

Study of hh production in the WWbb channel at the FCC-hh

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Motivation: probing the Higgs potential

Very well known (LEP, Flavour factories, Tevatron, LHC)

$$\mathcal{L} = -\frac{1}{4g'^4} B_{\mu\nu} B^{\mu\nu} - \frac{1}{4g^2} W_{\mu\nu}^a W^{\mu\nu a} - \frac{1}{4g_s^2} G_{\mu\nu}^a G^{\mu\nu a} + \bar{Q}_i i \not{D} Q_i + \bar{u}_i i \not{D} u_i + \bar{d}_i i \not{D} d_i + \bar{L}_i i \not{D} L_i + \left(Y_u^{ij} \bar{Q}_i u_j \tilde{H} + Y_d^{ij} \bar{Q}_i d_j H + Y_l^{ij} \bar{L}_i \ell_j H + c.c. \right) - \lambda (H^\dagger H)^2 + \lambda v^2 H^\dagger H - (D^\mu H)^\dagger D_\mu H - (D^\mu H)^\dagger D_\mu H \rightarrow -(\partial^\mu H)^\dagger \partial_\mu H - 2 \frac{M_W^2}{v} W^{+\mu} W_\mu^- H - \frac{M_Z^2}{v} Z^\mu Z_\mu H + \dots$$

almost known (LHC)

unknown

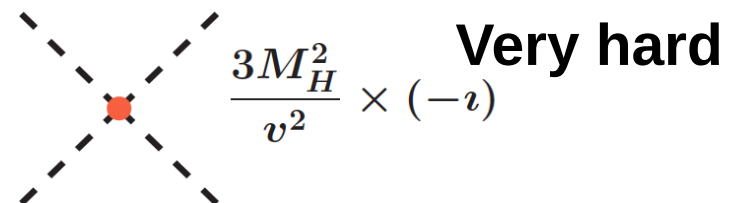
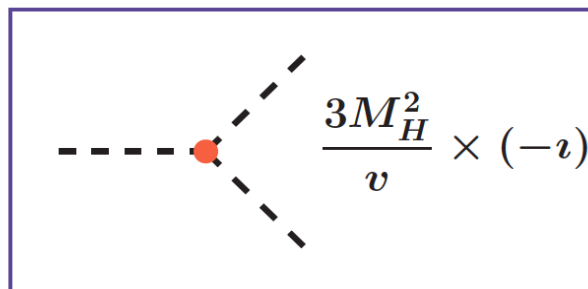
very well known

well known (LHC)

The last missing piece of our (Standard) theory of nature

$$V(H) = \frac{1}{2} M_H^2 H^2 + \frac{1}{2} \frac{M_H^2}{v} H^3 + \frac{1}{8} \frac{M_H^2}{v^2} H^4 + \text{constant}$$

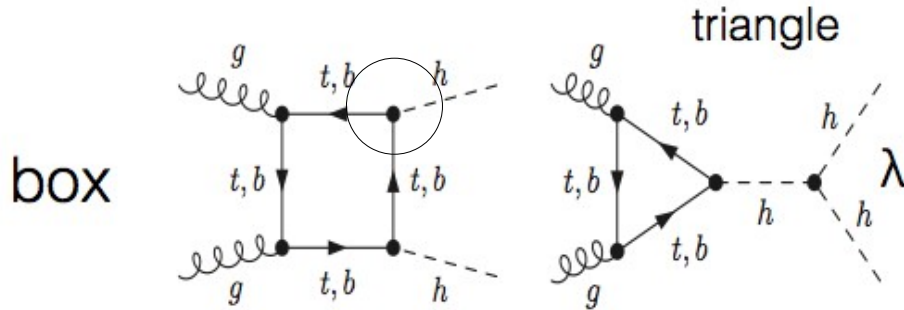
Possible
At FCC



Very hard

hh Production mechanism

~ x 40 at 100 TeV wrt to 14 TeV



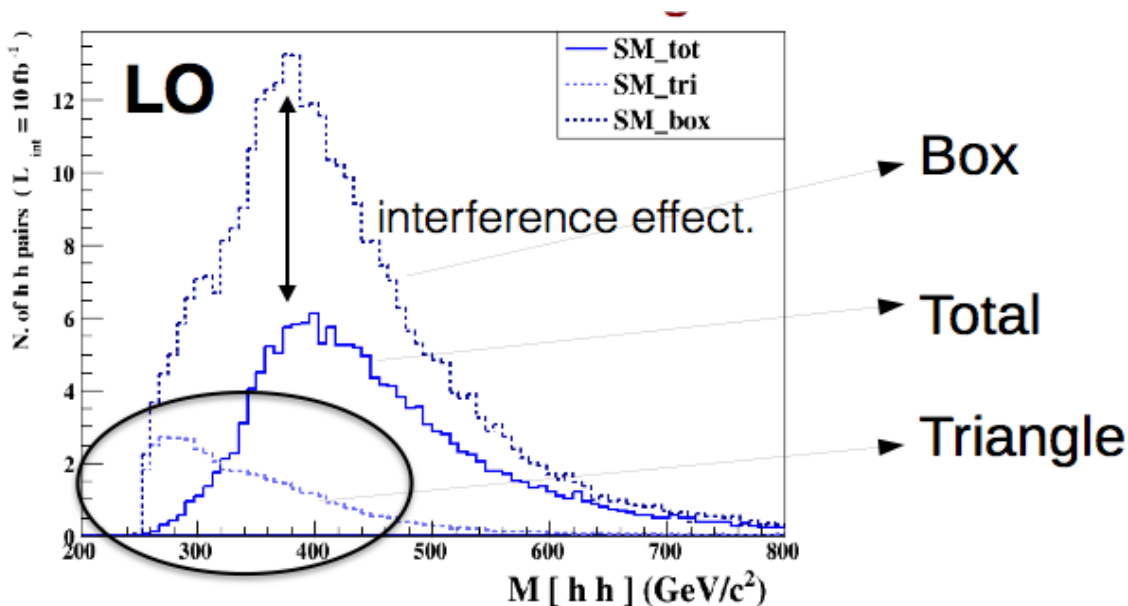
box

triangle

less interesting:
tth, bbh coupling

Interesting:
self-coupling

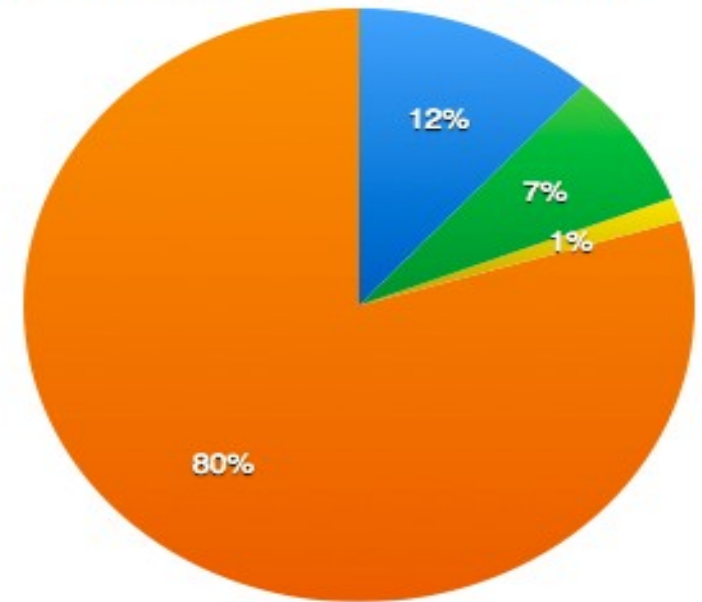
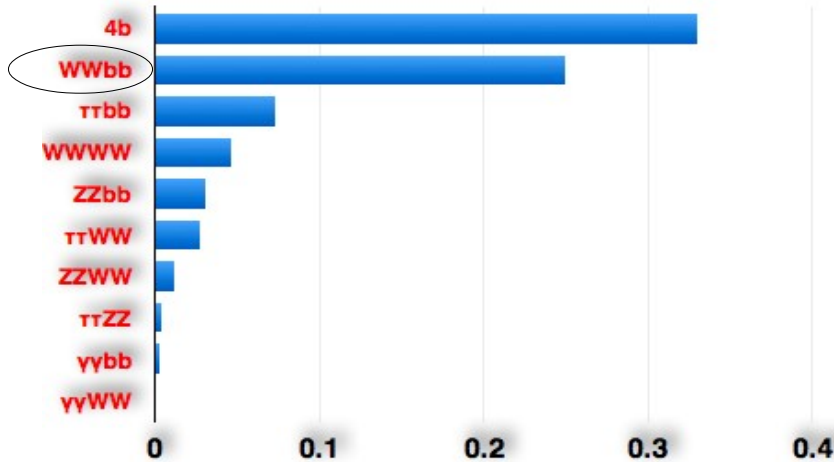
\sqrt{s} [TeV]	σ^{NLO} [fb]
8	8.2
14	33.9
33	207.3
100	1417.8



- Triangle mainly contributing to very low m_{hh} ,
- but moderate m_{hh} can be sensitive through interference with top-box.

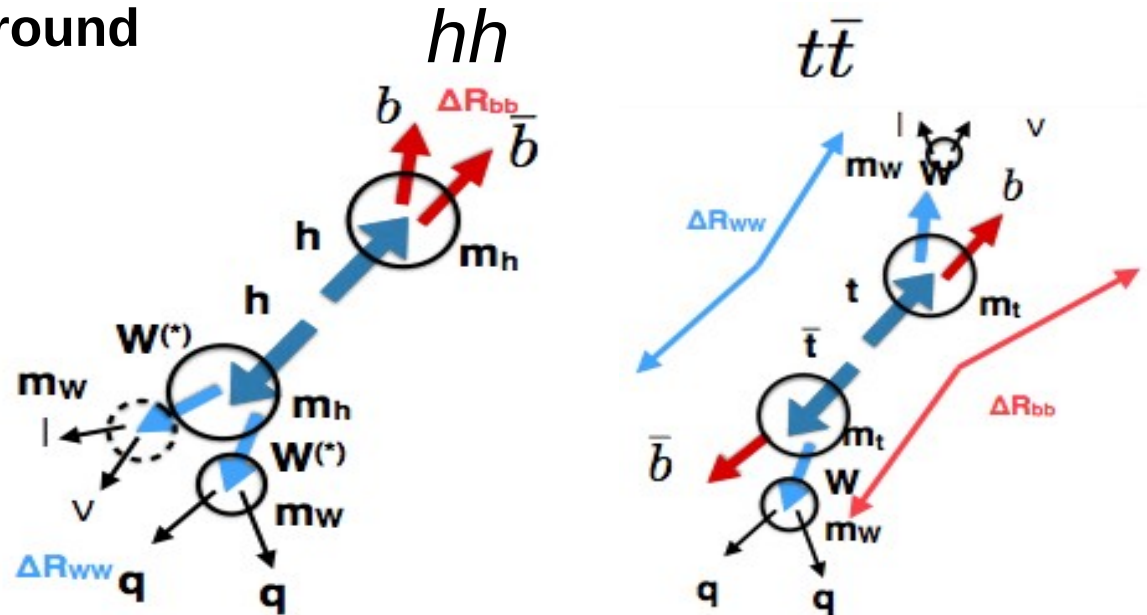
hh decays

● $hh \rightarrow WWbb \rightarrow 4jbb$ ● $hh \rightarrow WWbb \rightarrow lvjjbb$
● $hh \rightarrow WWbb \rightarrow lvlvbb$ ● $hh \rightarrow \text{others}$



- **BR $lvjj bb$** ~ 7% of the total
- **4j channel** also interesting to exploit, but overwhelming QCD background

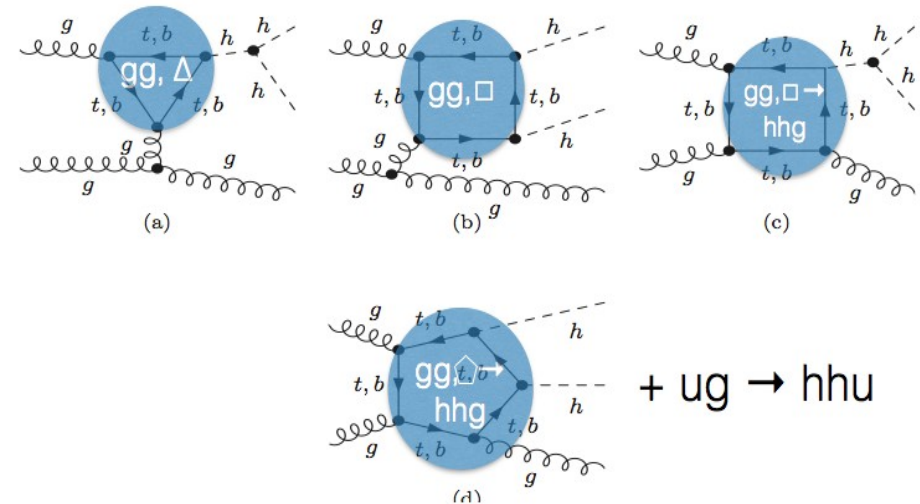
- Main background: $t\bar{t}$ with same final state
- Main discriminant variables: M_{bb} , ΔR_{bb} , ΔR_{ww}
- **Kinematics** can be **closed**
- Crucial to have good, E_T^{miss} and **jet**, p_T and angular **resolution**
- Challenging in **high pile-up** environments.



$\sigma(100 \text{ TeV}) / \sigma(14 \text{ TeV}) \sim \times 40(32)$ for HH ($t\bar{t}$)

Signal and background modeling

- **signal** events generated with Madgraph5_aMC@NLO 2.2.3 PDF CT10@NLO
- Shower: Herwig++ 2.7.1, PDF cteq6l1

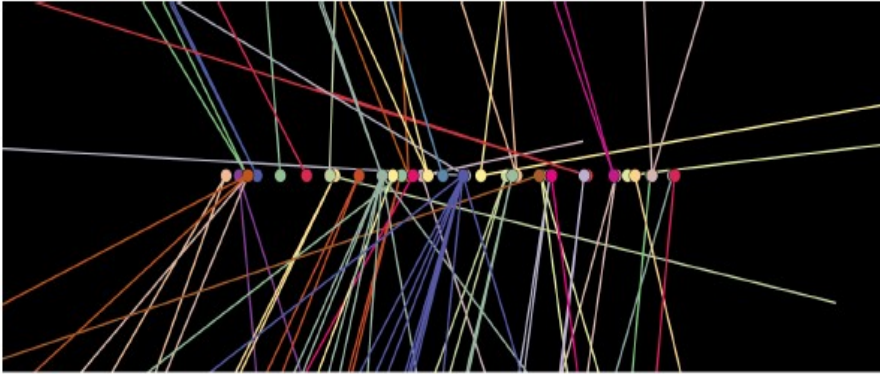


- $t\bar{t}$ background events simulated with Madgraph5_aMC@NLO,
- Decays forced to $lvjj$ using MadSpin (preserving spin correlations in the whole decay chain).
- 100k of Pile-up events simulated with Herwig++ minimum bias simulation

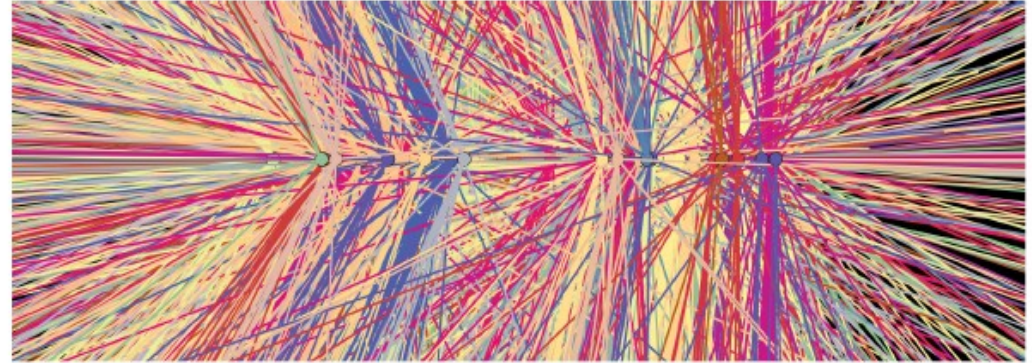
Sample	$\sigma (\pi\beta)$	$N_{\text{evts}}^{\text{gen.}}$
hh	1.4	1M
$t\bar{t}$		
$l^+ \nu \alpha \beta \beta$	$4.1 \cdot 10^3$	10M
$\tau^+ \nu \alpha \beta \beta$	$0.2 \cdot 10^3$	2M

Pile-up at FCC-hh

LHC condition



FCC-hh condition



Optimizing integrated luminosity of future hadron colliders, M. Benedikt et. al.

For bunch spacing of 25 ns

	FCC Phase 1	FCC Phase 2
Peak pileup	180	940
Peak pileup line density m^{-1}	≤ 3200	≤ 17000
rms bunch length [cm]	8	8

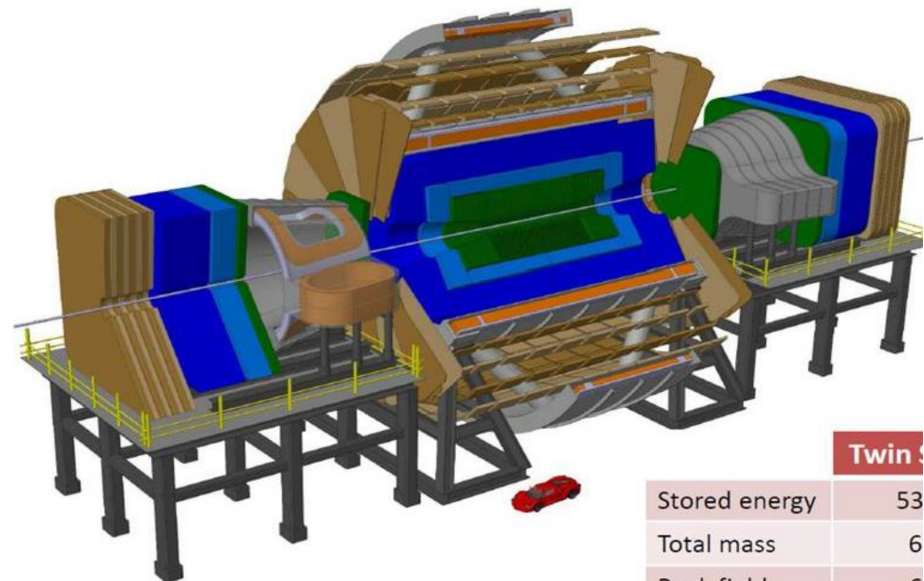
For 5 ns bunch spacing Pile-up \rightarrow Pileup / 5

Configurations chosen for this study:

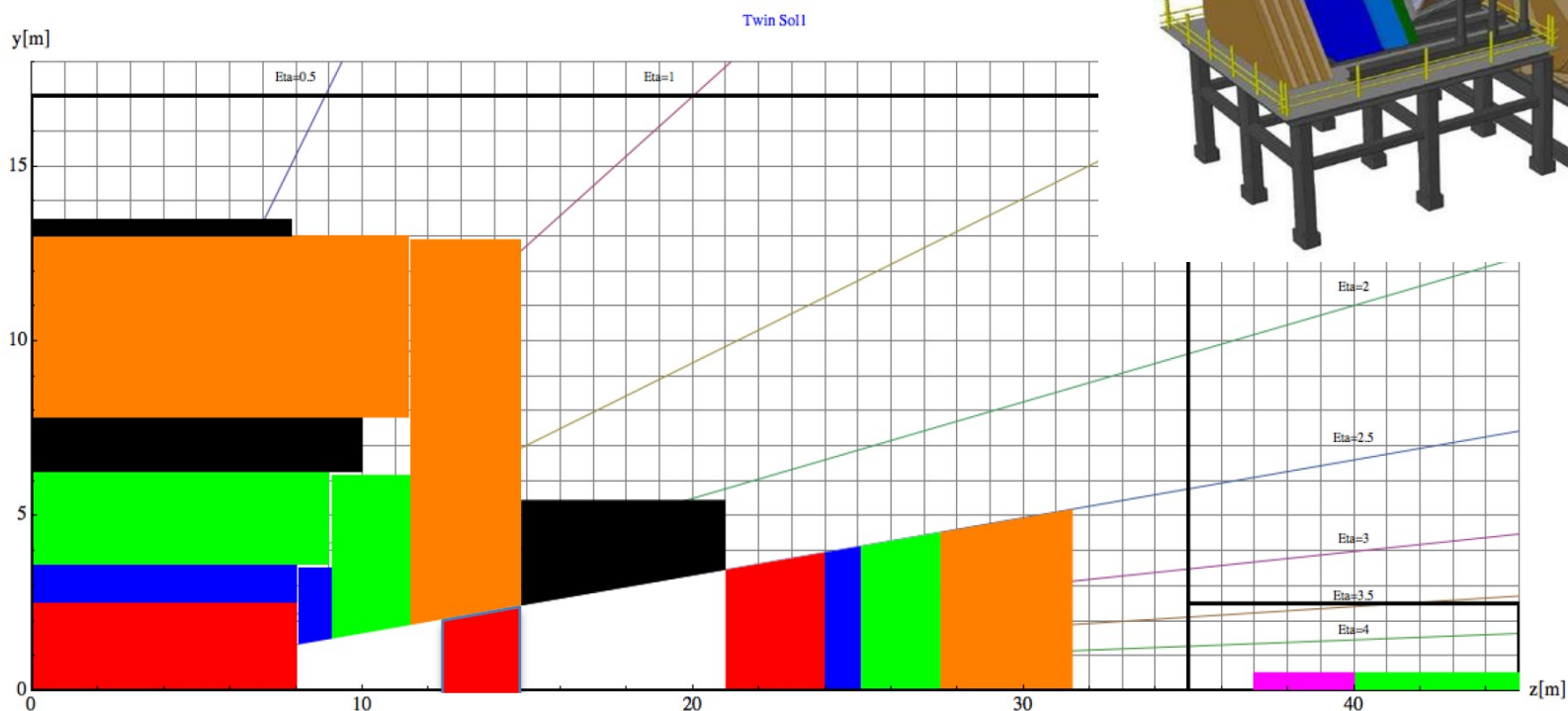
Pile-up = 50 \approx Pile-up at Phase 1 at 5 ns

Pile-up = 200 \approx Pile-up at Phase 1 at 25 ns OR Phase 2 at 5 ns

Base-line geometry Twin solenoid + Dipole magnetic system



	Twin Sol
Stored energy	53
Total mass	6
Peak field	6



Tracker

Fwd Tracker

EMCAL

Dipole

HCAL

Coil+Cryostat

Muon system

Detector Parametrization - Calorimeters

Based on Delphes card: FCChh_DelphesCard_WithDipole_v00.tcl

ECAL granularity

- 0.0125 x 0.0125 for $|\eta| < 2.5$
- 0.025 x 0.025 for $|\eta| < 4.0$
- 0.05 x 0.05 for $|\eta| < 6.0$

ECAL Energy resolution

$$\sigma E/E = 10\% / \sqrt{E} \oplus 1\%$$

HCAL granularity

- 0.05 x 0.05 for $|\eta| < 2.5$
- 0.1 x 0.1 for $|\eta| < 4.0$
- 0.2 x 0.2 for $|\eta| < 6.0$

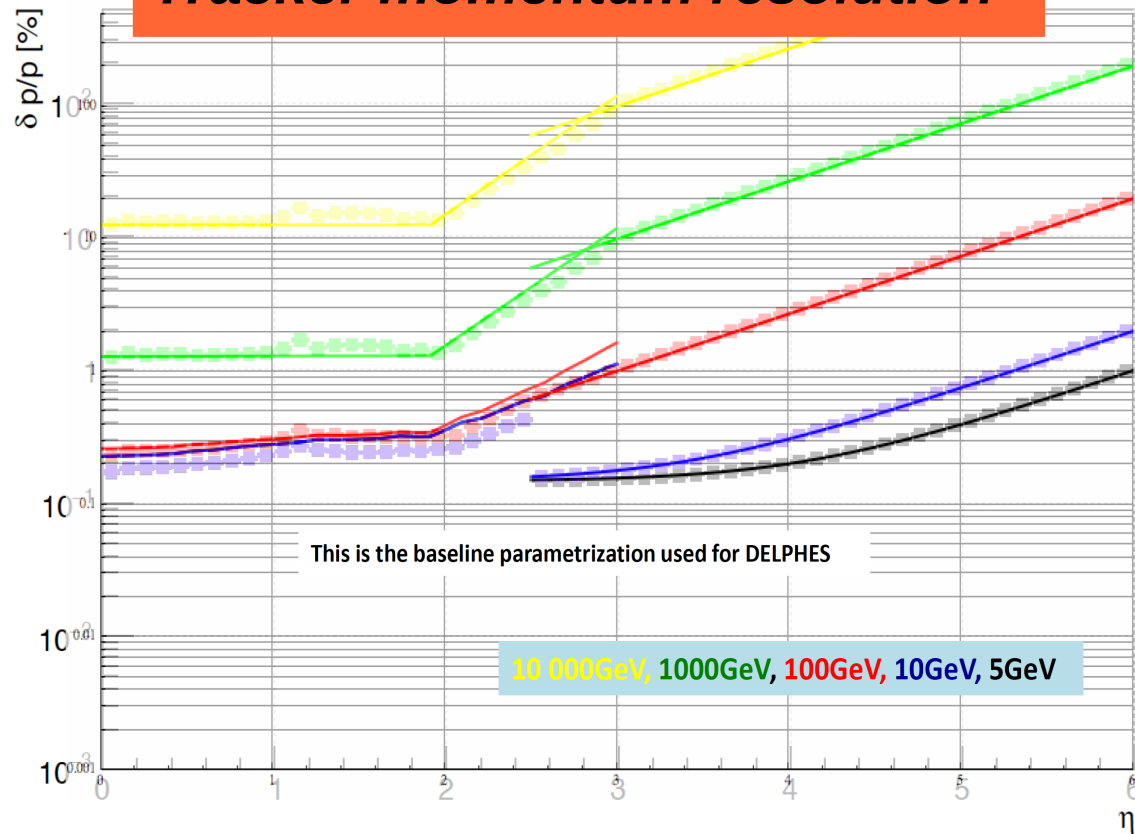
HCAL Energy resolution

- $\sigma E/E = 50\% / \sqrt{E} \oplus 3\%$ in $|\eta| < 4$
- $\sigma E/E = 100\% / \sqrt{E} \oplus 5\%$ in $4 < |\eta| < 6$

*Show only sub-detector ⁸
Most relevant for this study*

Detector Parametrization - Tracker

Tracker momentum resolution



z_0 resolution (*)

- in $|\eta| < 2.5$
 - $\sigma(z_0) = 0.01 \text{ mm}$, $p_T < 5 \text{ GeV}$
 - $\sigma(z_0) = 0.005 \text{ mm}$, $p_T > 5 \text{ GeV}$
- In $2.5 < |\eta| < 4$
 - $\sigma(z_0) = 0.1 \text{ mm}$, $p_T < 5 \text{ GeV}$
 - $\sigma(z_0) = 0.05 \text{ mm}$, $p_T > 5 \text{ GeV}$
- In $4.0 < |\eta| < 6.0$
 - $\sigma(z_0) = 1.0 \text{ mm}$, $p_T < 5 \text{ GeV}$
 - $\sigma(z_0) = 0.5 \text{ mm}$, $p_T > 5 \text{ GeV}$

* in official card

z_0 resolution constant

for $|\eta| < 2.5$ for all η

B-tagging

Efficiency for light jets	0.1 %
Efficiency for c-quark jets	4%
Efficiency for b-quark jets	75%

Caveat: same parametrization used for Pile-up 50 and 200⁹

Reconstruction

■ Particle Flow Reconstruction:

Using charged hadrons, muons and electrons to build

particles flow objects =

Tracks & Calorimeter deposit – charged deposit

- Tracks from Pileup are rejected if $|z_0 - z_{PV}| > \sqrt{\sigma^2(z_0) + \sigma^2(z_{PV})}$

■ Jets

- Anti-Kt (FastJet) JetAlgorithm
- Particle-flow objects as inputs
- cone 0.4
- Jet Area pile-up correction:

$$p_{T, \text{jet, corrected}} = p_{T, \text{jet, raw}} - \rho \cdot \text{Area}_{\text{jet}}$$

- *Private* calibration to the particle level:

- Evaluate $\langle p_{T, \text{reco jet}} / p_{T, \text{true jet}} \rangle$ vs $p_{T, \text{reco jet}}, \eta_{\text{reco jet}}$

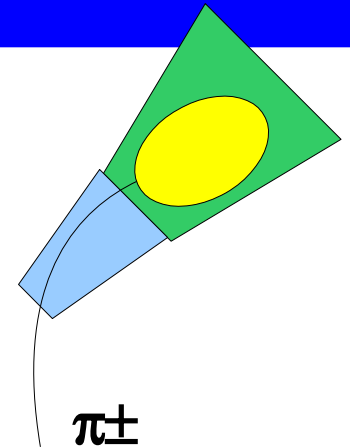
- Numeral inversion scale:

$$p_{T, \text{reco jet calibrated}} = f(\langle p_{T, \text{reco jet}} / p_{T, \text{true jet}} \rangle, p_{T, \text{reco jet}}, \eta_{\text{reco jet}}, p_T)$$

- $p_{T, \text{reco jet calibrated}} > 20 \text{ GeV}$

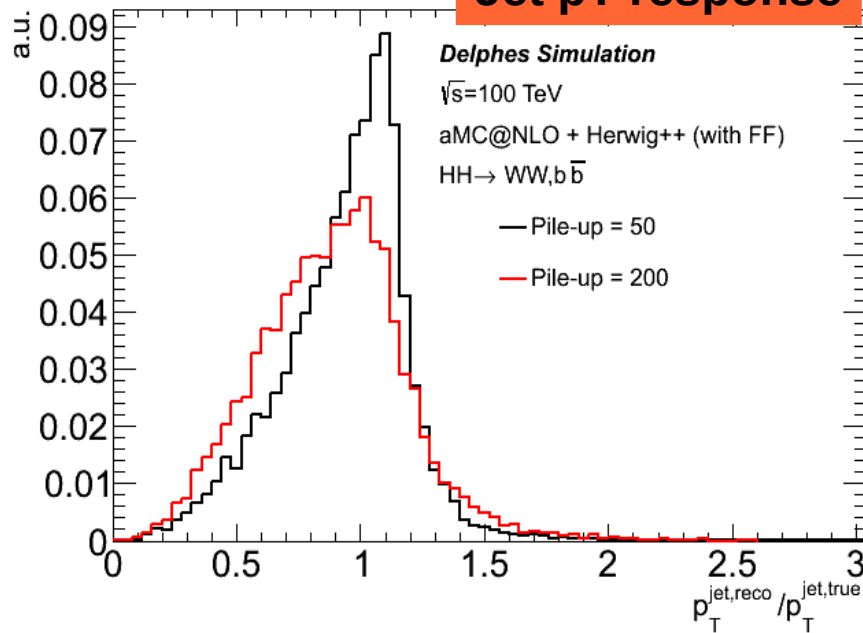
■ Missing Transverse Energy:

Negative vector sum of Jets, after pile-up correction and calibration



Reconstruction Performances of Jets and MET

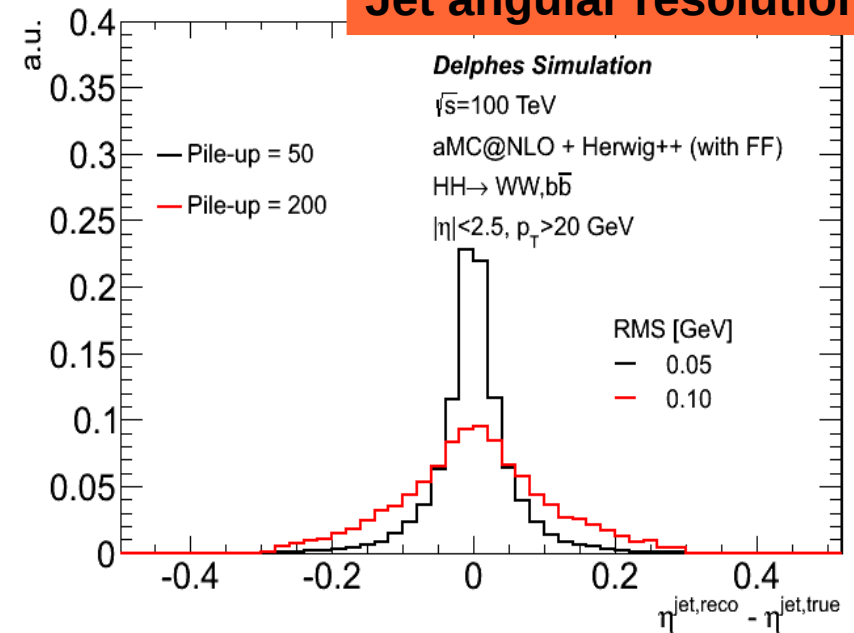
Jet p_T response



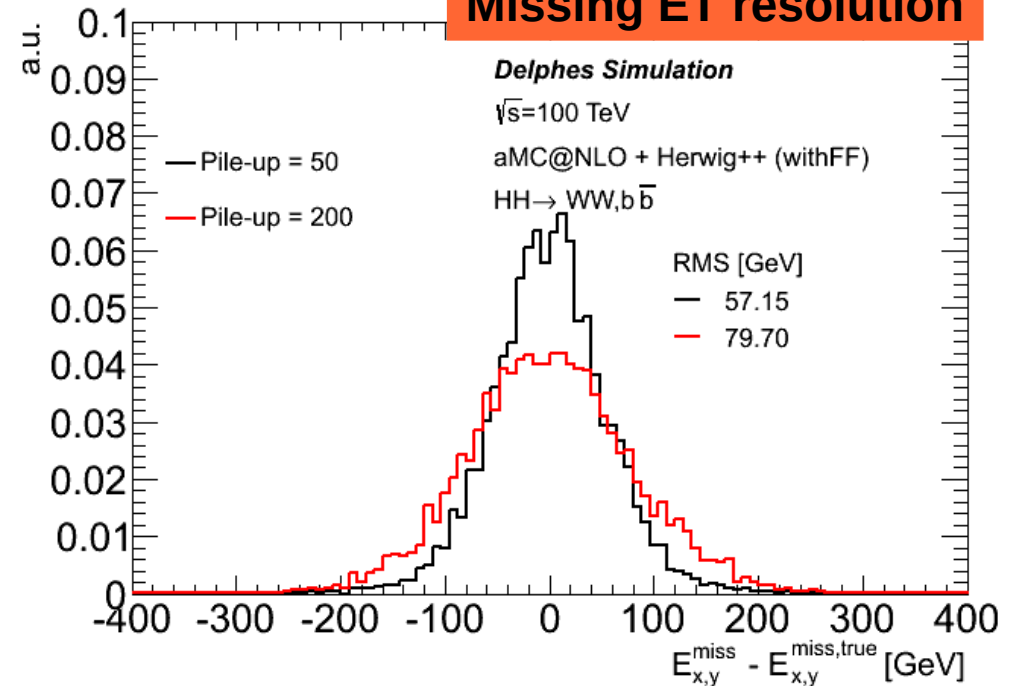
Clear deterioration from
Pileup = 50 to **200**

As exercise also tested PU=900
(computing very expensive)...

Jet angular resolution

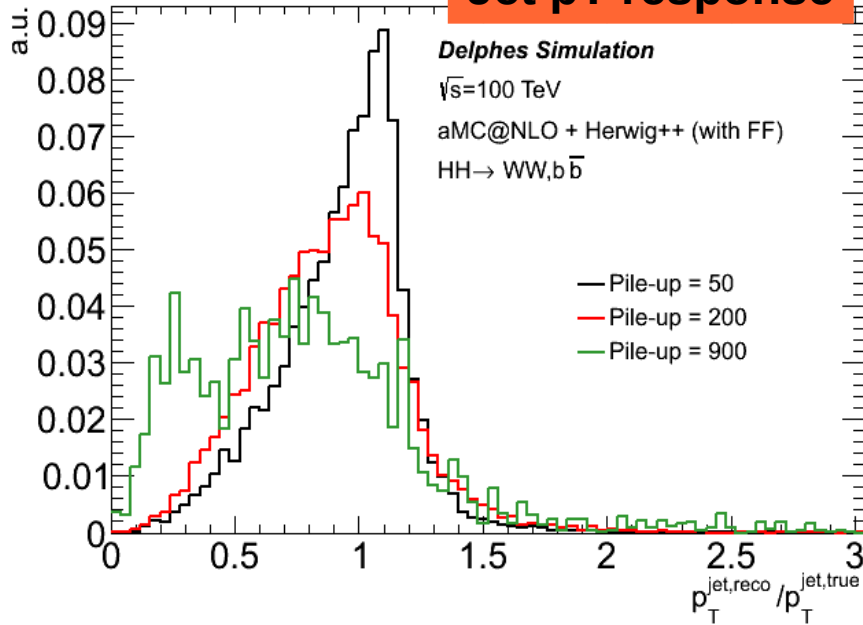


Missing ET resolution



Reconstruction Performances of Jets and MET

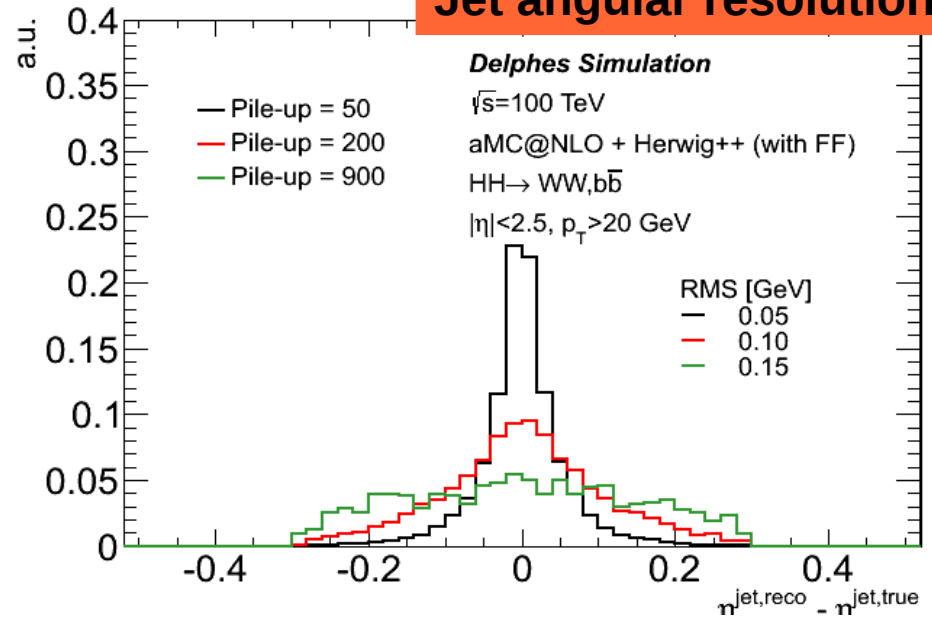
Jet p_T response



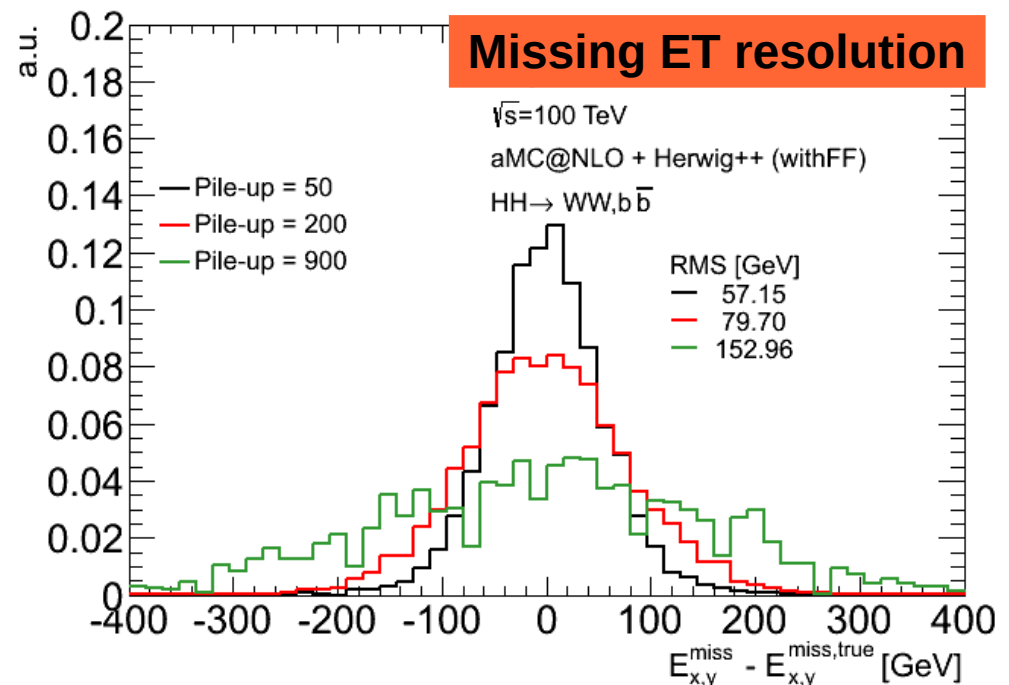
Clear deterioration from
Pileup = 50 to **200**

As exercise also tested **PU=900**
(computing very expensive)...

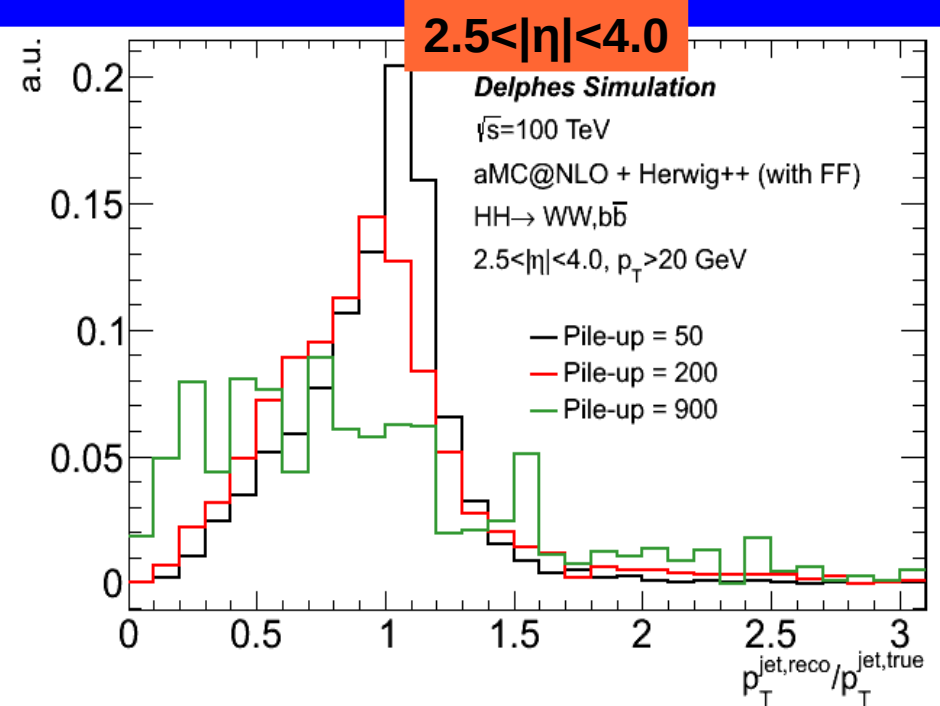
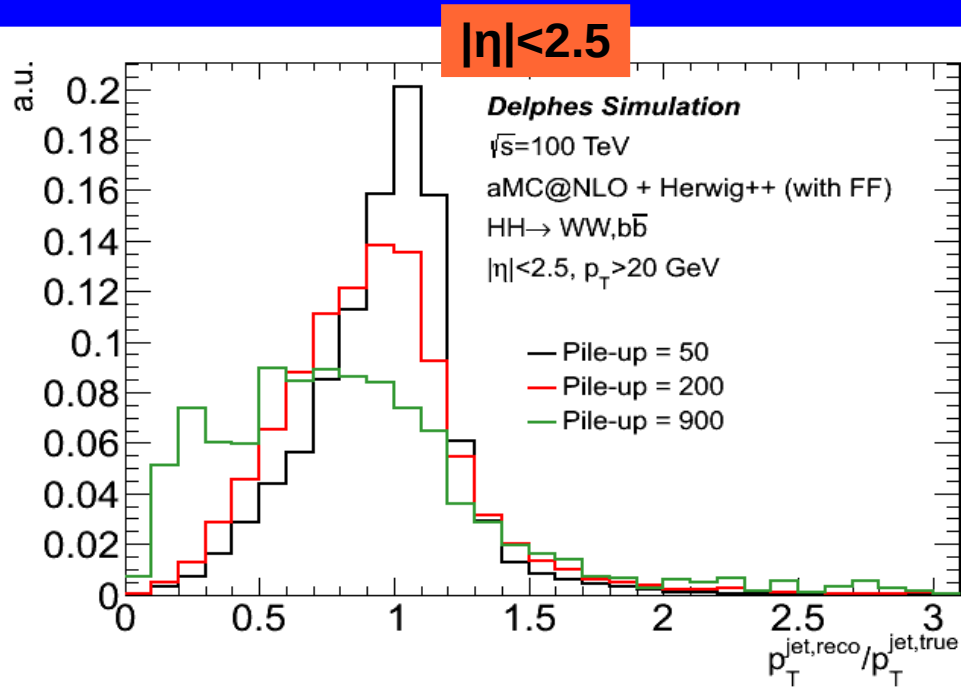
Jet angular resolution



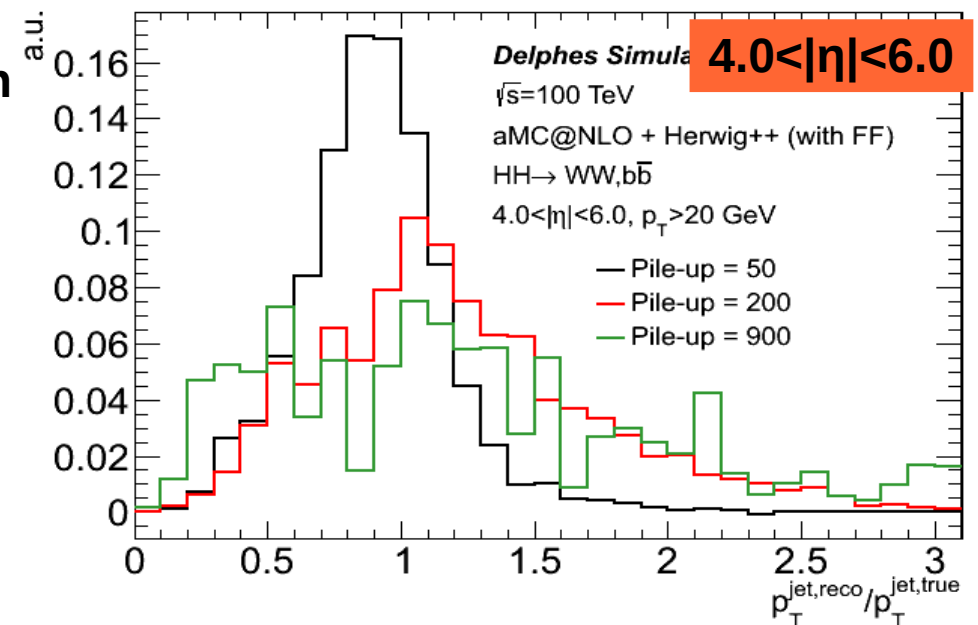
Missing ET resolution



Reconstruction Performances of Jets: η dependence

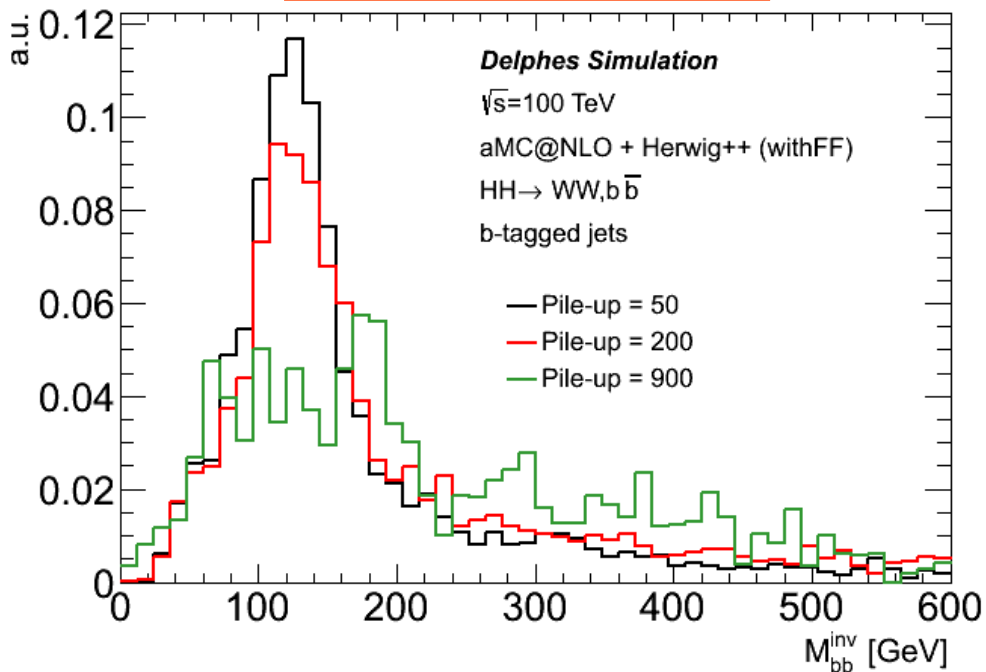


- Deterioration of jet response resolution with increasing η
- Expected due to higher pile-up signals

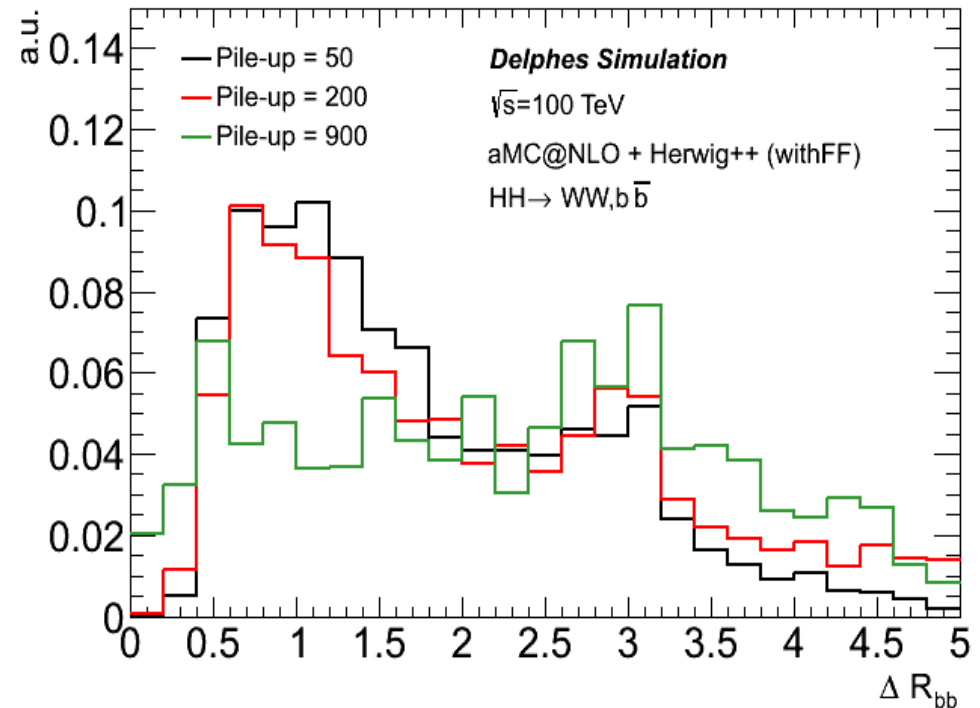


Discriminant variables at various pile-up

Mbb invariant mass



Rbb invariant mass



Clear deterioration from
Pileup = 50 to **200**
Pile-up = **900** seems very difficult

Detector parameter variations: Calorimeter resolution

- Constant term driven by requirement on Multi-TeV physics
- Here stochastic term is varied
 - Factor 2 Up and Down, HCal only Down

Nominal Calorimeter Resolution

ECAL Energy resolution
 $\sigma E/E = 10\% / \sqrt{E} \oplus 1\%$

HCal Energy resolution

- $\sigma E/E = 50\% / \sqrt{E} \oplus 3\%$ in $|\eta| < 4$
- $\sigma E/E = 100\% / \sqrt{E} \oplus 5\%$ in $4 < |\eta| < 6$

Calorimeter Resolution “Up”

ECAL Energy resolution
 $\sigma E/E = 20\% / \sqrt{E} \oplus 1\%$

HCal Energy resolution

- $\sigma E/E = 50\% / \sqrt{E} \oplus 3\%$ in $|\eta| < 4$
- $\sigma E/E = 100\% / \sqrt{E} \oplus 5\%$ in $4 < |\eta| < 6$

Calorimeter Resolution “Down”

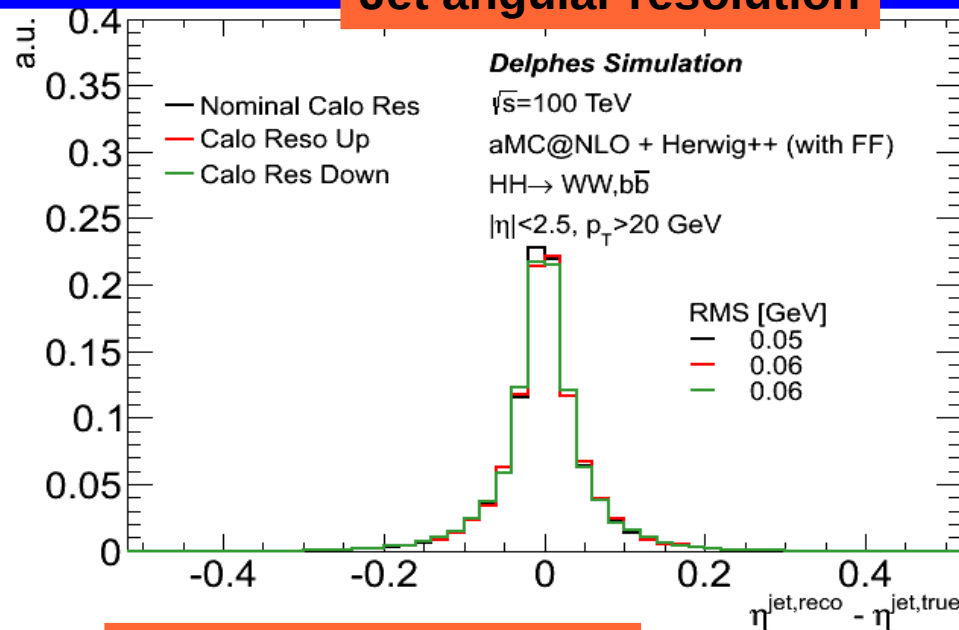
ECAL Energy resolution
 $\sigma E/E = 5\% / \sqrt{E} \oplus 1\%$

HCal Energy resolution

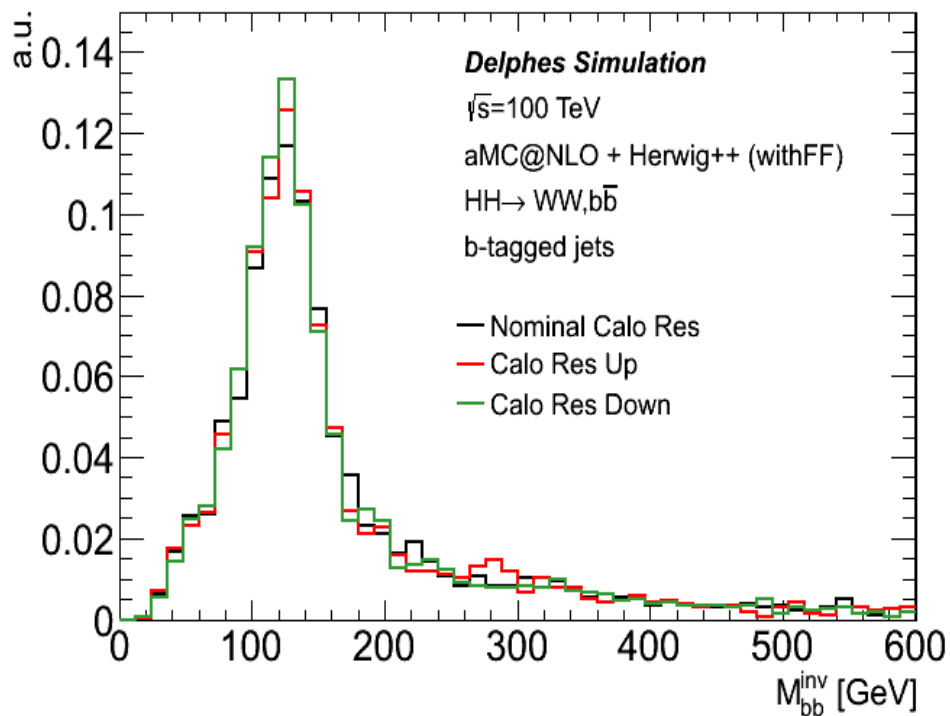
- $\sigma E/E = 25\% / \sqrt{E} \oplus 3\%$ in $|\eta| < 4$
- $\sigma E/E = 50\% / \sqrt{E} \oplus 5\%$ in $4 < |\eta| < 6$

Detector parameter variations: Calorimeter resolution

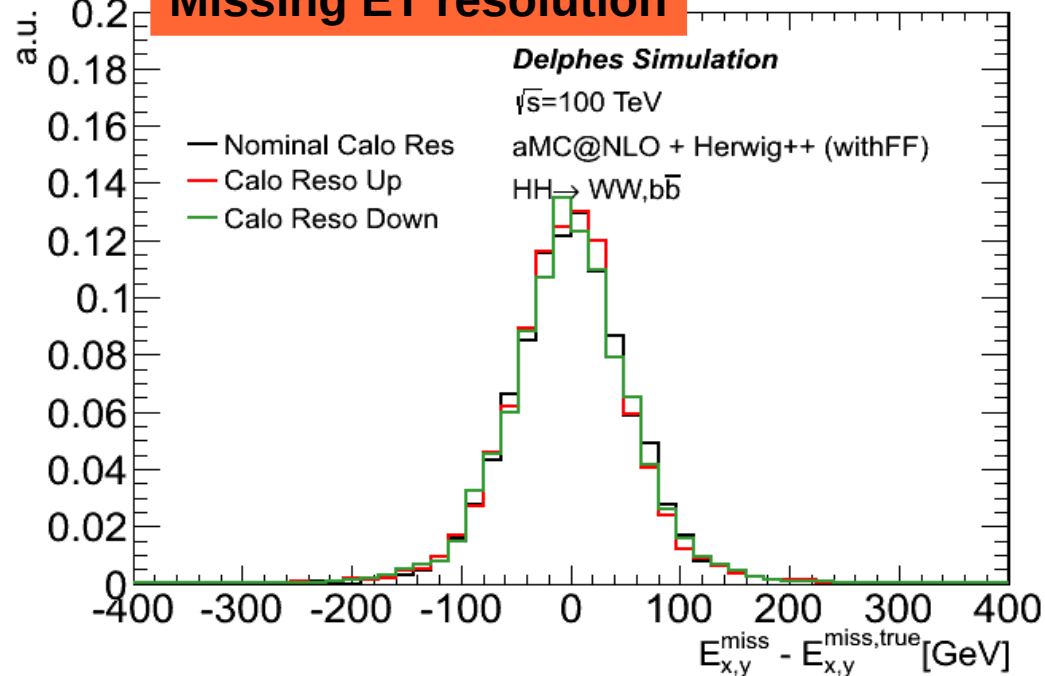
Jet angular resolution



Mbb invariant mass



Missing ET resolution



- Pile-up = 50 used
- Very small differences
- Effects likely washed-out by pileup

Detector parameter variations: z_0 resolution

- Tracks from Pileup are rejected if $|z_0 - z_{PV}| > \sqrt{\sigma^2(z_0) + \sigma^2(z_{PV})}$
- Expect effects on resolution of jets and Missing Transverse energy due to enhanced pile-up contributions
- Compare our choice = z_0 resolution dependent on η
vs official card = z_0 resolution constant on η

z_0 resolution

- in $|\eta| < 2.5$

$$\sigma(z_0) = 0.01 \text{ mm}, p_T < 5 \text{ GeV}$$

$$\sigma(z_0) = 0.005 \text{ mm}, p_T > 5 \text{ GeV}$$

- In $2.5 < |\eta| < 4$

$$\sigma(z_0) = 0.1 \text{ mm}, p_T < 5 \text{ GeV}$$

$$\sigma(z_0) = 0.05 \text{ mm}, p_T > 5 \text{ GeV}$$

- In $4.0 < |\eta| < 6.0$

$$\sigma(z_0) = 1.0 \text{ mm}, p_T < 5 \text{ GeV}$$

$$\sigma(z_0) = 0.5 \text{ mm}, p_T > 5 \text{ GeV}$$

z_0 resolution

$$\sigma(z_0) = 0.01 \text{ mm}, p_T < 5 \text{ GeV}$$

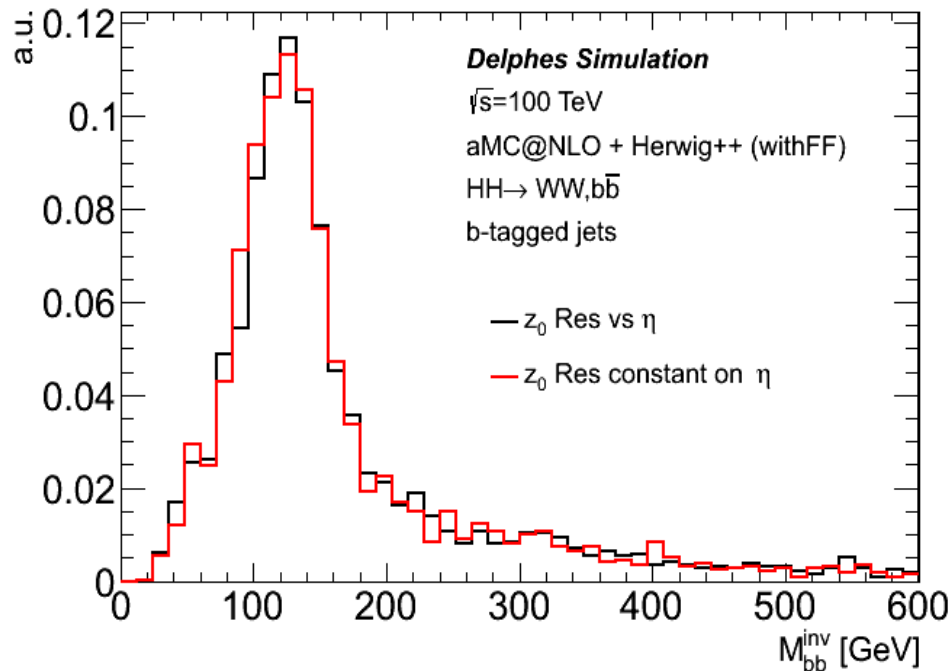
$$\sigma(z_0) = 0.005 \text{ mm}, p_T > 5 \text{ GeV}$$

For all η

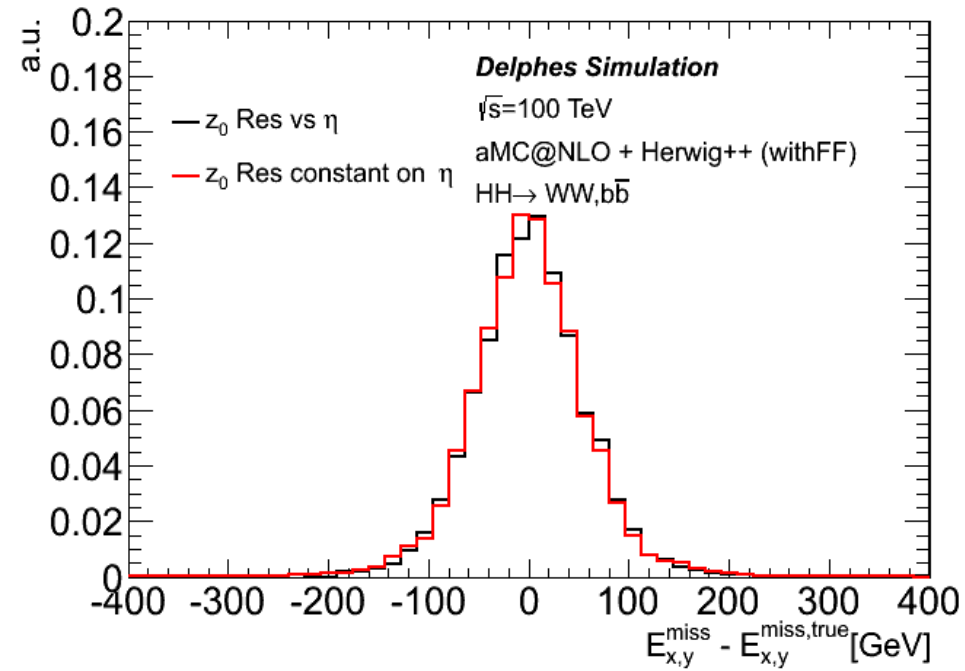
Detector parameter variations: z_0 resolution

Pile-Up = 50

Mbb invariant mass

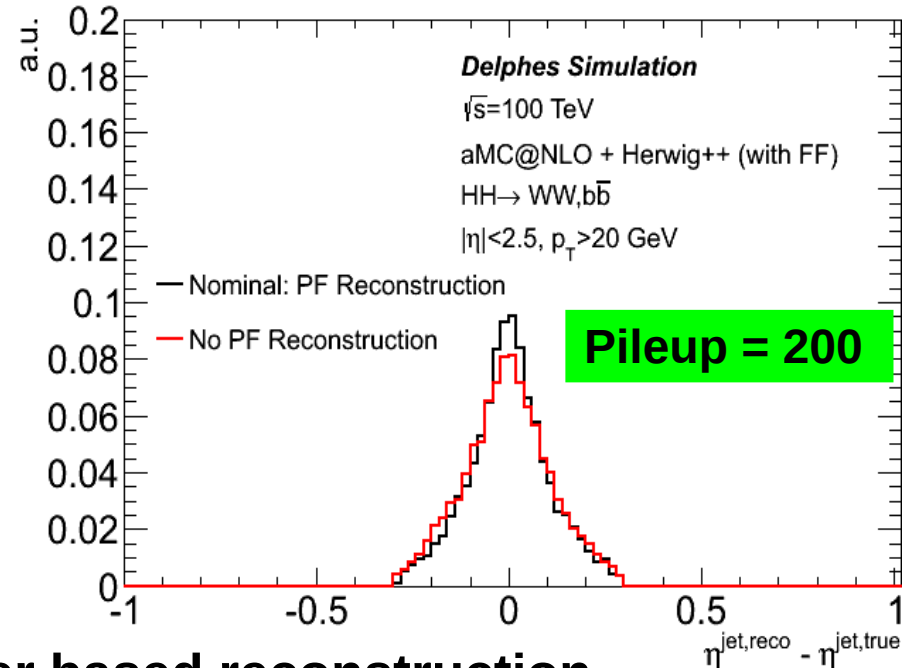
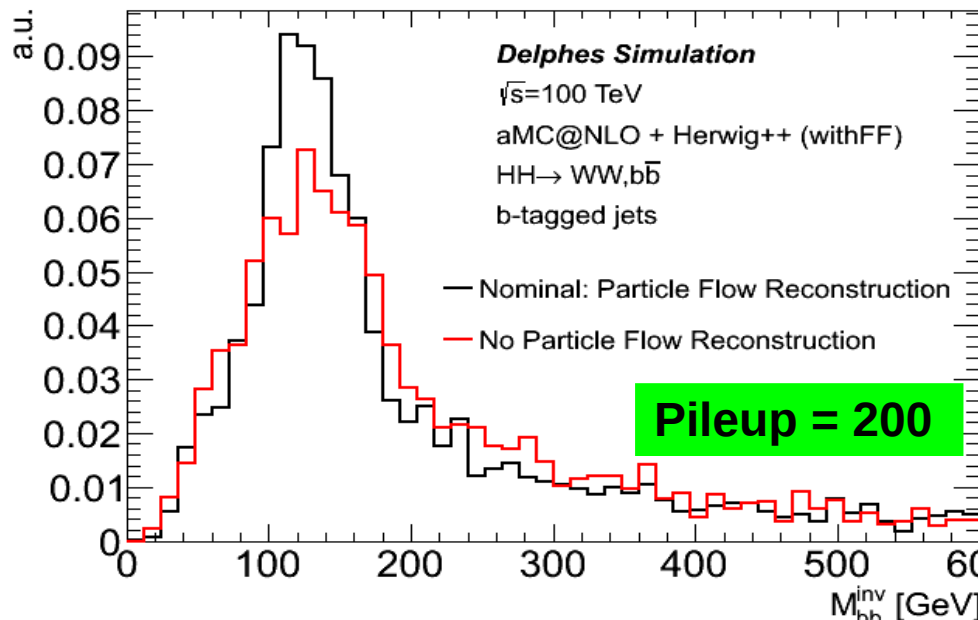
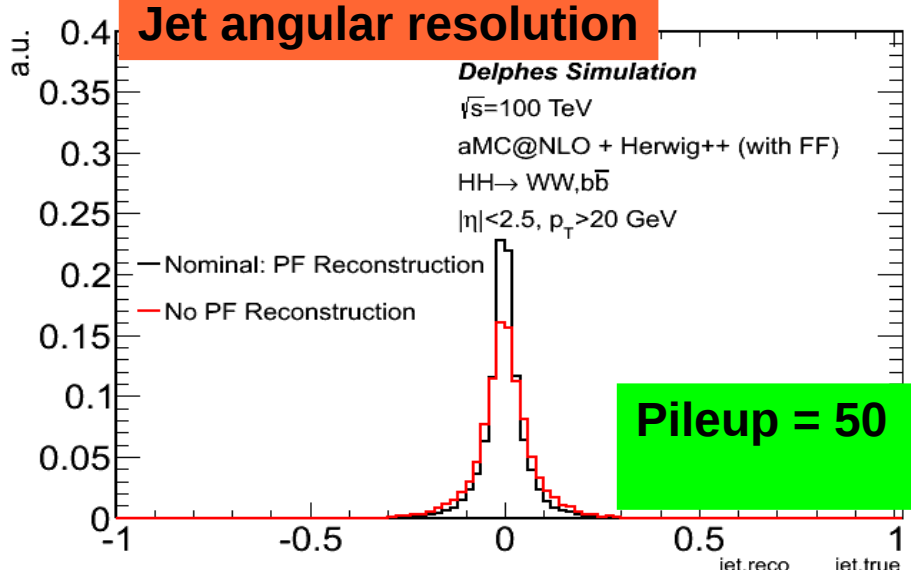
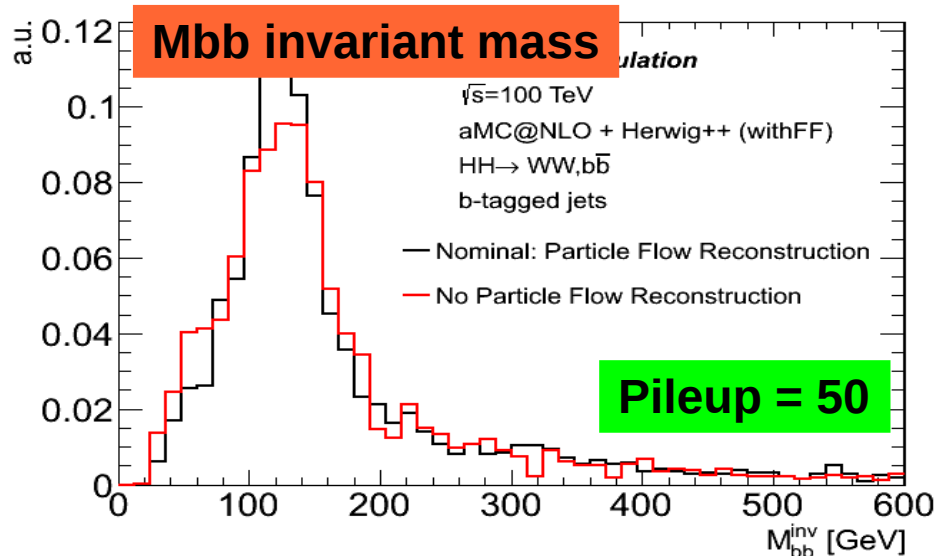


Missing ET resolution



- **Caveat: B-tagging not changed**
- **Mbb ~not sensitive: b-jets are mostly central**
- **MET ~not sensitive: driven by central jets**
- **Caveat: dependence on topology**
VBF, VBS would be different

Particle Flow vs Calorimeter based Jet reconstruction



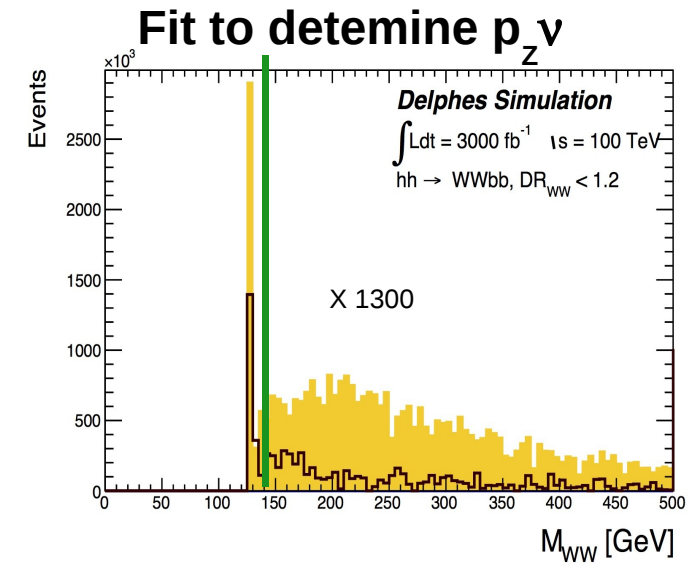
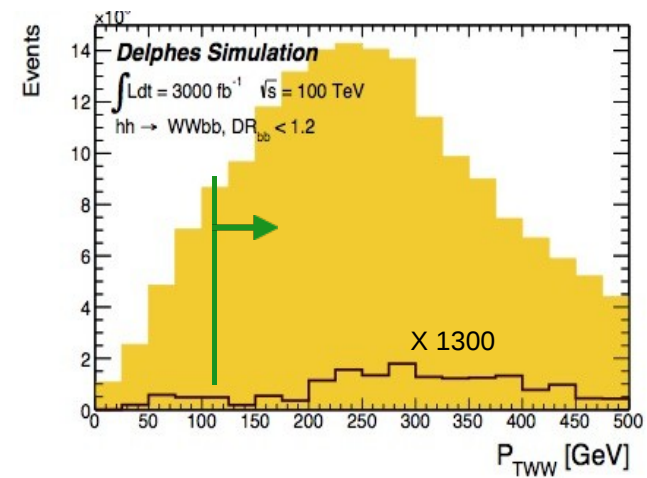
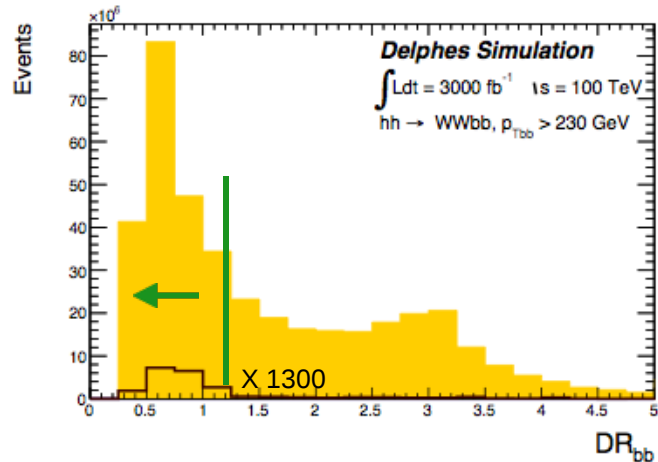
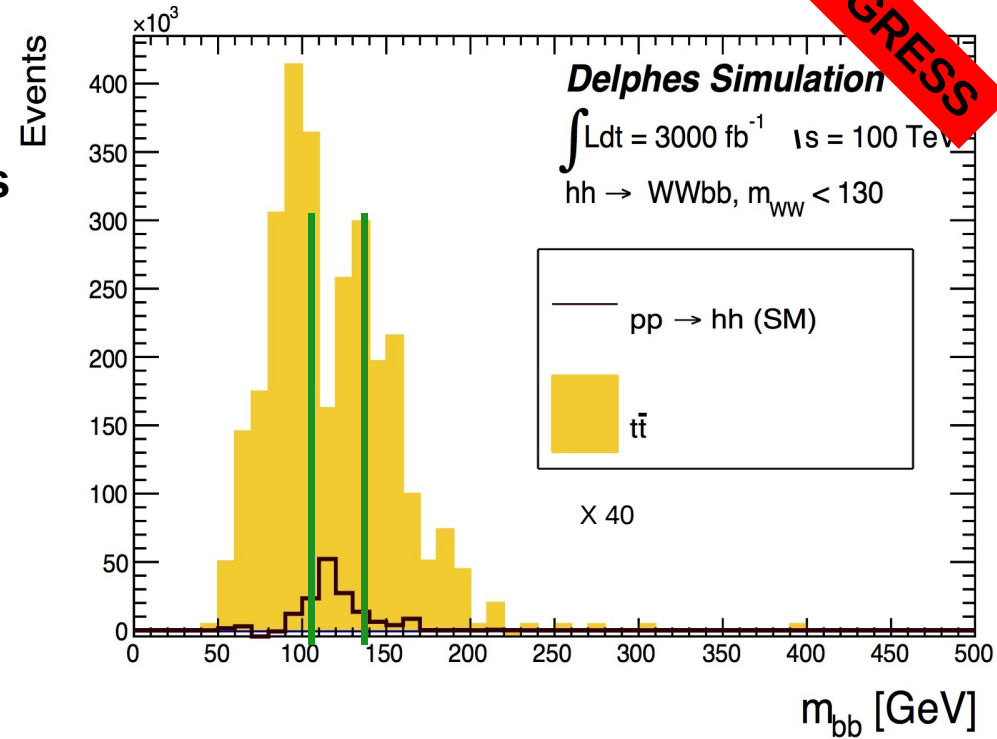
- Deterioration using calorimeter based reconstruction

Objects and Event selection

WORK in PROGRESS

- At least one isolated lepton with $p_T > 15$ GeV
- 4,5 jets with $p_T > 20$ GeV $|\eta| < 2.5$,
passing a Jet Vertex Fraction selection
- Overlap removal between muons, electron, jets

Variable	Cut
$p_T(bb)$	> 230 GeV
ΔR_{bb}	< 1.2
$p_T(WW)$	> 140 GeV
ΔR_{WW}	< 1.2
m_{WW}	< 130 GeV
m_{bb}	105 – 135 GeV



Analysis results

WORK in PROGRESS

Need more sophisticated techniques: kinematic fit, MVA analysis to bring S/Top > 10%.

3 ab ⁻¹ , PU 50	Object selection	Final Selection	ϵ
Signal	7084	803	2.5 10 ⁻³
Top bkg	5.4 10 ⁹	7.87 10 ⁵	
S/Top	1.31 10 ⁻⁶	1.02 10 ⁻³	

- PU = 200 configuration not been optimised
- 20% reduction in S/B
- ~× 3 reduction in the final signal yield

3 ab ⁻¹ , PU 200	Preselection	Final Selection	ϵ
Signal	5.4 10 ⁴	273	8.5 10 ⁻⁴
Top bkg	3.6 10 ⁹	3.4 10 ⁵	
S/Top	1.5 10 ⁻⁵	8.0 10 ⁻⁴	

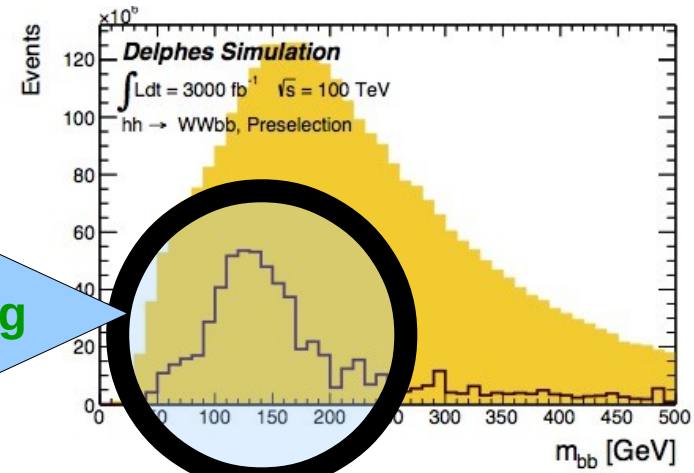
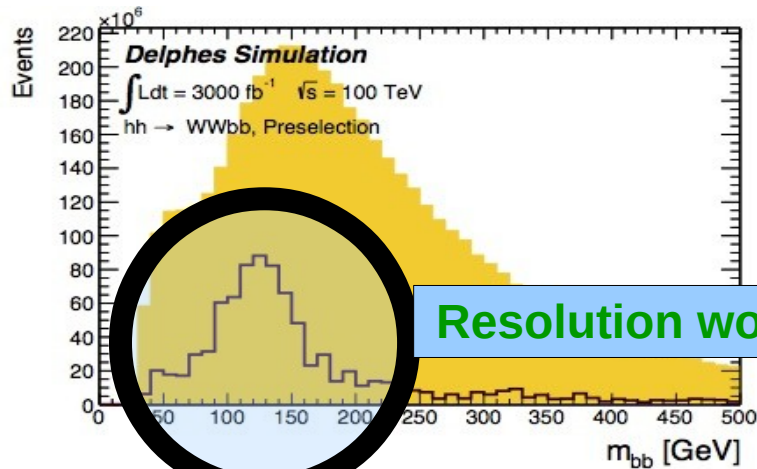
Conclusions

- First studies with realistic pile-up condition have been shown
 - Reconstruction and analysis degradation
 - At Pileup = 900 need smarter reconstruction
- Particle-flow reconstruction likely better for the hh kinematics (low E)
- Still a lot of work to be done:
 - Analysis still far to be sensitive to λ
 - top background difficult to handle
 - Optimization of cuts
 - fat jet and MVA technique
 - Additional pile-up suppression techniques
 - Change of other detector parametrizations
 - b-tagging, track resolution & efficiencies..

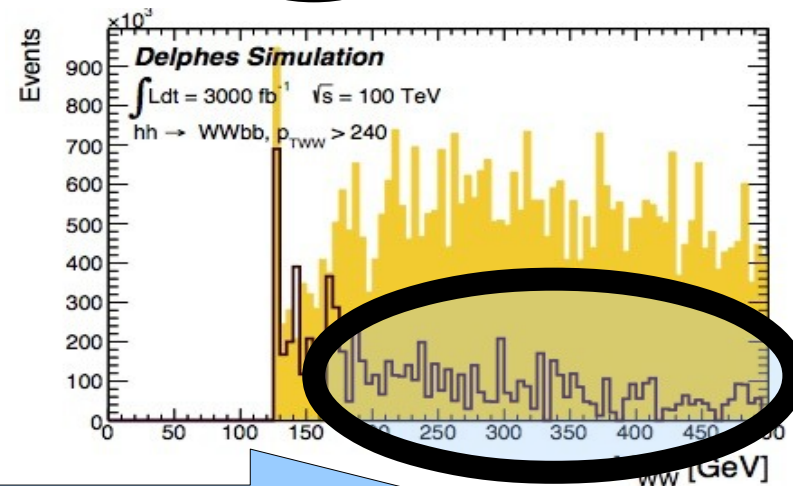
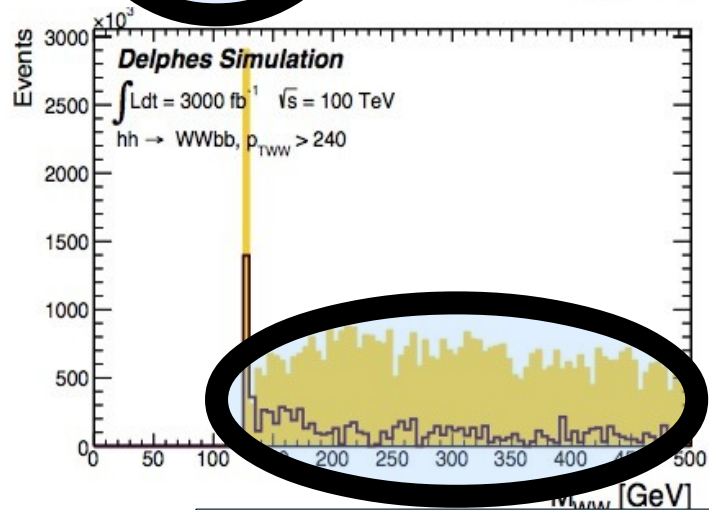
backup

50

200



Resolution worsening



Larger fraction of impossible solutions

Objects selection

- **At least one isolated lepton with $p_T > 15$ GeV (calo isolation corrected for pile-up and track isolation applied);**
- **4,5 jets with $p_T > 20$ GeV $|\eta| < 2.5$, passing a JVF selection:**
 - **$\Sigma p_T^{PV} / \Sigma p_T > 0.1$ for anti-btag jets, > 0.02 for b-tagged jets)**
- **Object overlap removal:**
 - **Leptons: take the highest p_T lepton;**
 - **preference order: muons, electrons, jets;**
 - **overlap removal cone: $\Delta R = 0.1$;**

m_{WW} distribution

- Neutrino p_z is computed using the relation $m_{WW} = m_h$, that is quadratic in p_z ;
- If two real solutions are found, that closest in ΔR to the lepton is taken, in this case $m_{WW} = m_h$ by definition;
- If 2 complex solutions are found only the real part is taken, in this case $m_{WW} > m_h$;
- The $m_{WW} > m_h$ represents the failure to find a solution consistent with the Higgs mass hypothesis

