

# Perturbative unitarity and the LHC di-photon excess

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Based on [arXiv:1604.05746](https://arxiv.org/abs/1604.05746) in collaboration with:

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# Outline

- Phenomenological aspects of the LHC di-photon excess
- Application of partial wave unitarity to the di-photon excess:

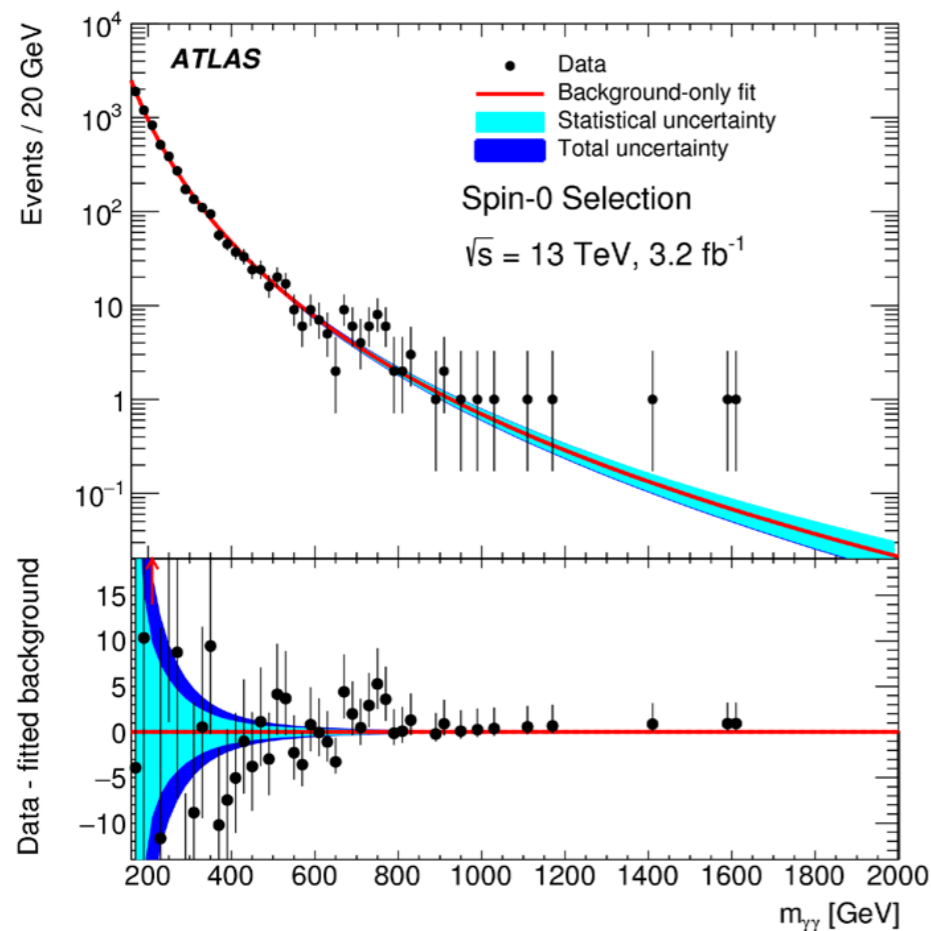
1) range of validity of the EFT → this talk

2) perturbativity bounds in weakly coupled models → see backup slides

# The LHC di-photon excess

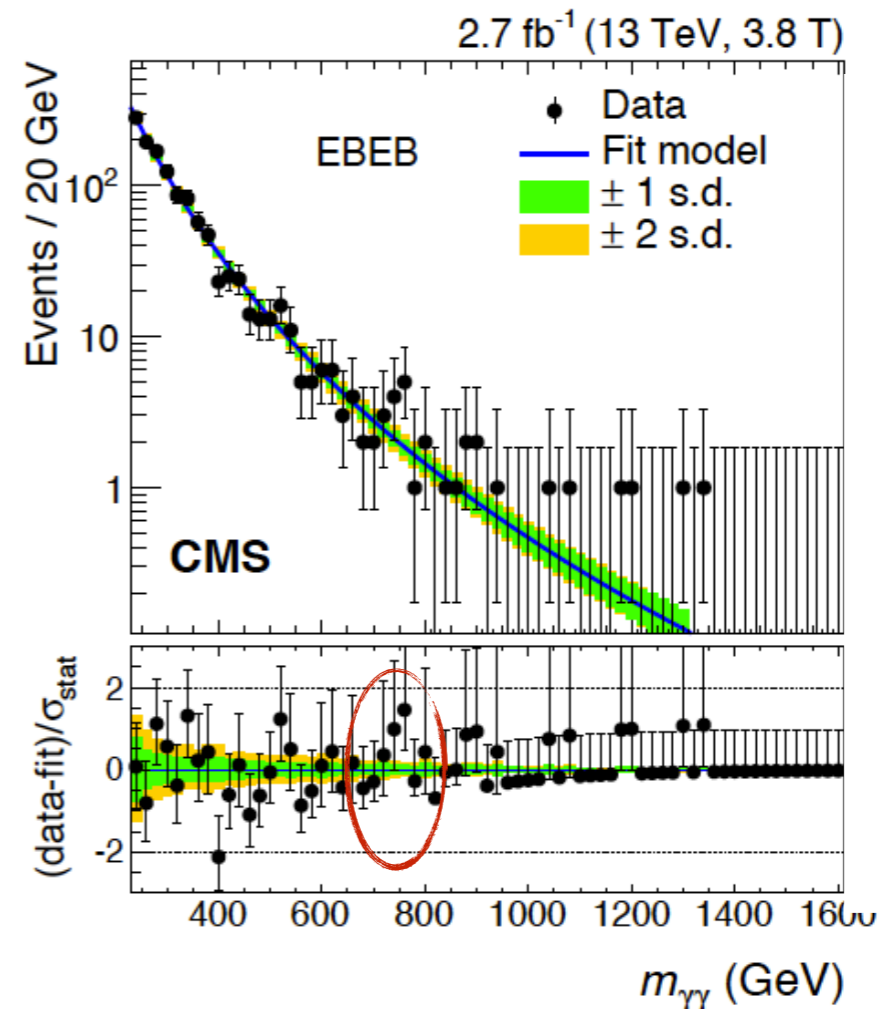
- Both ATLAS and CMS observe a di-photon excess at  $\sim 750$  GeV

[See F. Malek talk on Saturday]



$3.9\sigma$  local ( $2.1\sigma$  global)  
 - best fit for  $\Gamma/M \sim 6\%$

[See M. Quittnat talk on Saturday]



$2.9\sigma$  local ( $1.6\sigma$  global)  
 - narrow width

# The LHC di-photon excess

- Both ATLAS and CMS observe a di-photon excess at  $\sim 750$  GeV
- **Disclaimer**
  - I assume this is not a statistical fluctuation (we will know soon!)
  - $O(400)$  papers on the arXiv since Dec 15th (apologies for the missing refs.)
  - Here: not a specific model, but some general “theoretical constraints”

# Stick to the simplest interpretation

- A single 750 GeV resonance

[See A. Carmona talk on Monday]

- spin 0 (spin 1 not allowed by Landau-Yang theorem, spin 2 too exotic)

# Stick to the simplest interpretation

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[See A. Carmona talk on Monday]

- spin 0

- SM singlet without mixing with the H (extra EW and Higgs precision constraints)

# Stick to the simplest interpretation

- A single 750 GeV resonance

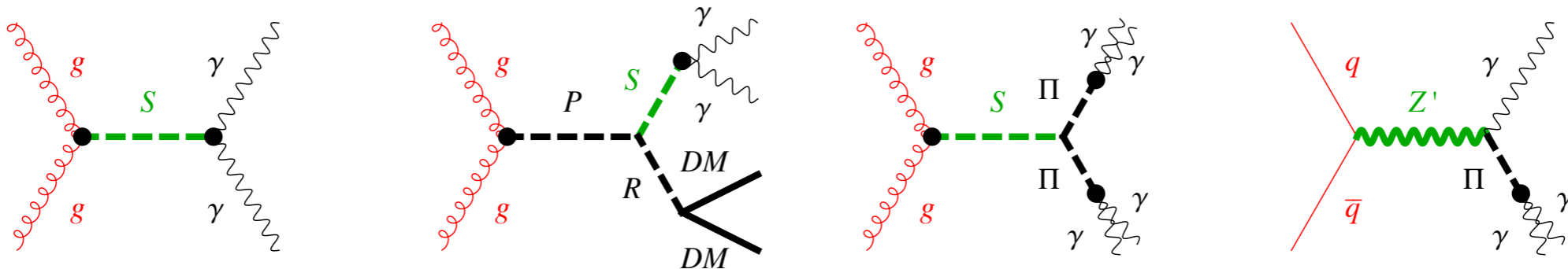
[See A. Carmona talk on Monday]

- spin 0
- SM singlet without mixing with the H
- CP scalar (pseudo-scalar also ok, if CP violated extra constraints from EDMs, ...)

# Stick to the simplest interpretation

- A single 750 GeV resonance
  - spin 0
  - SM singlet without mixing with the H
  - CP scalar
  - s-channel 2-body decay (other kinematical options available)

[See A. Carmona talk on Monday]



[Strumia, Moriond EW]





# EFT of a di-photon resonance

- Assuming a spin-0 SM gauge-singlet scalar resonance  $S$

[see e.g. 1512.04933, 1603.06566]

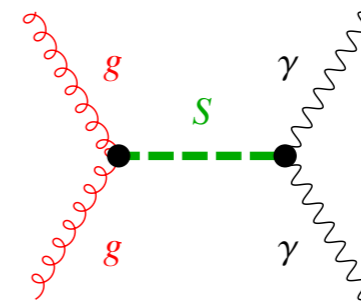
$$\mathcal{L}_{\text{eff}} \supset -\frac{g_3^2}{2\Lambda_g} S G_{\mu\nu}^2 - \frac{e^2}{2\Lambda_\gamma} S F_{\mu\nu}^2 - \sum_q y_{qS} S \bar{q}q$$

- Decay widths

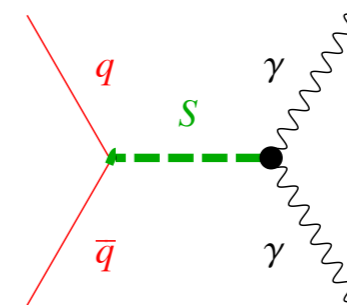
$$\Gamma_{gg} \equiv \Gamma(S \rightarrow gg) = 8\pi\alpha_s^2 \frac{M_S^3}{\Lambda_g^2}$$

$$\Gamma_{\gamma\gamma} \equiv \Gamma(S \rightarrow \gamma\gamma) = \pi\alpha_{\text{EM}}^2 \frac{M_S^3}{\Lambda_\gamma^2}$$

$$\Gamma_{q\bar{q}} \equiv \Gamma(S \rightarrow q\bar{q}) = \frac{3}{8\pi} y_{qS}^2 M_S$$



or



# EFT of a di-photon resonance

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[see e.g. 1512.04933, 1603.06566]

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- Fit cross-section

$$\sigma(pp \rightarrow S \rightarrow \gamma\gamma) = \sigma(pp \rightarrow S) \mathcal{B}_{\gamma\gamma} \simeq 3 \div 6 \text{ fb}$$

$$\sigma(pp \rightarrow S) = \frac{1}{M_{SS}} \left[ \sum_{\mathcal{P}} C_{\mathcal{P}\bar{\mathcal{P}}} \Gamma_{\mathcal{P}\bar{\mathcal{P}}} \right]$$

-  $C_{\mathcal{P}\bar{\mathcal{P}}}$  → parton luminosities

$\sqrt{s}$	$C_{b\bar{b}}$	$C_{c\bar{c}}$	$C_{s\bar{s}}$	$C_{d\bar{d}}$	$C_{u\bar{u}}$	$C_{gg}$	$C_{\gamma\gamma}$
8 TeV	1.07	2.7	7.2	89	158	174	54
13 TeV	15.3	36	83	627	1054	2137	11

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- Consistency b/w 8 and 13 TeV LHC data singles out **gluon fusion** or **heavy-Q annihilation**

$r_{b\bar{b}}$	$r_{c\bar{c}}$	$r_{s\bar{s}}$	$r_{d\bar{d}}$	$r_{u\bar{u}}$	$r_{gg}$	$r_{\gamma\gamma}$
5.4	5.1	4.3	2.7	2.5	4.7	1.9
✓	✓	✓	✗	✗	✓	✗

- Gain factor  $r = \sigma_{13 \text{ TeV}} / \sigma_{8 \text{ TeV}} \gtrsim 5$

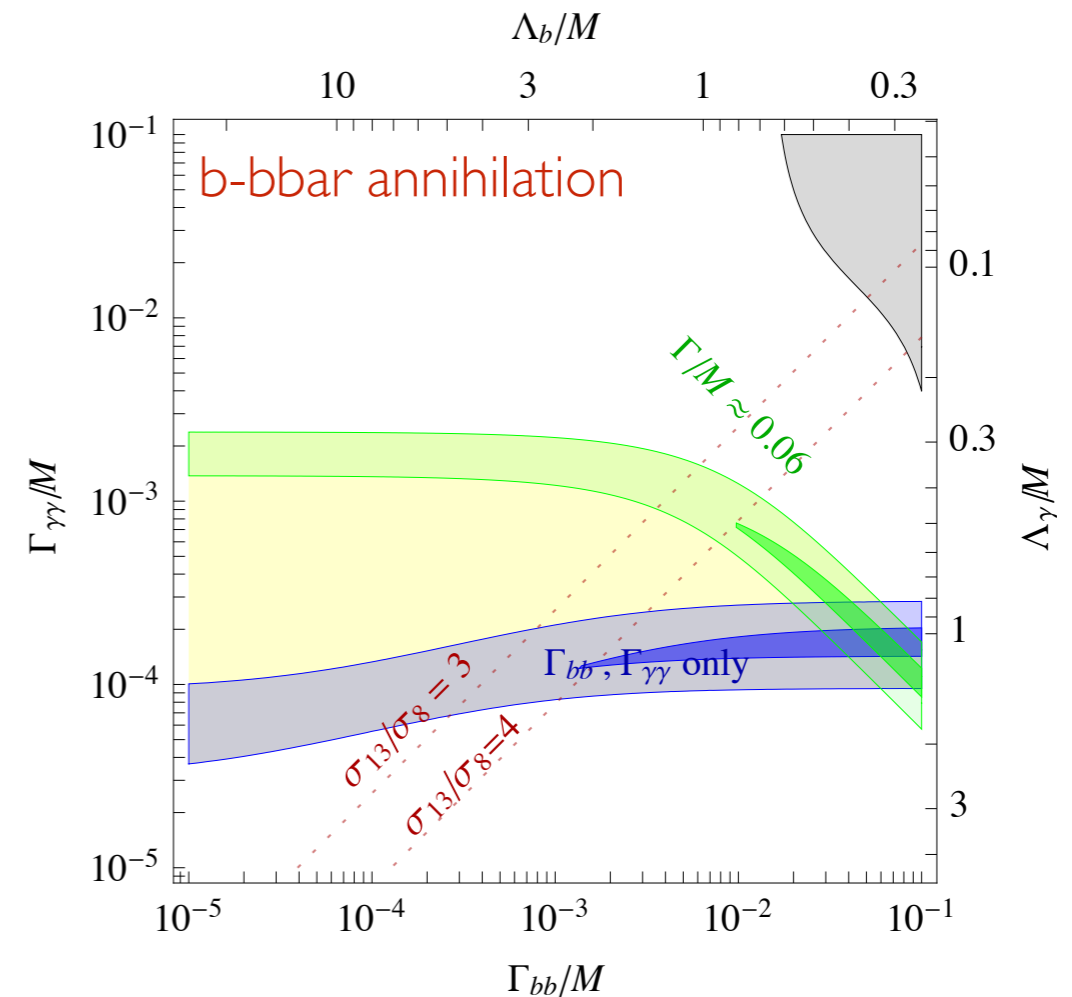
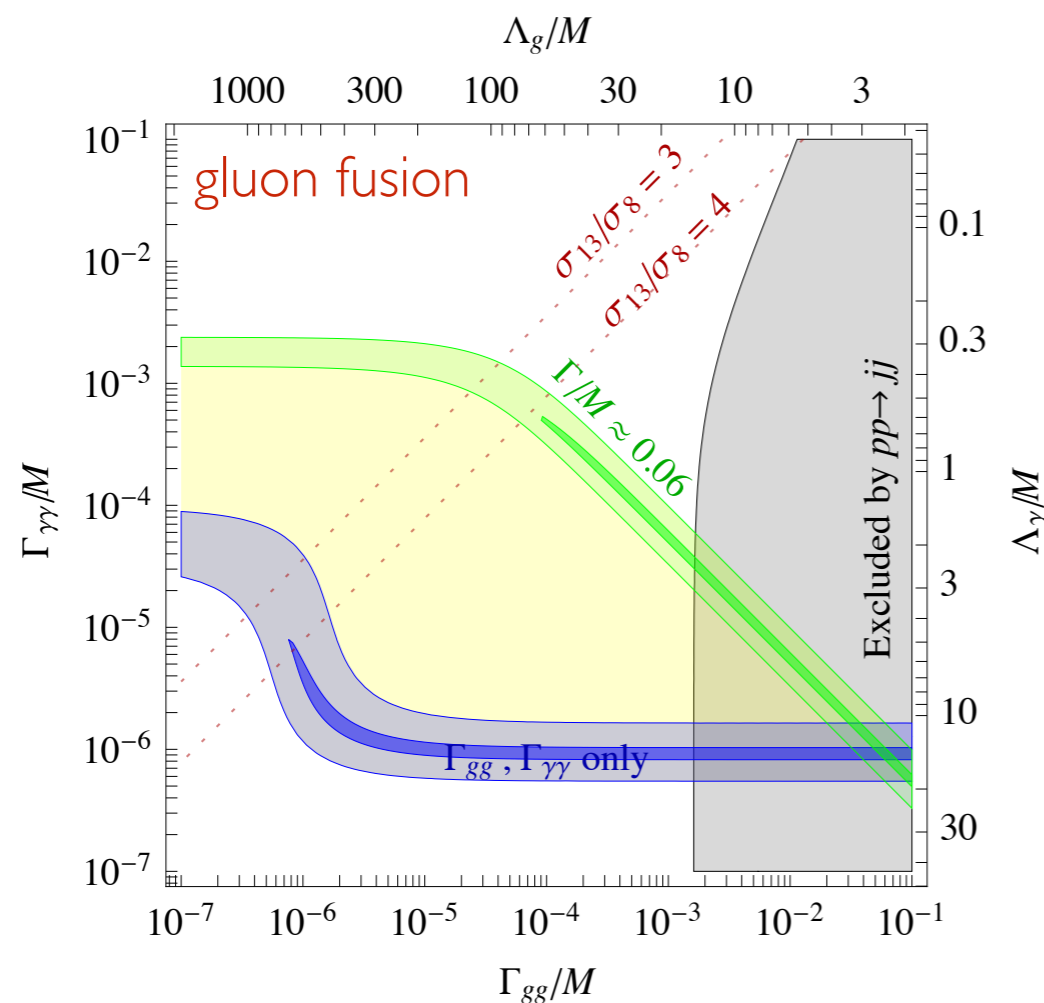
# EFT of a di-photon resonance

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- Production mechanisms



# EFT of a di-photon resonance

- Assuming a spin-0 SM gauge-singlet scalar resonance  $S$

[see e.g. 1512.04933, 1603.06566]

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- SM gauge-invariant EFT

$$\mathcal{L}_{\text{eff}}^{\text{SM-invariant}} \supset -\frac{g_3^2}{2\Lambda_g} S G_{\mu\nu}^2 - \frac{g_2^2}{2\Lambda_W} S W_{\mu\nu}^2 - \frac{g_1^2}{2\Lambda_B} S B_{\mu\nu}^2 - \frac{S}{\Lambda_q} (\bar{Q}_L q_R H + \text{h.c.})$$

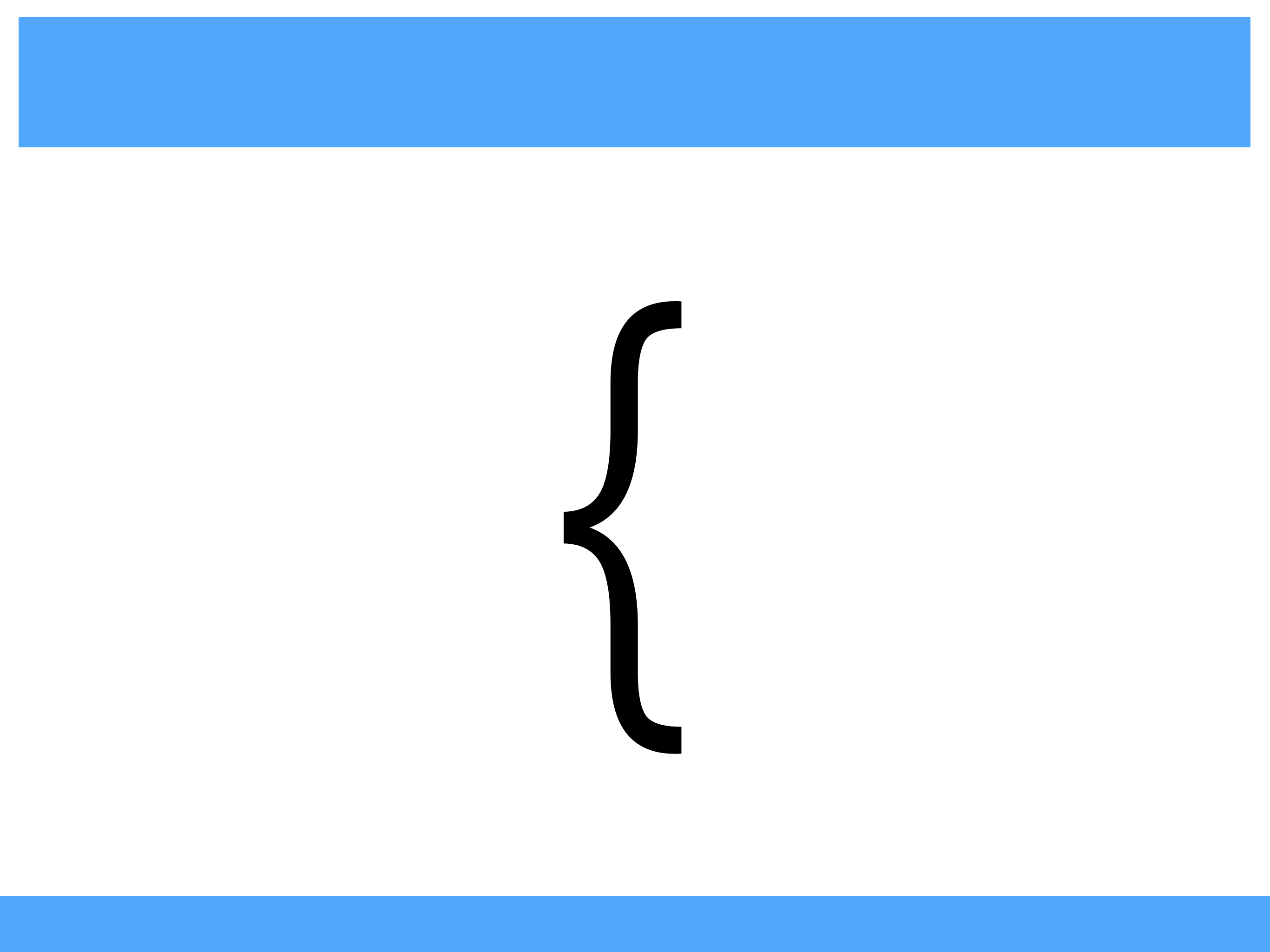
- matching:

$$\frac{1}{\Lambda_\gamma} = \frac{1}{\Lambda_B} + \frac{1}{\Lambda_W} \quad y_{qS} = \frac{v}{\sqrt{2}\Lambda_q}$$

- leading interactions of  $S$  to SM fields via dim=5 operators



*until which scale we do expect the  $S$ +SM EFT description to be valid?*



}

# A historical detour

- Unitarity arguments often served as a guide in HEP

1)  $\pi\pi$  scattering in  $\chi$ PT

[Weinberg (1966), ...]

- the scale of unitarity violation  $\sim 500$  MeV signals the onset of NP (QCD)

2) LHC “no lose theorem”  $\rightarrow \Lambda \lesssim 1$  TeV

[Lee, Quigg, Thacker (1977), ...]

- upper bound either on the Higgs mass or on the scale of NP unitarizing  $WW$  scattering

3) Upper bound on the mass of particle DM (if once in thermal equilibrium)

[Griest, Kamionkowski (1990), ...]

$$m_{\text{DM}} \lesssim 300 \text{ TeV}$$

# Partial wave projection

- Scattering matrix:  $S = 1 + iT$

- $2 \rightarrow 2$  scattering amplitude in momentum space

$$\langle f|T|i\rangle = (2\pi)^4 \delta^{(4)}(P_i - P_f) \mathcal{T}_{fi}(\sqrt{s}, \cos \theta)$$

- Dependence on  $\cos(\theta)$  eliminated by projection onto J-th partial waves [Jacob, Wick (1959)]

$$a_{fi}^J = \frac{\beta_f^{1/4}(s, m_{f1}^2, m_{f2}^2) \beta_i^{1/4}(s, m_{i1}^2, m_{i2}^2)}{32\pi s} \int_{-1}^1 d(\cos \theta) d_{\mu_i \mu_f}^J(\theta) \mathcal{T}_{fi}(\sqrt{s}, \cos \theta)$$



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-  $\beta(x, y, z) = x^2 + y^2 + z^2 - 2xy - 2yz - 2zx \rightarrow$  kinematics (zero at threshold)

-  $\mu_i = \lambda_{i1} - \lambda_{i2}$  and  $\mu_f = \lambda_{f1} - \lambda_{f2} \rightarrow$  helicity formalism

-  $d_{\mu_i \mu_f}^J(\theta) \rightarrow$  Wigner d-functions (e.g.  $d_{00}^J = P_J$  Legendre polynomials)

# Partial wave projection

- Scattering matrix:  $S = 1 + iT$
- $2 \rightarrow 2$  scattering amplitude in momentum space

$$\langle f|T|i\rangle = (2\pi)^4 \delta^{(4)}(P_i - P_f) \mathcal{T}_{fi}(\sqrt{s}, \cos \theta)$$

- Focus on  $J = 0$  partial wave

$$a_{fi}^0 = \frac{\beta_f^{1/4}(s, m_{f1}^2, m_{f2}^2) \beta_i^{1/4}(s, m_{i1}^2, m_{i2}^2)}{32\pi s} \int_{-1}^1 d(\cos \theta) \mathcal{T}_{fi}(\sqrt{s}, \cos \theta)$$

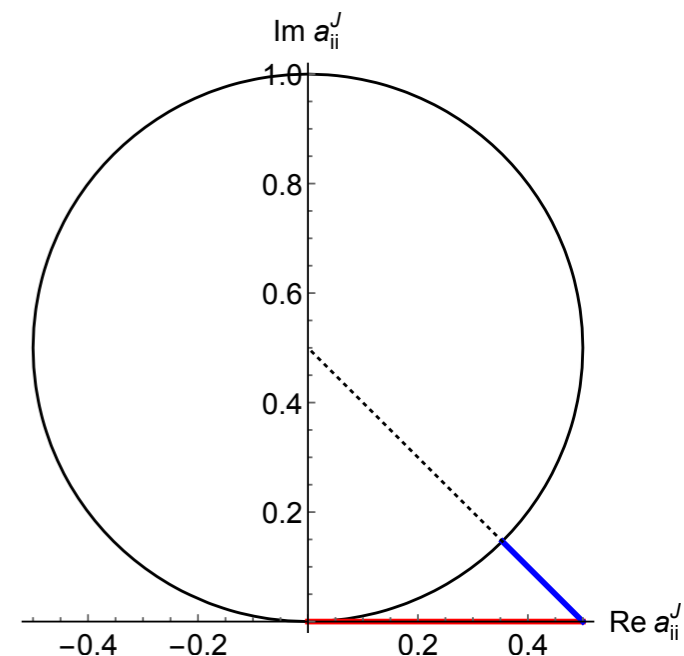
# Perturbative unitarity

- Unitarity (an axiom of QFT)

$$SS^\dagger = 1 \quad \longrightarrow \quad \frac{1}{2i} (a_{fi}^J - a_{if}^{J*}) \geq \sum_{h \in 2\text{-particle}} a_{hf}^{J*} a_{hi}^J$$

- For  $f = i$  (optical theorem)



$$\text{Im } a_{ii}^J \geq |a_{ii}^J|^2 \quad \longrightarrow \quad (\text{Re } a_{ii}^J)^2 + \left( \text{Im } a_{ii}^J - \frac{1}{2} \right)^2 \leq \frac{1}{4}$$



- In practical perturbative calculations S-matrix unitarity is always approximate

- perturbative expansion breaks down for

$$|\text{Re} (a_{ii}^J)^{\text{Born}}| \leq \frac{1}{2}$$



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# Di-photon scattering

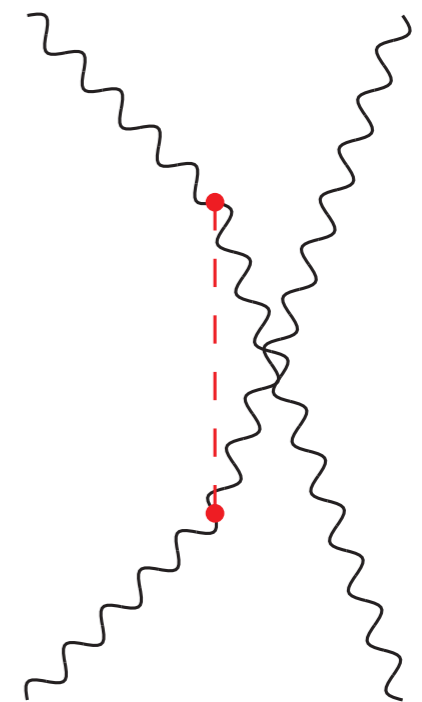
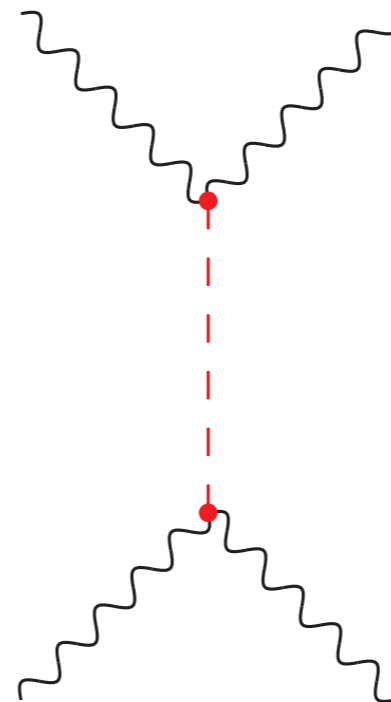
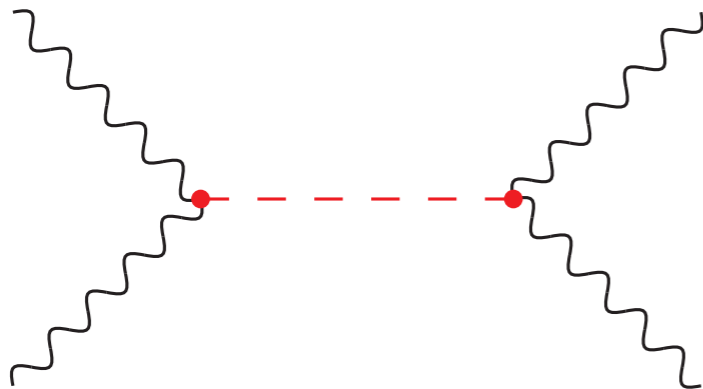
- $\gamma\gamma \rightarrow \gamma\gamma$  scattering (high-energy limit)

[see also 1604.01008]

$$\mathcal{L}_{\text{eff}} \supset -\frac{e^2}{2\Lambda_\gamma} S F_{\mu\nu}^2$$



$$a^0 \simeq -\frac{e^4 s}{32\pi\Lambda_\gamma^2}$$



# Di-photon scattering

- $\gamma\gamma \rightarrow \gamma\gamma$  scattering (high-energy limit) [see also 1604.01008]

$$\mathcal{L}_{\text{eff}} \supset -\frac{e^2}{2\Lambda_\gamma} S F_{\mu\nu}^2 \quad \longrightarrow \quad a^0 \simeq -\frac{e^4 s}{32\pi\Lambda_\gamma^2}$$

- Tree-level unitarity bound  $|\text{Re } a^0| \leq 1/2$

$$\sqrt{s} \lesssim \sqrt{16\pi} \frac{\Lambda_\gamma}{e^2} = M_S \left( \frac{\Gamma_{\gamma\gamma}}{M_S} \right)^{-1/2} \simeq 75 \text{ TeV} \left( \frac{\Gamma_{\gamma\gamma}/M_S}{10^{-4}} \right)^{-1/2}$$

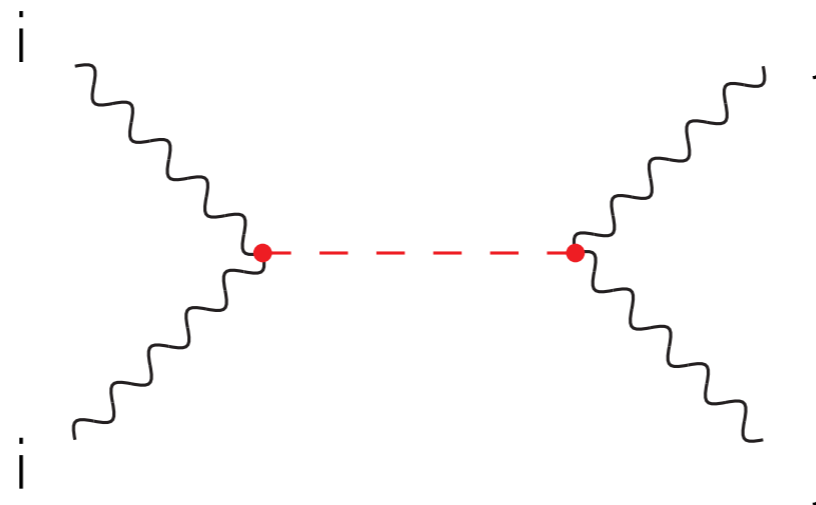


$$\Gamma_{\gamma\gamma} = \pi\alpha_{\text{EM}}^2 \frac{M_S^3}{\Lambda_\gamma^2}$$

- scale of unitarity violation fixed in terms of a “measured” quantity

# SM gauge boson scattering

- Bounds can be strengthened by looking at the full  $V_i V_i \rightarrow V_j V_j$  scattering matrix
  - $i =$  any of the  $8 + 3 + 1$  (transversely polarized) SM gauge bosons



$$m_{ij} = \frac{a_i a_j}{s - M_S^2}$$



$$\tilde{m}_{\text{eigen.}} \propto \sum_i a_i^2$$

(s-channel dominates at high energies)

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$$\mathcal{L}_{\text{eff}} \supset -\frac{g_3^2}{2\Lambda_g} S G_{\mu\nu}^2 - \frac{g_2^2}{2\Lambda_W} S W_{\mu\nu}^2 - \frac{g_1^2}{2\Lambda_B} S B_{\mu\nu}^2$$



$$\tilde{a}^0 \simeq -\frac{s}{32\pi} \left( \frac{8g_3^4}{\Lambda_g^2} + \frac{3g_2^4}{\Lambda_W^2} + \frac{g_1^4}{\Lambda_B^2} \right) \quad (\text{highest eigenvalue})$$



$$\frac{s}{32\pi} \left( 8 \frac{g_s^4}{\Lambda_g^2} + 3 \frac{g_2^4}{\Lambda_W^2} + \frac{g_1^4}{\Lambda_B^2} \right) \lesssim \frac{1}{2} \quad (\text{unitarity bound})$$



# SM gauge boson scattering

- Bounds can be strengthened by looking at the full  $V_i V_i \rightarrow V_j V_j$  scattering matrix
  - in terms of “measured” quantities:

$$\frac{1}{\Lambda_g^2} = \frac{\Gamma_{gg}}{8\pi\alpha_s^2 M_S^3} \quad r \equiv \frac{\Lambda_B}{\Lambda_W} \quad \sqrt{s} \lesssim M_S \left( \frac{\Gamma_{gg}}{M_S} + f(r) \frac{\Gamma_{\gamma\gamma}}{M_S} \right)^{-1/2}$$

$$\frac{1}{\Lambda_W^2} = \frac{\Gamma_{\gamma\gamma}}{\pi\alpha_{\text{EM}}^2 M_S^3} \left( \frac{r}{1+r} \right)^2 \quad \longrightarrow \quad f(r) = \frac{3r^2 s_W^{-4} + c_W^{-4}}{(1+r)^2}$$


$$\frac{1}{\Lambda_B^2} = \frac{\Gamma_{\gamma\gamma}}{\pi\alpha_{\text{EM}}^2 M_S^3} \left( \frac{1}{1+r} \right)^2$$

$$\frac{s}{32\pi} \left( 8 \frac{g_s^4}{\Lambda_g^2} + 3 \frac{g_2^4}{\Lambda_W^2} + \frac{g_1^4}{\Lambda_B^2} \right) \lesssim \frac{1}{2} \quad (\text{unitarity bound})$$

# SM gauge boson scattering

- Bounds can be strengthened by looking at the full  $V_i V_i \rightarrow V_j V_j$  scattering matrix
  - in terms of “measured” quantities:

i) gluon scattering

$$\sqrt{s} \lesssim 24 \text{ TeV} \left( \frac{\Gamma_{gg}/M_S}{10^{-3}} \right)^{-1/2}$$
$$r \equiv \frac{\Lambda_B}{\Lambda_W}$$
$$\sqrt{s} \lesssim M_S \left( \frac{\Gamma_{gg}}{M_S} + f(r) \frac{\Gamma_{\gamma\gamma}}{M_S} \right)^{-1/2}$$
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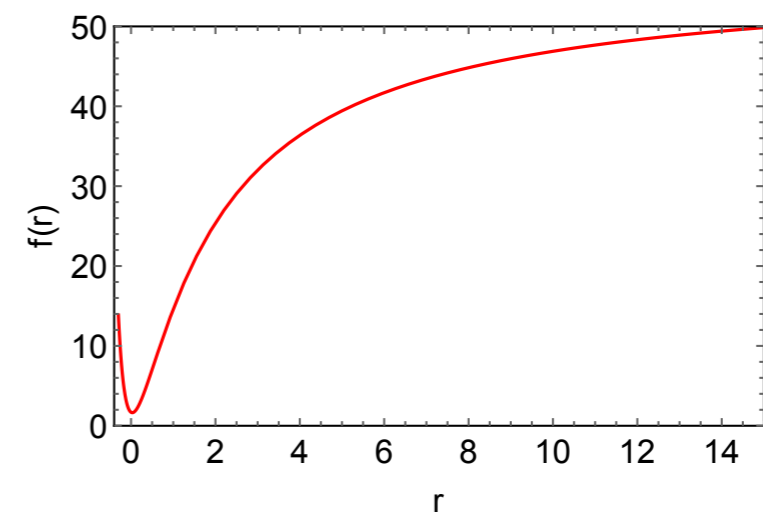
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$$f(r) = \frac{3r^2 s_W^{-4} + c_W^{-4}}{(1+r)^2}$$


ii) EW gauge boson scattering

$$\sqrt{s} \lesssim 11 \div 59 \text{ TeV} \left( \frac{\Gamma_{\gamma\gamma}/M_S}{10^{-4}} \right)^{-1/2}$$


max f(r)
min f(r)

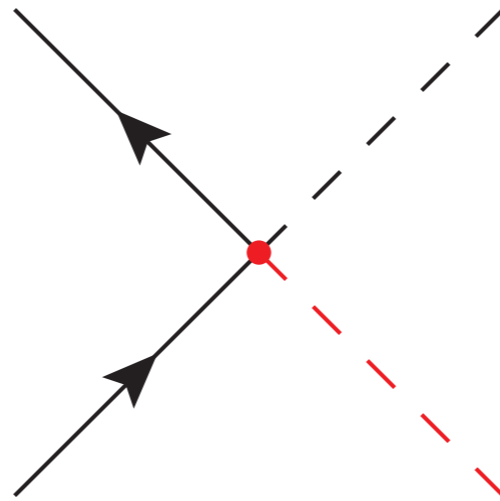


- future determination of  $S \rightarrow WW, ZZ, Z\gamma$  crucial to strengthen the bound

# SM quark annihilation

- $\bar{Q}q \rightarrow SH$  scattering

$$\mathcal{L}_{\text{eff}} \supset -\frac{1}{\Lambda_q} S \bar{Q}_L q_R H \quad \longrightarrow \quad a^0 \simeq \frac{1}{16\pi} \frac{\sqrt{s}}{\Lambda_q}$$



# SM quark annihilation

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- Tree-level unitarity bound

$$\sqrt{s} \lesssim 8\pi\Lambda_q = 2\sqrt{3}\pi v \left( \frac{\Gamma_{q\bar{q}}}{M_S} \right)^{-1/2} \simeq 6.2 \text{ TeV} \left( \frac{\Gamma_{q\bar{q}}/M_S}{0.06} \right)^{-1/2}$$

$$y_{qS} = \frac{v}{\sqrt{2}\Lambda_q}$$

$$\Gamma_{q\bar{q}} = \frac{3}{8\pi} y_{qS}^2 M_S$$

# Di-photon “no lose theorem”

- EFT of a di-photon resonance breaks down at scales of **few tens of TeV**

$$\sqrt{s} \lesssim 11 \div 59 \text{ TeV} \left( \frac{\Gamma_{\gamma\gamma}/M_S}{10^{-4}} \right)^{-1/2} \quad \longrightarrow \quad \text{independently of production mechanism}$$

$$\sqrt{s} \lesssim 24 \text{ TeV} \left( \frac{\Gamma_{gg}/M_S}{10^{-3}} \right)^{-1/2} \quad \longrightarrow \quad \text{gg initiated production}$$

$$\sqrt{s} \lesssim 6.2 \text{ TeV} \left( \frac{\Gamma_{q\bar{q}}/M_S}{0.06} \right)^{-1/2} \quad \longrightarrow \quad \text{q-qbar initiated production}$$

- new d.o.f. unitarizing the amplitudes' growth are expected below this scale
- **a physics case for the 50 TeV collider**

(a *worse case scenario*. In typical models new d.o.f. beyond  $S$  lie much below 10 TeV)

# Conclusions

- Perturbative unitarity as a tool to infer:
  - 1) the range of validity of a given EFT
    - EFT of a di-photon resonance breaks down at scales of **few tens of TeV**
  - 2) the range of validity of perturbation theory in renormalizable models
    - **Endangered calculability** in a wide class of di-photon models (**large width** scenario)

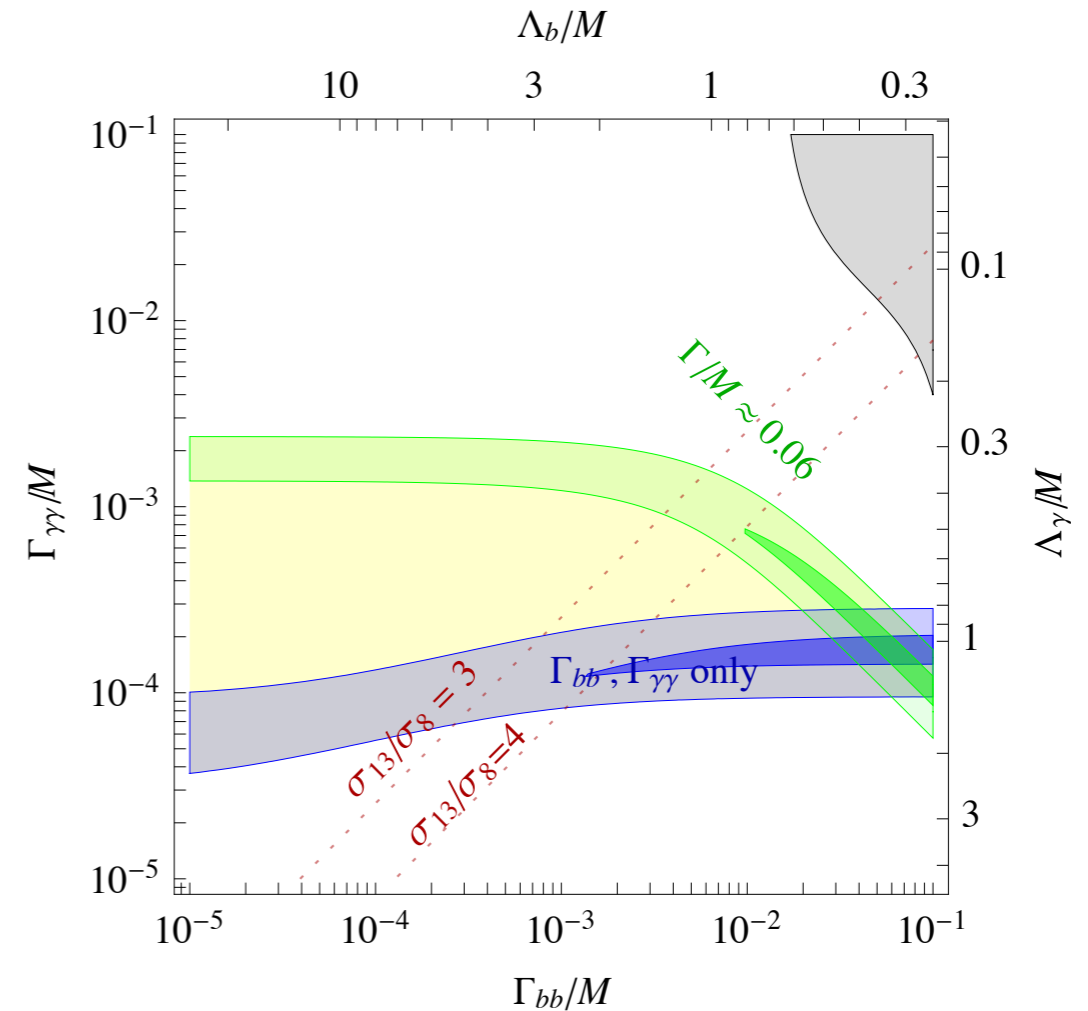
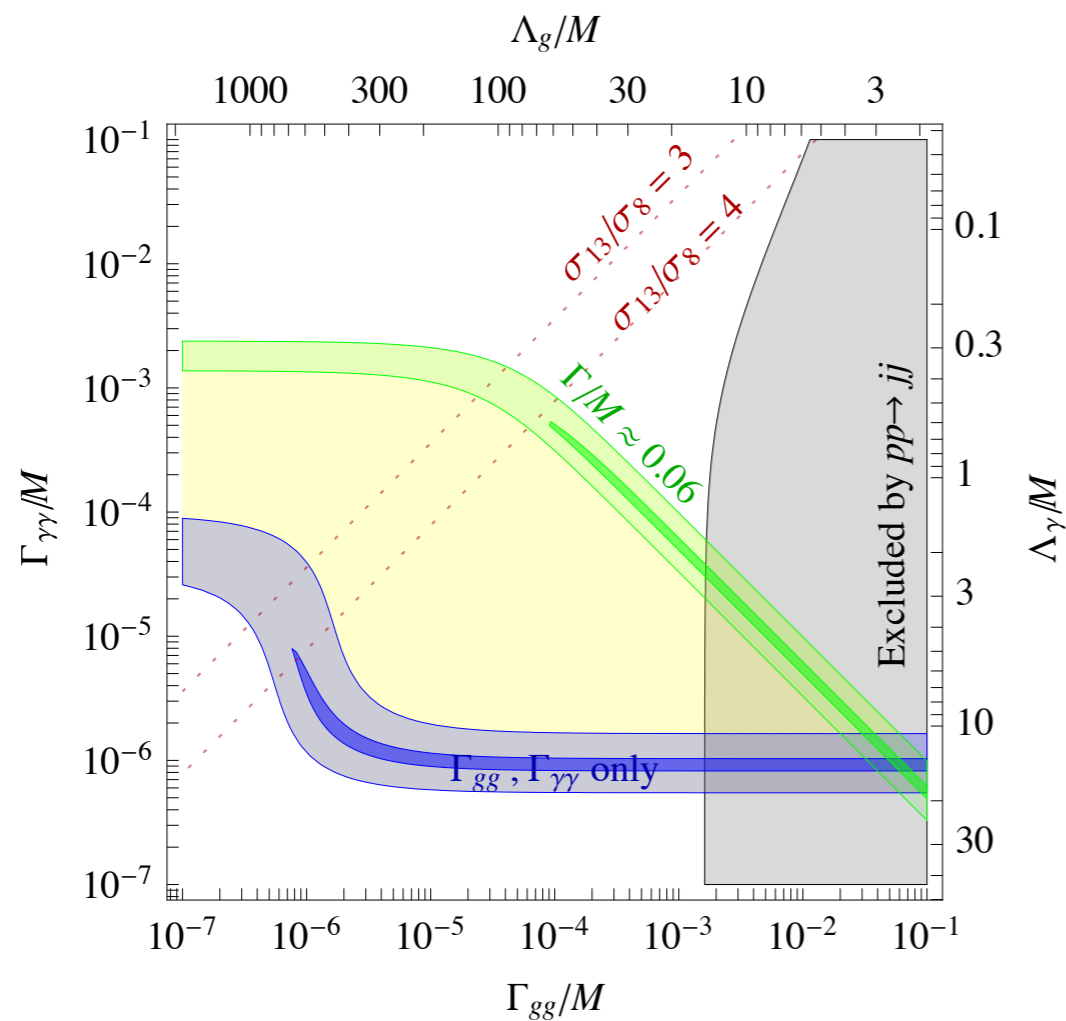
*[see backup slides]*

# Backup slides



# Production mechanisms

[from 1512.04933]

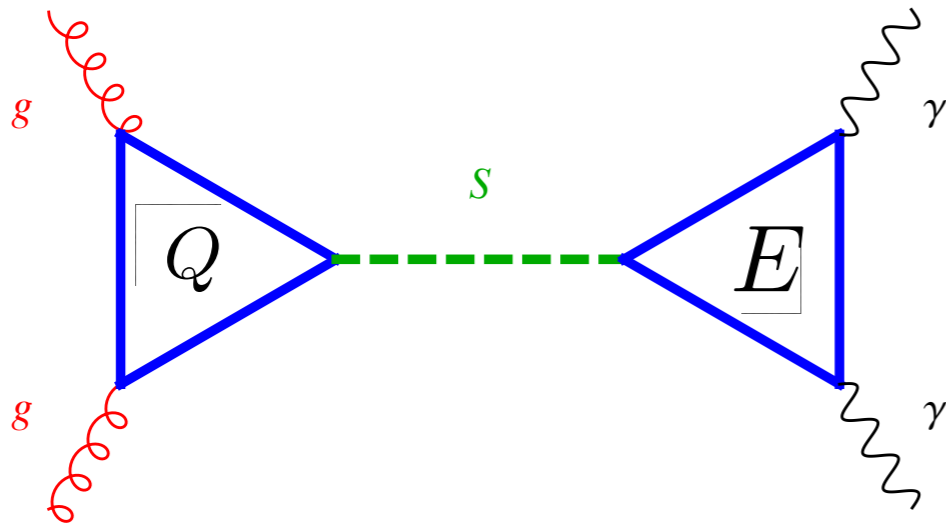


$$\frac{\Gamma_{\gamma\gamma}}{M_S} \frac{\Gamma_{gg}}{M_S} \simeq 4.9 \times 10^{-8} \left( \frac{\Gamma_S/M_S}{0.06} \right)$$

$$\frac{\Gamma_{\gamma\gamma}}{M_S} \frac{\Gamma_{b\bar{b}}}{M_S} \simeq 8.4 \times 10^{-6} \left( \frac{\Gamma_S/M_S}{0.06} \right)$$

# Weakly coupled models

- “Everybody’s model” [1512.04933, 1512.08500 + same mechanism in  $O(100)$  papers]



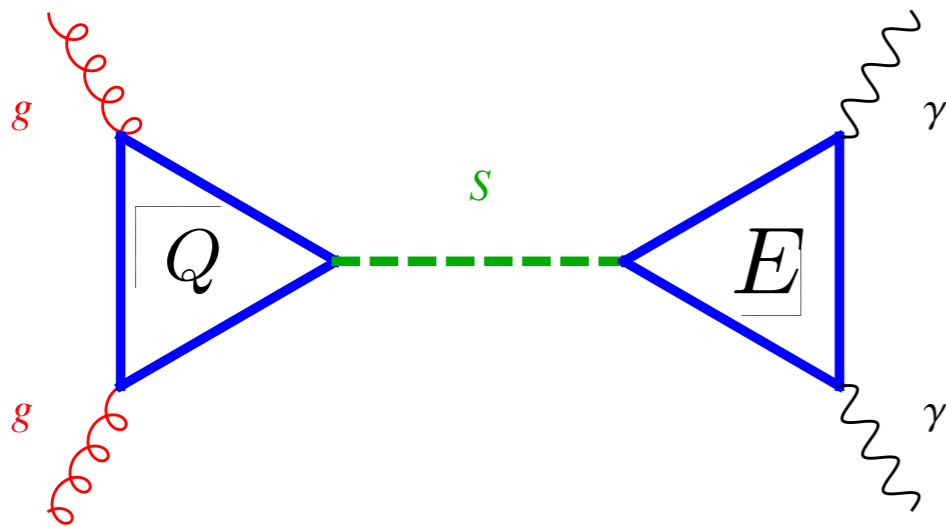
$$Q \sim (3, 1, 0) \times N_Q \quad S \sim (1, 1, 0)$$

$$E \sim (1, 1, Y) \times N_E$$

$$\mathcal{L}_I \supset y_Q S \bar{Q} Q + y_E S \bar{E} E$$

# Weakly coupled models

- “Everybody’s model” [1512.04933, 1512.08500 + same mechanism in  $O(100)$  papers]



$$Q \sim (3, 1, 0) \times N_Q \quad S \sim (1, 1, 0)$$

$$E \sim (1, 1, Y) \times N_E$$

$$\mathcal{L}_I \supset y_Q S \bar{Q} Q + y_E S \bar{E} E$$

- A large di-photon rate is required

$$\frac{\Gamma_{\gamma\gamma}}{M_S} = \frac{\alpha_{\text{EM}}^2}{16\pi^3} |N_E Q_E^2 y_E \sqrt{\tau_E} \mathcal{S}(\tau_E)|^2 \quad \xrightarrow{m_E \simeq 400 \text{ GeV}} \quad \frac{\Gamma_{\gamma\gamma}}{M_S} = 7.8 \times 10^{-8} N_E^2 Q_E^4 y_E^2$$

- Narrow width  $\Gamma_{\gamma\gamma}/M_S \gtrsim 10^{-6} \rightarrow N_E^2 Q_E^4 y_E^2 \gtrsim 10$  ( $\sim 1.5$  for a top-like state)

- Large width  $\Gamma_{\gamma\gamma}/M_S \gtrsim 10^{-4} \rightarrow N_E^2 Q_E^4 y_E^2 \gtrsim 10^3 \rightarrow$  perturbativity issue !

# Unitarity vs. RGE

- RGE arguments often employed to estimate perturbativity in ren. models
  - Landau poles
  - Beta function criterium [e.g. 1512.08500]

$$\mu \frac{d}{d\mu} y = \beta_y \quad \mathcal{A} = y + \beta_y \log \left( \frac{\mu}{E} \right) \quad |\beta_y/y| < 1$$



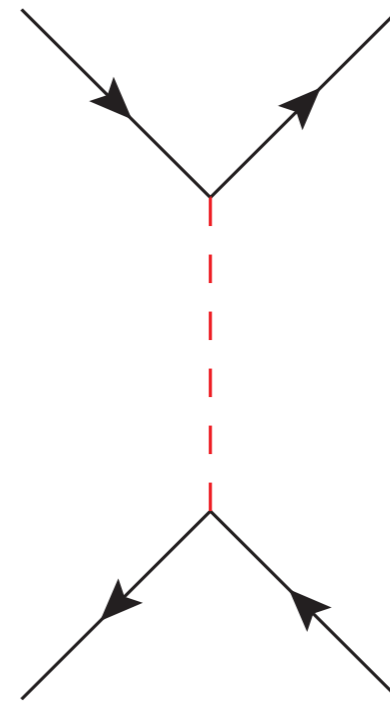
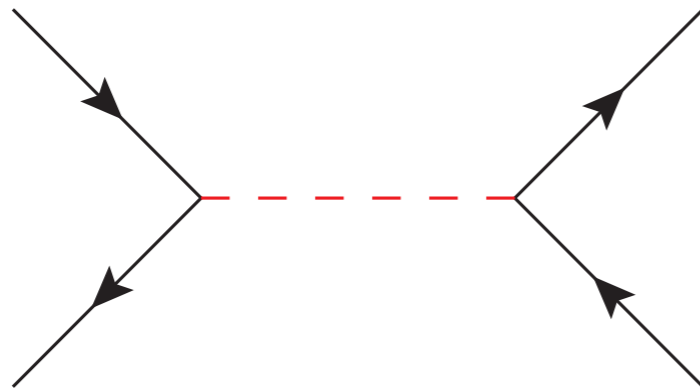
logarithmically sensitive to the UV scale (bounds can be in principle circumvented in UV completions featuring an IR fixed point)

- Unitarity bounds conceptually different
  - no calculations beyond tree level required
  - apply at any  $\sqrt{s}$  above threshold

# Unitarity bounds

- $2 \rightarrow 2$  scatterings of charged mediators  $\psi\bar{\psi} \rightarrow \psi\bar{\psi}$

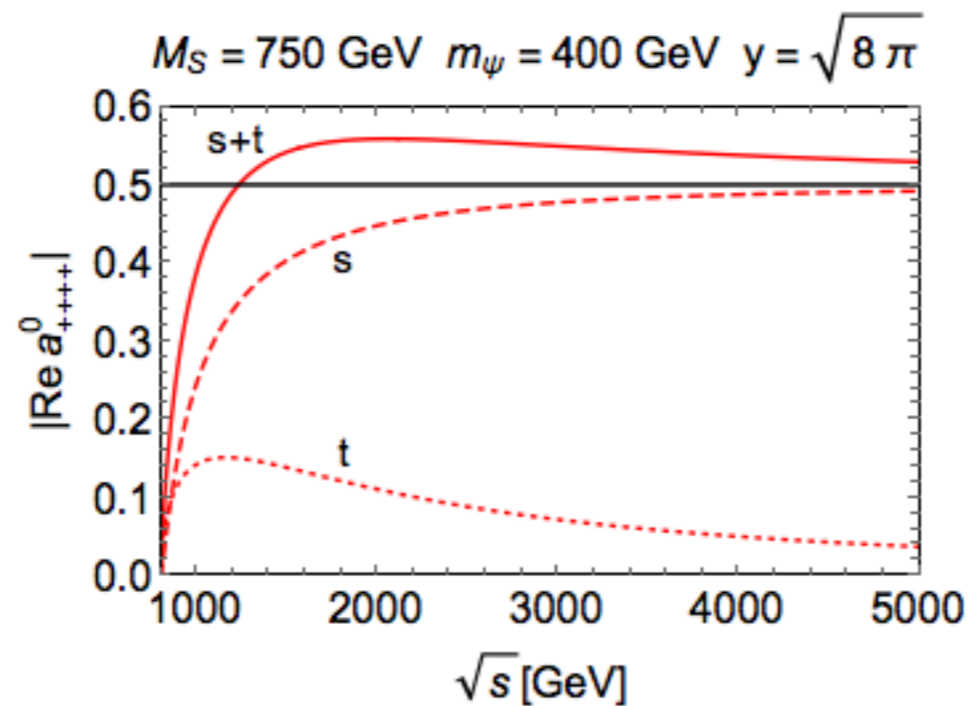
$$\mathcal{L}_I \supset -y S \bar{\psi} \psi \quad \longrightarrow \quad a^0 \simeq -\frac{y^2}{16\pi} \quad \longrightarrow \quad y \lesssim \sqrt{8\pi}$$



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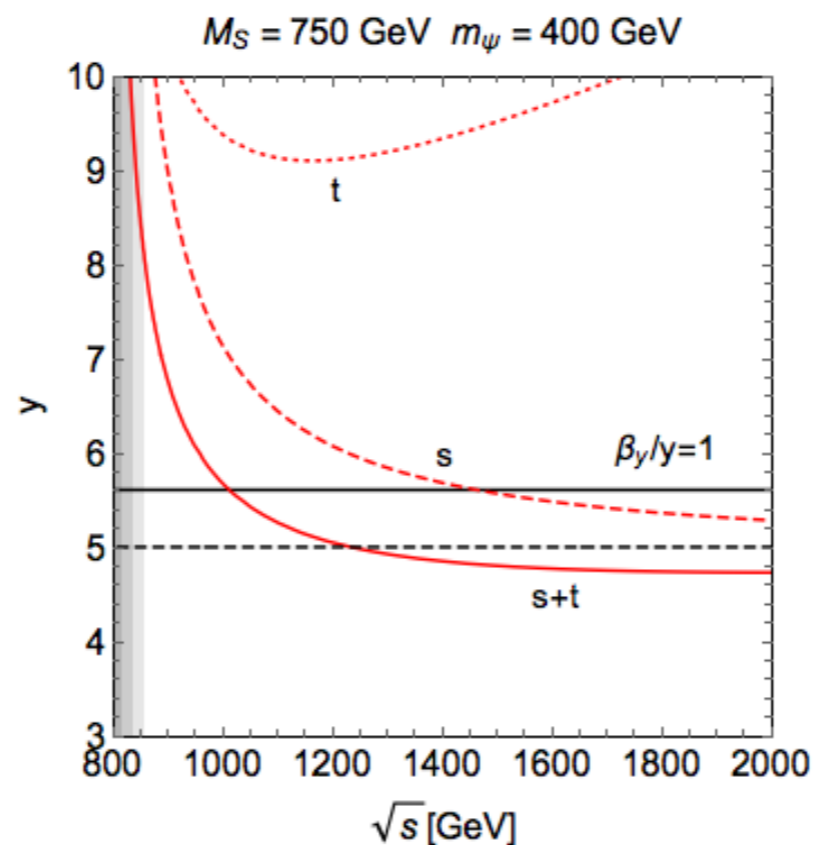
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- $O(1)$  agreement with beta function criterium  $\frac{\beta_y}{y} = \frac{5y^2}{16\pi^2} < 1$  [1512.08500]

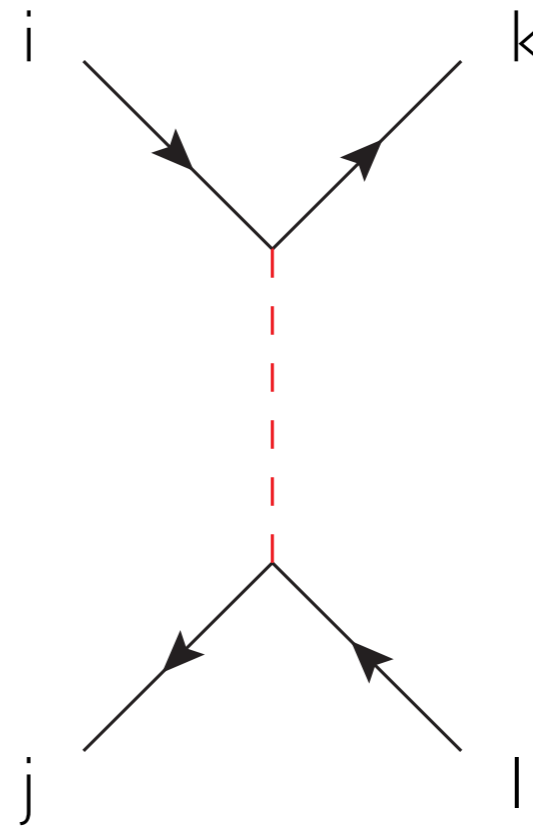
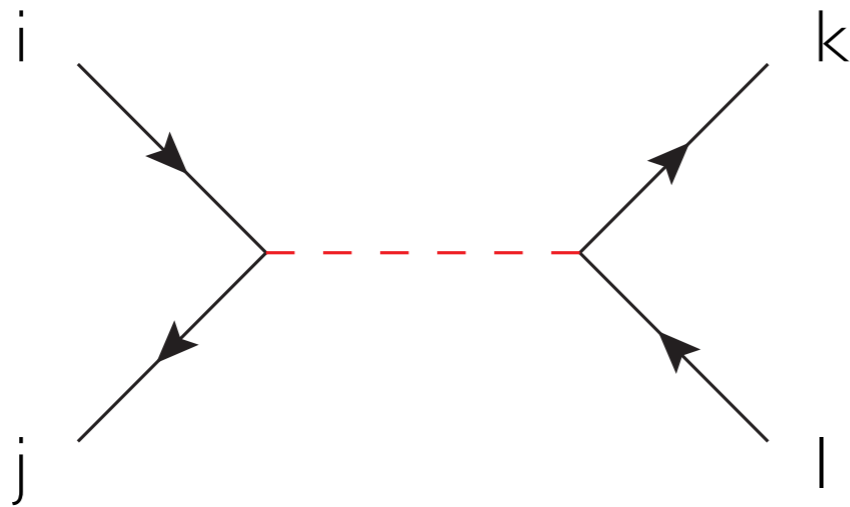
# Generalization in flavor space

- $N$  copies of mediators  $\psi_i$  ( $i = 1, \dots, N$ ) interacting via

$$\mathcal{L}_I \supset -y_{ij} S \bar{\psi}_i \psi_j$$



$$\langle \psi_k \bar{\psi}_l | \psi_i \bar{\psi}_j \rangle = i\mathcal{T}_s \delta_{ij} \delta_{kl} + i\mathcal{T}_t \delta_{ik} \delta_{jl}$$





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- e.g.  $y_{ij} = y \delta_{ij}$  in the mass basis (“everybody’s model”)

 exploit U(N) global symmetry to label the irreducible sectors of the scattering

$$N \otimes \bar{N} = \mathbf{1} \oplus \text{Adj}_N$$

- singlet channel  $|\psi\bar{\psi}\rangle_{\mathbf{1}} = \frac{1}{\sqrt{N}} \sum_i |\psi_i \bar{\psi}_i\rangle \rightarrow {}_{\mathbf{1}}\langle\psi\bar{\psi}|\psi\bar{\psi}\rangle_{\mathbf{1}} = i\mathcal{T}_s N + i\mathcal{T}_t$

- adjoint channel  $|\psi\bar{\psi}\rangle_{\text{Adj}}^A = T_{ij}^A |\psi_i \bar{\psi}_j\rangle \rightarrow {}_{\text{Adj}}^B \langle\psi\bar{\psi}|\psi\bar{\psi}\rangle_{\text{Adj}}^A = i\mathcal{T}_t \delta^{AB}$

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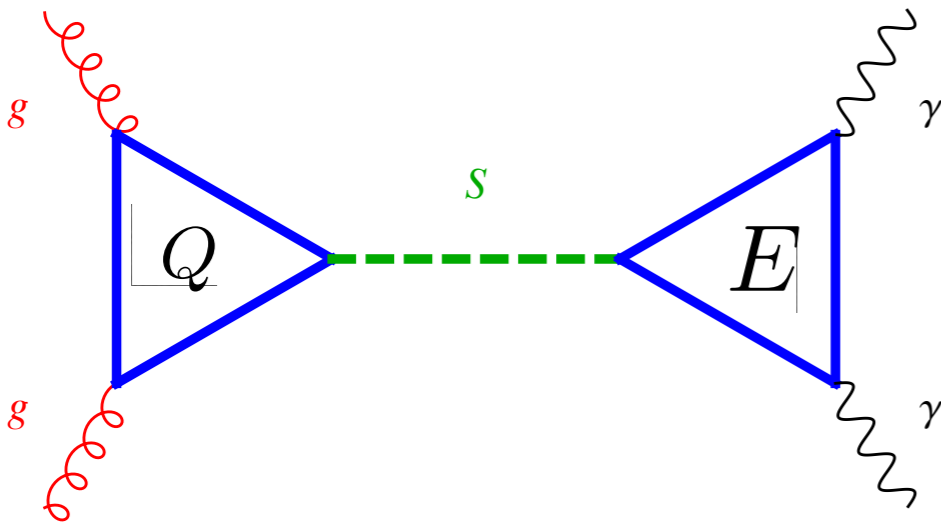
s-channel enhancement  $y^2 \rightarrow N y^2$  (’t Hooft scaling)

# Visualizing the bounds

- 5 parameters:  $y_E, y_Q, N_E, N_Q, Q_E$  ( $m_E = 400$  GeV and  $m_Q = 1$  TeV)

$$\begin{aligned} N_E y_E^2 &< 8\pi \\ 3N_Q y_Q^2 &< 8\pi \end{aligned} \quad \rightarrow \text{unitarity bounds}$$

$$N_E^2 N_Q^2 y_E^2 y_Q^2 Q_E^4 = 2.3 \times 10^5 \left( \frac{\Gamma_S/M_S}{0.06} \right) \quad \rightarrow \text{to fit the signal}$$



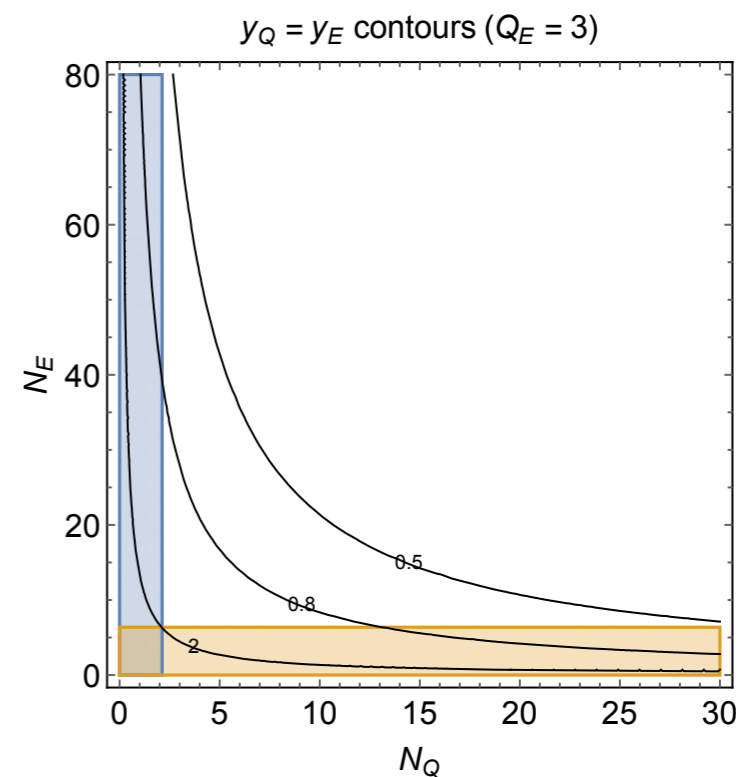
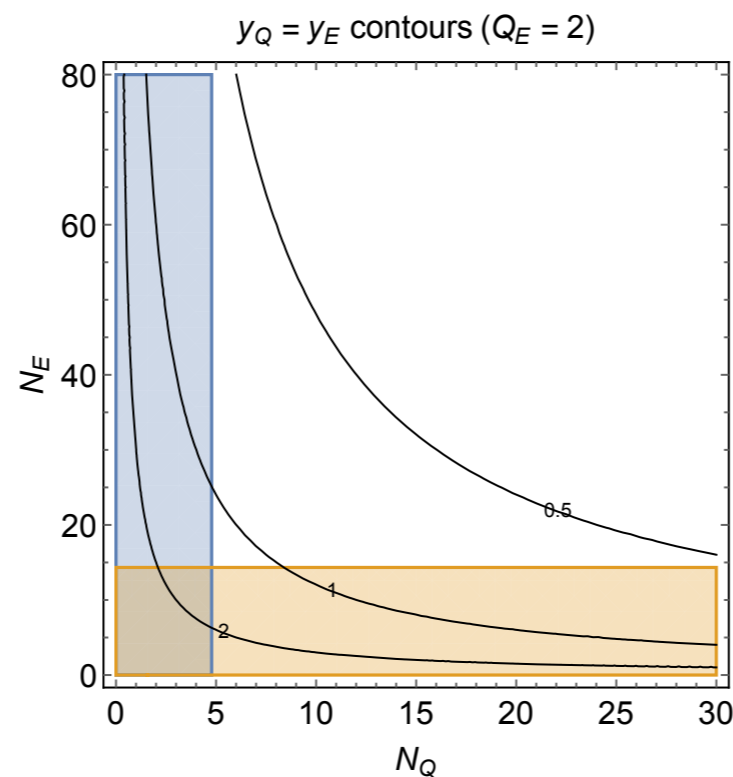
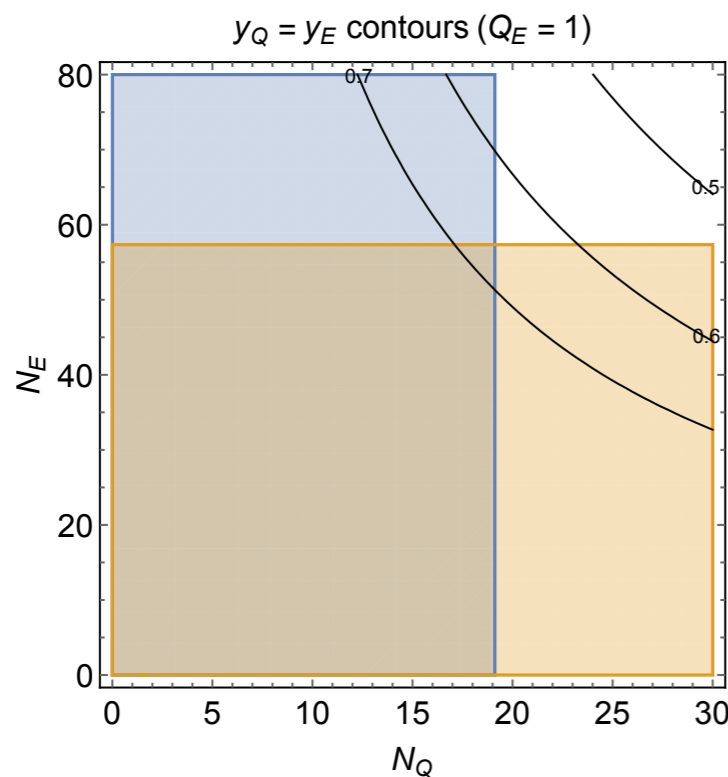
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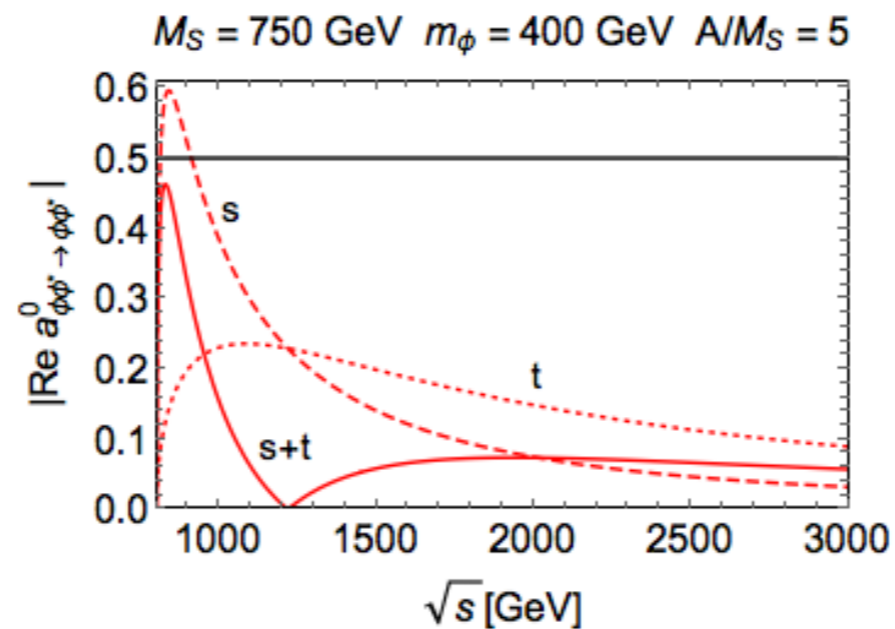


- Large width scenario  $\rightarrow$  requires either exotic EM charges or very large N

# Scalar mediators (gg initiated)

- $2 \rightarrow 2$  scatterings of charged (scalar) mediators  $\phi\phi^* \rightarrow \phi\phi^*$

$$\mathcal{L}_I \supset -AS\phi^*\phi \quad \longrightarrow \quad a_{\phi\phi^* \rightarrow \phi\phi^*}^0 = -A^2 \frac{\sqrt{s(s-4m_\phi^2)}}{16\pi s} \left( \frac{1}{s-M_S^2} - \frac{\log \frac{s-4m_\phi^2+M_S^2}{M_S^2}}{s-4m_\phi^2} \right)$$

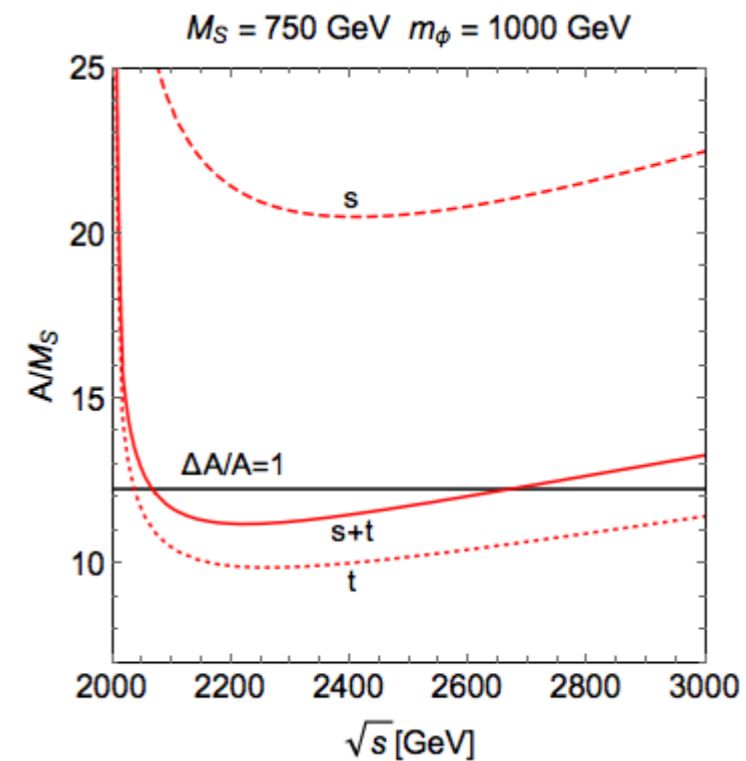
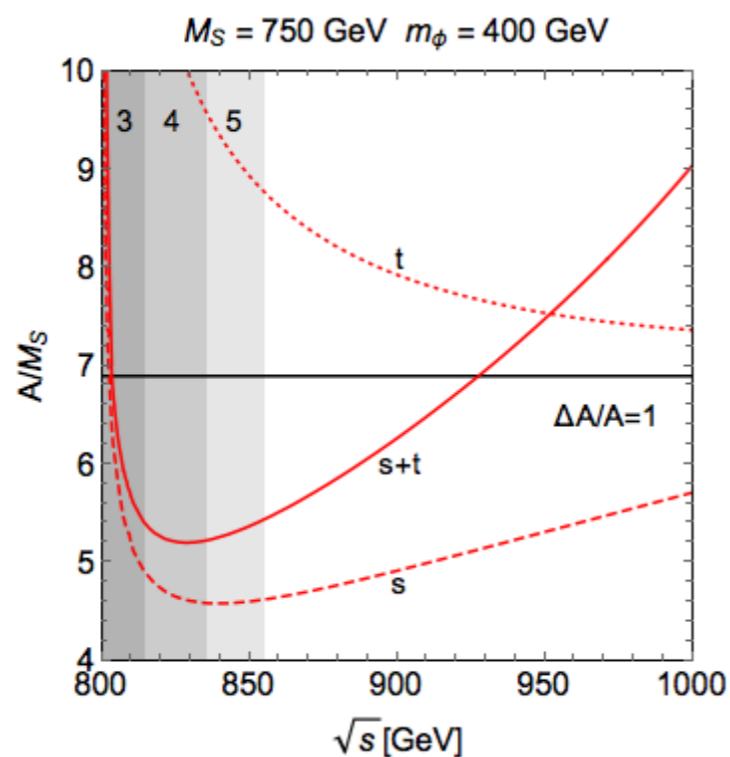


-  $A$  is a relevant coupling  $\rightarrow$  unitarity bounds saturated at low-energy

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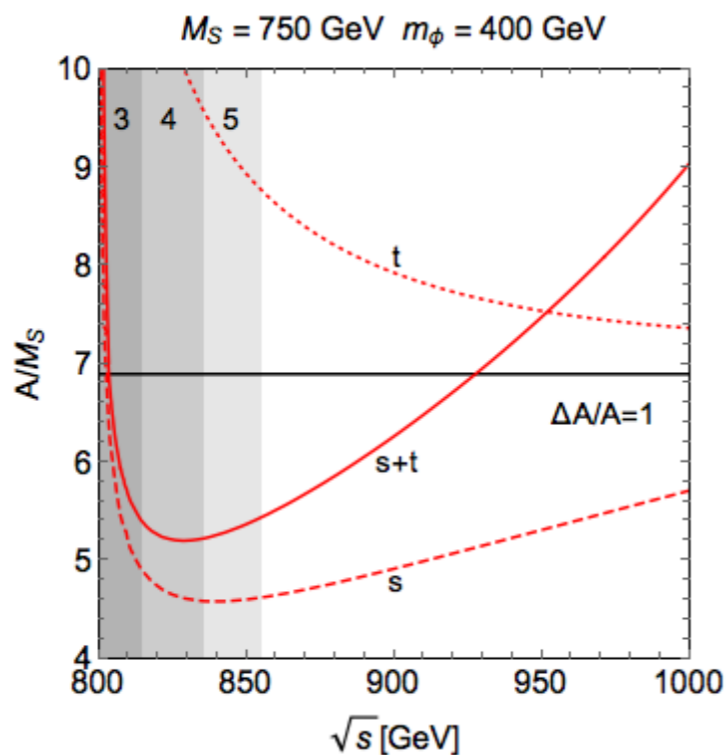


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$$\frac{\left| \frac{i}{s-M_S^2} \right|^2 - \left| \frac{i}{s-M_S^2+iM_S\Gamma_S} \right|^2}{\left| \frac{i}{s-M_S^2} \right|^2} < \Delta$$

$$\alpha = \sqrt{1/\Delta - 1} \quad (\alpha = 3 \rightarrow \Delta = 10\%)$$

-  $A$  is a relevant coupling  $\rightarrow$  unitarity bounds saturated at low-energy

- Width effects important near s-pole singularities  $\alpha = \frac{|s-M_S^2|}{\Gamma_S M_S} \quad (\Gamma_S/M_S = 0.06)$

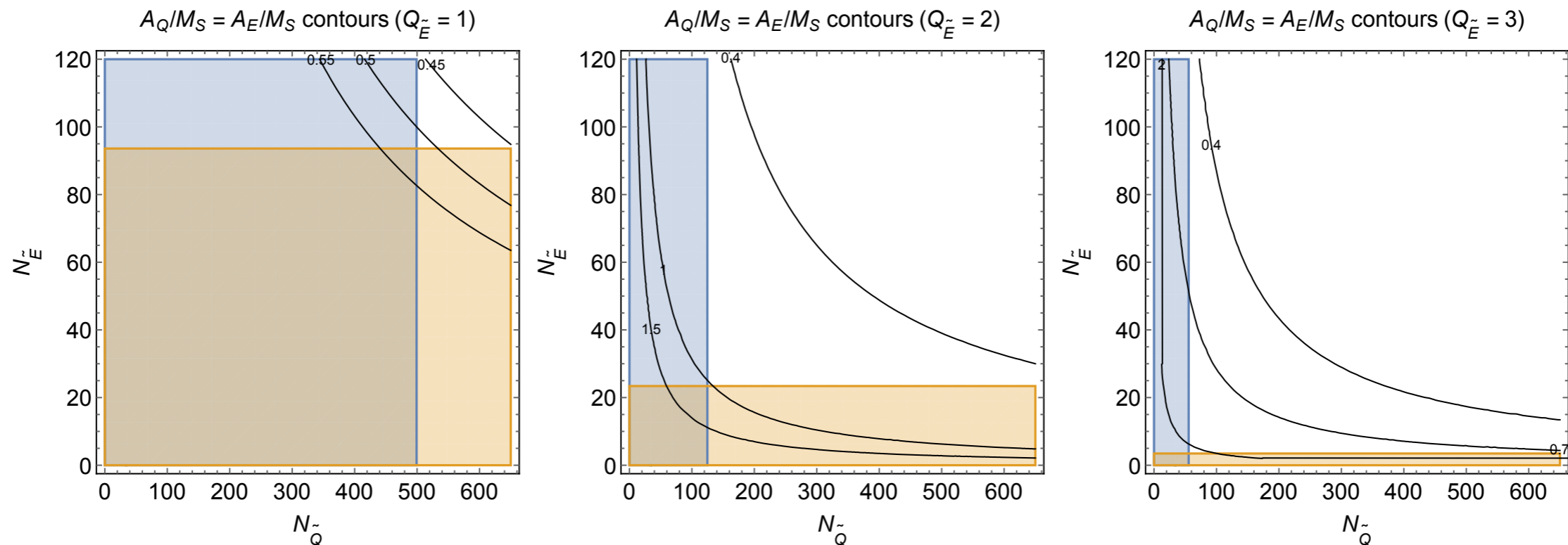
# Visualizing the bounds (scalars)

- Flavor enhancement from s-channel

$$N_{\tilde{E}} \left( \frac{A_E}{750 \text{ GeV}} \right)^2 < 25$$

$$3N_{\tilde{Q}} \left( \frac{A_Q}{750 \text{ GeV}} \right)^2 < 400$$

$$N_{\tilde{E}}^2 N_{\tilde{Q}}^2 \left( \frac{A_E}{750 \text{ GeV}} \right)^2 \left( \frac{A_Q}{750 \text{ GeV}} \right)^2 Q_{\tilde{E}}^4 = 1.6 \times 10^8 \left( \frac{\Gamma_S/M_S}{0.06} \right)$$





# q-qbar initiated

- A vector-like quark mixing with SM quarks, e.g.  $\mathcal{B} \sim (3, 1, -1/3)$

$$\mathcal{L}^{\mathcal{B}-b} = \bar{Q}_3 i \not{D} Q_3 + \bar{b}_R i \not{D} b_R + \bar{\mathcal{B}} i \not{D} \mathcal{B} - (M_{\mathcal{B}} + \tilde{y}_{\mathcal{B}} S) \bar{\mathcal{B}} \mathcal{B} - y_b \bar{Q}_3 H b_R - y_{\mathcal{B}} \bar{Q}_3 H \mathcal{B}_R - \tilde{y}_b \bar{\mathcal{B}}_L S b_R + \text{h.c.}$$

$$\begin{pmatrix} b'_{L,R} \\ \mathcal{B}'_{L,R} \end{pmatrix} = \begin{pmatrix} \cos \theta_{\mathcal{B}b}^{L,R} & \sin \theta_{\mathcal{B}b}^{L,R} \\ -\sin \theta_{\mathcal{B}b}^{L,R} & \cos \theta_{\mathcal{B}b}^{L,R} \end{pmatrix} \begin{pmatrix} b_{L,R} \\ \mathcal{B}_{L,R} \end{pmatrix}$$

$$\mathcal{L}^{\mathcal{B}-b} \ni S \bar{b}' b' \sin \theta_{\mathcal{B}b}^L (\sin \theta_{\mathcal{B}b}^R \tilde{y}_{\mathcal{B}} + \cos \theta_{\mathcal{B}b}^R \tilde{y}_b)$$

$$\theta_{\mathcal{B}b}^R \sim (m_b/m_{\mathcal{B}}) \theta_{\mathcal{B}b}^L$$



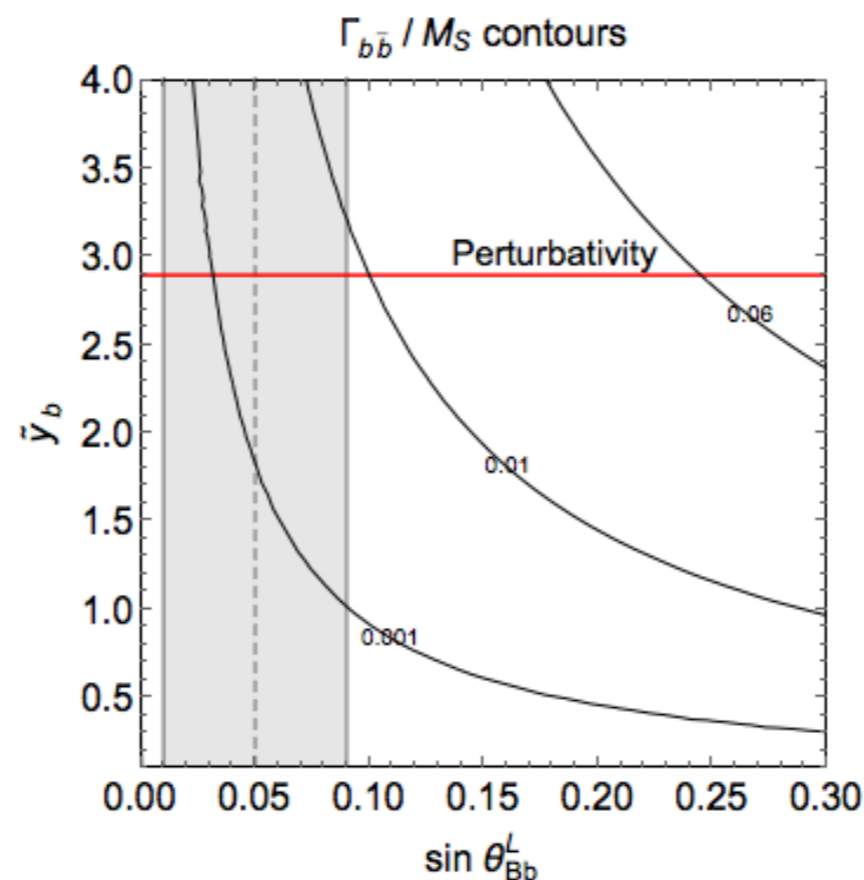
$$\sin \theta_{\mathcal{B}b}^L = 0.05(4)$$

$$\frac{\Gamma_{b\bar{b}}}{M_S} = \frac{3}{8\pi} \sin^2 \theta_{\mathcal{B}b}^L \tilde{y}_b^2 = 3 \times 10^{-4} \left( \frac{\sin \theta_{\mathcal{B}b}^L}{0.05} \right)^2 \tilde{y}_b^2$$

# q-qbar initiated (bounds)

- A vector-like quark mixing with SM quarks, e.g.  $\mathcal{B} \sim (3, 1, -1/3)$

$$\left(\frac{\sin \theta_{\mathcal{B}b}^L}{0.05}\right)^2 \tilde{y}_b^2 = 280 \left(\frac{\Gamma_S/M_S}{0.06}\right) \left(\frac{\Gamma_{\gamma\gamma}/M_S}{10^{-4}}\right)^{-1} \quad \tilde{y}_b^2 < \frac{8\pi}{3}$$



- $S \rightarrow b\bar{b}$  cannot saturate the large width in the perturbative setup