

# Study of the $K^\pm$ to $\pi^\pm \pi^0 e^+ e^-$ decay with NA48/2 @ CERN

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on behalf of the NA48/2 Collaboration



**KAON16**  
**10th International Conference on Kaon Physics**  
**University of Birmingham, UK , September 14-17**

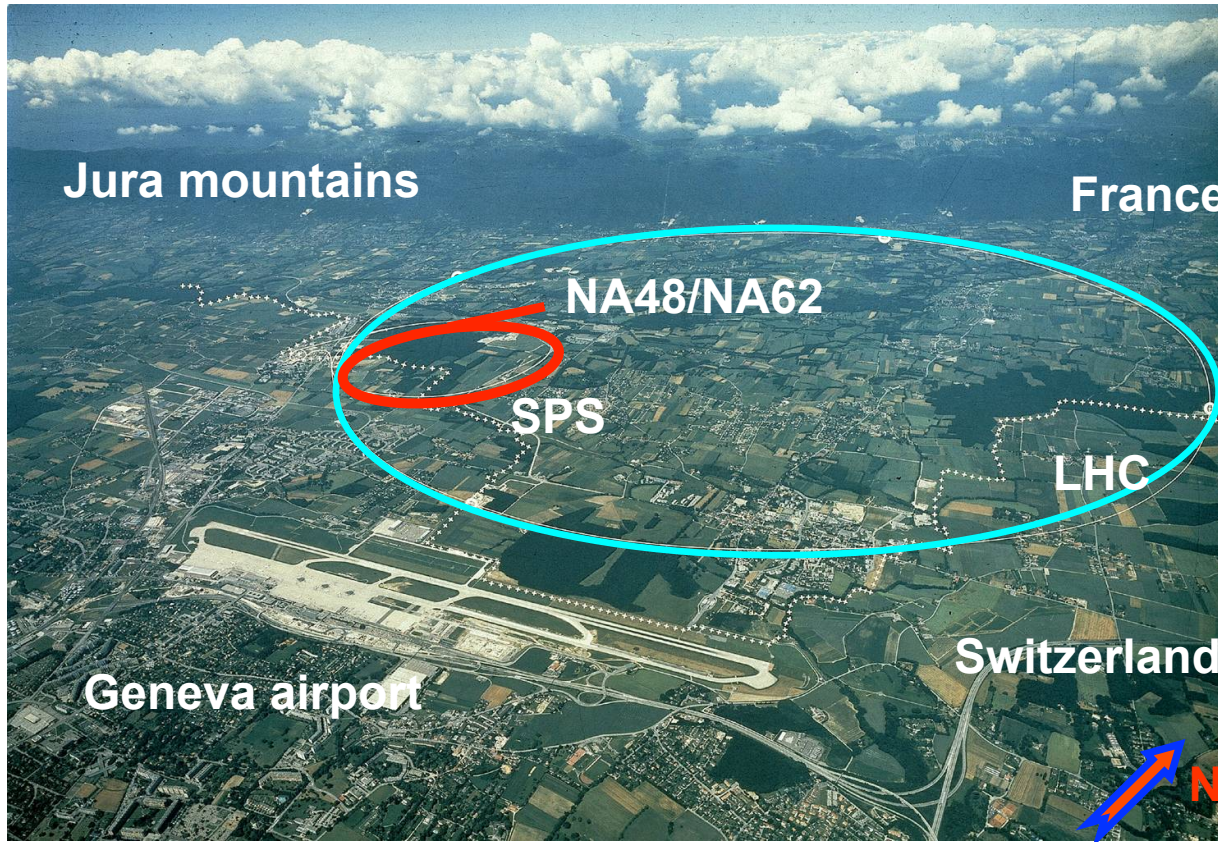
# Outline

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- ❖ NA48/2 description of experimental setup & detector performances...  
any need to repeat it ?
- ❖ ChPT and the  $K^\pm \rightarrow \pi^\pm \pi^0 e^+ e^-$  decay mode
- ❖ Selection and backgrounds
- ❖ Branching Ratio
- ❖ Summary/Prospects

Close to final !

# The NA48/NA62 experiments at CERN-SPS



NA48  
direct  
CPV  
 $\varepsilon' / \varepsilon$

NA48/1

NA48/2

NA62  
( $R_K$ )

NA62

1997: $K_L + K_S$
1998: $K_L + K_S$
1999: $K_L + K_S$
2000: $K_L$ only
2001: $K_L + K_S$
2002: $K_S$ /hyperons
2003 $K^+ K^-$ 2004 $A_g(\text{CPV})$
2007 $K^+ K^-$ 2008 $R_K + \text{tests}$
2007 design & 2013 construction
2012 technical run 2013 long shutdown 2014 commissioning & 2018 data taking

The NA48/2 collaboration:

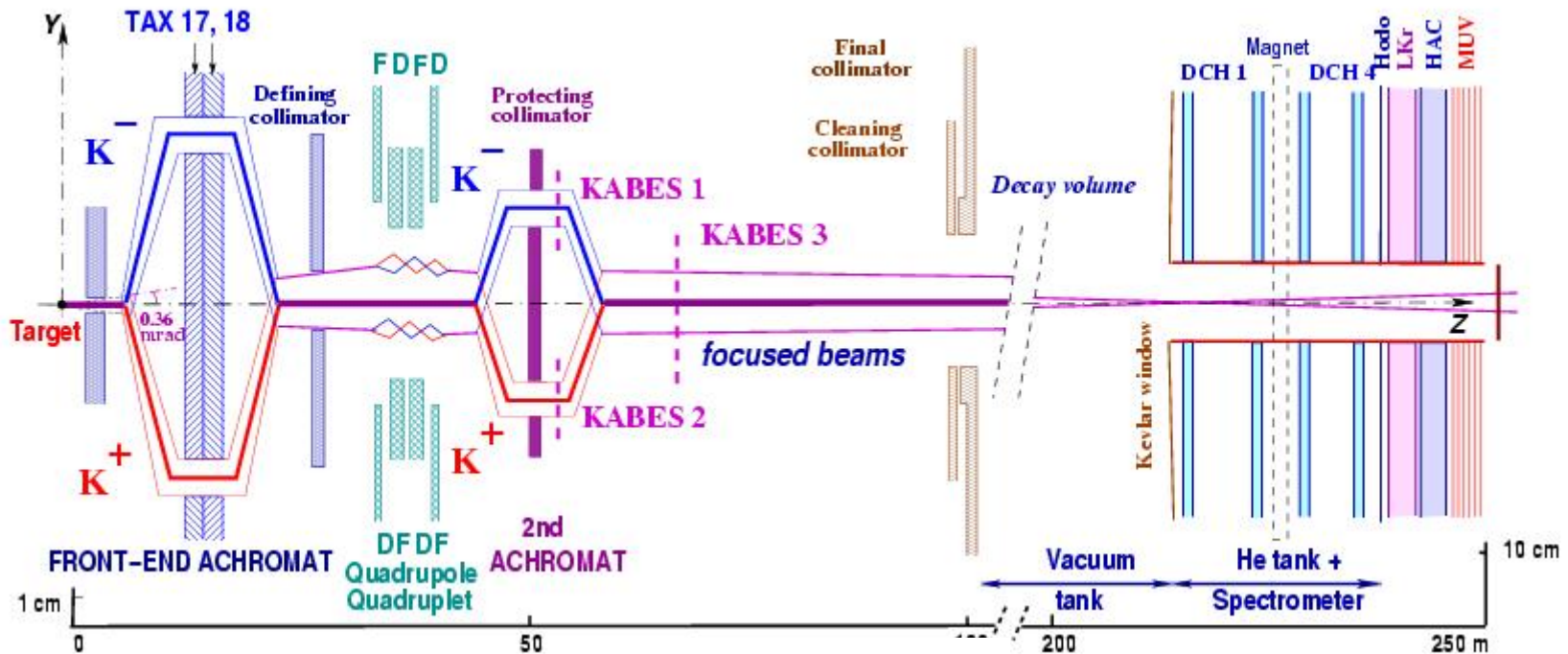
still analyzing > 10 years old valuable data !!

~100 physicists from 15 Institutes in 8 countries

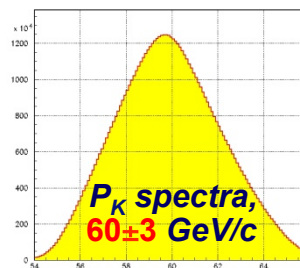
Cambridge, CERN, Chicago, Dubna, Edinburgh, Ferrara, Firenze  
Mainz, Northwestern, Perugia, Pisa, Saclay, Siegen, Torino, Wien

# The NA48/2 experimental setup; Kaon beam

2003 + 2004 run: ~ 6 months, ~  $2 \cdot 10^{11}$   $K^\pm$  decays in flight



Simultaneous  $K^+$  and  $K^-$  beams:  
large charge symmetrization of  
experimental conditions



Beams coincide within ~1mm  
all along the 114m decay volume  
flux ratio  $K^+/K^- \sim 1.8$



# NA48/2 detector and performances

## LKr electromagnetic calorimeter :

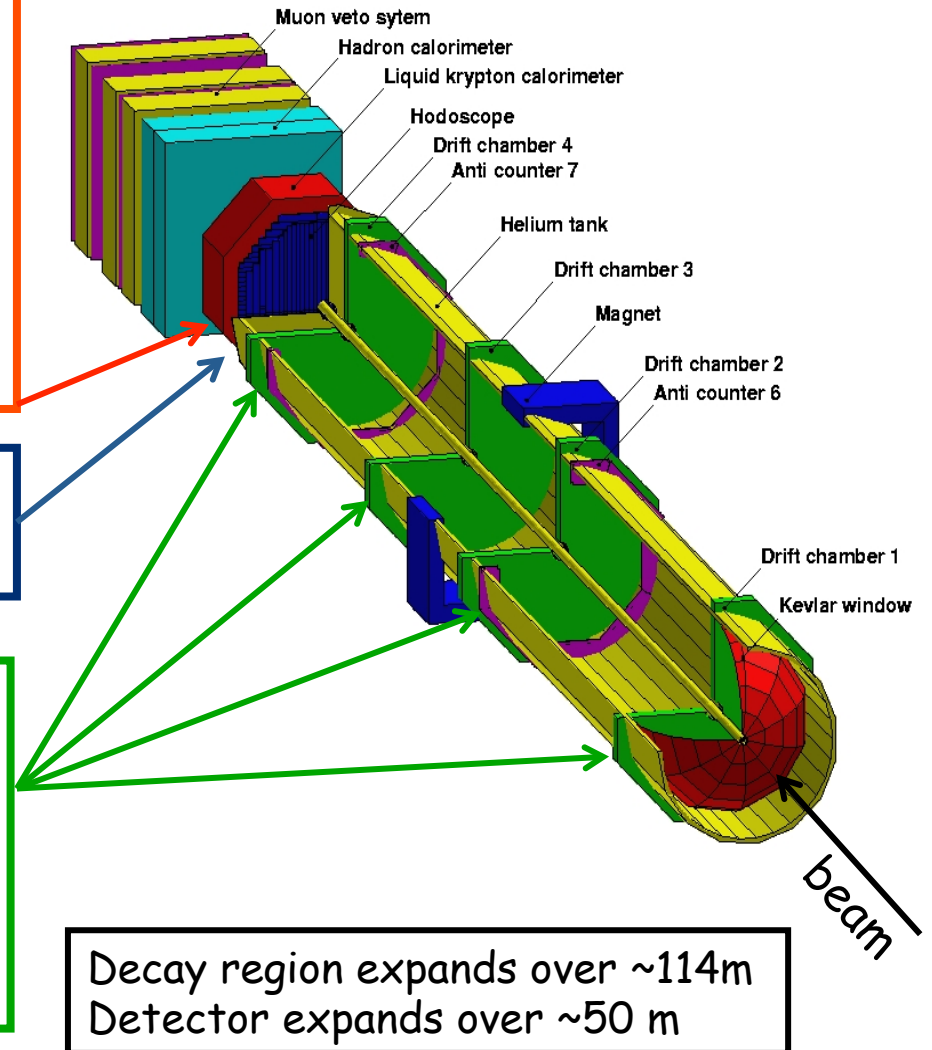
- quasi-homogenous and high granularity
- $\Delta E/E = (3.2/\sqrt{E} \oplus 9.0/E \oplus 0.42)\%$  (E in GeV)
- $\sigma_x = \sigma_y \sim 1.5 \text{ mm}$  for E=10 GeV
- Very good resolution for neutrals ( $\pi^0 \rightarrow \gamma\gamma$ )
- $\sigma(M_{\pi\pi^0\pi^0}) = 1.4 \text{ MeV}/c^2$
- E/p ratio can be used for e/ $\pi$  separation

## Hodoscope for fast charged trigger

precise time resolution  $\sigma_t = 150 \text{ ps}$

## Magnetic spectrometer :

- He tank to minimize multiple scattering
- 4 high-resolution DCH's + dipole magnet
- $\Delta p/p = (1.02 \oplus 0.044 p)\%$  (p in GeV/c)
- Very good resolution for charged invariant masses:  $\sigma(M_{3\pi^\pm}) = 1.7 \text{ MeV}/c^2$



# Chiral Perturbation Theory and Kaon decays

- Kaon decays are a perfect laboratory to study ChPT ( QCD at low energy )  
- see the many theory talks this week -

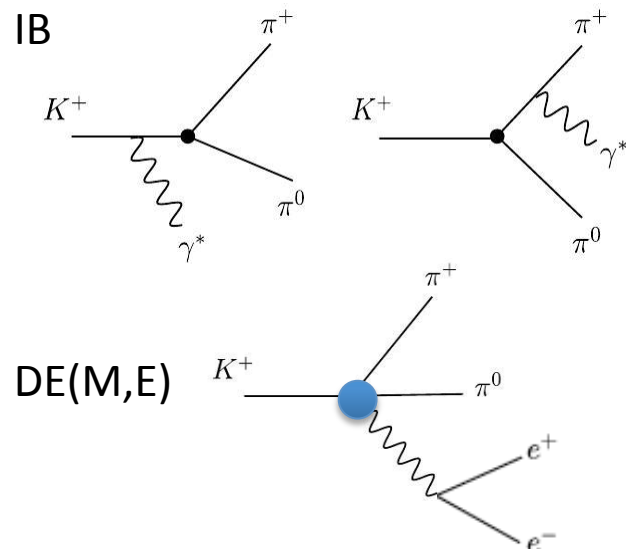
$K^\pm \rightarrow \pi^\pm l^+ l^-$  ,  $K^\pm \rightarrow \pi^\pm \gamma \gamma$  ,  $K^\pm \rightarrow \pi^\pm \pi^0 \gamma$  ,  $K^\pm \rightarrow \pi^\pm \pi^0 \gamma^* \rightarrow \pi^\pm \pi^0 e^+ e^-$  and more..  
 $\pi e e$  PLB 677 (2009),  $\pi \mu \mu$  PLB 697 (2011),  $\pi \gamma \gamma$  PLB730 (2014),  $\pi \pi^0 \gamma$  EPJC 68 (2010)

- What is so special about  $\pi^\pm \pi^0 e^+ e^-$  decay ?

H.Pichl, EPJ C20 (2001) 371

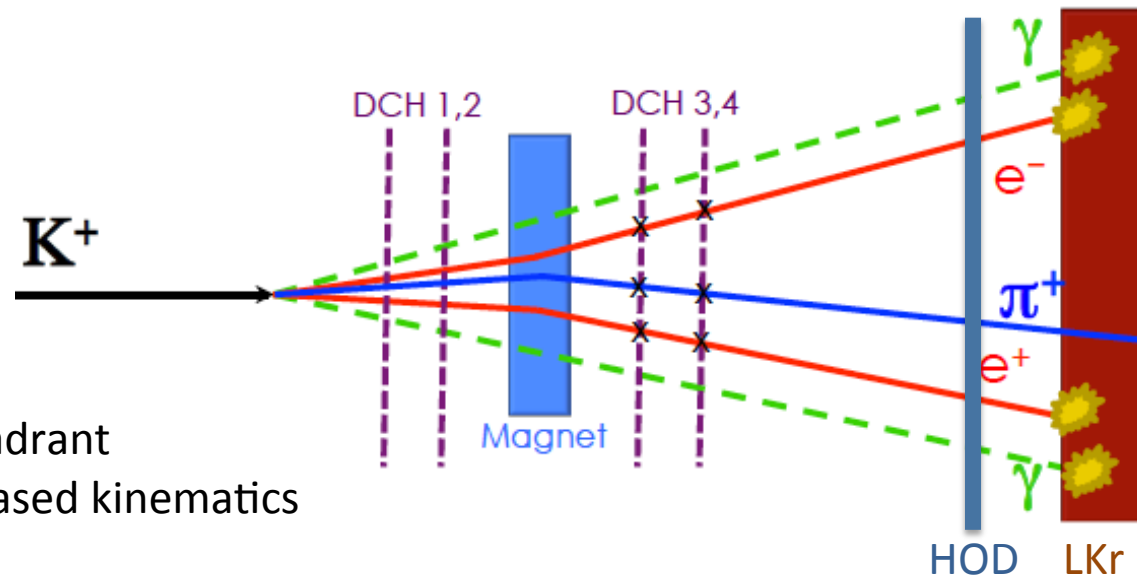
L. Cappiello, O. Catà, G. D'Ambrosio, D.Gao EPJ C72 (2012) 1872

$$\frac{d^3\Gamma}{dE_\gamma^* dT_c dq^2} = \frac{d^3\Gamma_{IB}}{dE_\gamma^* dT_c dq^2} + \frac{d^3\Gamma_E}{dE_\gamma^* dT_c dq^2} + \frac{d^3\Gamma_M}{dE_\gamma^* dT_c dq^2} + \frac{d^3\Gamma_{int}}{dE_\gamma^* dT_c dq^2}$$



- **Never observed so far**: confirmation of BR magnitude from ChPT predictions ?
- **If fine analysis possible** ( G.D'Ambrosio)
  - > sign of interference term (IB,E)
  - > Magnetic term through (IB,M) interference
  - > Charge asymmetry as direct CP violation (M.Pospelov)
- +.... > bump hunting in Mee spectrum

# Event selection : signal and normalization



Trigger:

L1 : > 1 HOD quadrant

L2 : DCH track based kinematics

**Signal:**  $\pi^\pm \pi^0 e^+ e^- = \pi^\pm \gamma \gamma e^+ e^-$

- Final state reconstructed from 3 charged track and 2 photons forming a  $\pi^0$  pointing to the same decay vertex

- Closed kinematics with two constraints on  $M_{\pi^0}, M_K$

- Differs from normalization by one extra  $\gamma$

**Normalization:**  $\pi^\pm \pi_D^0 = \pi^\pm e^+ e^- \gamma$

- Final state reconstructed from 3 charged tracks and 1 photon forming, with 2 opposite sign tracks, a  $\pi^0$  pointing to the same decay vertex

- Closed kinematics with two constraints on  $M_{\pi^0 D}, M_K$

- Very abundant:  $BR(\pi\pi^0) \times BR(\pi^0 D)$   
 $20.66\% \times 1.174\% = 2.425 \cdot 10^{-3}$

# Event selection: signal, normalization and backgrounds

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Signal:  $\pi^\pm \gamma \gamma e^+ e^-$

Normalization =  $\pi^\pm e^+ e^- \gamma$

Require 3 good quality tracks forming a vertex in the fiducial decay region

+ two good quality photon clusters

+ one good quality photon cluster

- do not use PID from LKr information but only kinematics
- no more limitation from LKr geometrical acceptance for tracks
- Assign electron mass to the track with Q opposite to vertex charge
- For both ( $m_e$ ,  $m_\pi$ ) assignments to same charge tracks, compute reconstructed  $M_{\pi^0}$  and  $M_{kaon}$  to be in a wide range and check kinematic correlation

$$| M_{\pi^0} - M_{PDG} | < 15 \text{ MeV}/c^2$$

$$| M_{kaon} - M_{PDG} | < 45 \text{ MeV}/c^2$$

$$| M_{\pi^0} - 0.42 m_K + 73.2 \text{ MeV}/c^2 | < 6 \text{ MeV}/c^2 \quad (\text{masses in MeV}/c^2)$$



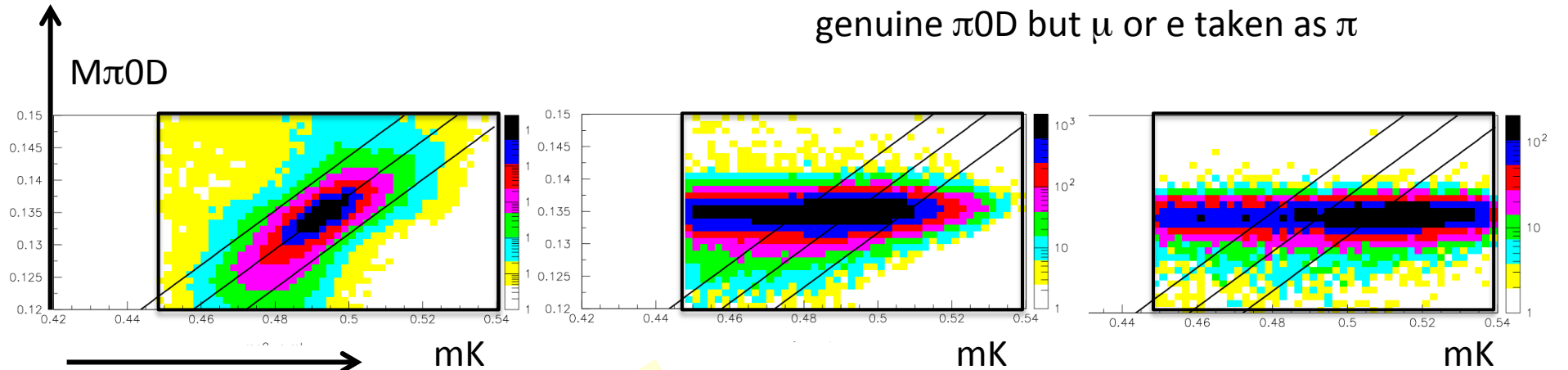
← Backgrounds →

Normalisation MC  $K \pi^0 D$

MC  $K\mu 3D = \mu \nu \pi^0 D$

MC  $Ke 3D = e \nu \pi^0 D$

genuine  $\pi^0 D$  but  $\mu$  or  $e$  taken as  $\pi$



99.1% in the band

54.6% in the band

34.6% in the band

NB: Log colour scale !

Signal MC  $K \pi^0 ee$

MC  $\pi^0 D$

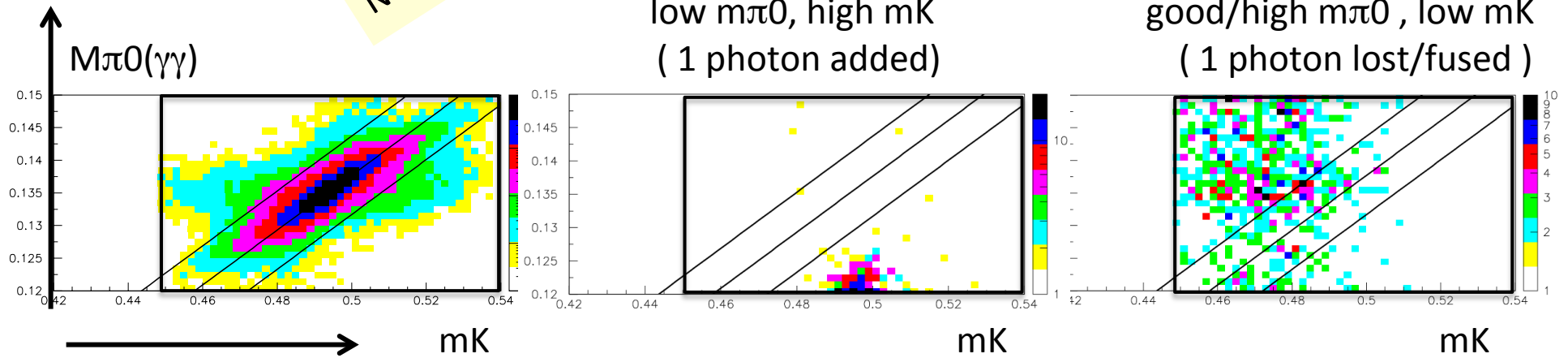
MC  $K \pi^0 \pi^0 D$

$\pi e e \gamma + \gamma$

$\pi e e \gamma \gamma (\gamma)$

low  $m_{\pi^0}$ , high  $m_K$   
( 1 photon added )

good/high  $m_{\pi^0}$ , low  $m_K$   
( 1 photon lost/fused )



96.5% in the band

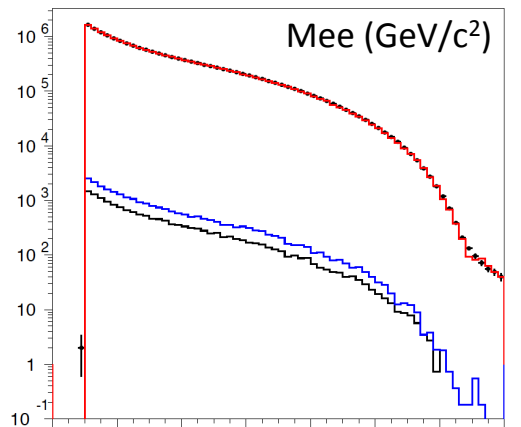
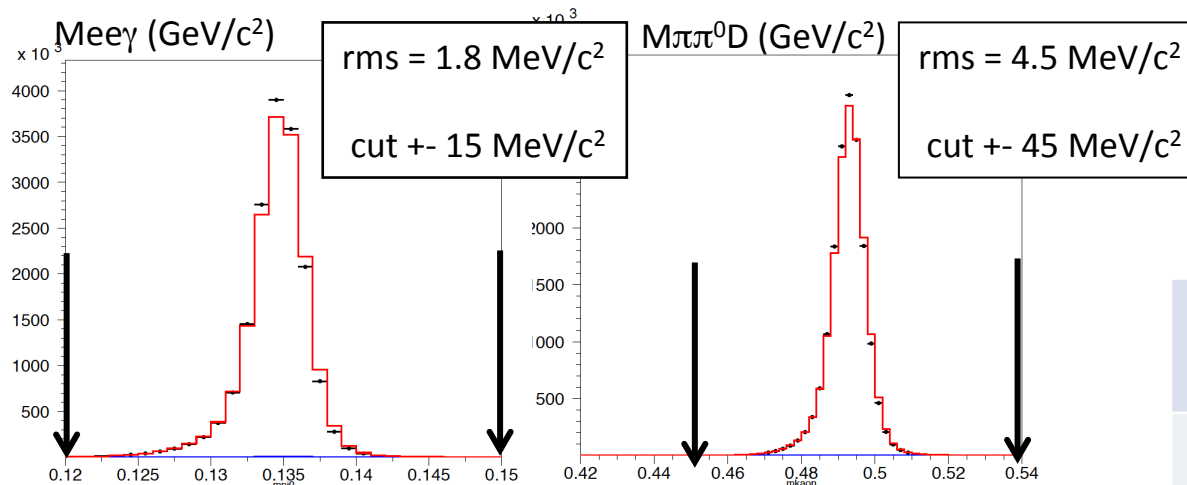
7.2% in the band

28.6% in the band

# Normalization : large very pure sample

## Normalisation $K \pi\pi^0 D$ :

- $K \pi\pi^0$  generator code including 1 real photon emission - Gatti EPJ C 45 (2006)
- $\pi^0 D$  decays including 1 extra photon emission - Husek, Kampf, Novotny PRD 92 (2015)
- also  $\pi^0 D$  decays including extra photon(s) emission - Photos Was et al CPC 79 (1994)



$K\mu^3$  Bkg 15182  $\pm$  173  
 $Ke^3$  Bkg 10334  $\pm$  140  
 $B/(S+B) = 0.15\%$   
 MC + rad cor.

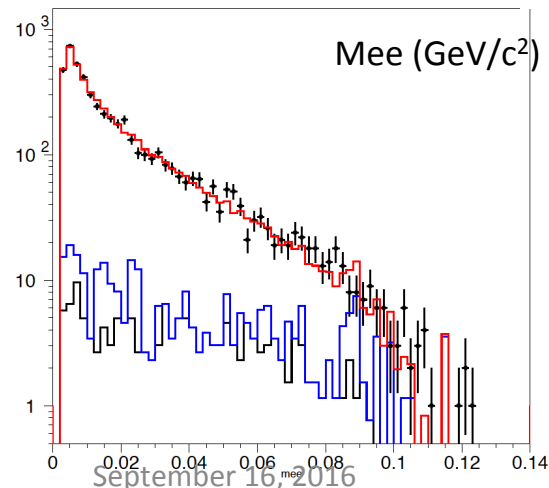
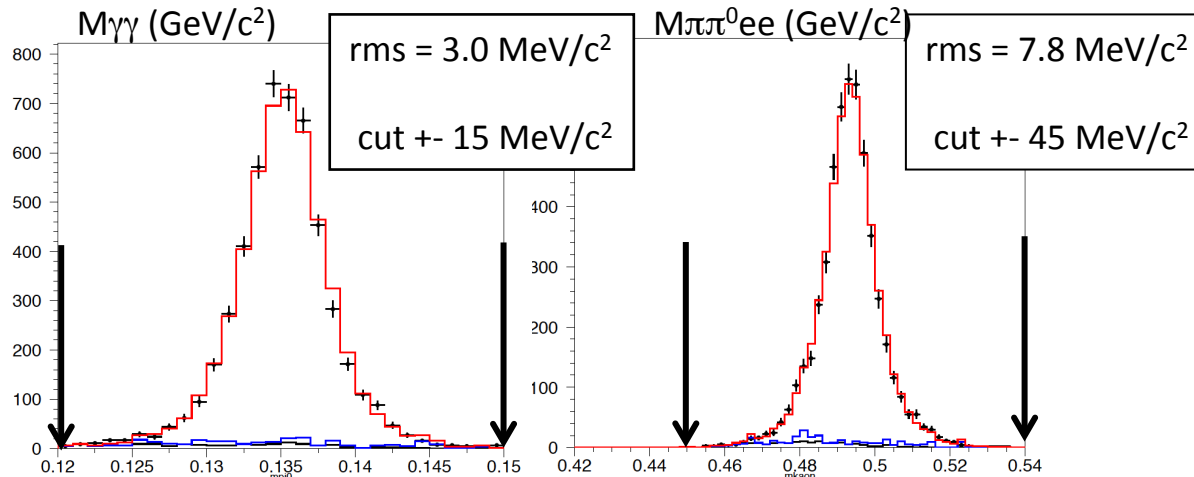
Normalization candidates	16 774 613
Background	25 517
A (rad cor HKN)	4.083 (2) %
L1 efficiency	99.767(3) %
L2 efficiency	98.584(7) %

$M_{ee} > 10 \text{ MeV}/c^2$ , low sensitivity to rad.corr. modeling

# Signal : small clean sample

Signal  $K \pi^0 e e$ : dominated by

- IB, then DE (M) and INT(IB,E) : 4 independent generations (IB, M, INT>0 and INT <0) with different acceptances ( A(M) and A(BE)  $\sim 3 \times A(\text{IB})$  )
- Rad. cor. adding extra photon(s) emission using Photos



$K3\pi D$  159  $\pm$  8  
 $K\pi^0 D$  130  $\pm$  24  
 $B/(S+B) = 5.4\%$   
 Signal IB +Photos

Signal candidates	5076
Background	289
A (rad cor) IB	0.650(1) %
A(rad cor) M	1.704(6) %
A(rad cor) INT>0	1.977(7) %
A(rad cor) INT <0	2.299(13) %
L1 efficiency	99.73(1) %
L2 efficiency	99.46(2) %

$M_{ee} > 3 \text{ MeV}/c^2$  , dominated by bkg at large values

# Branching ratio measurement and uncertainties

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$$BR = (N_s - N_{bs}) / (N_n - N_{bn}) \times (A_n / A_s) \times (\epsilon_{L1n} \times \epsilon_{L2n}) / (\epsilon_{L1s} \times \epsilon_{L2s}) \times BR_n$$

- **What is  $A_s$  ?** Define  $A_{eff}$  according to predicted fractions (IB/M) and (IB/BE) based on XE and XM measured in  $\pi\pi^0\gamma$  by NA48/2 (EPJ C68 (2010) 75):

$$[ A(IB) + 1/71 A(M) + 1/128 ( 0.732 INT>0 - 0.268 INT<0 ) ] / ( 1 + 1/71 + 1/128 )$$

$$A_{eff} = (0.666 \pm 0.001) \%$$

XE relative uncertainty  $\sim 30\%$  , XM relative uncertainty  $\sim 5\%$  translate to  
 $\delta A_{eff} / A_{eff} \sim 0.25\%$  due to mixture composition

- **Radiative corrections modeling ?**

$A_n$  : compare HKN and Photos implementations

Acceptances are close thanks to the  $M_{ee} > 10 \text{ MeV}/c^2$

quote the statistical error on the difference as systematics  $\sim 0.30\%$

$A_s$  : compare Photos and no Photos Acceptances, quote 1/10 of full effect  $\sim 0.48\%$

$\delta A_{eff} / A_{eff} \sim 0.56\%$  combined due to rad cor modeling

# Branching ratio measurement ingredients

Normalization candidates	16 774 613
Background	25 517
A (rad cor HKN)	4.083 (2) %
L1 efficiency	99.767(3) %
L2 efficiency	98.584(7) %

Signal candidates	5076
Background	289
A (rad cor) eff	0.666(1) %
L1 efficiency	99.73(1) %
L2 efficiency	99.46(2) %

Source	$\delta\text{BR}/\text{BR} \times 10^2$	
Ns	1.40	stat 1.49
Nbs	0.51	
Nn	0.02	
Nbn	Negl.	
As	0.18	
An	0.05	syst 1.03
L1n x L2n	0.01	
L1s x L2s	0.04	
A (rad corr)	0.56 *	
A (fraction DE,INT)	0.25 *	
Trigger efficiency	0.80 *	ext 3.00
BR $2\pi$	0.39	
BR $\pi 0D$	2.98	

\* = not final



# Branching ratio measurement @ NA48/2

$$BR = (4.22 \pm 0.06_{\text{stat}} \pm 0.04_{\text{syst}} \pm 0.13_{\text{ext}}) 10^{-6}$$

dominated by external error on BR( $\pi^0 D$ )

In perfect agreement with

Theory : ChPT calculations EPJ C72 (2012)

IB + DE + INT

BR (IB) =  $4.19 \cdot 10^{-6}$  no Rad Cor, No Isospin breaking Cor

Total  $4.29 \cdot 10^{-6}$

BR (IB) =  $4.10 \cdot 10^{-6}$  no Rad Cor, with Isospin breaking Cor\*\*

Total  $4.19 \cdot 10^{-6}$

(\*\* private communication from authors)

# Summary

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- NA48/2 has collected a clean sample of  $\sim 5000$   $\pi^0 e^+ e^-$  decay candidates with  $\sim 5\%$  background : first observation leading to a 3-4% BR measurement in perfect agreement with ChPT predictions.
- $BR = (4.22 \pm 0.08_{\text{exp}} \pm 0.13_{\text{ext}}) 10^{-6}$   
uncertainty is dominated by external error  
experimental error is dominated by signal statistics
- discussion with theorists is most important for a correct and precise formulation of radiative and isospin breaking corrections

Close to final !

Prospects to collect more decays in the current NA62 run :

- requiring 3 tracks + large electromagnetic energy incompatible with  $\pi^0 \nu \nu$  trigger
- parasitic 3-track trigger downscaled by a large factor : no way to collect more data than in 2003-2004 with this trigger ( $1.74 \cdot 10^{11}$  charged kaon decays analyzed)
- could be studied in Run 3 after LS2 (after 2020) with dedicated trigger

# Spares

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# What more ?

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Measure BR(K+) and BR(K-) as independent quantities

Statistics is even more limited as  $K^+/K^- \approx 1.8$  at production target

	K+	K-		K+	K-
Norm candidates	10776792	5997821	signal	3234	1842
Bkg	0.15%		Bkg	5%	
A (rad cor HKN)	4.087 (3) %	4.075 (4)%	Aeff	0.6687 (13) %	0.6605 (17) %
L1 efficiency	99.767(3) %		L1	99.73(1) %	
L2 efficiency	98.584(7) %		L2	99.46 (2) %	

$$BR(K^+) = (4.17 \pm 0.08) \times 10^{-6}$$

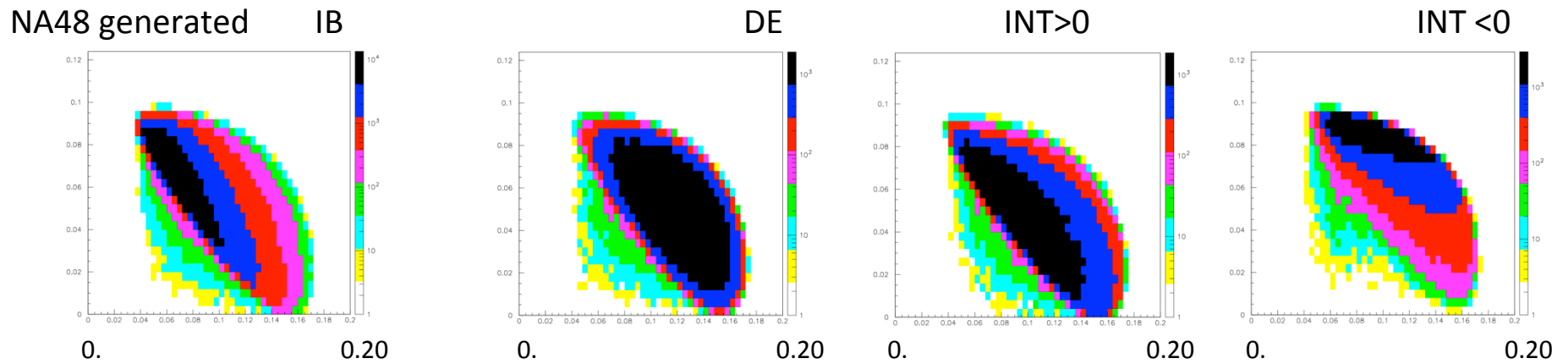
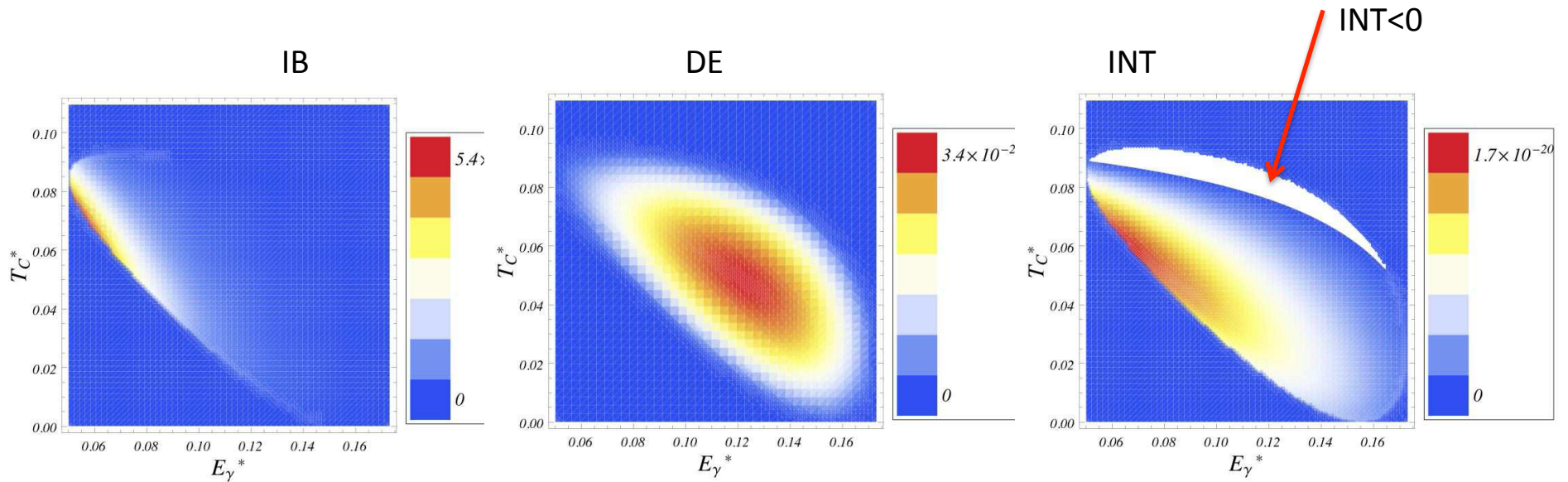
$$BR(K^-) = (4.30 \pm 0.11) \times 10^{-6}$$

$$\frac{(BR(K^+) - BR(K^-))}{(BR(K^+) + BR(K^-))} = -0.015 \pm 0.016$$

(stat errors only)

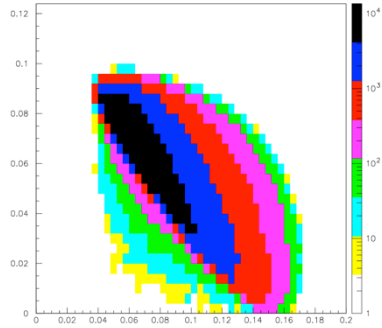
# and more ?

Cappiello et al. suggest to look at  $m_{ee} \sim 50 \text{ MeV}/c^2$  where IB, DE, INT populate differently the  $(E_\gamma^*, T^*\pi)$  plane

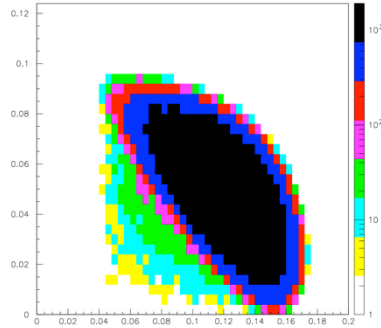




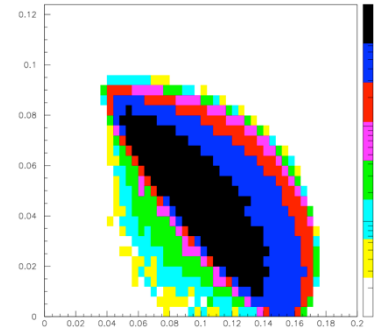
NA48 generated IB



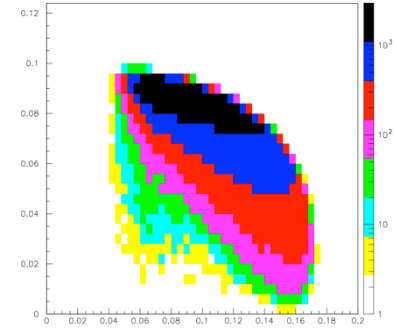
DE



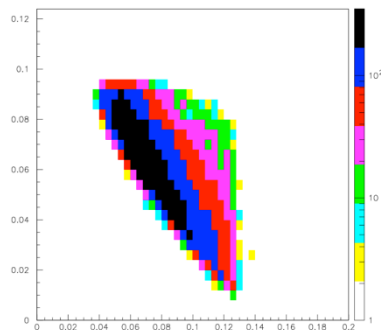
INT>0



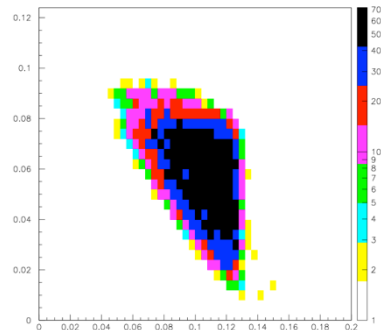
INT <0



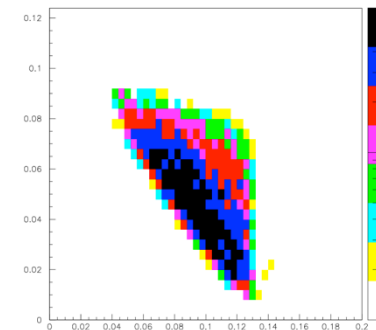
NA48 accepted IB  
2.9%



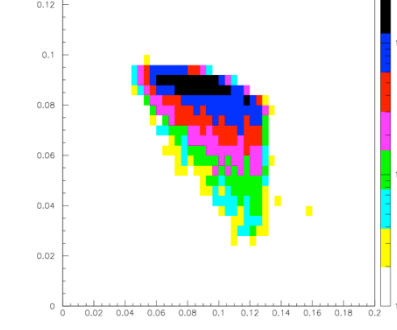
DE  
2.1%



INT>0  
2.3%



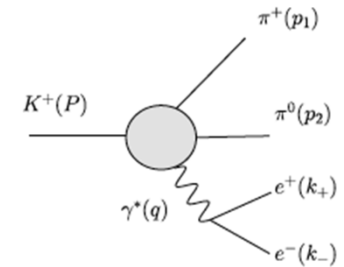
INT <0  
4.2%



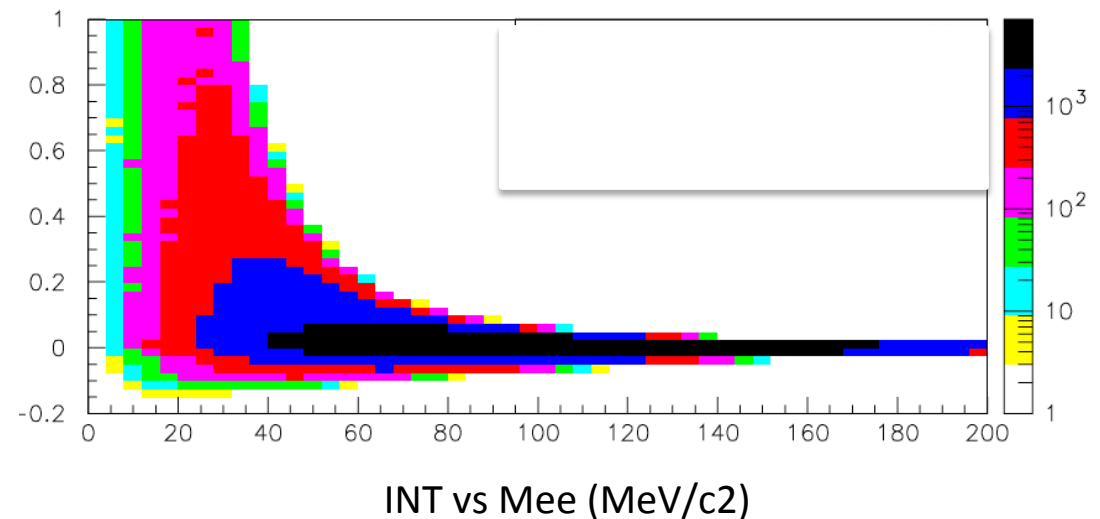
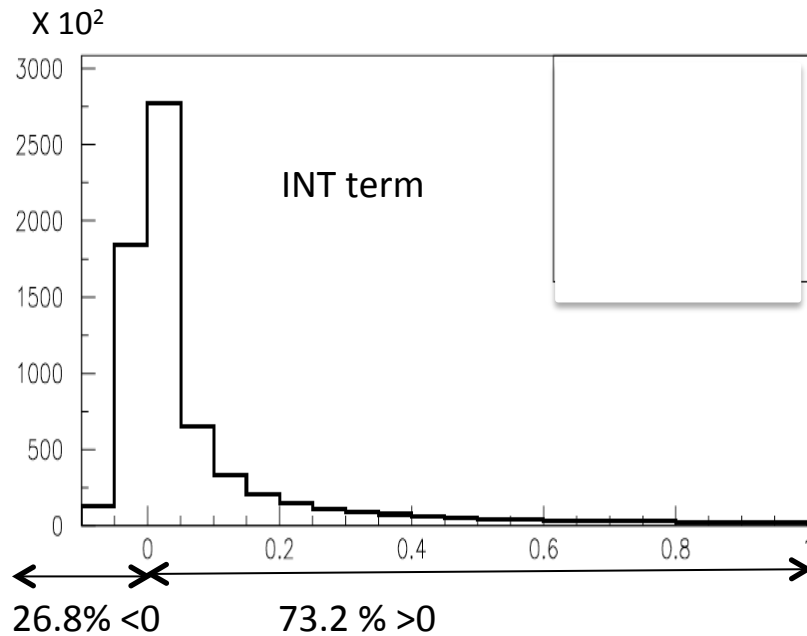
After acceptance, we would need large statistics to disentangle the various contributions ...

The INT term ( Capiello et al EPJ C72 (2012) 1872)

$$\frac{d^3\Gamma}{dE_\gamma^* dT_c^* dq^2} = \frac{d^3\Gamma_B}{dE_\gamma^* dT_c^* dq^2} + \frac{d^3\Gamma_E}{dE_\gamma^* dT_c^* dq^2} + \frac{d^3\Gamma_M}{dE_\gamma^* dT_c^* dq^2} + \frac{d^3\Gamma_{int}}{dE_\gamma^* dT_c^* dq^2},$$



Dominated by IB, DE mostly M (IB/M ~ 71) , INT mostly BE (IB/BE ~128)  
Independent MC simulations of IB, DE and INT terms but ....



- INT<0 relative contribution increasing with Mee
- Two MC simulations, INTp according to INT if >0 , INTn according to -INT if <0
- Combined acceptance obtained as:

$$[ A(\text{IB}) + 1/71 A(\text{DE}) + 1/128 ( 0.732 \text{INTp} - 0.268 \text{INTn} ) ] / ( 1 + 1/71 + 1/128 )$$