

# Neutralino relic density from ILC measurements in the CPV MSSM

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Based on arXiv:0803.2584 (PRD78)  
with G. Bélanger, O. Kittel, H.U. Martyn and A. Pukhov

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# Motivation

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- Cosmol. obs. → amount of DM:  $\Omega h^2 = 0.11 \pm 6\%$  (!) WMAP  
SDSS  
most attractive candidate: WIMP from BSM physics.
- Aim at colliders (after discovery) is to do precision measurements of BSM particles, incl DM candidate
- Hope to determine properties of BSM DM at LHC/ILC  
→ make a “collider prediction” of its  $\Omega h^2$   
→ test standard cosmological model
- In general, expected precision is O(10%) at LHC and few % at ILC → could match WMAP/PLANCK  
Nojiri, Polesello, Tovey; Arnowitt et al.; Bambade, Berggren, Richard, Zhang; Martyn; Baltz, Battaglia, Peskin, Wizansky; Berger, Gainer, Hewett, Lillie, Rizzo.
- Need precise measurements of masses and couplings ...



# MSSM with CP violation

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- In the general MSSM, gaugino and higgsino mass parameters and trilinear couplings can be complex:

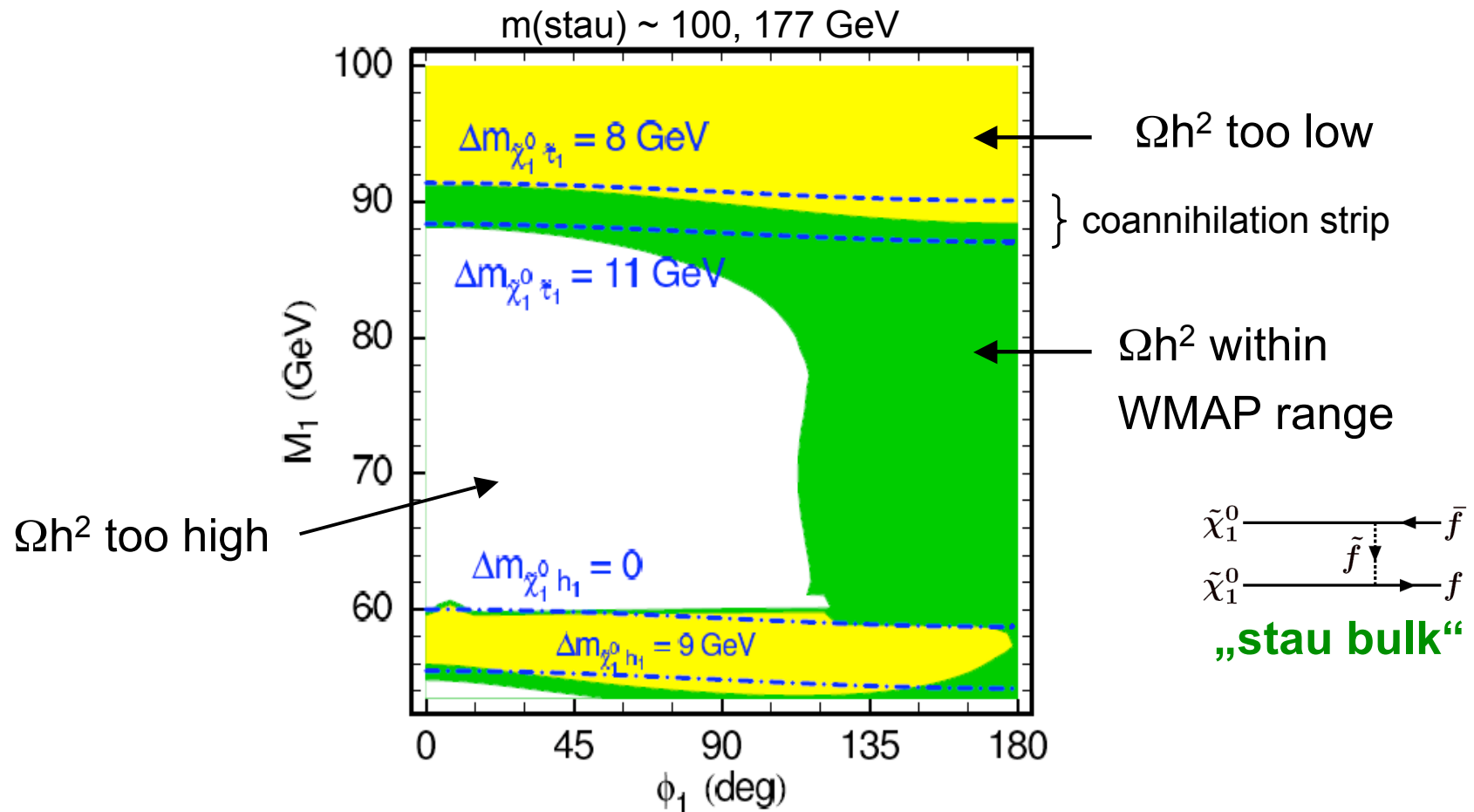
$$M_1 = |M_1|e^{i\phi_1}, \mu = |\mu|e^{i\phi_\mu}, A_f = |A_f|e^{i\phi_f}$$

- Well known that sparticle and Higgs phenomenology at colliders depends sensitively on CP phases; important variations in production and decay rates.
- In hep-ph/0604150\* we analysed all  $\chi^0$  annihilation channels and showed that CP phases can also have dramatic effects on the relic density (due to modif's in couplings!)

\*) Belanger, Boudjema, SK, Pukhov, Semenov, hep-ph/0604150 (PRD73)



# Example: light stau, t-channel



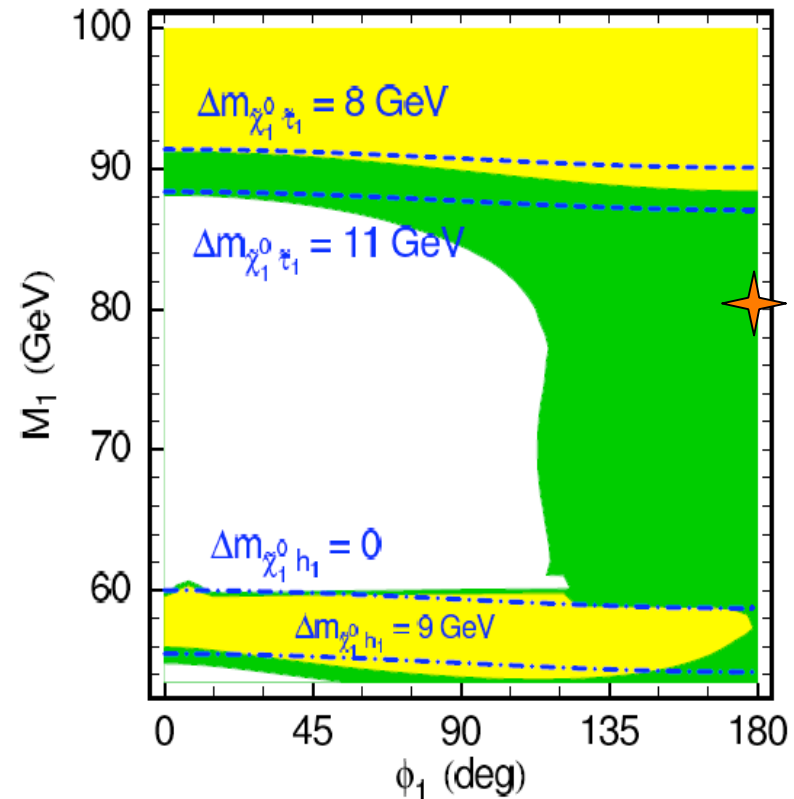
Belanger, Boudjema, SK, Pukhov, Semenov, hep-ph/0604150 (PRD73)

# How well could ILC resolve this?

- Pick a point for case study

	$\tilde{\chi}_1^0$	$\tilde{\chi}_2^0, \tilde{\chi}_1^+$	$\tilde{\chi}_3^0$	$\tilde{\chi}_4^0$
	80.7	164.9	604.8	610.5
	$\tilde{\tau}$	$\tilde{\nu}_\tau$	$\tilde{e}$	$\tilde{\nu}_e$
R(1)	100.9	–	1000.9	–
L(2)	177.2	123.1	1001.1	998.0

- For  $\phi_1 > 110^\circ$ ,  $\Omega h^2 < 0.136$
- For  $\phi_1 = 0$ , relic density would be too large:  
 $\Omega h^2 = 0.167$





# Stau-bulk benchmark point

## Input parameters

$$M_1 = 80.47\text{GeV} \quad M_2 = 170.35\text{GeV} \quad M_3 = 700\text{GeV} \quad \phi_1 = 180$$

$$\mu = 600\text{GeV} \quad \tan\beta = 10 \quad \phi_\mu = 0$$

$$M_{\tilde{\tau}_L} = 138.7\text{GeV} \quad M_{\tilde{\tau}_R} = 135.2\text{GeV} \quad A_\tau = 60\text{GeV} \quad \phi_\tau = 0$$

## Mass spectrum

	$\tilde{\chi}_1^0$	$\tilde{\chi}_2^0$	$\tilde{\chi}_3^0$	$\tilde{\chi}_4^0$	$\tilde{\chi}_1^+$	$\tilde{\chi}_2^+$	$h_1$	$h_{2,3}$
	80.7	164.9	604.8	610.5	164.9	612.1	116.1	997.
	$\tilde{\tau}$	$\tilde{\nu}_\tau$	$\tilde{e}$	$\tilde{\nu}_e$	$\tilde{u}$	$d$	$\tilde{t}$	$b$
R(1)	100.9	–	1000.9	–	999.4	1000.3	939.1	995.6
L(2)	177.2	123.1	1001.1	998.0	998.6	1001.7	1075.6	1006.4

- Light gauginos and staus, staus are strongly mixed
- LSP annihilates into tau pairs via stau exchange in t-channel  
efficient if staus are mixed – no coannihilation

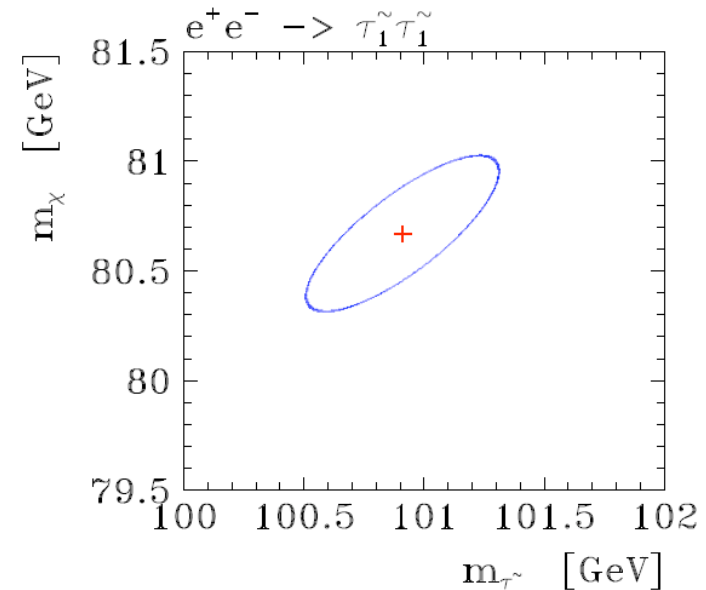


# ILC measurements

MC simulation by H.U. Martin

- Threshold scans
- Kinematic endpoints
- Polarized cross sections
- Tau polarization

Difficulty: all channels lead  
to same signature:  $\tau^+\tau^- E^{\text{miss}}$



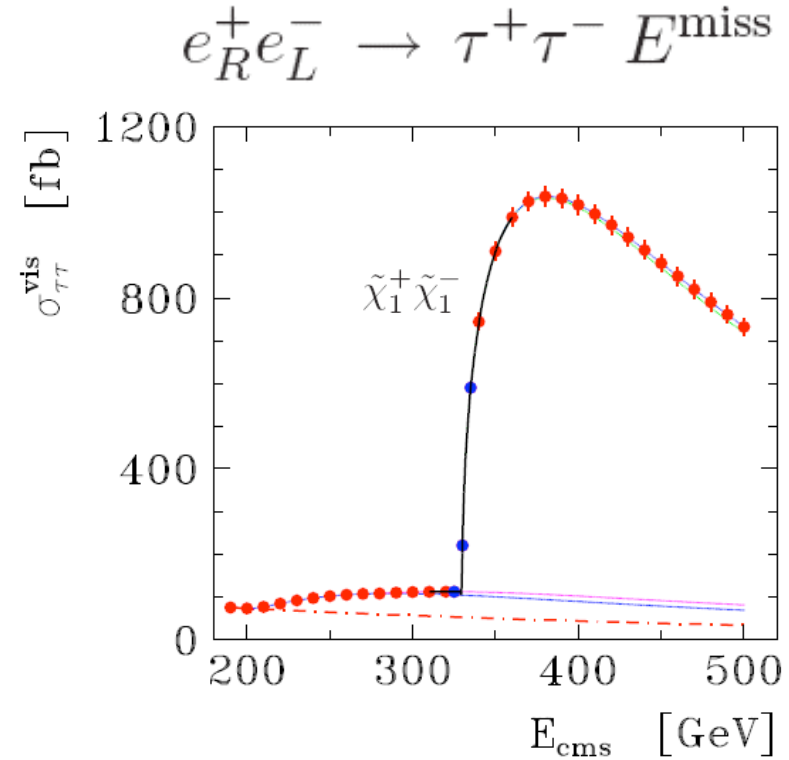
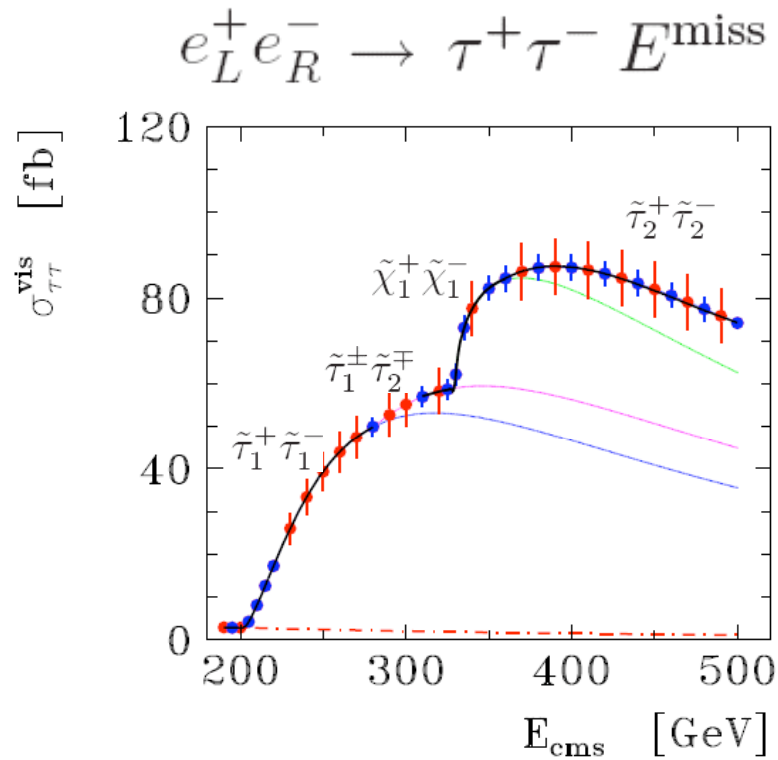
channel	observables
$\tilde{\tau}_1^+ \tilde{\tau}_1^-$	$m_{\tilde{\tau}_1} = 100.92 \pm 0.40 \text{ GeV}$ $m_{\tilde{\chi}_1^0} = 80.67 \pm 0.35 \text{ GeV}$ $\cos 2\theta_{\tilde{\tau}} = -0.065 \pm 0.028$ $\mathcal{P}_{\tau} = 0.64 \pm 0.035$
$\tilde{\tau}_2^+ \tilde{\tau}_2^-$	$m_{\tilde{\tau}_2} = 176.9 \pm 9.1 \text{ GeV}$
$\tilde{\chi}_1^+ \tilde{\chi}_1^-$	$m_{\tilde{\chi}_1^{\pm}} = 164.88 \pm 0.015 \text{ GeV}$

**per-mil level !**



# ILC cross sections

red (blue) points  
 $\mathcal{L} = 2 \text{ fb}^{-1} (10 \text{ fb}^{-1})$



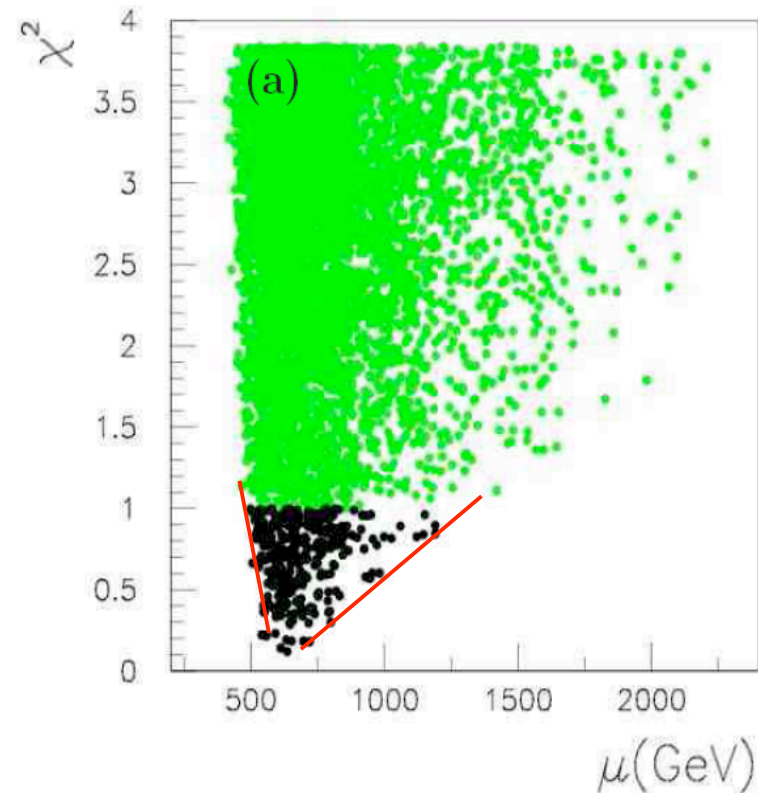
N.B. heavy selectrons to avoid EDM constraints; suppresses neutralino production





# Parameter fit with Markov Chain MC

- Perform a fit to the six measurements and  $\tau\tau$  total Xsect at 400 GeV
- Free parameters:  $M_1, \mu, \tan\beta, M_{L3}, M_{R3}, A_\tau, \phi_1, \phi_\tau$
- Use Markov Chain Monte Carlo (MCMC) to explore parameter space

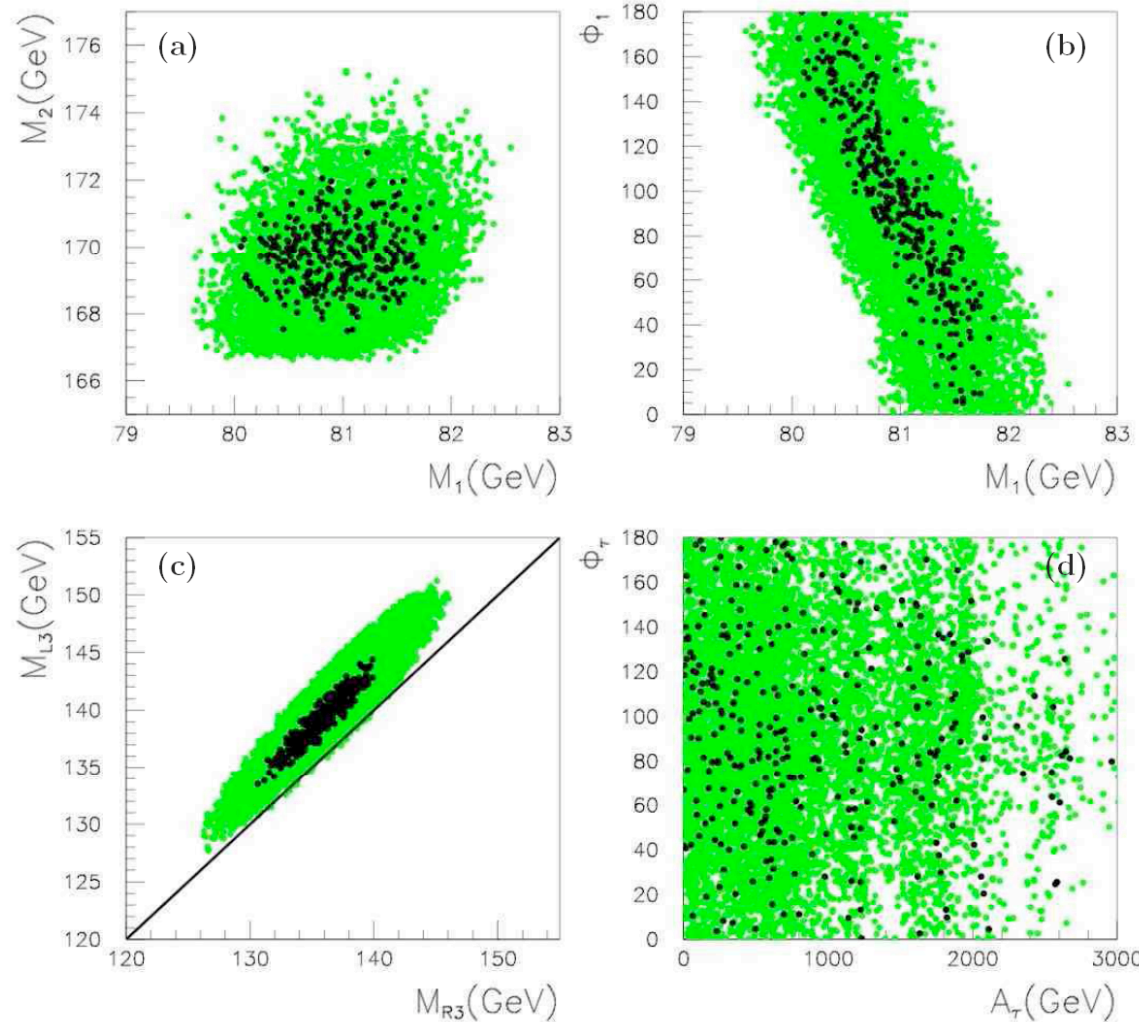




# Lagrangian parameters

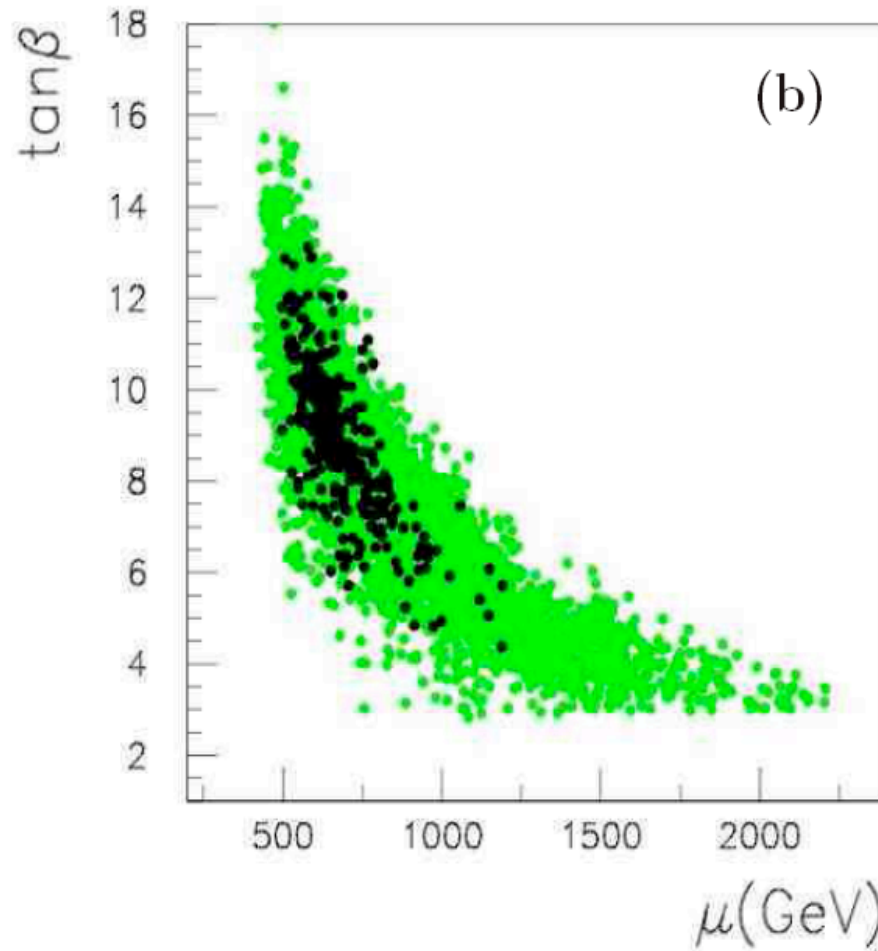
black:  $\chi^2 < 1$   
green:  $\chi^2 < 3.84$

NB: Gaugino & slepton  
mass parameters well  
determined;  
trilinear  $A_\tau$  and  
phases of  $M_1$  and  $A_\tau$   
undetermined





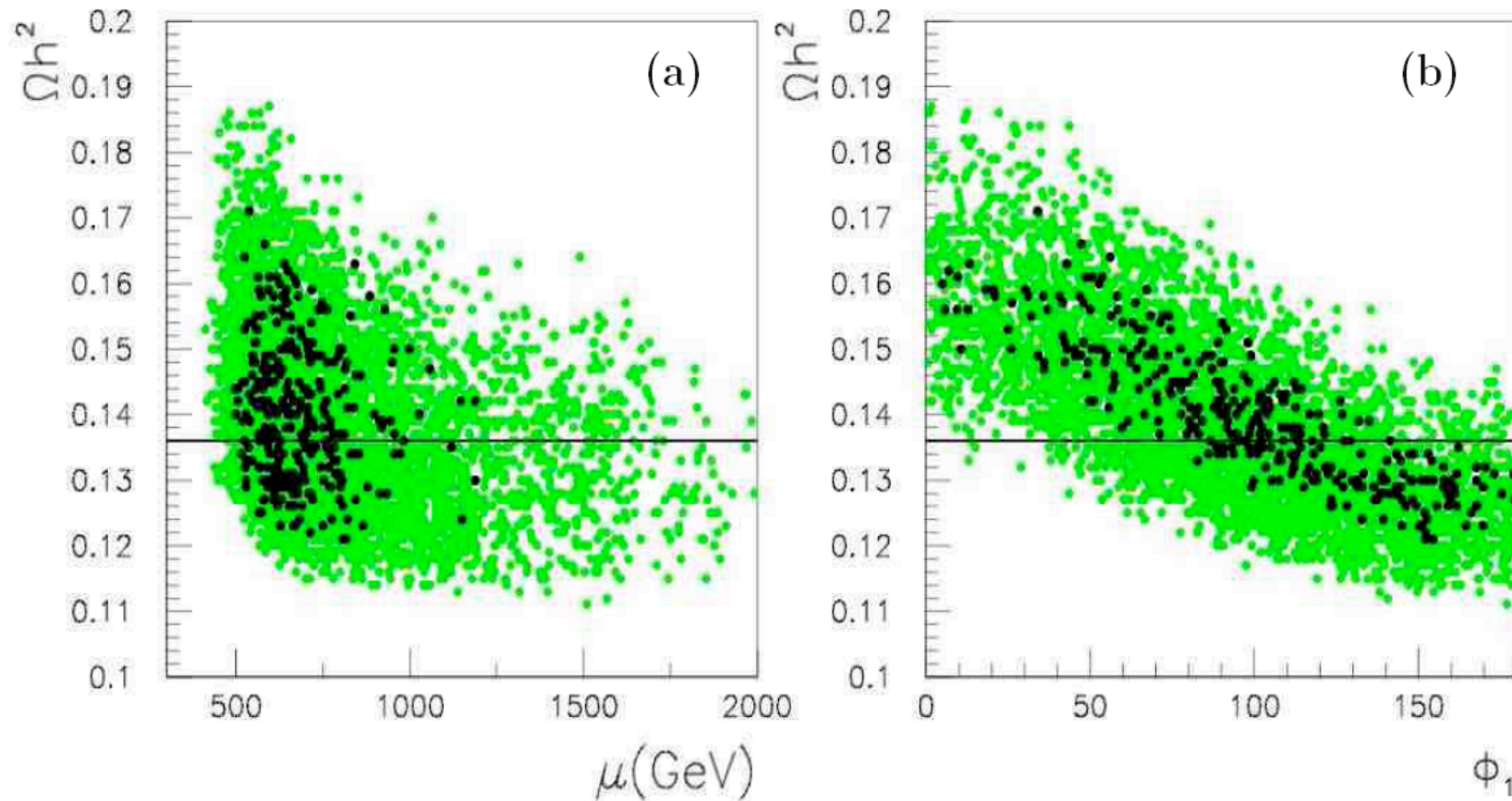
# $\mu - \tan\beta$ correlation



black:  $\chi^2 < 1$   
green:  $\chi^2 < 3.84$



# Impact on relic density



inferred range:  $0.11 < \Omega h^2 < 0.19$  at 95% CL



# Use CP-odd observables?

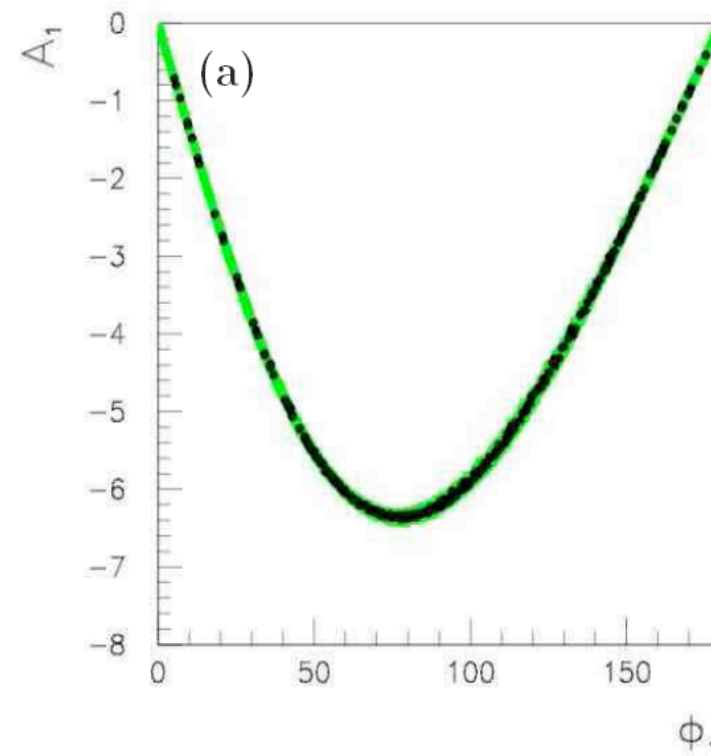
- Consider  $e^+e^- \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_2^0$

$$\tilde{\chi}_2^0 \rightarrow \tilde{\tau}_1^\pm \tau^\mp, \tilde{\tau}_1^\pm \rightarrow \tilde{\chi}_1^0 \tau^\pm$$

- define T-odd asymmetry

$$A_1 = \frac{\sigma(\mathcal{T} > 0) - \sigma(\mathcal{T} < 0)}{\sigma(\mathcal{T} > 0) + \sigma(\mathcal{T} < 0)},$$

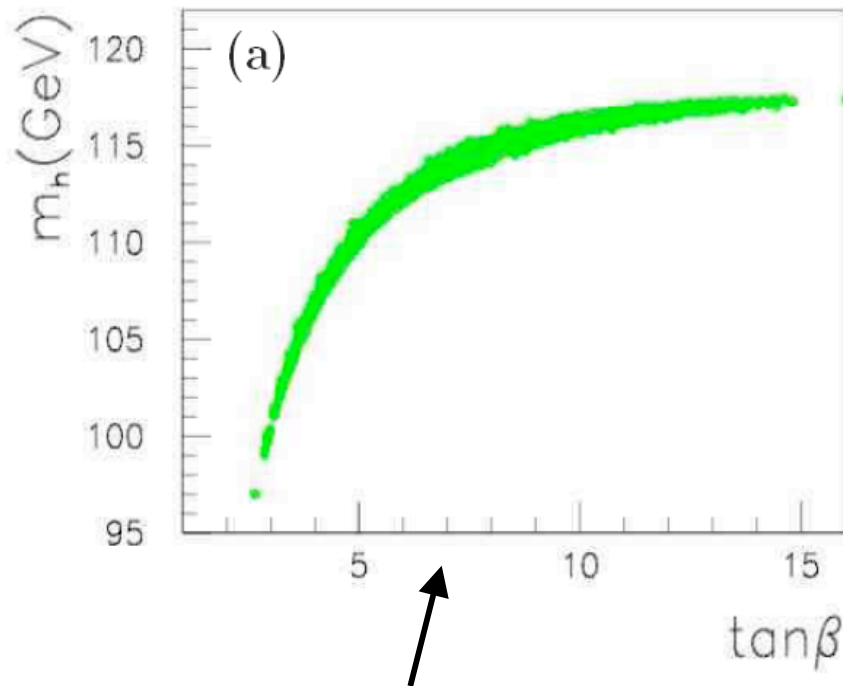
$$\mathcal{T} = (\mathbf{p}_{e^-} \times \mathbf{p}_{\tau^-}) \cdot \mathbf{p}_{\tau^+}$$



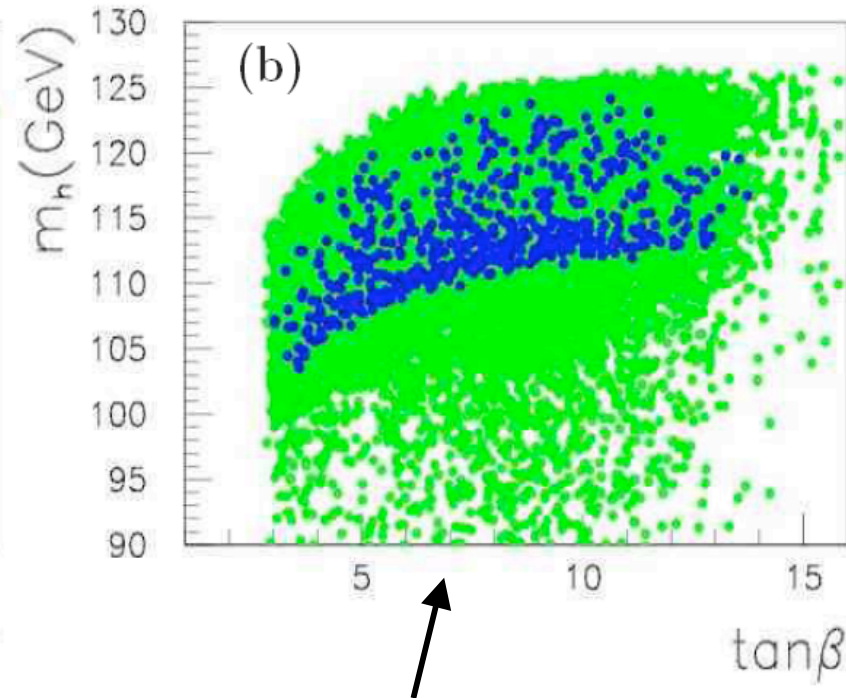
$A_1 \neq 0$  would be signal of CP violation. But does not help to constrain  $\Omega h^2$  because  $A_1$  symmetric around  $\phi_1 = 90^\circ$  ☹



# Include Higgs mass in fit? $\rightarrow$ No



Stop parameters fixed to their nominal values

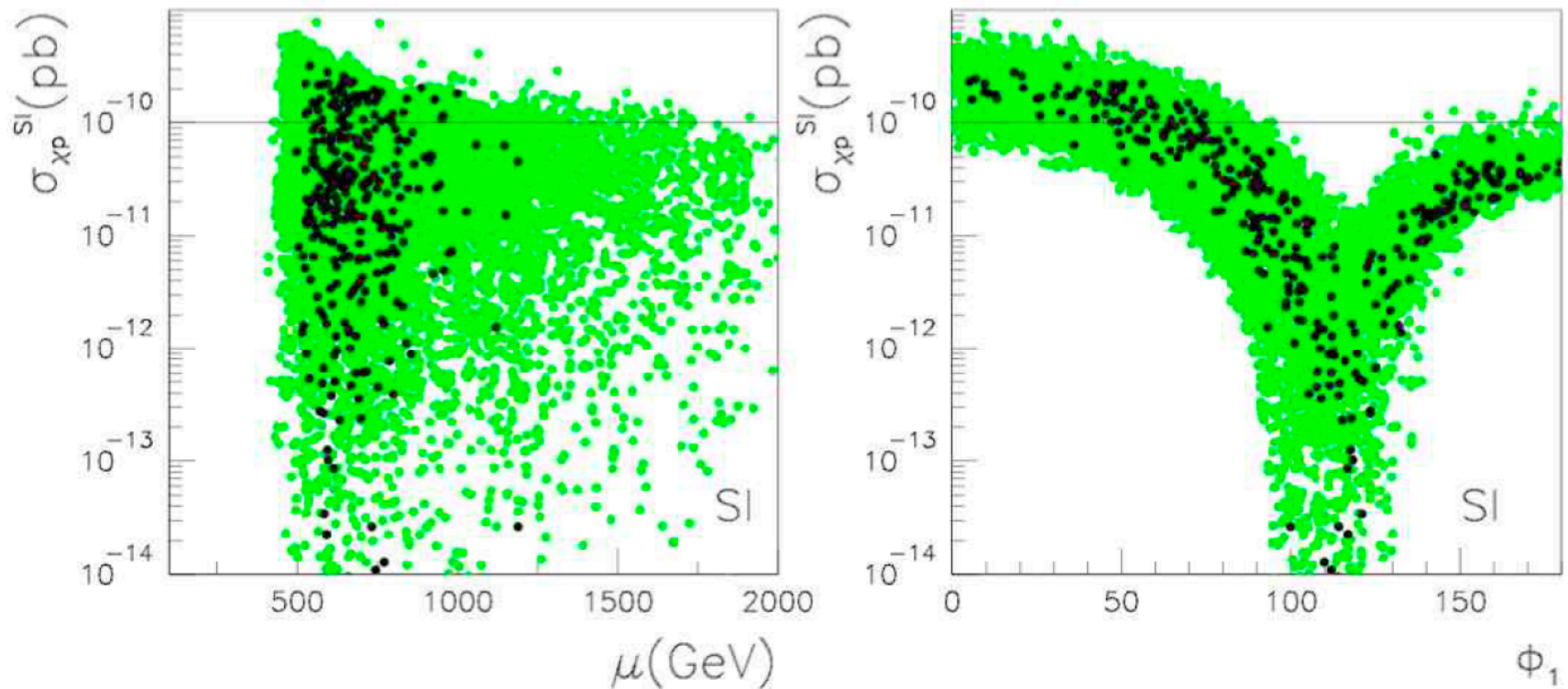


green: stop sector undetermined;  
blue: stop masses known to 10%



# Interplay with direct DM detection

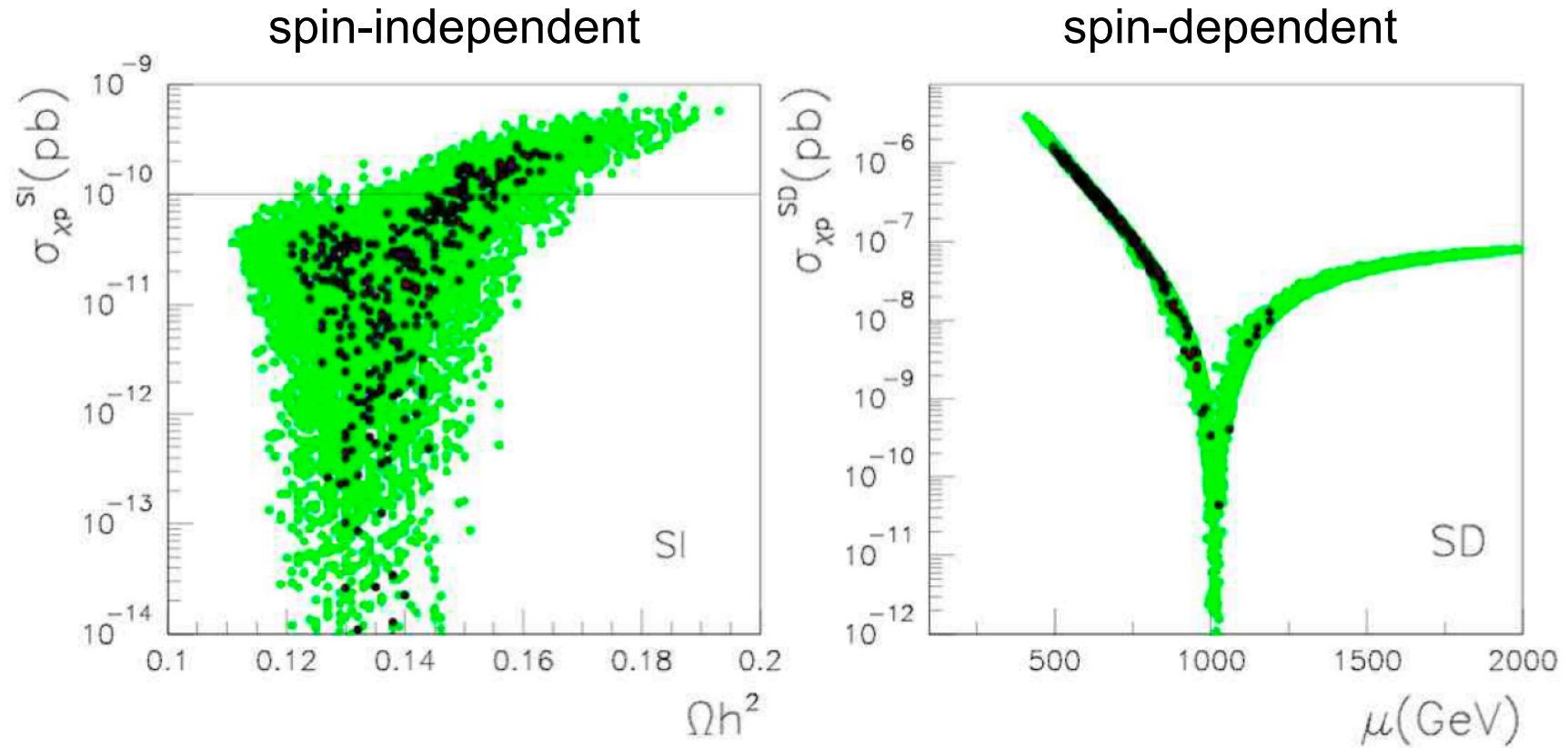
spin-independent neutralino-proton cross sections



Heavy squarks;  $\chi p$  interaction dominated by Higgs exchange



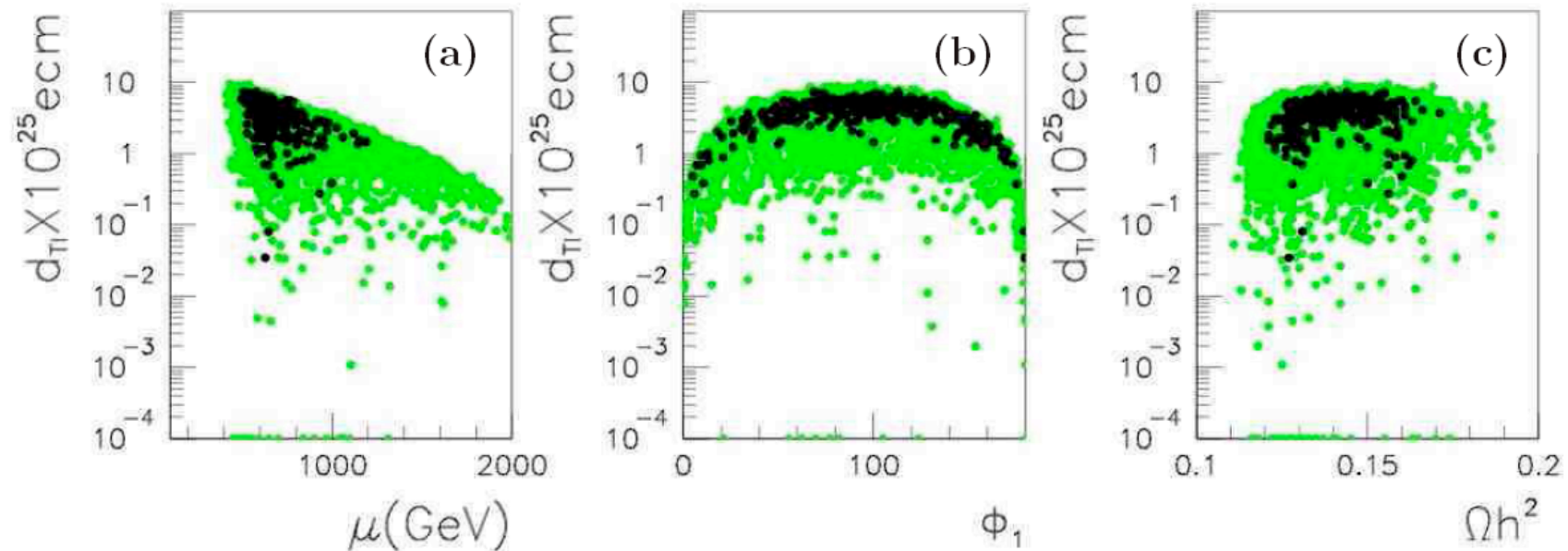
# Interplay with direct DM detection -cont-







# Interplay with EDM measurements (TI)



Present limit:  $d_{\tau} < 9 \cdot 10^{-25} \text{ e cm}$ . Future improvement by 2 orders of magnitude would probe most of the parameter space of this scenario; however not much impact on  $\Omega h^2$



# Conclusions

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- Collider determination of  $\Omega h^2$  needs precise measurements of masses \*and\* couplings → CP phases
- Investigated „stau bulk“ scenario in CPV-MSSM: only neutralino1, chargino1, stau1+2 detectable at ILC.
- Very good precision on masses and stau mixing 😊 however poor parameter determination ☹ [NB  $\mu$ -tan $\beta$ ]
- Parameter fit gives  $0.11 < \Omega h^2 < 0.19$  at 95% CL
- Direct DM detection and EDM experiments could somewhat help resolve the scenario.
- Would need complete  $\tilde{\nu}$ -ino system at LC  $\sqrt{s} \sim 1-2$  TeV;