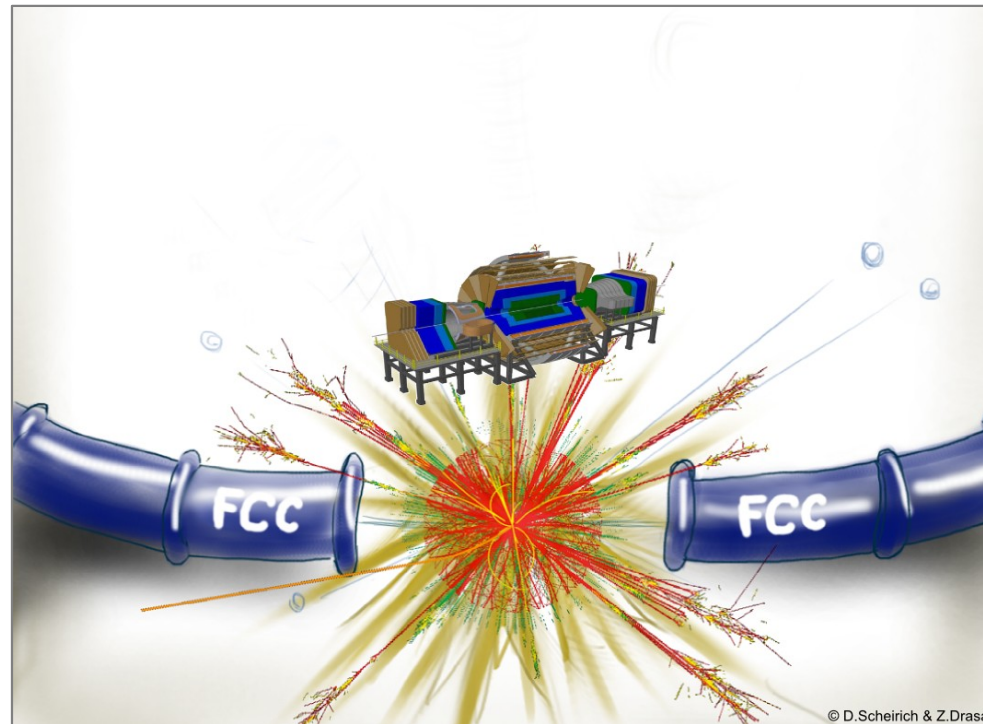


# Conceptual Study of FCC-hh Tracker Design



Zbyněk Drásal

CERN



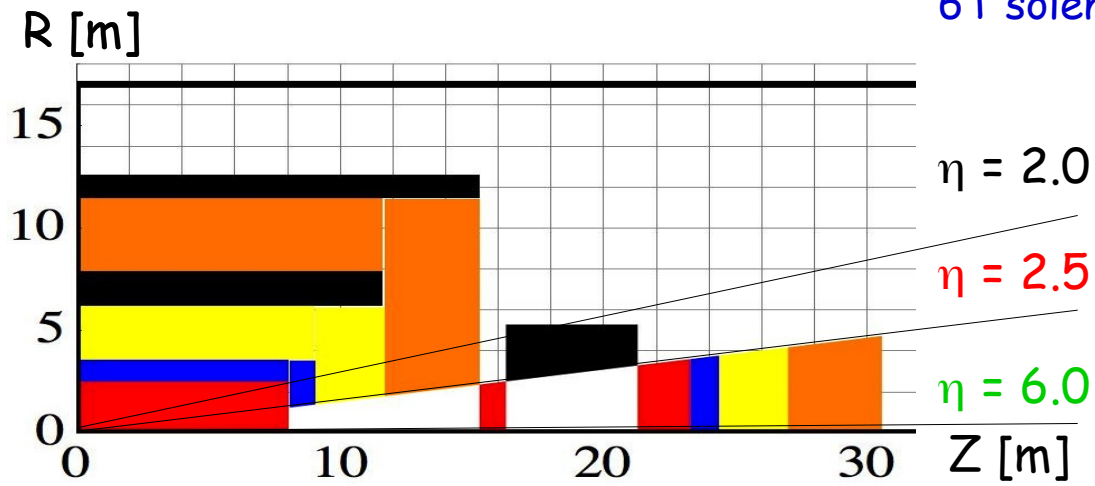
On behalf of FCC-hh detector group



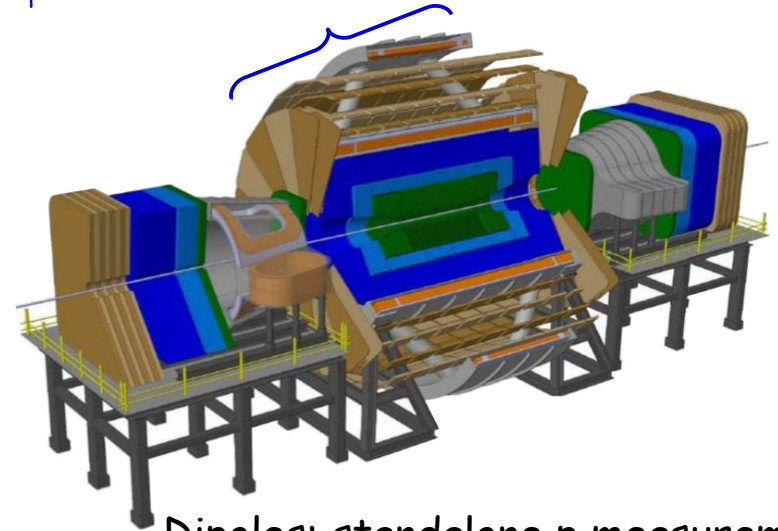
# Overview

- **FCC-hh tracker - Conceptual Design Study:**
  - **Introduction:**
    - Tracker geometry layout
    - Driving principles of momentum resolution measurement
    - Software toolkit - **tkLayout** (CMS phase 2 upgrade simulation toolkit)
  - **Expected tracker performance**
    - Tracker geometry layout & material budget
    - Tracker resolution → *two scenarios in forward region: forward dipole versus solenoid?*
  - **Implications of high pile-up & high-rate environment**
    - Tracker occupancy
    - Expected data rates
  - **Summary & Outlook**

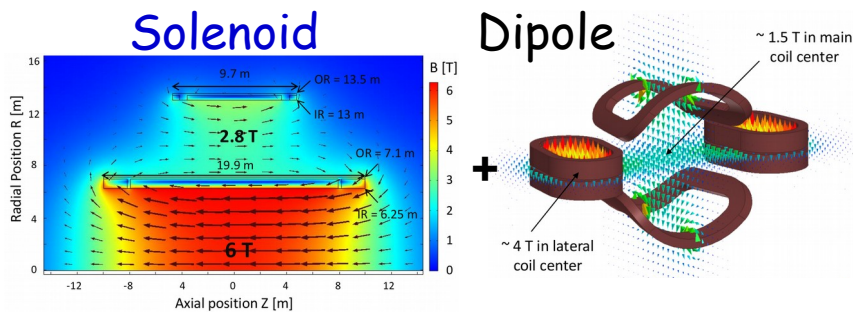
# FCC-hh Detector & Tracker Geometry



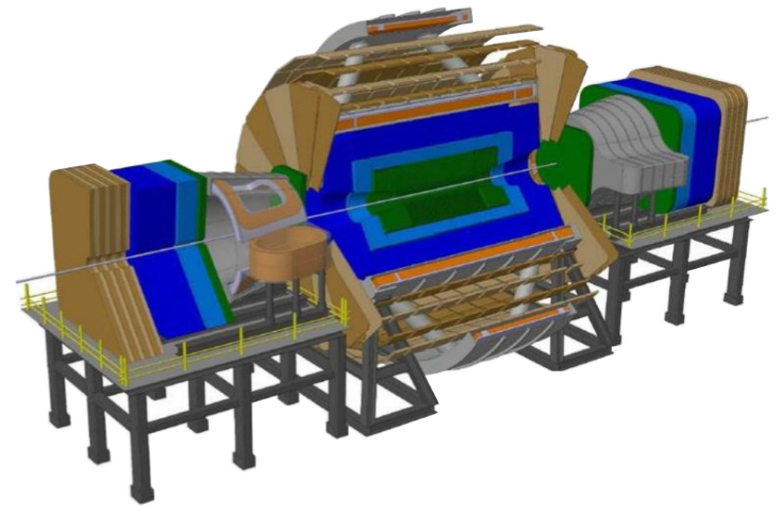
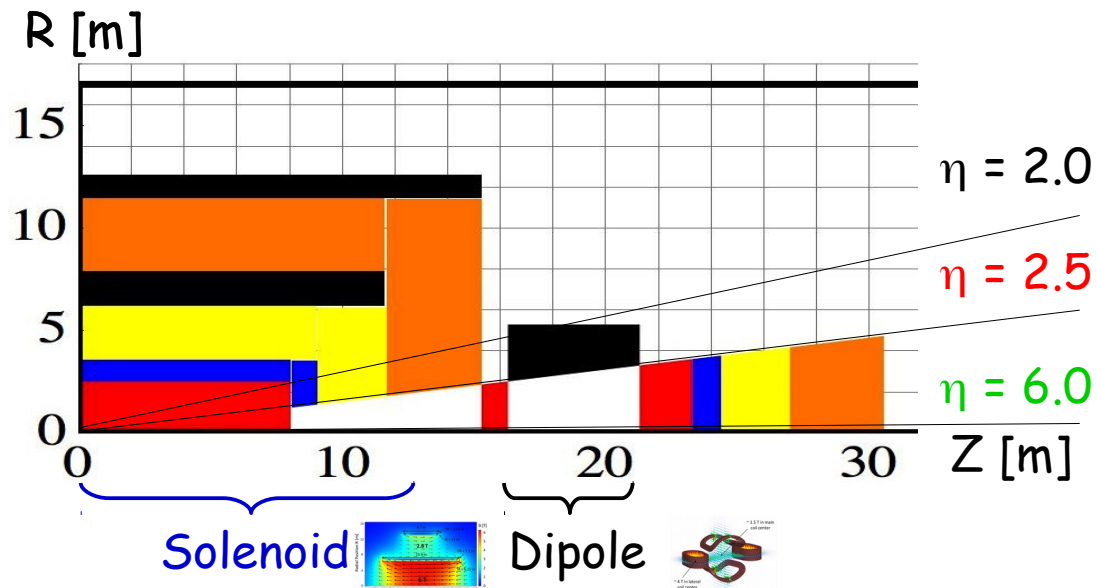
6T solenoid:  $P_T$  measurement in the central tracker



Dipoles: standalone  $p$  measurement



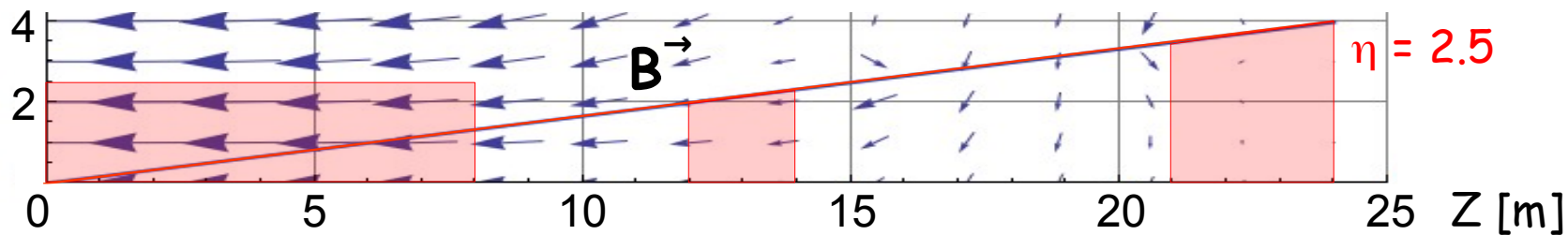
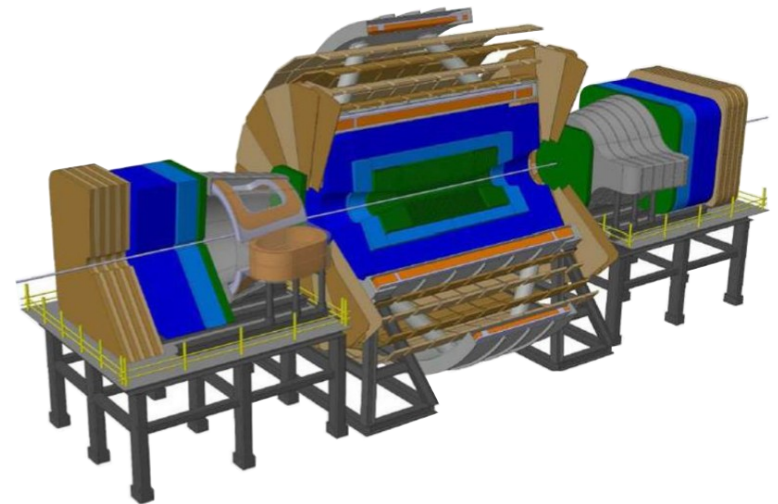
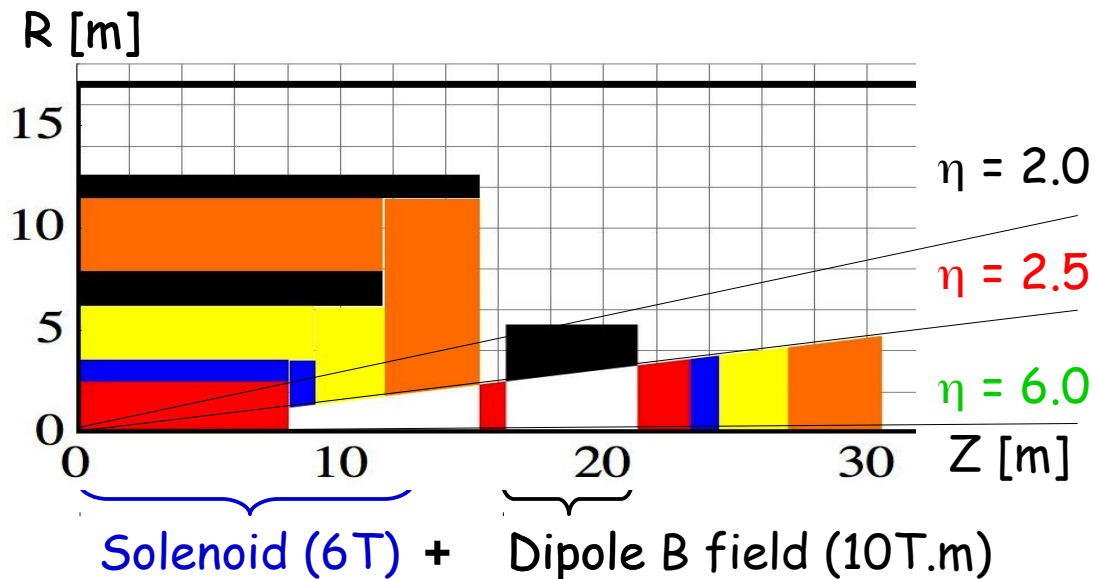
# FCC-hh Detector & Tracker Geometry



- Beam-pipe (BP):

- Beryllium  $R = 20\text{-}21\text{mm}$ ,  $x/x_0 = 0.286\%$   $\rightarrow 1/\sin(\theta)$  material factor in track fitting!
- $Z \geq 8.0\text{m}$   $\rightarrow$  conical shape with opening angle  $\alpha = 2.5\text{mrad}$

# FCC-hh Detector & Tracker Geometry

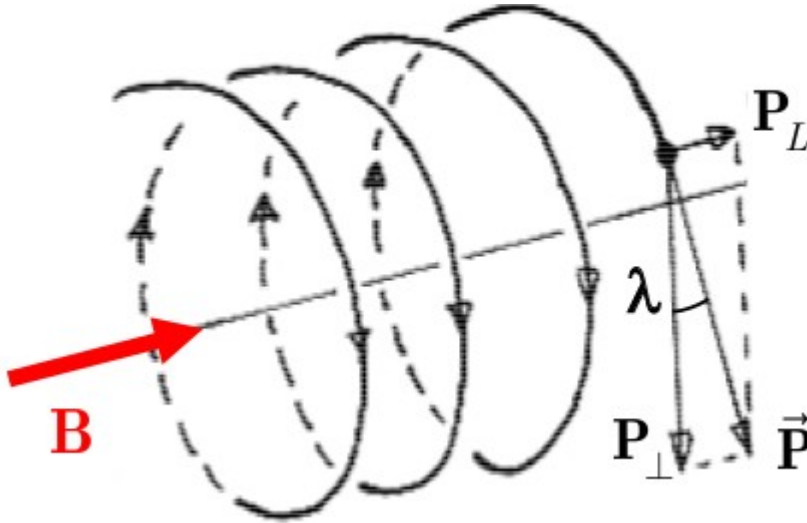


- **Tracker:** assuming  $x/x_0 = 3\%$  per layer
  - **Central:**  $Z = 0 - 8.0\text{m}$ ,  $R_{\text{max}} = 2.5\text{m}$  → detector layers (discs) @  $R = 25 - 2400\text{mm}$
  - **Fwd:**  $R_{\text{max}}$  limited by  $\eta = 2.5$  ( $R_{\text{min}}$  by conical shape of BP)

# Measuring Particle Momentum - Principals

- Tracking in magnetic field:

$$R[\text{m}] = \frac{p_T[\text{GeV}]}{0.3B[\text{T}]}$$

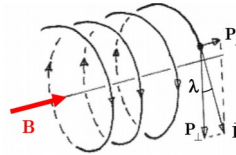


- **approximative approach**: separate movement in  $R-\Phi$  plane &  $s-z$  projection
- $R-\Phi$  plane → circle fitting →  $p_T$  measurement

# Measuring Particle Momentum - Principals

- Tracking in magnetic field:

$$R[\text{m}] = \frac{p_T[\text{GeV}]}{0.3B[\text{T}]}$$



- $R-\Phi$  plane  $\rightarrow$  circle fitting  $\rightarrow p_T$  measurement

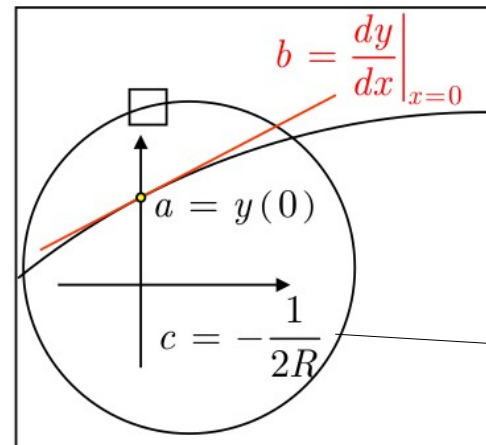
$$(y - y_0) = \sqrt{R^2 - (x - x_0)^2}$$

$$y \approx y_0 + R \left( 1 - \frac{(x - x_0)^2}{2R^2} \right)$$

$$y \approx \left( y_0 + R - \frac{x_0^2}{2R} \right) + \frac{x_0}{R}x - \frac{1}{2R}x^2$$

$$y \approx a + bx + cx^2$$

$\rightarrow$  for FCC dimensions: can use parabolic appr. for  $p_T \geq 10\text{GeV}$



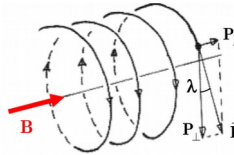
use

$$\frac{\Delta p_T}{p_T} = \frac{\Delta R}{R}$$

# Measuring Particle Momentum - Principals

- Tracking in magnetic field:

$$R[\text{m}] = \frac{p_T[\text{GeV}]}{0.3B[\text{T}]}$$



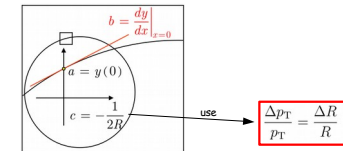
- $R-\Phi$  plane  $\rightarrow$  circle fitting  $\rightarrow p_T$  measurement  
 $\rightarrow$  can use parabolic approximation

$$(y - y_0) = \sqrt{R^2 - (x - x_0)^2}$$

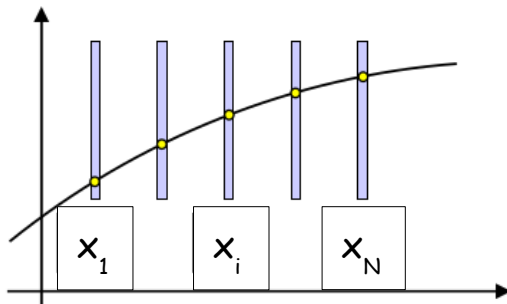
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$$y \approx a + bx + cx^2$$



- Assume  $N$  equidistant layers measuring the  $y$ -coordinate & applying global  $\chi^2$  fit [Gluckstern]



$$\frac{\Delta p_T}{p_T} = \frac{\sigma[\text{m}] p_T[\text{GeV}/c]}{0.3B[\text{T}] L^2[\text{m}^2]} \sqrt{\frac{720(N - 1)^3}{(N - 2)N(N + 1)(N + 2)}}$$

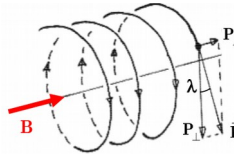
- $\rightarrow$  linearly increases with  $p_T$
- $\rightarrow$  scales linearly:  $B$  field (6T), sensor resolution in  $R-\Phi$   
quadratically: level-arm ( $\sim 2.4\text{m}$ )  
sqrt: #layers
- $\rightarrow$  affects the  $p_T$  resolution for high  $p_T$



# Measuring Particle Momentum - Principals

- Tracking in magnetic field:

$$R[\text{m}] = \frac{p_T[\text{GeV}]}{0.3B[\text{T}]}$$



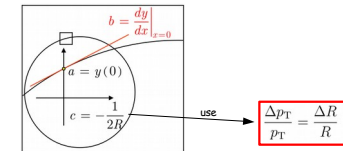
- $R$ - $\Phi$  plane  $\rightarrow$  circle fitting  $\rightarrow p_T$  measurement  
 $\rightarrow$  can use parabolic approximation

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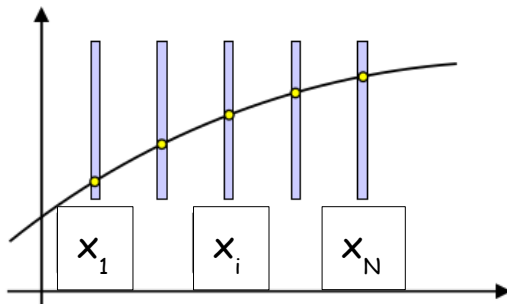
$$y \approx y_0 + R \left( 1 - \frac{(x - x_0)^2}{2R^2} \right)$$

$$y \approx \left( y_0 + R - \frac{x_0^2}{2R} \right) + \frac{x_0}{R}x - \frac{1}{2R}x^2$$

$$y \approx a + bx + cx^2$$



- Assume  $N$  equidistant layers measuring the  $y$ -coordinate & applying global  $\chi^2$  fit [Gluckstern]



$$\frac{\Delta p_T}{p_T} = \frac{\sigma[\text{m}] p_T[\text{GeV}/c]}{0.3B[\text{T}] L^2[\text{m}^2]} \sqrt{\frac{720(N - 1)^3}{(N - 2)N(N + 1)(N + 2)}}$$

- CMS  $\rightarrow$  FCC?

- $B = 4\text{T} \rightarrow 6\text{T}$
- $L = 1.1 (1.2) \rightarrow 2.4 (2.5)$

} Factor of 7 improvement

$\rightarrow$  further improvement by optimizing #layers & detector resolution

# Measuring Particle Momentum - Principals

- Multiple Coulomb scattering:

- $p_T$  resolution for low  $p_T$  tracks dominated by multiple Coulomb scattering:

$$\frac{\Delta p_T}{p_T} = \frac{0.0136}{0.3\beta B[\text{T}] L[\text{m}]} \sqrt{\frac{X_{\text{tot}}}{X_0}} \sqrt{\frac{10}{7}}$$

→  $p_T$  constant term

→ scales linearly: B field, level-arm

sqrt: material budget ( $\sim 3\% x/x_0/\text{layer}$ )

→ affects the  $p_T$  resolution for low  $p_T$

# TkLayout software toolkit

- TkLayout approach to momentum resolution:
  - Use [Karimäki] approach for circle (in polar coordinates)

$$\left(\frac{1}{2R}d^2 + d\right) - \left(1 + \frac{d}{R}\right) \sin(\phi_0 - \phi_i) r_i + \frac{1}{2R}r_i^2 = \varepsilon_i$$

$$\sin(\phi_0 - \phi_i) \approx (\phi_0 - \phi_i)$$

$$\left(\frac{1}{2R}d^2 + d\right) - \left(1 + \frac{d}{R}\right)(\phi_0 - \phi_i) r_i + \frac{1}{2R}r_i^2 \approx \varepsilon_i \longrightarrow \text{„Parabolic“ approx. in } r_i$$

→  $R$  = radius,  $d$  = impact parameter in  $R - \Phi$ ,  $\phi_0$  = initial angle,  $\varepsilon_i$  = residual for  $i$ -th measur.

# TkLayout software toolkit

- TkLayout approach:

- Use [Karimäki] approach for circle (in polar coordinates) → apply “parabolic” approximation:

$$\left(\frac{1}{2R}d^2 + d\right) - \left(1 + \frac{d}{R}\right)\sin(\phi_0 - \phi_i)r_i + \frac{1}{2R}r_i^2 = \varepsilon_i$$

$$\sin(\phi_0 - \phi_i) \approx (\phi_0 - \phi_i)$$

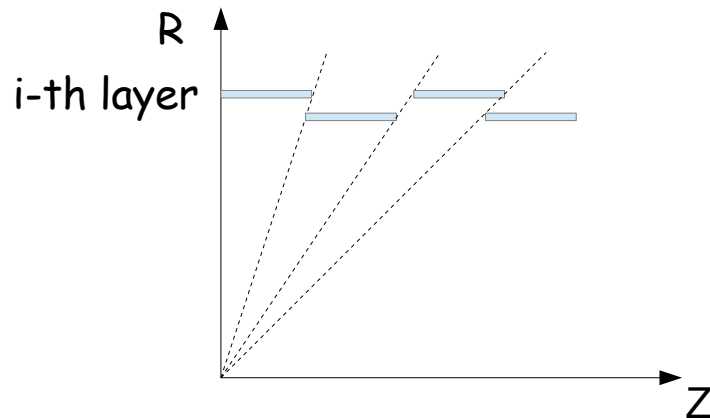
$$\left(\frac{1}{2R}d^2 + d\right) - \left(1 + \frac{d}{R}\right)(\phi_0 - \phi_i)r_i + \frac{1}{2R}r_i^2 \approx \varepsilon_i$$



$$\sum_{i=1}^N \varepsilon^T \mathbf{V}^{-1} \varepsilon$$

$R$  = radius,  $d$  = impact parameter in  $R - \Phi$ ,  $\phi_0$  = initial angle,  $\varepsilon_i$  = residual for  $i$ -th measur.

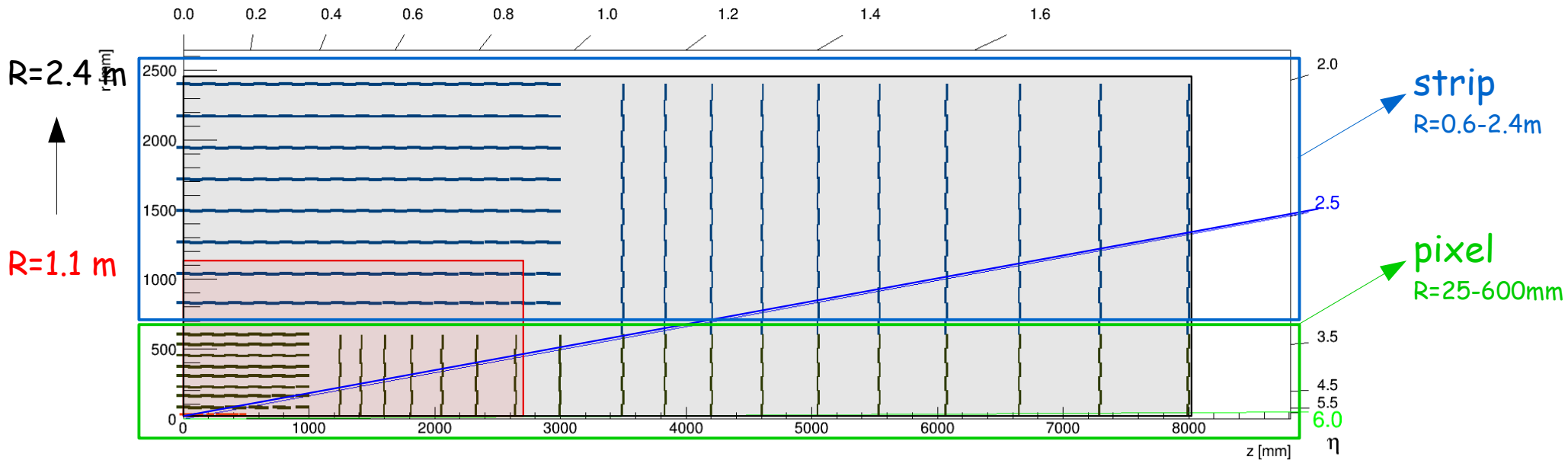
- Build an optimized geometry layout in ROOT TGeo & do global  $\chi^2$  fit  $\sum_{i=1}^N \varepsilon^T \mathbf{V}^{-1} \varepsilon$



→ tkLayout: SW for tracker studies of CMS Phase 2 upgrade → adapted for FCC-hh

# FCCh Tracker - Material Budget

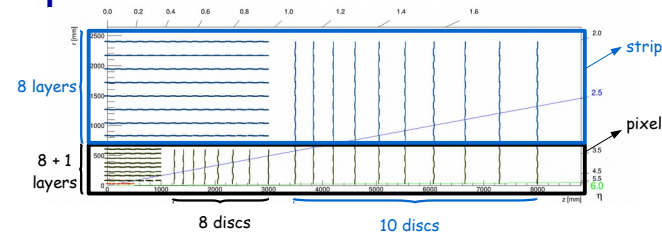
- Implicitly assumed  $x/x_0 = 3\%$  per layer  $\rightarrow$  Expected material distribution?
  - Starting from the following geometry layout ("default") ...
  - MB of each detector ( $t_{\text{mod}} = 0.43\text{cm}$ ) represented as: 20% Si, 42% C, 2% Cu, 6% Al, 30% Plastic



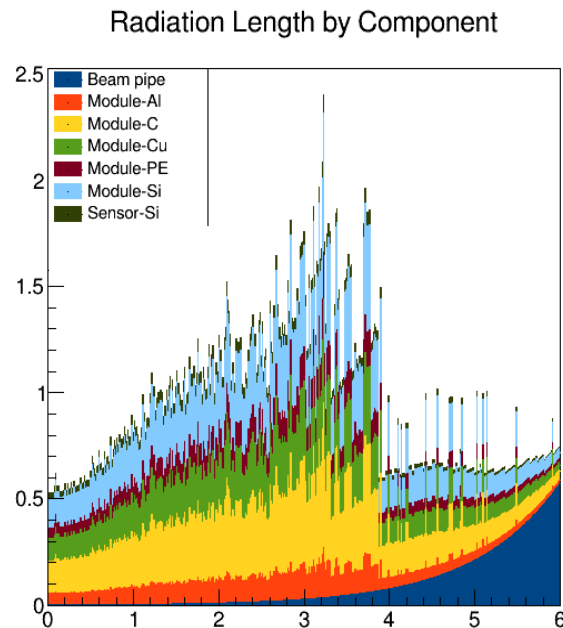
CMS  $\rightarrow$  FCC

# FCCh Tracker - Material Budget (MB)

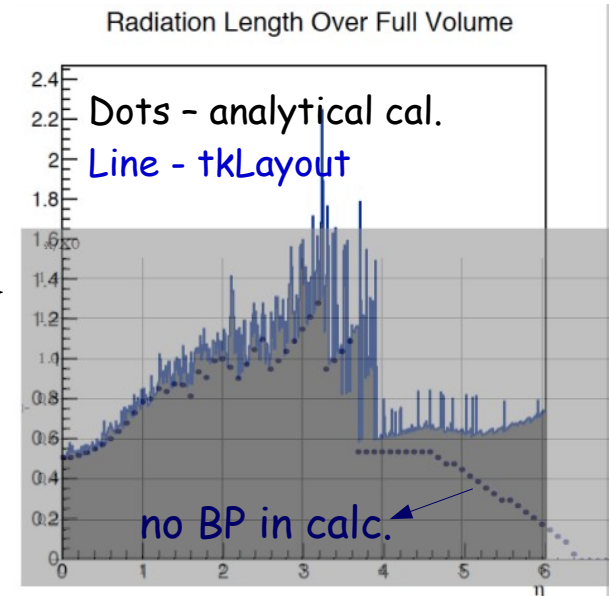
- Implicitly assumed  $x/x_0 = 3\%$  per layer  $\rightarrow$  Expected material distribution?
  - Starting from the following geometry layout ...



## - Material budget:



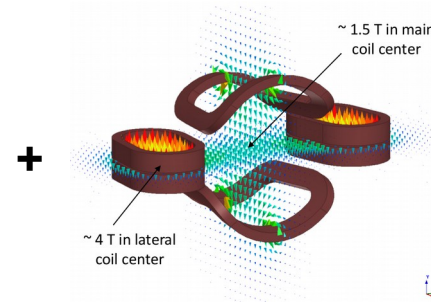
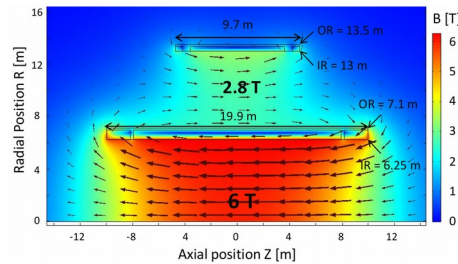
Compared to  
analytical calc.  
by W. Riegler



# FCCh Tracker - Resolution Studies

- What is the tracker  $p_T$  resolution? Two approaches in fwd region: dipole versus solenoid?

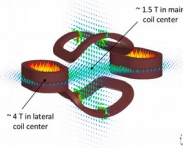
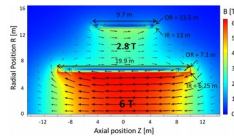
- Dipole scenario:



# FCCh Tracker - Resolution Studies

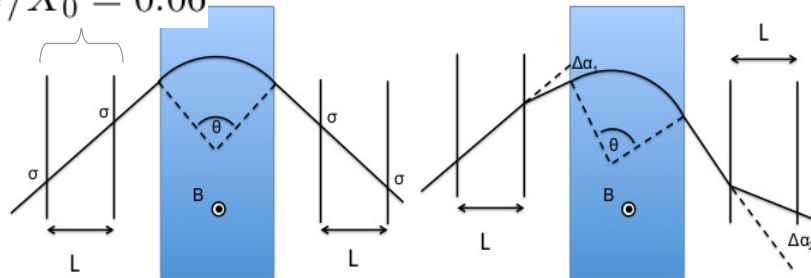
- What is the tracker  $p_T$  resolution? Two approaches in fwd region: dipole versus solenoid?

- Dipole scenario:



- Measure  $p_L(p)$  using forward tracker & dipole (calculations by W.Riegler):

$$x_f/X_0 = 0.06$$



Using  $L = 2$  m,  $\sigma = 30 \mu\text{m}$ ,  $x_f/X_0 = 0.06$

$$\left(\frac{\Delta p_L}{p_L}\right)^2 = \left(\frac{2\sigma p_L}{0.3L \int B_T dl}\right)^2 + \left(\frac{0.0136}{0.3 \int B_T dl} \sqrt{2 \frac{x_f}{X_0}}\right)^2$$

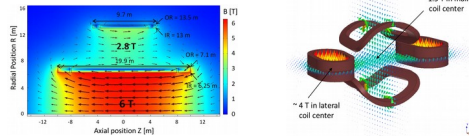
Tracking resolution
MS resolution



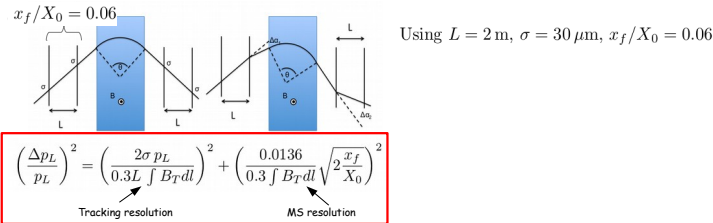
# FCChh Tracker - Resolution Studies

- What is the tracker  $p_T$  resolution? Two approaches in fwd region: dipole versus solenoid?

– Dipole scenario:



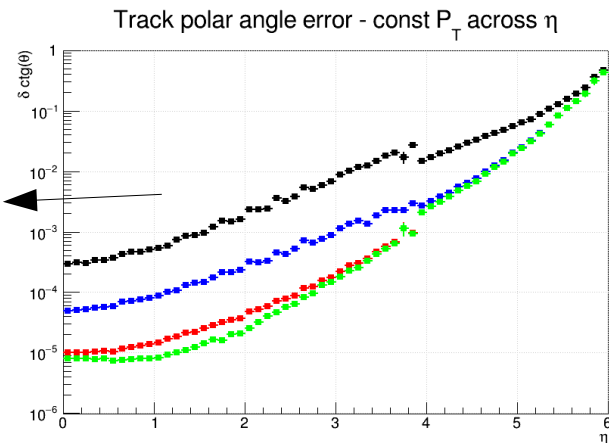
- Measure  $p_L(p)$  using forward tracker & dipole (calculations by W.Riegler):



- Using the  $\cotg(\vartheta_{\text{emission}})$  measurement (by tkLayout) determine the  $p_T$  from  $p_L(p)$

$$p_T = p_L \tan \vartheta_e$$

$$\left(\frac{\Delta p_T}{p_T}\right)^2 = \left(\frac{\Delta p_L}{p_L}\right)^2 + \left(\frac{1}{\sin \vartheta_e \cos \vartheta_e}\right)^2 \Delta \vartheta_e^2$$

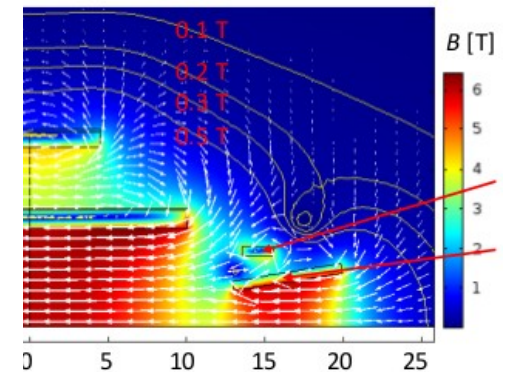


Simulated  $p_T$ :

- 10 GeV
- 100 GeV
- 1 TeV
- 10 TeV

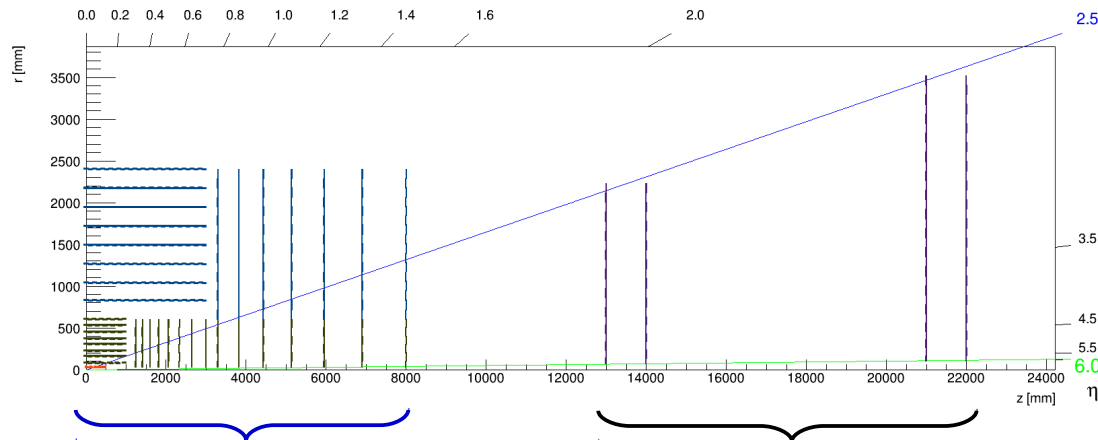
# FCCh Tracker - Resolution Studies

- Compared to the second scenario ...
  - **Solenoid** scenario (see talk by M.Mentink)
    - In tkLayout the 2 solenoids modelled as one 6T solenoid covering central+fwd tracker



# FCCh Tracker - Resolution Studies

- Tracker geometry:



Central tracker

- $R-\Phi$  res. = 25 $\mu$ m

Fwd inner discs:

- $R-\Phi$  res. = 25 $\mu$ m

Fwd outer discs:

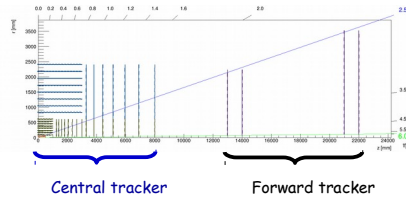
- Variable resol. in  $R-\Phi$ : 25 - 130 $\mu$ m to get const pt resol. to  $\eta=3.0$  (const. 25 $\mu$ m resol. would improve the result even more!)

The level-arm playing a role  
in the solenoid+solenoid scenario

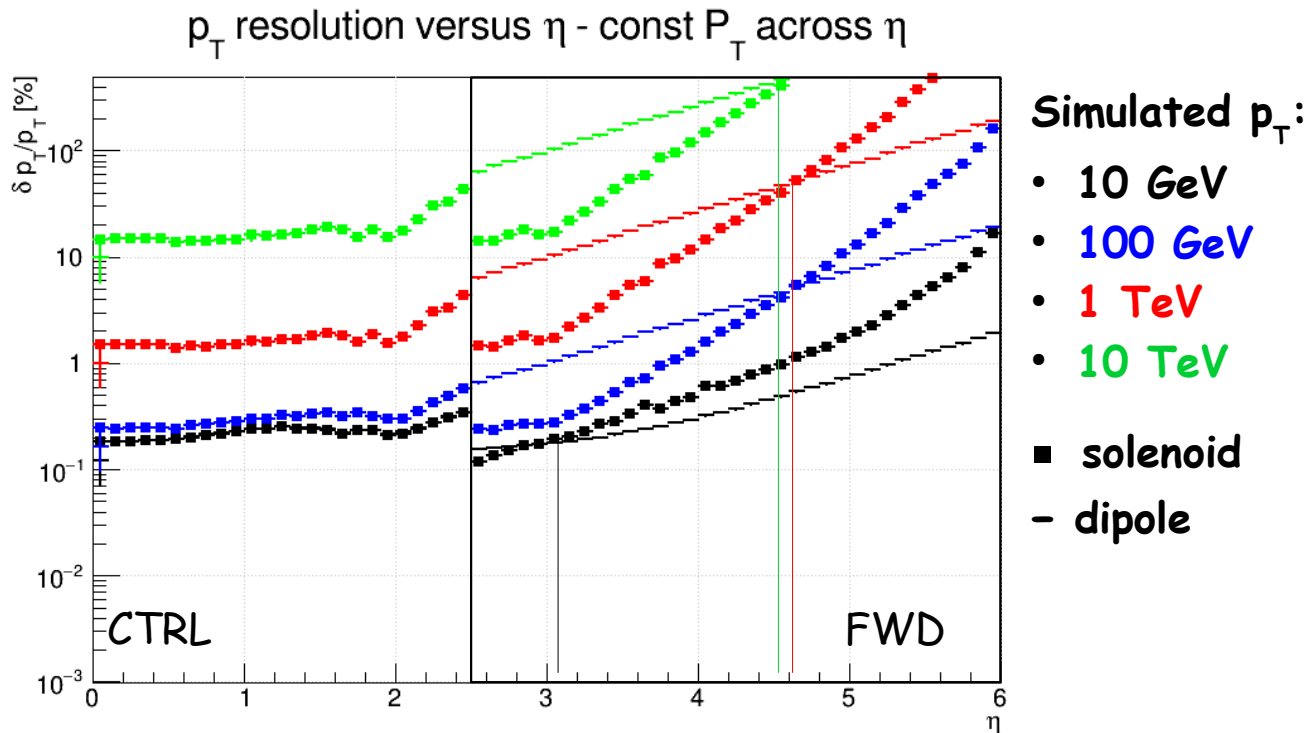
The level-arm playing a role  
in the solenoid+dipole scenario

# FCChh Tracker - Resolution Studies

- Tracker geometry:



- Estimated  $p_T$  resolution:

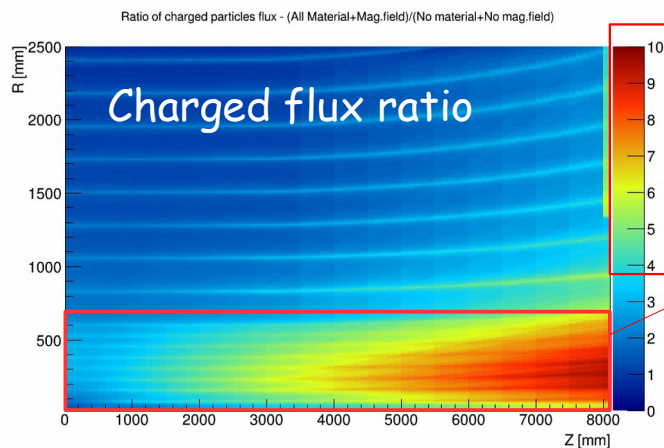


# Tracker in High Pile-up & High Rate Environment

- Implications of high pile-up and high-rate environment on the tracker design

- Use Fluka irradiation map (by F.Cerutti & M.I.Besana) → calculate flux ratio:

$$\text{Flux}_{\text{MB\_on} + \text{BField\_on}} / \text{Flux}_{\text{MB\_off} + \text{BField\_off}} \rightarrow \text{study effect of MB \& B field:}$$



Multiplication factor → effect of material & B field

Particles compressed to the R = 600mm in strong mag. field of 6T → **region unsuitable for strip detectors**

# Tracker Occupancy Studies

- Study of tracker occupancy:
  - Use the flux [particles/cm<sup>2</sup>] normalized to 1000 pile-up events
  - **Estimate occupancy & minimum pitch** to get ~ 1% occupancy for pixel detectors

## Pixel - BRL

Number of pile-up events: 1000

Layer no :	1	2	3	4	5	6	7	8	9
Radius [mm] :	25.0	93.3	169.2	232.9	317.9	381.6	466.5	530.1	600.0
Min flux in Z [particles/cm <sup>-2</sup> ] :	468.9	51.8	20.3	12.3	6.7	4.8	3.0	2.4	1.7
Max flux in Z [particles/cm <sup>-2</sup> ] :	592.5	74.3	27.3	16.4	8.3	6.0	3.6	2.8	2.0
Z position [mm] related to max flux :	500.0	1000.0	1000.0	1000.0	1000.0	1000.0	1000.0	1000.0	1000.0
Max cell area in Z (1% occupancy) [mm <sup>2</sup> ] :	0.0017	0.0135	0.0367	0.0609	0.1203	0.1662	0.2806	0.3542	0.4998

→ 40x40um<sup>2</sup> @ 1<sup>st</sup> layer

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40x40um<sup>2</sup> @ 1<sup>st</sup> layer

## Pixel - ENDCAP

Number of pile-up events: 1000

Ring no :	1	2	3	4	5	6	7	8	9	10	11
Average radius [mm] :	53.5	78.5	123.5	179.5	235.5	291.5	347.5	403.5	459.5	515.5	571.5
Min flux in R [particles/cm <sup>2</sup> -R] :	110.5	61.1	38.6	20.1	12.6	8.9	6.7	4.5	3.3	2.7	2.1
Max flux in R [particles/cm <sup>2</sup> -R] :	1145.8	308.6	128.8	60.6	36.6	25.2	17.0	12.3	9.3	6.9	5.3
Z position [mm] related to max flux :	7996.0	8004.0	7996.0	8004.0	7996.0	8004.0	7996.0	8004.0	7996.0	8004.0	7996.0
Max cell area in R (1% occupancy) [mm <sup>2</sup> ]	0.0009	0.0032	0.0078	0.0165	0.0273	0.0396	0.0588	0.0812	0.1075	0.1458	0.1902

30x30um<sup>2</sup> @ 1<sup>st</sup> endcap ring

→ no stringent limit on min pitch (the dominant limit might be driven by physics of high collimated objects)

# Tracker Data Rates

- Expected data rates (required bandwidth):
  - Use Fluka simulated flux scaled to 1000 pile-ups & calculate hit rates:
    - Non-triggered data  $\rightarrow f = 40$  MHz
    - Triggered data  $\rightarrow f \sim 1$  MHz (value given by hardware limits, e.g. FPGA etc.)



# Tracker Data Rates

- Expected data rates (required bandwidth):
  - Use Fluka simulated flux scaled to 1000 pile-ups & calculate hit rates:
  - Estimate the bandwidth for **sparsified data**:
    - address read-out channel :  $n\text{Bits} = \log_2(n\text{Rows}) + \log_2(n\text{Columns})$
    - add data block for cluster width: 2bits (cluster width  $\sim 3$ )
    - add data block for pulse-height: 0bits (binary read-out), 4-8bits (analog read-out)

# Tracker Data Rates - PXL BRL

- Expected data rates for CMS-like geometry (required bandwidth):
  - Use Fluka simulated flux scaled to 1000 pile-ups & calculate hit rates:
  - Estimate the bandwidth for sparsified data:

## Pixel - BRL

Number of pile-up events: 1000

Layer no :	1	2	3	4	5	6	7	8	9	Total [TB/s]
Radius [mm] :	25.0	93.3	169.2	232.9	317.9	381.6	466.5	530.1	600.0	
Module bandwidth/(addr+clsWidth=2b[b] :	19	19	19	19	19	19	19	19	19	
Mod. bandwidth(#chnls*(addr+clsWidth)[kb] :	96.93	11.52	8.62	5.15	2.70	1.93	1.18	0.92	0.66	
Mod. bandwidth (matrix*1b/channel) [kb] :	128.00	128.00	128.00	128.00	128.00	128.00	128.00	128.00	128.00	
Data rate per layer - 40Mhz, spars [Tb/s] :	823	540	359	295	211	181	134	120	99	345
Data rate per layer - 1Mhz, spars [Tb/s] :	20	13	8	7	5	4	3	3	2	8
Data rate per ladder - 40Mhz, spars [Gb/s] :	70257	15377	11513	6872	3610	2579	1569	1231	878	
Data rate per ladder - 1Mhz, spars [Gb/s] :	1756	384	287	171	90	64	39	30	21	
Data rate per module - 40Mhz, spars [Gb/s]:	3697.74	439.35	328.95	196.37	103.17	73.70	44.83	35.18	25.09	
Data rate per module - 1Mhz, spars [Gb/s]:	92.44	10.98	8.22	4.91	2.58	1.84	1.12	0.88	0.63	

Total data flow from inner barrel

9.5 Gb/s/cm<sup>2</sup> @ 1MHz trigger & with binary read-out

- The triggered (1MHz) data in the first 2 layers with data flows >> 10Gb/s per module
- Out of current scale → need for trigger & advanced technologies!

# Tracker Data Rates - PXL Endcap

- Expected data rates for CMS-like geometry (required bandwidth):
  - Use Fluka simulated flux scaled to 1000 pile-ups & calculate hit rates:
  - Estimate the bandwidth for sparsified data:

Pixel - BRL

Number of pile-up events: 1000

Total data flow from inner barrel

Layer no :	1	2	3	4	5	6	7	8	9	Total [TB/s]
Radius [mm] :	25.0	93.3	169.2	232.9	317.9	381.6	466.5	530.1	600.0	
Module bandwidth/(addr+clsWidth=2b[b] :	19	19	19	19	19	19	19	19	19	
Mod. bandwidth(#chnls*(addr+clsWidth)[kb] :	96.93	11.52	8.62	5.15	2.70	1.93	1.18	0.92	0.66	
Mod. bandwidth (matrix*1b/channel) [kb] :	128.00	128.00	128.00	128.00	128.00	128.00	128.00	128.00	128.00	
Data rate per layer - 40MHz,spars [Tb/s] :	823	540	359	295	211	181	134	120	99	345
Data rate per layer - 1MHz,spars [Tb/s] :	20	13	8	7	5	4	3	3	2	8
Data rate per ladder - 40MHz,spars [Gb/s] :	70257	15377	11513	6872	3610	2579	1569	1231	878	
Data rate per ladder - 1MHz,spars [Gb/s] :	1756	384	287	171	90	64	39	30	21	
Data rate per module - 40MHz,spars [Gb/s] :	3697.74	439	5	328.95	196.37	103.17	73.70	44.83	35.18	25.09
Data rate per module - 1MHz,spars [Gb/s] :	92.44	10.8	8.22	4.91	2.58	1.84	1.12	0.88	0.63	

9.5 Gb/s/cm<sup>2</sup> @ 1 MHz trigger & with binary read-out

## Pixel - ENDCAP

Number of pile-up events: 1000

Ring no :	1	2	3	4	5	6	7	8	9	10	11	Total [TB/s]
Average radius [mm] :	53.5	78.5	123.5	179.5	235.5	291.5	347.5	403.5	459.5	515.5	571.5	
Module bandwidth/(addr+clsWidth=2b[b] :	19	19	19	19	19	19	19	19	19	19	19	
Mod. bandwidth(#chnls*(addr+clsWidth)[kb] :	36.89	25.35	11.37	12.89	8.38	5.43	3.72	2.72	2.07	1.51	1.14	
Mod. bandwidth (matrix*1b/channel) [kb] :	128.00	128.00	128.00	128.00	128.00	128.00	128.00	128.00	128.00	128.00	128.00	
Data rate per ringLayer-40MHz,spars [Tb/s] :	989	1223	915	691	584	465	358	305	266	210	177	773
Data rate per ringLayer- 1MHz,spars [Tb/s] :	24	30	22	17	14	11	8	7	6	5	4	19
Data rate per ring - 40MHz,spars [Gb/s] :	28144	34814	26031	19668	16621	13246	10203	8703	7582	5999	5040	
Data rate per ring - 1MHz,spars [Gb/s] :	703	870	650	491	415	331	255	217	189	149	126	
Data rate per module - 40MHz,spars [Gb/s] :	1407.21	967.08	433.86	491.71	319.65	206.97	141.72	103.61	78.98	57.69	43.45	
Data rate per module - 1MHz,spars [Gb/s] :	35.18	24.18	10.85	12.29	7.99	5.17	3.54	2.59	1.97	1.44	1.09	

3.6 Gb/s/cm<sup>2</sup> @ 1MHz trigger & with binary read-out

→ Out of current scale → need for trigger & advanced technologies!

# Summary & Outlook

- tkLayout, a software toolkit for CMS tracker phase 2 upgrade design studies, has been adapted & setup for FCC(-hh) needs:
  - An important toolkit providing “engineering” approach to geometry layout with the capability to study performance of a designed tracker
  - Details of already studied layouts can be found at <http://fcc-tklayout.cern.ch>
- Design study concentrated on resolution, material budget, occupancy & data rates of FCC-hh tracker in a magnet scenario of 6T has been done:
  - Particularly, with a focus on the interplay between the central tracker & forward region in 2 magnet scenarios: dipole versus solenoid in the forward region
  - Another scenarios (e.g. pushing the detector resolution to their technology limits) can be easily studied with tkLayout
- Future studies need to be focused on the pattern recognition and its impact on the tracker design
  - Either using the tkLayout software with a combinatorial approach as a starting study or more advanced techniques using tkLayout and/or FCC full simulation software