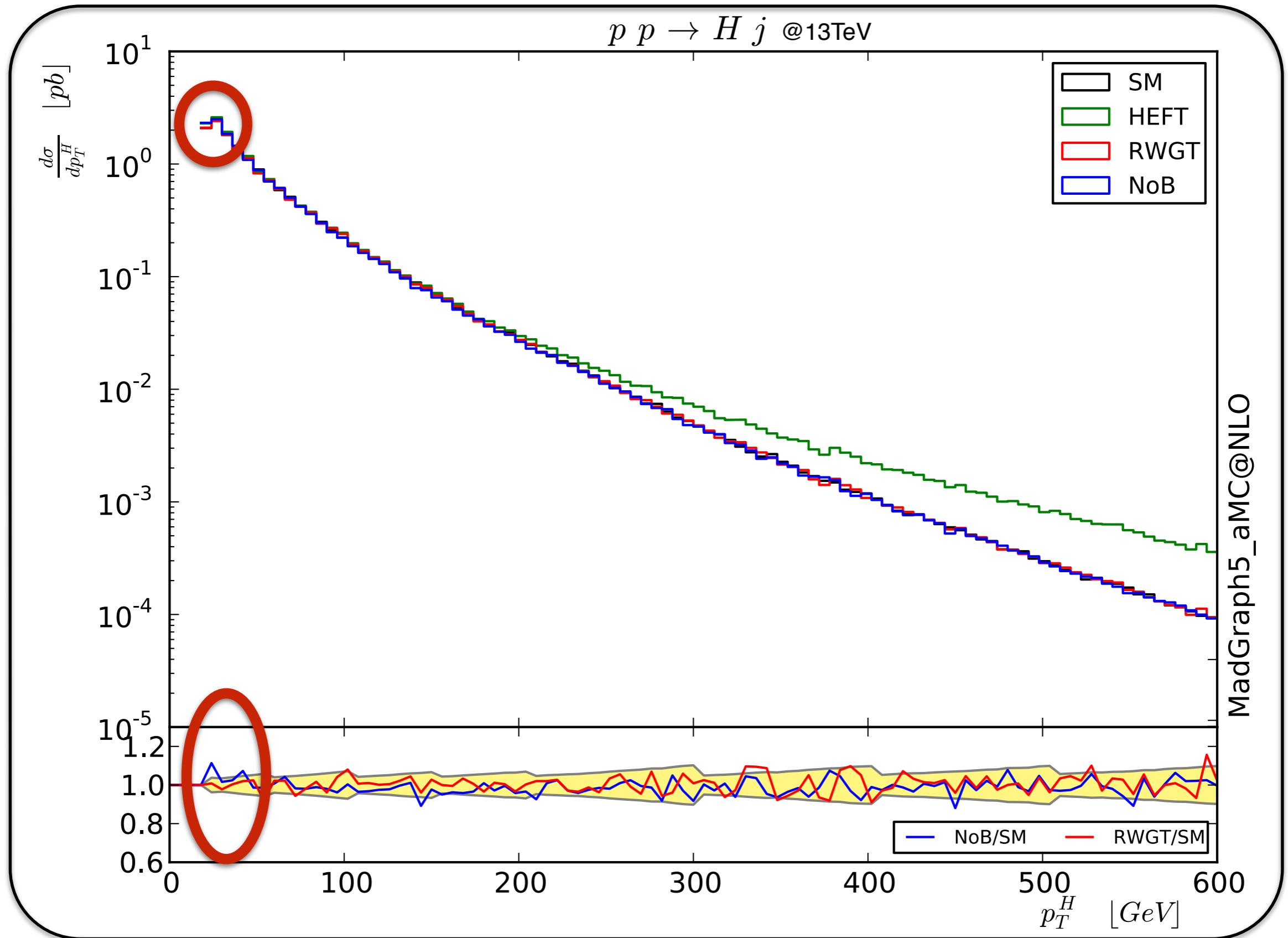
- the phase-space integration is based on the born diagram
- loop evaluation are extremely slow
- need Leading Color information for writing Events associated to the loop

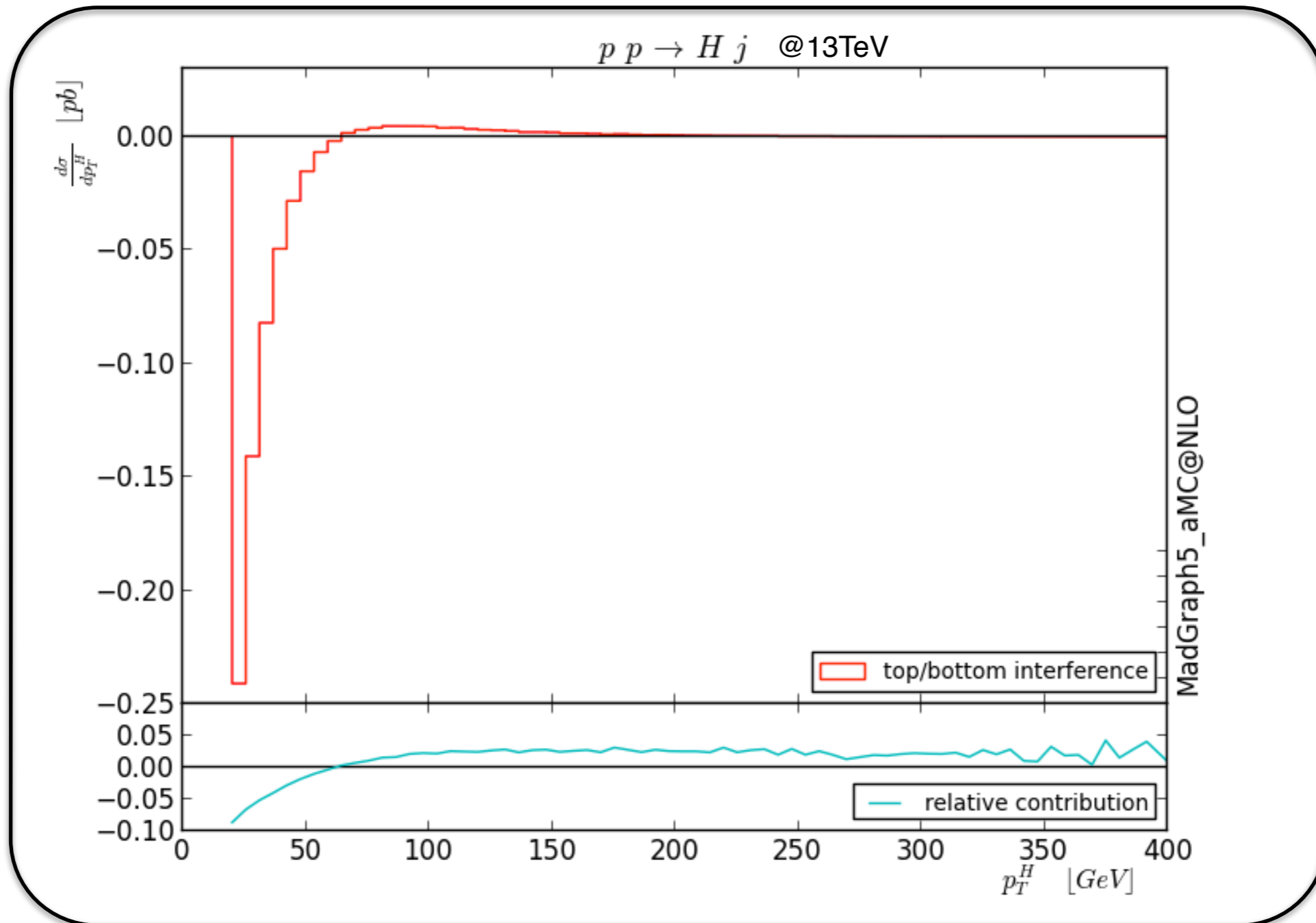
Difficulties?

- the phase-space integration is based on the born diagram
- loop evaluation are extremely slow
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Our Solution

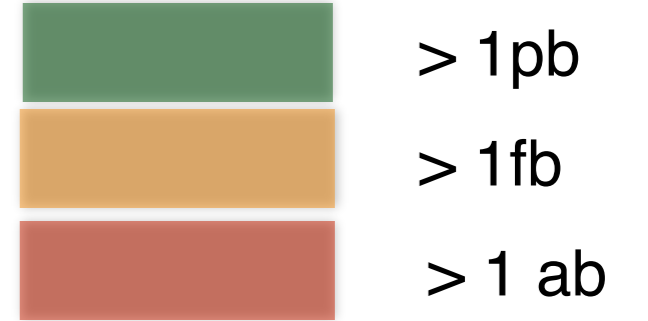
- contract the loop to have tree-level diagrams which drive the integration multi-channel
- use Monte-Carlo over helicity
- compute the loop with the color flow algebra
- increase parallelisation

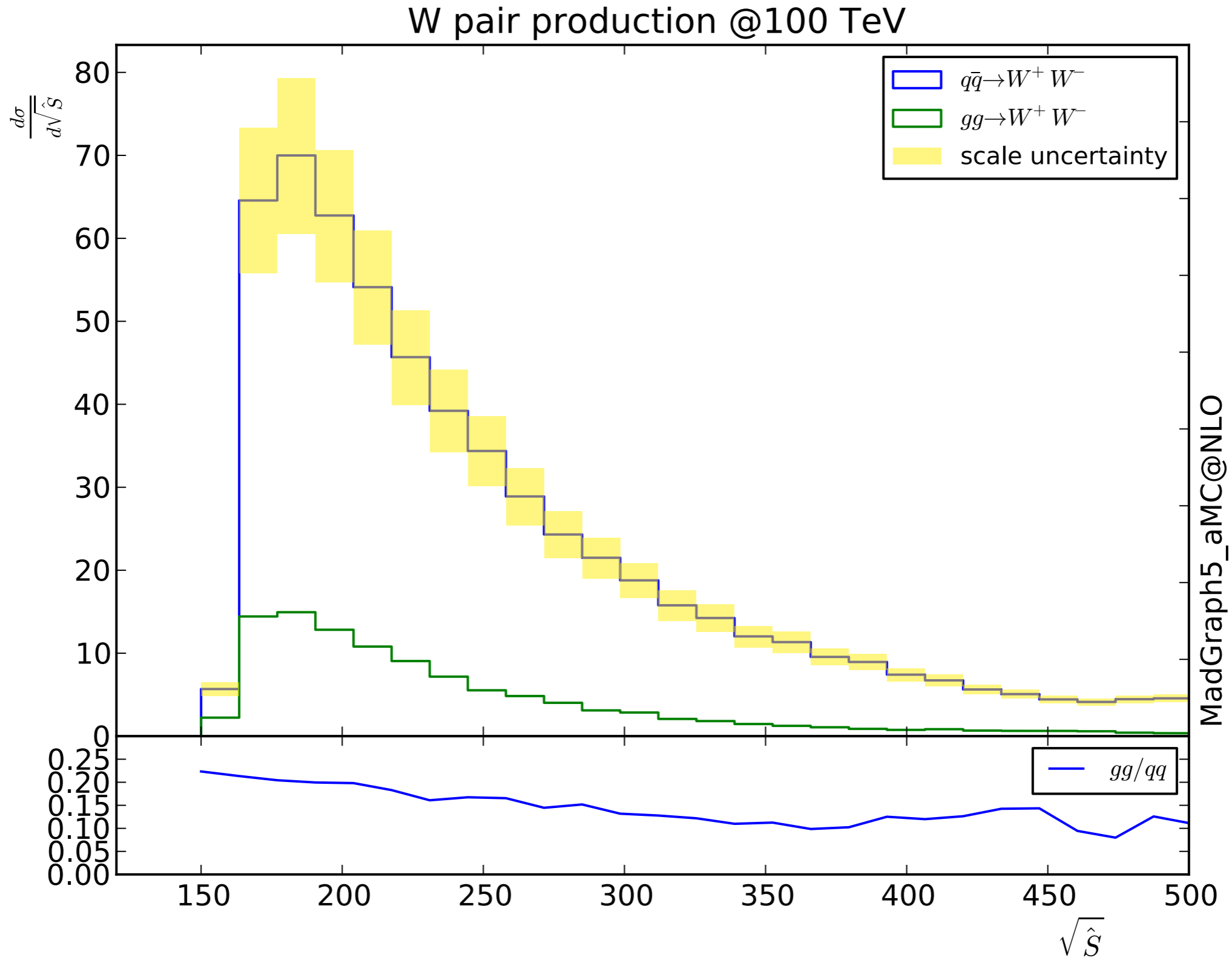




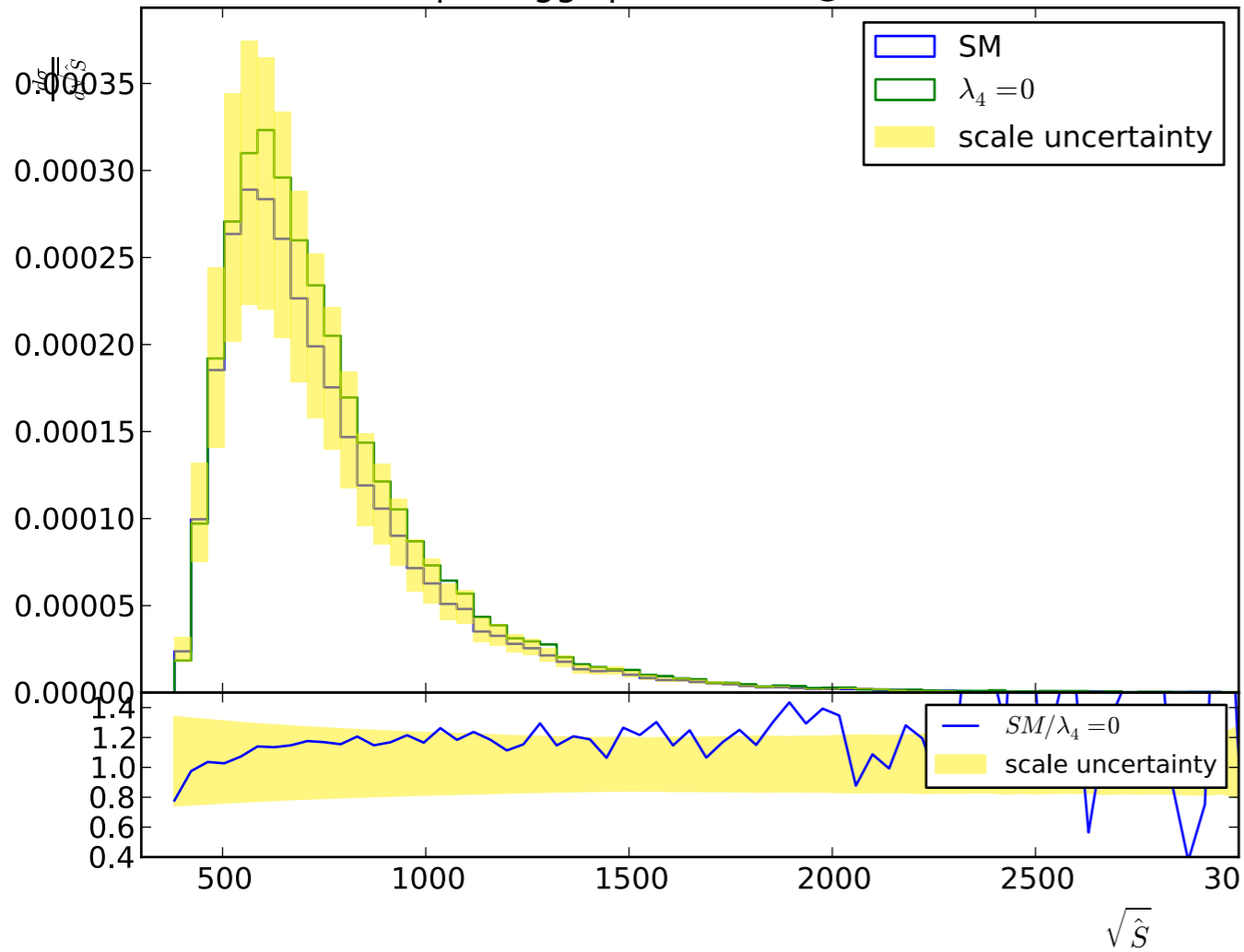
- b effect only important at low pt
- at large pt, this is just a re-scaling

Loop Induced Process	$\sigma_{\text{NLO}}(8 \text{ TeV})$ [fb]	$\sigma_{\text{NLO}}(100 \text{ TeV})$ [fb]	ρ
$gg \rightarrow H$	$6.85 \cdot 10^3$ $\begin{matrix} +33\% & +1\% \\ -24\% & -1\% \end{matrix}$	$2.21 \cdot 10^5$ $\begin{matrix} +58\% & +1\% \\ -39\% & -1\% \end{matrix}$	32
$pp \rightarrow Hjj$	$1.89 \cdot 10^3$ $\begin{matrix} +67\% & +1\% \\ -37\% & -1\% \end{matrix}$	$2.02 \cdot 10^5$ $\begin{matrix} +66\% & +0\% \\ -38\% & -1\% \end{matrix}$	107
$gg \rightarrow HZ$	22.9 $\begin{matrix} +33\% & +1\% \\ -23\% & -2\% \end{matrix}$	$2.50 \cdot 10^3$ $\begin{matrix} +35\% & +1\% \\ -26\% & -1\% \end{matrix}$	109
$gg \rightarrow HW^+W^-$	$8.28 \cdot 10^{-2}$ $\begin{matrix} +38\% & -13\% \\ -26\% & -16\% \end{matrix}$	16.8 $\begin{matrix} +31\% & +8\% \\ -23\% & +6\% \end{matrix}$	203
$gg \rightarrow HZ\gamma$	$2.12 \cdot 10^{-3}$ $\begin{matrix} +34\% & +1\% \\ -23\% & -2\% \end{matrix}$	0.279 $\begin{matrix} +33\% & +0\% \\ -25\% & -1\% \end{matrix}$	132
$gg \rightarrow HH$	5.46 $\begin{matrix} +34\% & +2\% \\ -24\% & -2\% \end{matrix}$	$7.74 \cdot 10^2$ $\begin{matrix} +32\% & +0\% \\ -24\% & -1\% \end{matrix}$	142
$gg \rightarrow ZZ$	$4.93 \cdot 10^2$ $\begin{matrix} +30\% & +1\% \\ -21\% & -1\% \end{matrix}$	$2.92 \cdot 10^4$ $\begin{matrix} +42\% & +1\% \\ -30\% & -1\% \end{matrix}$	59
$gg \rightarrow Z\gamma$	$3.98 \cdot 10^2$ $\begin{matrix} +29\% & +1\% \\ -21\% & -1\% \end{matrix}$	$1.70 \cdot 10^4$ $\begin{matrix} +52\% & +1\% \\ -35\% & -1\% \end{matrix}$	43
$gg \rightarrow \gamma\gamma$	$2.54 \cdot 10^4$ $\begin{matrix} +56\% & +1\% \\ -37\% & -1\% \end{matrix}$	$4.59 \cdot 10^5$ $\begin{matrix} +89\% & +3\% \\ -50\% & -3\% \end{matrix}$	18
$gg \rightarrow W^+W^-$	$1.37 \cdot 10^3$ $\begin{matrix} +32\% & -8\% \\ -23\% & -10\% \end{matrix}$	$8.06 \cdot 10^4$ $\begin{matrix} +48\% & +31\% \\ -33\% & +29\% \end{matrix}$	59
$gg \rightarrow HZZ$	$3.56 \cdot 10^{-2}$ $\begin{matrix} +35\% & +2\% \\ -24\% & -2\% \end{matrix}$	7.29 $\begin{matrix} +28\% & +0\% \\ -22\% & -1\% \end{matrix}$	205
$gg \rightarrow H\gamma\gamma$	$2.23 \cdot 10^{-3}$ $\begin{matrix} +38\% & -13\% \\ -26\% & -16\% \end{matrix}$	0.374 $\begin{matrix} +33\% & +10\% \\ -25\% & +9\% \end{matrix}$	167
$gg \rightarrow W^+W^-Z$	2.82 $\begin{matrix} +38\% & -13\% \\ -26\% & -16\% \end{matrix}$	$4.72 \cdot 10^2$ $\begin{matrix} -100\% & +0\% \\ -100\% & +0\% \end{matrix}$	167
$gg \rightarrow Z\gamma\gamma$	$5.58 \cdot 10^{-2}$ $\begin{matrix} +28\% & +1\% \\ -21\% & -1\% \end{matrix}$	3.42 $\begin{matrix} +44\% & +1\% \\ -31\% & -1\% \end{matrix}$	61
$gg \rightarrow \gamma ZZ$	$1.13 \cdot 10^{-3}$ $\begin{matrix} +33\% & +1\% \\ -23\% & -2\% \end{matrix}$	0.13 $\begin{matrix} +34\% & +1\% \\ -25\% & -1\% \end{matrix}$	115
$gg \rightarrow HHH$	$1.16 \cdot 10^{-2}$ $\begin{matrix} +39\% & -14\% \\ -26\% & -17\% \end{matrix}$	2.99 $\begin{matrix} +29\% & +5\% \\ -22\% & +4\% \end{matrix}$	258
$gg \rightarrow HHHH$	$2.63 \cdot 10^{-5}$ $\begin{matrix} +39\% & +3\% \\ -26\% & -3\% \end{matrix}$	$1.30 \cdot 10^{-2}$ $\begin{matrix} +23\% & +1\% \\ -18\% & -1\% \end{matrix}$	494
$gg \rightarrow HHZ$	$1.60 \cdot 10^{-2}$ $\begin{matrix} +36\% & +2\% \\ -24\% & -2\% \end{matrix}$	3.35 $\begin{matrix} +29\% & +0\% \\ -22\% & -1\% \end{matrix}$	209

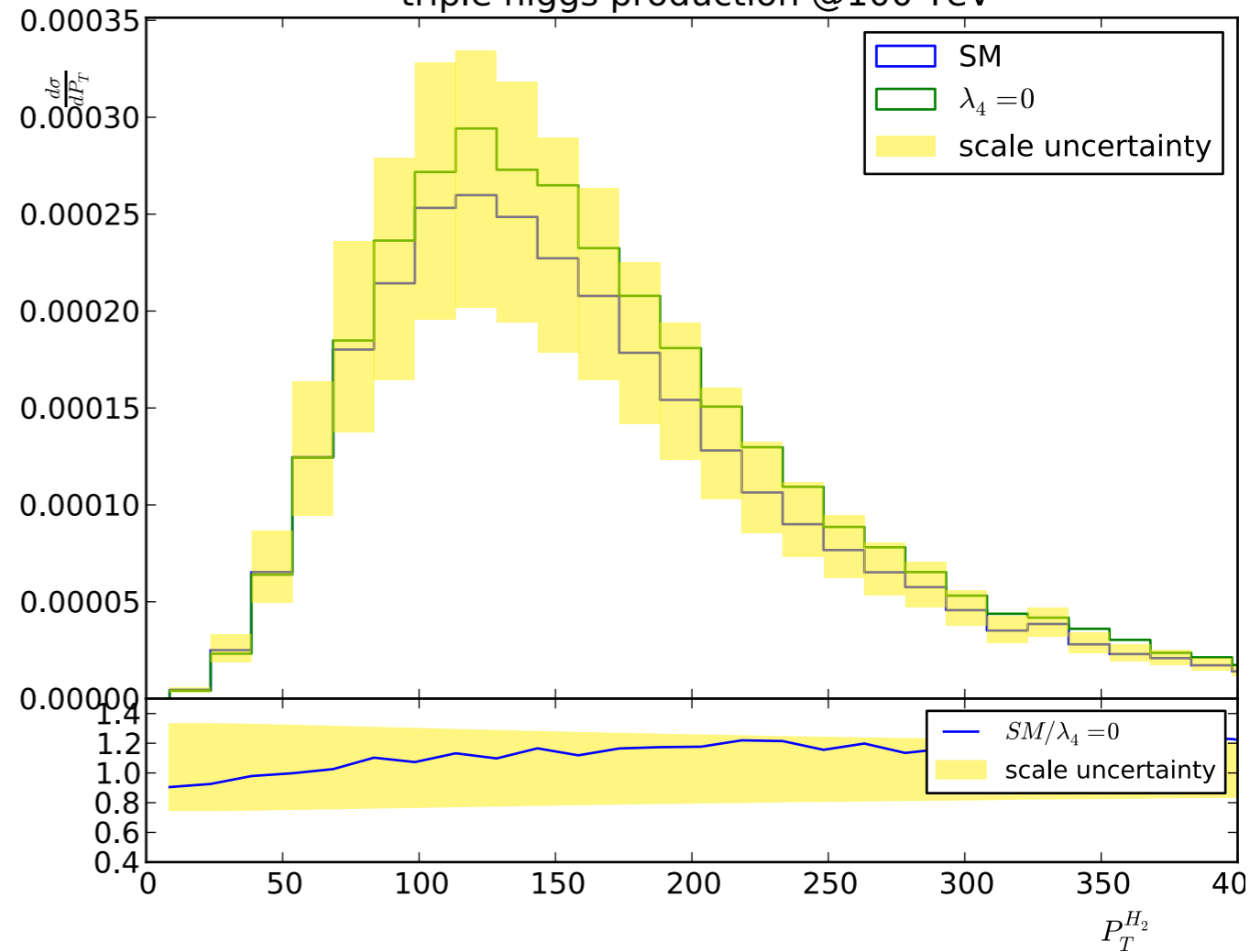




triple higgs production @100 TeV



triple higgs production @100 TeV



- cross-section @NLO for 100TeV collision
 - Huge enhancement of rare processes at 100TeV compare to 8/13 TeV
- cross-section for loop-induced process @LO
 - Huge enhancement as well