Lessons for particle physics from gravitational waves

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based on 1605.01209 with M. McCullough & A. Urbano

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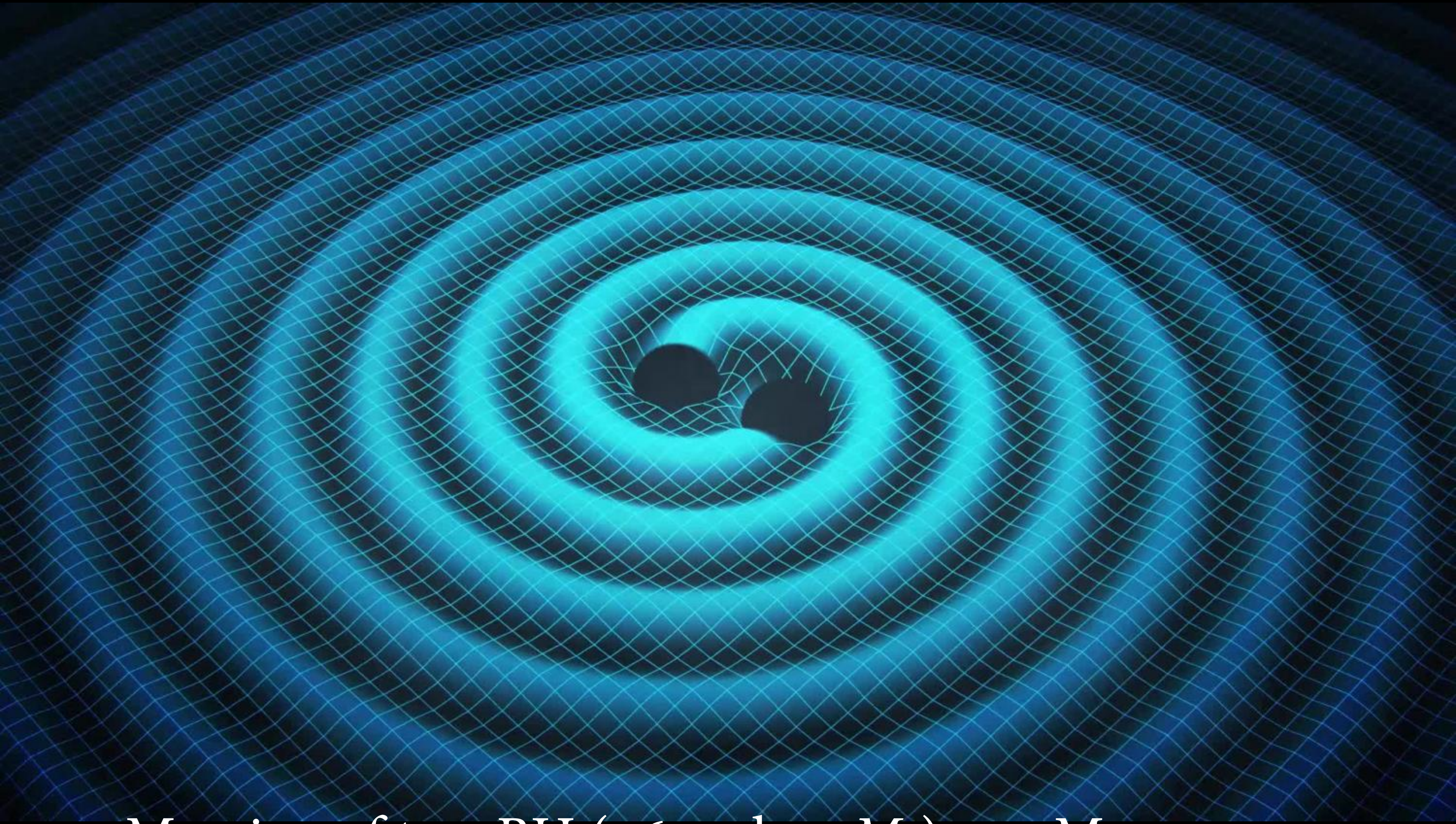
Ορθόδοξος
Ακαδημία
Κρήτης (OAK)

Dedicated to the memory of Guido Altarelli

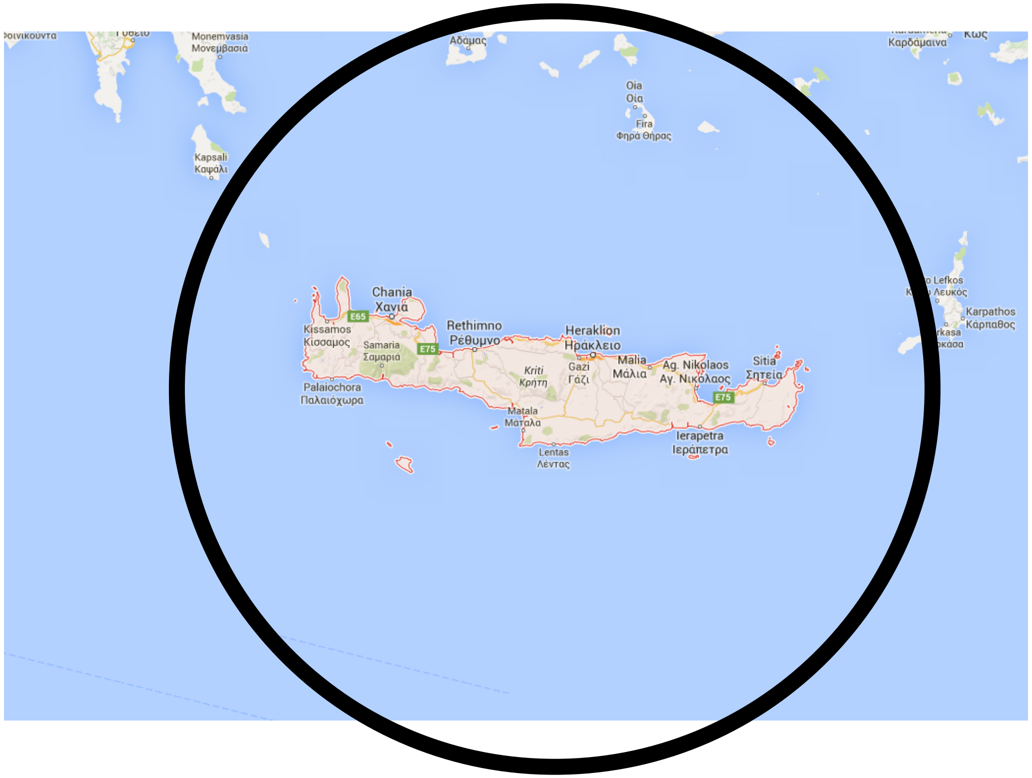
GW: science fiction come true!



Merging of two BH (36 and 29 $M_\odot$) 410 Mpc away, emitting 3 $M_\odot$ in GW

BH radius:

$$R_{BH} = \frac{2M_{BH}\,G_N}{c^2} = 106\ \text{km}\ \frac{M_{BH}}{36\,M_\oplus}$$



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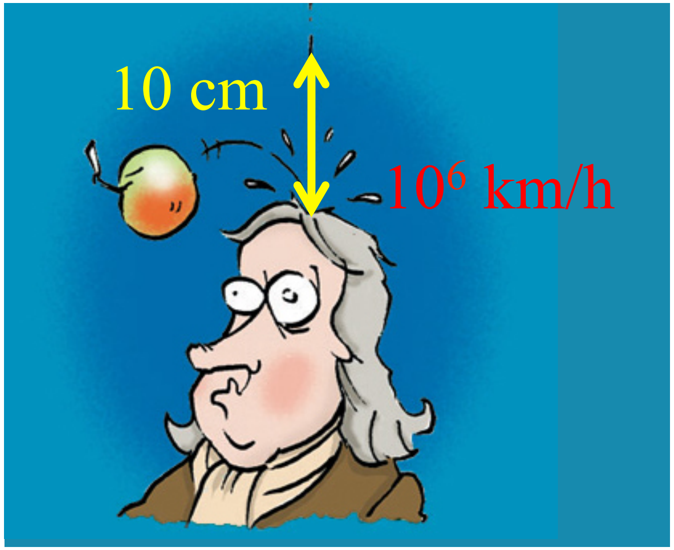
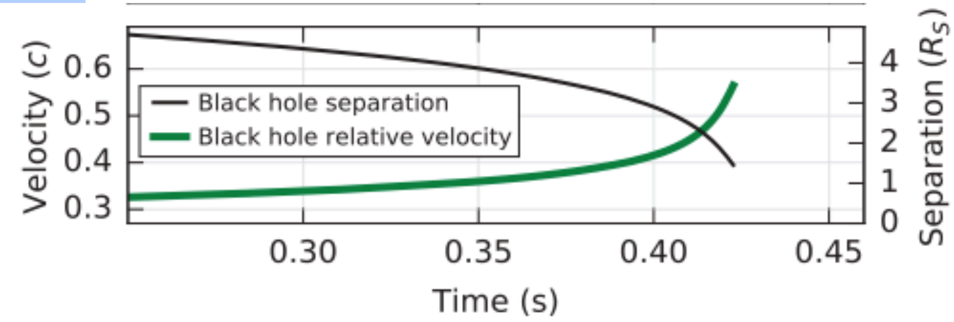
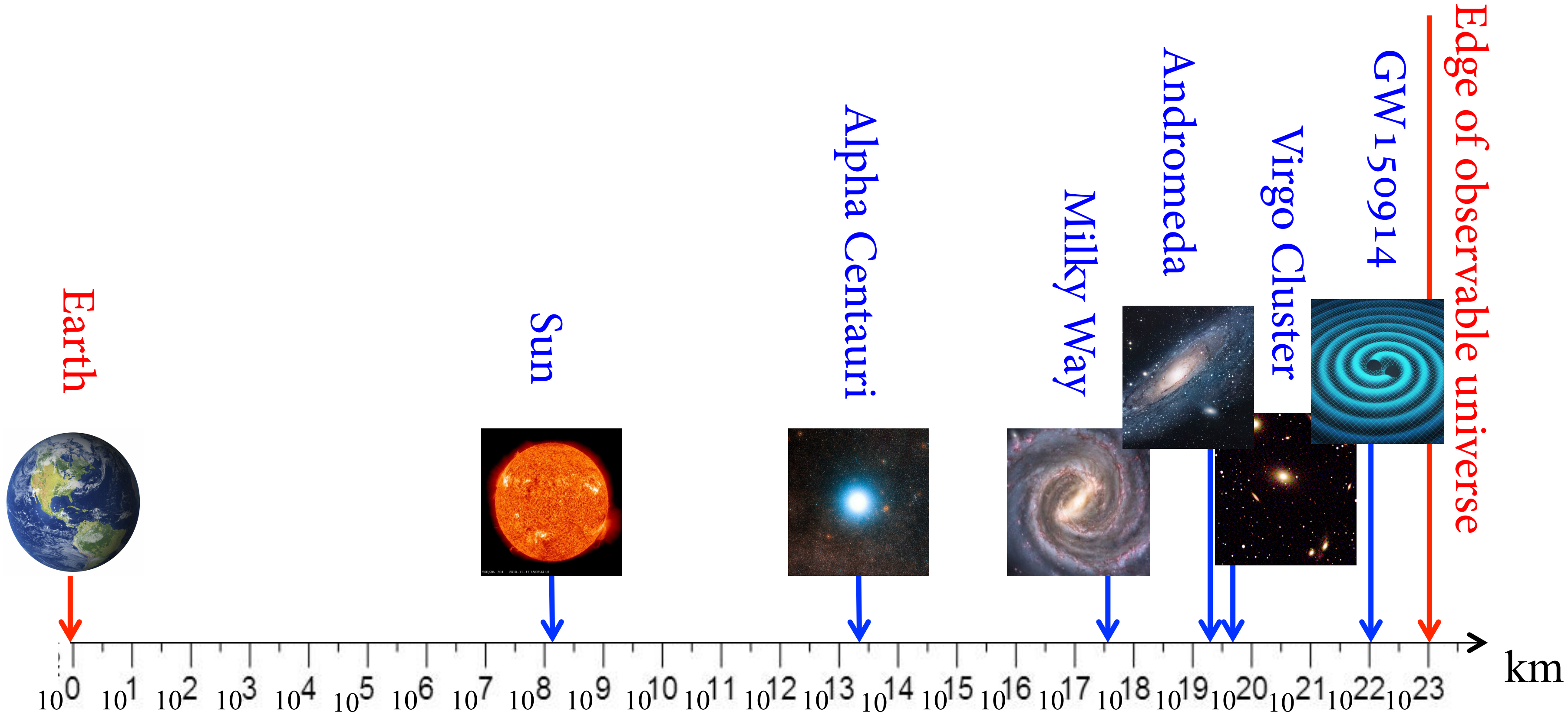
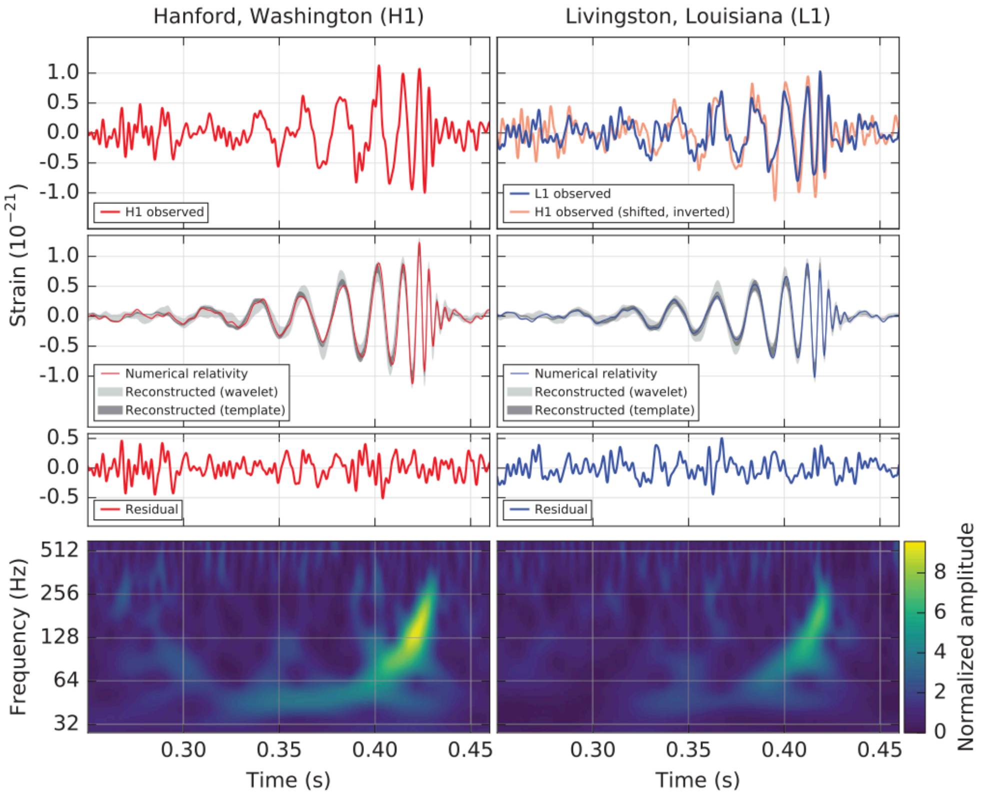


relativistic velocities!



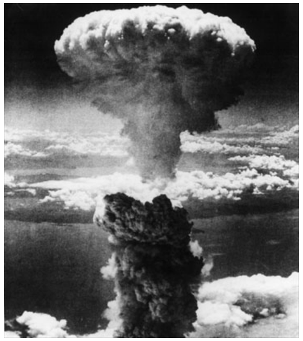

Earth
Sun
Alpha Centauri
Milky Way
Andromeda
Virgo Cluster
GW150914
Edge of observable universe
10^0 10^1 10^2 10^3 10^4 10^5 10^6 10^7 10^8 10^9 10^{10} 10^{11} 10^{12} 10^{13} 10^{14} 10^{15} 10^{16} 10^{17} 10^{18} 10^{19} 10^{20} 10^{21} 10^{22} 10^{23}
km



Energetic output

$\approx 3\ M_\odot$ in 0.1 s

$3\ M_\odot = 2\times10^{41}$ kWh $\approx 10^{34}$ Hiroshima



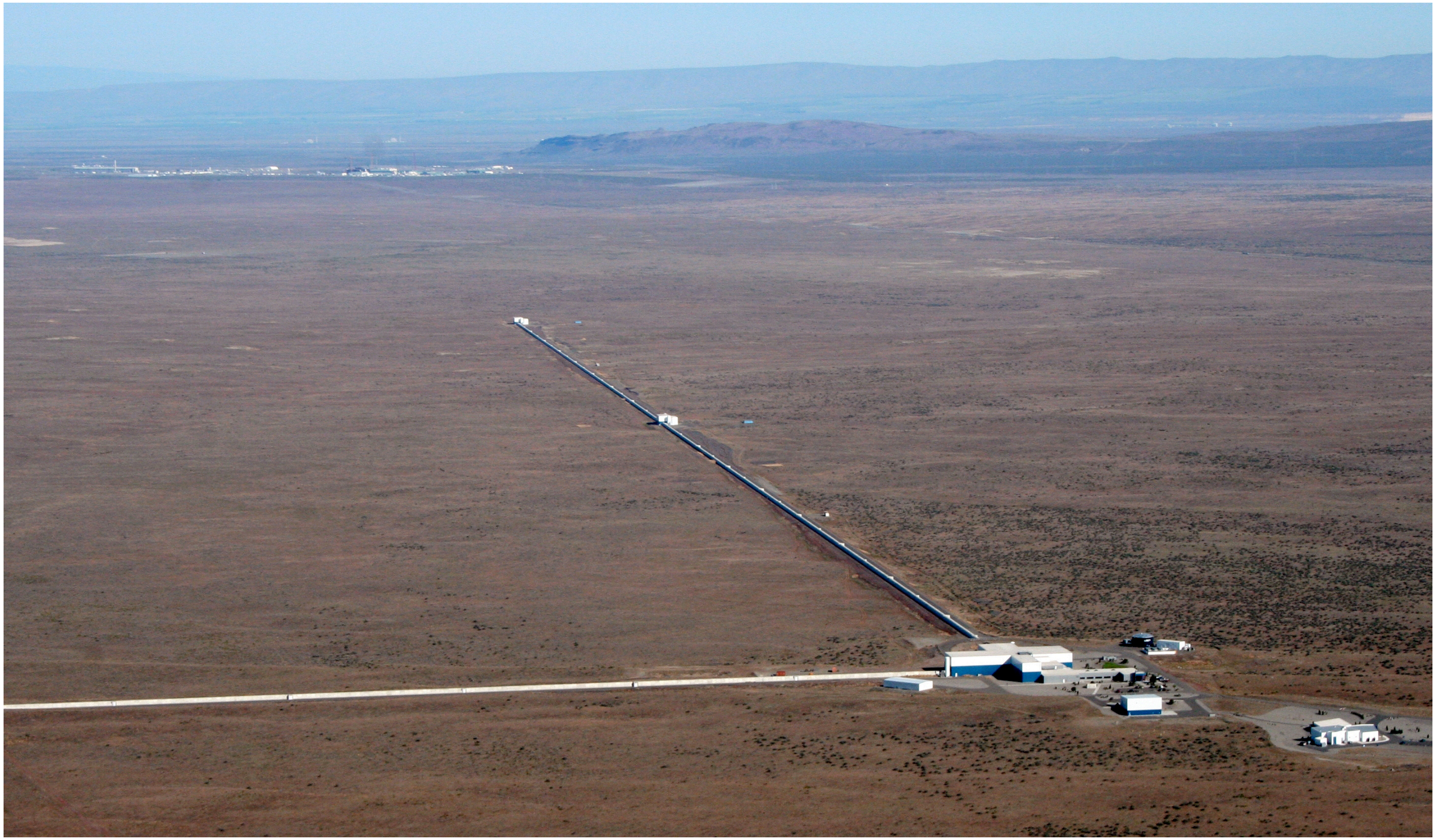
Power: $3\ M_\odot$ / 0.1 s = 10^{46} kW = $3\times10^{22}\ L_\odot$

Stars in the universe: 10^{22}-10^{24}

Flux: 5×10^{-3} W/m$^2 = 4\times10^{-6}\ F_\odot$

Strain: 10^{-21}-10^{-22} of 4 km arms

$\Rightarrow 10^{-18}$ m $\approx 10^{-3}$ proton radius



Not only a fantastic tool for astronomy, but a new testing ground for fundamental physics

Testing gravity under extreme conditions

- gravitational field is strong and rapidly changing
- curvature of spacetime is large
- dynamics of event horizons
- velocities are relativistic

GW can be used to test:

equivalence principle, modifications of gravity,
quantum structure of BH, propagation of GW, ...

Search for new physics in the form of Exotic Compact Objects (ECO)

- DM primary motivation
- New light elusive particles that can coalesce into ECOs
- GW offer unique tool for probing the existence of ECOs

Boson stars

- Supported by Heisenberg's principle

$R \sim \frac{\hbar}{m_B c}$ no gravitational collapse if $R > R_{BH} = \frac{2G_N M}{c^2} \Rightarrow$

$$M_{\max} = 0.633\ \frac{M_P^2}{m_B} \approx \left(\frac{10^{-10}\ \mathrm{eV}}{m_B}\right) M_\odot$$

- Supported by repulsive self-interaction

$$V(\phi) = m_B^2|\phi|^2 + \frac{\lambda}{2}|\phi|^4$$

$$M_{\max} = 0.06\sqrt{\lambda}\ \frac{M_P^3}{m_B^2} \approx \sqrt{\lambda}\left(\frac{100\ \mathrm{MeV}}{m_B}\right)^2 10\ M_\odot$$

- Non-topological solitons (localized solutions of EoM in presence of a conserved charge Q and with trivial asymptotic behaviour)

Fermion stars

Supported by Fermi pressure

Chandrasekhar limit $(M \lesssim M_P^3/m_F^2)$

Multi-component stars

Mixtures of exotic or ordinary/exotic matter components

Dark-matter stars

- Strongest motivation for exotic matter
- Is DM collisionless?

Problems of simulations with collisionless DM:

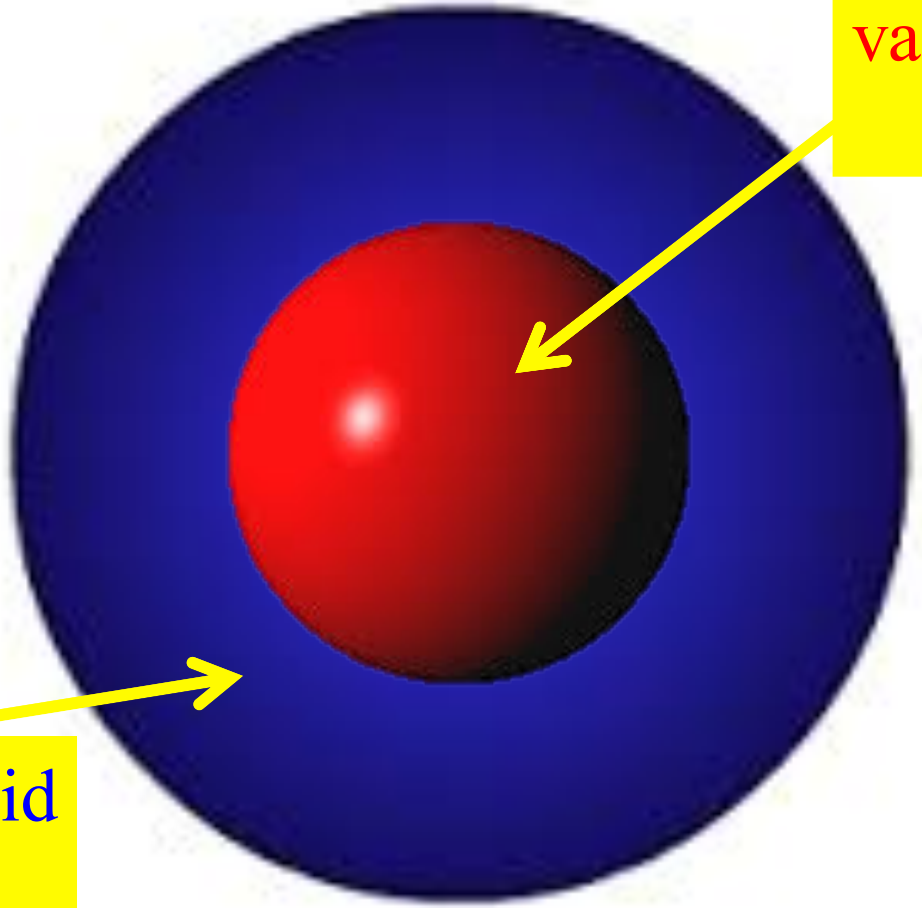
- profiles of dwarf galactic haloes too cuspy
- too many satellite galaxies
- dwarf galaxies too massive

+ indications from gravitational lensing of elliptical galaxies falling into Abell 3827 cluster

$$\Rightarrow \frac{\sigma}{m_{DM}} \approx 0.1-1 \ \frac{\mathrm{cm}^2}{\mathrm{g}}$$

ECO formation?

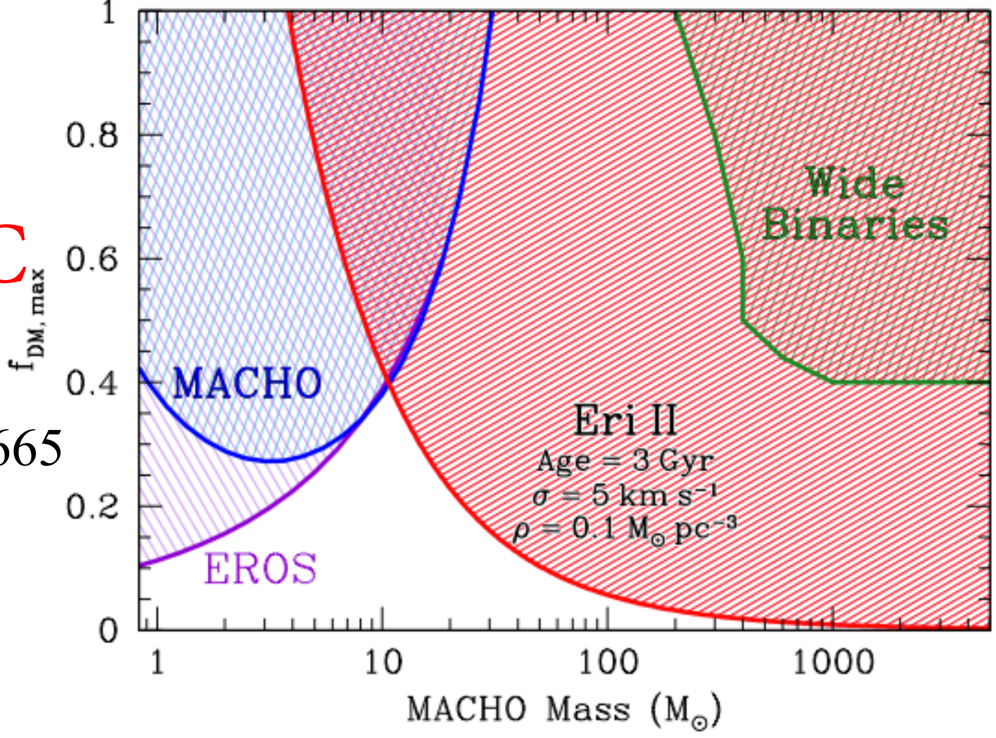
Dark-energy stars (gravastars)



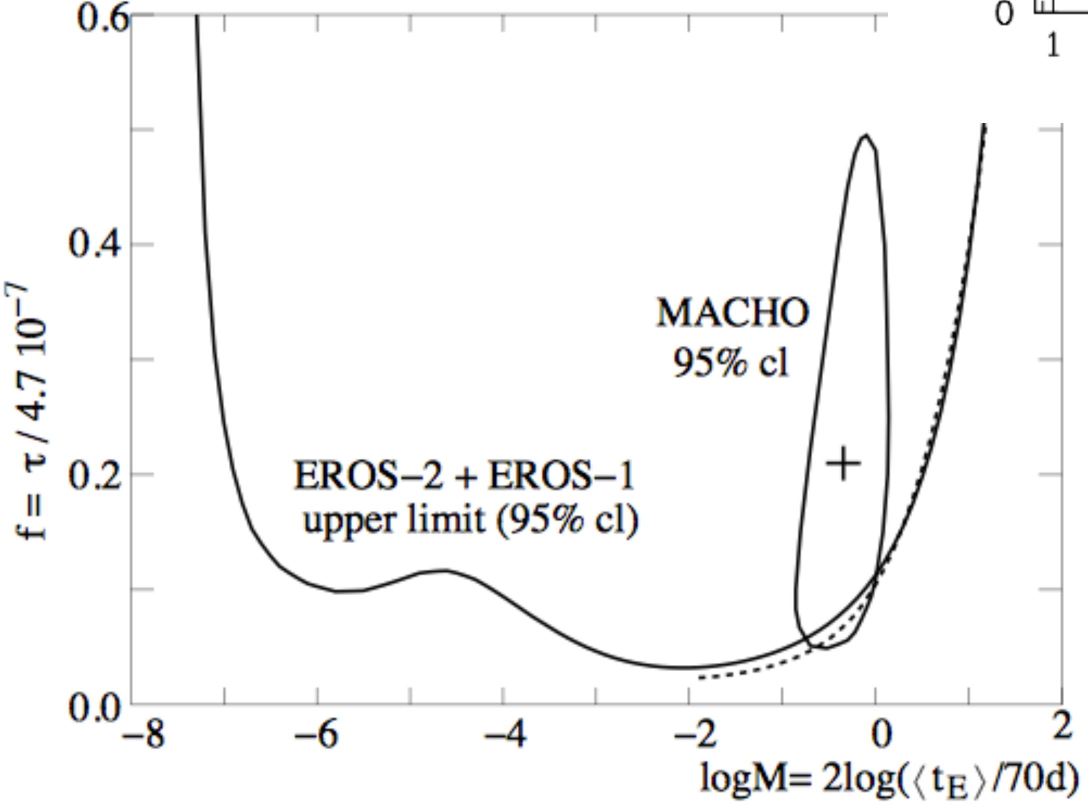
vacuum energy
$p = -\rho_0$

relativistic fluid
$p = \rho$

Limits from microlensing in the LMC



Brandt 1605.03665



For $M \sim 1$ to tens of $M_\odot$ 20-40% of halo DM is allowed:

- ECO can be as numerous as ordinary stars
- ECO could be made of DM, if DM is both in dust and compact objects

LIGO sensitivity to ECO binary mergers

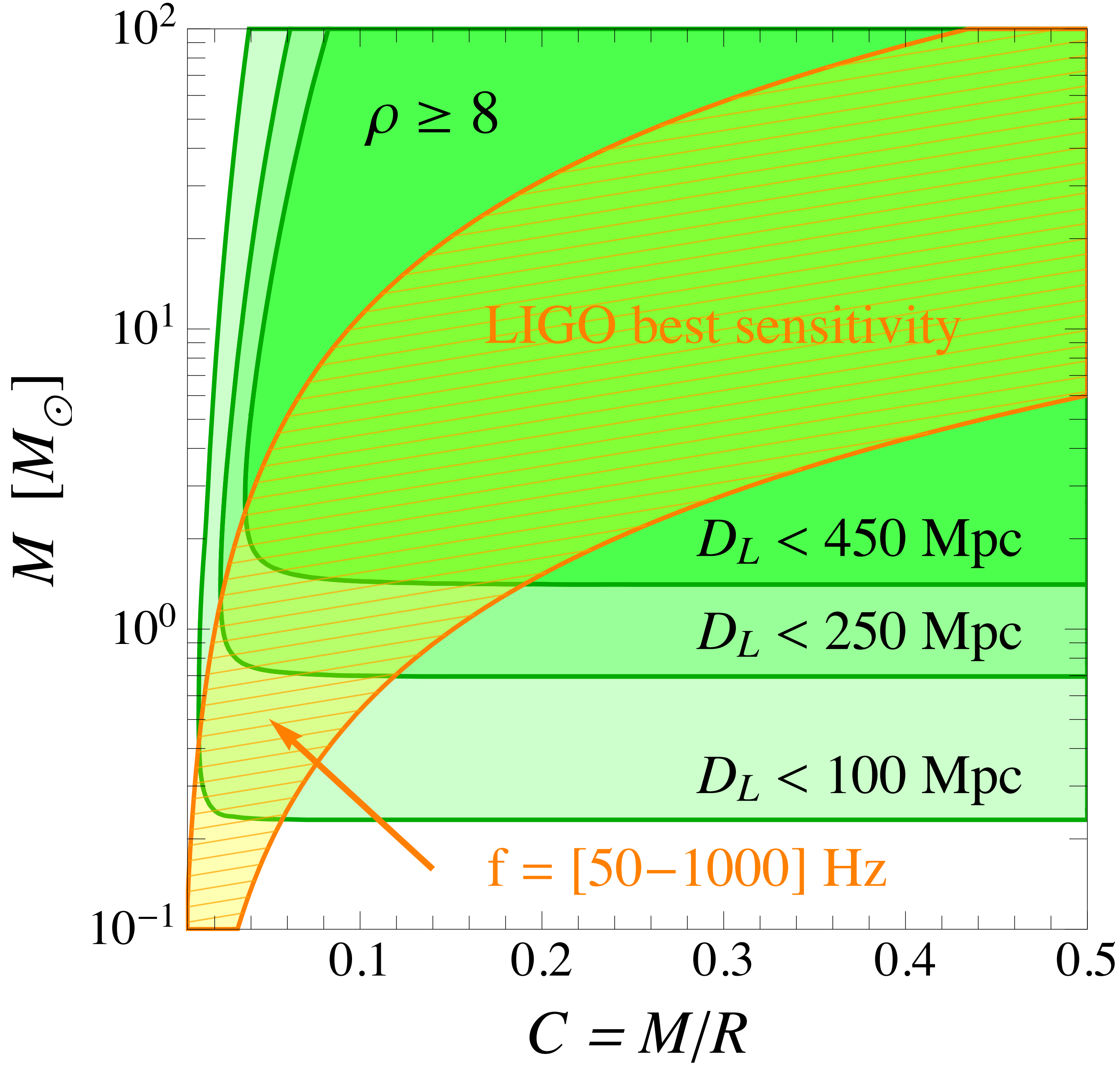
In terms of the astrophysical parameters only:

- mass M (for $M_1=M_2$)
- compactness $C = M/R$ $(C_{BH}=1/2)$

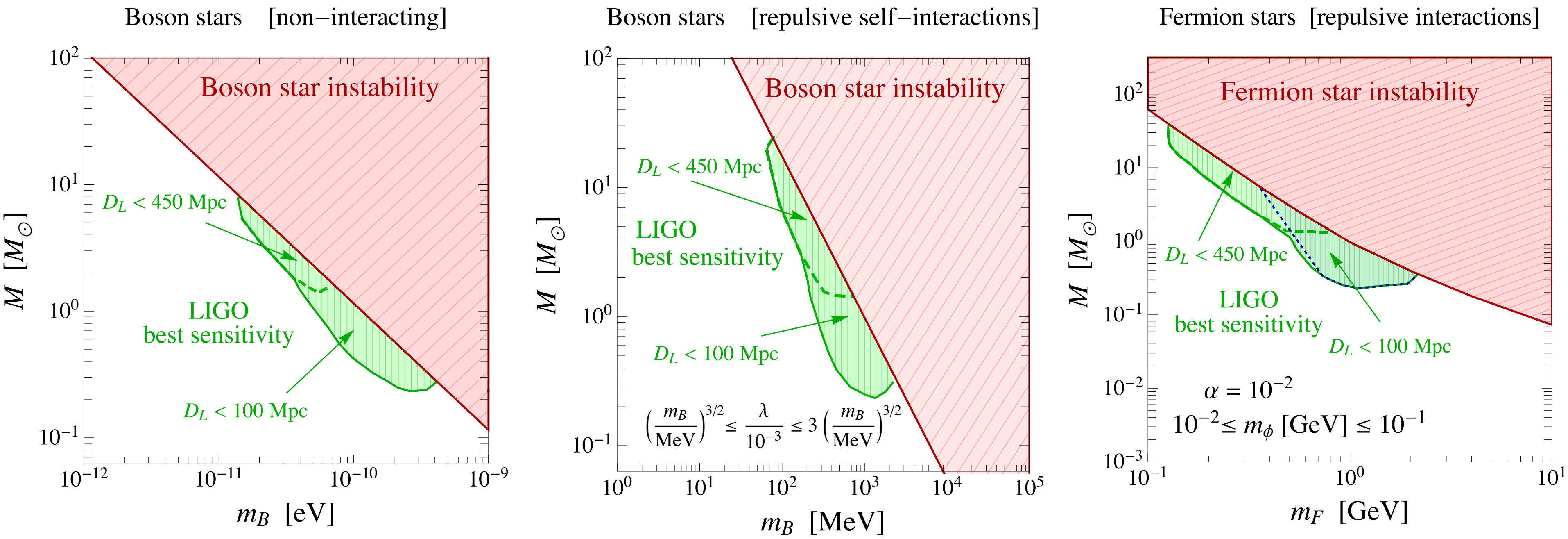
GW frequency grows as the two objects approach ⇒ sensitivity to size

At innermost stable orbit: $f = \dfrac{\sqrt{2}\,C^{3/2}}{3\sqrt{3}\,\pi M}$ $f_{LIGO} \sim 50 - 1000 \text{ Hz}$

Signal/noise must be sufficiently large (depends on D_L)



$\rho \geq 8$
LIGO best sensitivity
$D_L < 450$ Mpc
$D_L < 250$ Mpc
$D_L < 100$ Mpc
f = [50−1000] Hz
10^2
10^1
10^0
10^{-1}
$M\ [M_\odot]$
0.1
0.2
0.3
0.4
0.5
$C = M/R$



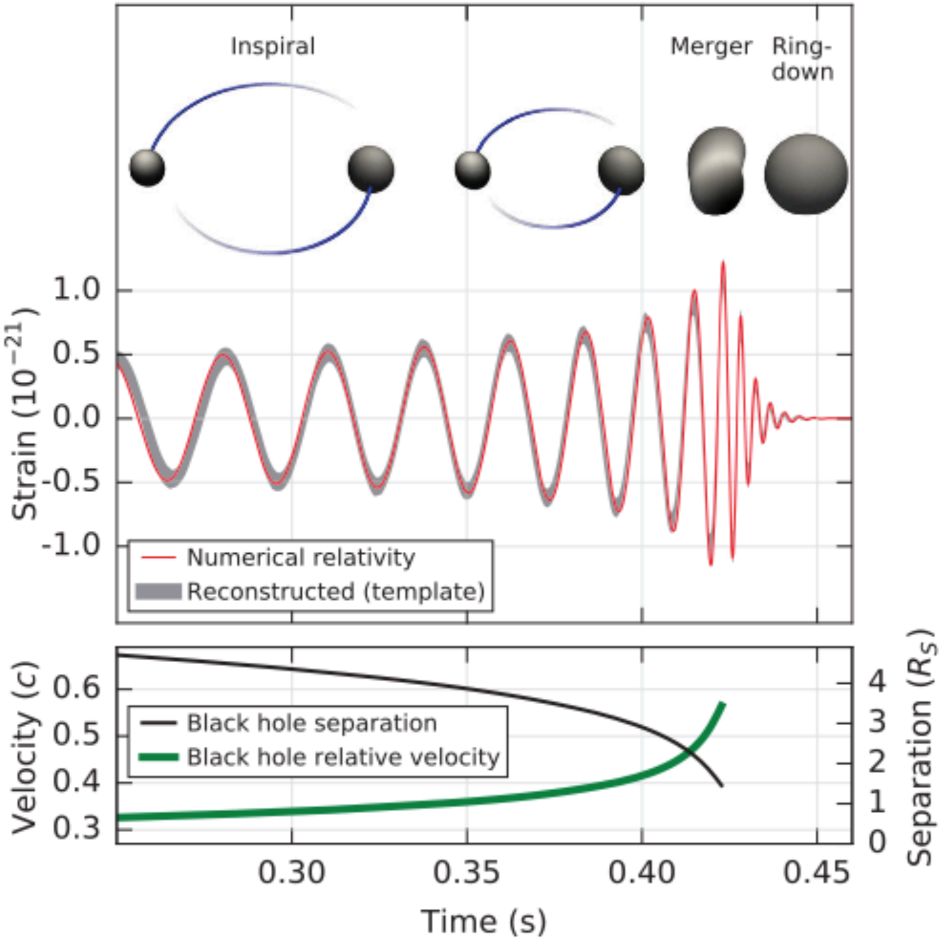
Interesting for axion-like DM:

$$m_a = \left(\frac{10^{17}\ \mathrm{GeV}}{f_a}\right)\ 0.6 \times 10^{-10}\ \mathrm{eV}$$

Interesting for asymmetric DM:

$$m_{DM} = \frac{\eta_b}{\eta_{DM}}\ 5\ \mathrm{GeV}$$

How to detect ECO in a single GW event



Inspiral

- post-Newtonian expansion
- chirp mass $M_c = \dfrac{(M_1 M_2)^{3/5}}{(M_1 + M_2)^{1/5}}$
- redshift (from the way frequency and amplitude change)

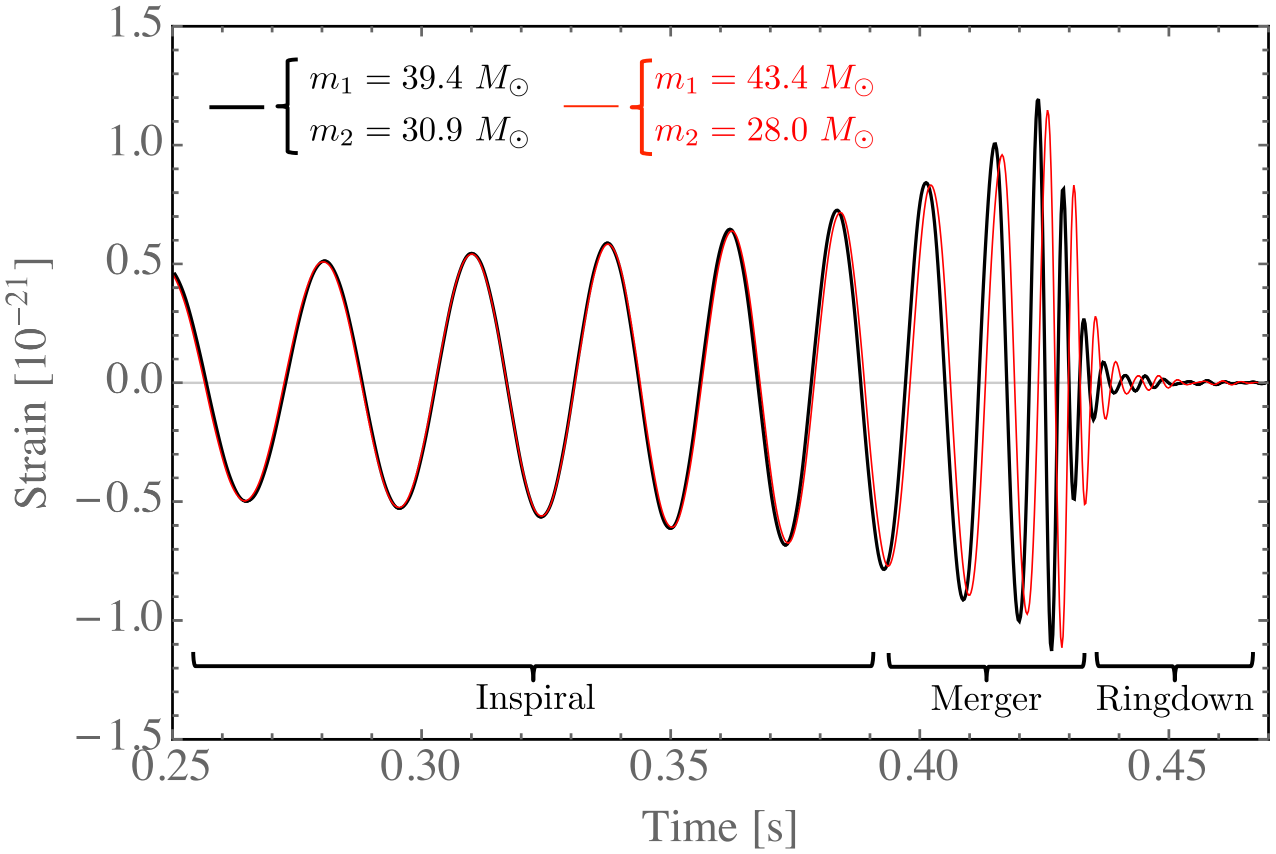
Merger

- numerical relativity (progress in the last 10 yrs)
- need to develop ECO simulations

Ringdown

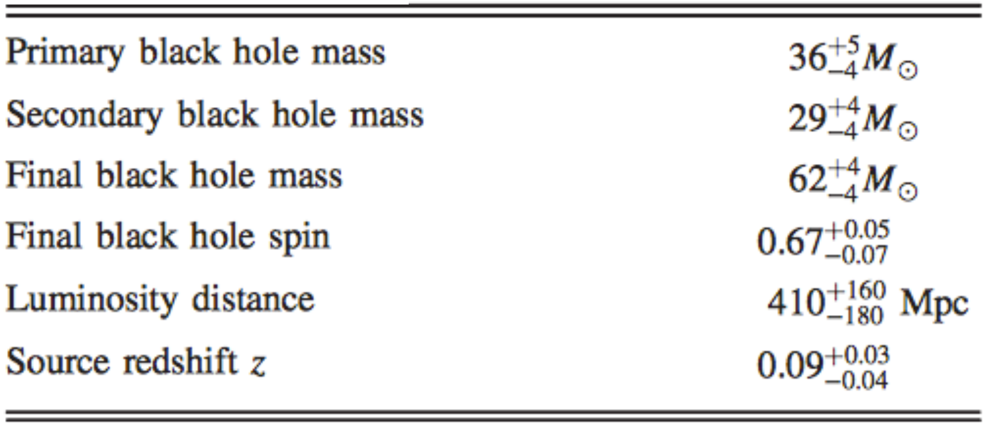
- QNM as perturbations of Kerr BH solution

Extraordinary sensitivity



Black: LIGO best fit

Red: same chirp mass,
but mass ratio excluded
@ 90% CL



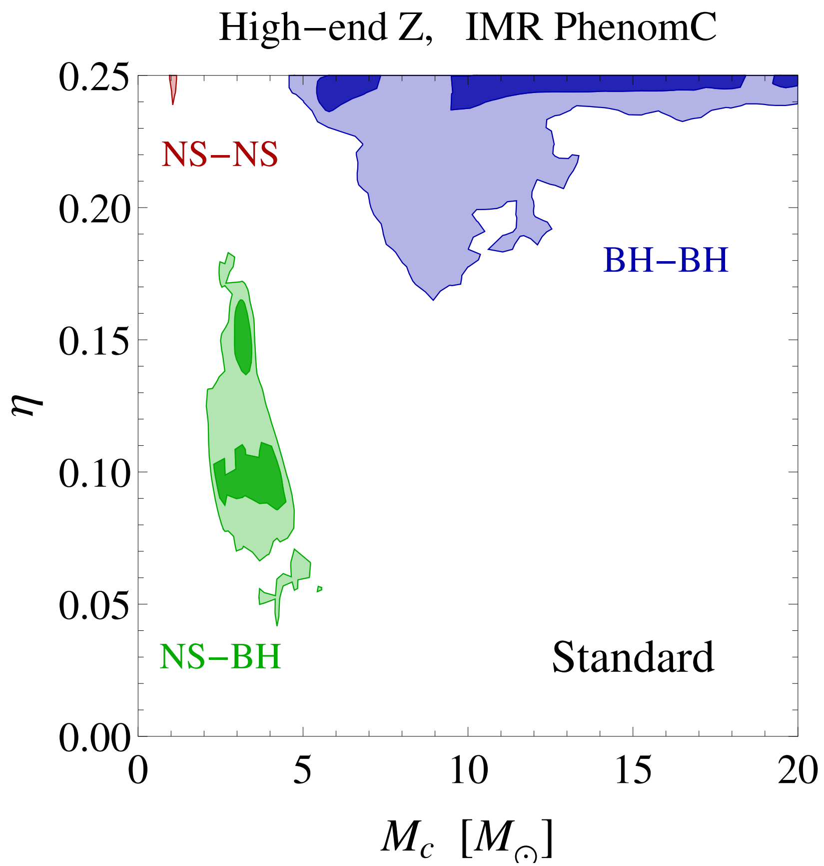
Primary black hole mass	$36^{+5}_{-4} M_\odot$
Secondary black hole mass	$29^{+4}_{-4} M_\odot$
Final black hole mass	$62^{+4}_{-4} M_\odot$
Final black hole spin	$0.67^{+0.05}_{-0.07}$
Luminosity distance	410^{+160}_{-180} Mpc
Source redshift z	$0.09^{+0.03}_{-0.04}$

What can be learned from GW event distributions?

Conventional heavy objects:

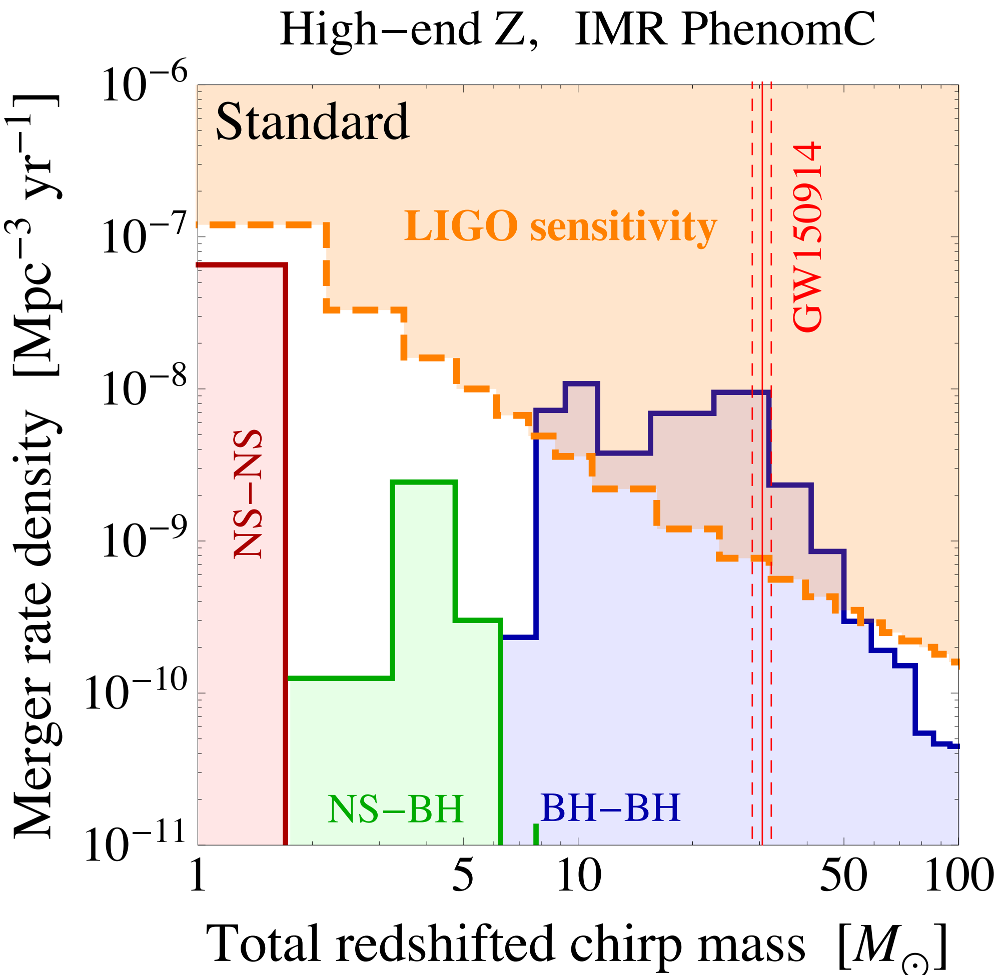
- NS: most massive observed M=2.01±0.04 $M_\odot$ and most models hardly exceed 2 $M_\odot$ (0.13≤C≤0.23)
- Stellar BH: mass distribution expected to start at 5 $M_\odot$ (C=0.5)

Mass gap can be explained in stellar evolution models



$$M_c = \frac{(M_1 M_2)^{3/5}}{(M_1 + M_2)^{1/5}}$$

$$\eta = \frac{M_1 M_2}{(M_1 + M_2)^2}$$



- Filling the gap is evidence of a new population of exotic objects
- Distribution is an essential tool to understand ECO mass function and formation process

Test of Area Theorem

Hawking's Area Theorem: the sum of the horizon areas of a system of BHs never decreases
It follows from GR + null energy condition

Hawking's radiation: M decreases ⇒ R decreases ⇒ A decreases
Violation of the theorem?

Thermodynamics interpretation: BH temperature $T = M_P^2/M$
BH entropy $S = A/4$
Second law of thermodynamics ⇒ Area Theorem
Once the entropy of the emitted radiation is taken into account, no violation of the "generalized" second law of thermodynamics

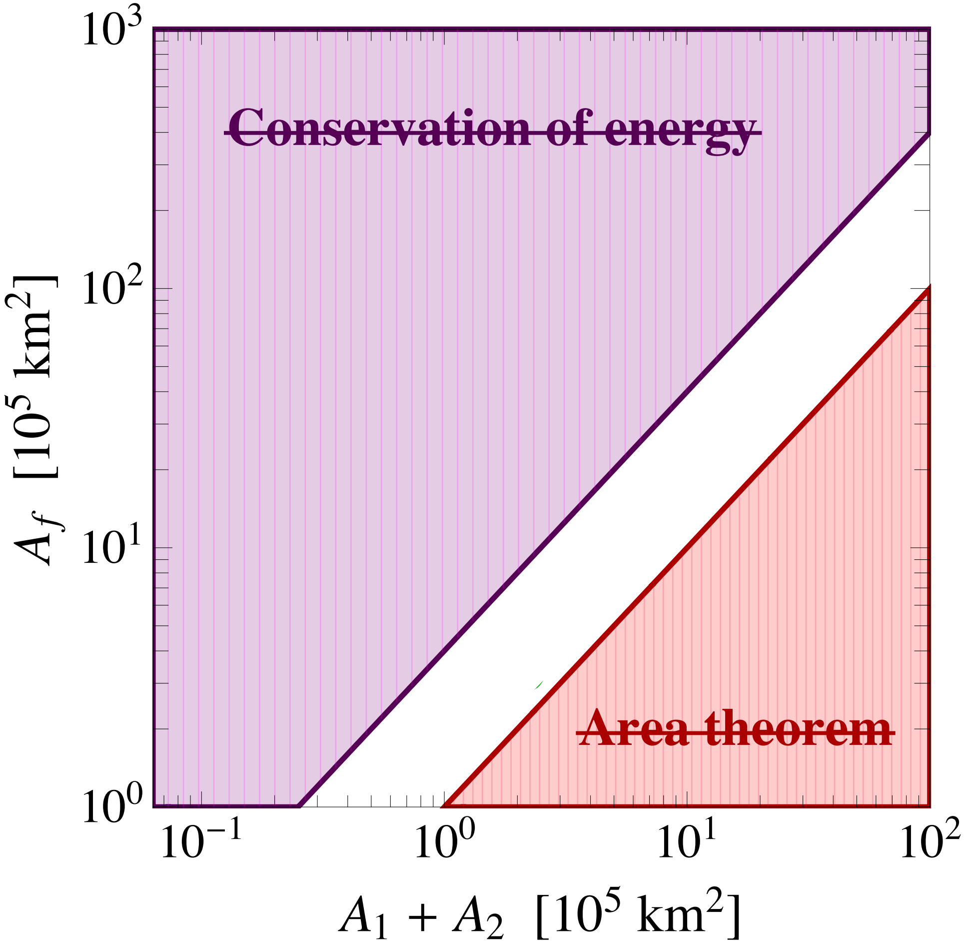
Test of Area Theorem in BH mergers

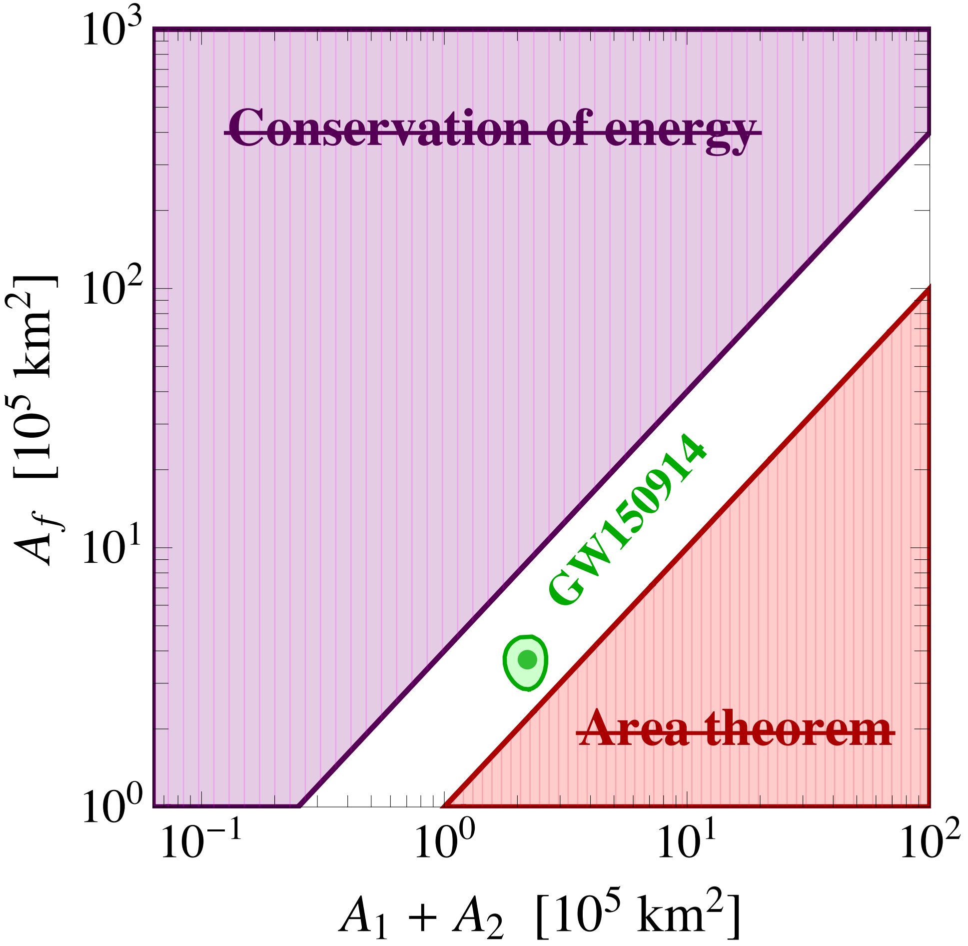
For a Kerr BH: $A = 8\pi M^2 \left(1 + \sqrt{1 - a^2}\right) \qquad a \equiv \frac{J}{M^2}$

Hawking's Area Theorem: $A_f > A_1 + A_2$

$$M_f > \sqrt{M_1^2\, s_1 + M_2^2\, s_2}\,, \qquad s_{1,2} \equiv \frac{1 + \sqrt{1 - a_{1,2}^2}}{1 + \sqrt{1 - a_f^2}}$$

Hawking's Area Theorem:
lower bound on M_f ⇒ upper bound on efficiency of GW emission


~~Conservation of energy~~
~~Area theorem~~
A_f [10^5 km^2]
$A_1 + A_2$ [10^5 km^2]
10^3
10^2
10^1
10^0
10^{-1}
10^0
10^1
10^2



What if the Area Theorem is observed to be violated?

A BH-mimicker ECO can violate it by emitting dark radiation

- Test of fundamental principles
- Test of undetected radiation

Conclusions

- GW observations have opened a new avenue in astronomy
- A unique tool to test gravity in the regime of strong and rapidly-changing field, and relativistic velocities
- Search for new forms of matter in compact objects
- Probing DM clumping in astronomical bodies
- Probing a variety of new-physics ideas
- Information in single GW events and event distribution
- Testing Hawking's Area Theorem can probe dark radiation