



# Loophole in $K \rightarrow \pi\nu\nu$ Search & $K_L \rightarrow \pi^0\nu\nu$ Beyond Grossman-Nir Bound

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15 Sept @ KAON 2016, Birmingham



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# $K_L \rightarrow \pi^0 \nu \bar{\nu}$ Beyond Grossman-Nir Bound



## Outline

I. Intro: Kaon, as old as Particle Physics

...  $KOTO$ 's public neglect, Until Now!

II. Blinding  $[K^+ \rightarrow \pi^+] \pi^0$ : Blessed are the Blind

—  $K_L \rightarrow \pi^0 + \text{Nothing}$  above “GN Bound”? —

[CMS  \$\rightarrow\$  Kaon](#)

III. A Motivated Model (existence proof)

Gauged  $L_\mu - L_\tau$  related to muon  $g - 2$  + ...

IV. What Then? — an Illustration of Impact

“Exotic” Rare K & B Decays

V. Conclusion

Fuyoto, WSH, Kohda, 1412.4397 (PRL'15)  
and 1512.09026 (PRD'16)



69+

# I. Intro: Kaon, as old as Particle Physics

and Andrzej



- $V$  particles from cosmic
- $g - 2 = \alpha/\pi$  at one loop
- But still NP Frontier:

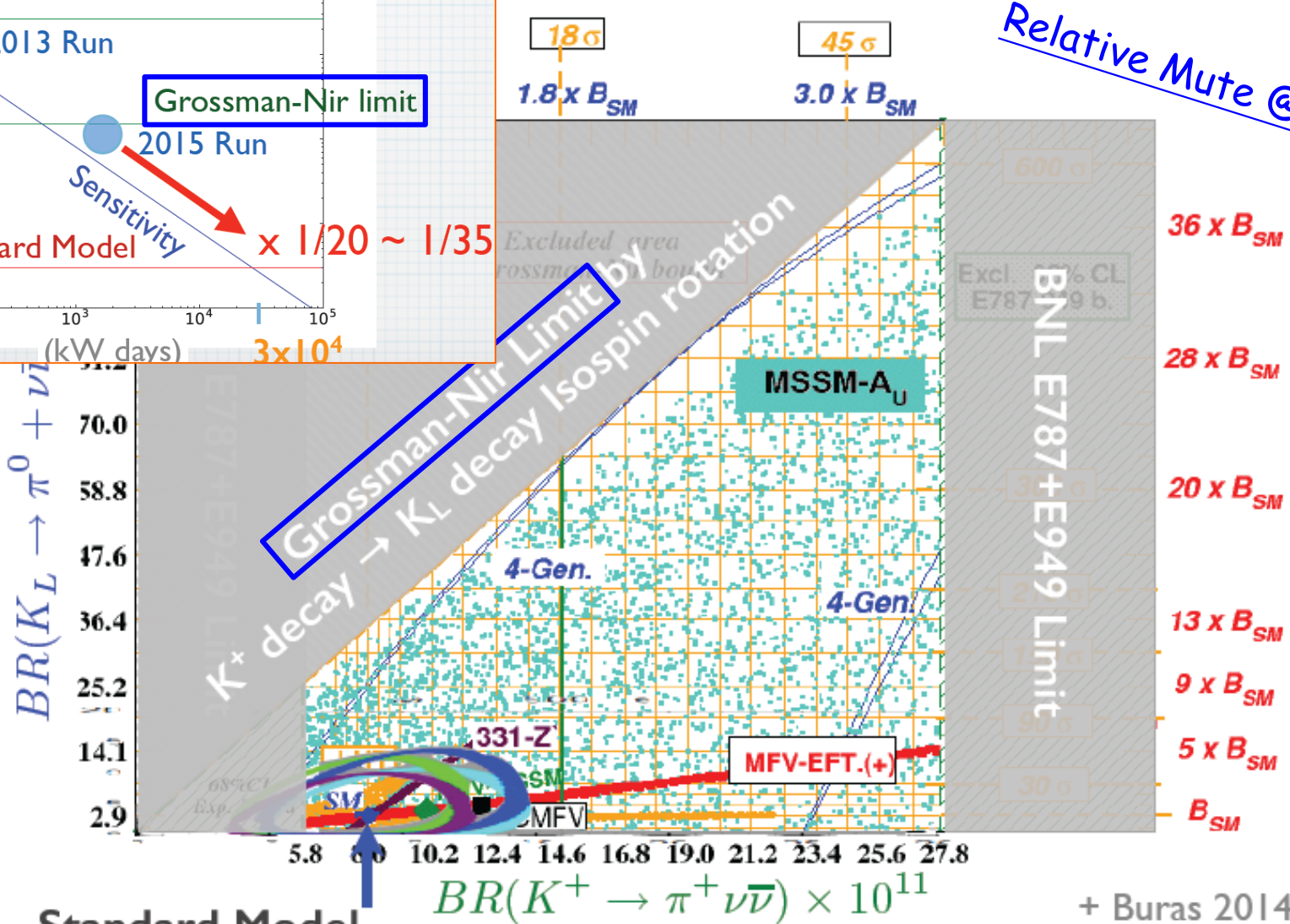
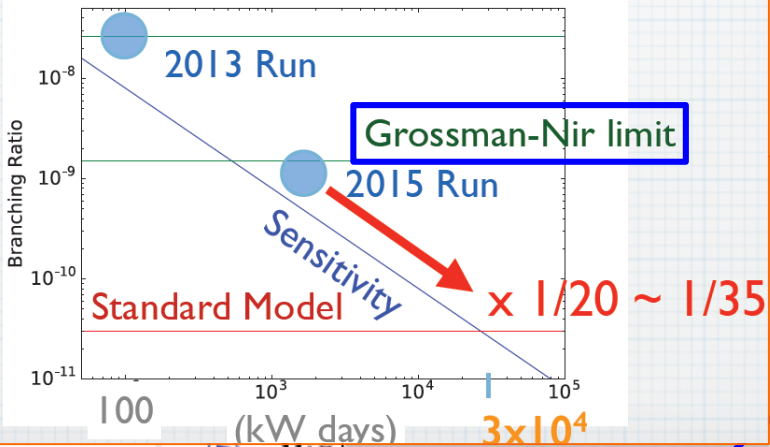




# Taku at FPCP2016, Caltech



p. 26



+ Buras 2014

<http://www.lnf.infn.it/wg/vus/content/Krare.html>

p. 14

$K_L \rightarrow \pi^0 \nu\bar{\nu} > GN?$

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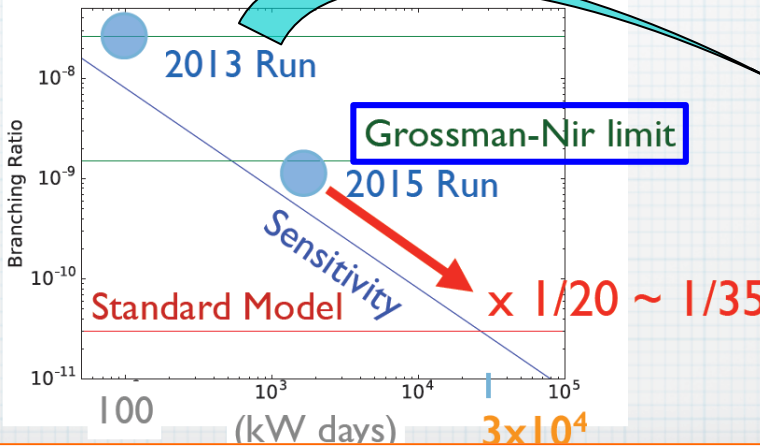


# ... KOTO's public neglect, Until Now!



1609.03637, and Shiomi's talk

p. 26



**PTEP**

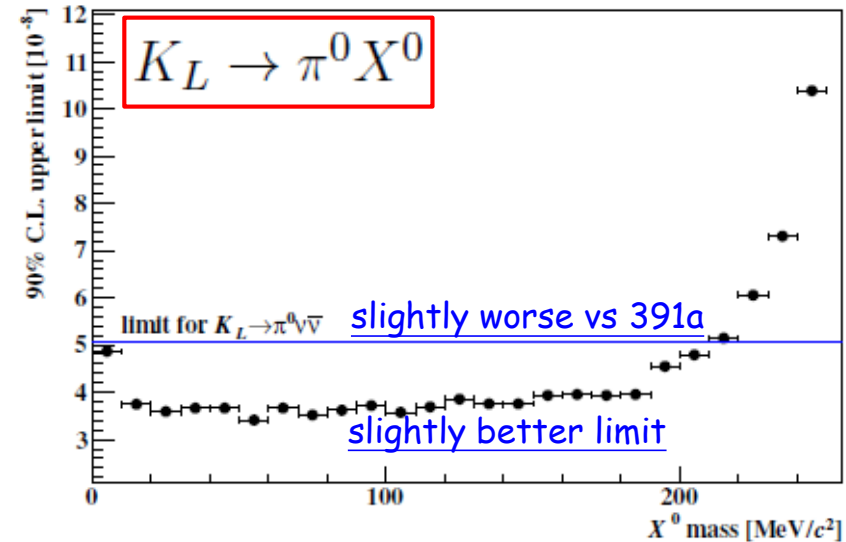
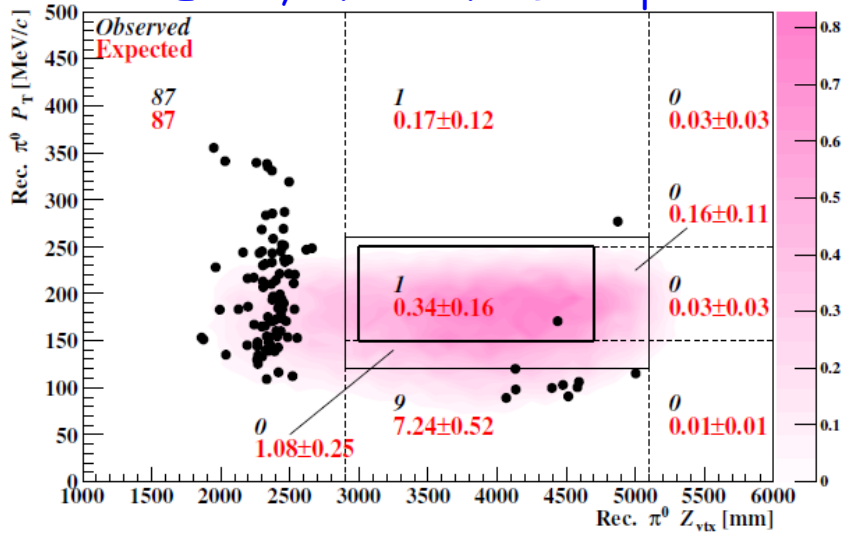
Prog. Theor. Exp. Phys. **2015**, 00000 (11 pages)  
DOI: 10.1093/ptep/0000000000

## A New Search for the $K_L \rightarrow \pi^0 \nu \bar{\nu}$ and $K_L \rightarrow \pi^0 X^0$ decays

J-PARC KOTO collaboration

We searched for the  $CP$ -violating rare decay of neutral kaon,  $K_L \rightarrow \pi^0 \nu \bar{\nu}$ , in data from the first 100 hours of physics running in 2013 of the J-PARC KOTO experiment. **One candidate event** was observed while  $0.34 \pm 0.16$  background events were expected. We set an **upper limit of  $5.1 \times 10^{-8}$**  for the branching fraction at the 90% confidence level (C.L.). **An upper limit of  $3.7 \times 10^{-8}$  at the 90% C.L. for the  $K_L \rightarrow \pi^0 X^0$  decay was also set** for the first time, where  $X^0$  is an invisible particle with a mass of  $135 \text{ MeV}/c^2$ .

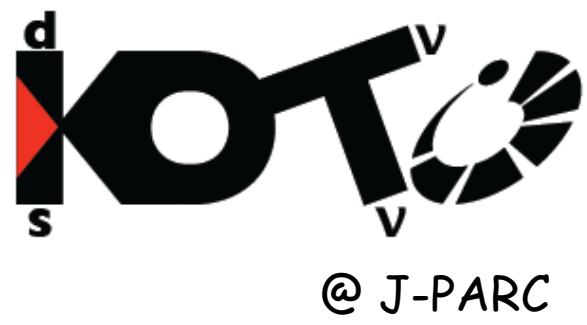
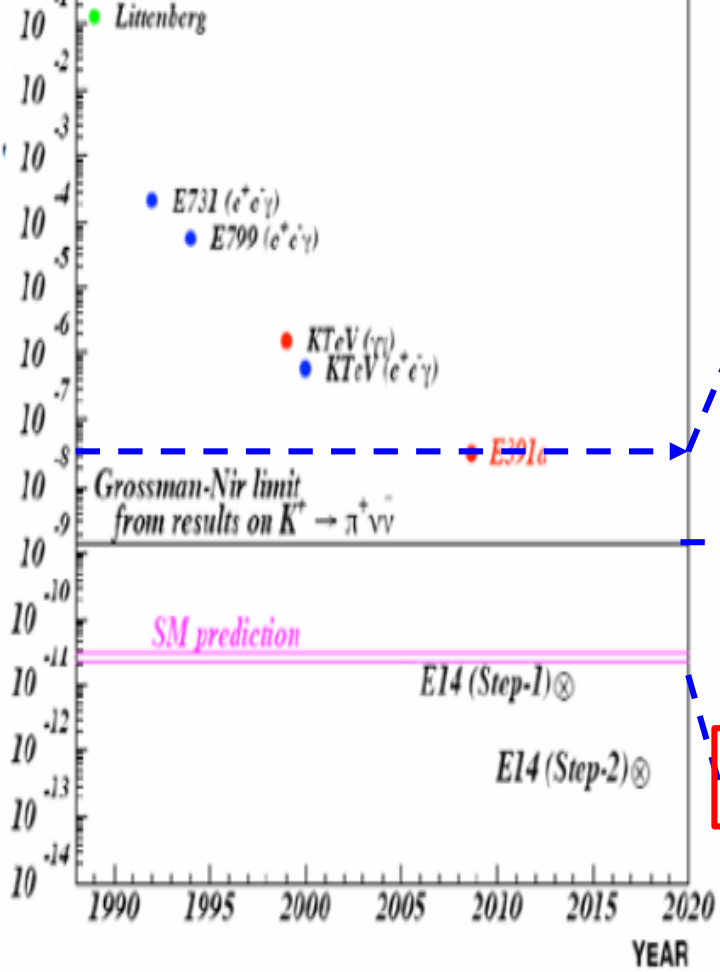
One Event,  $0.34 \pm 0.16$  BG expected



$K_L \rightarrow \pi^0 \nu \bar{\nu} > \text{GN?}$

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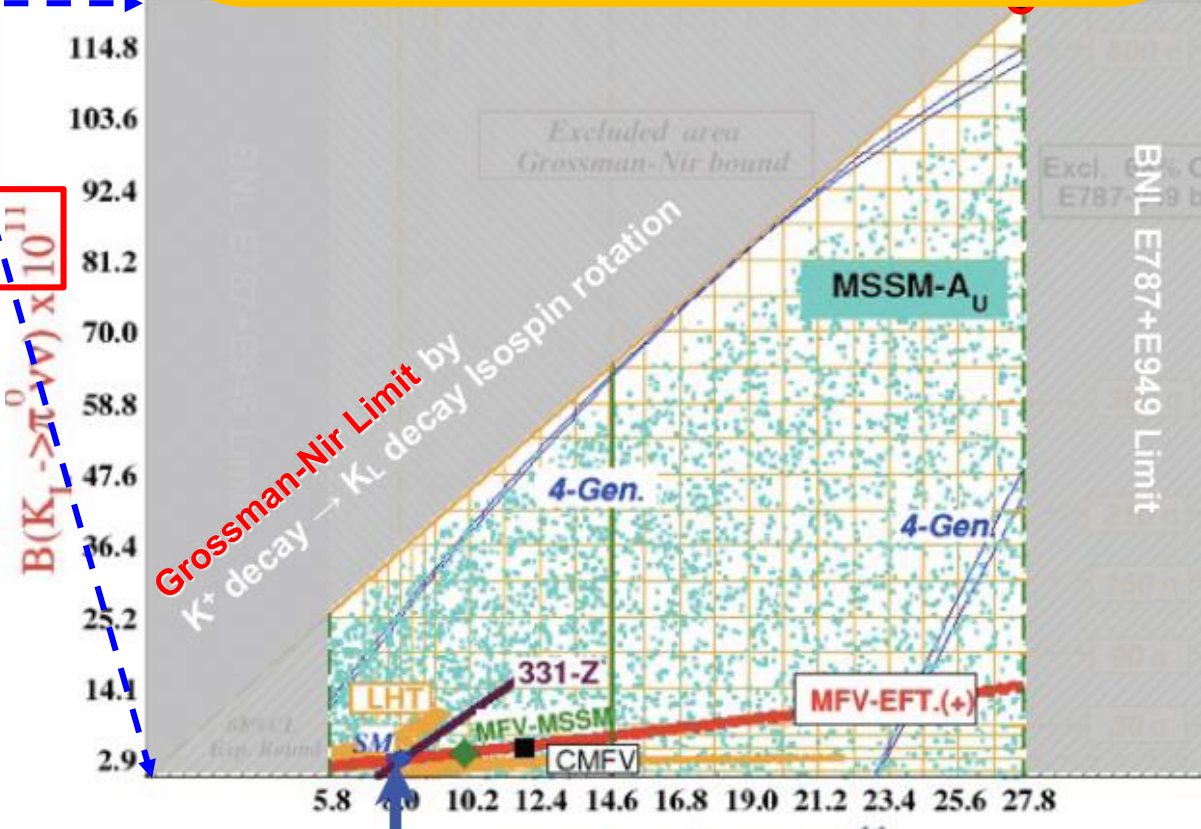
mostly  $\tau_{K_L}/\tau_{K^+}$

$$\mathcal{B}(K_L \rightarrow \pi^0 \nu \bar{\nu}) \lesssim 4.3 \times \mathcal{B}(K^+ \rightarrow \pi^+ \nu \bar{\nu})$$

$$< 1.4 \times 10^{-9}. \quad (\text{GN bound})$$

**KOTO @ 100 hrs (2013), paper finally ...**

Shaken It Off!



$K_L \rightarrow \pi^0 \nu \bar{\nu} > \text{GN?}$

Excl. E787+ E949 Limit  
BNL E787+E949 Limit



## II. Blinding $[K^+ \rightarrow \pi^+] \pi^0$ : Blessed are the Blind

Or: Stupid is as stupid does.

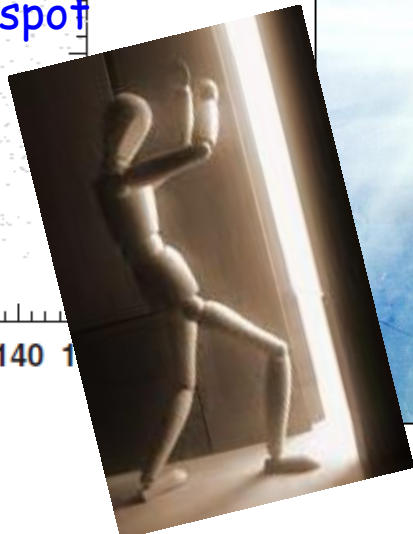
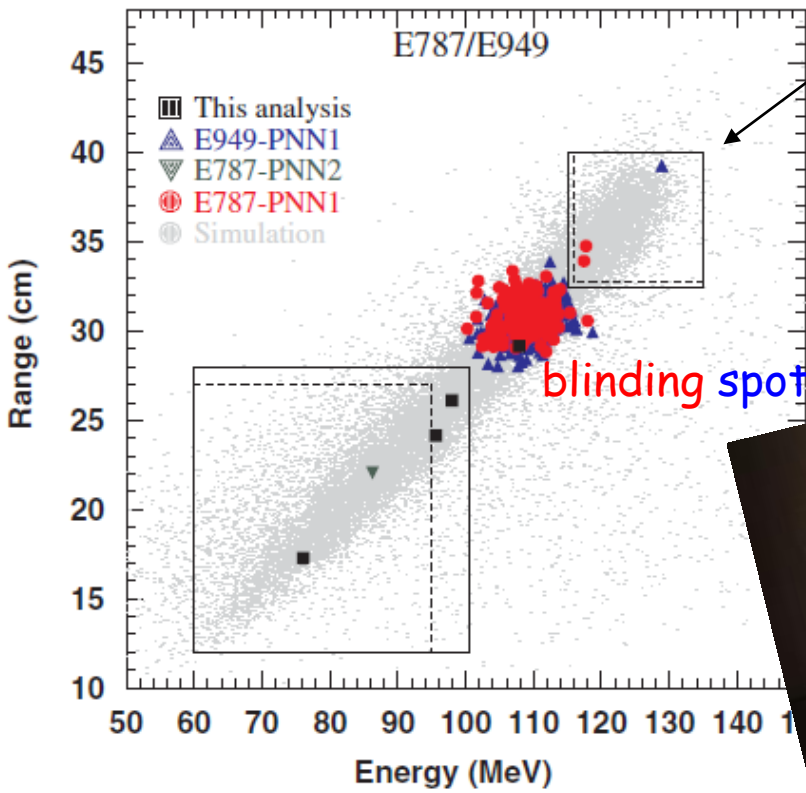


# The Blinding $K^+ \rightarrow \pi^+\pi^0$



I (We) have (all) stared at this gazillion times, and became numb.

PHYSICAL REVIEW D 79, 092004 (2009)







# The Blinding $K^+ \rightarrow \pi^+ \pi^0$

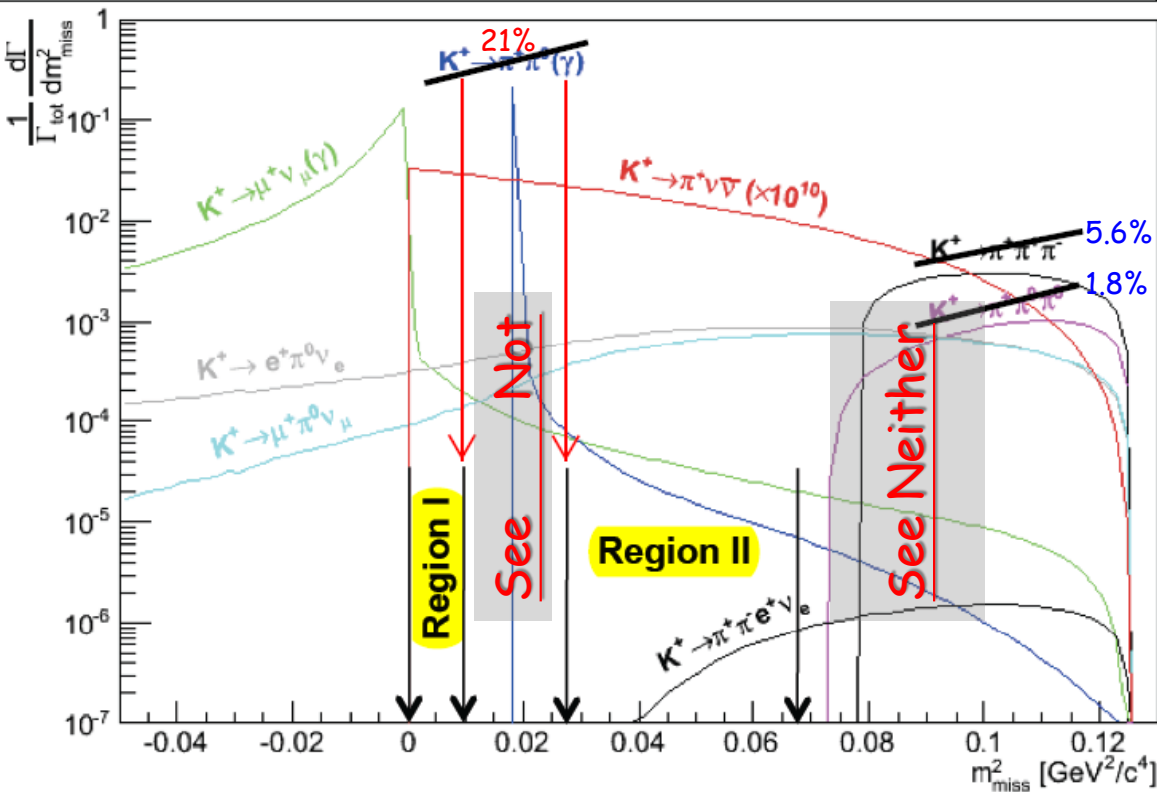


Window basically Same as E787/949 @ BNL

@ CERN

Kinematic exclusion:

exclude  $0.01 - 0.025 \text{ GeV}^2$  [ $(100)^2 - (160)^2 \text{ MeV}^2$ ]



**Kinematic Control:**  
use  $K^+$  and  $\pi^+$  momenta to block out blinding zone



# The Blinding $K^+ \rightarrow \pi^+ \pi^0$



Not a great limit

BV. The E949 limit of  $\mathcal{B}(\pi^0 \rightarrow \nu\bar{\nu}) < 2.7 \times 10^{-7}$  at 90% C.L. [60] can be combined with the world average value of  $\mathcal{B}(K^+ \rightarrow \pi^+ \pi^0)$  [24] to set a 90% C.L. limit of  $\mathcal{B}(K^+ \rightarrow \pi^+ X) < 5.6 \times 10^{-8}$  for  $M_X = M_{\pi^0}$  with  $X$  stable

PHYSICAL REVIEW D 79, 092004 (2009)

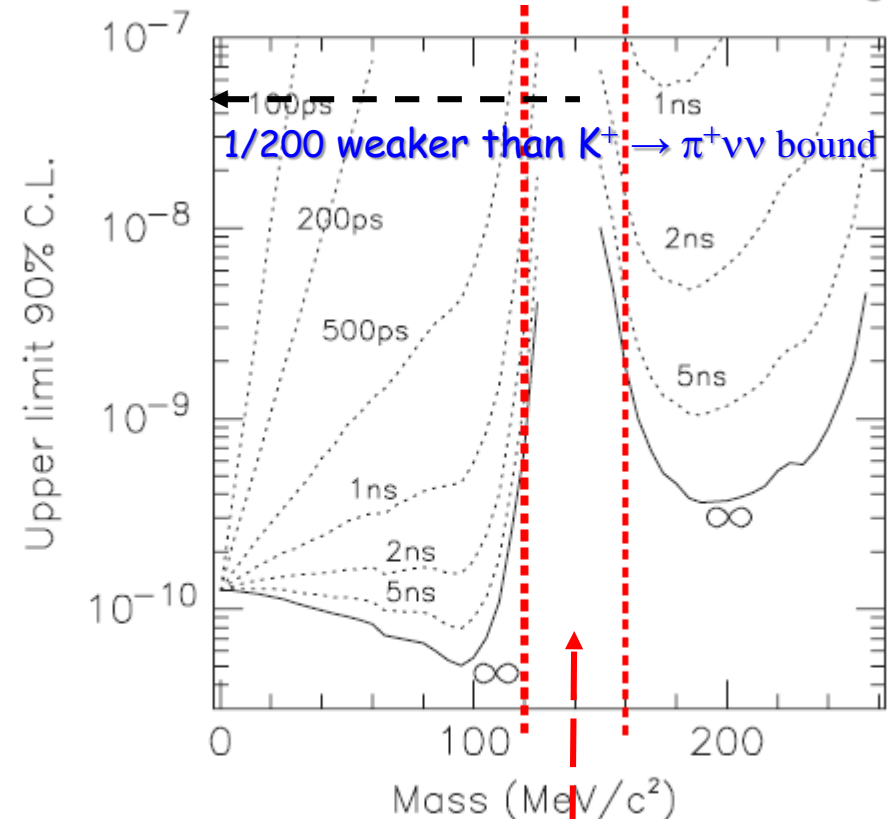
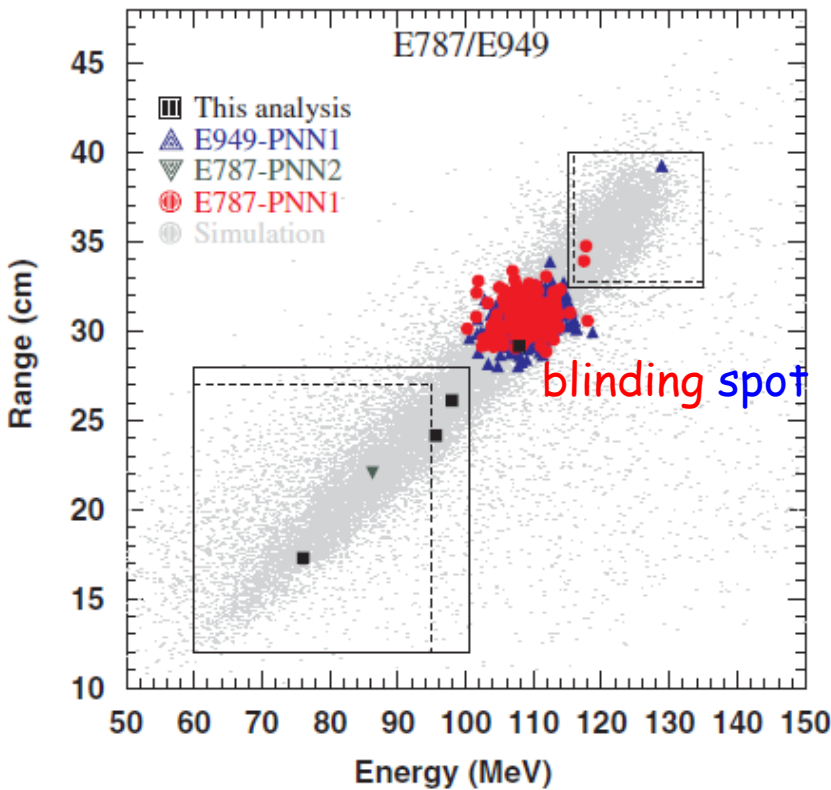
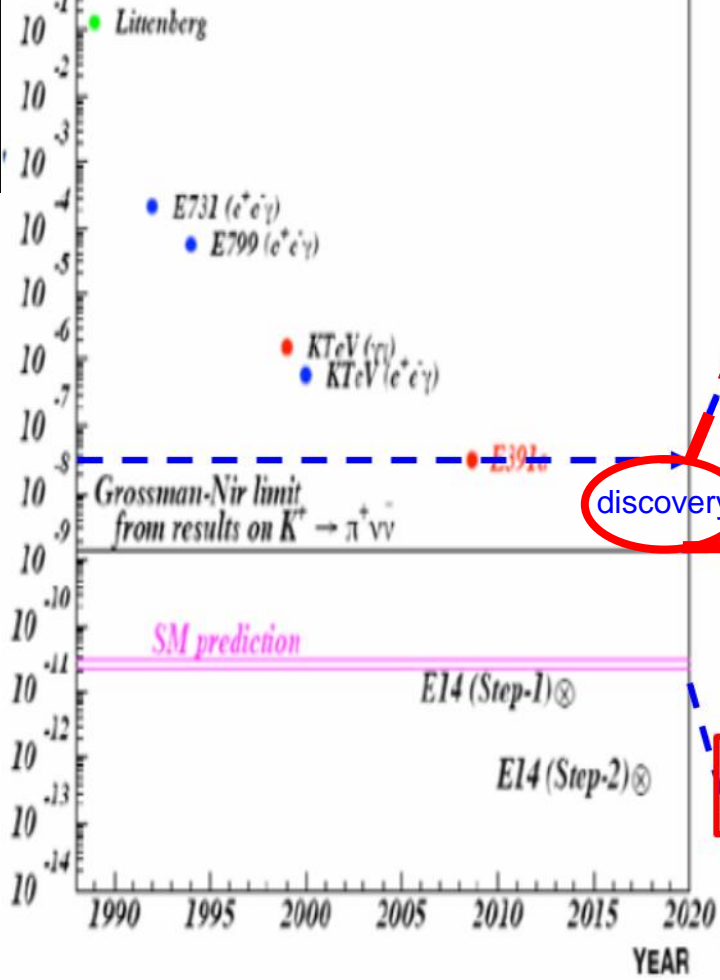


FIG. 18. The solid lines represent the 90% C.L. upper limit on  $\mathcal{B}(K^+ \rightarrow \pi^+ X)$  as a function of the mass of  $X$  assuming  $X$  is

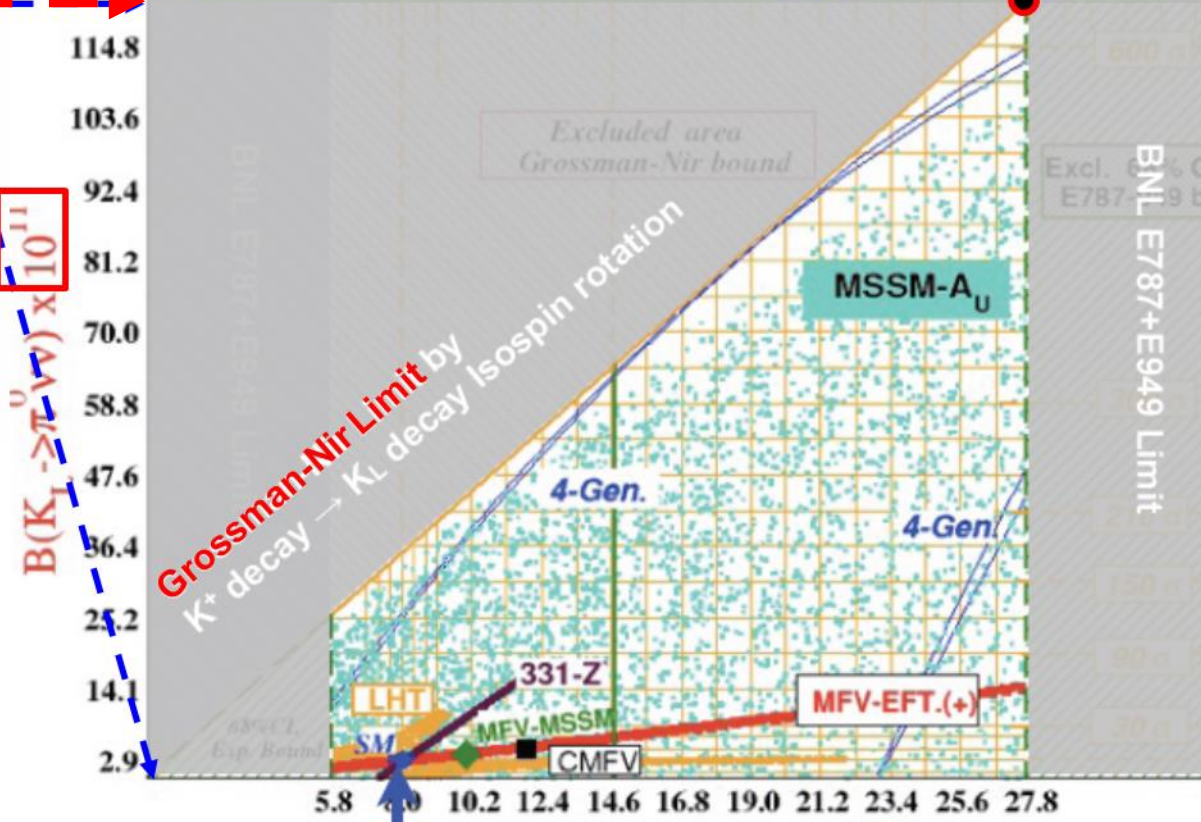
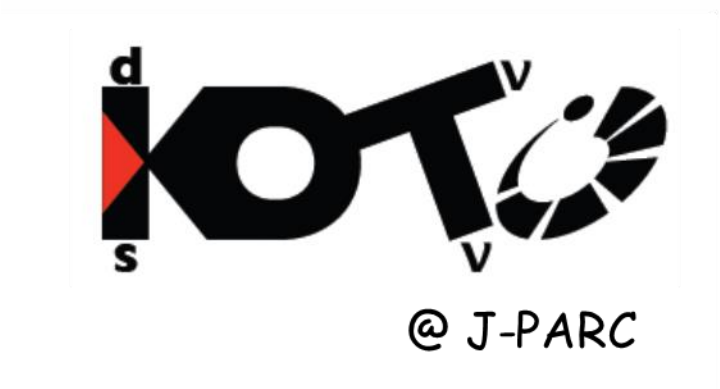




**Discovery Starting "Now"! It Off!**

The KOTO Expt at J-PARC can discover  $K_L \rightarrow \pi^0 X^0$  above the Grossman-Nir Bound!

KOTO @ 100 hrs (2013), paper finally ...



$K_L \rightarrow \pi^0 \nu \bar{\nu} > GN?$

Standard Model  $B(K^+ \rightarrow \pi^+ \nu \bar{\nu}) \times 10^{11}$



Continuing from what Pospelov  
left off this morning ...  $K_L$

—  $K_L \rightarrow \pi^0 + \text{Nothing}$  above “GN Bound”? —

- What you learned in “school” not quite right
- Seeing the possibility was inadvertent
- It all started from *CMS* & *TopCNC* Pheno ...

A Story of *CMS*-related work leading to Kaon physics ... ☺



### III. A Motivated Model (existence proof)

gauged  $L_\mu - L_\tau$  related to muon  $g - 2$   
+ ...



# Gauged $L_\mu - L_\tau$ model

Altmannshofer, Gori, [Pospelov](#) and Yavin, PRD89, 095033 (2014)

- $U(1)'$ : gauging  $L_\mu - L_\tau$  ( $\mu$ -number minus  $\tau$ -number)  
 → anomaly free within SM particle content

X.G. He et al., PRD1991

- $U(1)'$  breaking:  $\langle \Phi \rangle = \frac{v_\Phi}{\sqrt{2}}$ 
  - SM singlet
  - $U(1)'$  charge +1
  - $Z'$  mass:  $m_{Z'} = g' v_\Phi$
  - $L_\mu - L_\tau$  current:

$$\mathcal{L} \supset -g' Z'_\alpha (\bar{\mu} \gamma^\alpha \mu + \bar{\nu}_{\mu L} \gamma^\alpha \nu_{\mu L} - \bar{\tau} \gamma^\alpha \tau - \bar{\nu}_{\tau L} \gamma^\alpha \nu_{\tau L})$$

- Quarks? Introduce New **Vector-like Quarks**

	<u>"4G" chiral quarks</u>			<u>chiral partners</u>		
	$Q_L = \begin{pmatrix} U_L \\ D_L \end{pmatrix}$	$U_R$	$D_R$	$\tilde{Q}_R = \begin{pmatrix} \tilde{U}_R \\ \tilde{D}_R \end{pmatrix}$	$\tilde{U}_L$	$\tilde{D}_L$
$U(1)'$ charges:	+1	-1	-1	+1	-1	-1

g.i. mass, plus  
Yuk. Mixing w/  
SM Quarks



# $P_5'$ -motivated $Z'$ induces $t \rightarrow cZ'$ also

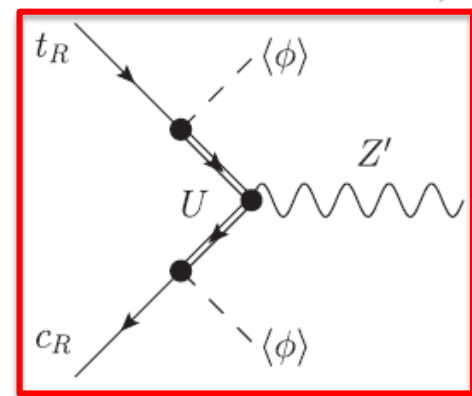
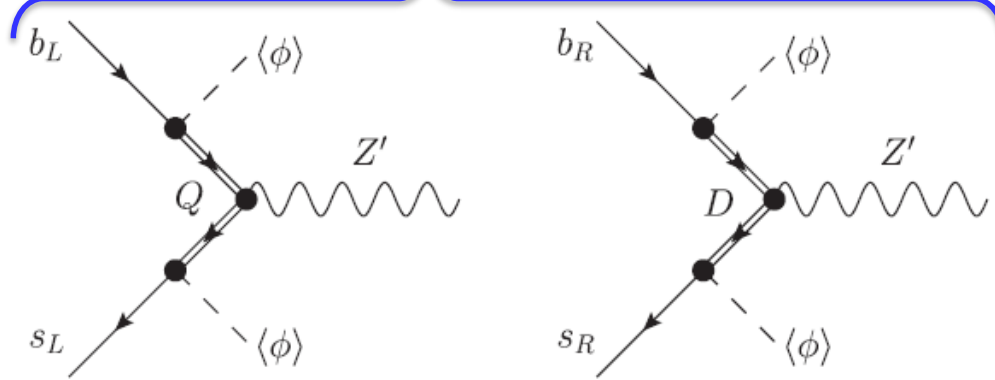


$B \rightarrow K^* \mu^+ \mu^-$

Our Original Interest

ALTMANNSHOFER *et al.*

PHYSICAL REVIEW D 89, 095033 (2014)



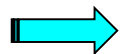
$Q, D, U$ : vector-like quarks with  $Z'$  charge

$$\text{BR}(t \rightarrow Z' c) \simeq \frac{2(1-x')^2(1+2x')}{(1-x)^2(1+2x)}$$

$$x = \frac{m_W^2}{m_t^2}, \quad x' = \frac{m_{Z'}^2}{m_t^2}$$

$$\times \left( |Y_{Qt} Y_{Qc}^*|^2 \frac{v^2 v_\Phi^2}{4m_Q^4} + |Y_{Ut} Y_{Uc}^*|^2 \frac{v^2 v_\Phi^2}{4m_U^4} \right)$$

"unconstrained"



Should Search for  $t \rightarrow cZ' \rightarrow c\mu^+\mu^-$

$Z' \rightarrow \mu^+\mu^-$

BR  $\sim 1/3!$

"gauged  $L_\mu - L_\tau$ "





# Linking Leptonic $Z'$ to **Muon $g - 2$**



gauged  $L_\mu - L_\tau$

Cannot Affect  $P'_5$

1406.2332

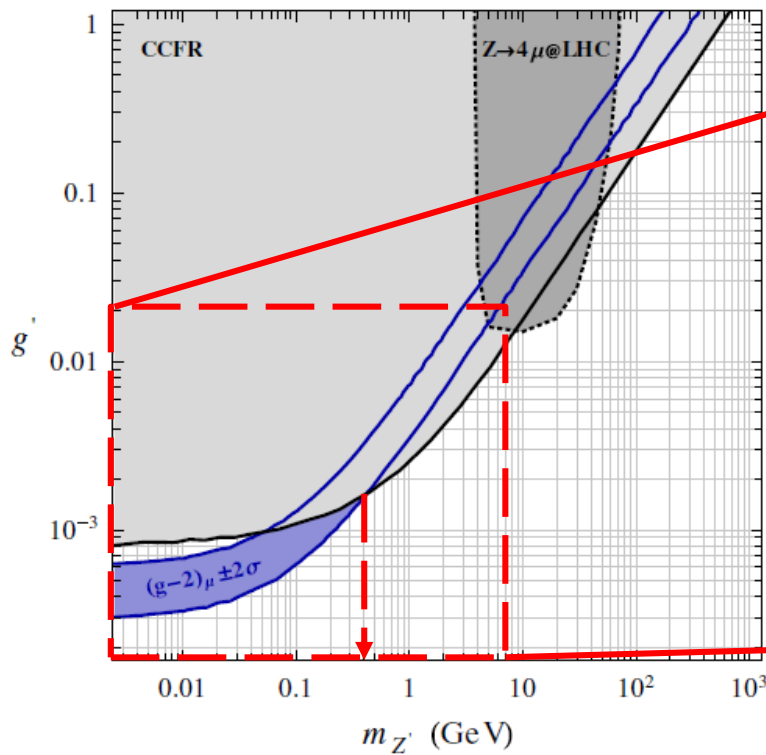
Altmannshofer, Gori, Pospelov, Yavin [PRD  $\rightarrow$  PRL]

PRL 113, 091801 (2014)

PHYSICAL REVIEW LETTERS

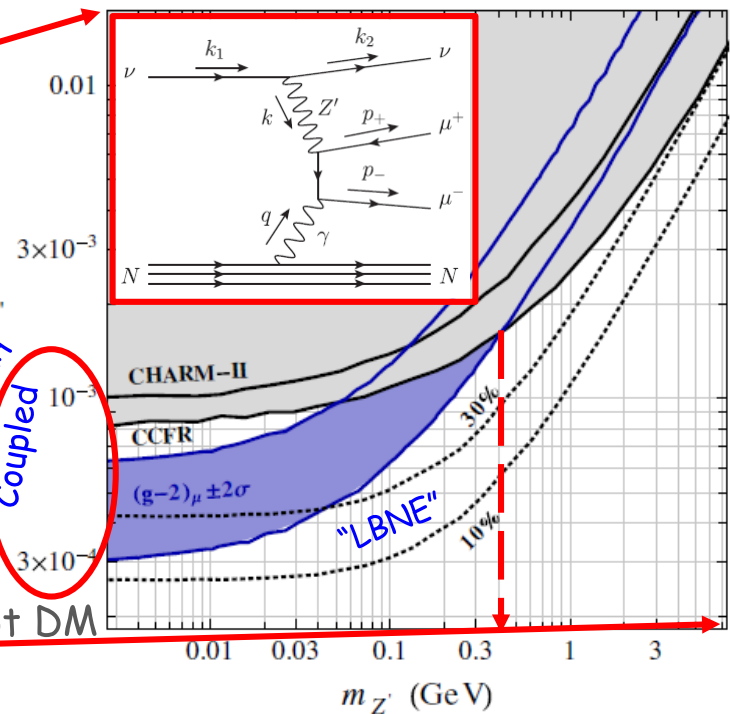
“Neutrino Trident Production”

week ending  
29 AUGUST 2014



Quite Weakly Coupled

but not DM



Muon  $g - 2$  related  $Z' \lesssim 400 \text{ MeV} < m_K?$

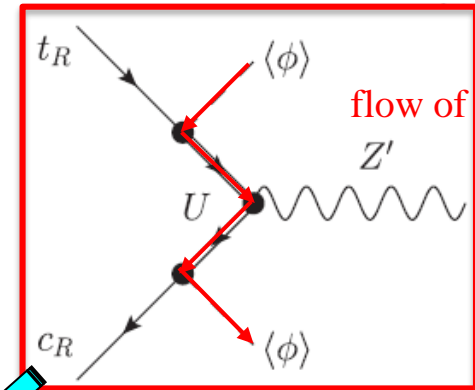
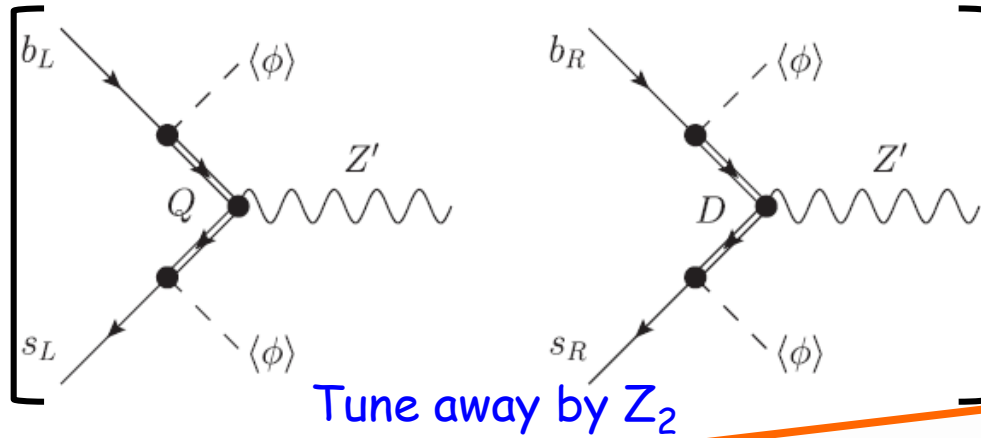
New Physics from Light Particle!?



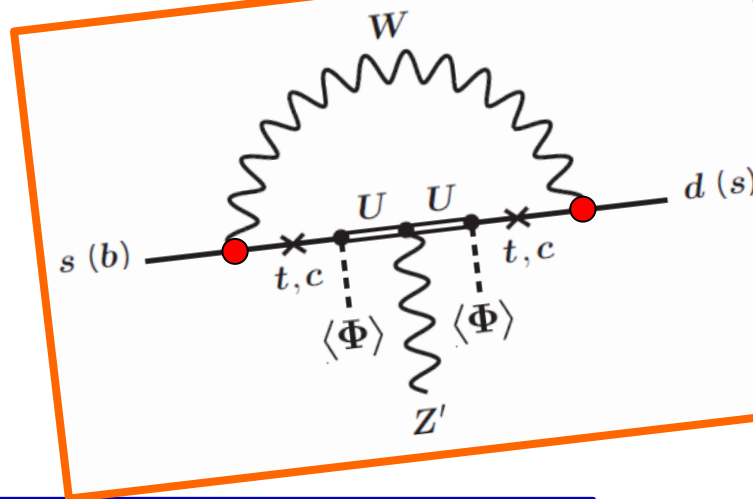
# Leptonic $Z'_{g-2}$ -induced FCNC



gauged  $L_\mu - L_\tau$



$Q, D, U$ : vector-like quarks with  $Z'$  charge  
 $\langle\phi\rangle$ : generates  $Z'$  mass



SM-assisted loop  
 $s \rightarrow dZ'$ ;  $b \rightarrow sZ'$

Fuyoto, WSH, Kohda, PRL'15

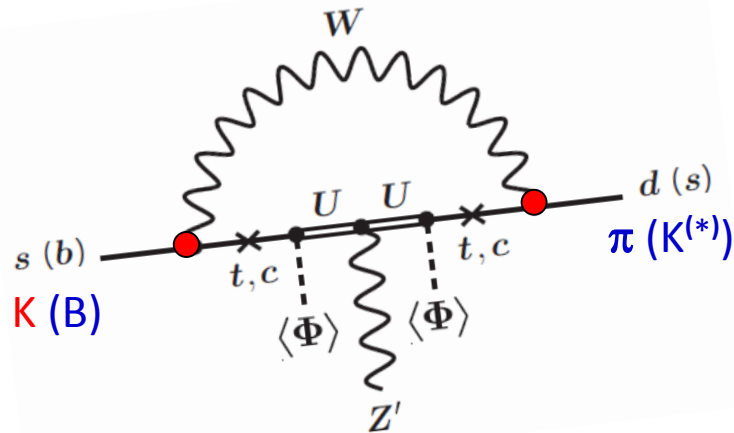
$K_L \rightarrow \pi^0 Z'$

Muon  $g - 2$  related  $Z' \lesssim 400 \text{ MeV} < m_K!$

New Physics from Light Particle!?



# A Little Some Work ...



$$Z' \lesssim 400 \text{ MeV} < m_K$$

**Aim: allowed  $t \rightarrow cZ'$  rate**

But,

$$K_L \rightarrow \pi^0 Z' ?$$

The effective  $\bar{d}_L \gamma^\mu s_L Z'_\mu$  coupling [16] has coefficient

$$g_{ds} = \frac{g' v_\phi^2}{32\pi^2 v^2} [c_{cc} f_{cc} + (c_{tc} + c_{ct}) f_{ct} + c_{tt} f_{tt}], \quad (6)$$

where  $v_\phi$  is the extra  $U(1)'$  breaking scale,  $c_{ij} = V_{is} V_{jd}^* Y_{Ui} Y_{Uj}^* m_i m_j / m_U^2$ ,  $Y_{Ui}$  are Yukawa couplings, and

$$f_{ct} = 1 + \log \frac{m_U^2}{m_t^2} + \frac{3m_W^2}{m_t^2 - m_W^2} \log \frac{m_t^2}{m_W^2},$$

$$f_{tt} = \frac{3m_W^2}{m_t^2 - m_W^2} \left( 1 - \frac{m_W^2}{m_t^2 - m_W^2} \log \frac{m_t^2}{m_W^2} \right) + \log \frac{m_U^2}{m_t^2},$$

with  $f_{cc}$  obtainable from  $f_{tt}$  in  $m_t^2 \ll m_W^2$  limit. These

$$\mathcal{B}(K^+ \rightarrow \pi^+ Z')$$

$$= \frac{m_{K^+}}{\Gamma_{K^+}} \frac{|g_{ds}|^2}{64\pi \hat{m}_{Z'}^2} \lambda^{3/2}(1, \hat{m}_{\pi^+}^2, \hat{m}_{Z'}^2) [f_+^{K\pi}(m_{Z'}^2)]^2, \quad (7)$$

where  $\lambda(x, y, z) \equiv x^2 + y^2 + z^2 - 2(xy + yz + zx)$ ,  $\hat{m} \equiv m/m_{K^+}$ , and  $f_+^{K\pi}$  is a form factor. The formula for  $K_L \rightarrow \pi^0 Z'$  is analogous, with  $|g_{ds}|$  replaced by  $\text{Im } g_{ds}$ .





# $K^+ \rightarrow \pi^+ \pi^0$ Loophole vs $K_L \rightarrow \pi^0 X^0$

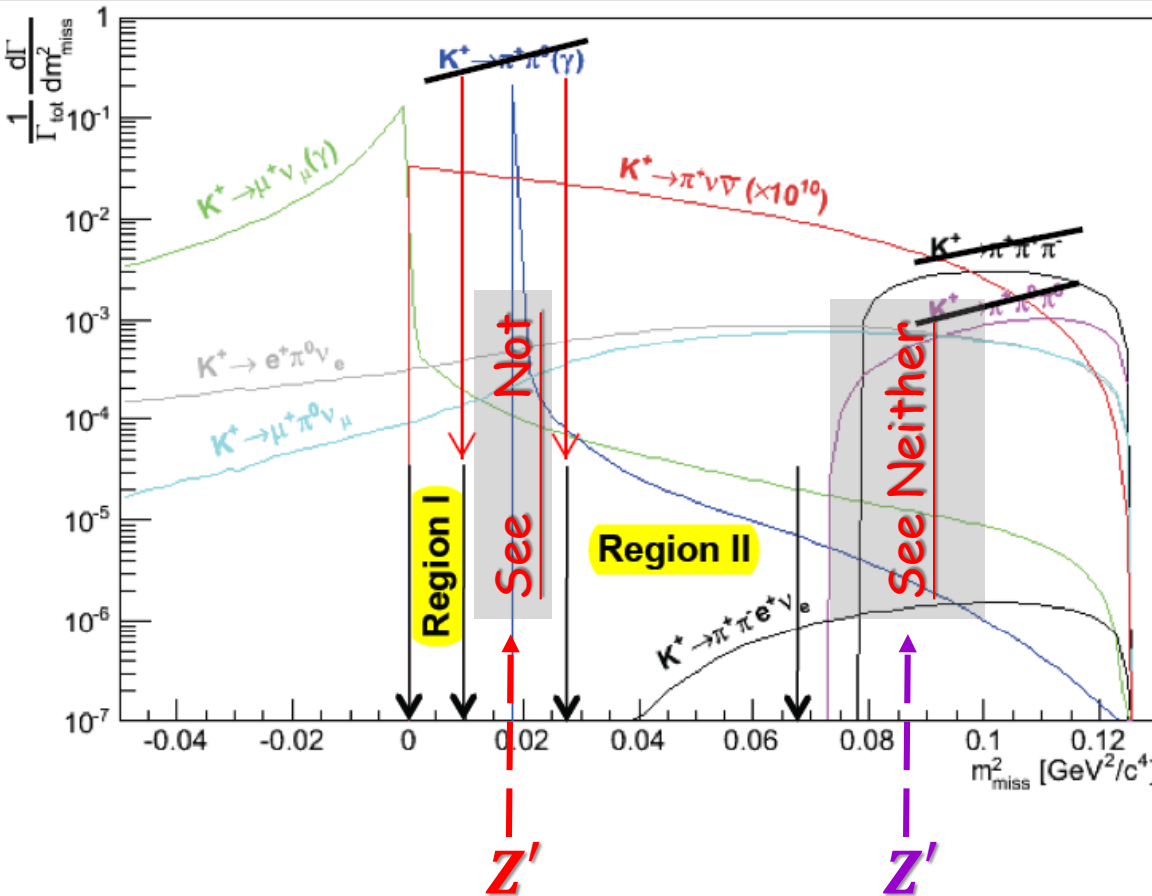


Window basically Same as E787/949 @ BNL

@ CERN

Kinematic exclusion:

exclude  $0.01 - 0.025 \text{ GeV}^2$  [ $(100)^2 - (160)^2 \text{ MeV}^2$ ]



The KOTO Expt at J-PARC can discover  $K_L \rightarrow \pi^0 Z'$  above the Grossman-Nir Bound!

$$\mathcal{B}(K_L \rightarrow \pi^0 \nu \bar{\nu}) \lesssim 4.3 \times \mathcal{B}(K^+ \rightarrow \pi^+ \nu \bar{\nu}) < 1.4 \times 10^{-9} \text{ (GN bound)}$$

“Blessed are the Blind.”

A Surprise! “Trivial”

$K_L \rightarrow \pi^0 \nu \nu$   
 “Nothing to Nothing” (just  $\gamma\gamma$ )  
 — Veto Everything!  
 But: Cannot Veto WILPs.  
 (Weakly Int. Light Particle)

Fuyoto, WSH, Kohda, PRL'15



## IV. What Then? — an Illustration of Impact

Circumstantial Hints/Possibilities in Rare B & K Decays

$Z' < 2m_\mu$ :  $\nu\nu$  **only**

$Z' > 2m_\mu$ :  $\nu\nu/\mu\mu$

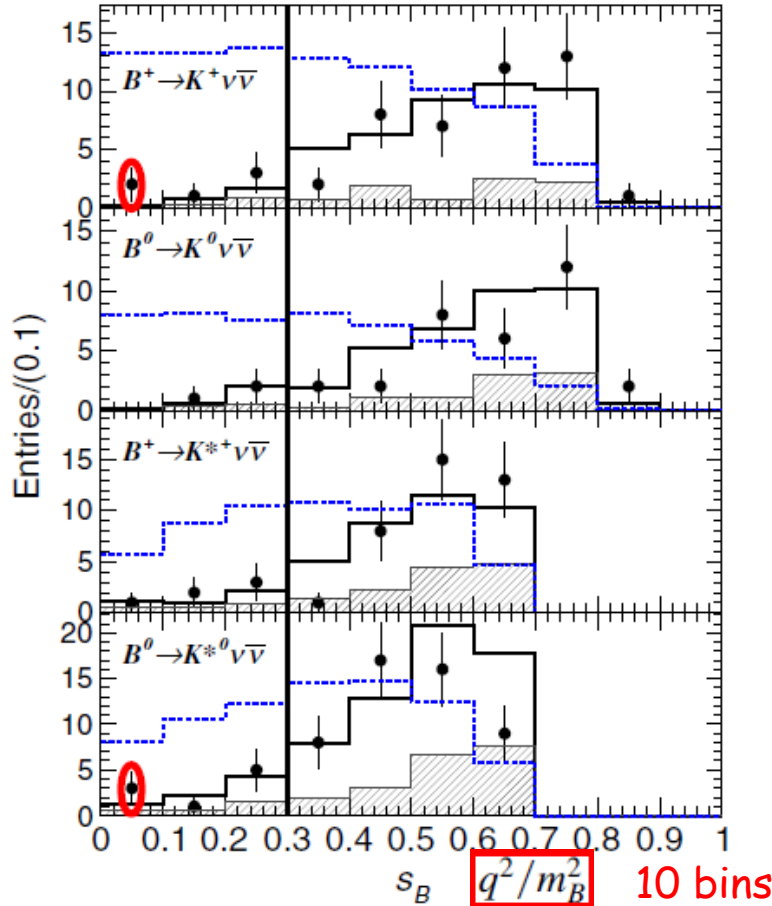


# BaBar: mild hint in $B^+ \rightarrow K^+ \nu \bar{\nu}$

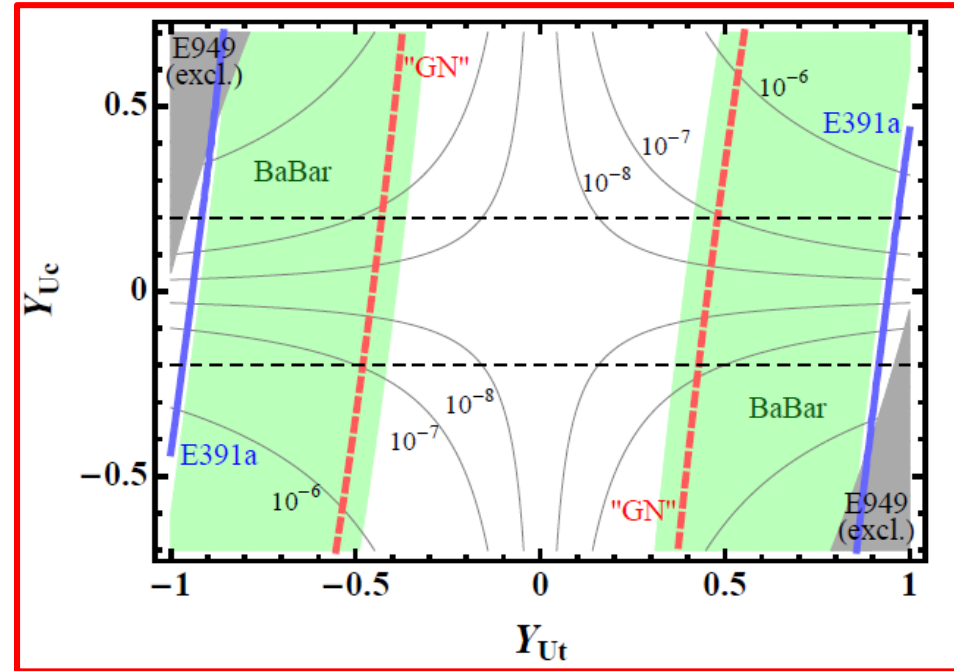


SEARCH FOR  $B \rightarrow K^{(*)} \nu \bar{\nu}$  AND ... BaBar'13 (471M BB(bar))

N.B.  $B(B \rightarrow K\pi^0) \ll B(K \rightarrow \pi\pi^0)$



small excess over the expected background in the  $K^+$  channel, we report a two-sided 90% confidence interval, driven by lowest bin. Gaussian significance of about  $1.4\sigma$ . Therefore, this excess is not considered significant.



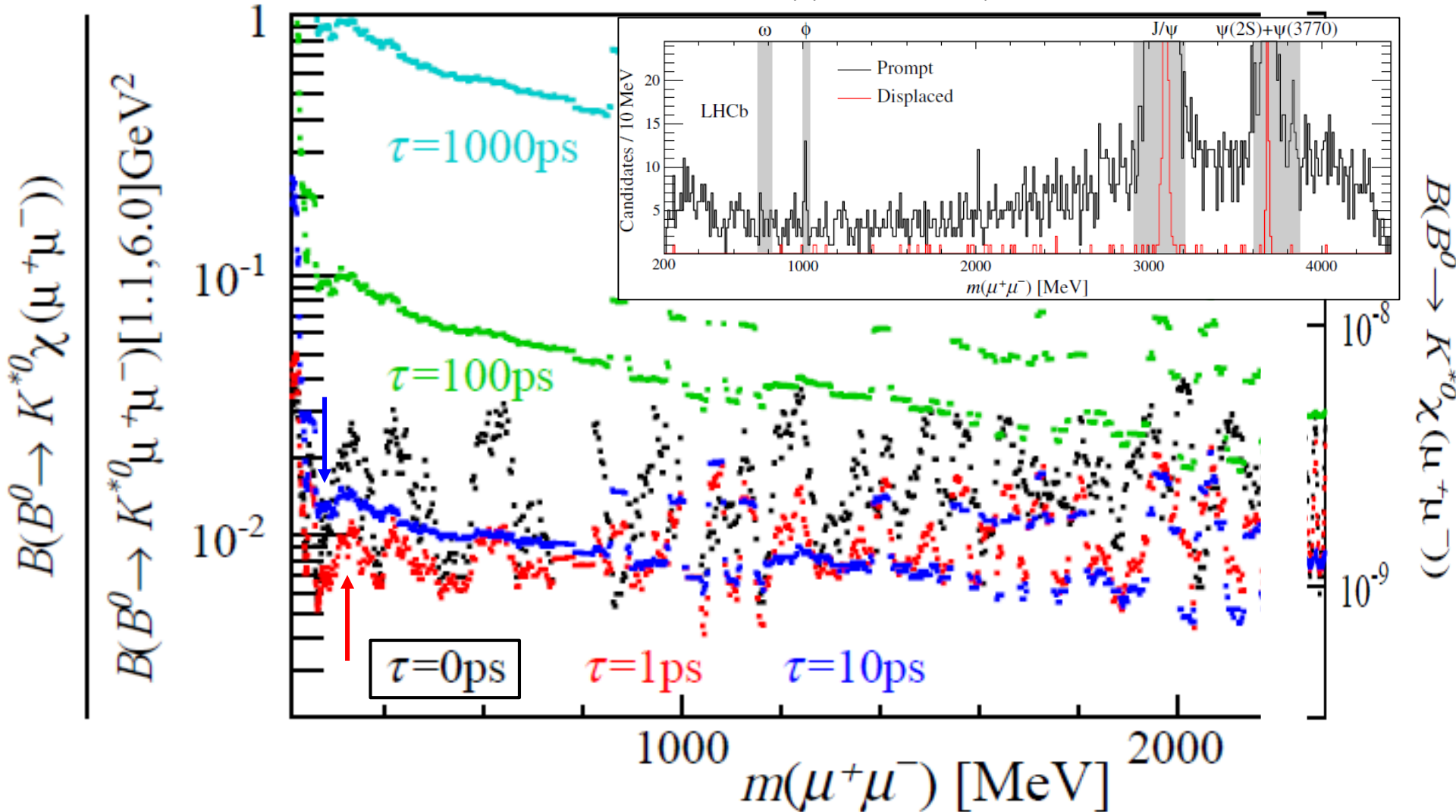
Belle needs to follow up with the **Binned  $m_{\text{mis}}$**  analysis. ( $\rightarrow$  Belle II)



# Search for Hidden-Sector Bosons in $B^0 \rightarrow K^{*0} \mu^+ \mu^-$



LHCb 1508.04094 [PRL'15 supplementary]



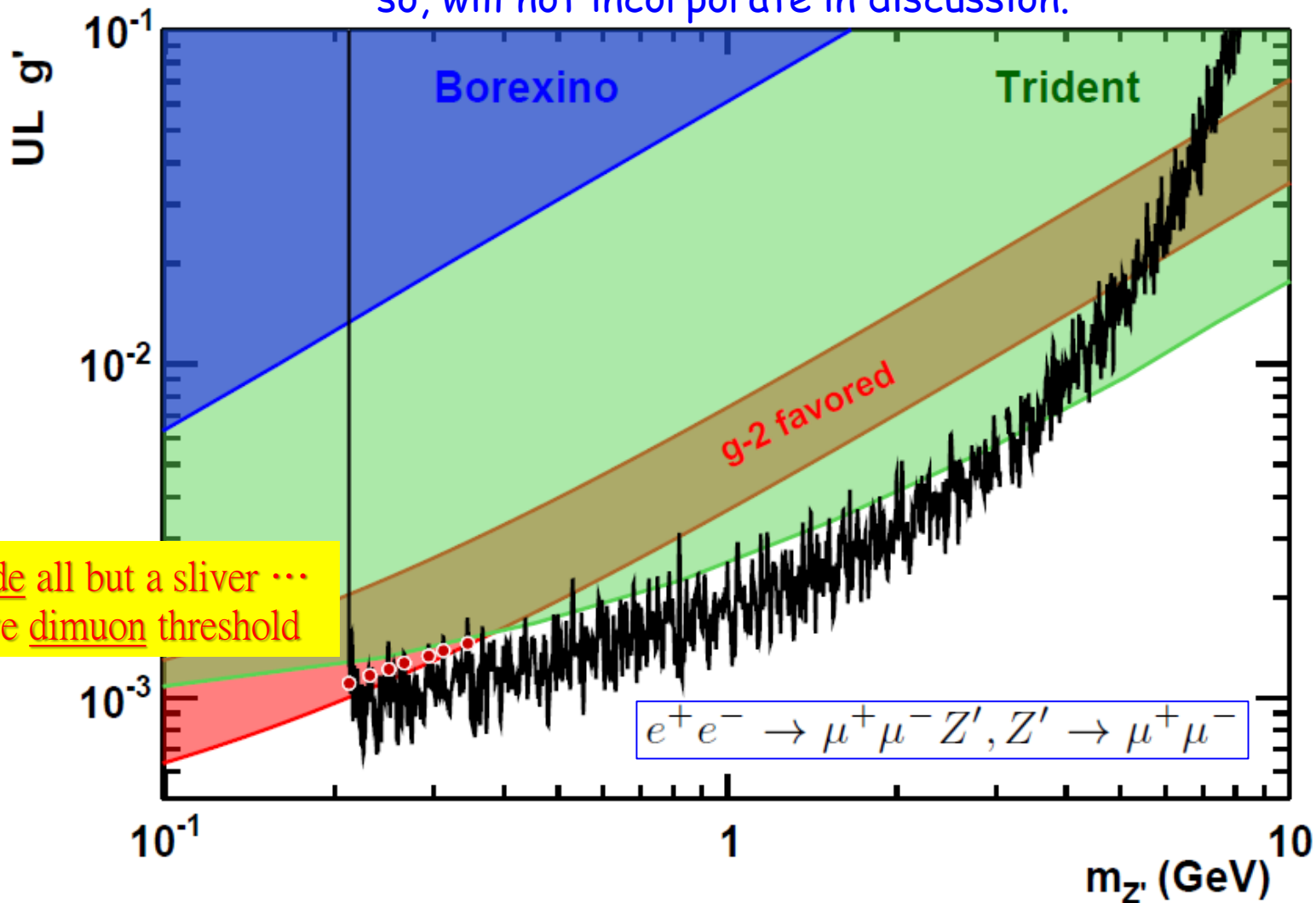


# Search for a muonic dark force at *BABAR*

1606.03501



"Pockets" exist, but paper came after our PRD, so, will not incorporate in discussion.



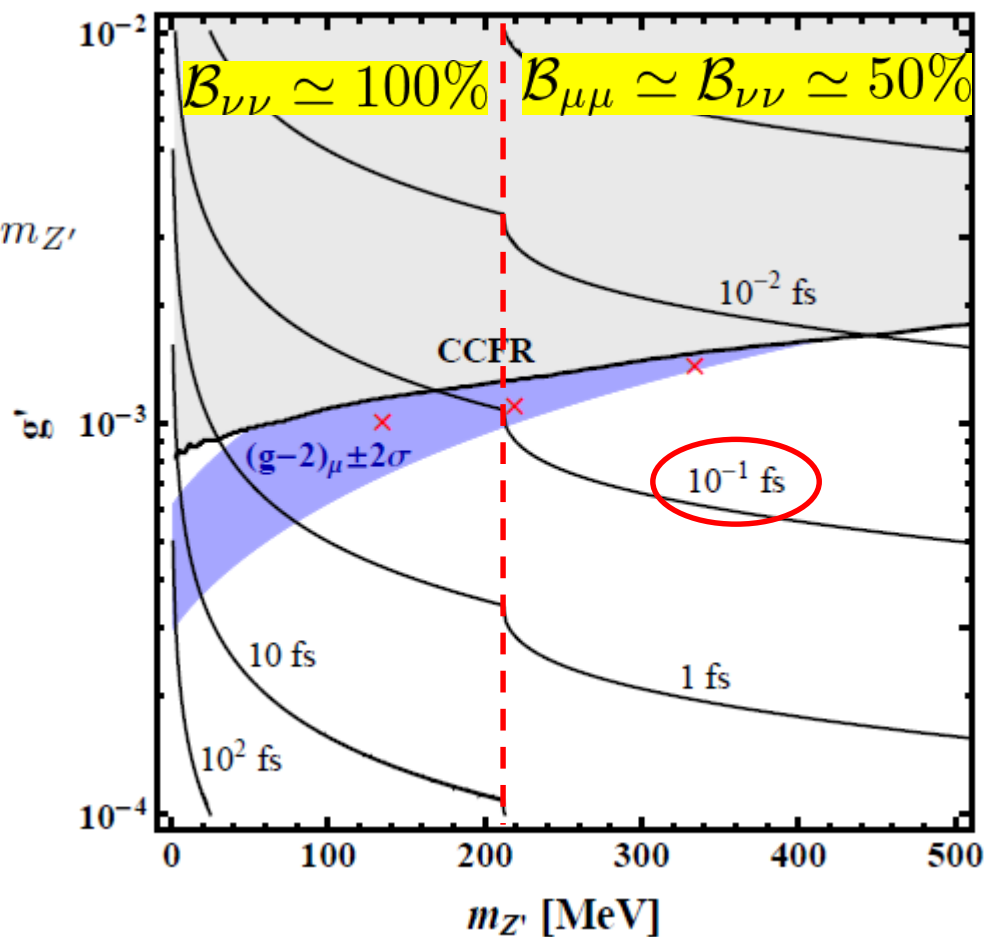




Comment: Light “g-2” Z' decay is prompt, even when highly boosted.



$$\Gamma(Z' \rightarrow \nu_\ell \bar{\nu}_\ell) = \frac{g'^2}{24\pi} m_{Z'}$$



$$\gamma_{CTZ'} \simeq 0.4 \mu\text{m} \left[ \frac{2}{N_{\text{eff}}} \right] \left[ \frac{10^{-3}}{g'} \right]^2 \left[ \frac{0.3 \text{ GeV}}{m_{Z'}} \right]^2 \left[ \frac{E_{Z'}}{10 \text{ GeV}} \right]$$

Fuyoto, WSH, Kohda, PRD'16

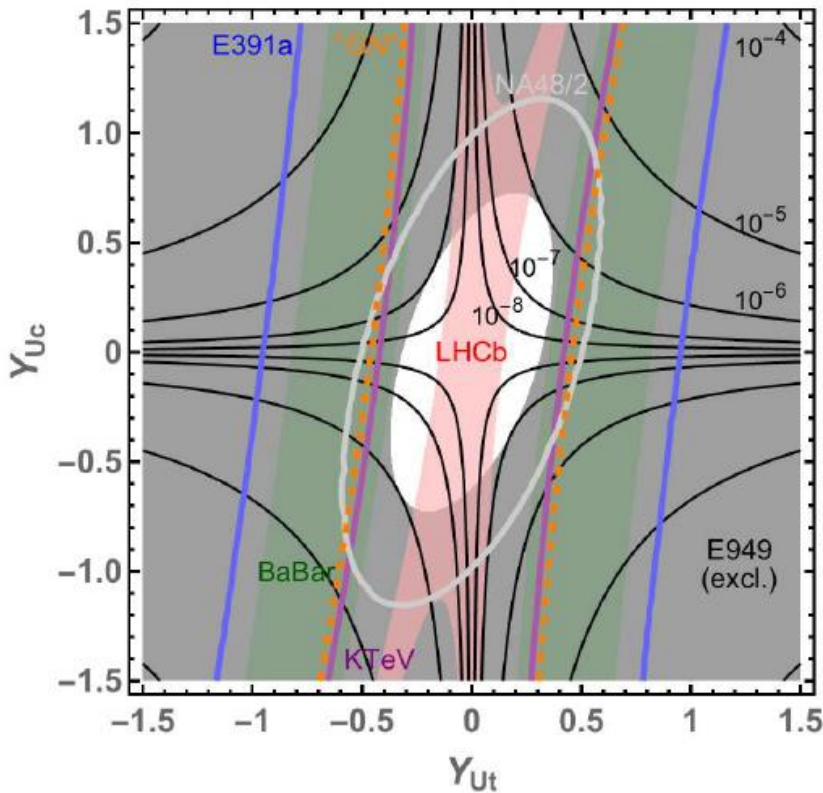


$$Z' > 2m_\mu: \nu\nu/\mu\mu$$



# The 2<sup>nd</sup> Window: "pocket physics"

219 MeV  $Z'$

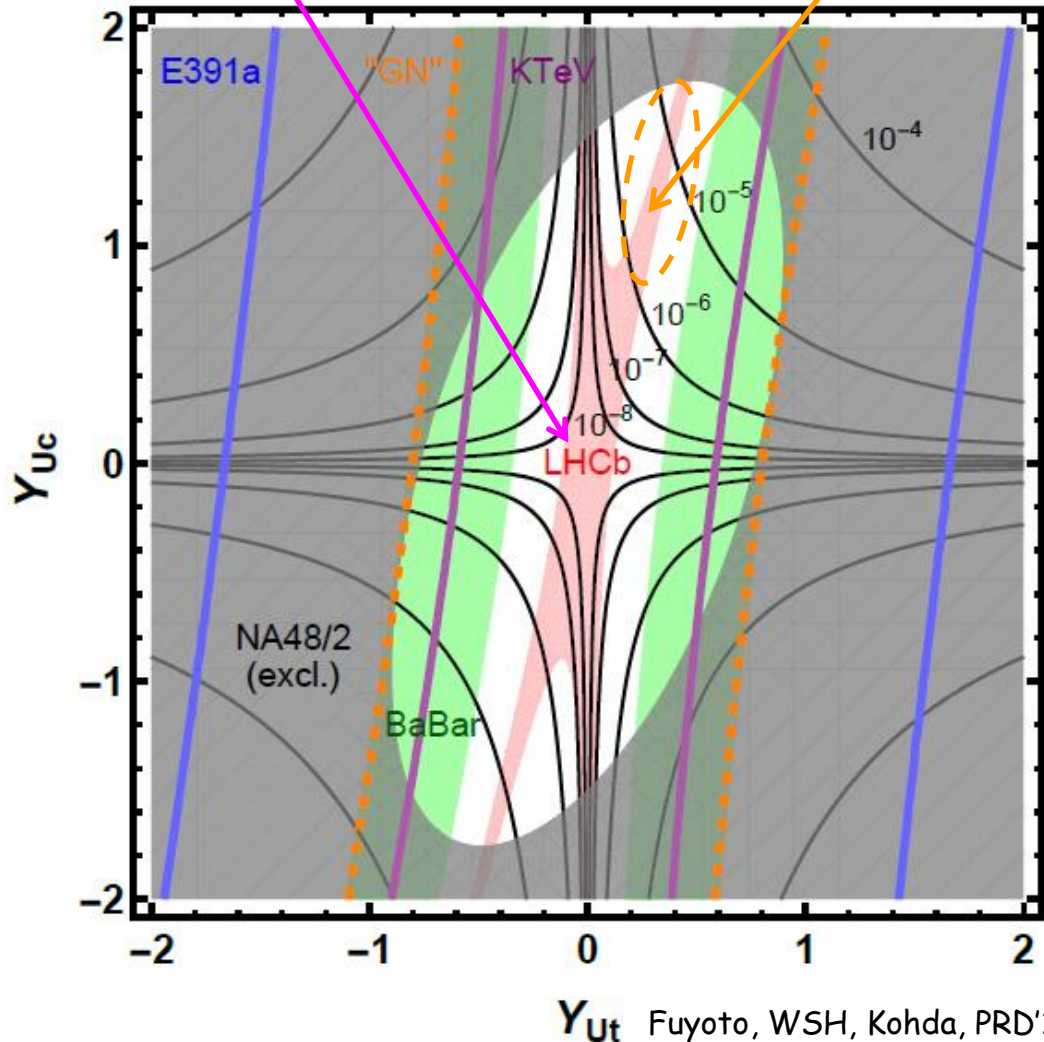


Funnel regions excluded by E949  $K^+ \rightarrow \pi^+ X(\rightarrow \nu\nu)$ ; no fun

BR( $t \rightarrow c Z'$ ) >  $10^{-6}$  possible

Allowed

334 MeV  $Z'$



$Y_{Ut}$  Fuyoto, WSH, Kohda, PRD'16



# The Light $Z'_{g-2}$ Landscape (illustration)



Perhaps 100 TeV SPPC/FCChh Needed

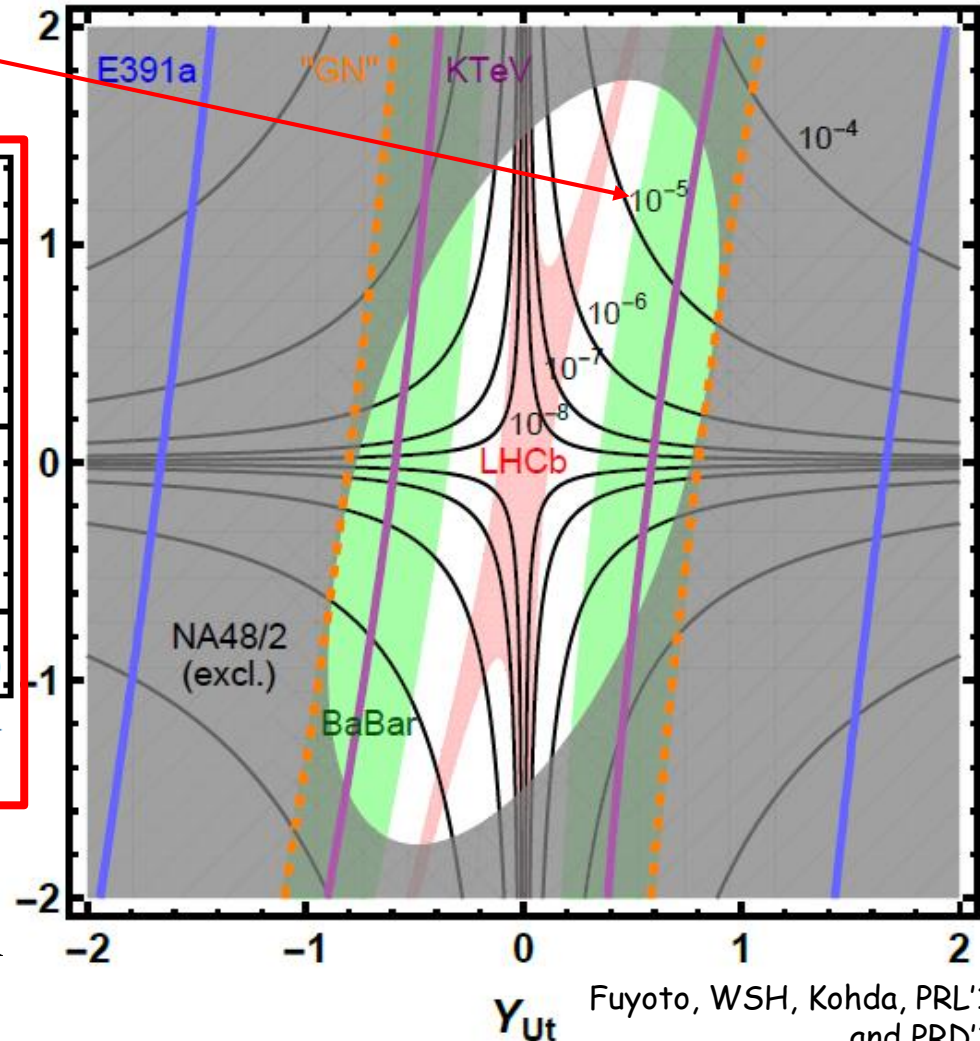
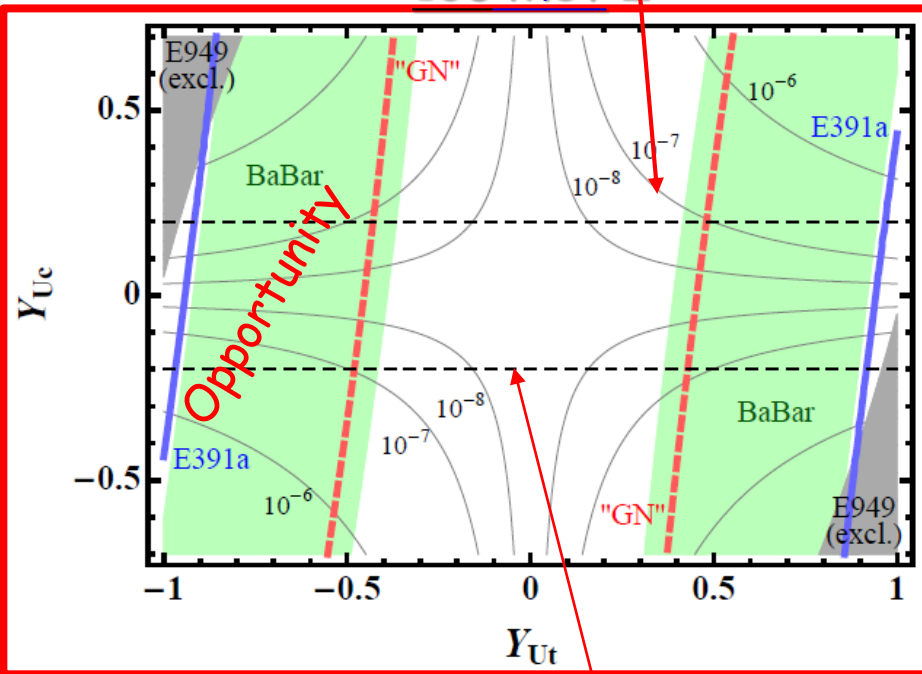
....

Or not? [50%  $\mu\mu$ ]

Contour in backdrop is  $t \rightarrow c Z'_{g-2}$

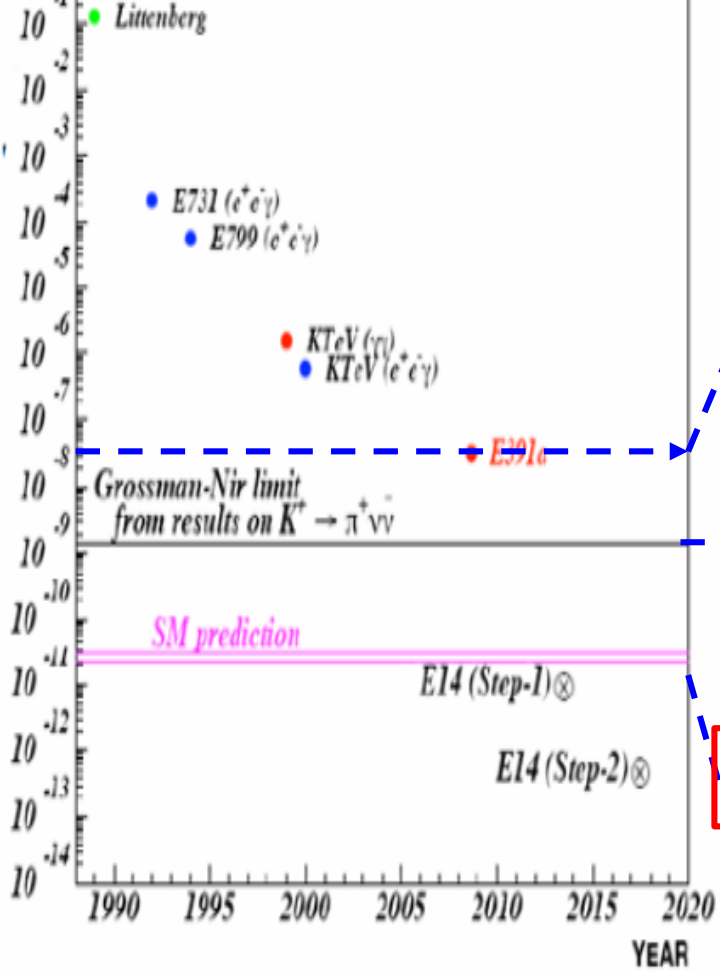
334 MeV  $Z'$

135 MeV  $Z'$



$Y_{Uc}$  &  $Y_{Ut}$  reasonable in strength

Fuyoto, WSH, Kohda, PRL'15 and PRD'16

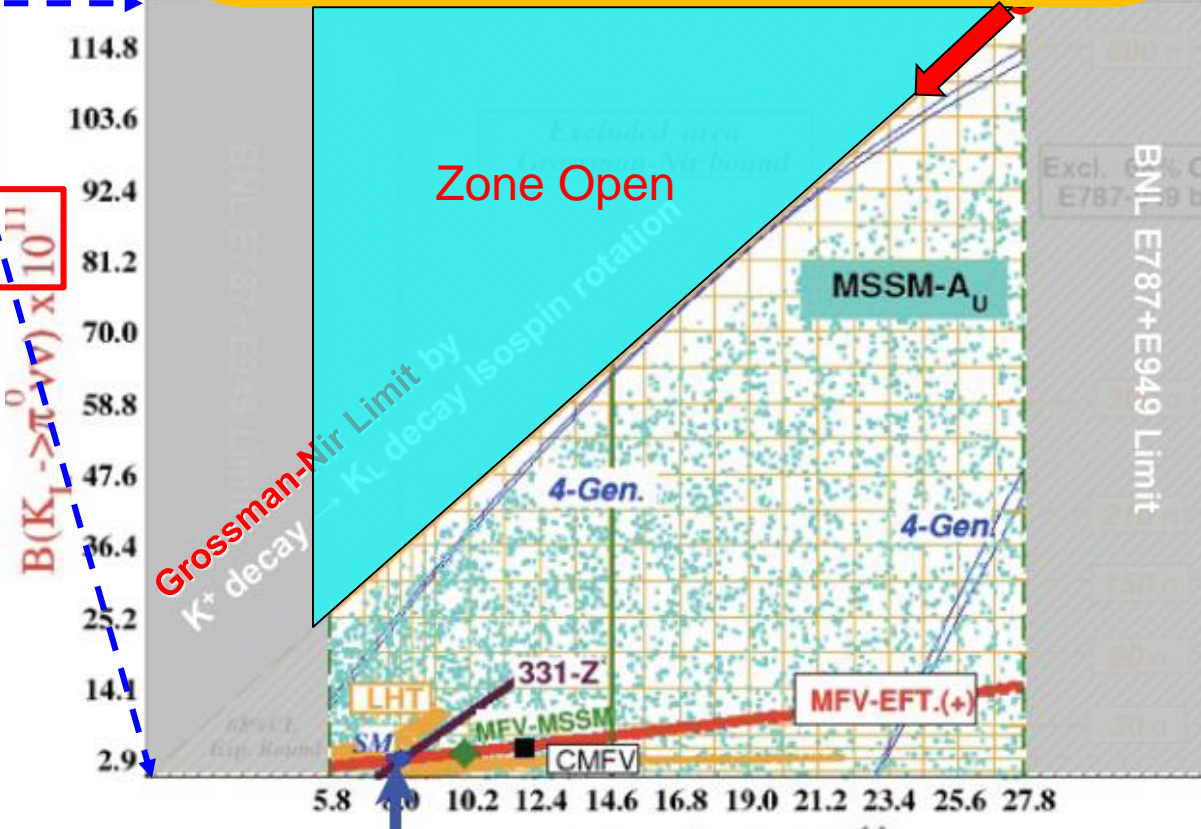
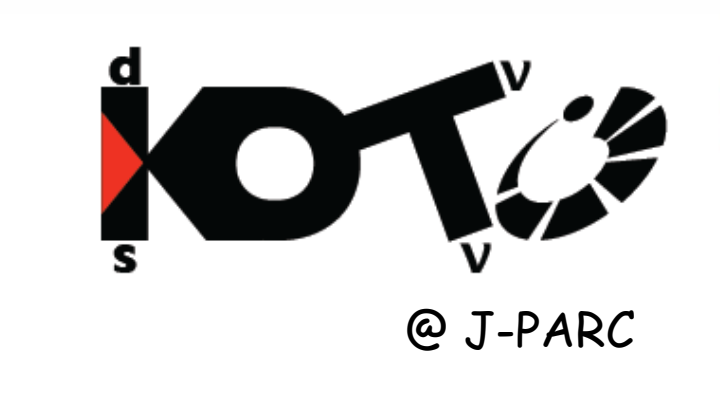


Shaken It Off!

Discovery Zone  
(2015 Data!)

$$\frac{\mathcal{B}(K_L \rightarrow \pi^0 \nu \bar{\nu})}{\mathcal{B}(K^+ \rightarrow \pi^+ \nu \bar{\nu})} < 1.4 \times 10^{-9} \quad (\text{GN bound})$$

KOTO @ 100 hrs (2013), paper finally ...



$K_L \rightarrow \pi^0 \nu \bar{\nu} > \text{GN?}$

Standard Model  $B(K^+ \rightarrow \pi^+ \nu \bar{\nu}) \times 10^{11}$

BNL E787+E949 Limit

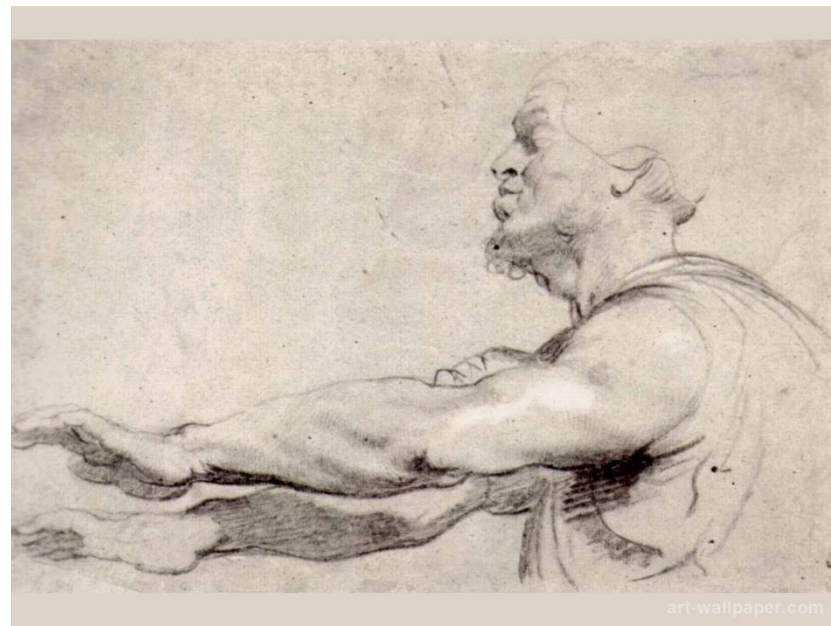


# V. Conclusion



- $K_L \rightarrow \pi^0 + \text{nothing}$ : can occur above “Grossman-Nir Bound”  $\rightarrow$  KOTO!  
If See Early Event(s), Try Hard to Kill ... But [Not Overkill](#).
- **If above GN Bound, then likely “ $\pi^0$ ” mass object** (that slips thru NA62)
- When KOTO reaches below current GN Bound, concept still effective.  
 $\rightarrow$  KOTO/NA62/Belle(II) (/LHCb) all in game.

*Analyze, KOTO, Analyze!*







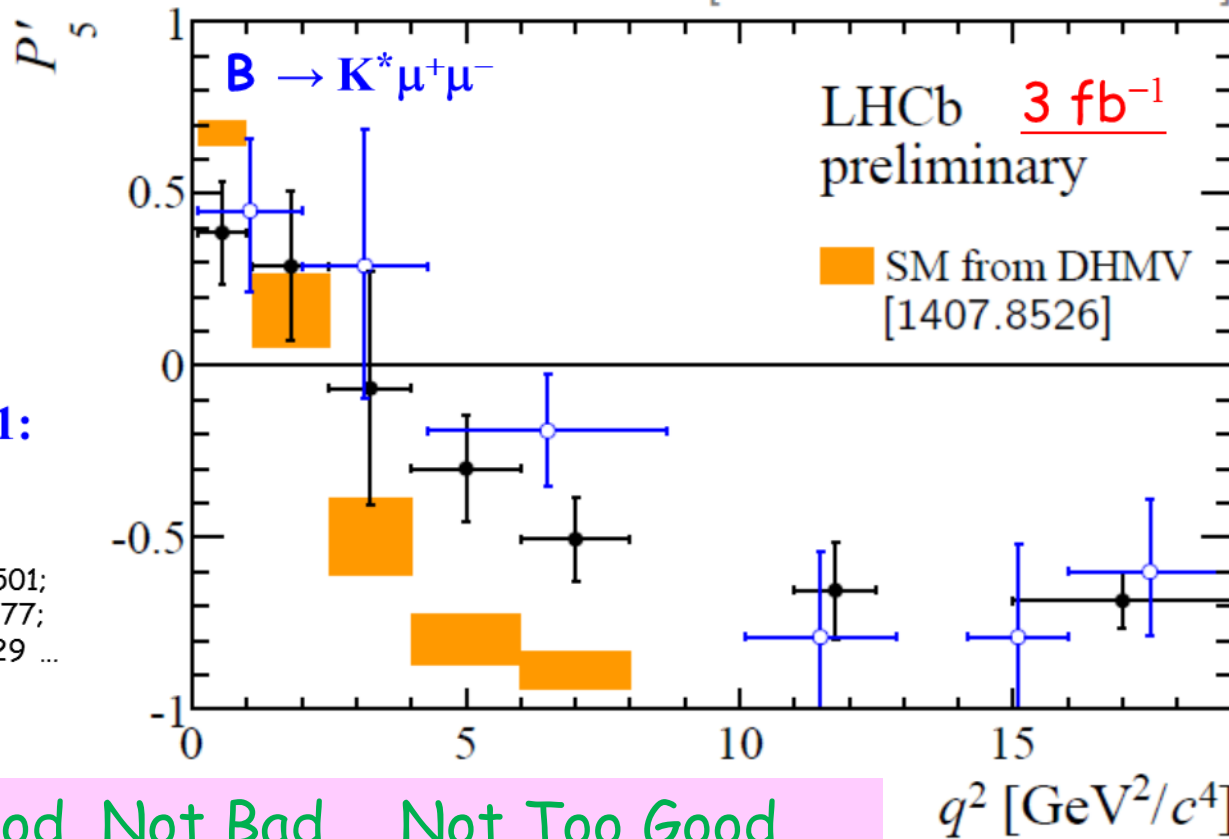
# $P'_5$



Ex: Tolk yesterday;  
Th: Turstall this morning

C. Langenbruch @ Moriond EW

[LHCb-CONF-2015-002]



NP?  $\Delta C_9 \sim -1$ :  
heavy  $Z'$

e.g. 1307.5683; 1308.1501;  
1310.2478; 1310.3877;  
1310.1082; 1311.6729 ...

Not Good, Not Bad ... Not Too Good ...

- Tension seen in  $P'_5$  in [PRL 111, 191801 (2013)] confirmed
- [4.0, 6.0] and [6.0, 8.0]  $\text{GeV}^2/c^4$  show deviations of  $2.9\sigma$  each
- Naive combination results in a significance of  $3.7\sigma$   $3.4\sigma$
- Compatible with  $1 \text{ fb}^{-1}$  measurement  $3.7\sigma$



# Pick up $t \rightarrow cZ'$ topic at LHCP2014



## Models with Light $Z'$ Gauge Bosons

consider a  $Z'$  gauge boson at (or below) the electro-weak scale associated with the anomaly free  $L_\mu - L_\tau$  symmetry

difference between muon- and tau-lepton number

X.G. He et al., PRD1991

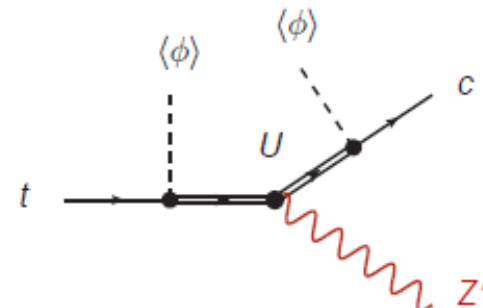
couple the  $Z'$  to quarks by mixing with heavy vector-like quarks

( such a  $Z'$  was proposed to solve an anomaly in the rare  $B \rightarrow K^* \mu^+ \mu^-$  decay

WA, Gori, Pospelov, Yavin 1403.1269 ) [1403.1269](#)

can also lead to **non-standard top decays**

$$\text{BR}(t \rightarrow cZ') \simeq |Y_{Ut} Y_{Uc}^*|^2 \frac{v^2 v_\phi^2}{2m_U^4}$$



I ask from back of room: "How to Search?".  
Came the reply: " $\mu\mu$  or  $\tau\tau$ " mode.

a dedicated search with existing LHC data should be able to constrain this branching ratio at the level of  $\text{BR}(t \rightarrow cZ') \sim 10^{-3}$

at run 2, the sensitivity could be at the level of  $\text{BR}(t \rightarrow cZ') \sim 10^{-4}$



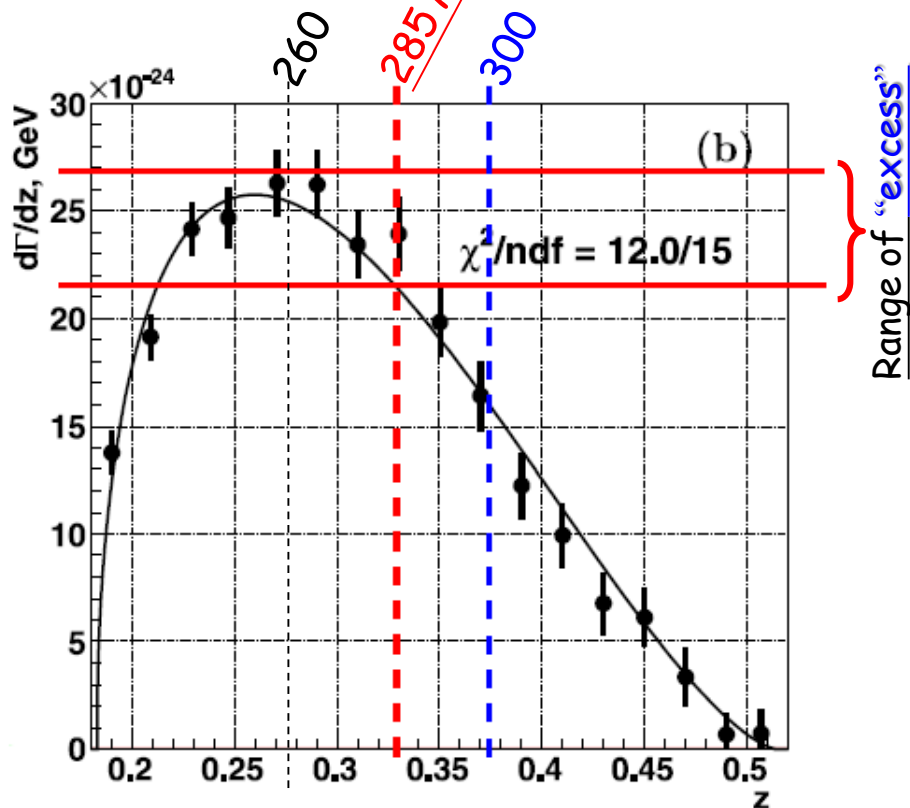


$Z' > 2m_\mu: \nu\nu/\mu\mu$

# The 2<sup>nd</sup> Window

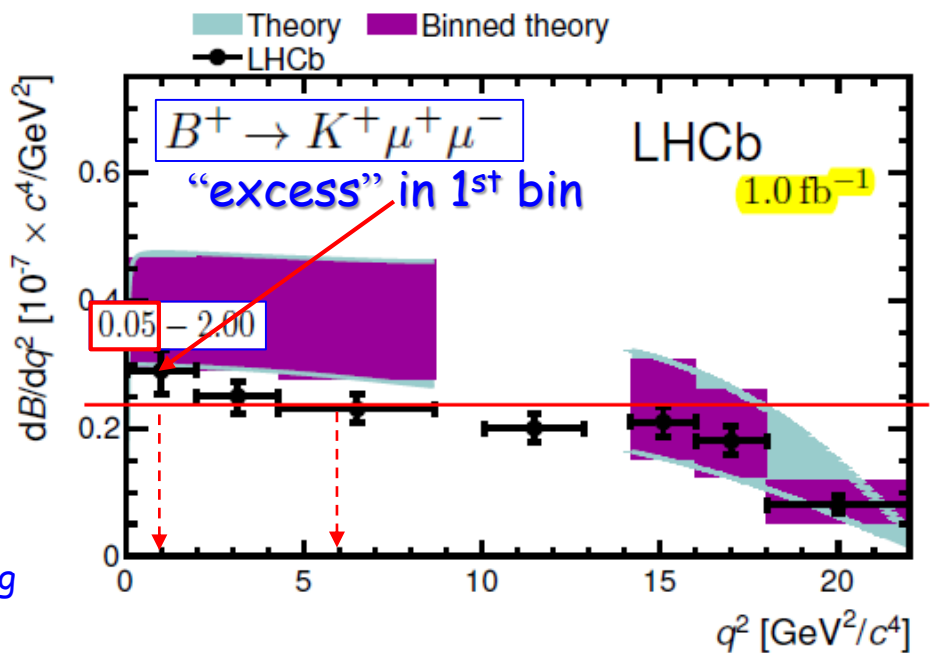
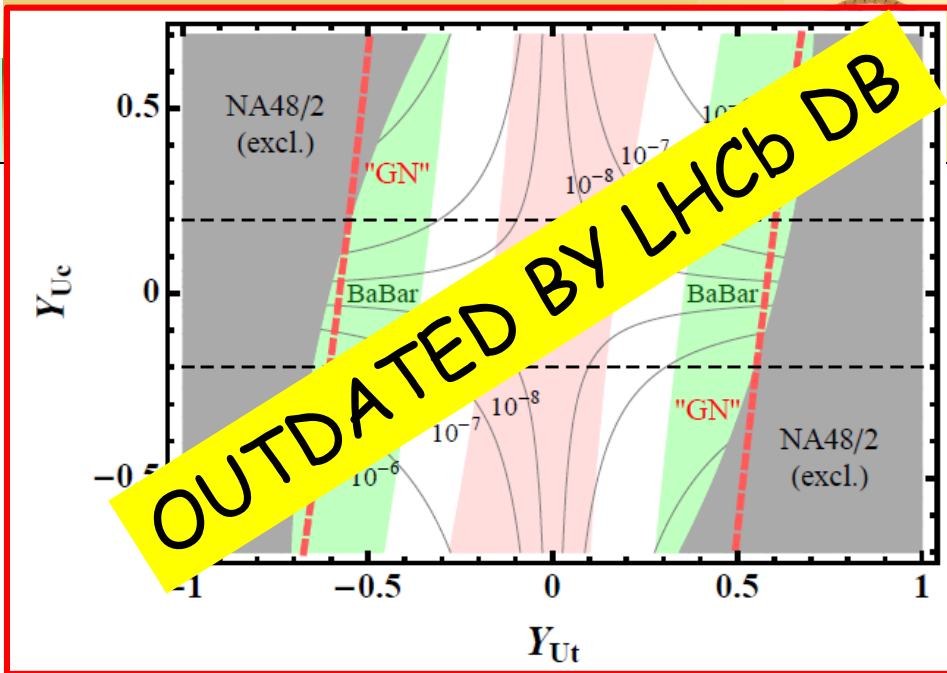
NA48/2 Collaboration / Physics Letters B 697 (2011)

$$K^\pm \rightarrow \pi^\pm \mu^+ \mu^-$$



Can be refined by NA62

Piccini talk this morning





# The Blinding $K^+ \rightarrow \pi^+\pi^0$



I (We) have (all) stared at this gazillion times, and became numb.

PHYSICAL REVIEW D 79, 092004 (2009)

