

# Odd features of heavy flavored jets

*Boris Kopeliovich*  
*Valparaiso*

In collaboration with  
Jan Nemchik, Irina Potashnikova  
and Ivan Schmidt

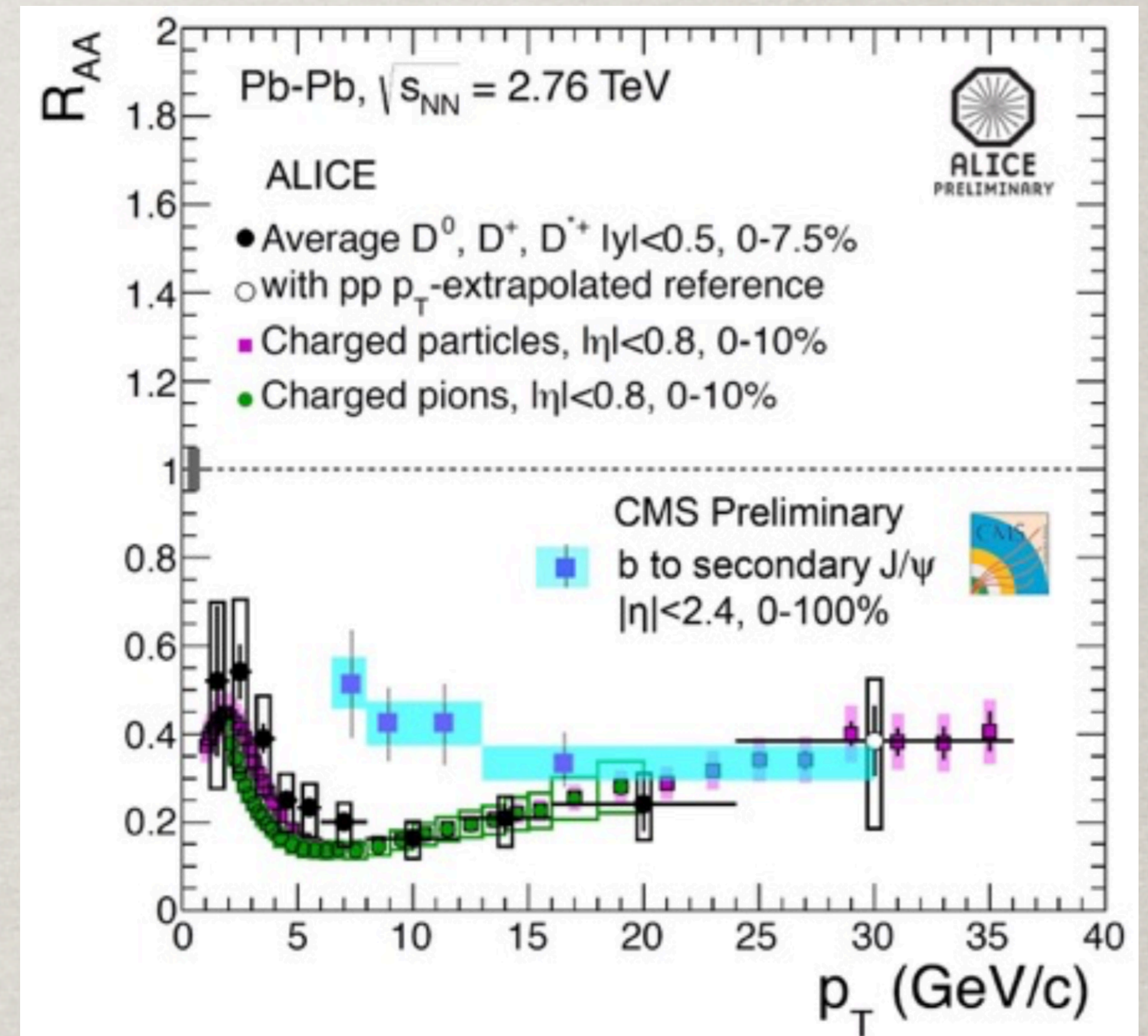


# Quenching of heavy flavors at high $p_T$

In the popular scenario, explaining jet quenching, observed in heavy ion collisions, by induced energy loss in the created hot medium, a much weaker suppression was anticipated for heavy flavored mesons, caused by the **dead-cone effect**.

Yu.Dokshitzer, D.Kharzeev, PLB 519(2001)199

Later, however, measurements revealed similar magnitudes of suppression for heavy and light hadrons.





# Hard parton collision

- High-pt parton scattering leads to formation of **4** cones of gluon radiation:
- (i) the color field of the colliding partons is **shaken off** in forward-backward directions.
  - (ii) the scattered partons carry **no field** up to transverse frequencies  $k \ll p_T$ .

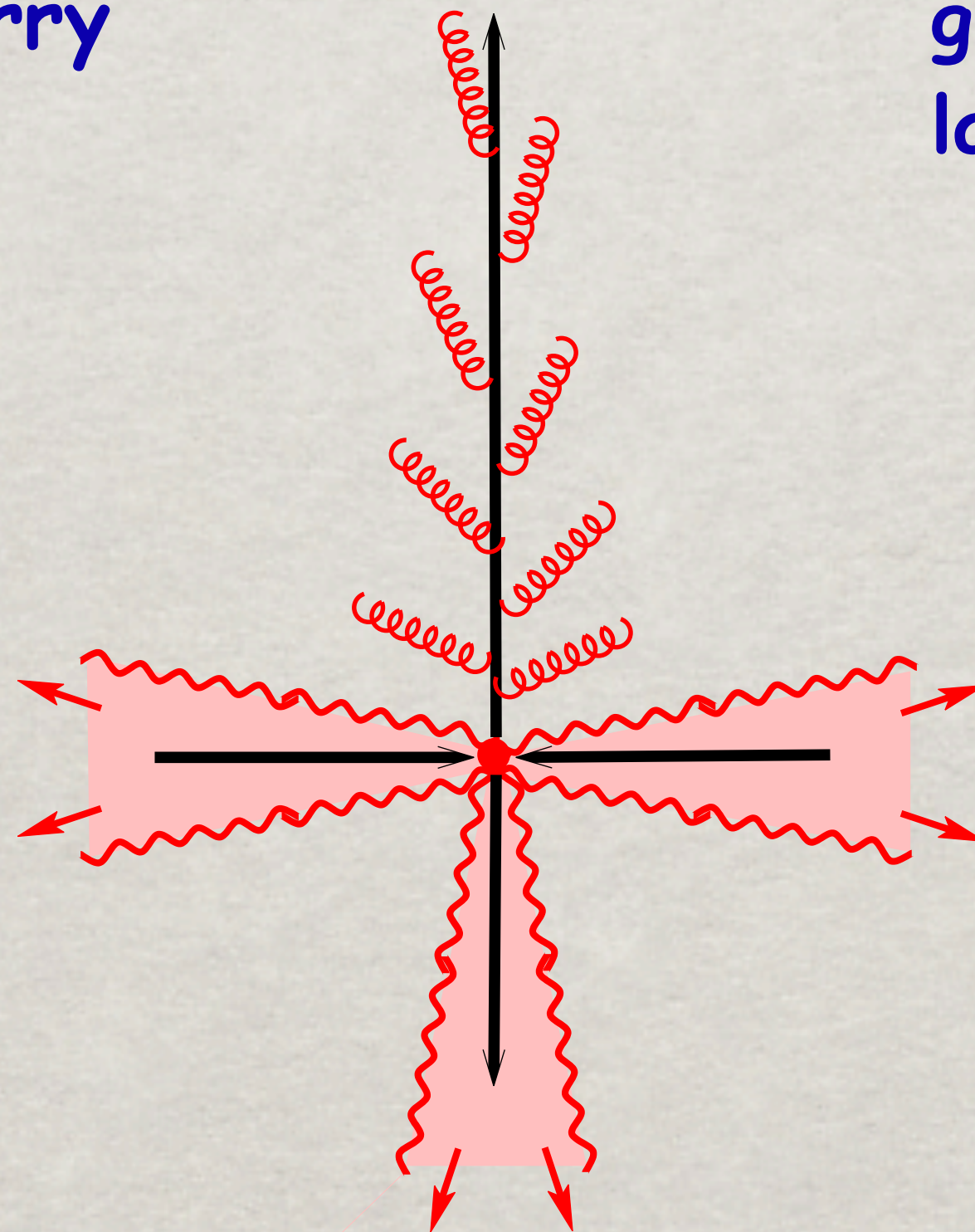
The final state high- $p_T$  partons **regenerate** the lost color field by radiating gluons and forming the up-down jets.

The coherence length/time of gluon radiation

$$l_c = \frac{2E_q x(1-x)}{k_T^2 + x^2 m_q^2}$$

**First** are radiated, i.e. **regenerated**, gluons with small longitudinal and large transverse momenta.

In heavy ion collisions the regeneration process proceeds within a hot environment (QGP), and additional radiation (much weaker than vacuum) is induced by multiple interactions.





# Heavy flavored jets

How much energy is radiated over path length  $L$ ?

$$\Delta E(L) = E \int_{\Lambda^2}^{p_T^2} dk^2 \int_0^1 dx x \frac{dn_g}{dx dk^2} \Theta(L - l_c)$$

$$\frac{dn_g}{dx dk^2} = \frac{2\alpha_s(k^2)}{3\pi x} \frac{k^2[1 + (1-x)^2]}{[k^2 + x^2 m_q^2]^2}$$

**Dead-cone effect:**

gluons with  $k^2 < x^2 m_q^2$  are suppressed.

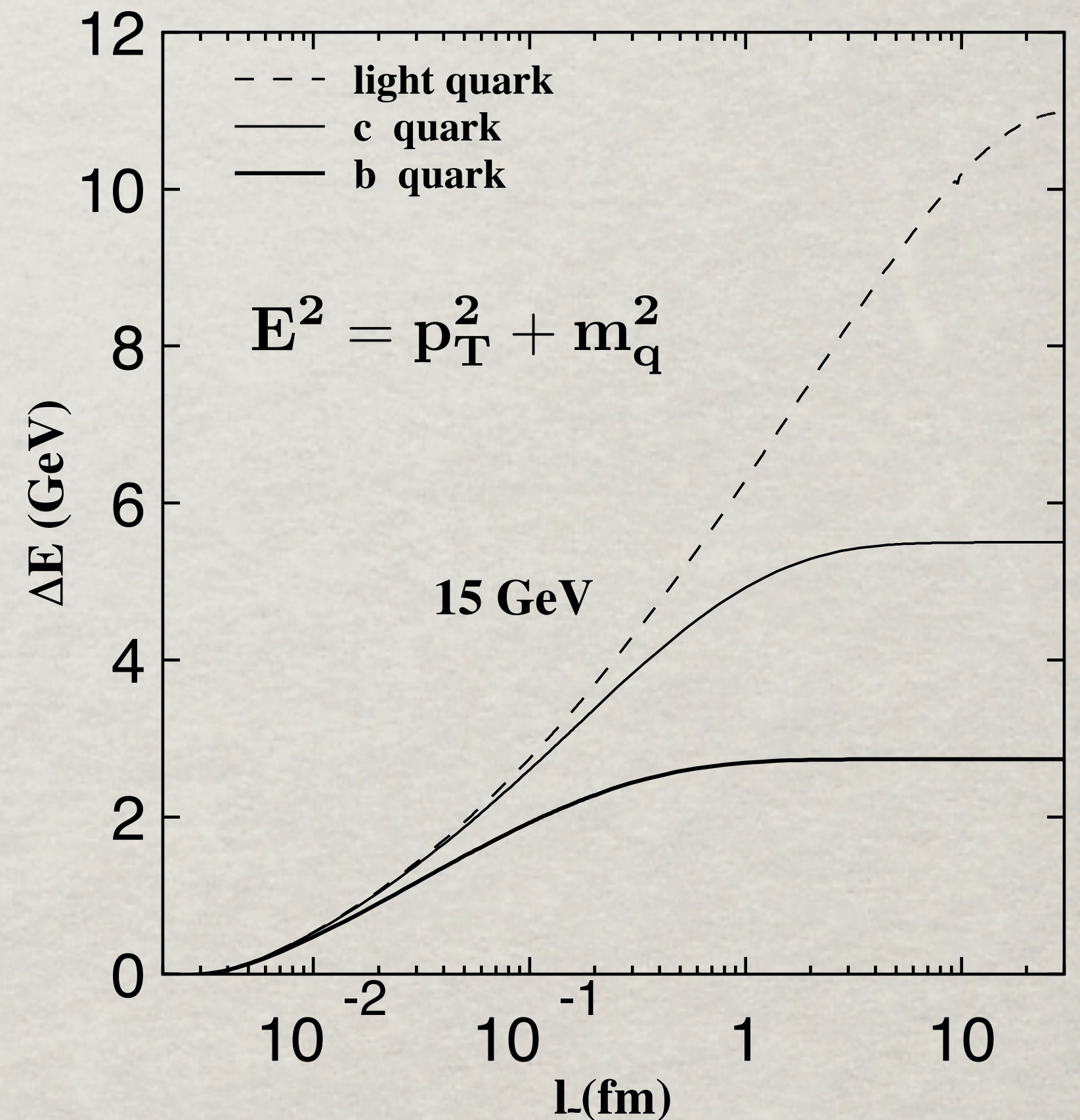
Correspondingly, the radiation length is short

$$l_c = \frac{2E_q x(1-x)}{k_T^2 + x^2 m_q^2}$$

Radiation of heavy quarks ceases shortly.

Only a small fraction of the quark energy,  $\Delta z \sim \Delta E/E$ , is radiated (differently from light quarks). Therefore, the final B-meson carries almost the whole momentum of the b-jet.

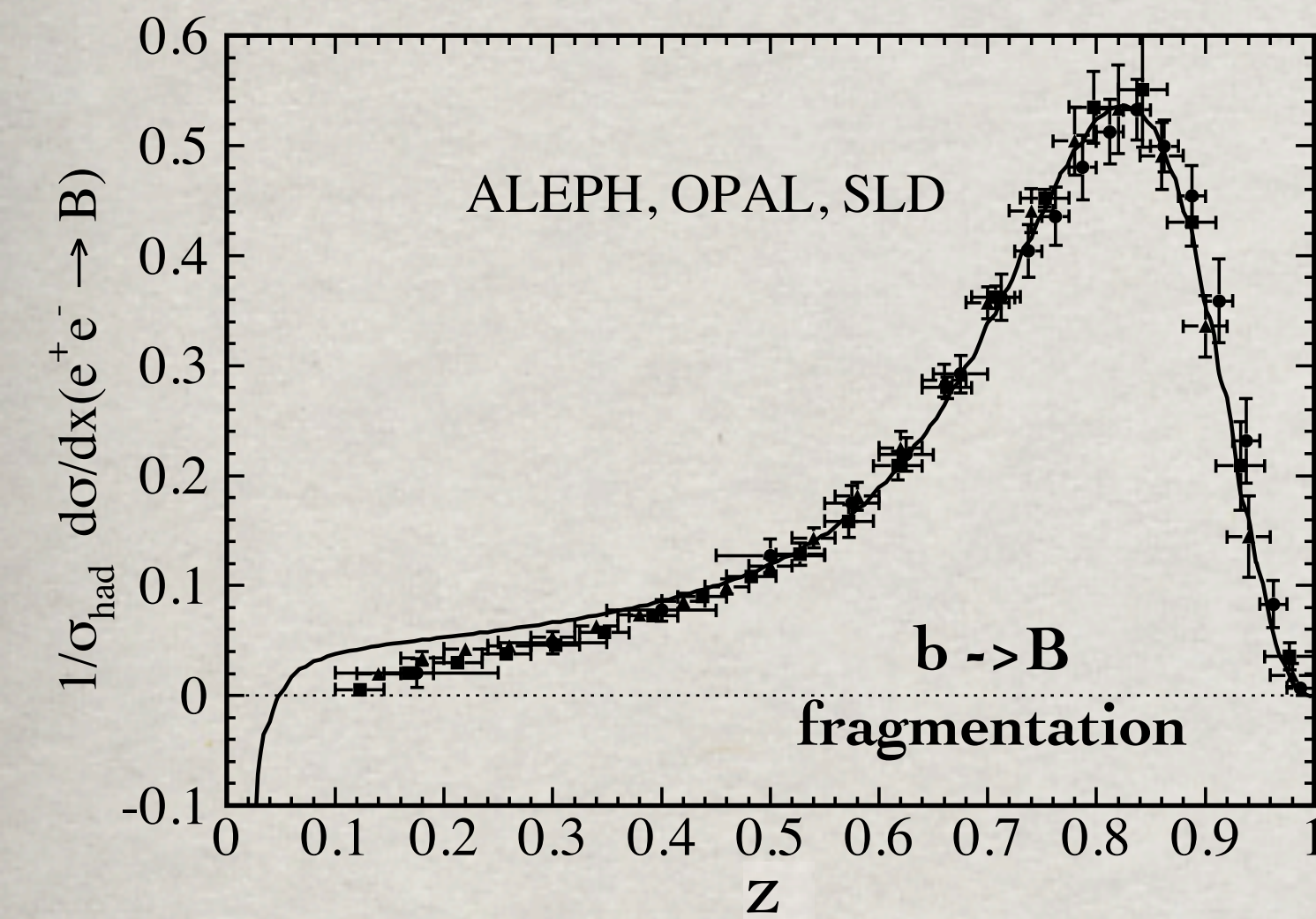
$p_T$  of the jet plays roles of the jet momentum and scale simultaneously.



I.Potashnikova, I.Schmidt & B.K.  
PRC 82(2010)037901

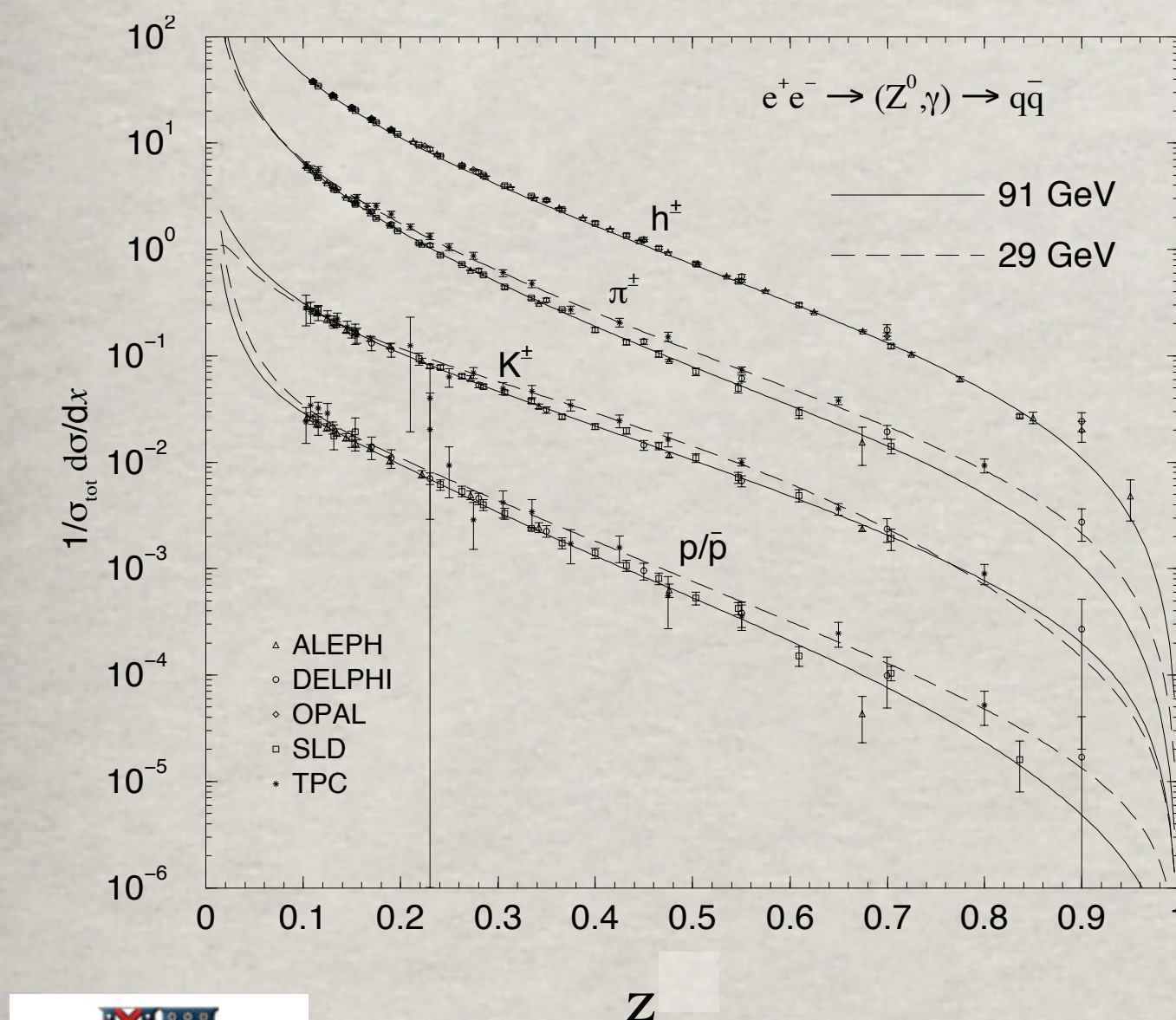
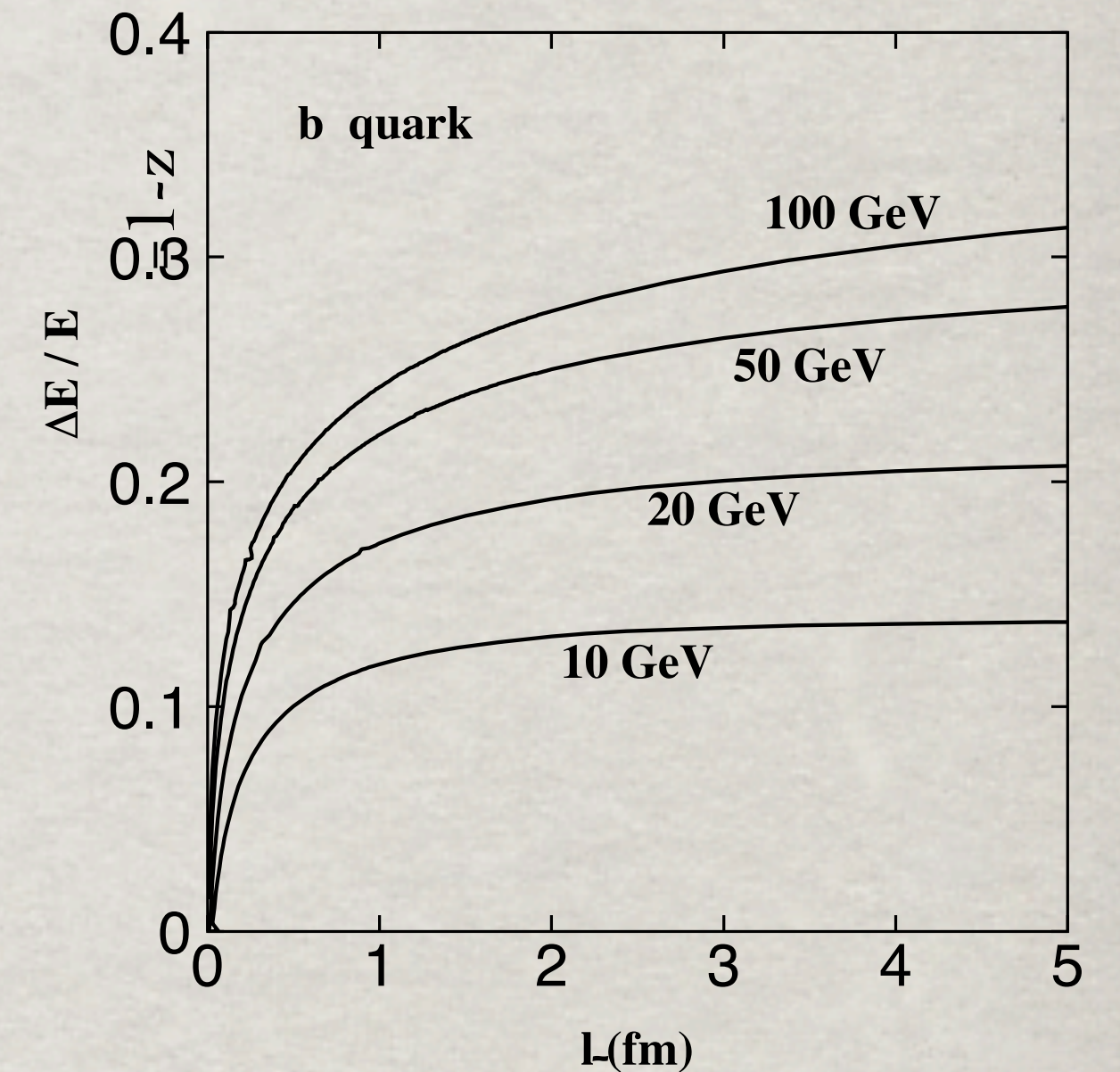


# Fragmentation function of heavy quarks



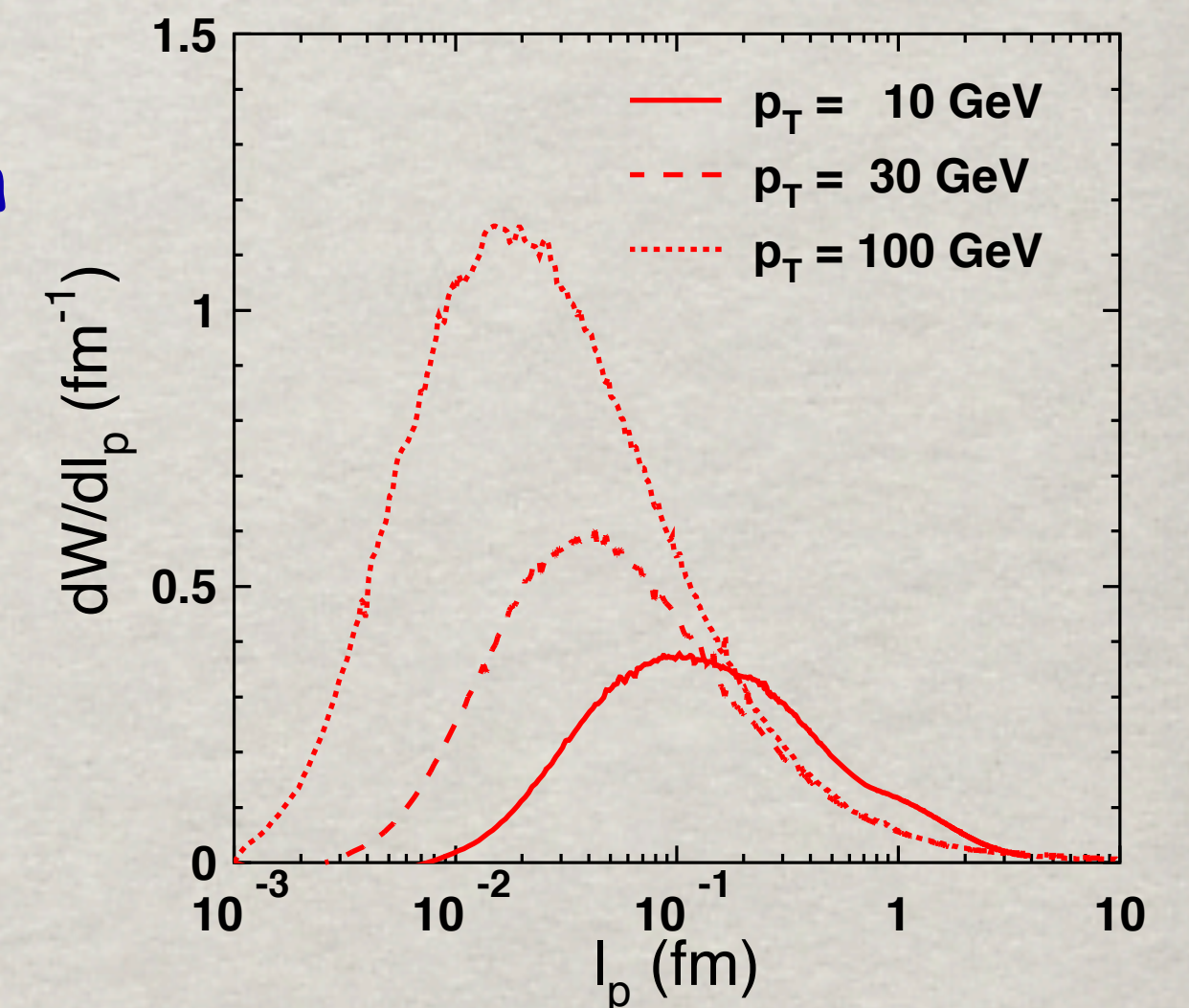
This is why large  $z$  are enhanced in the fragmentation function of heavy flavors,  $b \rightarrow B$ ,  $c \rightarrow D$ .

On the contrary, large  $z$  fragmentation of light quarks is strongly suppressed.



As far as we are able to calculate  $\Delta z(L)$ , we can extract the production length  $l_p$  of B-mesons directly from data for  $D_{b/B}(z)$

Remarkably, the mean value of  $l_p$  shrinks with rising  $p_T$





# Attenuation in a hot medium

The light quarks in the B-meson carries a tiny fraction of the momentum,

$$x \sim m_q/m_b \approx 5\%$$

Therefore, even if the produced b-q dipole has a small transverse separation, its size expands with a high speed, enhanced by  $1/x$ . The formation time of the B-meson wave function (in the medium rest frame) is very short,

$$t_f^B = \frac{\sqrt{p_T^2 + m_B^2}}{2m_B\omega} \quad (\omega=300\text{MeV})$$

The mean free path of such a meson in a hot medium is very short

$$\lambda_B \sim \frac{1}{\hat{q} \langle r_T^2 \rangle}, \quad \text{where} \quad \langle r_T^2 \rangle = \frac{8}{3} \langle r_{ch}^2 \rangle$$

B meson is nearly as big as a pion,  $\langle r_{ch}^2 \rangle_B = 0.378 \text{ fm}^2$  [Ch.-W. Hwang (2001)]

E.g. at  $\hat{q} = 1 \text{ GeV}^2/\text{fm}$   $\lambda_B = 0.04 \text{ fm}$ , i.e. the b-quark propagates through the hot medium, picking up and losing light quarks. Meanwhile the b-quark keeps losing energy with a rate, enhanced by medium-induced effects. Eventually the detected B-meson is formed and survives in the dilute medium at the surface.



# Where the nuclear suppression comes from?

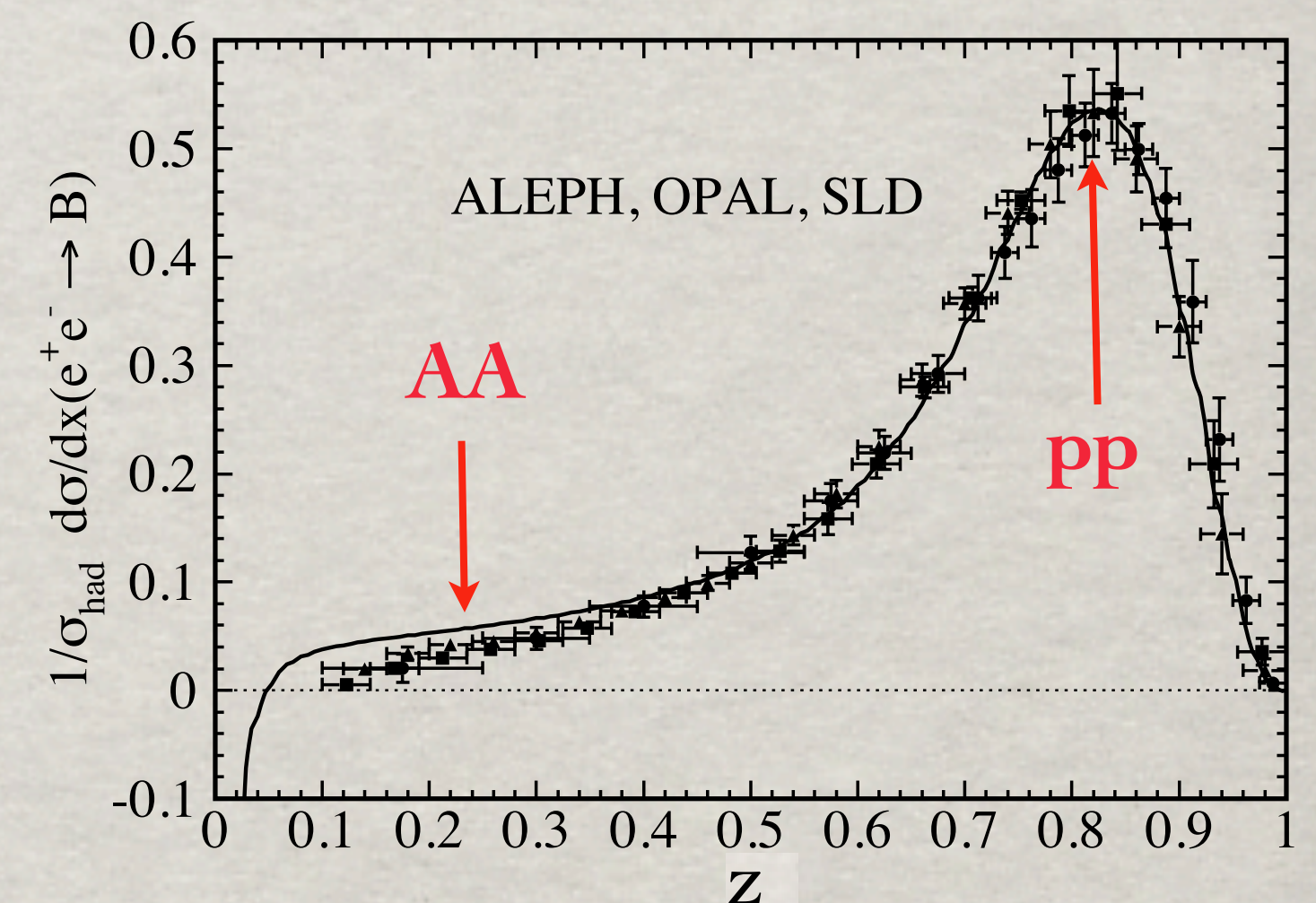
A high- $p_T$   $b$ -quark, produced in  $pp$  collisions, starts radiating so intensely, that loses 20-30% of its initial energy on a very short distance, then picks-up a light antiquark. The produced colorless B-meson stops radiating and retains its fractional momentum  $z$ .

If, however, the  $b$ -quark is produced in a dense environment, it has to propagate a long distance up to the medium surface, where the final B-meson can survive. All this long path the quark keeps losing energy and eventually produces a B-meson with reduced fractional momentum  $z$ , which is suppressed by the fragmentation function.

$$\frac{d\sigma(pp \rightarrow BX)}{d^2p_T} = \int d^2p_T^b \frac{d\sigma(pp \rightarrow bX)}{d^2p_+^b} \frac{1}{z} D_{b/B}(z),$$

$$\frac{d\sigma(AA \rightarrow BX)}{d^2p_T} = \int d^2p_T^b \frac{d\sigma(pp \rightarrow bX)}{d^2p_T^b} \frac{1}{z_{AA}} D_{b/B}(z_{AA}) S(l_p^{AA})$$

$$S(l_p^{AA}) = \exp \left[ - \int_{l_p^{AA}}^{\infty} \frac{dl}{\lambda_B(l)} \right]$$





# Attenuation of a B-meson in a hot medium

## Path-integral description

The survival probability of a  $q\bar{q}$  dipole in a medium

$$S(l_1, l_2) \propto \left| \int_0^1 d\alpha \int d^2r_1 d^2r_2 \Psi_M^\dagger(r_2, \alpha) G_{Q\bar{q}}(l_1, r_1; l_2, r_2) \Psi_{in}(r_1, \alpha) \right|^2$$

The Green function describing propagation of the dipole between coordinates  $l_1, l_2$  with initial and final separations  $r_1, r_2$  satisfies the 2-dimensional LC equation

$$i \frac{d}{dl_2} G_{Q\bar{q}}(l_1, \tilde{r}_1; l_2, \tilde{r}_2) = \left[ -\frac{\Delta_{r_2}}{2 p_T \alpha (1 - \alpha)} + V_{Q\bar{q}}(l_2, \tilde{r}_2) \right] G_{Q\bar{q}}(l_1, \tilde{r}_1; l_2, \tilde{r}_2)$$

The imaginary part of the LC potential is responsible for absorption,

$$\text{Im } V_{Q\bar{q}}(l, \tilde{r}) = -\frac{1}{4} \hat{q}(l) r^2$$

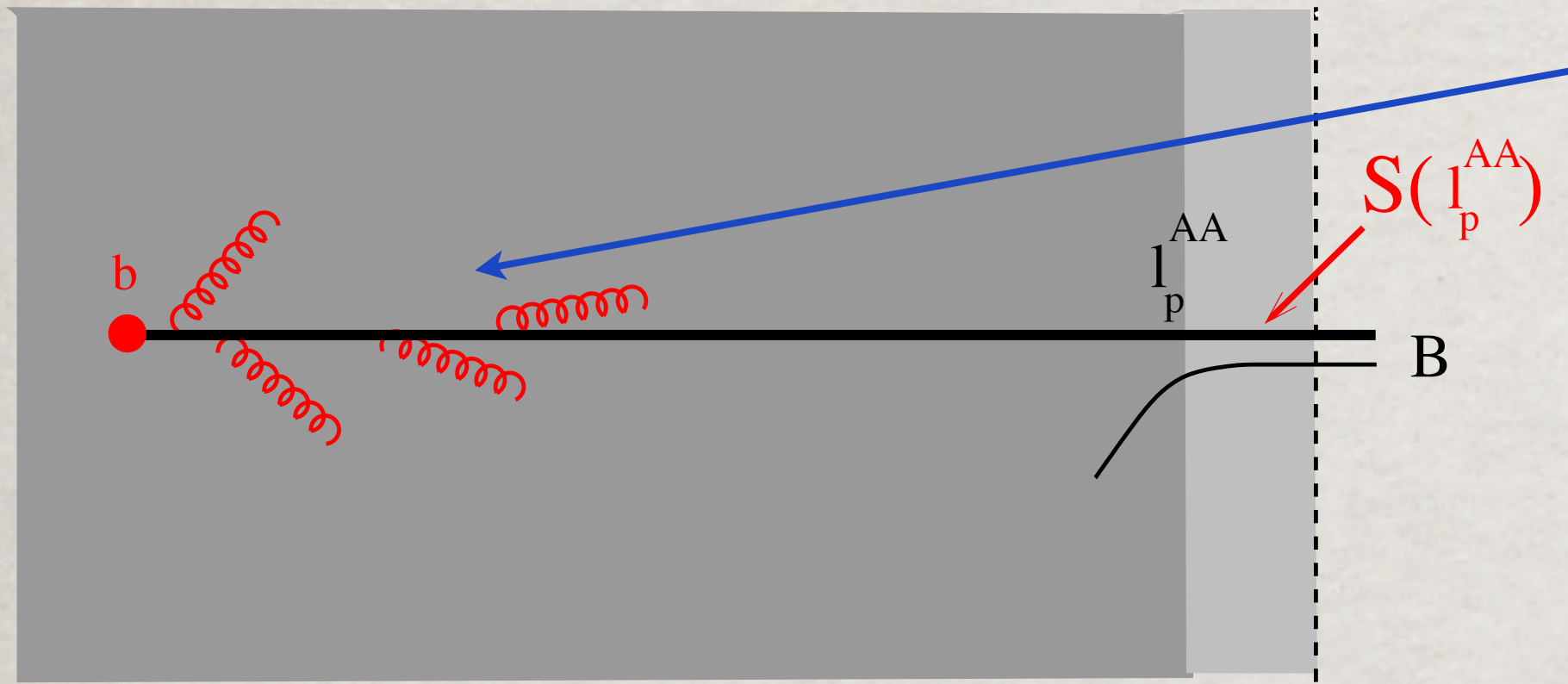
The real part is a phenomenological Cornell-type potential, adjusted to reproduce the masses and decay constants for B and D mesons.

Mao-Zhi Yang (2011); Ch.-W. Hwang (2002)





# Interplay between energy loss & absorption



Energy loss in the medium: radiational vacuum and induced, collisional, string.

In vacuum: gluon radiation plus string

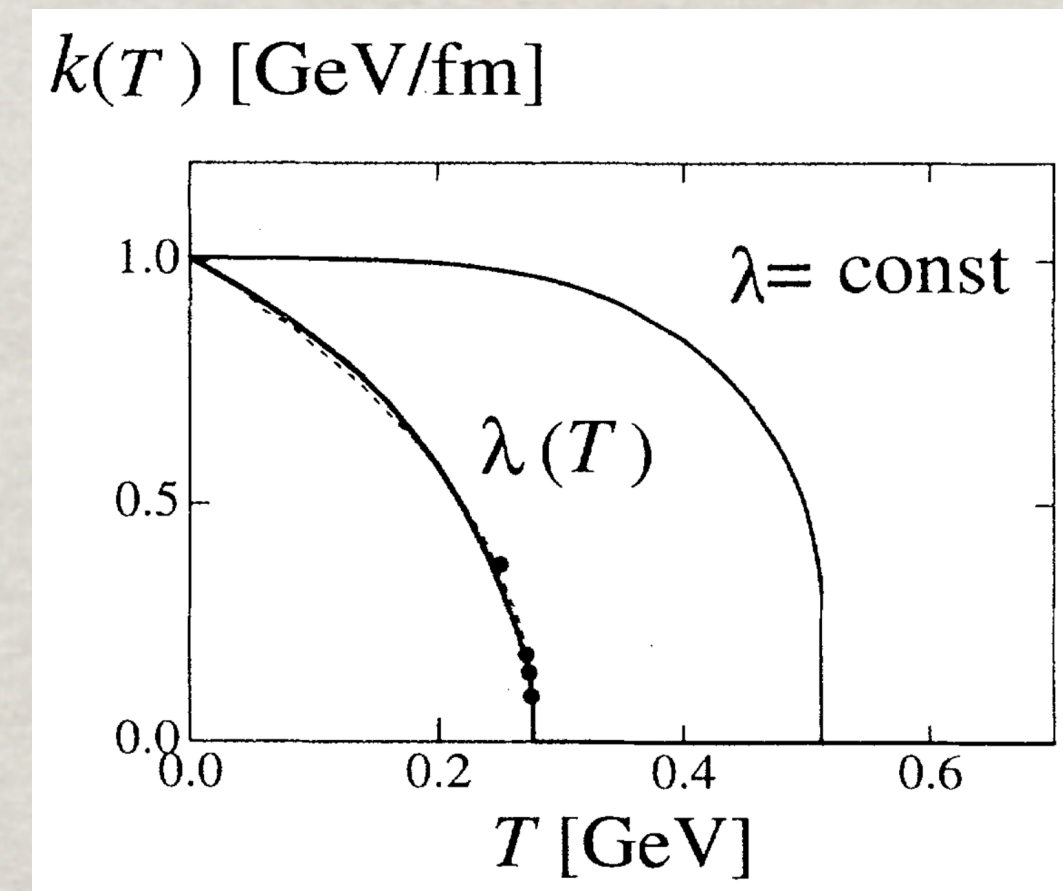
$$dE_{\text{string}}/dl = -\kappa \approx -1 \text{ GeV/fm}$$

String tension is falling with temperature:

$$\kappa(T) = \kappa (1 - T/T_c)^{1/3}$$

While in vacuum a B-meson is produced on a very short length  $l_p \ll 1 \text{ fm}$ , in a hot medium strong absorption pushes the production point to the dilute medium surface. However, energy loss on a longer  $l_p^{AA} \gg l_p$  causes a large shift down to small  $z$ , suppressed by  $D(z)$ .

Thus, the two sources of suppression are in conflict, leaving no good solution.



H.Ichie, H.Suganuma & H.Toki(1996)



# Results

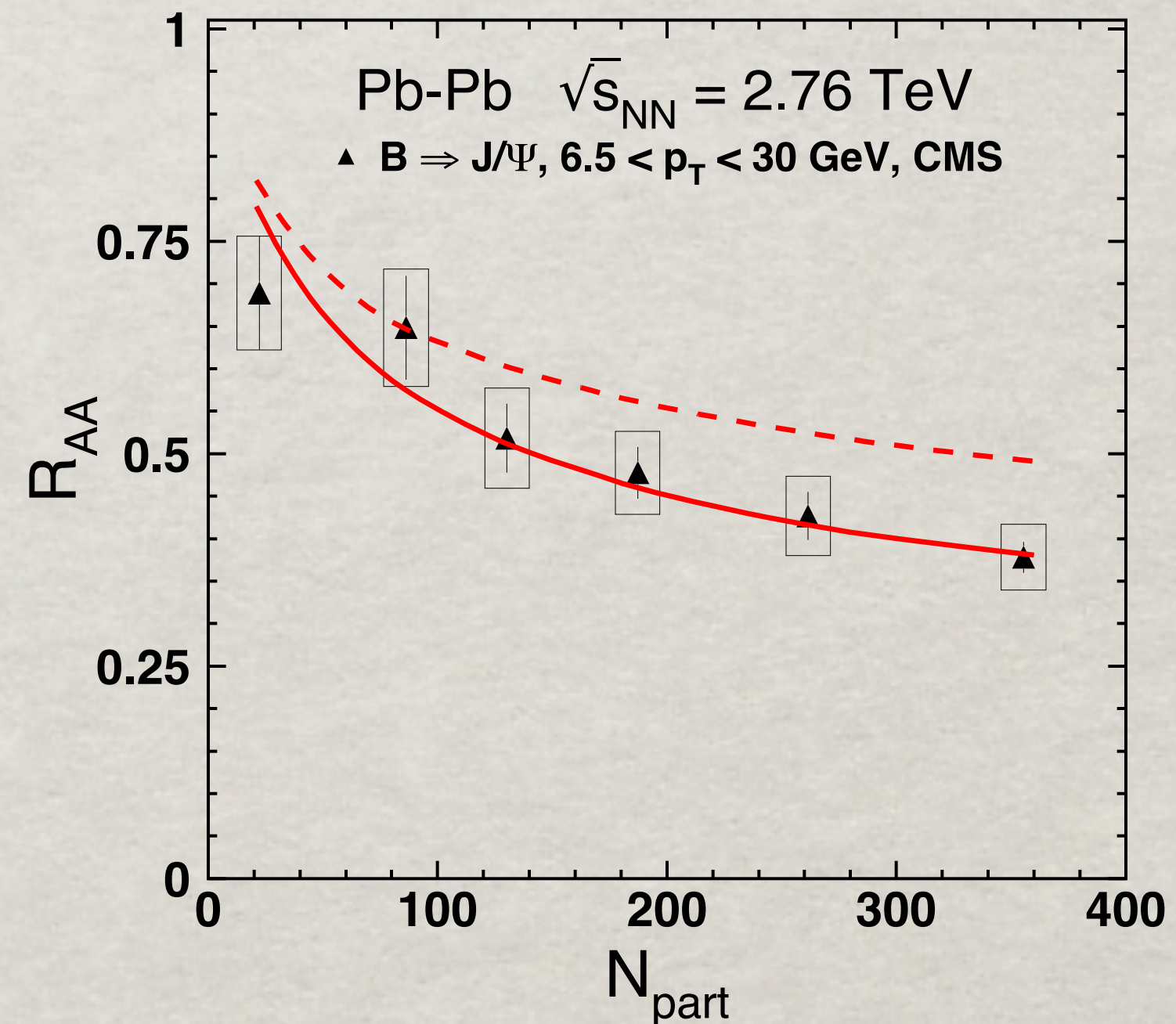
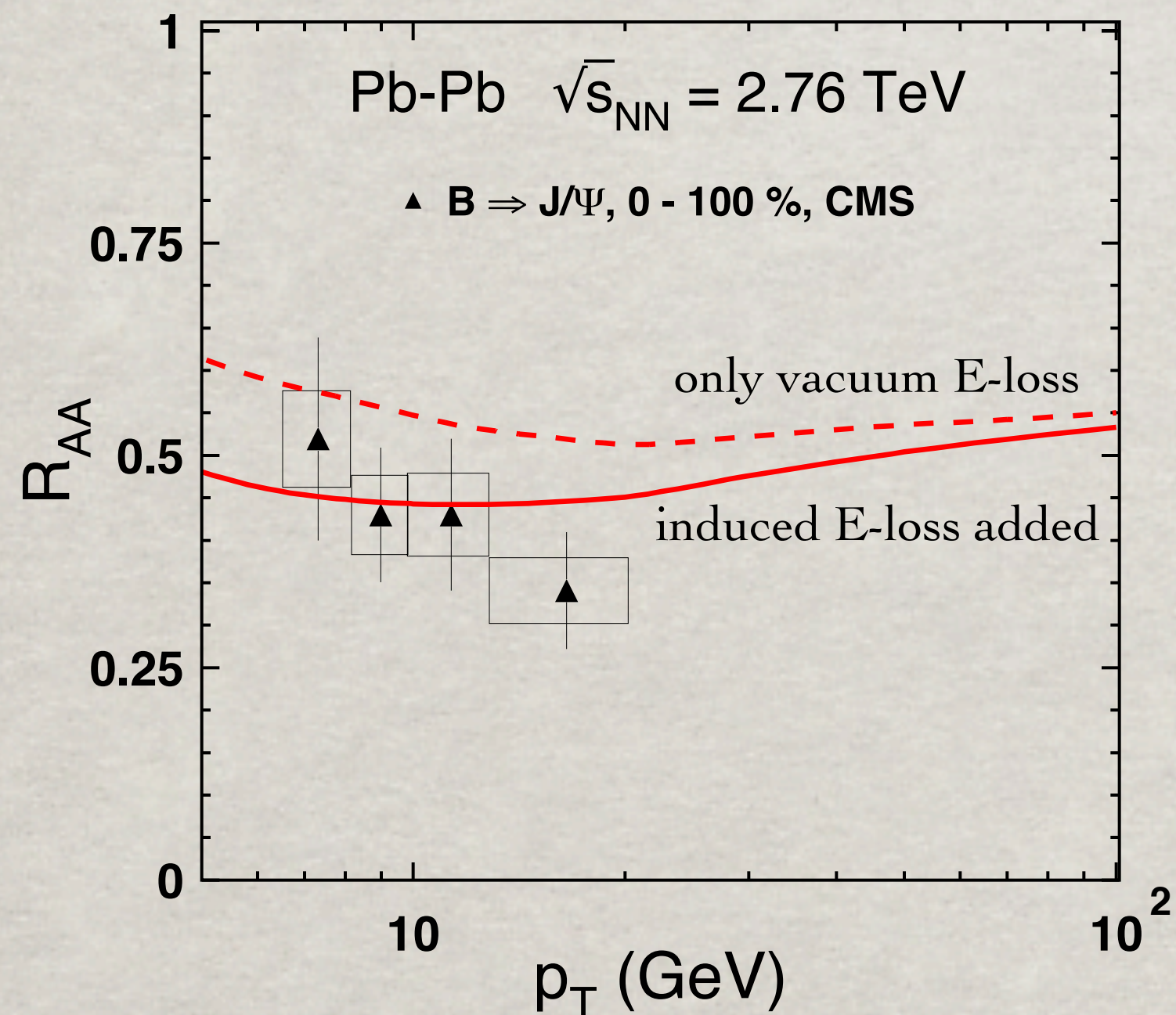
$$\hat{q}(l, \tilde{b}, \tilde{\tau}) = \frac{\hat{q}_0 l_0}{l} \frac{n_{\text{part}}(\tilde{b}, \tilde{\tau})}{n_{\text{part}}(0, 0)} \Theta(1 - l_0),$$

$$q_0 = 2 \text{ GeV}^2/\text{fm} \\ (1.6 \text{ GeV}^2/\text{fm})$$

fixed by quenching of pions  
at LHC (RHIC)

J.Nemchik, I.Potashnikova, I.Schmidt & B.K.  
PRC 86(2012)054904

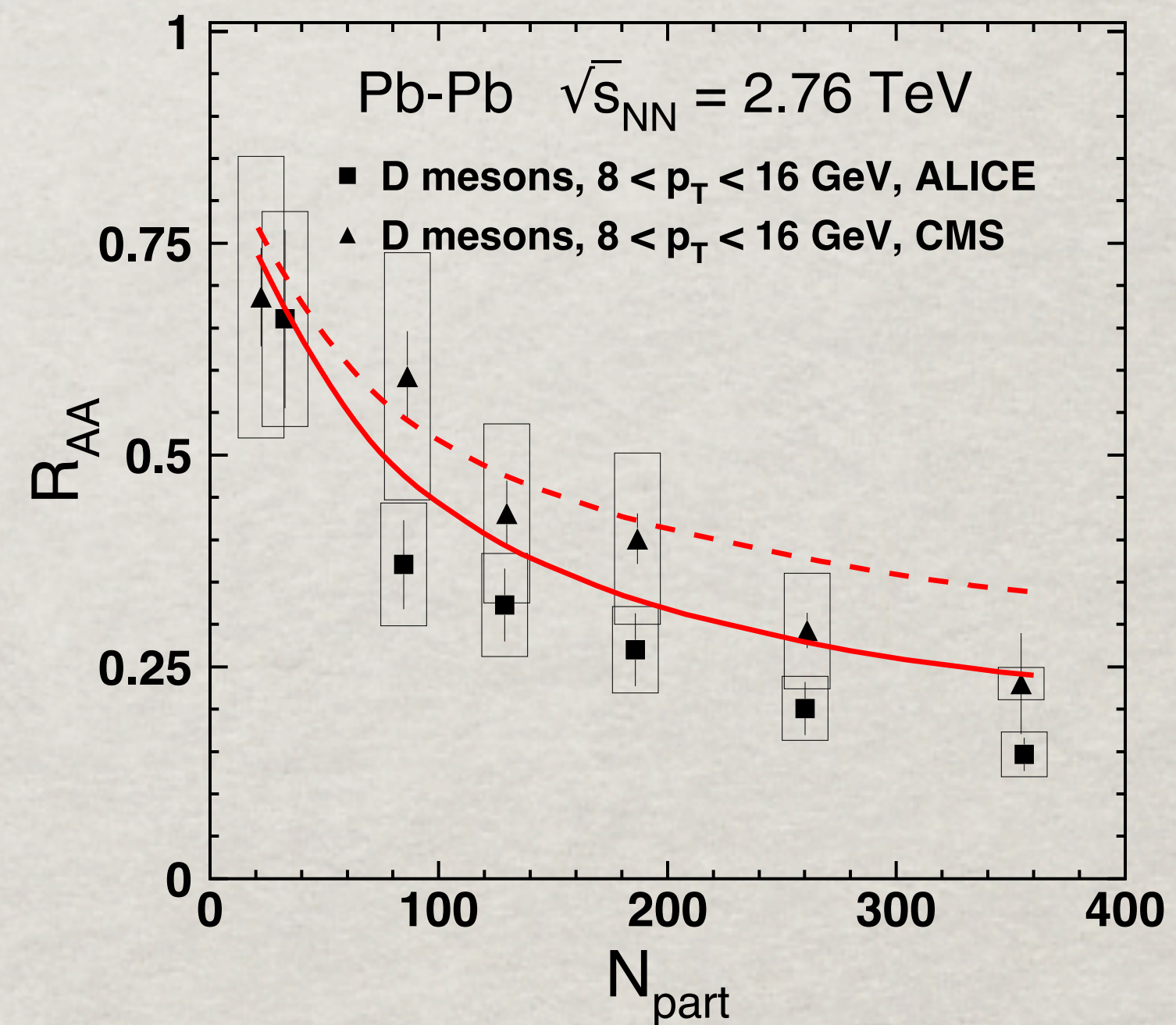
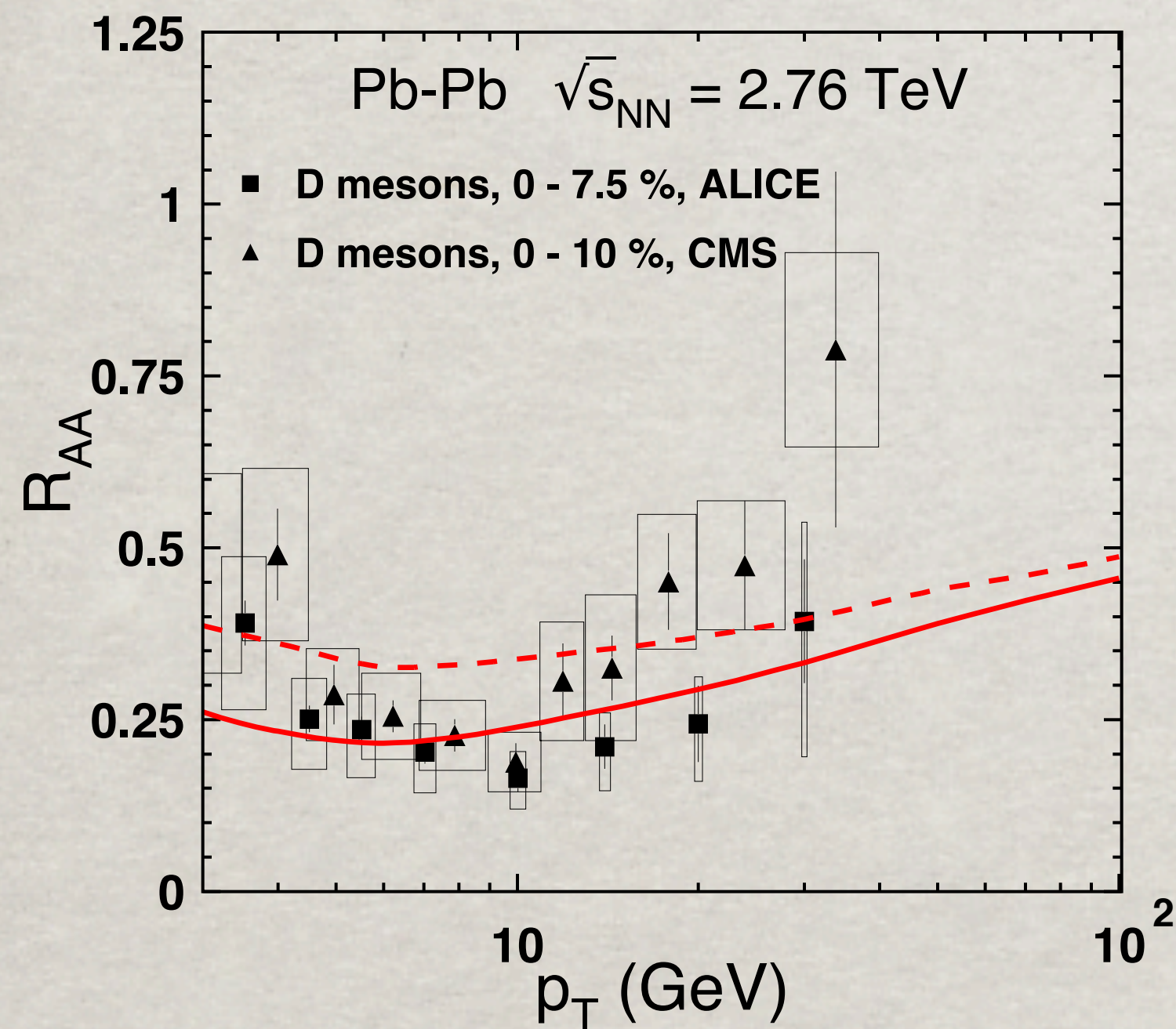
Different sources of time-dependent energy loss should be added up. Medium-induced energy loss is much smaller than the vacuum one, and should not produce a dramatic effect. They are particularly small for heavy flavors (Yu.Dokshitzer & D.Kharzeev (2001))





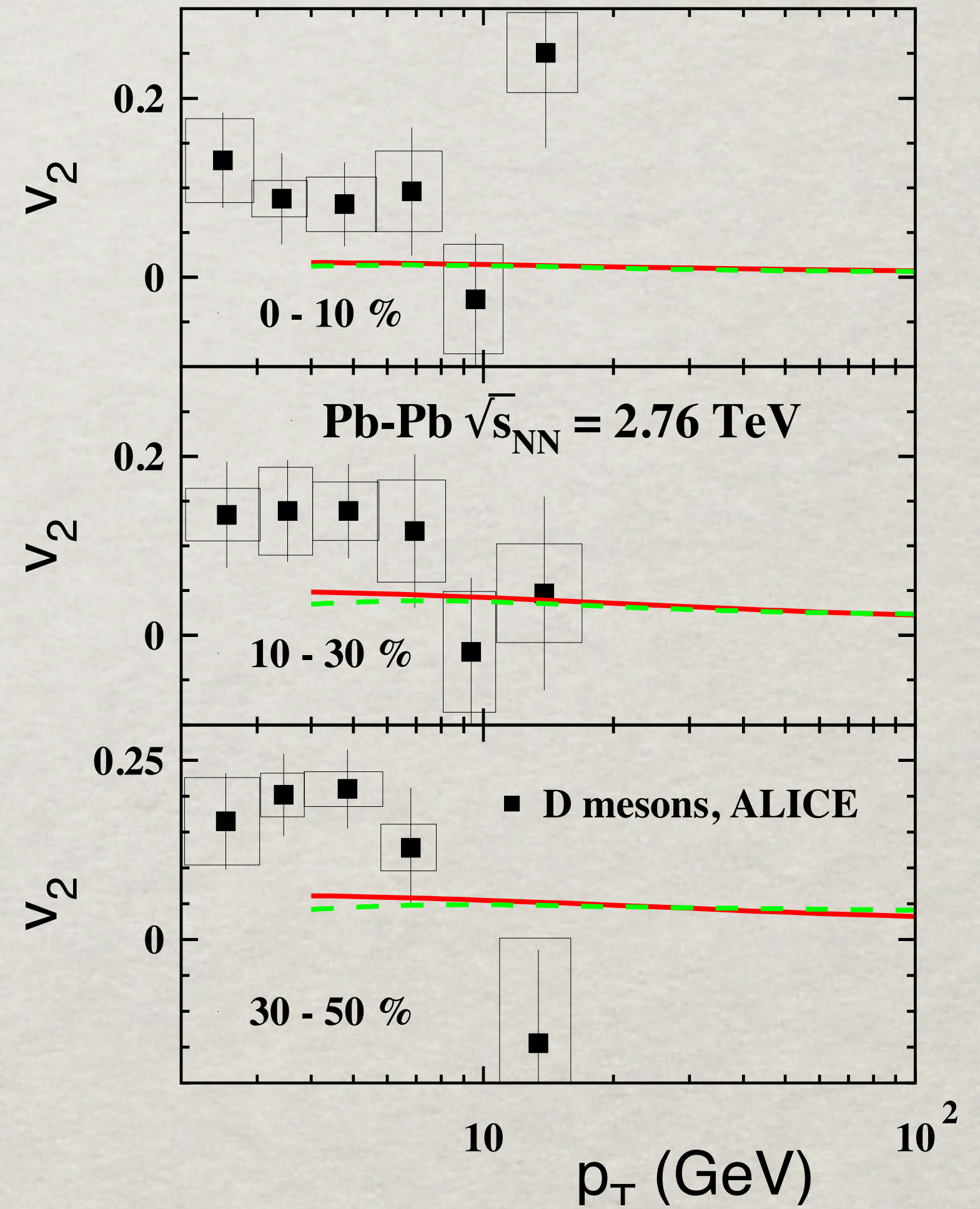
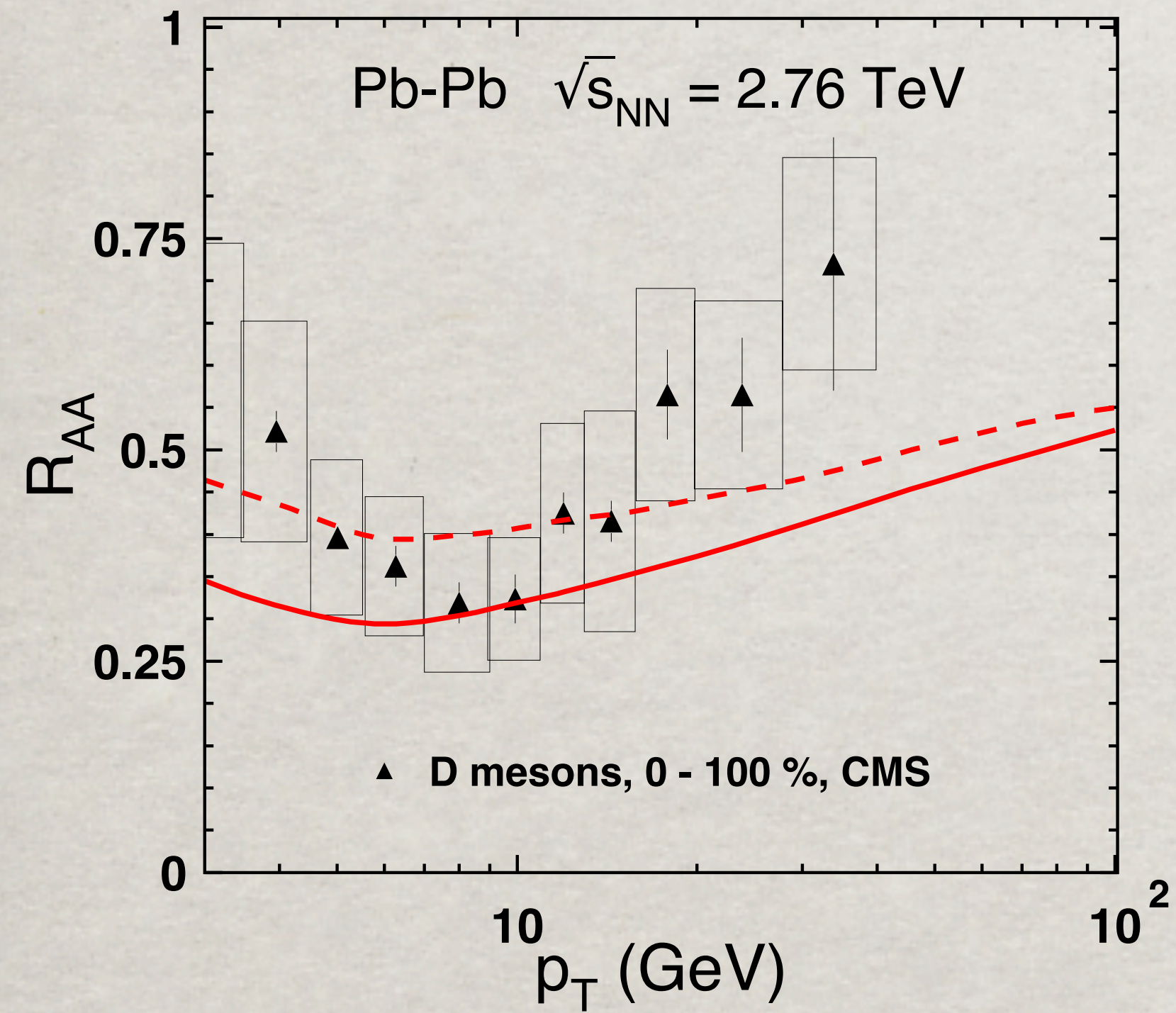
# Results

c-quarks radiate in vacuum much more energy than b-quarks, while the effects of absorption of c-q and b-q dipoles in the medium are similar. Therefore D-mesons are suppressed in AA collisions more than B-mesons.





# Results



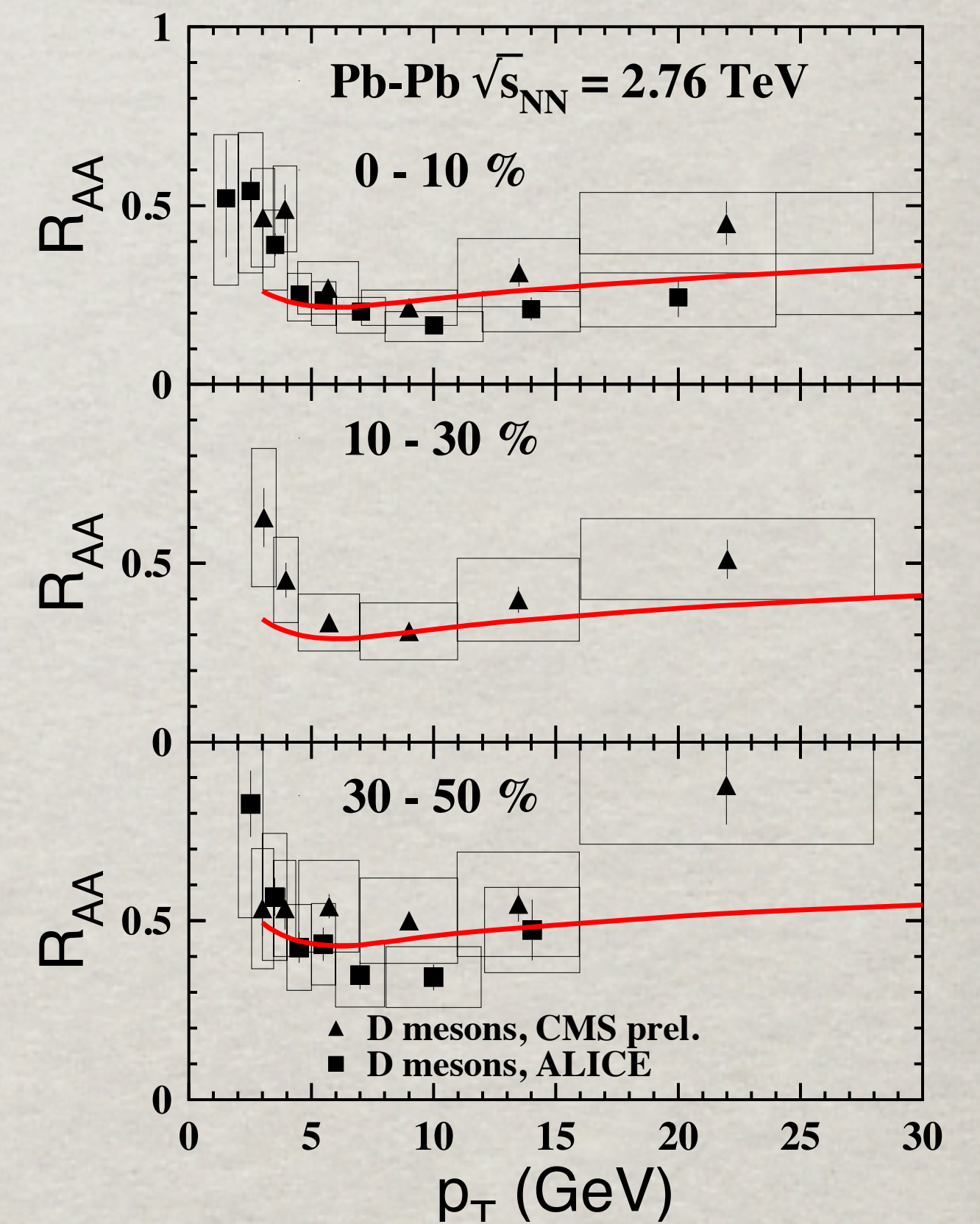
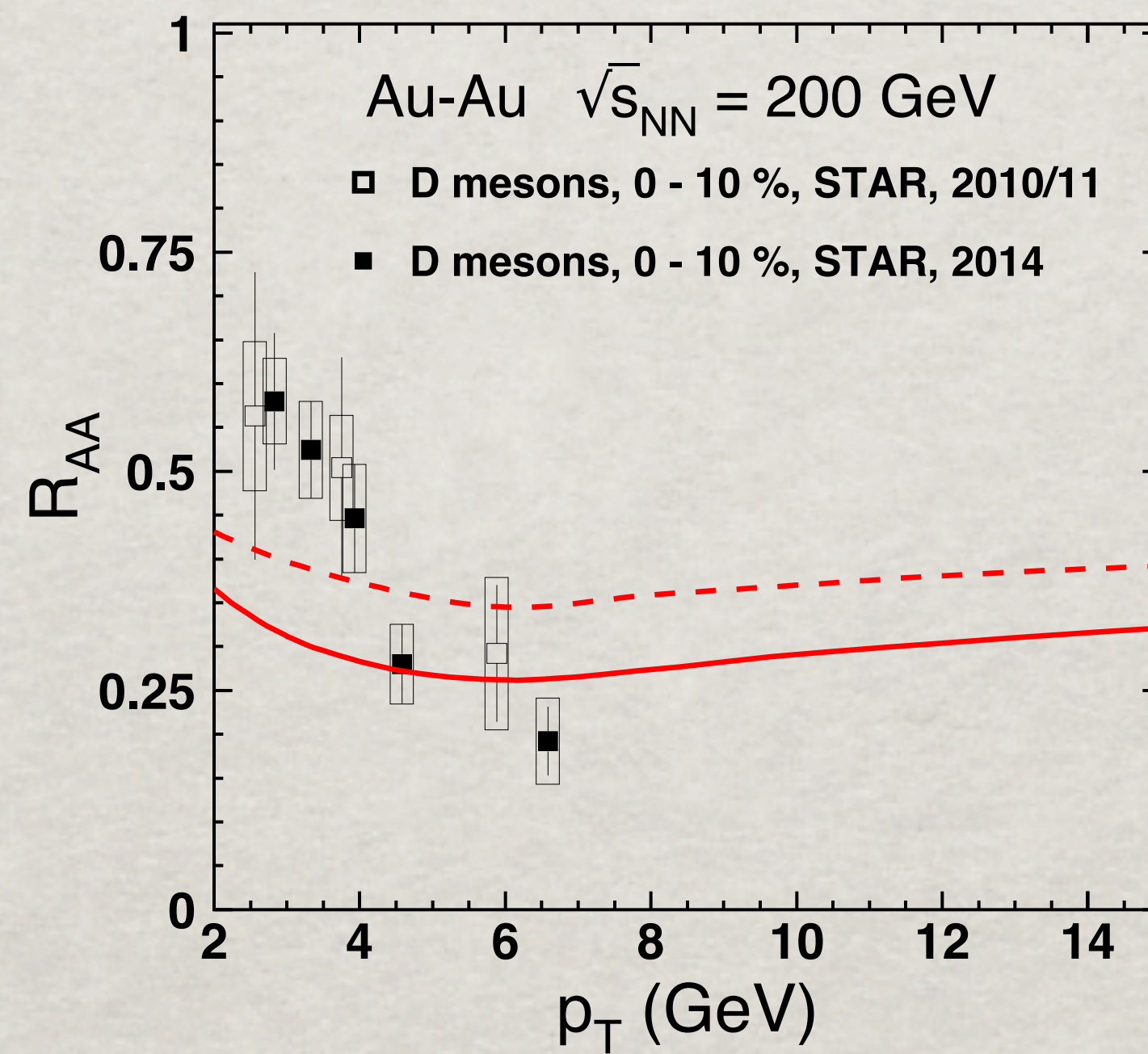
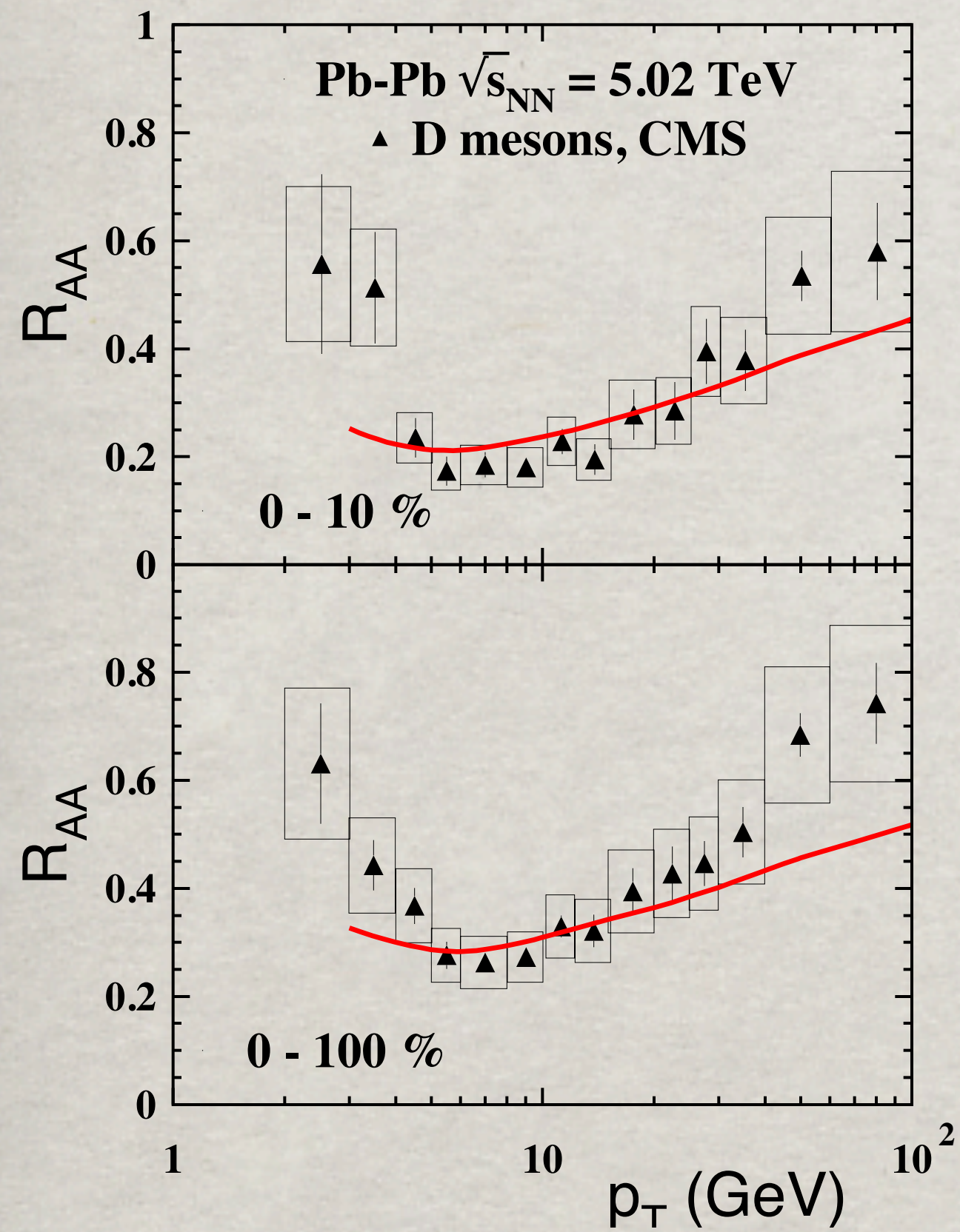


# Summary

Fragmentation of high- $p_T$  heavy quarks expose nontrivial features.

- Heavy and light quarks produced in high- $p_T$  partonic collisions radiate differently. Heavy quarks regenerate their stripped-off color field much faster than light ones and radiate a significantly smaller fraction of the initial energy.
- This peculiar feature of heavy-quark jets leads to a specific shape of the fragmentation functions. Differently from light flavors, the heavy quark fragmentation function strongly peaks at large fractional momentum  $z$ , i.e. the produced heavy-light meson, B or D, carry the main fraction of the jet momentum. This is a clear evidence of a short production time of a heavy-light mesons.
- Contrary to the propagation of a small  $q-\bar{q}$  dipole, which survives in the medium due to color transparency, a  $\bar{q}-Q$  dipole promptly expands to a large size. Such a big dipole has no chance to survive intact in a hot medium. On the other hand, a breakup of such a dipole does not suppress the production rate of  $\bar{q}-Q$  mesons, differently from light  $qq$  mesons.
- Data for production of high- $p_T$  B and D mesons are explained in a parameter-free way.



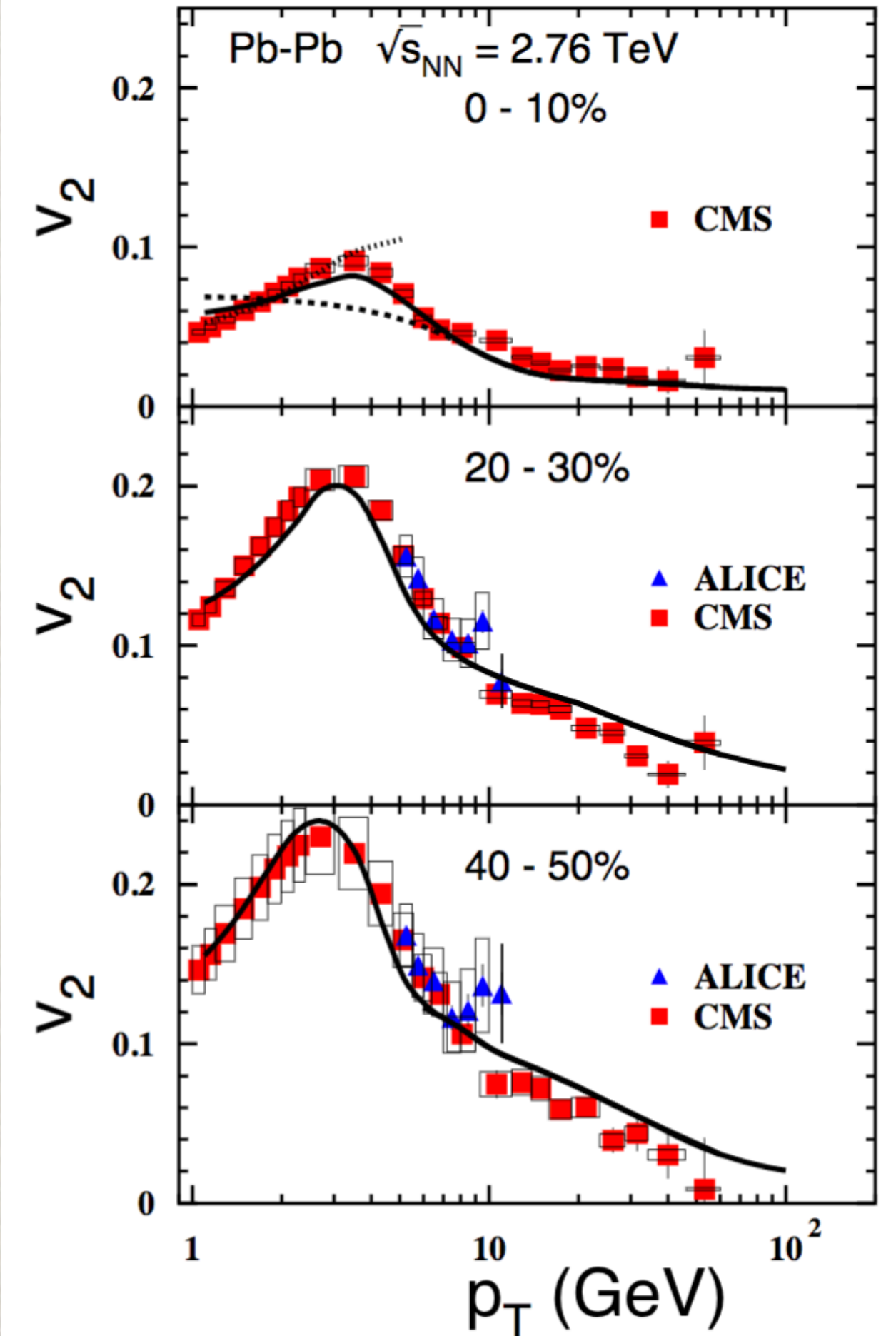
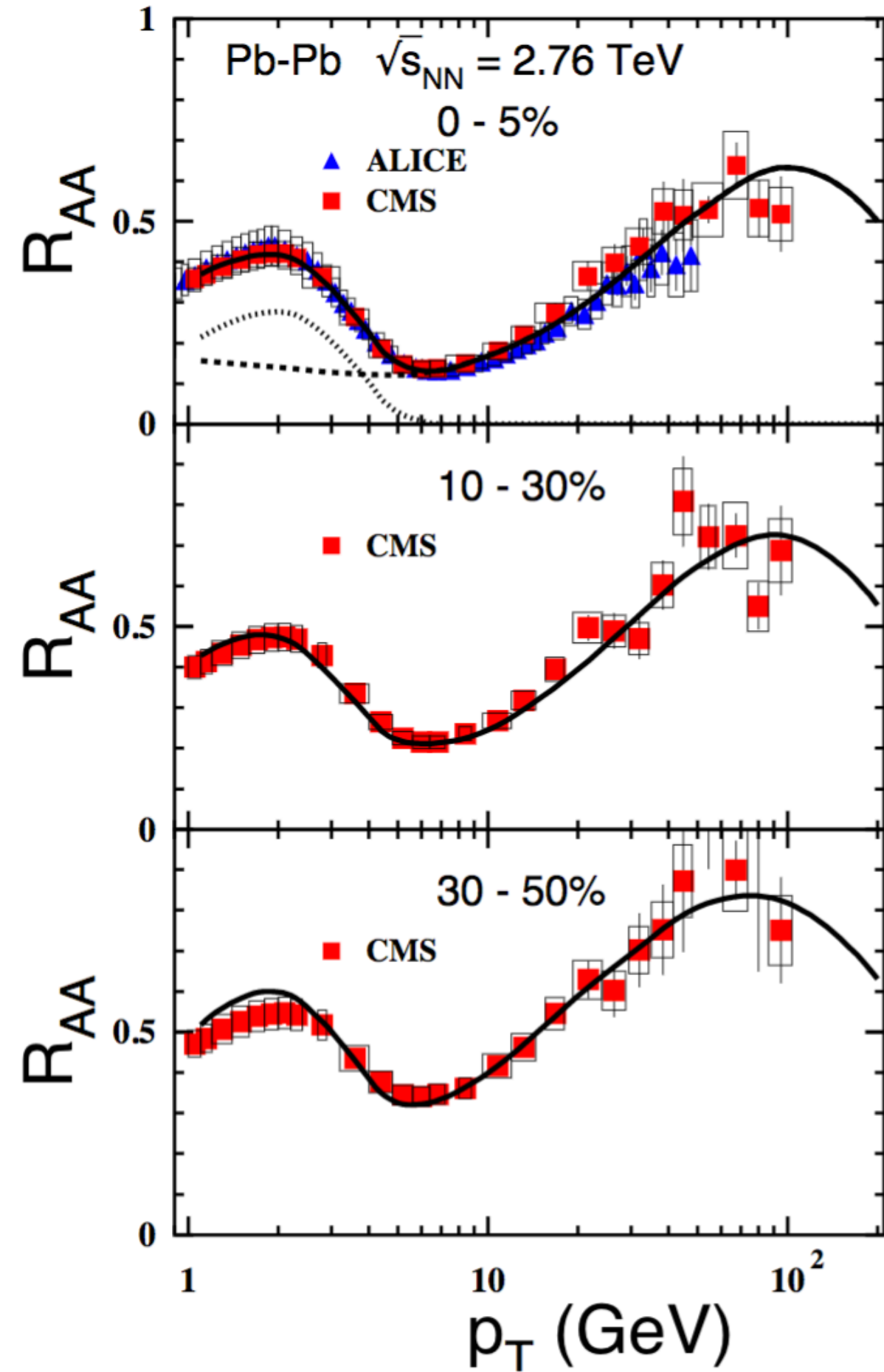




# Quenching of high- $p_T$ hadrons

## HYDRO + pQCD

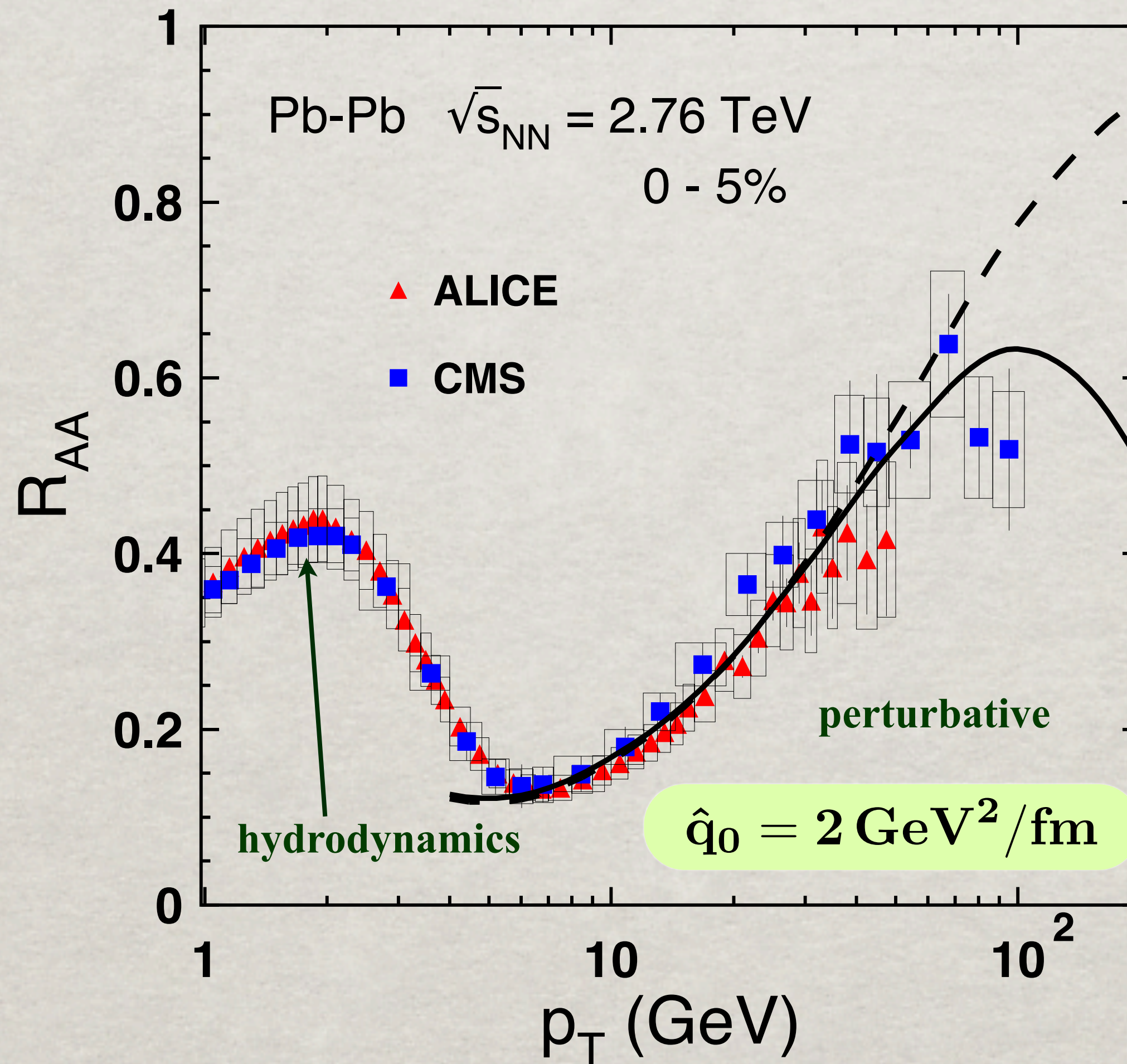
J.Nemchik, Yu.Karpenko, I.Potashnikova  
I.Schmidt, Yu.Sinyukov & B.K.  
[arXiv:1310.3455](https://arxiv.org/abs/1310.3455)





# Quenching of high- $p_T$ hadrons

BK, J.Nemchik, I.Potashnikova, I.Schmidt  
Phys.Rev. C86(2012)054904





# Quenching of high- $p_T$ hadrons

