

Higgs Coupling measurements

W. Verkerke (Nikhef)

Outline of this presentation

① Introduction

② Higgs boson phenomenology & interpretation framework

③ Combination procedure & experimental inputs

④ Signal strength measurements

⑤ Constraints on Higgs boson couplings

⑥ Improving on systematic uncertainties

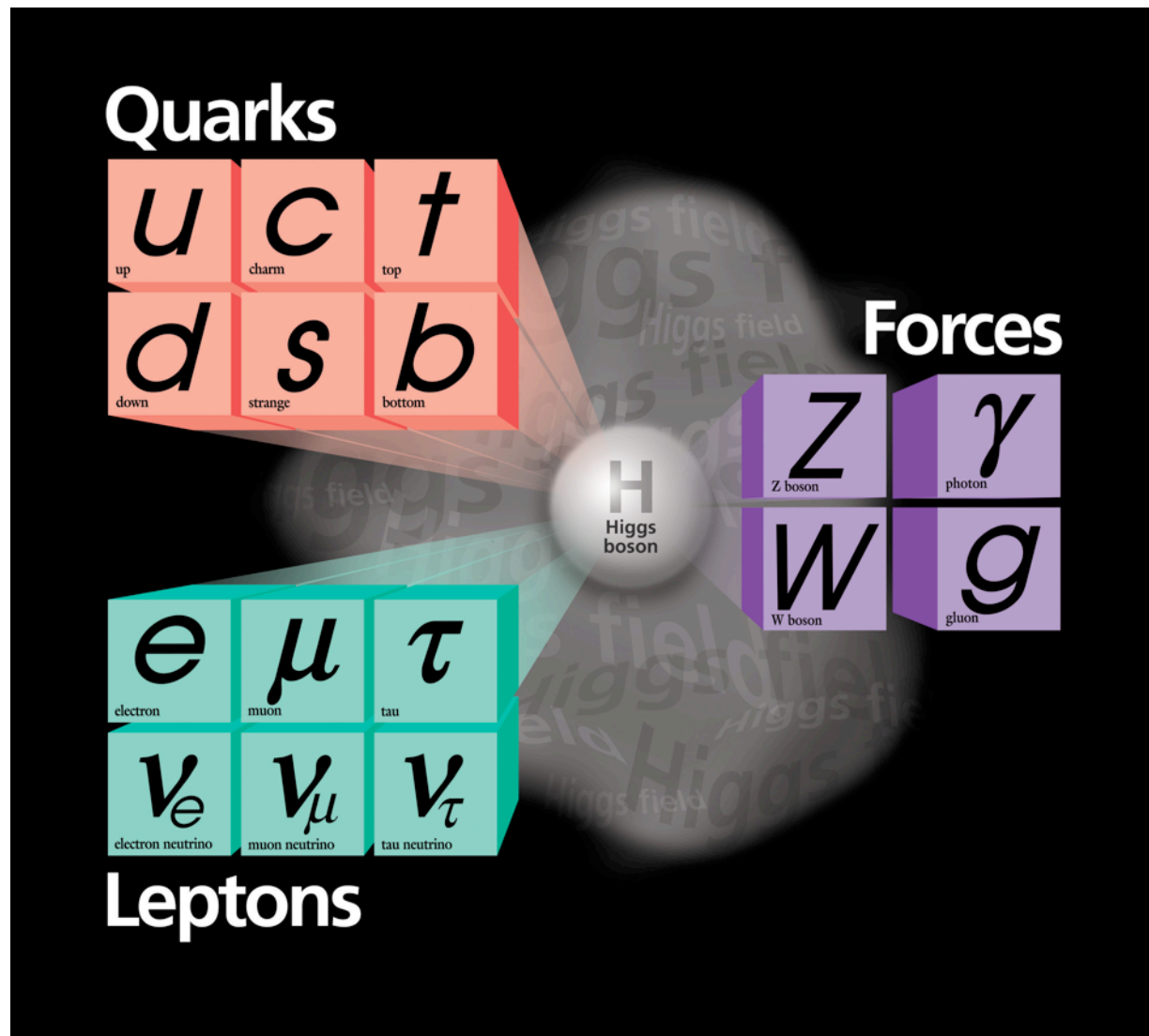
⑦ Improving on Higgs signal models

Today

Tomorrow

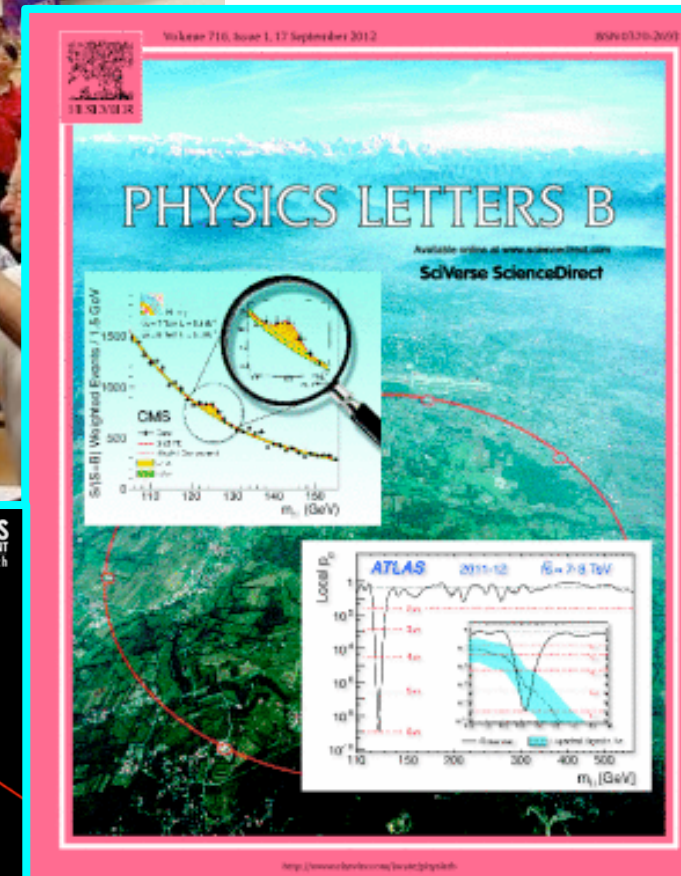
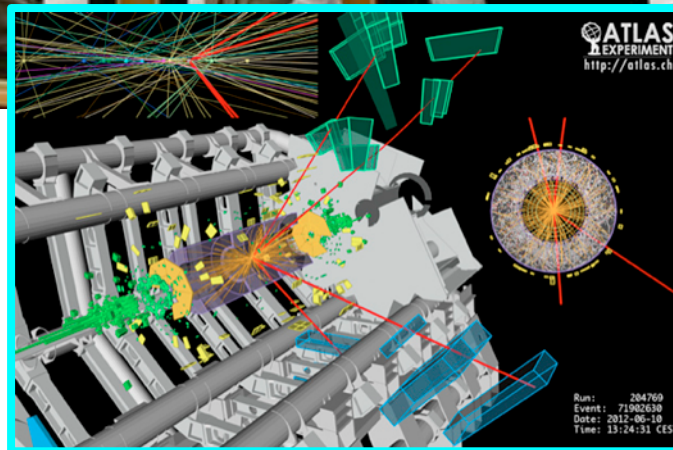
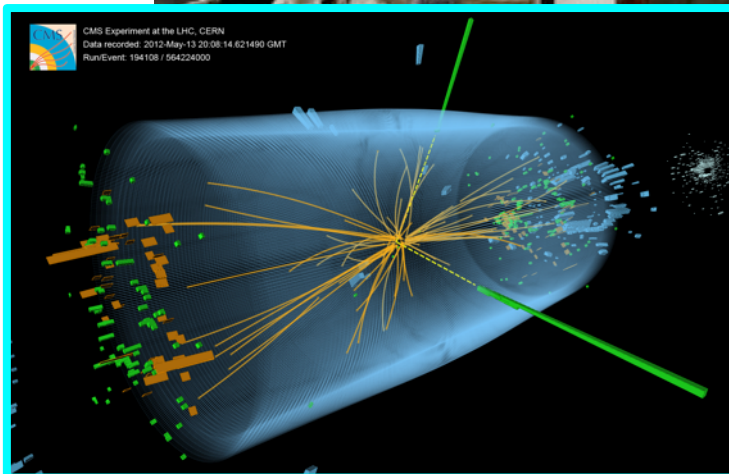
Introduction – Brout-Englert-Higgs mechanism in the SM

- The Brout-Englert-Higgs mechanism plays a pivotal role in the Standard Model



Run 1- Discovery of SM-like Higgs boson

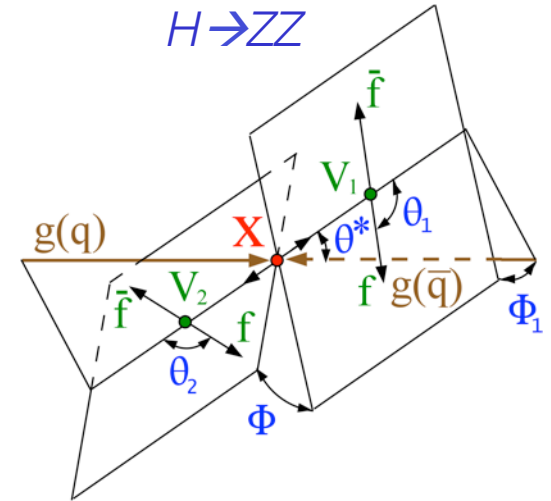
- Discovery of Standard-Model like Higgs boson in 2012 offers opportunity to investigate Higgs sector of nature in detail



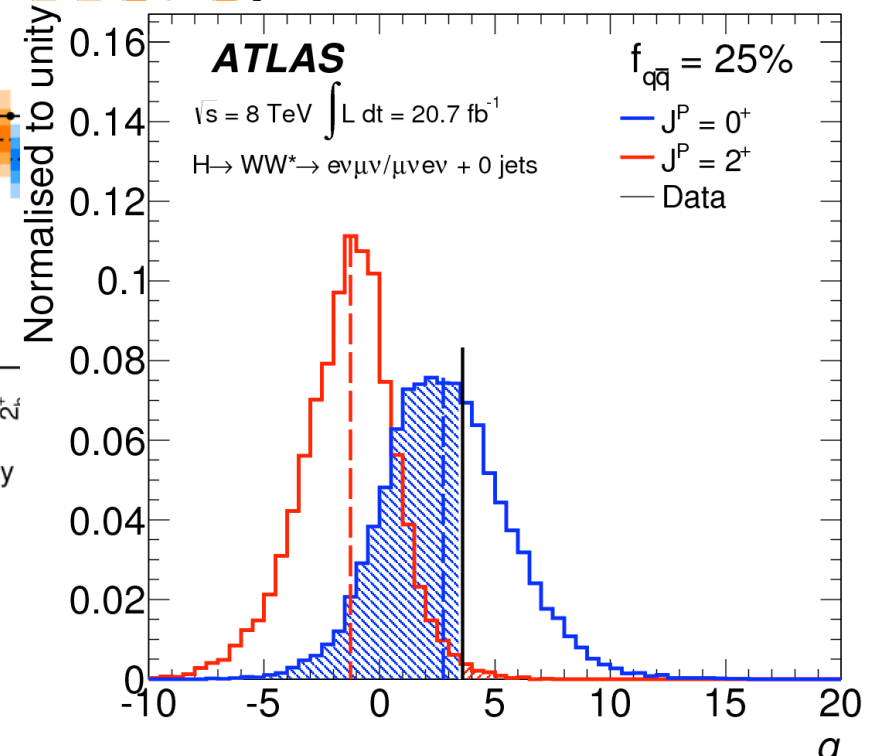
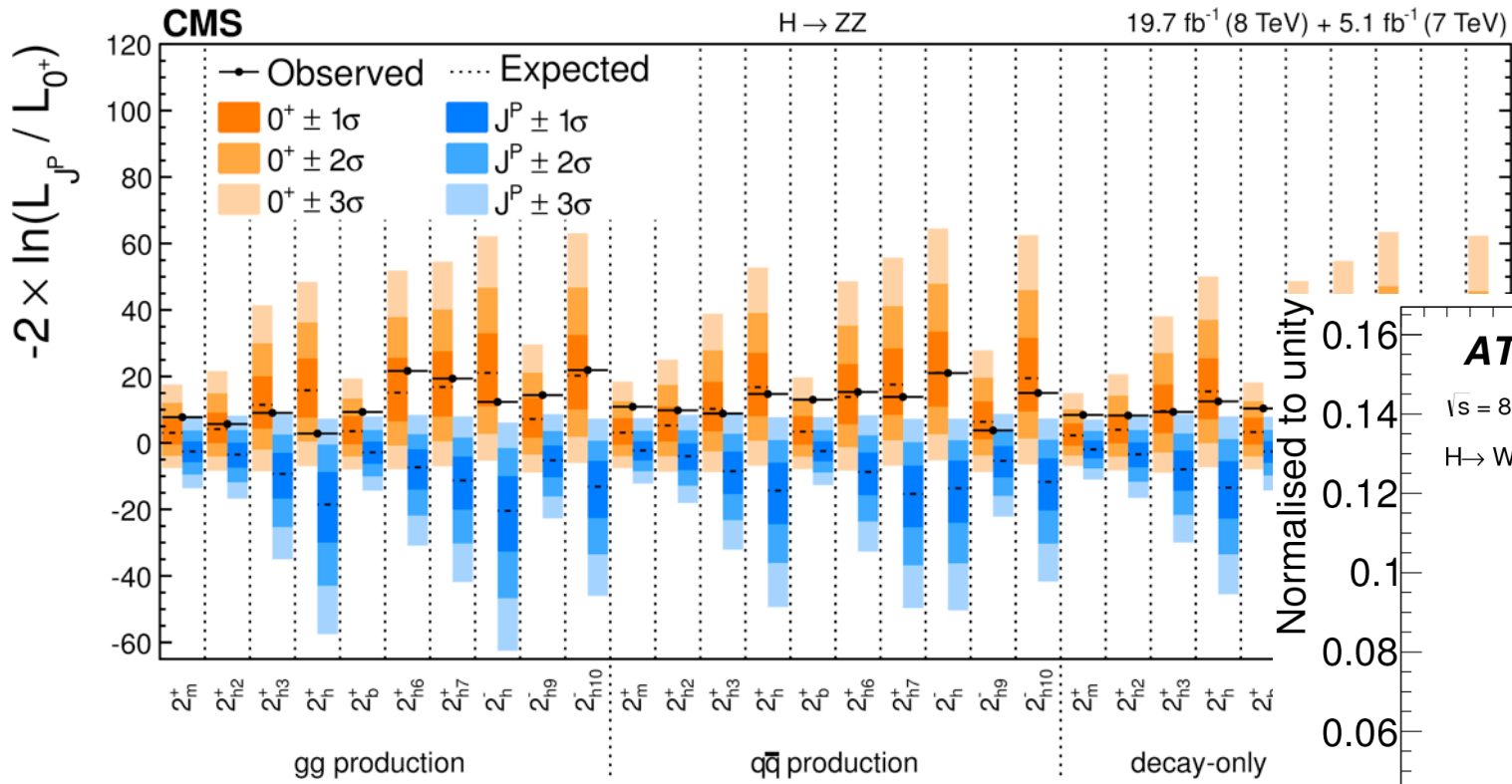
The observed Higgs boson is a spin-0 particle, compatible with CP-even

- Angular analysis of CMS and ATLAS run-1 data rules out spin-2 at >99.9% C.L.

PRD 92 (2015) 012004

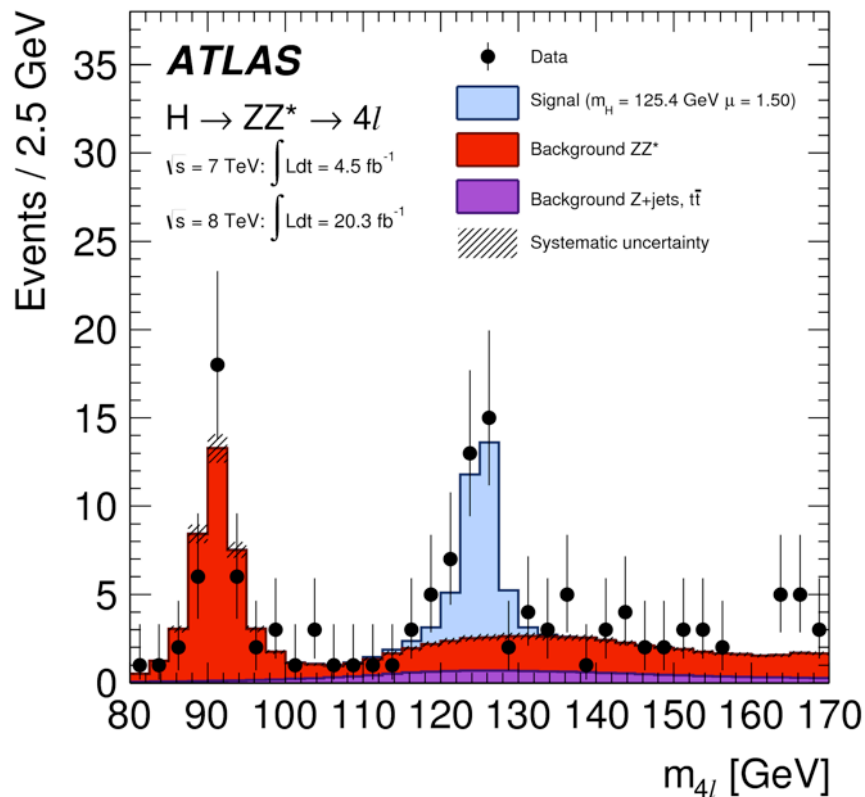


Eur. Phys. J. C75 (2015) 231

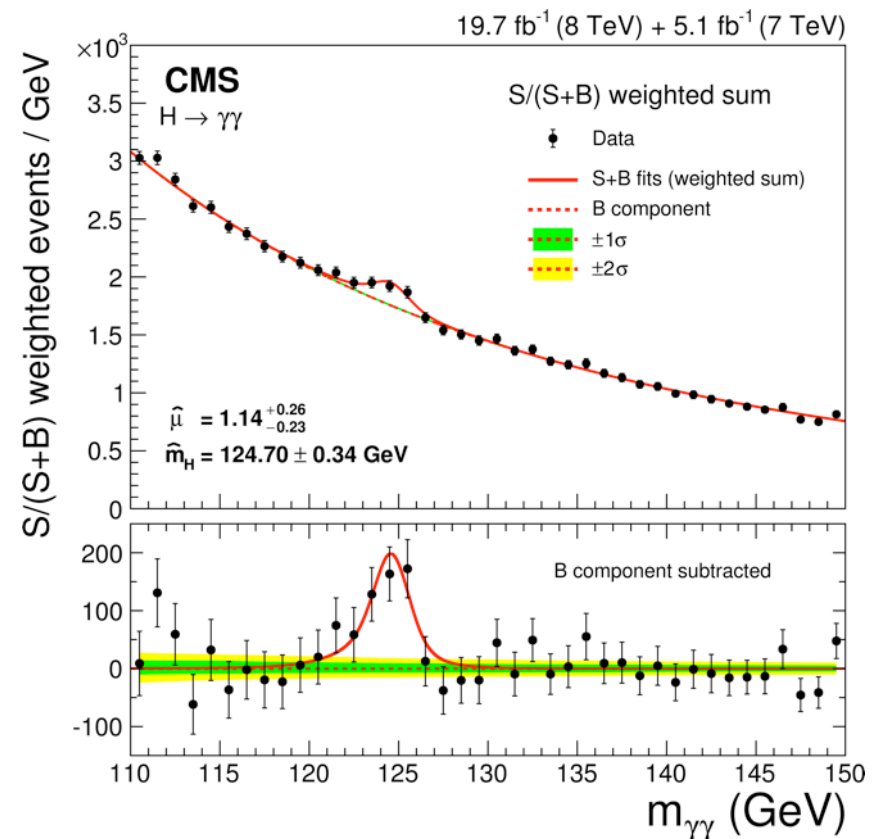


Mass of Higgs boson measured with $<0.2\%$ precision

- Higgs boson mass is only parameter unconstrained by SM
- But crucial in SM prediction of Higgs production and decay rates
- Measurement based on $H \rightarrow ZZ^*$ and $H \rightarrow \gamma\gamma$ final states, for which invariant mass can be reconstructed with high precision



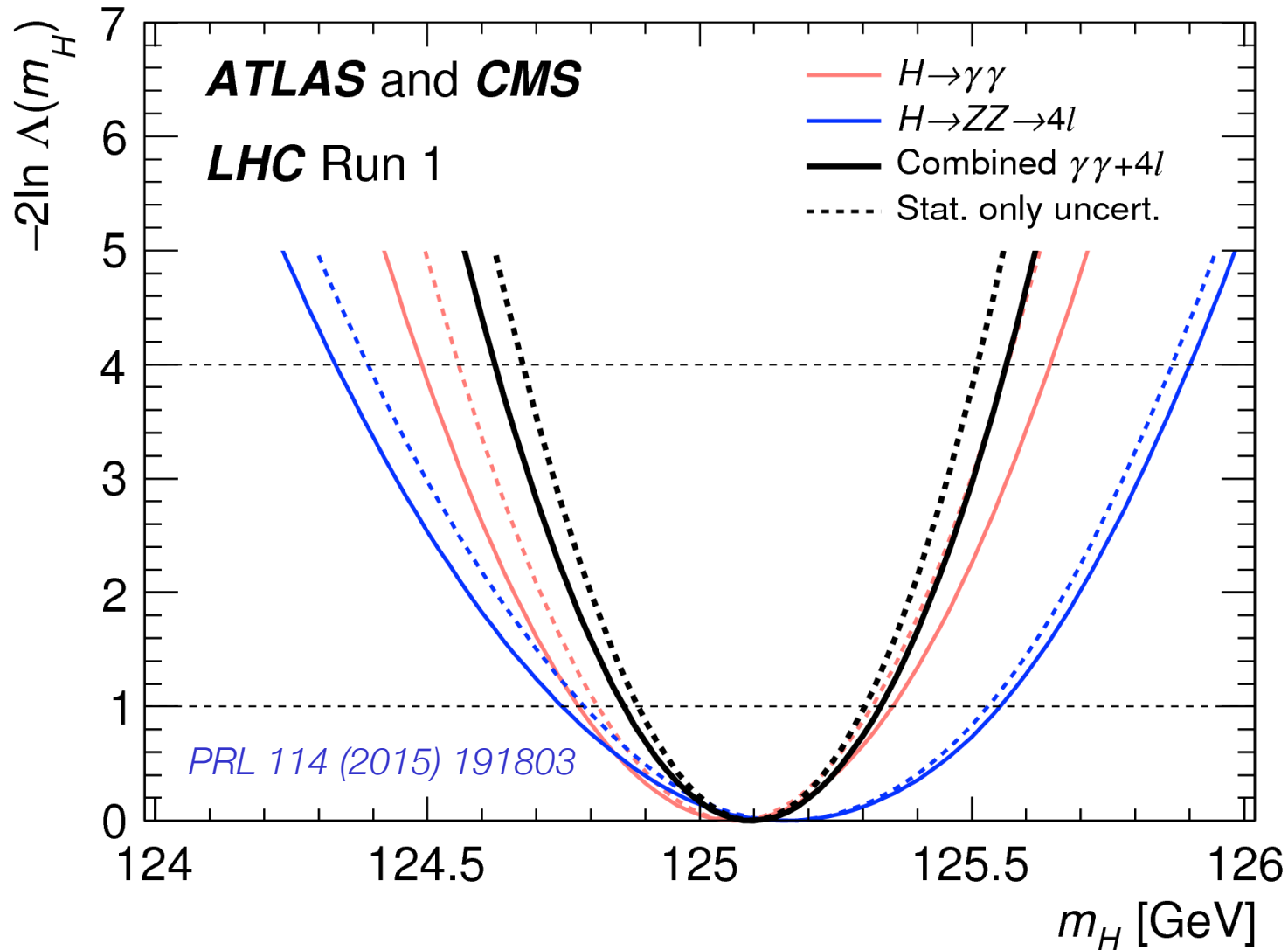
Phys. Rev. D. 90, 052004 (2014)



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Mass of Higgs boson measured with <0.2% precision

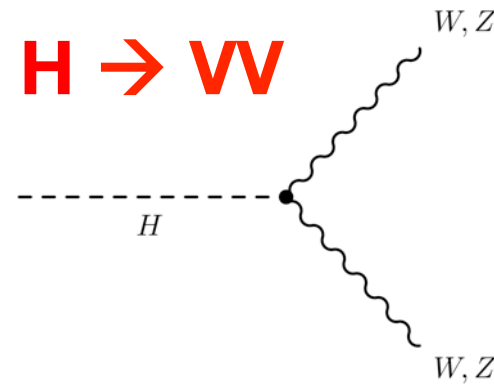
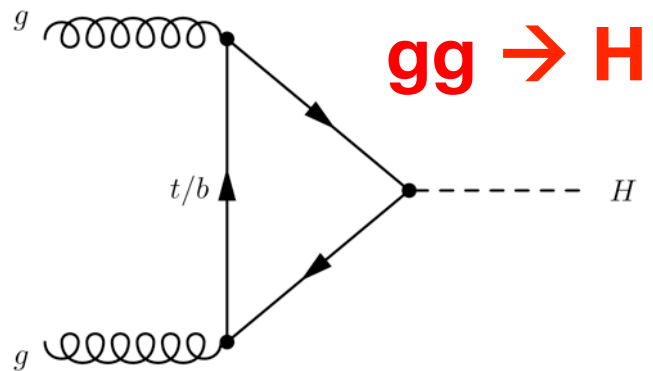
- Result from combination of ATLAS and CMS results



$$M_H = 125.09 \pm 0.24 \text{ GeV} [\pm 0.21 \text{ (stat.) } \pm 0.11 \text{ (syst.) }]$$

Today's focus - Higgs boson couplings

- Rich experimental area of Higgs properties: the Higgs coupling strength to other SM particles, e.g.



- All coupling strengths predicted by SM, given known Higgs boson mass
- Accessible in various combinations and admixtures. Large variety of ATLAS & CMS observed Higgs boson decay rates
- Powerful test of nature of Higgs boson: SM, or subtly different?

Higgs bosons – Alternatives to the SM Higgs boson

- **What else could the 125 GeV state be?**
Many alternative theories exist, for example
- Light CP-even $h(125)$ of a Two Higgs Doublet Model (h, H, H^\pm, A)
- Pseudo NG boson from higher energy theory (Composite Higgs)

In either case couplings of BSM $h(125)$ candidate (slightly) different from SM Higgs boson

- Can either pick a specific BSM model to interpret data, or develop a **generic framework to quantify possible deviations** in Higgs couplings from SM. Today will focus on generic framework

Outline of this presentation

① Introduction

② **Higgs boson phenomenology & interpretation framework**

③ Combination procedure & experimental inputs

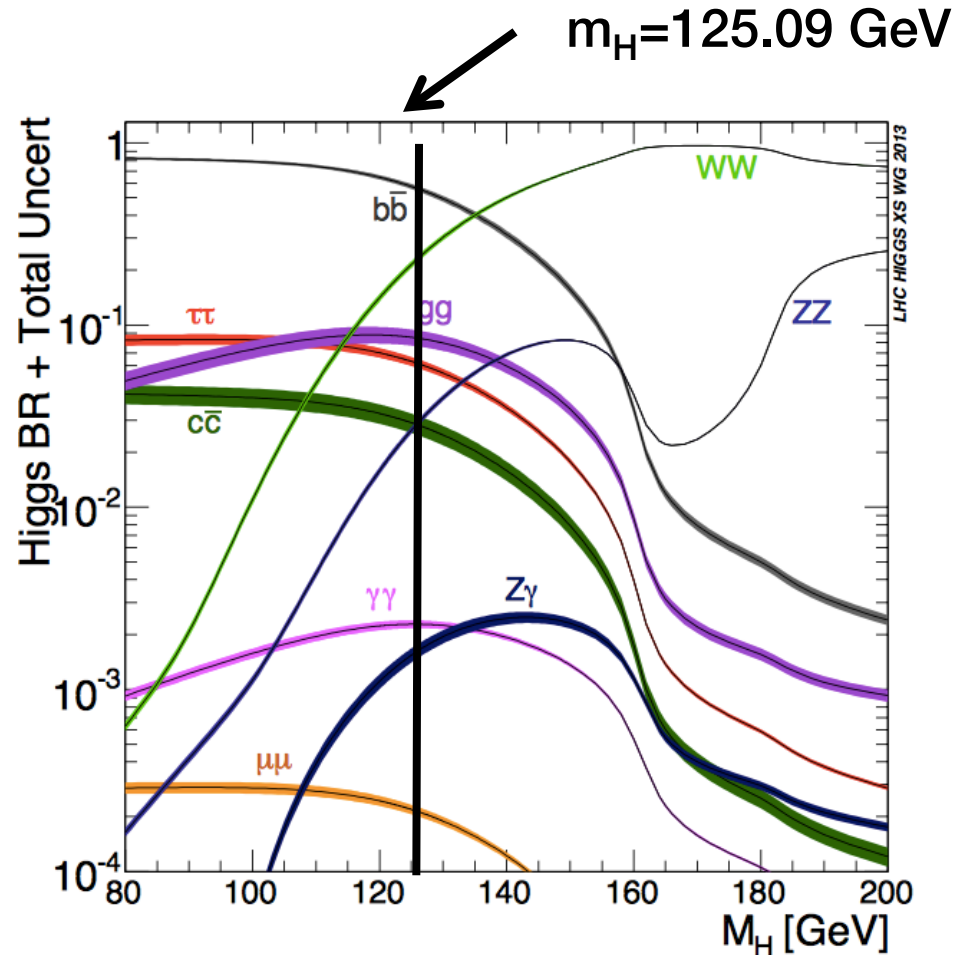
④ Signal strength measurements

⑤ Constraints on Higgs boson couplings

⑥ Improving on systematic uncertainties

⑦ Improving on Higgs signal models

Standard Model Higgs boson decays



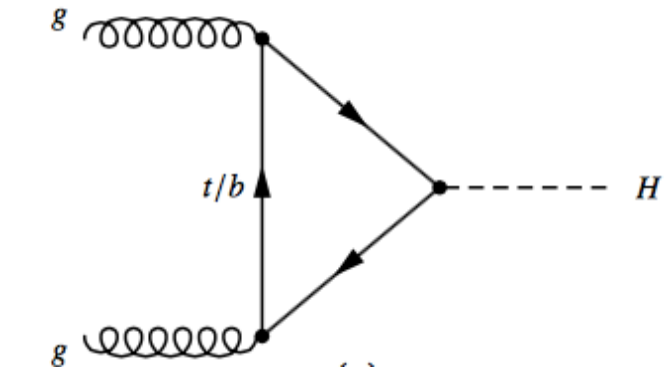
Decay channel	Branching ratio [%]
$H \rightarrow b\bar{b}$	57.5 ± 1.9
$H \rightarrow WW$	21.6 ± 0.9
$H \rightarrow gg$	8.56 ± 0.86
$H \rightarrow \tau\tau$	6.30 ± 0.36
$H \rightarrow c\bar{c}$	2.90 ± 0.35
$H \rightarrow ZZ$	2.67 ± 0.11
$H \rightarrow \gamma\gamma$	0.228 ± 0.011
$H \rightarrow Z\gamma$	0.155 ± 0.014
$H \rightarrow \mu\mu$	0.022 ± 0.001

SM BR theory uncertainties
2-5% for most important decays

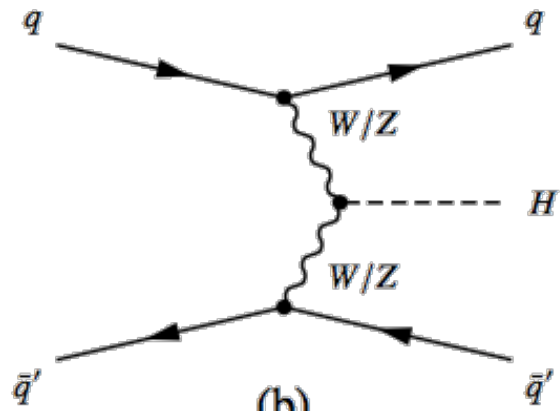
The natural width of the Higgs boson is expected to be very small (\ll resolution)

See “Handbook of LHC Higgs Cross Sections: 3. Higgs Properties”
(arXiv:1307.1347) for further details on Higgs phenomenology

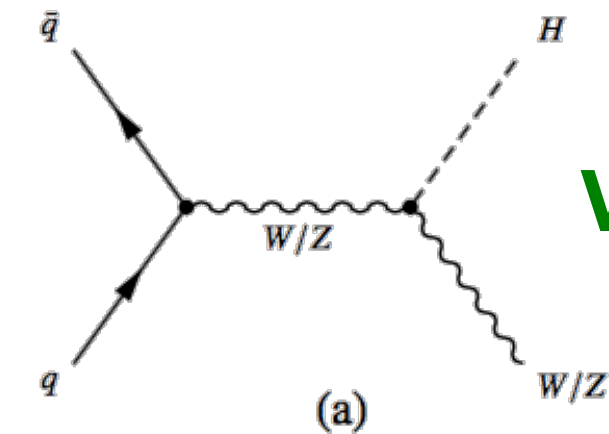
Higgs boson production in the SM



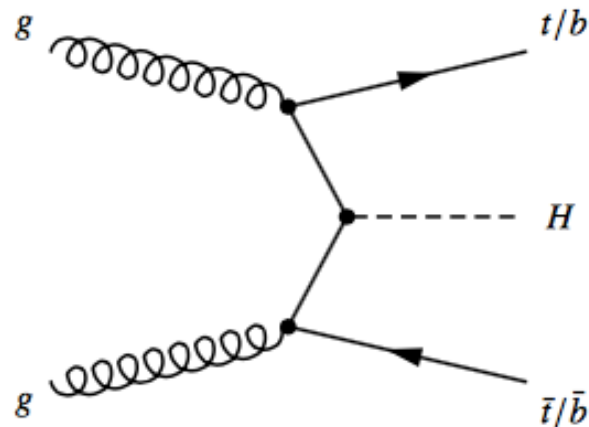
ggF



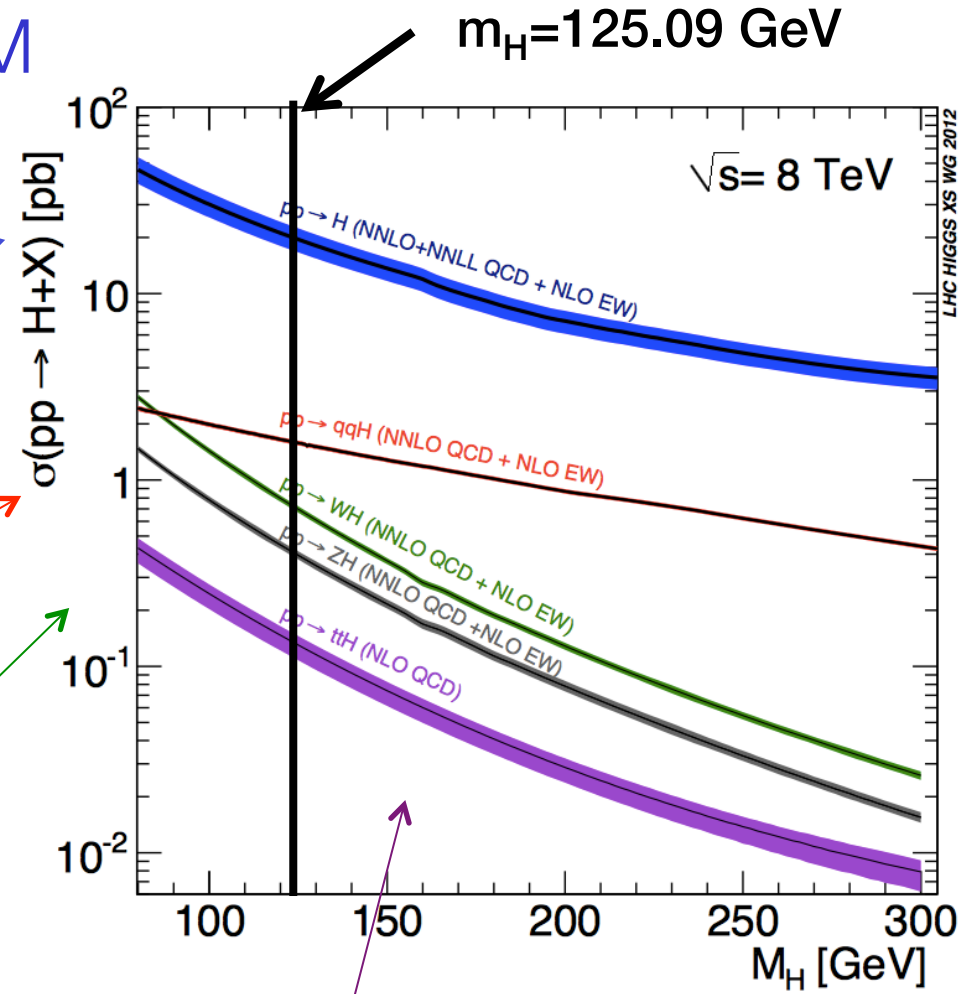
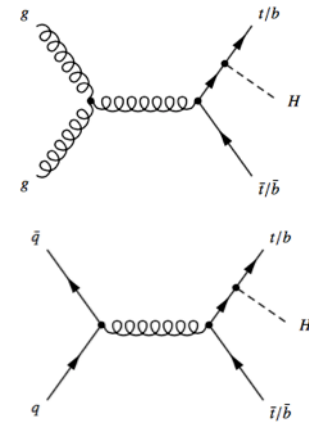
VBF



VH

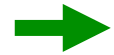
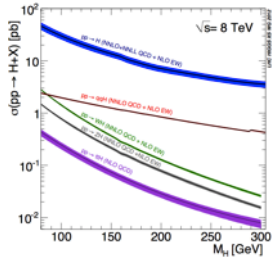


ttH



LHC HIGGS XS WG 2012

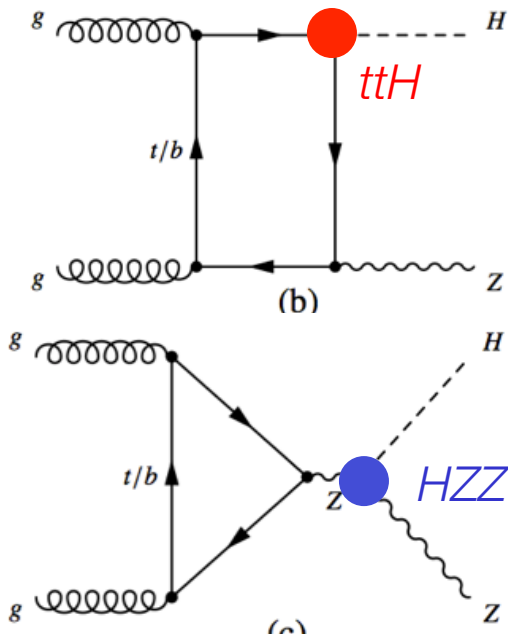
Higgs boson production in the SM



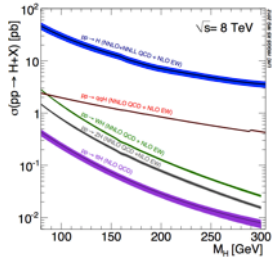
Production process	Cross section [pb]		Order of calculation
	$\sqrt{s} = 7 \text{ TeV}$	$\sqrt{s} = 8 \text{ TeV}$	
ggF	15.0 ± 1.6	19.2 ± 2.0	NNLO(QCD)+NLO(EW)
VBF	1.22 ± 0.03	1.58 ± 0.04	NLO(QCD+EW)+~NNLO(QCD)
WH	0.577 ± 0.016	0.703 ± 0.018	NNLO(QCD)+NLO(EW)
ZH	0.334 ± 0.013	0.414 ± 0.016	NNLO(QCD)+NLO(EW)
$[ggZH]$	0.023 ± 0.007	0.032 ± 0.010	NLO(QCD)
bbH	0.156 ± 0.021	0.203 ± 0.028	5FS NNLO(QCD) + 4FS NLO(QCD)
ttH	0.086 ± 0.009	0.129 ± 0.014	NLO(QCD)
tH	0.012 ± 0.001	0.018 ± 0.001	NLO(QCD)
	17.4 ± 1.6	22.3 ± 2.0	

Gluon-initiated ZH production represents ~8% of total ZH cross-section, has harder p_T distribution

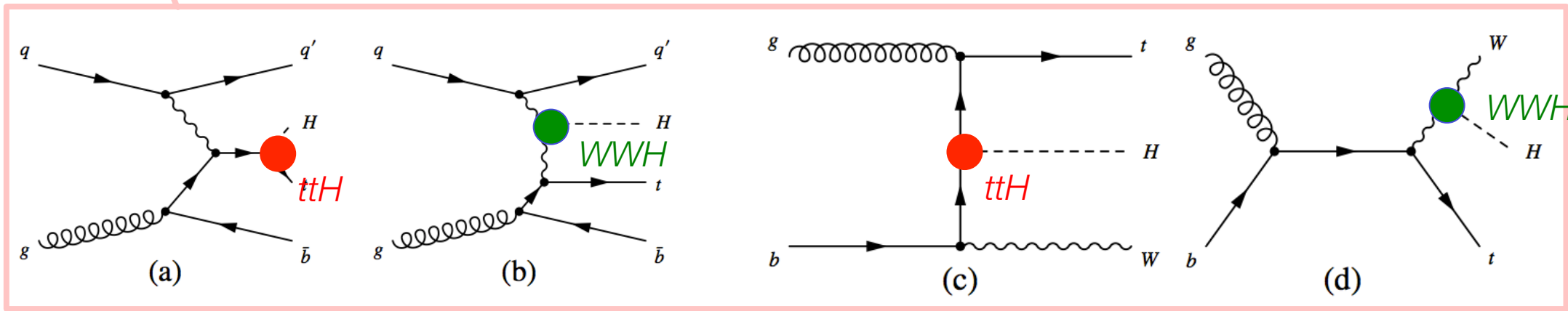
Modeled separately because Higgs coupling structure of $gg \rightarrow ZH$ is different from $qq \rightarrow ZH$



Higgs boson production in the SM



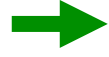
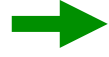
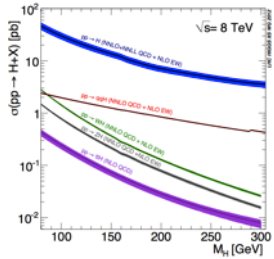
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tH	0.012 ± 0.001	0.018 ± 0.001	NLO(QCD)
Total	17.4 ± 1.6	22.3 ± 2.0	



Very small SM cross-section due to almost completely destructive interference

For opposite sign W/t Higgs couplings, $\sigma(tHq\bar{b})$ increases by factor 13 and $\sigma(WtH)$ by factor 6

Higgs boson production in the SM



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Diagrams similar to *ttH*,
but experimentally not really distinguishable from *ggF* and 100x smaller in SM

Higgs production and decay – Run 1 input measurements

Channel	References for individual publications	
	ATLAS	CMS
$H \rightarrow \gamma\gamma$	[51]	[52]
$H \rightarrow ZZ \rightarrow 4\ell$	[53]	[54]
$H \rightarrow WW$	[55, 56]	[57]
$H \rightarrow \tau\tau$	[58]	[59]
$H \rightarrow b\bar{b}$	[38]	[39]
$H \rightarrow \mu\mu$	[60]	[61]
$t\bar{t}H$ production	[28, 62, 63]	[65]

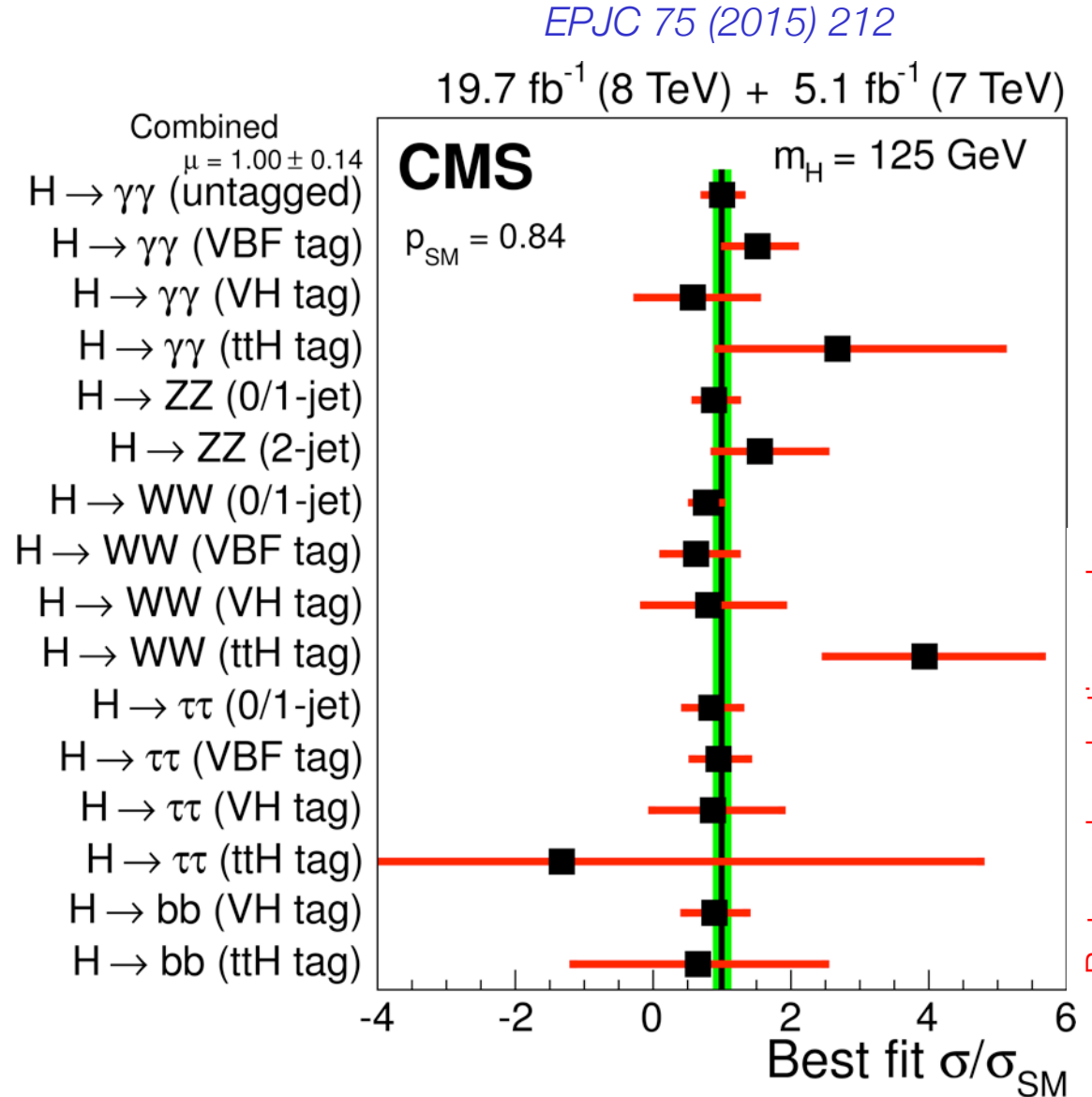
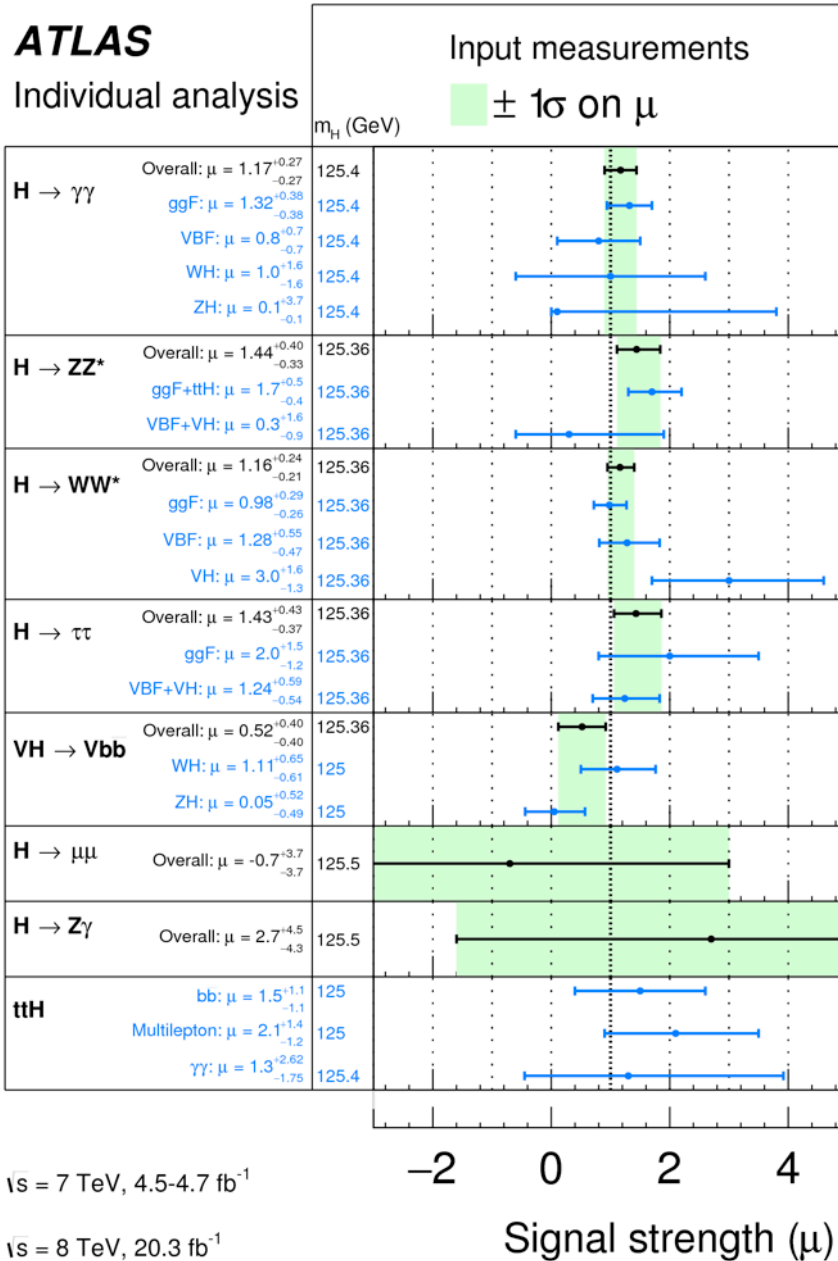
ATLAS, CMS Higgs signal strength measurements, and signal searches used in this combination are documented in 17 journal publications

- [28] ATLAS Collaboration, *Search for $H \rightarrow \gamma\gamma$ produced in association with top quarks and constraints on the Yukawa coupling between the top quark and the Higgs boson using data taken at 7 TeV and 8 TeV with the ATLAS detector*, *Phys. Lett.* **B740** (2015) 222, [arXiv:1409.3122 \[hep-ex\]](#).
- [38] ATLAS Collaboration, *Search for the $b\bar{b}$ decay of the Standard Model Higgs boson in associated (W/Z)H production with the ATLAS detector*, *JHEP* **1501** (2015) 069, [arXiv:1409.6212 \[hep-ex\]](#).
- [39] CMS Collaboration, *Search for the standard model Higgs boson produced in association with a W or a Z boson and decaying to bottom quarks*, *Phys. Rev. D* **89** (2014) 012003, [arXiv:1310.3687 \[hep-ex\]](#).
- [51] ATLAS Collaboration, *Measurement of Higgs boson production in the diphoton decay channel in pp collisions at center-of-mass energies of 7 and 8 TeV with the ATLAS detector*, *Phys. Rev.* **D90** (2014) 112015, [arXiv:1408.7084 \[hep-ex\]](#).
- [52] CMS Collaboration, *Observation of the Standard Model decay of the 125 GeV Higgs boson and measurement of its production cross section*, *Phys. J. C* **74** (2014) 3006, [arXiv:1407.0558 \[hep-ex\]](#).
- [53] ATLAS Collaboration, *Measurements of Higgs boson production and couplings in the four-lepton final state in pp collisions at center-of-mass energies of 7 and 8 TeV with the ATLAS detector*, *Phys. Rev.* **D91** (2015) 012006, [arXiv:1408.5191 \[hep-ex\]](#).
- [54] CMS Collaboration, *Measurement of the properties of the Higgs boson in the four-lepton final state*, *Phys. Rev. D* **89** (2014) 092007, [arXiv:1407.5553 \[hep-ex\]](#).
- [55] ATLAS Collaboration, *Observation and measurement of Higgs boson decays to WW^* with the ATLAS detector*, *Phys. Rev.* **D92** (2015) 012006, [arXiv:1412.2641 \[hep-ex\]](#).
- [56] ATLAS Collaboration, *Study of the Higgs boson decaying to WW^* produced in association with a weak boson with the ATLAS detector at the LHC*, *JHEP* **1508** (2015) 137, [arXiv:1506.06641 \[hep-ph\]](#).
- [57] CMS Collaboration, *Measurement of Higgs boson production and properties in the WW decay channel with leptonic final states*, *JHEP* **01** (2014) 096, [arXiv:1312.1129 \[hep-ex\]](#).
- [58] ATLAS Collaboration, *Evidence for the Higgs-boson Yukawa coupling to tau leptons with the ATLAS detector*, [arXiv:1501.04943 \[hep-ex\]](#).
- [59] CMS Collaboration, *Evidence for the 125 GeV Higgs boson decaying to a pair of τ leptons*, *JHEP* **05** (2014) 104, [arXiv:1401.5041 \[hep-ex\]](#).
- [60] ATLAS Collaboration, *Search for the Standard Model Higgs boson decay to $\mu^+\mu^-$ with the ATLAS detector*, *Phys. Lett.* **B738** (2014) 68, [arXiv:1406.7663 \[hep-ex\]](#).
- [61] CMS Collaboration, *Search for a standard model-like Higgs boson in the $\mu^+\mu^-$ and e^+e^- decay channels at the LHC*, *Phys. Lett.* **B** (2015), [arXiv:1410.6679 \[hep-ex\]](#).
- [62] ATLAS Collaboration, *Search for the Standard Model Higgs boson produced in association with top quarks and decaying into $b\bar{b}$ in pp collisions at $\sqrt{s} = 8$ TeV with the ATLAS detector*, *Eur. Phys. J. C* **75** (2015) 349, [arXiv:1503.05066 \[hep-ex\]](#).
- [63] ATLAS Collaboration, *Search for the associated production of the Higgs boson with a top quark pair in multi-lepton final states with the ATLAS detector*, ATLAS-CONF-2015-007 (2015).
- [65] CMS Collaboration, *Search for the associated production of the Higgs boson with a top-quark pair*, *JHEP* **09** (2014) 087, [arXiv:1408.1682 \[hep-ex\]](#).

Higgs production and decay – Run 1 measurements

Signal strength fits of individual experiments

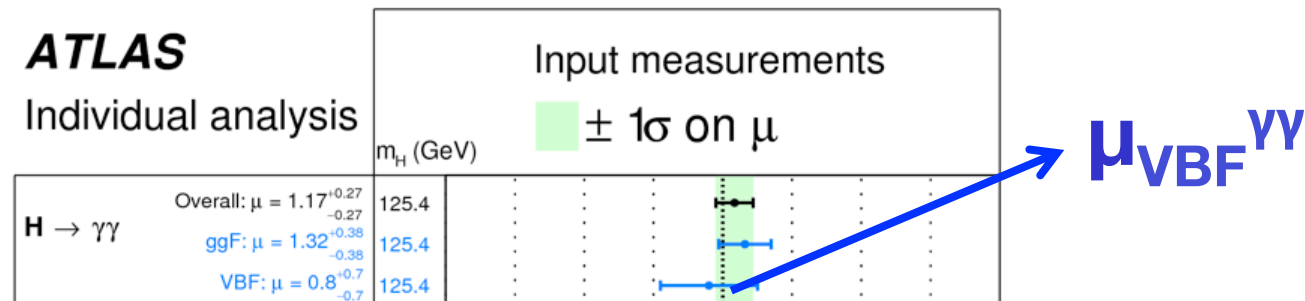
arXiv:1507.04548 [hep-ex]



Understanding signal strengths for process $i \rightarrow H \rightarrow f$

- Signal strength μ is observed rate normalized by SM prediction

$$\mu_i^f \equiv \frac{\sigma_i \cdot \text{BR}^f}{(\sigma_i \cdot \text{BR}^f)_{\text{SM}}} = \mu_i \times \mu^f$$



- Disentangling production (μ_i) & decay (μ_f) always **requires assumption of narrow Higgs width.**
- Additional assumptions required** when combining measurements, e.g

$$\mu_i = \frac{\sigma_i}{\sigma_i^{\text{SM}}} \quad \text{and} \quad \mu^f = \frac{\text{BR}^f}{\text{BR}_{\text{SM}}^f}$$

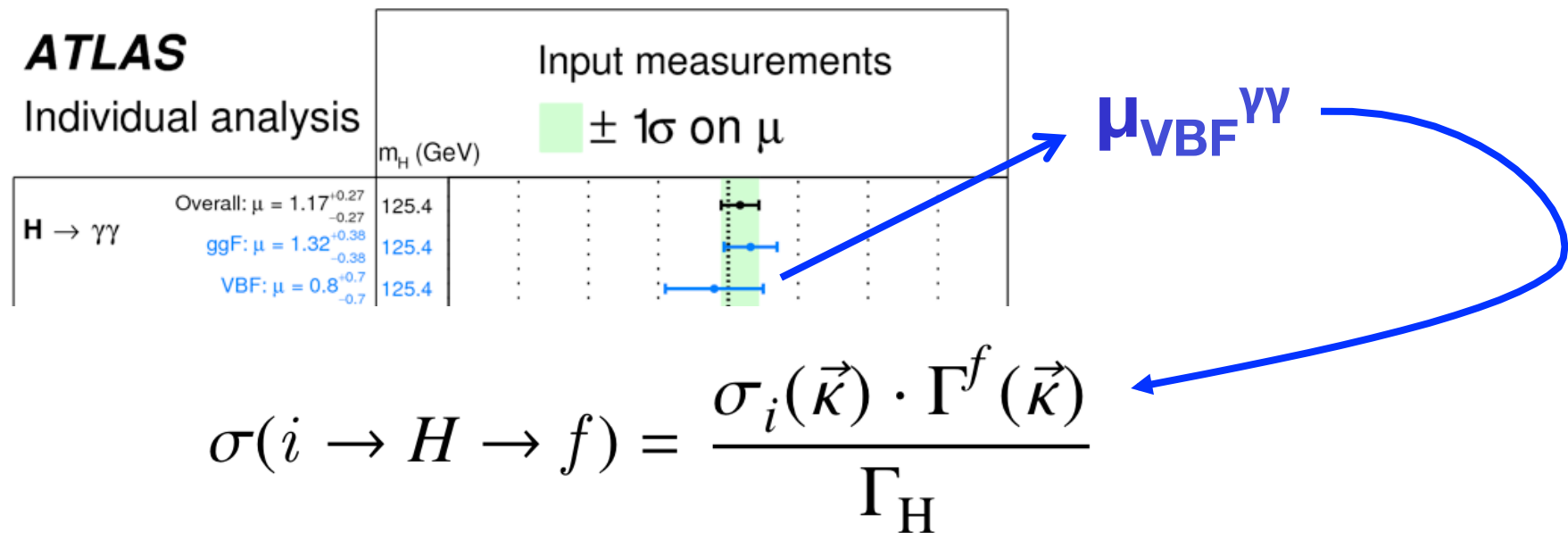
*Assumes SM value
of decay BRs*

*Assumes SM value
of production σ 's*

Interpretation beyond signal strengths – the κ framework

See “Handbook of LHC Higgs Cross Sections: 3. Higgs Properties” (arXiv:1307.1347) for further details κ framework

- Alternative one can disentangle deviations in production and decay with explicit modeling of Higgs width



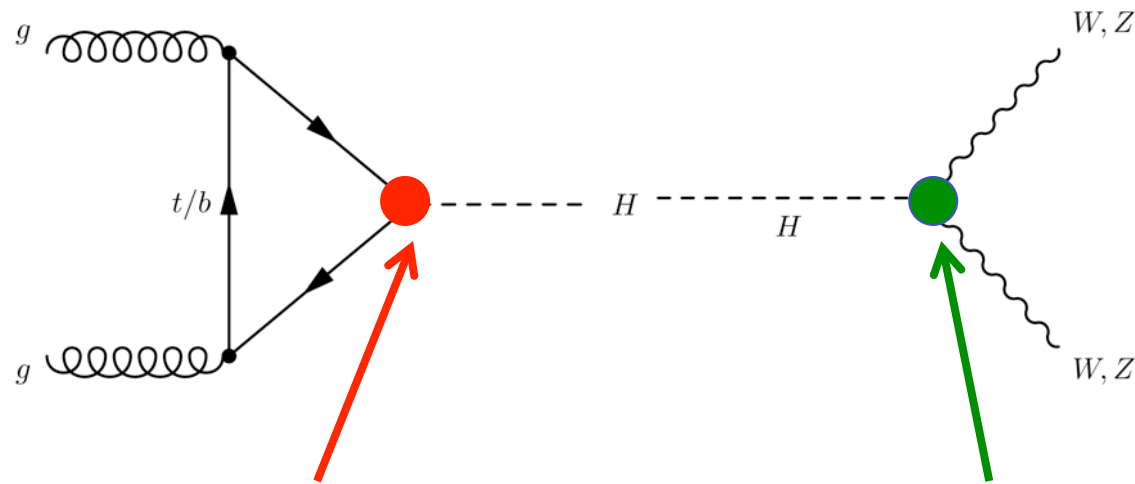
- Introduce functions κ_j** \rightarrow describe deviations from SM predictions.

$$\sigma_i = \kappa_i^2(\vec{K}) \cdot \sigma_i^{SM} \quad \Gamma^f = \kappa_f^2(\vec{K}) \cdot \Gamma^{f,SM}$$

so that for $\kappa_j=1 \rightarrow \sigma_i, \Gamma_f, \Gamma_H$ give SM prediction

Interpretation beyond signal strengths – the κ framework

- Parameters κ_j correspond to LO degrees of freedom
- Example for ggF production of $H \rightarrow W$



$$\sigma_{ggF} = (1.06 \kappa_t^2 + 0.01 \kappa_b^2 - 0.07 \kappa_b \kappa_t) \sigma_{ggF}(SM)$$

$$\Gamma_{W,Z} = \kappa_{W,Z}^2 \Gamma_{W,Z}(SM)$$

$$\sigma(i \rightarrow H \rightarrow f) = \frac{\sigma_i(\vec{k}) \cdot \Gamma^f(\vec{k})}{\Gamma_H}$$

NB: $\sigma_{ggF}(SM)$ from NNLO(QCD) + NLO(EW) calculation!

The κ framework – the total width

- Note that total H width scales all observed cross-sections

$$\sigma(i \rightarrow H \rightarrow f) = \frac{\sigma_i(\vec{k}) \cdot \Gamma^f(\vec{k})}{\Gamma_H}$$

- Since Γ_H is not yet directly measured with a meaningful precision, **must make an assumption on Γ_H** to interpret cross-sections in terms of Higgs couplings.
- E.g. in absence of BSM H decays (invisible, undetected etc...),** can assume SM width, adjusted by effect of κ -rescaled couplings

$$\Gamma_H(\vec{k}) = \kappa_H^2(\vec{k}) \cdot \Gamma_H^{\text{SM}}$$

$\kappa_H^2 \sim$

$$0.57 \cdot \kappa_b^2 + 0.22 \cdot \kappa_W^2 + 0.09 \cdot \kappa_g^2 + \\ 0.06 \cdot \kappa_\tau^2 + 0.03 \cdot \kappa_Z^2 + 0.03 \cdot \kappa_c^2 + \\ 0.0023 \cdot \kappa_\gamma^2 + 0.0016 \cdot \kappa_{Z\gamma}^2 + 0.00022 \cdot \kappa_\mu^2$$

Factors depend on

- Assumed value m_H ,
- Calculations of σ, Γ
- Kinematic selections

The kappa framework – the dictionary

Production	Loops	Interference	Multiplicative factor
$\sigma(ggF)$	✓	$b-t$	$\kappa_g^2 \sim 1.06 \cdot \kappa_t^2 + 0.01 \cdot \kappa_b^2 - 0.07 \cdot \kappa_t \kappa_b$
$\sigma(VBF)$	–	–	$\sim 0.74 \cdot \kappa_W^2 + 0.26 \cdot \kappa_Z^2$
$\sigma(WH)$	–	–	$\sim \kappa_W^2$
$\sigma(qq/qg \rightarrow ZH)$	–	–	$\sim \kappa_Z^2$
$\sigma(gg \rightarrow ZH)$	✓	$Z-t$	$\sim 2.27 \cdot \kappa_Z^2 + 0.37 \cdot \kappa_t^2 - 1.64 \cdot \kappa_Z \kappa_t$
$\sigma(ttH)$	–	–	$\sim \kappa_t^2$
$\sigma(gb \rightarrow WtH)$	–	$W-t$	$\sim 1.84 \cdot \kappa_t^2 + 1.57 \cdot \kappa_W^2 - 2.41 \cdot \kappa_t \kappa_W$
$\sigma(qb \rightarrow tHq)$	–	$W-t$	$\sim 3.4 \cdot \kappa_t^2 + 3.56 \cdot \kappa_W^2 - 5.96 \cdot \kappa_t \kappa_W$
$\sigma(bbH)$	–	–	$\sim \kappa_b^2$
Partial decay width			
Γ^{ZZ}	–	–	$\sim \kappa_Z^2$
Γ^{WW}	–	–	$\sim \kappa_W^2$
$\Gamma^{\gamma\gamma}$	✓	$W-t$	$\kappa_\gamma^2 \sim 1.59 \cdot \kappa_W^2 + 0.07 \cdot \kappa_t^2 - 0.66 \cdot \kappa_W \kappa_t$
$\Gamma^{\tau\tau}$	–	–	$\sim \kappa_\tau^2$
Γ^{bb}	–	–	$\sim \kappa_b^2$
$\Gamma^{\mu\mu}$	–	–	$\sim \kappa_\mu^2$
Total width for $BR_{BSM} = 0$			
Γ_H	✓	–	$\kappa_H^2 \sim 0.57 \cdot \kappa_b^2 + 0.22 \cdot \kappa_W^2 + 0.09 \cdot \kappa_g^2 + 0.06 \cdot \kappa_\tau^2 + 0.03 \cdot \kappa_Z^2 + 0.03 \cdot \kappa_c^2 + 0.0023 \cdot \kappa_\gamma^2 + 0.0016 \cdot \kappa_{Z\gamma}^2 + 0.0001 \cdot \kappa_s^2 + 0.00022 \cdot \kappa_\mu^2$

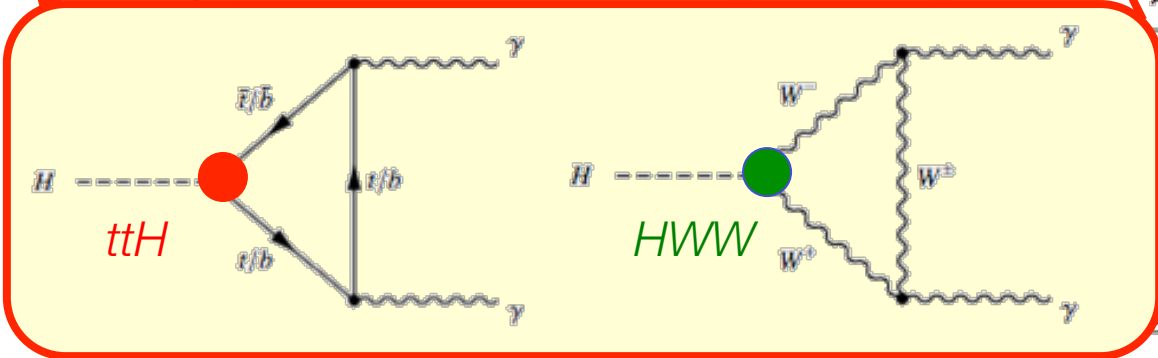
The kappa framework – the dictionary

Production	Loops	Interference	M
$\sigma(ggF)$	✓	$b-t$	κ_t
$\sigma(VBF)$	–	–	–
$\sigma(WH)$	–	–	–
$\sigma(qq/qg \rightarrow ZH)$	–	–	–
$\sigma(gg \rightarrow ZH)$	✓	$Z-t$	–
$\sigma(ttH)$	–	–	–
$\sigma(gb \rightarrow WtH)$	–	$W-t$	–
$\sigma(qb \rightarrow tHq)$	–	$W-t$	–
$\sigma(bbH)$	–	–	–
Partial decay width			
Γ^{ZZ}	–	–	–
Γ^{WW}	–	–	–
$\Gamma^{\gamma\gamma}$	✓	$W-t$	–
$\Gamma^{\tau\tau}$	–	–	–
Γ^{bb}	–	–	–
$\Gamma^{\mu\mu}$	–	–	–

Processes with **interference** allow (in principle) to measure the relative sign of coupling strengths

Since all interferences considered always involve the top quark, **choose sign of top coupling positive** by construction (no loss of generality)

→ can allow data to constrain sign of b,W,Z coupling w.r.t top quark coupling



$$\begin{aligned} \kappa_W^2 &\sim \kappa_W^2 \\ \kappa_\gamma^2 &\sim 1.59 \cdot \kappa_W^2 + 0.07 \cdot \kappa_t^2 - 0.66 \cdot \kappa_W \kappa_t \\ \kappa_\tau^2 &\sim \kappa_\tau^2 \\ \kappa_b^2 &\sim \kappa_b^2 \\ \kappa_\mu^2 &\sim \kappa_\mu^2 \end{aligned}$$

$$\begin{aligned} &0.57 \cdot \kappa_b^2 + 0.22 \cdot \kappa_W^2 + 0.09 \cdot \kappa_g^2 + \\ &+ 0.06 \cdot \kappa_\tau^2 + 0.03 \cdot \kappa_Z^2 + 0.03 \cdot \kappa_C^2 + \\ &+ 0.0023 \cdot \kappa_\gamma^2 + 0.0016 \cdot \kappa_{Z\gamma}^2 + \\ &+ 0.0001 \cdot \kappa_S^2 + 0.00022 \cdot \kappa_\mu^2 \end{aligned}$$

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- ③ Combination procedure & experimental inputs**
 - ④ Signal strength measurements
 - ⑤ Constraints on Higgs boson couplings
 - ⑥ Most generic parametrizations

Signal strength measurements by ATLAS and CMS

Each experiment has $O(15)$ signal strength measurements focusing on a wide variety of production and decay models

Measurements of μ_i^f entering combined analysis *Dominated by ggF* *Includes gg → ZH* *Includes tH*

Decay / Production	Untagged	VBF	VH	ttH
$H \rightarrow \gamma\gamma$	Green	Green	Green	Green
$H \rightarrow ZZ \rightarrow 4l$	Green	Green	Green	Green
$H \rightarrow WW \rightarrow 2l2\nu$	Green	Green	Green	Green
$H \rightarrow \tau\tau$	Green	Green	Green	Green
$H \rightarrow bb$	White	White	Green	Green
$H \rightarrow \mu\mu$	Green	Green	White	White
$H \rightarrow \text{invisible}$	White	White	White	White

Difficult due to large backgrounds

CMS measurement exists, but not in time for combination

Extremely small cross-section

CMS and ATLAS also performed **off-shell measurements**

in WW/ZZ that allow to constrain Higgs width with assumptions

Not included in this combination
(was included in ATLAS combination)

CMS and ATLAS also performed searches for $H \rightarrow$ invisible in VH, VBF production modes

Not included in this combination
(included in CMS combination, and separate combination by ATLAS)

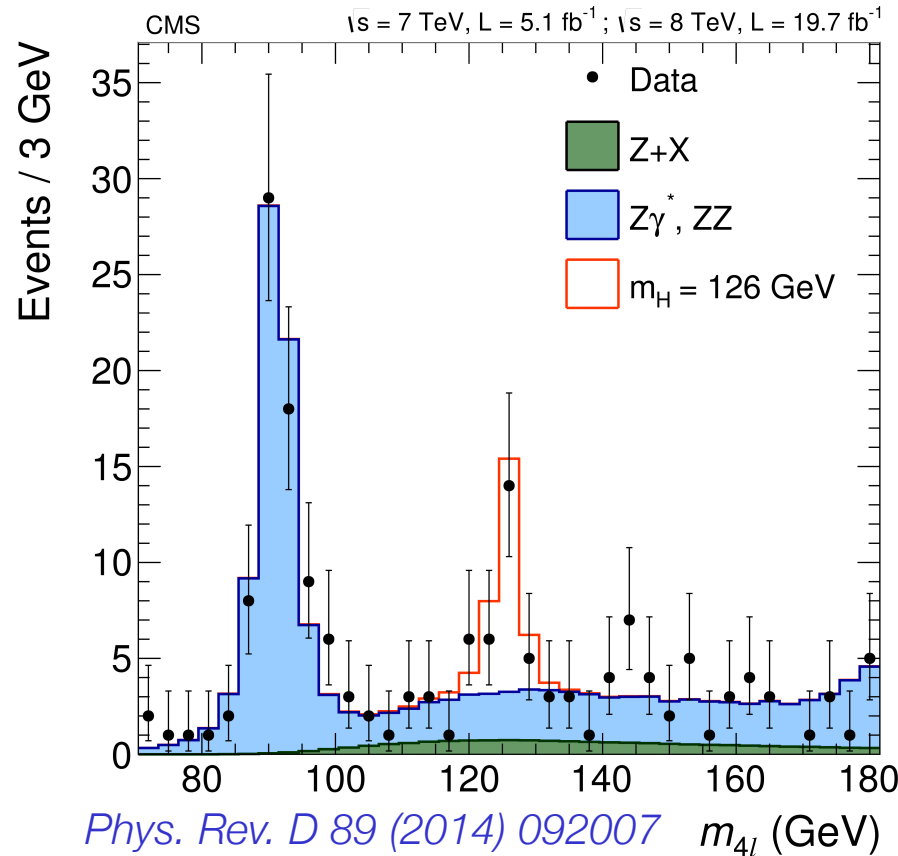
combined analysis by ggF

Decay / Production	Untagged	VBF	VH	ttH
$H \rightarrow \gamma\gamma$	Green	Green	Green	Green
$H \rightarrow ZZ \rightarrow 4l$	Green	Green	Green	Green
$H \rightarrow WW \rightarrow 2l2\nu$	Green	Green	Green	Green
$H \rightarrow \tau\tau$	Green	Green	Green	Green
$H \rightarrow bb$	White	White	Green	Green
$H \rightarrow \mu\mu$	Green	Green	White	White
$H \rightarrow$ invisible	White	Green	Green	White

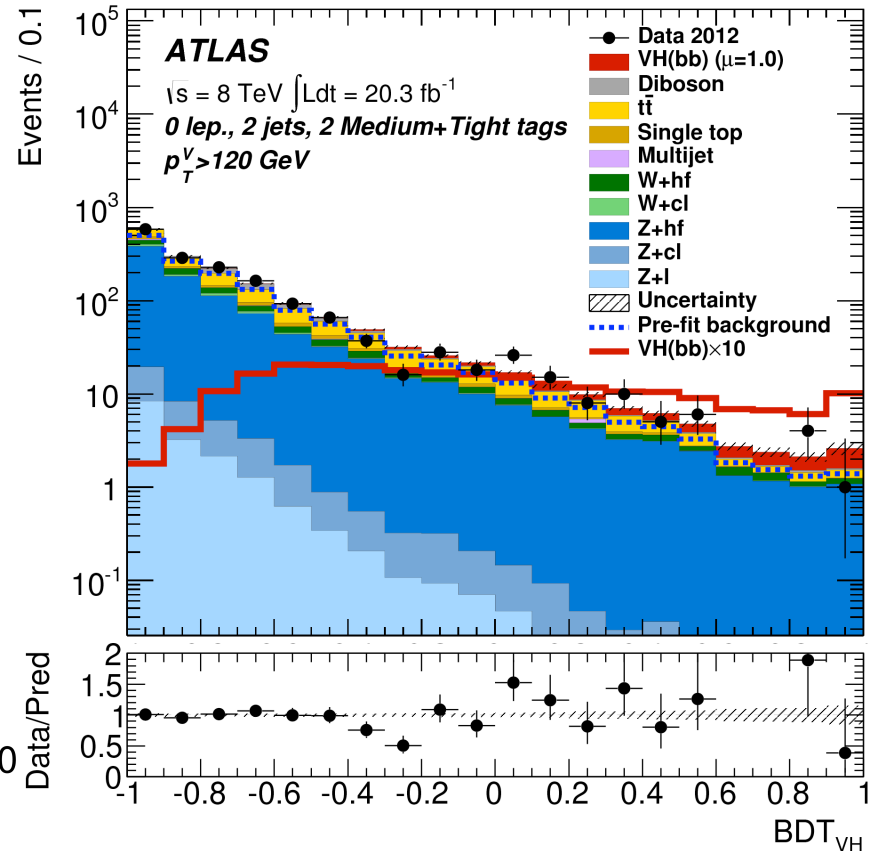
Anatomy of a single measurement

- Every measurement consists of one or more signal regions, designed to selected target Higgs production/decay
- Distribution of a (multivariate) discriminant is interpreted in terms of sum of signal and background contributions

“Low bkg / high mass resol.” ($H \rightarrow ZZ^*$)



“High bkg / worse resol.” ($WH \rightarrow bb$)



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Profile likelihood formalism for (systematic) uncertainties

- Build likelihood function for *each* signal, control region of the data

$$L(\vec{N} | \vec{\mu}_i, \vec{\mu}_f, \vec{\theta}) = \prod_{k=0, nbins} Poisson \left(N_k | \sum_{i,f} \mu_i \cdot \mu^f \cdot S_{i,k}^f(\vec{\theta}) + \sum_m B_m(\vec{\theta}) \right)$$

i → *H* → *f* Background

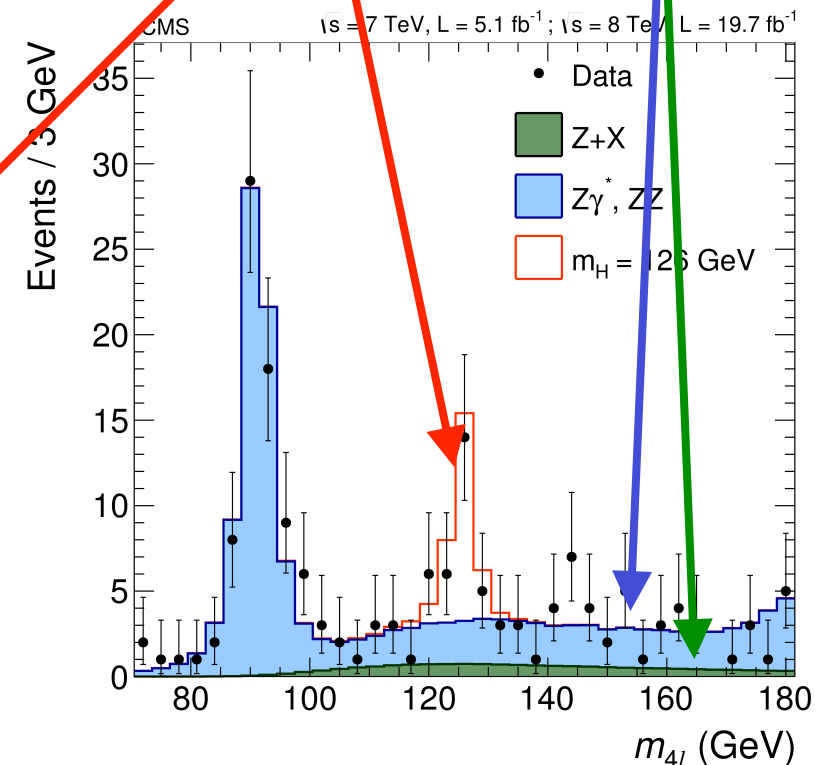
Inclusive SM cross-section

Acceptance (from MC)

Efficiency (from MC)

Higgs BR

Luminosity

$$\mathcal{L}(k) \times \left\{ \sigma_i^{SM} \times A_i^f(k) \times \varepsilon_i^f(k) \times BR_{SM}^f \right\}$$


Profile lik

- Build lik

$$L(\vec{N} | \vec{\mu})$$

Assume SM Higgs boson for acceptance & efficiency

Production process	Event generator	
	ATLAS	CMS
ggF *	POWHEG [30–34]	POWHEG
VBF	POWHEG	POWHEG
WH	PYTHIA8 [35]	PYTHIA6.4 [36]
ZH (qq → ZH or qg → ZH)	PYTHIA8	PYTHIA6.4
ggZH (gg → ZH)	POWHEG	See text
ttH	POWHEL [44]	PYTHIA6.4
tHq (qb → tHq)	MADGRAPH [46]	AMC@NLO [29]
tHW (gb → tHW)	AMC@NLO	AMC@NLO
bbH	PYTHIA8	PYTHIA6, AMC@NLO

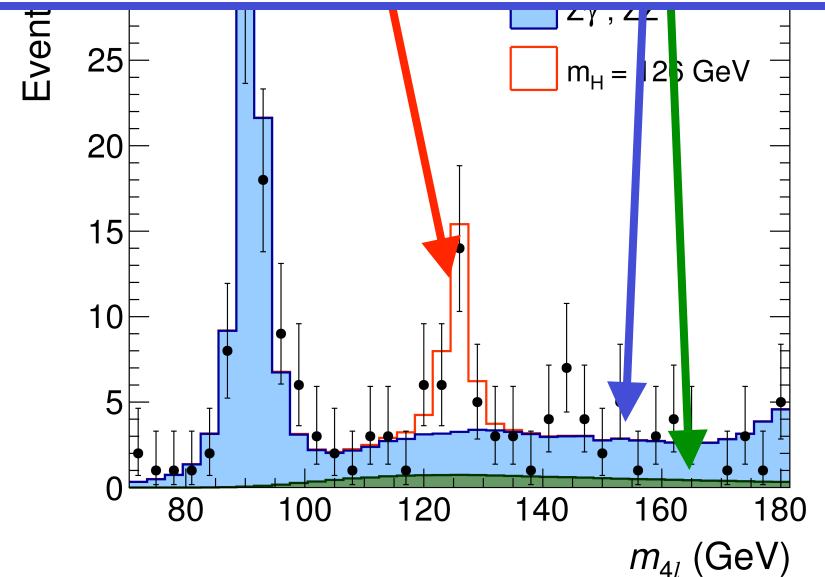
(* Higgs p_T distribution of ggF production reweighted to match HiRes 2.1 calculation (includes NNLO and NNLL QCD corrections)

Inclus

Luminosity

$$\mathcal{L}(k) \times \left\{ \sigma_i^{\text{SM}} \times A_i^f(k) \times \varepsilon_i^f(k) \times \text{BR}_{\text{SM}}^f \right\}$$

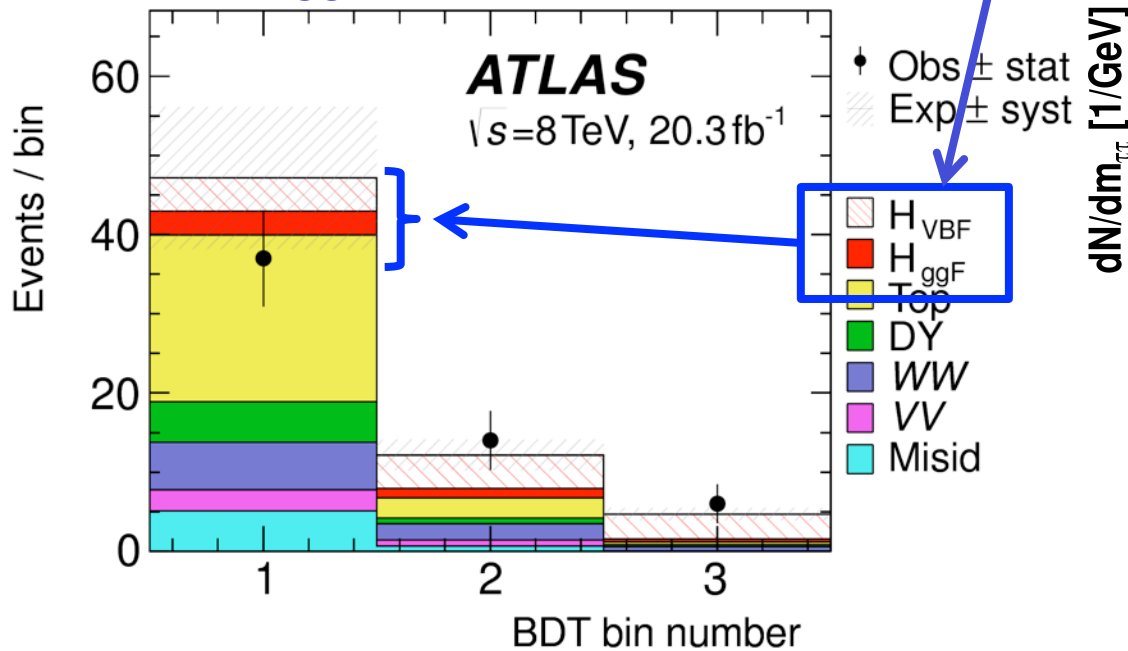
Higgs BR



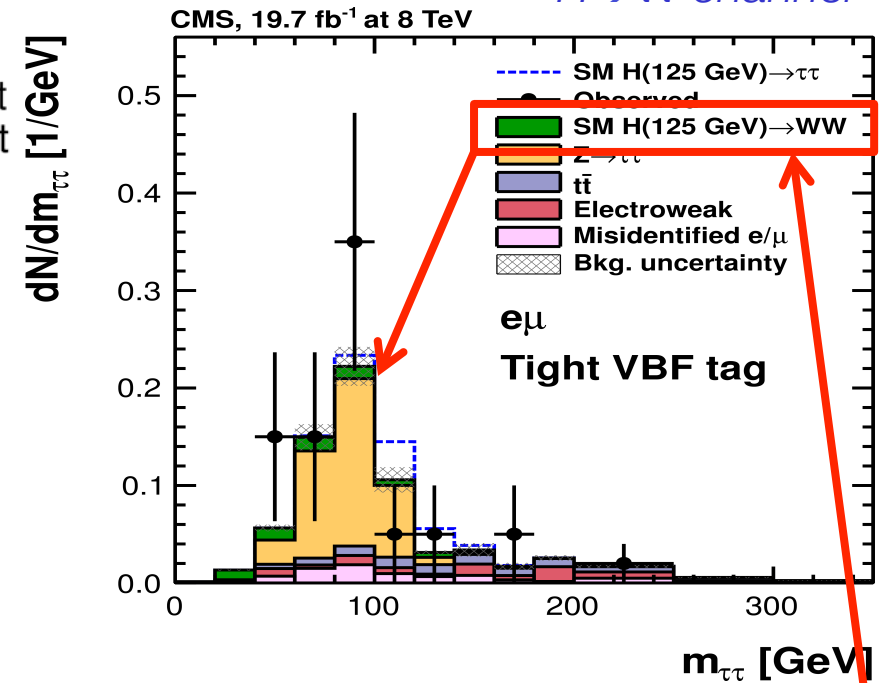
Decomposition of Higgs signal contributions in channels

- Channels selections hardly ever 100% pure in production process (especially ‘untagged’) → separately model distributions from all contributing Higgs production processes

“Untagged” $H \rightarrow WW$ channel

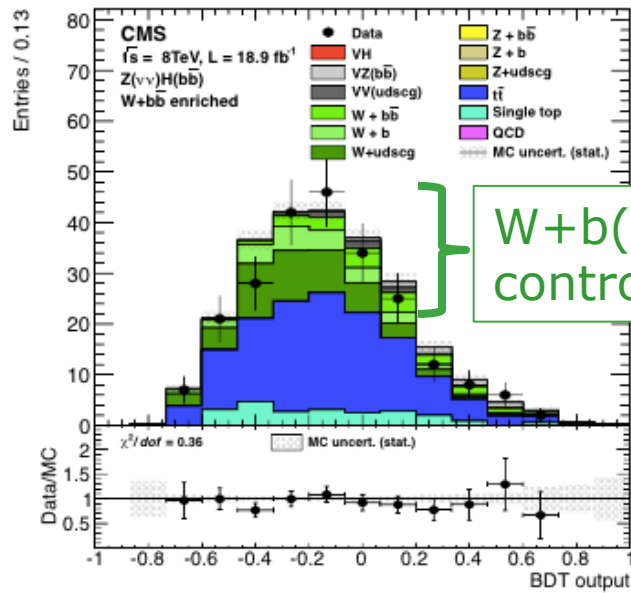


$H \rightarrow \tau\tau$ channel

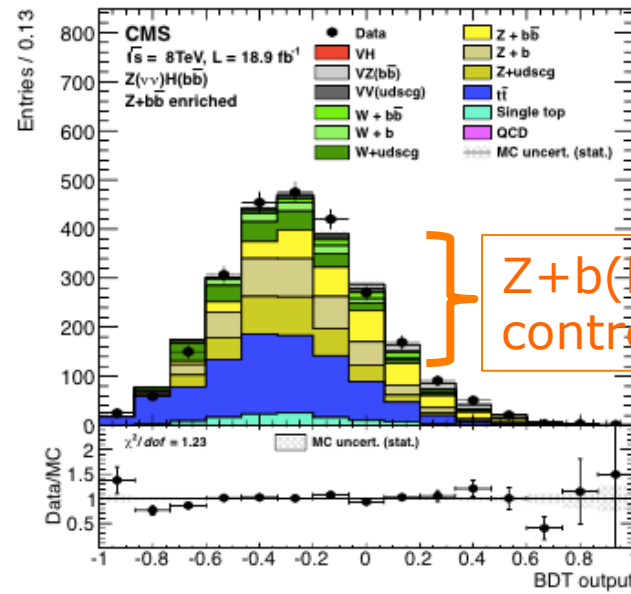


- Some channels also not 100% pure in decay mode (e.g. $H \rightarrow WW$ selection has contributions of $H \rightarrow \tau\tau$ decays). Interpret such contributions as Higgs signal (of appropriate type) in coupling analysis

Measurements of backgrounds often data-driven using control regions

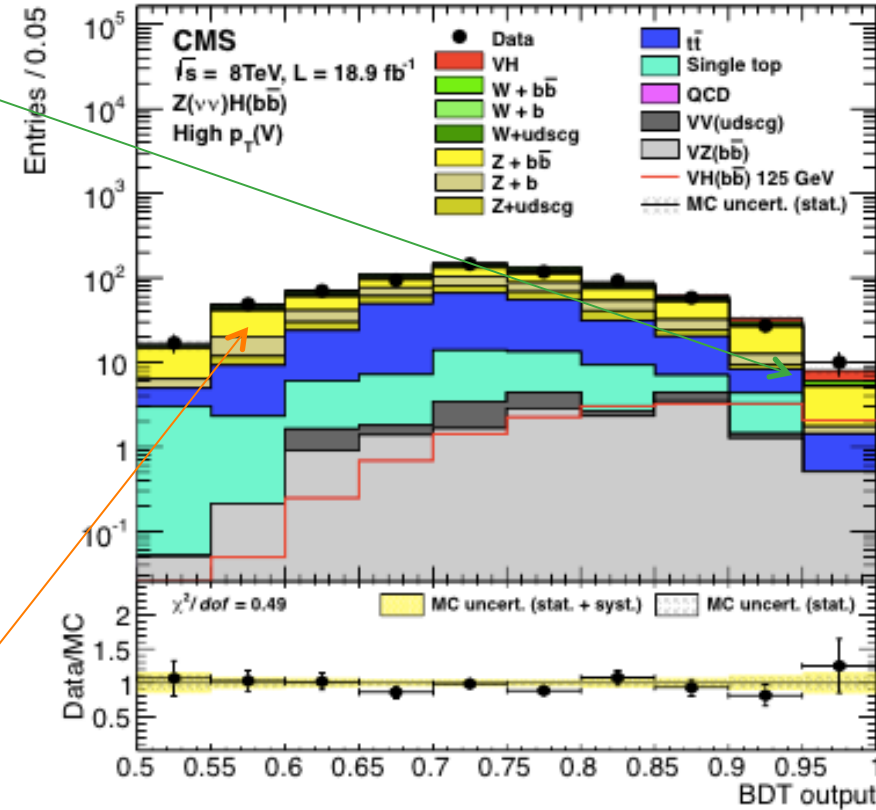


W+b(b) enriched control region



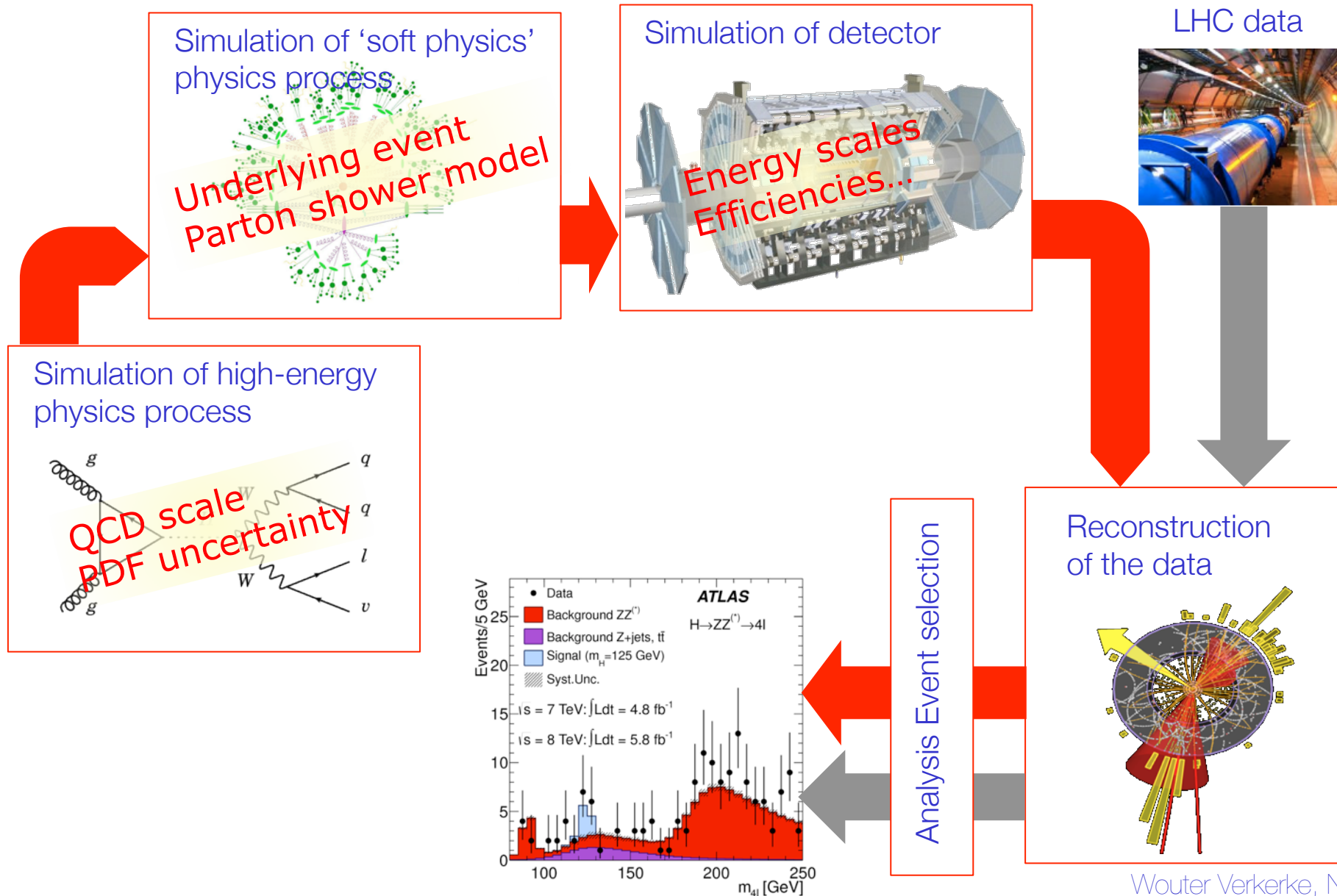
Z+b(b) enriched control region

PRD 89 (2014) 012003



Most expected distributions subject to **systematic uncertainties**

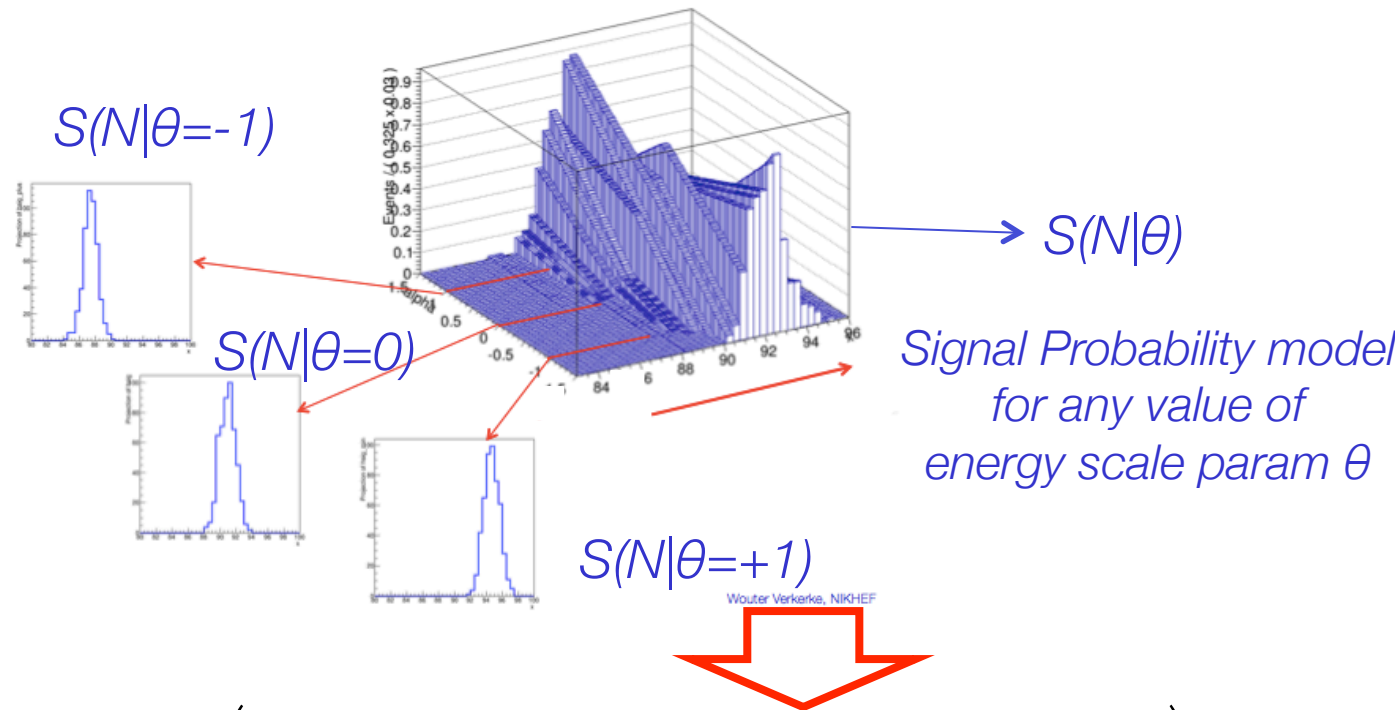
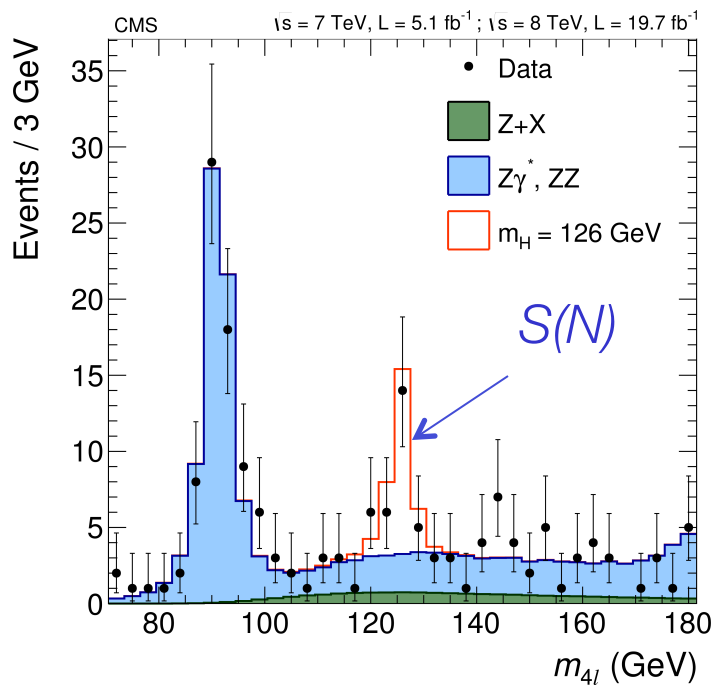
- Expected distributions mostly derived from simulation chain



Profile likelihood formalism for (systematic) uncertainties

- Extend description of each signal/background distribution** so that it can *describe distribution under a wide range of parameters* for which the true values are unknown (energy scales, QCD scales...)

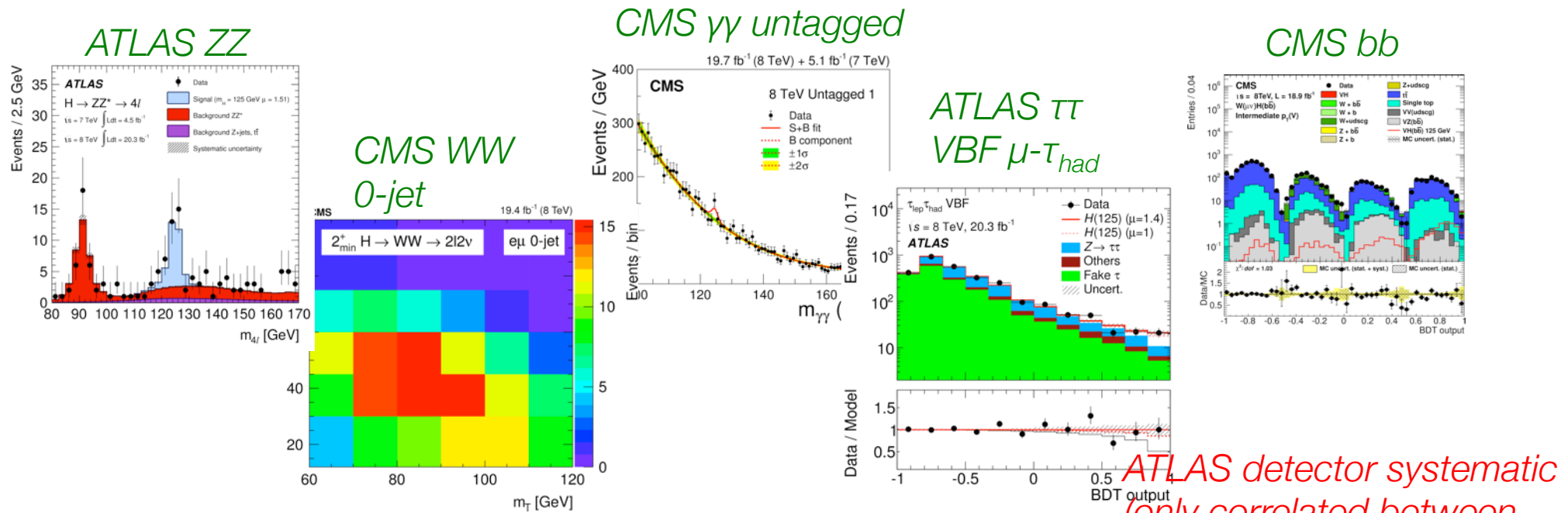
Illustration: modeling of energy scale uncertainty



$$L(\vec{N} | \vec{\mu}_i, \vec{\mu}_f, \vec{\theta}) = \prod_{k=0, nbins} \text{Poisson} \left(N_k | \sum_{i,f} \mu_i \cdot \mu_f \cdot S_{i,k}^f(\vec{\theta}) + \sum_m B_m(\vec{\theta}) \right)$$

Profile likelihood formalism for (systematic) uncertainties

- Correlated parameters as needed between channels, experiments



ATLAS detector systematic (only correlated between ATLAS measurements)

$$L_{ATLAS,ZZ}(N|\mu, \theta_{QCDscale}, \theta_{ATLSDet}, \theta, \theta, \theta, \dots)$$

$$L_{ATLAS,\tau\tau}(N|\mu, \theta_{QCDscale}, \theta_{ATLSDet}, \theta, \theta, \theta, \dots)$$

$$L_{CMS,WW}(N|\mu, \theta_{QCDscale}, \theta_{CMSDet}, \theta, \theta, \theta, \dots)$$

Fully correlated theory uncertainty

Correlated uncertainties in ATLAS/CMS combination

- Full combination describes ~580 signal regions & control regions from both experiments. Grand total of ~4200 nuisance parameters, related to (systematic) uncertainties
- Correlation strategy of nuisance parameters a delicate and complicated task
 - **Detector systematic uncertainties** → follow strategy of ATLAS and CMS internal combinations (**generally correlated within, not between experiments**)
 - **Signal theory uncertainties** (QCD scales, PDF, UEPS) on **inclusive cross-sections** generally **correlated between experiments**.
 - **Signal theory uncertainties on acceptance and selection efficiency** are **uncorrelated between experiments**, as these are small and estimation procedures are generally different.
 - **PDF uncertainties on signal cross-sections uncorrelated between channels**, except WH/ZH = correlated (effect of ignoring other correlations is $\leq 1\%$)
 - **No correlations assumed between Higgs BRs** (except for WW/ZZ).
Effect of ignoring correlations shown to be generally small, except for a few specific measurements, in which case full correlation structure is retained

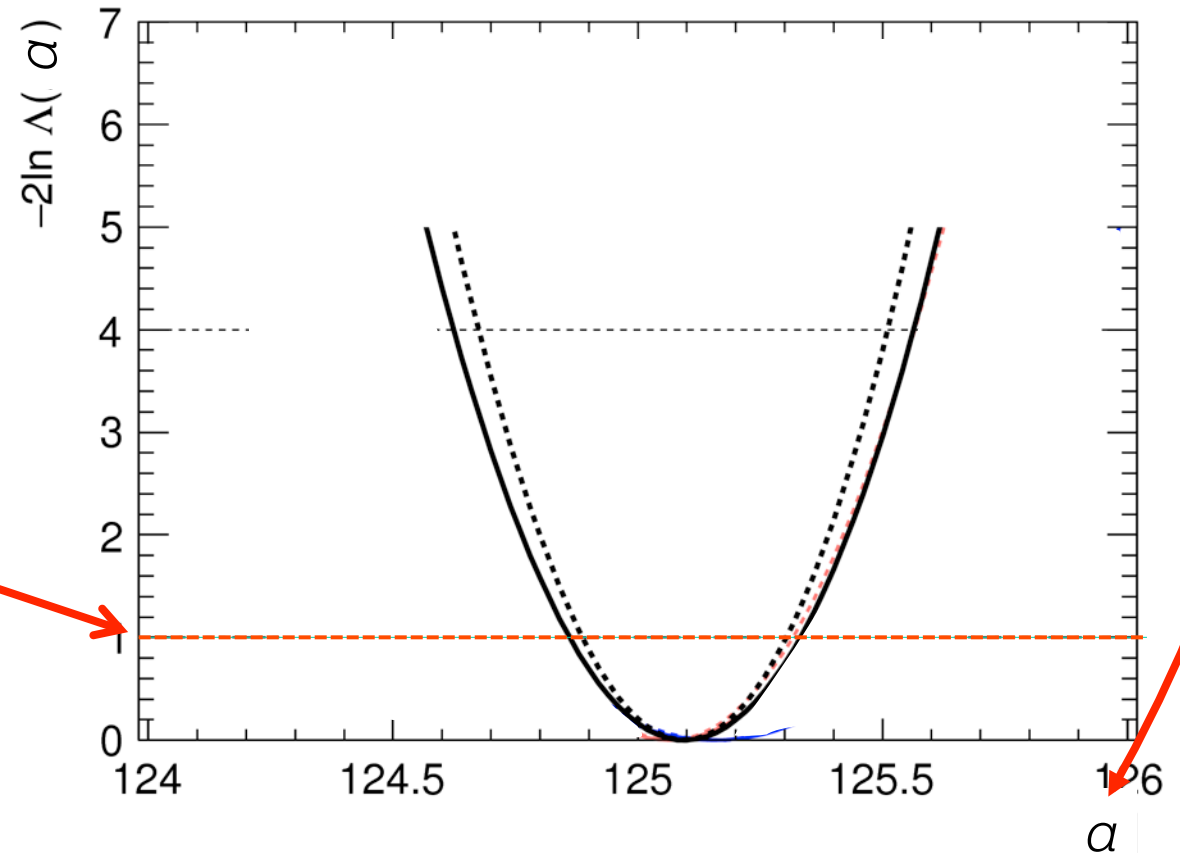
Statistical treatment – profile likelihood

Θ : vector of ~4200 nuisance parameters

- From $L(\text{ATLAS+CMS})$ construct the **profile likelihood** for a statement on the parameter(s) of interest α

$$\Lambda(\vec{\alpha}) = \frac{L(\vec{\alpha}, \hat{\vec{\theta}}(\vec{\alpha}))}{L(\hat{\vec{\alpha}}, \hat{\vec{\theta}})}$$

- 68% Confidence interval defined by a rise of 1 unit in $\Lambda(\alpha)$ (asymptotic limit)

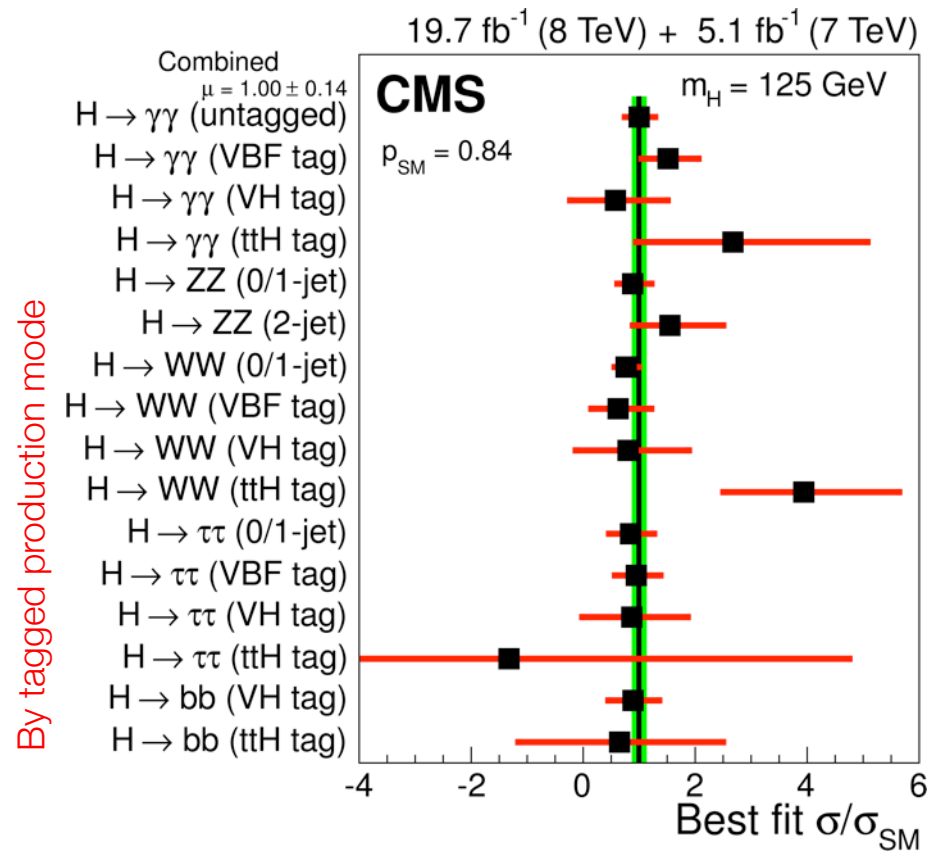
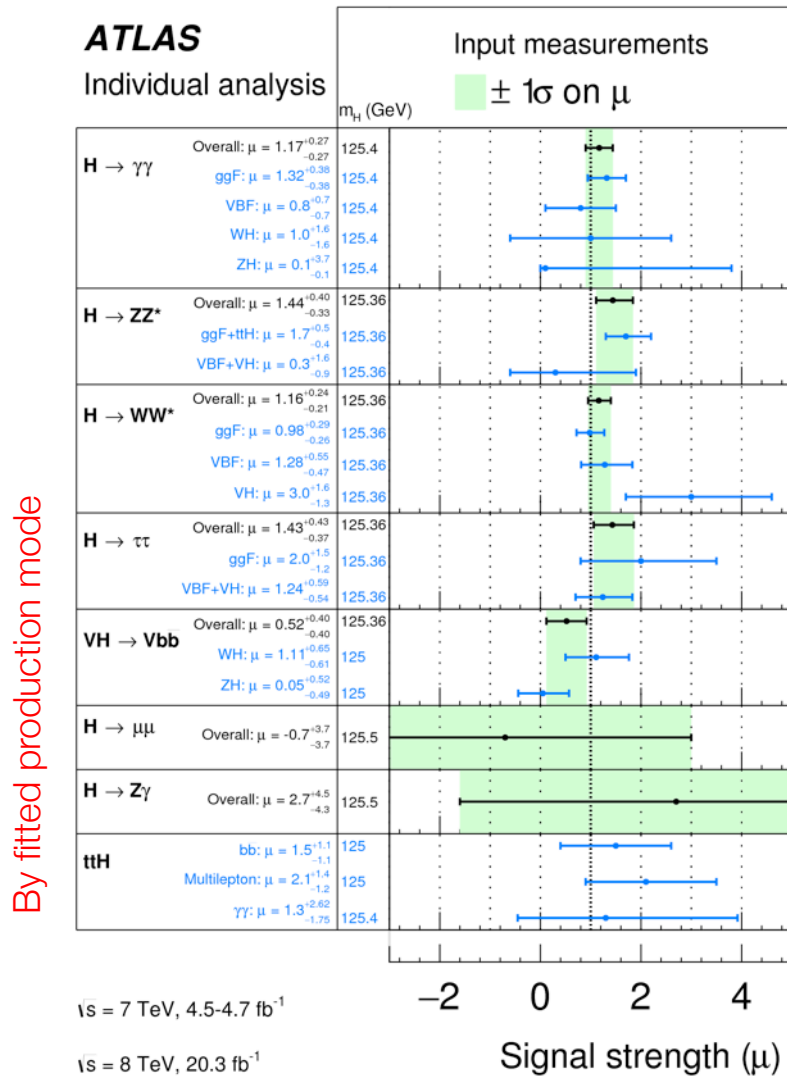


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Reminder – the signal strengths in the individual channels

Signal strength fits of individual experiments/channels



The global signal strength

- Assuming SM ratios of production cross-sections and decay rates

$$\mu = 1.09^{+0.11}_{-0.10}$$

Most precise result at the expense of the largest assumptions

$$= 1.09^{+0.07}_{-0.07} \text{ (stat)} \quad ^{+0.04}_{-0.04} \text{ (expt)} \quad ^{+0.03}_{-0.03} \text{ (thbgd)} \quad ^{+0.07}_{-0.06} \text{ (thsig)}$$

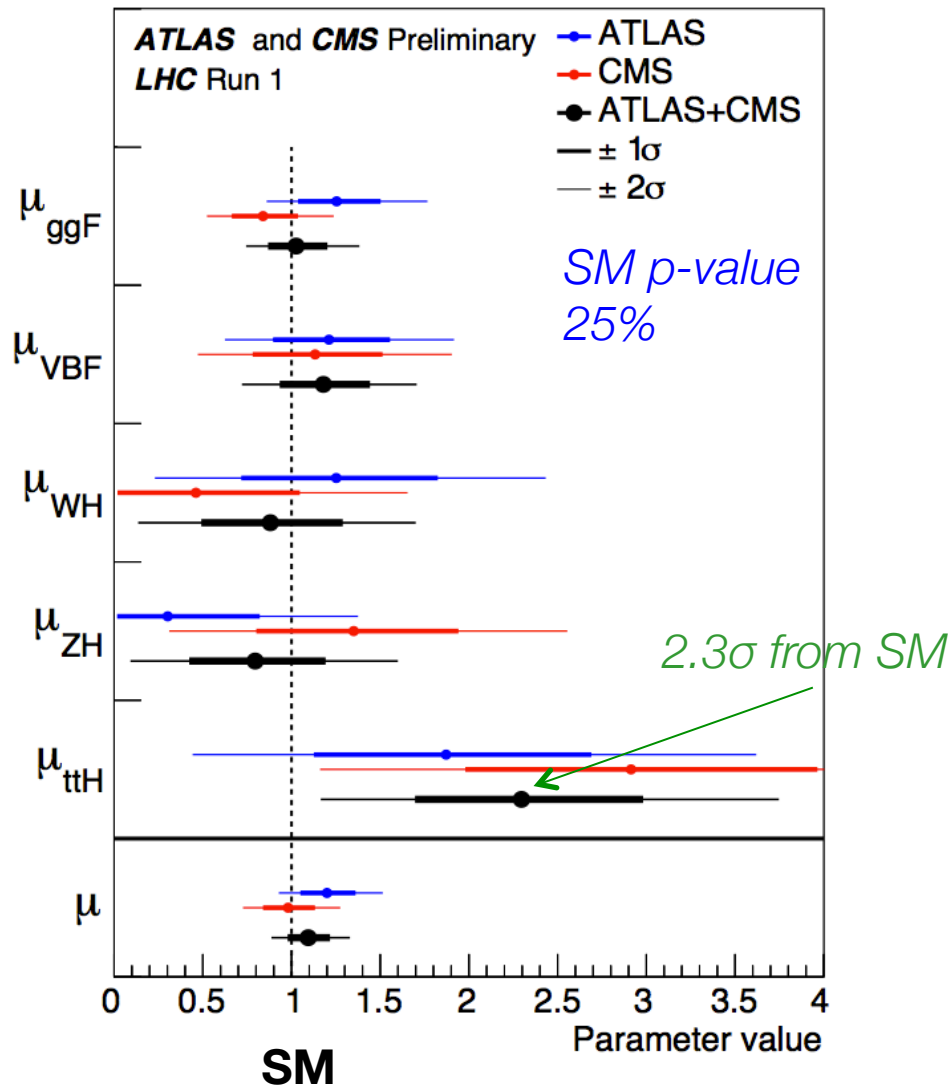
*Stat and Th.Sig of comparable size
(Th.Sig dominated by ggF cross-section uncertainty)*

- NB: Theory uncertainties on the inclusive SM cross-section enter through denominator in Higgs signal strength

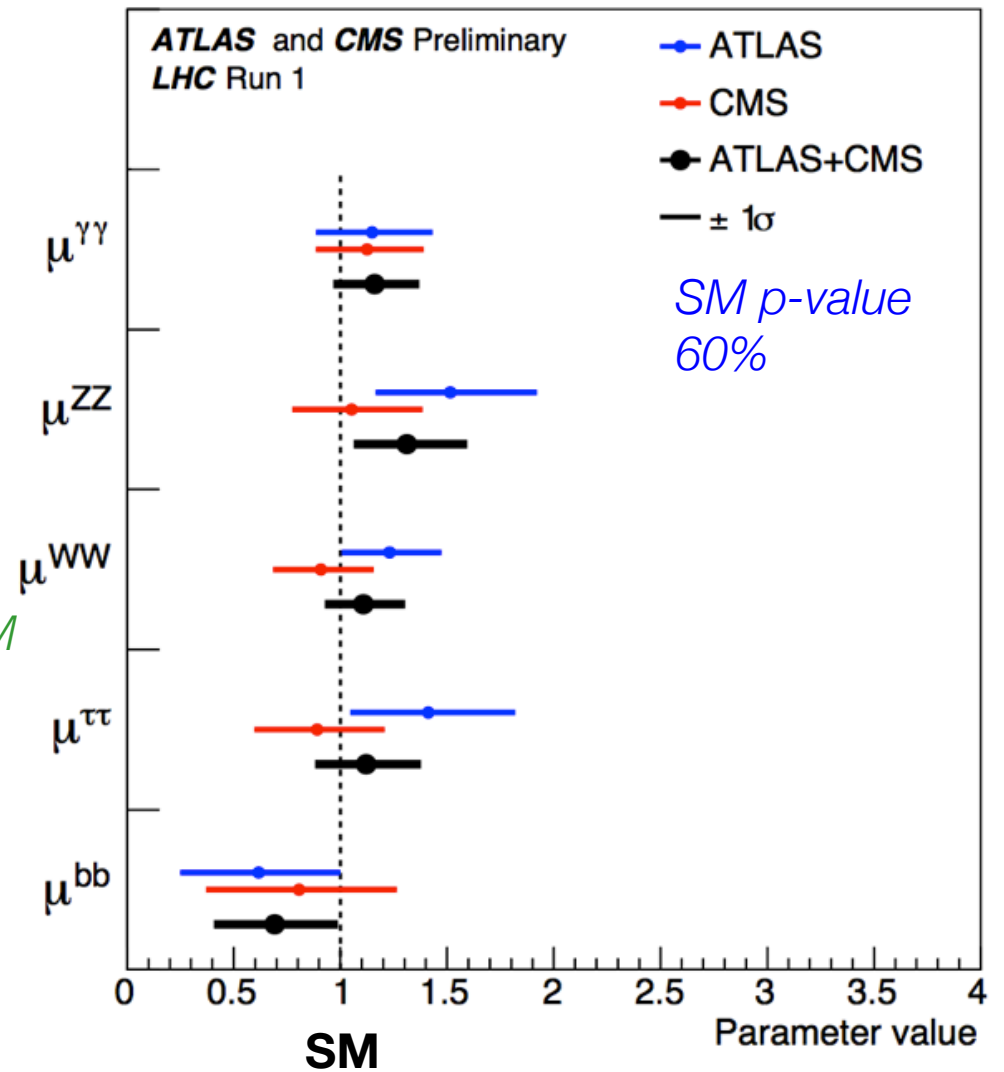
$$\mu_i^f \equiv \frac{\sigma_i \cdot \text{BR}^f}{(\sigma_i \cdot \text{BR}^f)_{\text{SM}}} = \mu_i \times \mu^f$$

Higgs signal strength by production and decay mode

Production signal strengths (SM values of BRs assumed)



Decay signal strengths (SM value of production σ 's assumed)



Significance of combined observations

- Comparing likelihood of the best-fit with likelihood assuming $\mu_{\text{prod}}=0$ or $\mu^{\text{decay}}=0$ we obtain:

Production process	Observed Significance(σ)	Expected Significance (σ)
VBF	5.4	4.7
WH	2.4	2.7
ZH	2.3	2.9
VH	3.5	4.2
ttH	4.4	2.0
Decay channel		
$H \rightarrow \tau\tau$	5.5	5.0
$H \rightarrow bb$	2.6	3.7

*VBF production and $H \rightarrow \tau\tau$ now established at over 5σ .
 ggF and $H \rightarrow ZZ, \gamma\gamma, WW$ already established by each experiment*

Signal strength in V,F-mediated production by decay

- Measure $ggF+ttH$ production “fermion-mediated” and VBF+VH production “boson-mediated” for each decay mode

$$\mu_{VBF+VH}^f$$

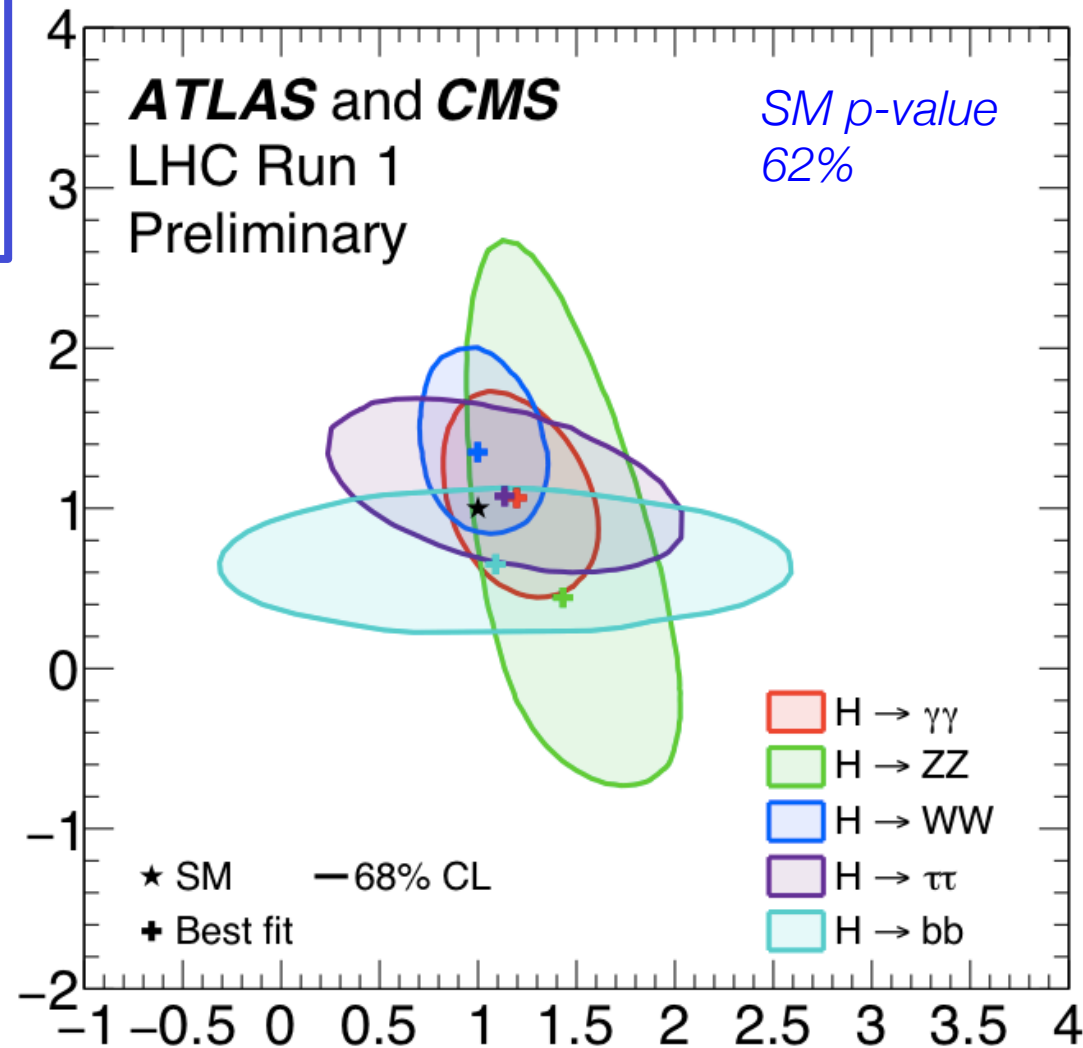
(No assumption on SM production or decay rates needed for individual channels)

- Can also measure combined ratio

$$\frac{\mu_{VBF+VH}}{\mu_{ggF+ttH}} = 1.06^{+0.35}_{-0.27}$$

over all decay modes

without assumptions on SM decay rates (BRs cancel in ratio)



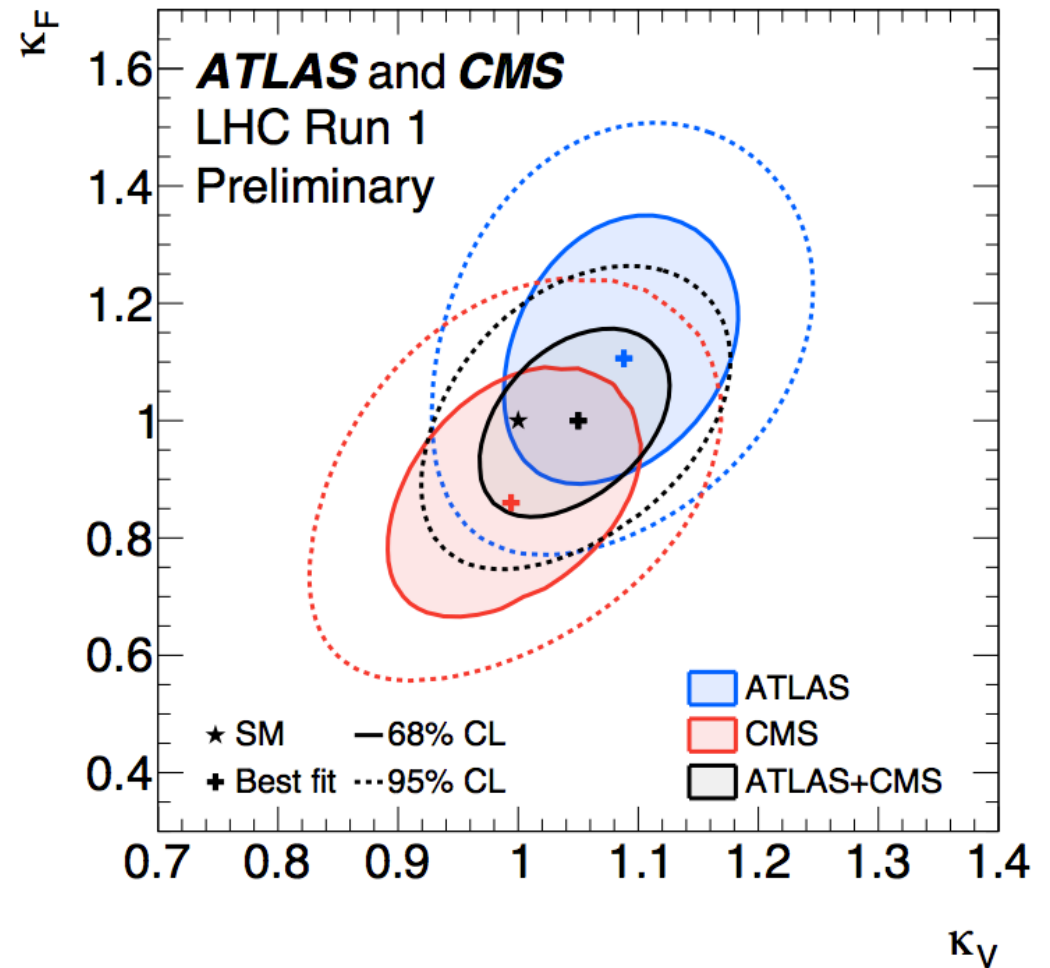
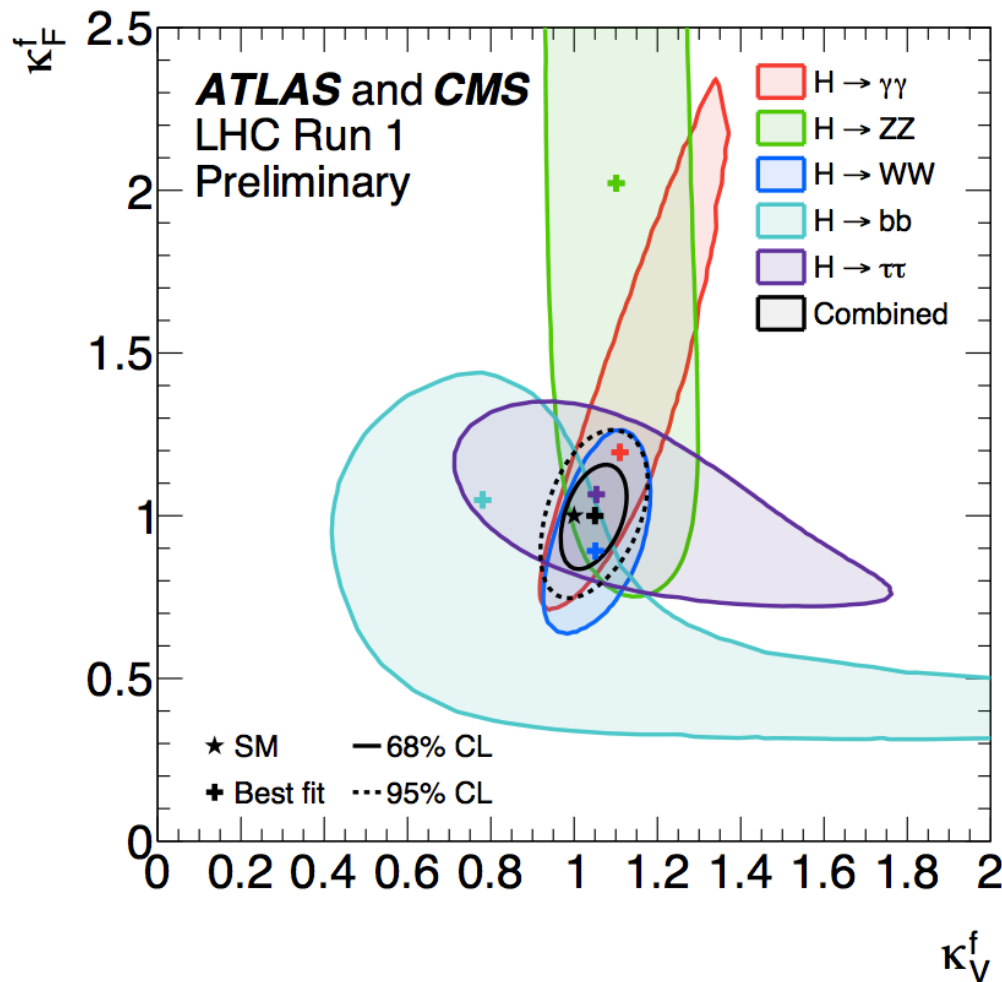
$$\mu_{ggF+ttH}^f$$

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- ④ Signal strength measurements
- ⑤ **Constraints on Higgs boson couplings**
- ⑥ Most generic parametrizations

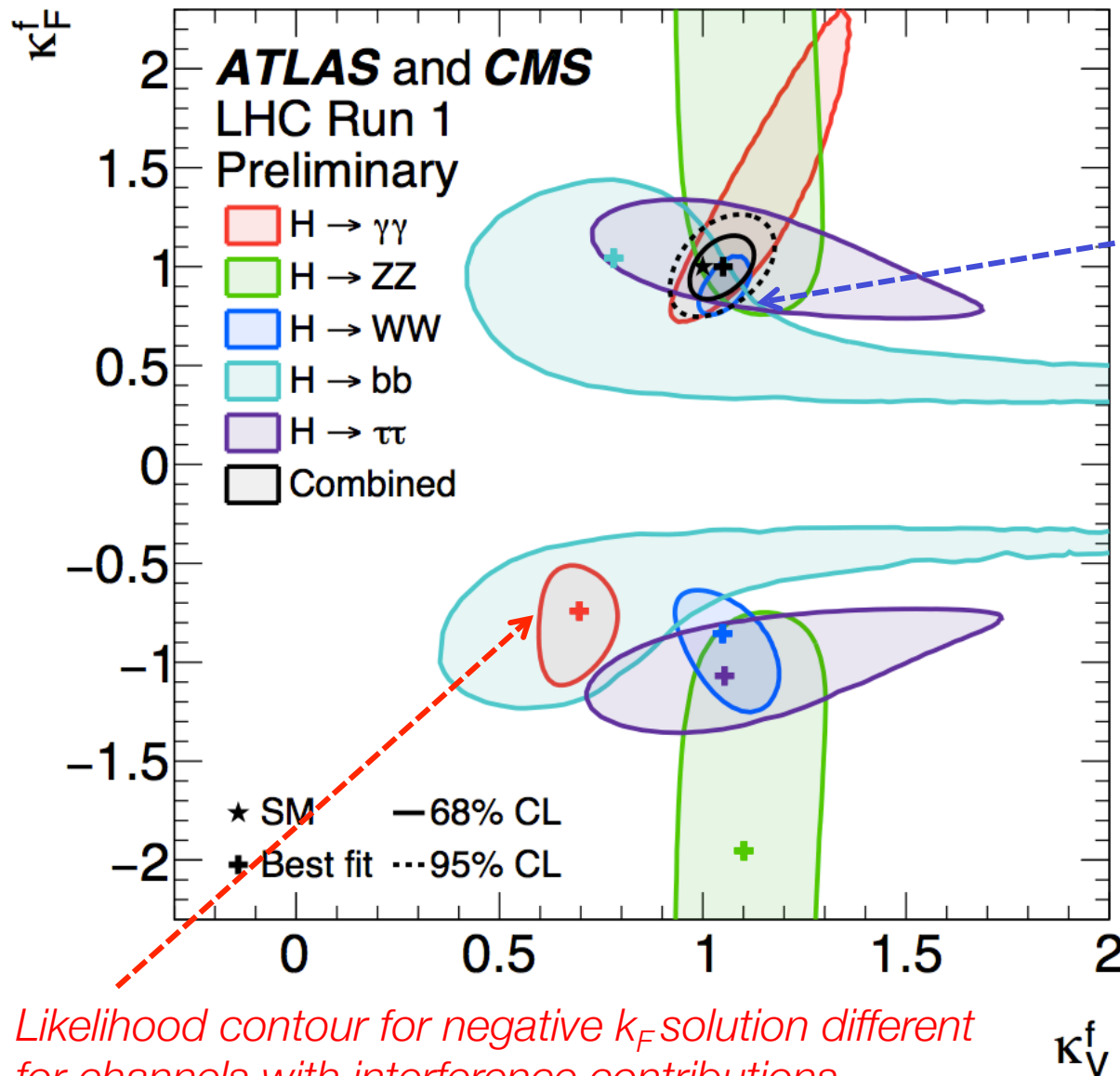
Constraints for Higgs couplings to fermions, bosons

- Assume universal scaling parameters for Higgs couplings to fermions (κ_F), bosons (κ_V)
$$\sigma(i \rightarrow H \rightarrow f) = \frac{\sigma_i(\vec{k}) \cdot \Gamma^f(\vec{k})}{\Gamma_H}$$
- Assume only SM physics in loops, no invisible Higgs decays, $\kappa_{F,V} \geq 0$

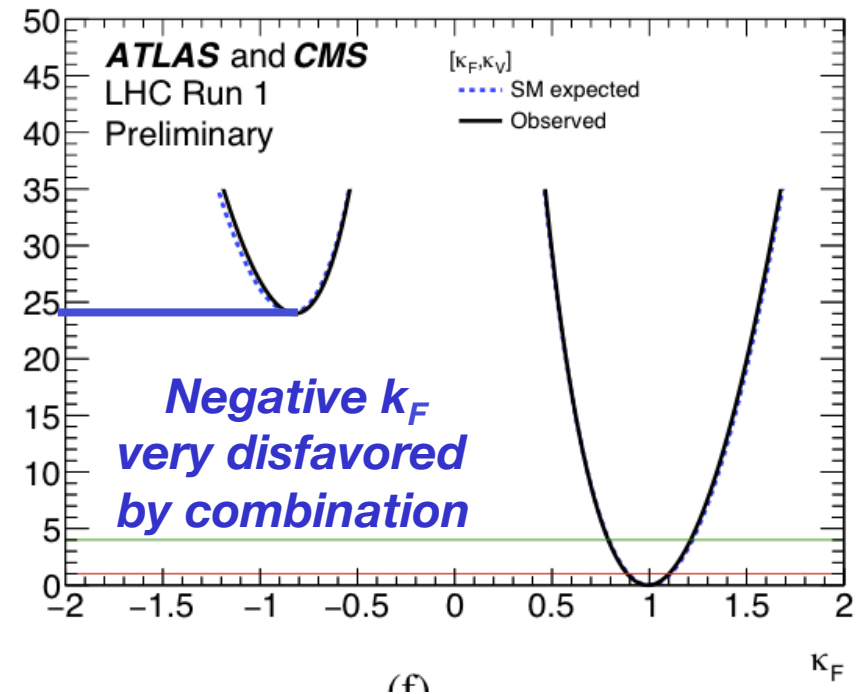


Constraints for Higgs couplings to fermions, bosons

- Expanding parameter ranges to include negative couplings



Positive WW contour reduced due to preferred negative solution



Likelihood contour for negative k_F solution different for channels with interference contributions

Constraints on tree-level Higgs couplings

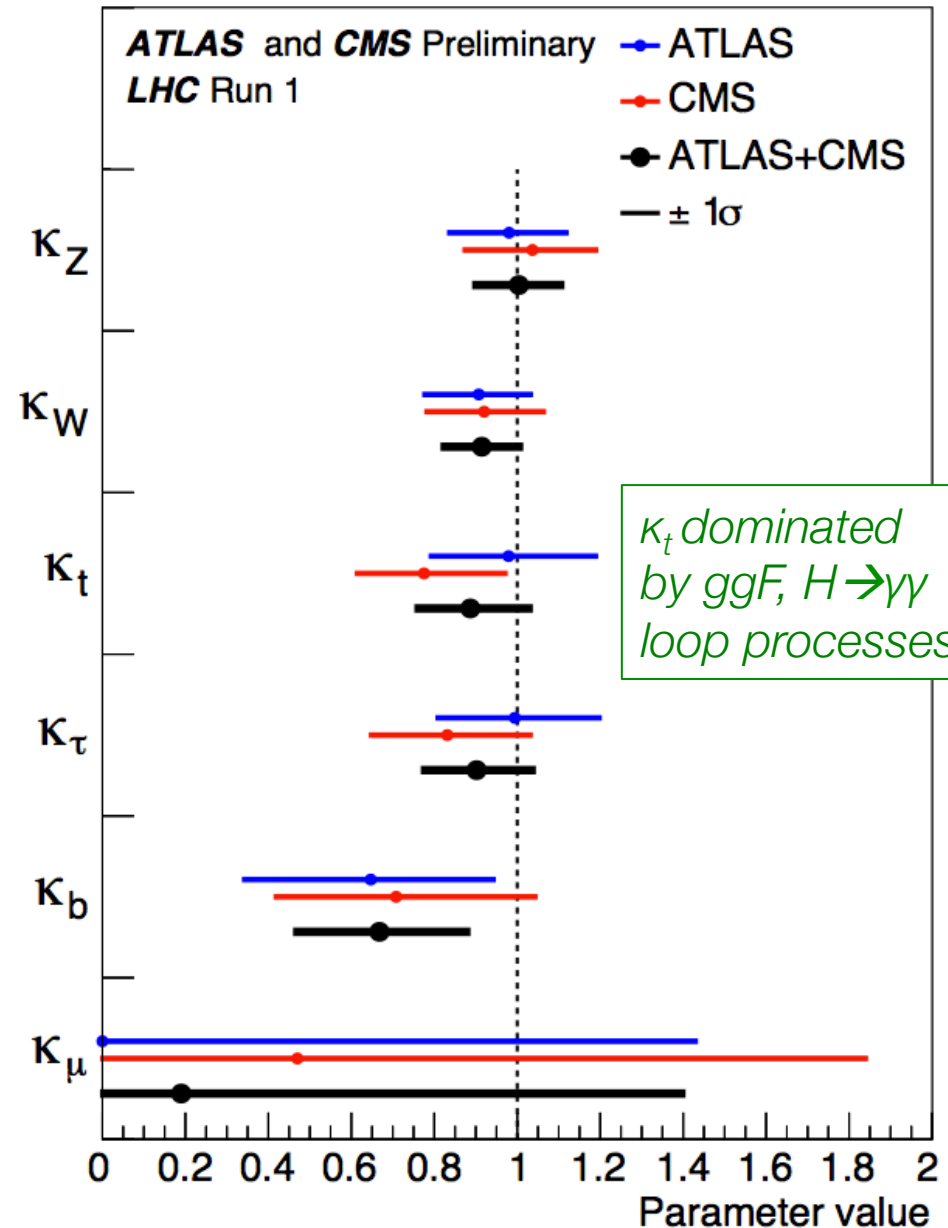
- Assume only SM physics in loops, no invisible Higgs decays
- Fit for scaling parameters for Higgs couplings to

W, Z, b, t, τ, μ

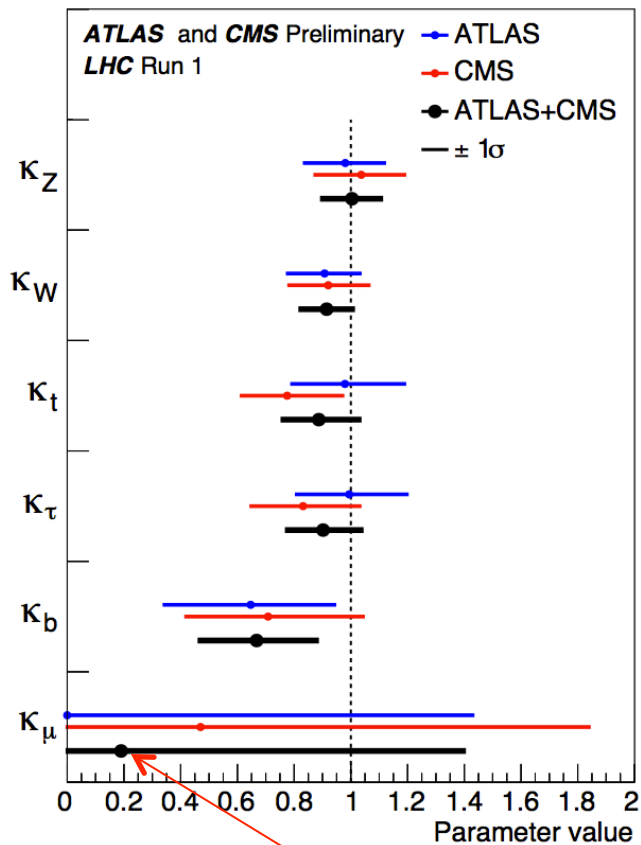
- *NB: low measured value of κ_b reduces total width Γ_H*
 \rightarrow all κ_i measured low [w.r.t $\mu=1.09$]

$$\sigma(i \rightarrow H \rightarrow f) = \frac{\sigma_i(\vec{\kappa}) \cdot \Gamma^f(\vec{\kappa})}{\Gamma_H}$$

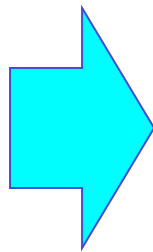
$$\kappa_H^2 \sim 0.57 \cdot \kappa_b^2 + 0.22 \cdot \kappa_W^2 + 0.09 \cdot \kappa_g^2 + 0.06 \cdot \kappa_\tau^2 + 0.03 \cdot \kappa_Z^2 + 0.03 \cdot \kappa_c^2 + 0.0023 \cdot \kappa_\gamma^2 + 0.0016 \cdot \kappa_{Z\gamma}^2 + 0.00022 \cdot \kappa_\mu^2$$



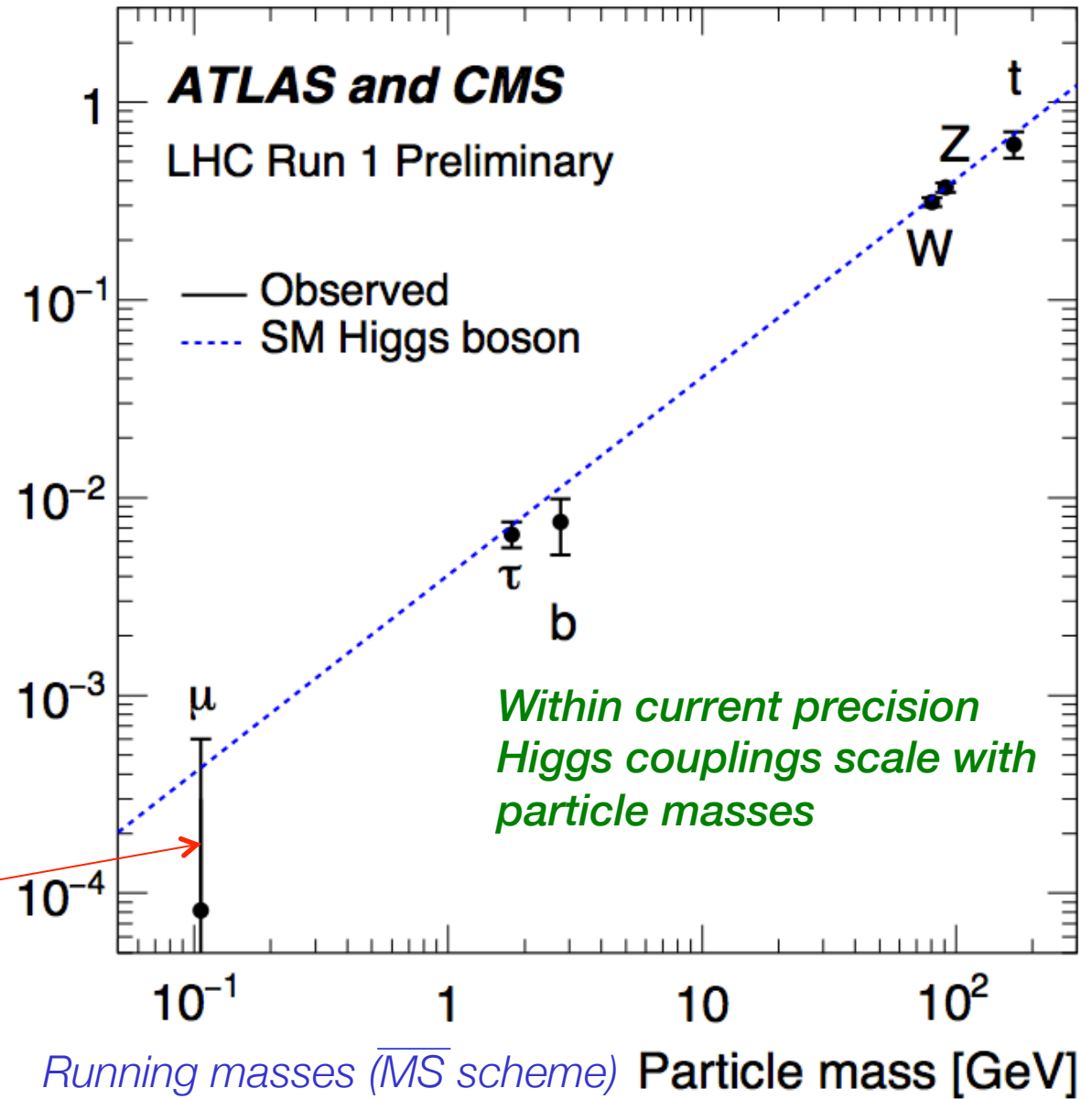
Constraints on tree-level Higgs couplings



Observed κ_μ compatible with 0

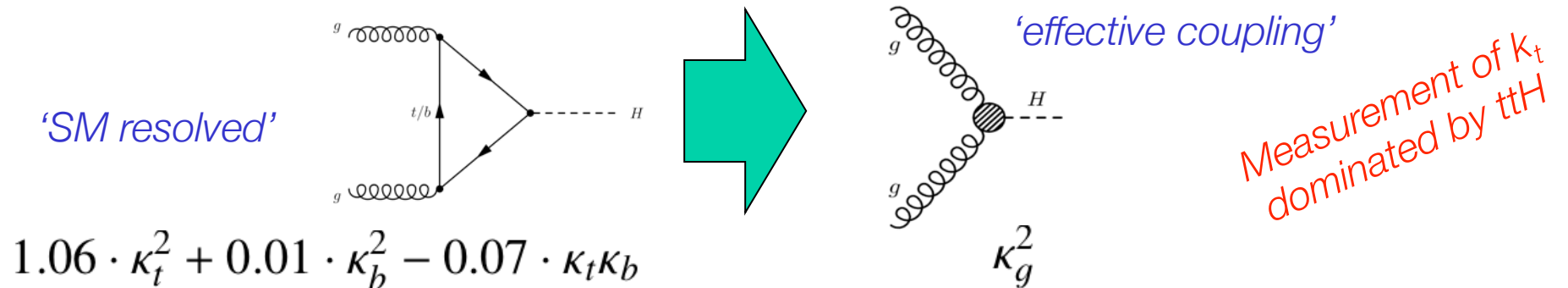


$$\frac{m_F}{\kappa_F V} \text{ or } \frac{m_Y}{\sqrt{\kappa_Y} V}$$



Allowing for BSM contributions in Higgs coupling interpretations

- Results shown so far assumed no invisible (BSM) Higgs decays nor BSM contributions to loops. **Now drop these assumptions.**
- 1. **Represent loop processes (ggF, $H \rightarrow Z/\gamma\gamma$) with effective params (κ_g, κ_γ), rather than assuming SM content**



- 2. **Allowing BSM Higgs decays (invisible, undetected etc...) to increase the total width**

$$\Gamma_H = \frac{\kappa_H^2 \cdot \Gamma_H^{\text{SM}}}{1 - \text{BR}_{\text{BSM}}}$$

If $\text{BR}_{\text{BSM}} > 0$ then all observed cross-sections lowered by common factor

$$\sigma(i \rightarrow H \rightarrow f) = \frac{\sigma_i(\vec{k}) \cdot \Gamma^f(\vec{k})}{\Gamma_H}$$

Limit on invisible Higgs decays from Higgs couplings

- Concept: set limit on BR to (invisible, undetected) Higgs decays

$$\Gamma_H = \frac{\kappa_H^2 \cdot \Gamma_H^{\text{SM}}}{1 - \text{BR}_{\text{BSM}}}$$

- When κ_H is modeled by 6+2 κ_i 's it has no strong upper bound
→ BR_{BSM} not bounded (Γ_H due to large κ_H or to large BR_{BSM} ?)
→ Must introduce some assumptions to bound κ_H
- **Scenario 1** – Assume 6 tree-level couplings at SM ($k=1$),
but leaving 2 effective couplings for loops floating
- **Scenario 2** – Keep all 6+2 coupling parameters floating,
but bound vector boson couplings $\kappa_W, \kappa_Z \leq 1$

(Bound $\kappa_V \leq 1$ occurs naturally in many BSM physics models, e.g. Electroweak Singlet, 2HDM, MCHM...)

(alternatively, use off-shell coupling strength measurements to constrain Γ_H , albeit with additional assumptions)

Focus on effective couplings for loop processes

'Scenario 1'

- Fix all tree-level Higgs couplings to SM ($\kappa_W, \kappa_Z, \kappa_b, \kappa_t, \kappa_\mu, \kappa_\tau=1$) and $BR_{inv}=0$

