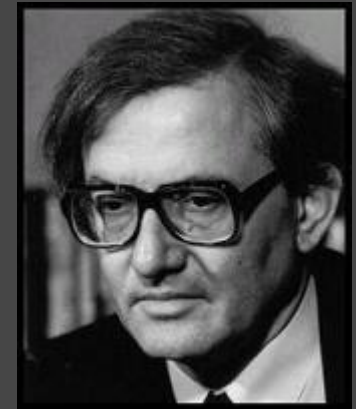




# Femtoszkópiai munkamegbeszélés

2015. Augusztus 17-19.  
Gyöngyös



## INITIAL ENERGY DENSITY IN LHC P+P COLLISIONS

18 Aug 2015

M. Csanád & T. Csörgő & M. Nagy

# The Bjorken-estimate

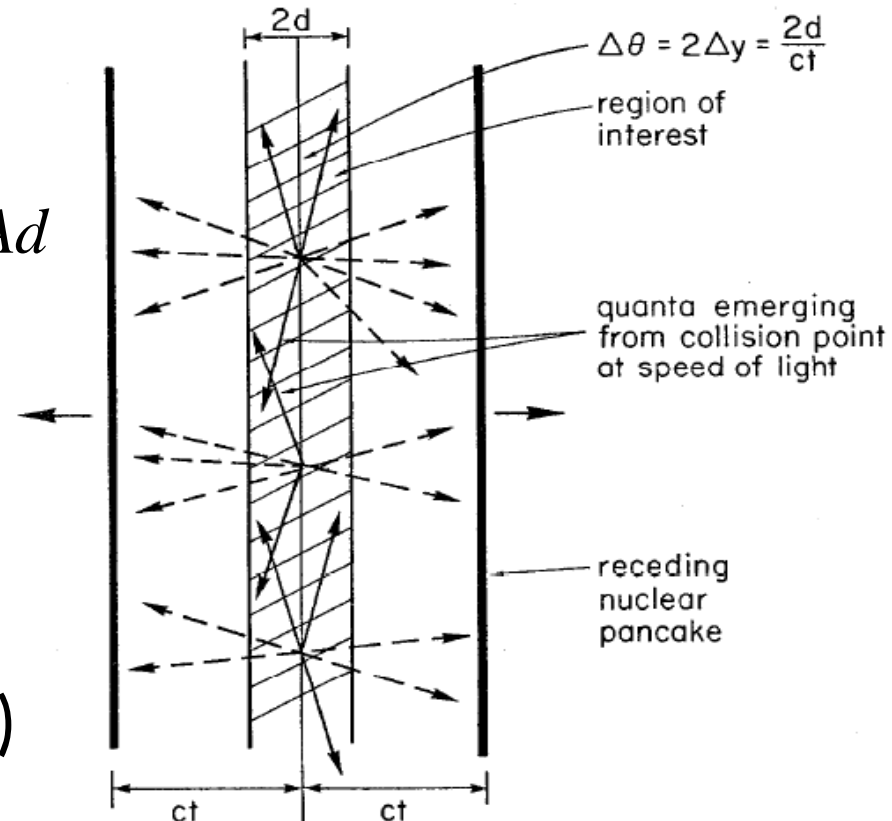
2

- The original idea: energy density based on  $dE/dy$
- QGP critical  $\varepsilon$ :  $\leq 1 \text{ GeV}/\text{fm}^3$  (from  $\varepsilon_c = 6-8 \times T_c^4$ )
- Result ( $\sim 2000x$  cited)

$$E = N \frac{dE}{dy} \Delta y = N \frac{dE}{dy} \frac{1}{2} \frac{2d}{t} = \varepsilon \cdot Ad$$

$$\varepsilon_{Bj} = \frac{1}{R^2 \pi_0} \frac{dE}{d\eta} = \frac{\langle E \rangle}{R^2 \pi_0} \frac{dn}{d\eta}$$

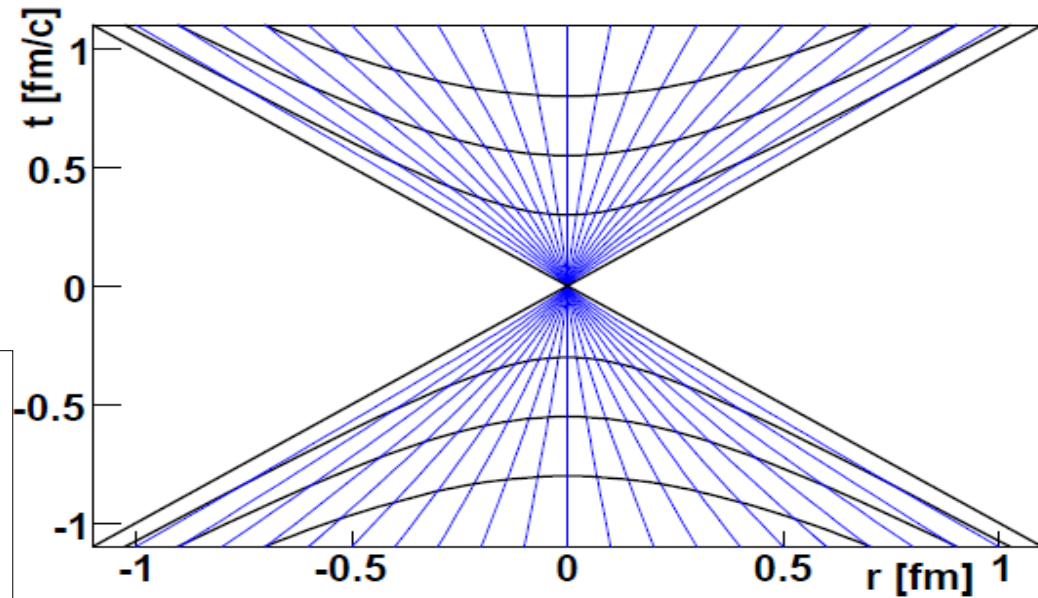
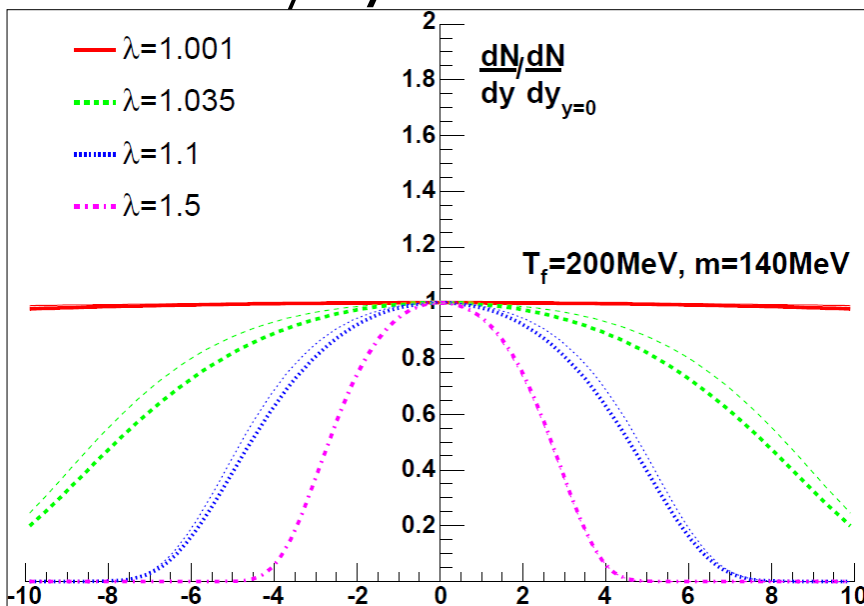
- Needs correction!
- Ref.: Phys.Rev. D27 (1983)



# A solution of relativistic hydro

3

- Velocity:  $\tanh(\lambda\eta)$
- Acceleration:  $\lambda \neq 1$
- Density:  $(\tau/\tau_0)^\lambda$
- $dn/dy$  calculable!



- Compare this to RHIC data!
- $dn/dy$  measurement yields advanced initial  $\varepsilon$  estimate
- Significant correction at RHIC!

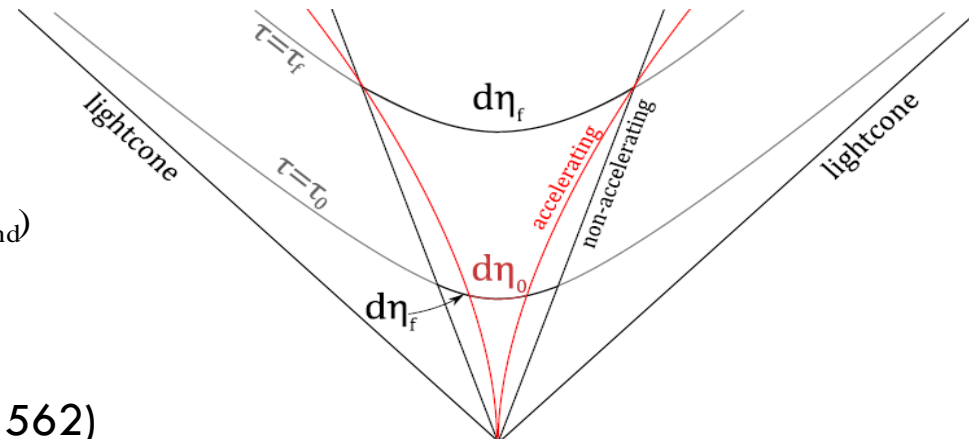
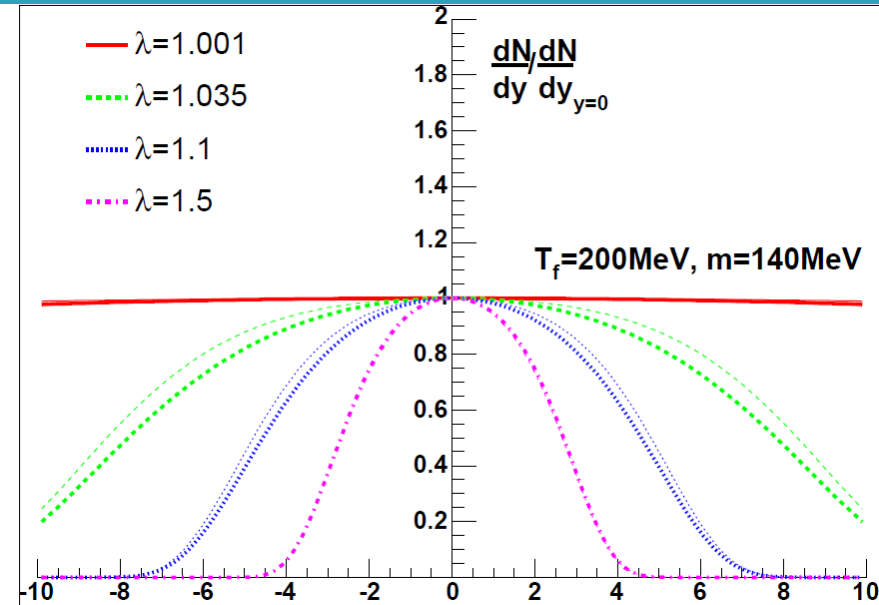
□ Reference: Phys.Lett. B663 (2008) 306-311 (nucl-th/0605070)

# An advanced estimate

4

- Fact:  $dn/dy$  not flat
- Finiteness & acceleration
- Analytical investigation:
  - ▣ Acceleration parameter  $\lambda$
- Two modifications:
  - ▣  $y \neq \eta$  &  $\eta_{\text{final}} \neq \eta_{\text{initial}}$
- Work by acceleration!
- Correction w.r.t. EoS:

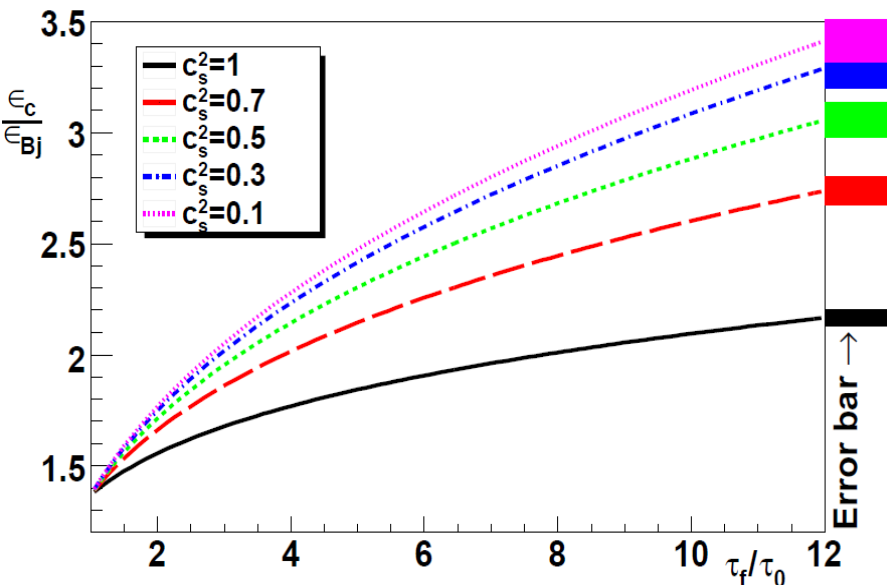
$$\mathcal{E} = \mathcal{E}_{Bj} (2\lambda - 1) \left( \frac{\tau_f}{\tau_i} \right)^{(\lambda-1)(2-c_{\text{sound}}^2)}$$



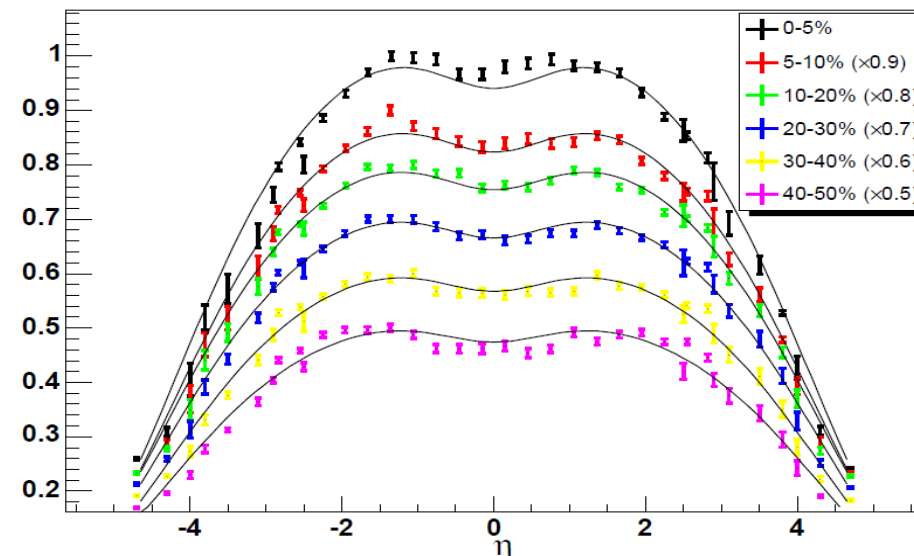
# Initial energy density at RHIC

5

- Bjorken estimate from BRAHMS:  $5 \text{ GeV}/\text{fm}^3$
- Advanced estimate gives:  $\varepsilon = \varepsilon_{Bj} (2\lambda - 1) \left( \frac{\tau_f}{\tau_i} \right)^{(\lambda-1)(2-c_{\text{sound}}^2)}$
- Correction: 2-3x, result  $15 \text{ GeV}/\text{fm}^3$ , QCD agreement!
- Corresponds to  $T_{\text{ini}} \cong 2T_c \cong 340 \text{ MeV}$
- Confirmed by photon spectra at PHENIX, published 2010
- Reference e.g.: J.Phys.G35 (2008) 104128 (arXiv:0805.1562)



Normalized pseudorapidity distributions from BRAHMS



# Initial energy density at LHC

6

- Rough estimate possible via the Bjorken formula
  - ▣ Number of particles at midrapidity: 5.89 (CMS, ALICE)
  - ▣ Average energy:  $\langle m_{\uparrow} \rangle = 0.562$  GeV (CMS)
  - ▣ Initial radius of the system  $R$ :  $\sim 1.081$  fm (TOTEM,  $\sigma_{\text{inel}}$ )
  - ▣ Formation time  $\tau_0$ : 1 fm/c (conservative estimate)
- Energy density from this:

$$\varepsilon_{\text{Bj}} = \frac{1}{R^2 \pi_0} \frac{dE}{d\eta} = \frac{\langle E \rangle}{R^2 \pi_0} \frac{dn}{d\eta} = \frac{0.562 \times 5.89 \text{ GeV} / c}{3.67 \text{ fm}^3 / c} \approx 0.90 \text{ GeV} / \text{fm}^3$$

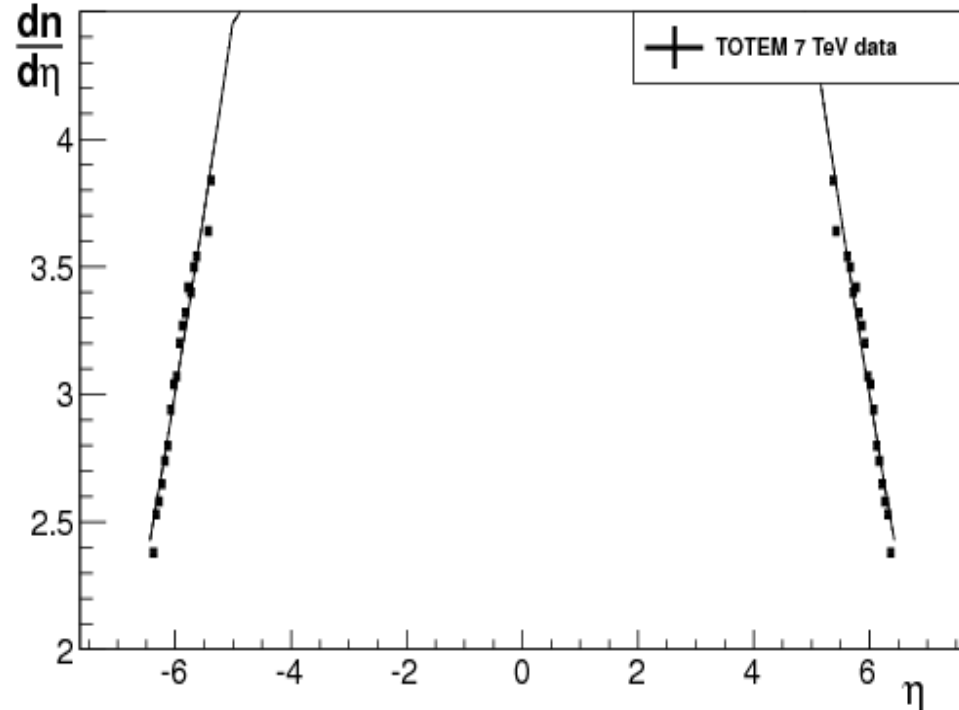
- Just below critical? Important question!

# Correction from initial acceleration

7

- Initial acceleration pushes outer volume elements
- This modifies the  $dn/d\eta$  distribution
- Estimate acceleration from it!
- $\lambda = 1$ : no acceleration
- TOTEM fit:  $\lambda = 1.073 \pm 0.001 \pm 0.004$
- Without EoS: 20%

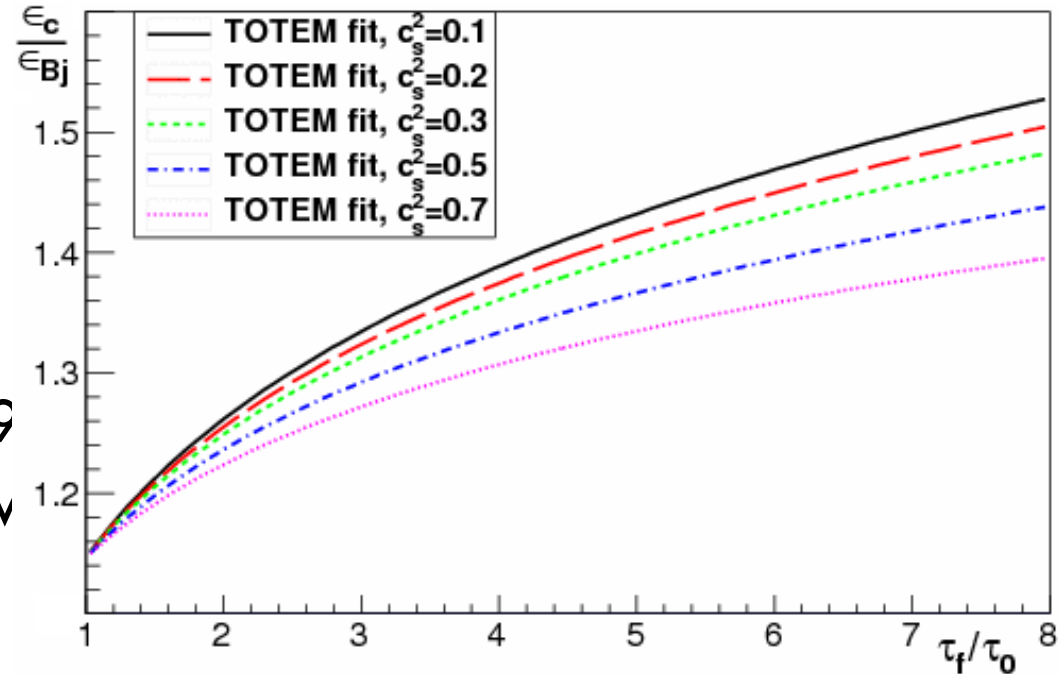
$$\varepsilon = \varepsilon_{Bj} (2\lambda - 1) \left( \frac{\tau_f}{\tau_i} \right)^{(\lambda-1)(1-c_s^2)}$$



# Advanced estimate at 7 TeV

8

- Fit result:  $\lambda=1.073$
- Conservatively:  $c_s^2=0.1$
- $\sim 25\%$  correction
- Input parameters:
  - ▣  $dN/dy$  at midrap.: 5.89
  - ▣ Average  $m_T$ : 0.562 GeV
  - ▣ Area: 3.67 fm<sup>2</sup>
    - From cross sections
  - ▣ Freeze-out time / form. time: at least 2
- Bjorken result: 0.90 GeV/fm<sup>3</sup>
- Corrected result: 1.14 GeV/fm<sup>3</sup>





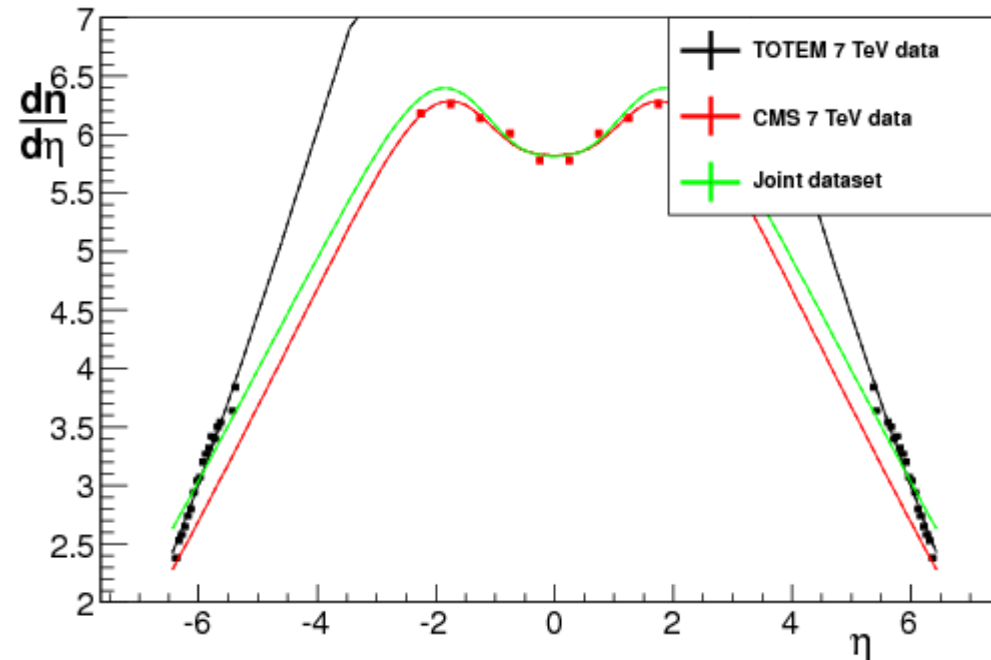
# TOTEM & CMS data combined (7 TeV)

9

- Fit results:
  - ▣ TOTEM:  $\lambda = 1,073 \pm 0,003$
  - ▣ CMS:  $\lambda = 1,061 \pm 0,002$
  - ▣ Joint data:  $\lambda = 1,054 \pm 0,001$

- Normalization OK?
  - ▣ Single diffractive vs. non-single diffractive?

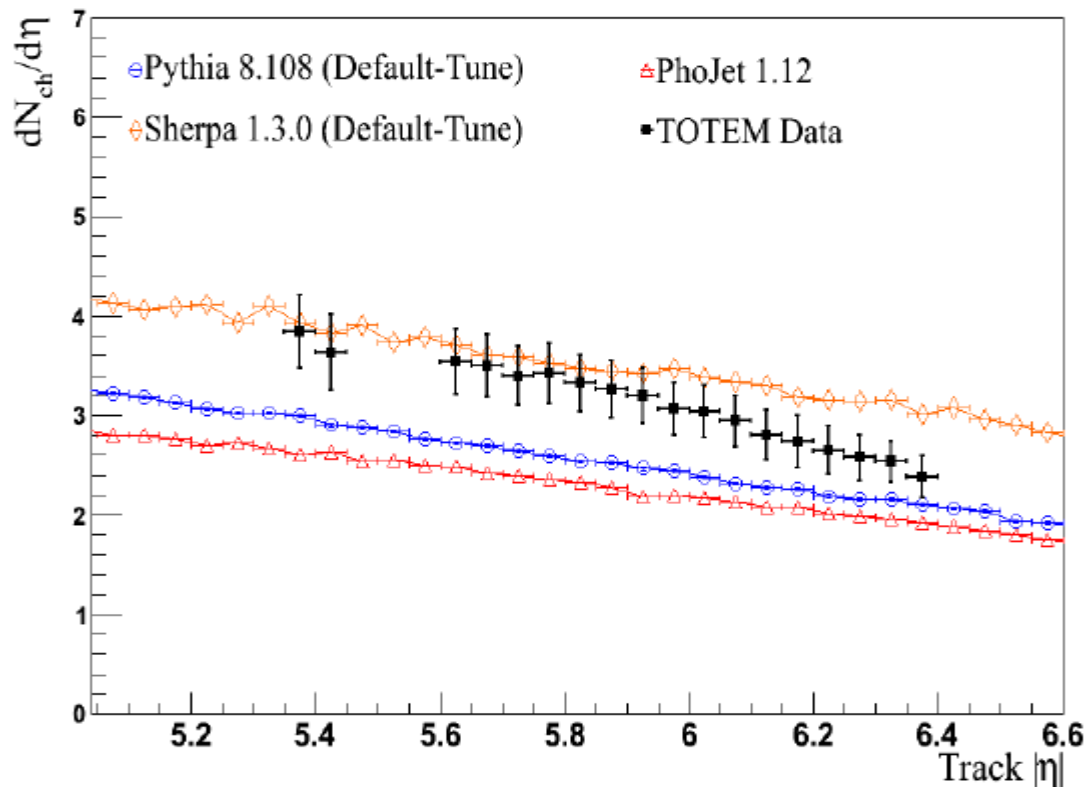
- Lambda does not change significantly



# Comment: $dn/d\eta$ @ 7 TeV is not trivial

10

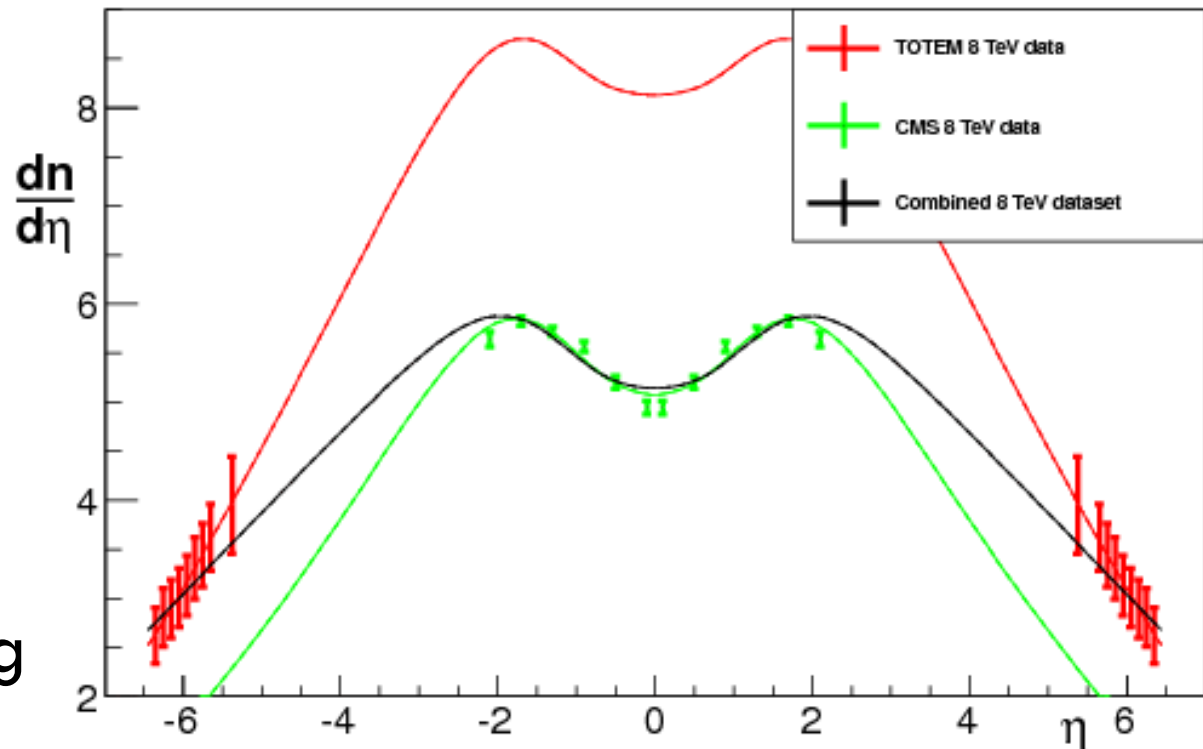
- Not trivial for MC models
- TOTEM Coll., EPL, 98 (2012) 31002



# Preliminary results on 8 TeV

11

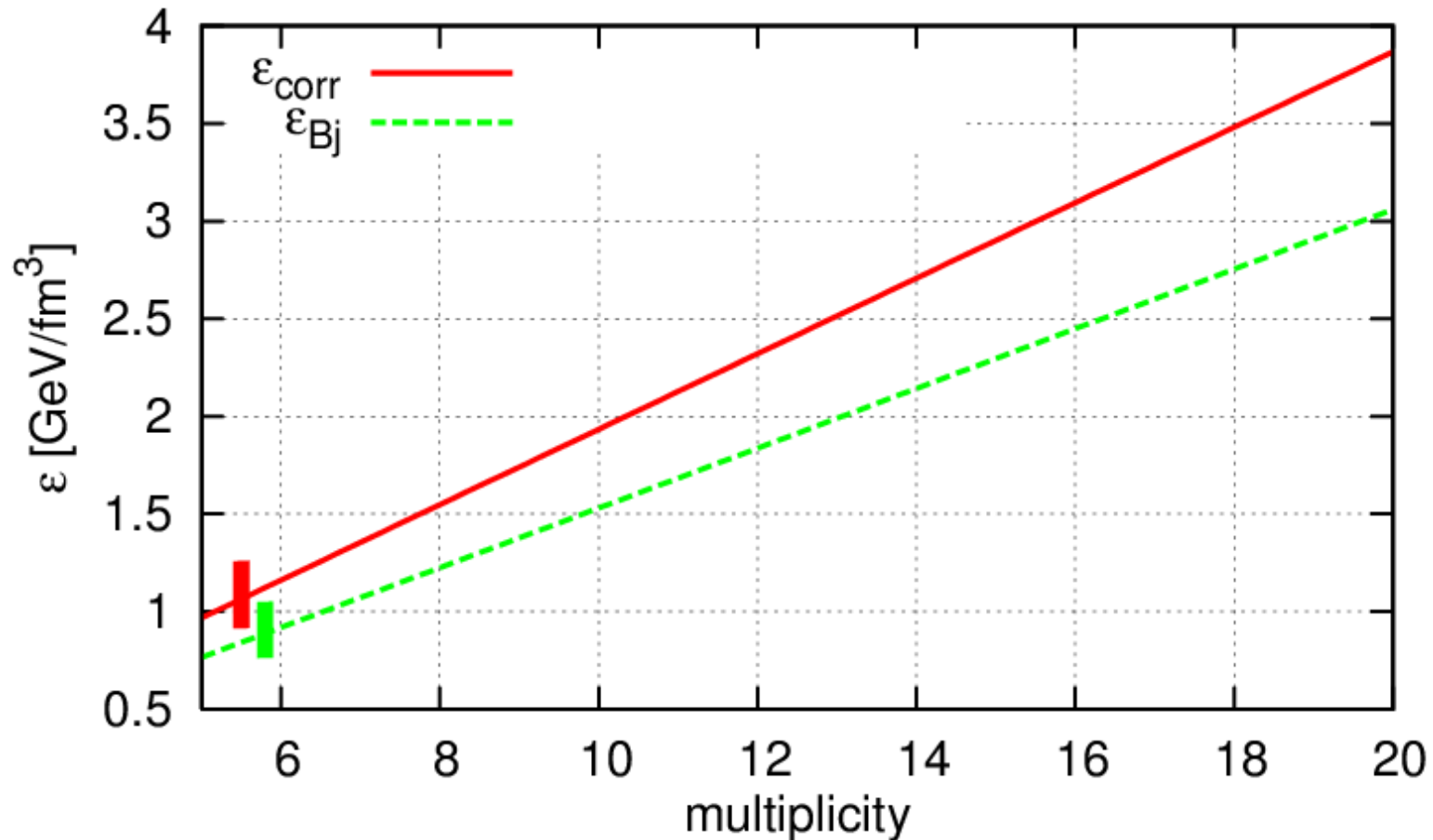
- CMS vs. TOTEM normalization not trivial
- Both datasets describable by  $\lambda = 1.07 \pm 0.01$
- Joint fit:  
 $\lambda = 1.046 \pm \pm 0.001$
- Data are not final
- Systematic analysis coming



# Dependence on particle number

12

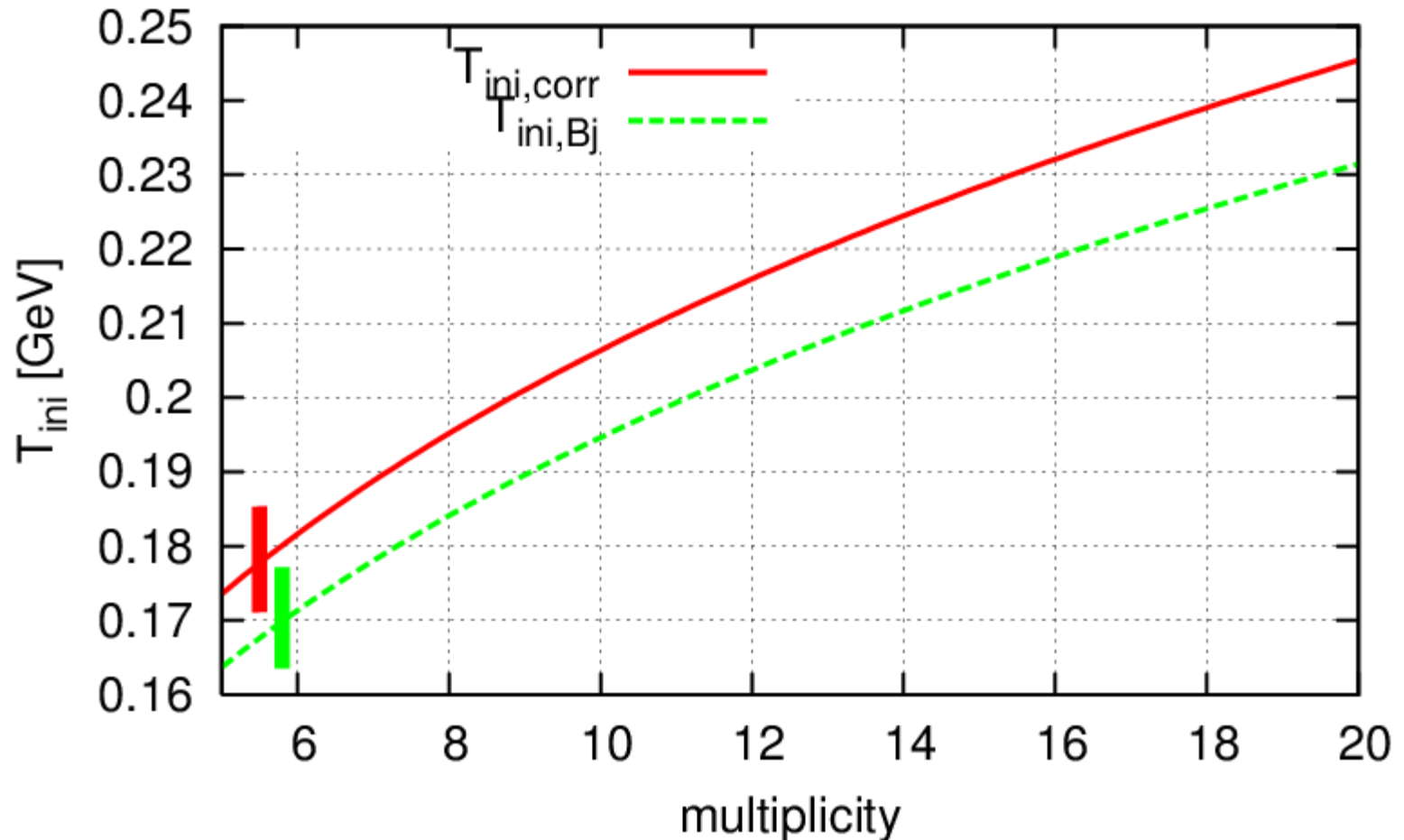
- Several multiplicity classes, 6-20, even 30 seen!



# Initial temperature estimate

13

- Temperature from  $\varepsilon \sim T^4$



# Sources of uncertainties

14

- For the correction factor  $\varepsilon/\varepsilon_{\text{Bj}}$ :
  - Fit parameter  $\lambda$
  - Statistical error (from the data)
  - Speed of sound  $c_s^2$
  - Duration  $\tau_f/\tau_i$
- For the original Bjorken-estimate:
  - Main uncertainty source: multiplicity at midrapidity  $dN/dy$
  - Area (if taken from cross-section): very precise
  - Formation time
  - Average transverse mass

# Systematic uncertainties

15

## □ All sources of uncertainties:

parameter	value	statistical uncertainty	systematic uncertainty
$\lambda$	1.073	0.1%	0.4% (from data)
$c_s^2$	0.1	-	-2%+0.2% (if $0.05 < c_s^2 < 0.5$ )
$\tau_f/\tau_0$	2	-	-4%+10% (if ratio 1.5...4)
$\tau_0$	1 fm/c	-	underestimation on $\varepsilon$
R (from $\sigma_{inel}$ )	1.081 fm	0.5%	1.5% (from data)
$\langle m_t \rangle$	0.562 GeV/c <sup>2</sup>	0.5%	3% (from data)
dN/d $\eta$	5.985	0.2%	3% (from data)

## □ Conclusion at 7 TeV:

$$\square \varepsilon_{ini} = (1.14 \pm 0.01(\text{syst})^{+0.21}_{-0.16}(\text{syst})) \text{ GeV/fm}^3$$

# Is it unprecedented? Consequences?

16

- Bjorken and Landau worked out hydro for pp and pA
- Success of hydro to describe h+p, with  $\langle n \rangle = 7-8...$   
Phys.Lett. B422 (1998) 359-368
- Bjorken: it is not hadrons that play billiard balling
- If p+p is a complex system:
  - ▣ Gamma/pi0 ratio
  - ▣ Radial flow
  - ▣ Elliptic flow, scaling
  - ▣ HBT radii, scaling
  - ▣ Low mass dilepton enhancement
  - ▣ Direct photon enhancement
- $R_{AA}$  might not be the best measure: divide by length scale?



# Summary

17

- Experimentally widely used Bjorken est. at 7 TeV
- Advanced estimate: acceleration work, from  $dn/d\eta$
- Results on the initial  $\varepsilon$  for  $c_s^2=0.1$ , at  $\tau_f/\tau_{ini}=2$
- From TOTEM data:  $\varepsilon_{ini} = (1.14 \pm 0.01 \pm 0.2) \text{ GeV}/\text{fm}^3$ 
  - ▣ This at  $dN/dy=6$  & linearly rises with multiplicity!
- Critical energy density:  $1 \text{ GeV}/\text{fm}^3$
- Results not incompatible with supercrit. sQGP phase