



UNIT 11 ELECTROMAGNETIC DESIGN EPISODE III

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- Where can we operate the magnet ? How far from the critical surface ?
- Efficiency: the last Teslas are expensive ... are there techniques to save conductor ?





- What is the effect of iron ? Does it help in having higher short sample fields ?
- What happens in coil heads ?
- Are there other possible lay-outs ?







- 1. Operational margin
- 2. Grading techniques
- 3. Iron yoke
- 4. Coil ends
- 5. Other designs
- 6. A review of dipole and quadrupole lay-outs





- Magnets have to work at a given distance from the critical surface, i.e. they are never operated at short sample conditions
 - At short sample, any small perturbation quenches the magnet
 - One usually operates at a fraction of the loadline which ranges from 60% to 90%





This fraction translates into a temperature margin

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- How to compute the temperature margin ?
 - One needs an analytic fit of the critical surface $j_{ss}(B,T)$
 - The temperature margin ΔT is defined by the implicit equation

$$j_{ss}(B_{op}, T_{op} + \varDelta T) = j_{op}$$



• Nb-Ti at 1.9 K at 80% of the loadline has about 2 K of temperature margin



1. OPERATIONAL MARGIN



- Some parametric analysis
 - Nb-Ti at 4.2 K loses at least 1/3 of temperature margin w.r.t. 1.9 K
 - But the specific heat is larger ...
 - But helium is not superfluid ...
 - Nb₃Sn has a temperature margin 2.5 times larger than Nb-Ti
 - This is due to the shape of the critical surface

• At 80%, Nb₃Sn has about 5 K of temperature margin





1. OPERATIONAL MARGIN



- Two regimes
- 1. Fast losses or fast release of energy (J/cm³)
 - Adiabatic case all heat stays there
 - Main issue: the conductor must have high enough thermal inertia
 - The deposited energy must not exceed the enthalpy margin
 - Enthalpy margin is the critical parameter
- 2. Continuous losses (as debris coming from collisions, or losses from the beam) (W/cm^3)
 - All heat is removed stationary case
 - Main issue: the heat must be extracted efficiently
 - The gradient between the heat sink and the coil must not exceed the temperature margin
 - Temperature margin is the critical parameter







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2. GRADING TECHNIQUES



- The idea
 - The map of the field inside a coil is strongly non-uniform
 - In a two layer configuration, the peak field is in the inner layer, and outer layer has systematically a lower field
 - A higher current density can be put in the outer layer
- How to realize it
 - First option: use two different power supplies, one for the inner and one for the outer layer (not common)
 - Second option: use a different cable for the outer layer, with a smaller cross-section, and put the same current (cheaper)
 - The inner and outer layer have a splice, and they share the same current
 - Since the outer layer cable has a smaller section, it has a higher current density





- Examples of graded coils
 - LHC main dipole (~9 T)
 - grading of 1.23 (i.e. +23% current density in outer layer)
 - 3% more in short sample field, 17% save of conductor
 - MSUT Nb₃Sn model of Univ. of Twente (~11 T)
 - strong grading 1.65
 - 5% more in short sample field, 25% save of conductor







MSUT dipole Unit 11: Electromagnetic design episode III – 11.10





- Short sample limit for a graded Nb-Ti dipole
 - Each block has a current density $j_1 \dots j_n$, each one with a dilution factor $\kappa_1 \dots \kappa_n$
 - We fix the ratios between the current densities

$$\chi_1 \equiv \frac{j_1}{j_1} = 1$$
 $\chi_2 \equiv \frac{j_2}{j_1}$ $\chi_n \equiv \frac{j_n}{j_1}$

• We define the ratio between central field and current densities

$$B = \sum j_n \gamma_{c,n} \equiv j_1 \gamma_c$$

We define the ratio between peak field in each block and central field

$$B_{p,n} \equiv \lambda_n B = \lambda_n \gamma_c j_1 = \frac{1}{\chi_n} j_n \lambda_n \gamma_c$$

USPAS January 2012, Superconducting accelerator magnets

Unit 11: Electromagnetic design episode III - 11.11





• Short sample limit for a graded Nb-Ti dipole (continued I)

$$B = \sum j_n \gamma_{c,n} \equiv j_1 \gamma_c \qquad \qquad B_{p,n} = \frac{1}{\chi_n} j_n \lambda_n \gamma_n$$

• In each layer one has $j_{c,n} \leq \kappa_n s(B_{c2}^* - B_{p,n})$ and substituting the peak field expression one has

$$j_{c,n} \leq \frac{\chi_n \kappa_n s}{\chi_n + \lambda_n \kappa_n s \gamma_c} B_{c2}^*$$

• All these *n* conditions have to be satisfied – since the current densities ratios are fixed, one has

$$j_{c,1} = \frac{j_{c,n}}{\chi_n} \le \frac{\kappa_n s}{\chi_n + \lambda_n \kappa_n s \gamma_c} B_{c2}^*$$

$$j_{c,1} = \operatorname{Min}_{n} \frac{\kappa_{n} s}{\chi_{n} + \lambda_{n} \kappa_{n} s \gamma_{c}} B_{c2}^{*}$$





- Short sample limit for a graded Nb-Ti dipole (continued II)
 - The short sample current is

$$j_{c,1} = \operatorname{Min}_{n} \frac{S \kappa_{n}}{\chi_{n} + \lambda_{n} S \kappa_{n} \gamma_{c}} B_{c2}^{*}$$

- and the short sample field is $B_{ss} = \operatorname{Min}_{n} \frac{S \kappa_{n} \gamma_{c}}{\chi_{n} + \lambda_{n} S \kappa_{n} \gamma_{c}} B_{c2}^{*}$
- Comments
 - The grading factor χ in principle should be pushed to maximize the short sample field
 - A limit in high grading is given by quench protection issues, that limit the maximal current density in general the outer layer has lower filling factor to ease protection
 - Please note that the equations depend on the material a graded layout optimized for Nb-Ti will not be optimized for Nb₃Sn





- Results for a two layer with same width sector case, Nb-Ti
 - The gain in short sample field is $\sim 5\%$
 - But given a short sample field, one saves a lot !
 - At 8 T one can use 30 mm instead of 40 mm (-25%)
 - At 9 T one can use 50 mm instead of 80 mm (-37%)







- Similar strategy for quadrupoles gain of 5-10% in G_{ss}
 - LHC MQXB quadrupole for IR regions
 - grading of 1.24 (i.e. +24% current density in outer layer)
 - 6% more in short sample field, 41% save of conductor
 - LHC MQY quadrupole close to IR regions
 - Special grading (grading inside outer layer, upper pole with lower density) of 1.43
 - 9% more in short sample field, could not be reached without grading











1. Operational margin

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3. Iron yoke

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6. A review of dipole and quadrupole lay-outs





- An iron yoke usually surrounds the collared coil it has several functions
 - Keep the return magnetic flux close to the coils, thus avoiding fringe fields
 - In some cases the iron is partially or totally contributing to the mechanical structure
 - RHIC magnets: no collars, plastic spacers, iron holds the Lorentz forces
 - LHC dipole: very thick collars, iron give little contribution
 - Considerably enhance the field for a given current density
 - The increase is relevant (10-30%), getting higher for thin coils
 - This allows using lower currents, easing the protection
 - Increase the short sample field
 - The increase is small (a few percent) for "large" coils, but can be considerable for small widths
 - This action is effective when we are far from reaching the asymptotic limit of *B*^{*}_{c2}





- A rough estimate of the iron thickness necessary to avoid fields outside the magnet
 - The iron cannot withstand more than 2 T (see discussion on saturation, later)
 - Shielding condition for dipoles:

$$rB \sim t_{iron}B_{sat}$$

- i.e., the iron thickness times 2 T is equal to the central field times the magnet aperture One assumes that all the field lines in the aperture go through the iron (and not for instance through the collars)
- Example: in the LHC main dipole the iron thickness is 150 mm

$$t_{iron} \sim \frac{rB}{B_{sat}} = \frac{28*8.3}{2} \sim 100 \text{ mm}$$

• Shielding condition for quadrupoles:

$$\frac{r^2 G}{2} \sim t_{iron} B_{sat}$$





- The iron yoke contribution can be estimated analytically for simple geometries
 - Circular, non-saturated iron: image currents method
 - Iron effect is equivalent to add to each current line a second one







3. IRON YOKE – IMAGE METHOD



- Remarks on the equations
 - When iron is not saturated, one has $\mu >>1$ and then I' = I
 - Since the image is far from the aperture, its impact on high order multipoles is small
 - The impact of the iron is negligible for
 - Large coil widths
 - Large collar widths
 - High order multipoles
 - The iron can be relevant for
 - Small coil widths, small collar widths, low order multipoles, main component
 - At most, iron can double the main component for a given current density (i.e. can give a $\Delta\gamma$ =100%)
 - This happens for infinitesimally small coil and collar widths



 $\rho' = \frac{R_I^2}{\rho} \qquad I' = \frac{\mu - 1}{\mu + 1}I$

 $\frac{\Delta B_1^{iron}}{B_{\cdot}} = \frac{\mu - 1}{\mu + 1} \frac{(r + w)r}{R_I^2}$

- Estimate of the gain in main field $\Delta \gamma$ for a sector coil
 - $B_{1} = kjw \qquad \Delta B_{1}^{iron} = kj'(R_{2} R_{1}) \qquad R_{1} = \frac{R_{I}^{2}}{r+w}$ $\frac{\Delta B_{1}^{iron}}{B_{1}} = \frac{j'(R_{2} R_{1})}{jw} \qquad R_{2} = \frac{R_{I}^{2}}{r}$

the current density has to satisfy the integral condition

$$j[(r+w)^{2} - r^{2}] = \frac{\mu - 1}{\mu + 1} j' [R_{2}^{2} - R_{1}^{2}]$$

and one obtains

• The relative contribution becomes very small











• Estimate of the gain in main field for fixed current in a sector coil

$$\frac{\Delta B_1^{iron}}{B_1} = \frac{\mu - 1}{\mu + 1} \frac{(r + w)r}{R_I^2}$$

Examples of several built dipoles

- Smallest: LHC ~ 16% (18% actual value)
- Largest: RHIC ~ 55% (56% actual value)







• Impact of the iron yoke on dipole short sample field, Nb-Ti

$$B_{ss} = \frac{\kappa \gamma_c}{1 + \lambda \kappa \gamma_c} B_{c2}^*$$

- The change of γ_c is the change of B for a fixed current, previously computed
 - Two regimes:
 - for λκsγ_c<<1 the increase in γ corresponds to the same increase in the short sample field ("thin coils")
 - for $\lambda \kappa s \gamma_c >>1$ no increase in the short sample field ("thick coils")
 - Please note that the "thin" and "thick" regimes depend on filling ratio κ and on the slope s of the critical surface
 - For the Nb₃Sn one has to use the corresponding equations
 - Phenomenology is similar, but quantitatively different



3. IRON YOKE - DIPOLES



- Impact of the iron yoke on short sample field
 - Large effect (25%) on RHIC dipoles (thin coil and collars)
 - Between 4% and 10% for most of the others (both Nb-Ti and Nb₃Sn)



100

80





- Similar approach can be used in quadrupoles
 - Large effect on RHIC quadrupoles (thin coil and collars)
 - Between 2% and 5% for most of the others
 - The effect is smaller than in dipoles since the contribution to *B*₂ is smaller than to *B*₁



40



3. IRON YOKE - SATURATION



• Iron saturation: **B-H curve** $B = \mu \mu_0 H$

- for B<2 T, one has μ>>1 (μ~10³-10⁴), and the iron can give a relevant contribution to the field according to what discussed before
- for B>2 T, $\mu \rightarrow 1$, and the iron becomes "transparent" (no effect on field)





3. IRON YOKE - SATURATION



• Impact on calculation

- When iron saturates → image current method cannot be applied, finite element method is needed (Poisson, Opera, Ansys, Roxie, ...)
- Accuracy of model is good (error less than 10% if B-H well known)
- Impact on main component and multipoles
 - The main field is not ∞ current → transfer function *B/i* drops of several (tens) of units
 - Since the field in the iron has an azimuthal dependence, some parts of the iron can be saturated and others not → variation of b₃
 - It was considered critical
 - Led to warm iron design in Tevatron
 - Today, even few % of saturation seem manageable in operation



Impact of yoke saturation in HERA dipole and quadrupoles, From Schmuser, pg 58, fig. 4.12





- Corrective actions: shaping the iron
 - In a dipole, the field is larger at the pole over there, iron will saturate
 - The dependence on the azimuth of the field in the coil provokes different saturations, and a strong impact on multipole
 - One can optimize the shape of the iron to reduce these effects
 - Optimization of the position of holes (holes anyway needed for cryogenics) to minimize multipole change
 - RHIC is the most challenging case, since the iron gives a large contribution (50% to γ, i.e. to central field for a given current)







• Corrective actions: shaping the iron – the RHIC dipole

- The field in the yoke is larger on the pole
- Drilling holes in the right places, one can reduce saturation of b₃ from 40 units to less than 5 units (one order of magnitude), and to correct also b₅





Field map in the iron for the RHIC dipole, with and without holes From R. Gupta, USPAS Houston 2006, Lecture V, slide 12

• A similar approach has been used for the LHC dipole

- Less contribution from the iron (20% only), but left-right asymmetries due to two-in-one design [S. Russenschuck, C. Vollinger,]
- Another possibility is to shape the contour of the iron (elliptical and not circular)







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4. COIL ENDS



- Main features of the coil end design
 - ++Mechanical: find the shape that minimizes the strain in the cable due to the bending (constant perimeter)
 - In a cosθ magnet this strain can be large if the aperture is small
 - In a racetrack design the cable is bent in the 'right' direction and therefore the strain is much less
 - It is important to have codes to design the end spacers that best fit the ends, giving the best mechanical support iteration with results of production is usually needed



End of a cosθ coil [S. Russenschuck, World Scientific, Fig. 32.13]



End spacers supporting the ends of a $\cos\theta$ coil [S. Russenschuck,World Scientific, Fig. 32.13]



4. COIL ENDS



- Main features of the coil end design
 - + Magnetic: find the shape that allows to avoid a higher field in the ends
 - Due to the coil return, the main field in the ends is enhanced (typically several %)
 - On the other hand, end are the most difficult parts to manufacture → are the most unstable from a mechanical point of view
 - It is wise to reduce the main field in the ends by adding spacers this makes the design a bit more complicated



Simple coil end with increased field in P [Schmuser,pg. 58]



Coil end with spacers to decrease the main field in the end [Schmuser,pg. 58]



4. COIL ENDS



- Main features of the coil end design
 - +/- Magnetic: take care of field quality (especially if magnet is short)
 - In general a coil end will give a non-negligible contribution to multipoles
 - Two possibilities
 - Leave it as it is and compensate the coil end with the straight part so that the multipoles integral over the magnet is optimal (cheap, simple)
 - Optimize the end spacer positions to set to zero the integral multipoles in each the head (more elegant, complicated)
 - In the plot pseudo-multipoles are shown, extracted as Fourier coefficients
 - The scaling with the reference radius is not valid
 - They are not unique if you start from radial or tangential expression, B_x or B_y you get different things
 - They give an idea of the behavior of the field harmonics, and way to get a compensation
 - The real 3d expansion can be written (see A. Jain, USPAS 2006 in Phoenix: "Harmonic description of 2D fields", slide 4) Main field and pseudo-multipoles in coil end optimized to have null integrated b₃









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5. OTHER DESIGNS: RACETRACK



Vertical iron pad

• Block coil

- Cable is not keystoned
- Cables are perpendicular to the midplane
- Ends are wound in the easy side, and slightly opened
- Internal structure to support the coil needed
- Example: HD2 coil design



Key Bladder Al rod location Horizontal iron pad

HD2 design: 3D sketch of the coil (left) and magnet cross section (right) [from P. Ferracin et al, MT19, IEEE Trans. Appl. Supercond. **16** 378 (2006)]

Al shell



5. OTHER DESIGNS: RACETRACK



- Block coil HD2
 - Two layers, two blocks
 - Enough parameters to have a good field quality
 - Ratio peak field/central field not so bad:
 1.05 instead of 1.02 as for a cosθ with the same quantity of cable
 - Ratio central field/current density is 12% less than a cosθ with the same quantity of cable
 - Short sample field is around 5% less than what could be obtained by a cosθ with the same quantity of cable
 - Reached 87% of short sample







5. OTHER DESIGNS: COMMON COIL



• Common coil

- A two-aperture magnet
- Cable is not keystoned
- Cables are parallel to the mid-plane
- Ends are wound in the easy side





Common coil lay-out and cross-section R. Gupta, *et al.*, "React and wind common coil dipole", talk at *Applied Superconductivity Conference 2006*, Seattle, WA, Aug. 27 - Sept. 1, 2006.







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RHIC MB

- Main dipole of the RHIC
- 296 magnets built in 04/94 01/96



• Nb-Ti, 4.2 K



- w_{eq}~9 mm к~0.23
- 1 layer, 4 blocks
- no grading







Tevatron MB

- Main dipole of the Tevatron
- 774 magnets built in ~1980



• Nb-Ti, 4.2 K



- w_{eq}~14 mm к~0.23
- 2 layer, 2 blocks
- no grading







HERA MB

- Main dipole of the HERA
- 416 magnets built in ~1985/87



- Nb-Ti, 4.2 K
- w_{eq}~19 mm к~0.26
- 2 layer, 4 blocks
- no grading







SSC MB

- Main dipole of the ill-fated SSC
- 18 prototypes built in ~1990-5



- Nb-Ti, 4.2 K
- w_{eq}~22 mm к~0.30
- 4 layer, 6 blocks
- 30% grading







HFDA dipole

- Nb₃Sn model built at FNAL
- 6 models built in 2000-2005



- Nb₃Sn, 4.2 K
- $j_c \sim 2000$ to 2500 A/mm² at 12 T, 4.2 K (different strands)
- w_{eq}~23 mm к~0.29
- 2 layers, 6 blocks
- no grading







LHC MB

- Main dipole of the LHC
- 1276 magnets built in 2001-06



- Nb-Ti, 1.9 K
- w_{eq}~27 mm к~0.29
- 2 layers, 6 blocks
- 23% grading







FRESCA

- Dipole for cable test station at CERN
- 1 magnet built in 2001



- Nb-Ti, 1.9 K
- w_{eq}~30 mm κ~0.29
- 2 layers, 7 blocks
- 24% grading







MSUT dipole

- Nb₃Sn model built at Twente U.
- 1 model built in 1995



- Nb₃Sn, 4.2 K
- $j_c \sim 1100 \text{ A/mm}^2$ at 12 T, 4.2 K
- w_{eq}~35 mm к~0.33
- 2 layers, 5 blocks
- 65% grading







D20 dipole

- Nb₃Sn model built at LBNL (USA) Nb₃Sn, 4.2 K
- 1 model built in ???



- $j_c \sim 1100 \text{ A/mm}^2$ at 12 T, 4.2 K
- w_{eq}~45 mm κ~0.48
- 4 layers, 13 blocks
- 65% grading







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HD2

- Nb₃Sn model being built in LBNL
- 1 model to be built in 2008



- Nb₃Sn, 4.2 K
- $j_c \sim 2500 \text{ A/mm}^2$ at 12 T, 4.2 K
- w_{eq}~46 mm к~0.35
- 2 layers, racetrack, no grading







Fresca2 dipole

- Nb₃Sn test station founded by UE
- cable built in 2004-2006
- Operational field 13 T
- To be tested in 2014



- $j_c \sim 2500 \text{ A/mm}^2$ at 12 T, 4.2 K
- w_{eq}~80 mm κ~0.31
- Block coil 4 layers











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RHIC MQX

- Quadrupole in the IR regions of the RHIC
- 79 magnets built in July 1993/ December 1997
- Nb-Ti, 4.2 K
- w/r~0.18 κ~0.27
- 1 layer, 3 blocks, no grading







RHIC MQ

- Main quadrupole of the RHIC
- 380 magnets built in June 1994 October 1995
- Nb-Ti, 4.2 K
- w/r~0.25 κ~0.23
- 1 layer, 2 blocks, no grading







LEP II MQC

- Interaction region quadrupole of the LEP II
- 8 magnets built in ~1991-3
- Nb-Ti, 4.2 K, no iron
- w/r~0.27 κ~0.31
- 1 layers, 2 blocks, no grading













LEP I MQC

- Interaction region quadrupole of the LEP I
- 8 magnets built in ~1987-89
- Nb-Ti, 4.2 K, no iron
- w/r~0.29 к~0.33
- 1 layers, 2 blocks, no grading





Tevatron MQ

- Main quadrupole of the Tevatron
- 216 magnets built in ~1980
- Nb-Ti, 4.2 K
- w/r~0.35 κ~0.250
- 2 layers, 3 blocks, no grading







HERA MQ

- Main quadrupole of the HERA
- Nb-Ti, 1.9 K
- w/r~0.52 κ~0.27
- 2 layers, 3 blocks, grading 10%







LHC MQM

- Low-gradient quadrupole in the IR regions of the LHC
- 98 magnets built in 2001-2006
- Nb-Ti, 1.9 K (and 4.2 K)
- *w/r*~0.61 *к*~0.26
- 2 layers, 4 blocks, no grading







LHC MQY

- Large aperture quadrupole in the IR regions of the LHC
- 30 magnets built in 2001-2006
- Nb-Ti, 4.2 K
- w/r~0.79 к~0.34
- 4 layers, 5 blocks, special grading 43%







LHC MQXB

- Large aperture quadrupole in the LHC IR
- 8 magnets built in 2001-2006
- Nb-Ti, 1.9 K
- w/r~0.89 к~0.33
- 2 layers, 4 blocks, grading 24%











SSC MQ

- Main quadrupole of the ill-fated SSC
- Nb-Ti, 1.9 K
- *w/r*~0.92 *к*~0.27
- 2 layers, 4 blocks, no grading







LHC MQ

- Main quadrupole of the LHC
- 400 magnets built in 2001-2006
- Nb-Ti, 1.9 K
- w/r~1.0 κ~0.250
- 2 layers, 4 blocks, no grading











LHC MQXA

- Large aperture quadrupole in the LHC IR
- 18 magnets built in 2001-2006
- Nb-Ti, 1.9 K
- w/r~1.08 к~0.34
- 4 layers, 6 blocks, special grading 10%











LHC MQXC

- Nb-Ti option for the LHC upgrade
- LHC dipole cable, graded coil
- 1-m-long model built in 2011-2 to be tested in 2012
- *w/r*~0.5 *κ*~0.33 2 layers, 4 blocks









LARP HQ

- 120 mm aperture Nb₃Sn option for the LHC upgrade (IR triplet)
- 1-m-long model tested in 2011, more to come plus a 3.4-m-long
- *w/r*~0.5 *κ*~0.33 2 layers, 4 blocks







CONCLUSIONS



- **Grading** the current density in the layers can give a larger performance for the same amount of conductor
 - 3-5% more in dipoles, 5-10% more in quadrupoles
- The iron has several impacts
 - Useful for shielding, can considerably increase the field for a given current the impact on the performance is small but not negligible
 - Drawbacks: saturation, inducing field harmonics at high field can be cured by shaping or drilling holes in the right place
- Coil ends the design must aim at reducing the peak field
- Other lay-outs: pro and cons
- We shown a gallery of dipole and quadrupole magnetic designs used in the past 30 years



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 - Work by G. Ambrosio, S. Zlobin on common coil magnets at FNAL



REFERENCES



- Plus...
 - A whole series of papers about each magnet that has been presented



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