# Superconductivity in Nanodiamond

# NANO-SCALE TRANSPORT PHYSICS LABORATORY

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NECSA-Wits Workshop, North West Province, South Africa



B-NCD covalent SC with interesting microstructure

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## Superconductivity in Nanodiamond

- Diamond, intrinsically a high bandgap semiconductor (5.5 eV). Boron substitutionally incorporated. Diamond has highest Debye temperature, ~2 300 K.
- Creates deep, narrow impurity acceptor band 0.37 eV above the valence band.
- Difficult to dope, high structural integrity. Hence doping introduces disorder. Superconductivity, T<sub>c</sub> high as 10 K.





- Experiments show Anderson-Mott insulator to metal transition, evidence of non-rigid impurity band states.
- Experimental work in BNCD needed to interpret grain boundary effects. Vortices not yet studied.
- Theoretical work needed to interpret the role of disorder in BNCD.

 We present tandem experimental and theoretical work towards understanding superconductivity in BNCD, focusing on the influence of disorder. Studies samples with different boron concentrations and microstructures.



**Experimental** Transport Measurements

 $1 \% H_2 BNCD$ 



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- Region of negative MR decreases with temperature, vanishes around 2.4 K (just above the metal-insulator transition).
- Gradient of MR in high field region changes little in temperature range. Characteristic of disordered metal.



5 % H<sub>2</sub> BNCD

## **Superfluid** (T < T<sub>c</sub>)





 In strictly 2D type II superconductors, vortex-antivortex pairs decouple (known as BKT transition in analogy with X-Y model.)

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## Inhomogeneous Mean Field Bogoliubov-de Gennes Study

- Study boron-doped diamond using the inhomogeneous Bogoliubov de-Gennes theory within a mean-field approximation.
- Boron doping forms narrow boron acceptor band in diamond. Degeneracy lifted by inhomogeneity.
- Treat single narrow boron acceptor band, therefore include Coulomb interaction. Mean field Hamiltonian:

$$\mathcal{H} = \sum_{i,\sigma} (\epsilon_i - \mu_i) c_{i\sigma}^{\dagger} c_{i\sigma} + \sum_i (\Delta(r_i) c_{i\uparrow}^{\dagger} c_{i\downarrow}^{\dagger} + \Delta^*(r_i) c_{i\downarrow} c_{i\uparrow})$$
$$-t_{i,j} \sum_{\langle i,j \rangle, \sigma} (c_{i\sigma}^{\dagger} c_{j\sigma} + h.c.) + \sum_{\langle i,j \rangle} W_{i,j}(n_i n_j),$$

 Hamiltonian rendered diagonalizable through Bogoliubov-Valatin transformation of the Fermion operators

$$c_{i\sigma}(r_i) = \sum_{i,\sigma} u_{n\sigma\sigma'}(r_i)\gamma_{n\sigma'} + v_{n\sigma\sigma'}^*(r_i)\gamma_{n\sigma'}^{\dagger}$$



Theoretical Outline Inhomogeneous Mean Field Bogoliubov-de Gennes Study

The resulting matrix equation is of the form:

$$\begin{pmatrix} H_{BdG} & \Delta \\ \Delta^* & H_{BdG}^* \end{pmatrix} \begin{pmatrix} u_{n\sigma}(r_i) \\ v_{n\sigma}(r_i) \end{pmatrix} = E_n \begin{pmatrix} u_{n\sigma}(r_i) \\ v_{n\sigma}(r_i) \end{pmatrix}$$

• The pairing amplitude can then be expressed in terms of the Bogoliubov operators as:

$$\Delta(r_i) = V \sum_n u_{n\uparrow}(r_i) v_{n\downarrow}^*(r_i) [1 - f(E_n)] + u_{n\downarrow}(r_i) v_{n\uparrow}^*(r_i) f(E_n),$$

In this representation, the occupation number is

$$n(r_i) = \sum_{n} |u_{n\uparrow}(r_i)|^2 f(E_n) + |v_{n\uparrow}(r_i)|^2 (1 - f(E_n))$$

• The system is solved self-consistently by updating the eigenvalues and iterating.



### **On-site Disorder**

- Shift in the local chemical potential of the boron sites (diagonal disorder).
- Chemical potential of boron sites assumed to follow Gaussian distribution about self-consistently determined chemical potential of boron sites.
- Disorder parameter defined as the FWHM of the Gaussian.

### **Structural Disorder**

- Inhomogeneous hopping parameter between all sites (non-diagonal disorder), represents bond-length disorder.
- Hopping parameter assumed to follow Gaussian distribution about some mean value.
- Disorder parameter defined as the FWHM of the Gaussian.

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#### Theoretical Results

# Inhomogeneous Mean Field Bogoliubov-de Gennes Study



### **Occupation Number**

Boron sites are occupied. Slight on-site disorder spreads occupation slightly.



### Local Pairing Amplitude

- Local pairing amplitude maximal at boron sites.
- Sensitive to slight disorder, pairing amplitude less uniform than occupation.

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### **On-site Disorder Only**



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### Structural Disorder Only



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### **On-site vs. Structural Disorder**



- Distribution of the local pairing amplitude (on-site disorder only).
- Distribution around 1.6 decreases sightly.
- Slight change in distribution around 0.
- Localized regions with relatively high pairing amplitude.

- Structural disorder. Distribution around 1.6 decreases rapidly.
- Pairing amplitude around 0 increases.
  Illustrates overall increase in the mean pairing amplitude.
- Interconnected regions with small PA.

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## **Correlated Structural Disorder**



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#### Theoretical Results

### **Temperature Dependence**





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### Conclusion

- Possibility of type II superconductivity in BNCD demonstrated in samples with grain sizes
  50 70 nm. Unusual features in high temperature MR.
- Suggest model of disordered array of weakly coupled Josephson junctions for samples closer to the Anderson-Mott transition. Possibility of BKT transition?
- Still to do: devices with different boron concentrations. AC Josephson effect. Thin film devices.
- Illustrated the interplay between structural and on-site disorder and the influence on the local and mean pairing amplitude.
- Shown that structural disorder can enhance mean pairing amplitude, results in more interconnected disordered superconductor with smaller local pairing amplitude.
- Still to do: build in Josephson junctions and vortices. Kubo treatment to merge theory and transport measurements.



Conclusion

Conclusion

- Nano-scale nano-Ο diamond devices
  - Quantum Ο information **Bolometers**, Ο **Medical imaging**

probes

probes



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- The Nano-scale Transport team : Zivayi Chiguvare, Dmitry Churochkin, Michael Katkov, Kunjal Shah, George Chimowa, Davie Mtsuku, Christopher Coleman, Tahir Aslan, Siphe Ncube and Charles Sandrock. We thank David Tomanek, Gehan Amaratunga, Ravi Silva, Jiri Mares and Ping Sheng for useful discussions.
- Centre for Theoretical Studies, Indian Institute of Technology, Kharagpur. We thank Swagata Acharya for useful discussions.
- Condensed Matter Physics Group, University of Leeds, B.J. Hickey, O. Cespedes, Mannan Ali, Fatma Al'Mamri, May Wheeler, Tim Moorsom, Joseph Bately, Nathen Satchell.
- The NRF for the Nanoflagship Project awarded to S. Bhattacharyya and financial support as well as the CoE in Strong Materials.
- Thank you for your attention!

Conclusion







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### Superconductivity BNCD

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