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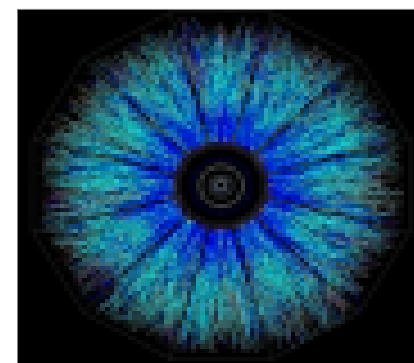


# **Proton-proton correlations**

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**International Conference on New Frontiers in Physics  
Kolumbari, Crete – Greece - 2016**





# Introduction

# 1) Motivation

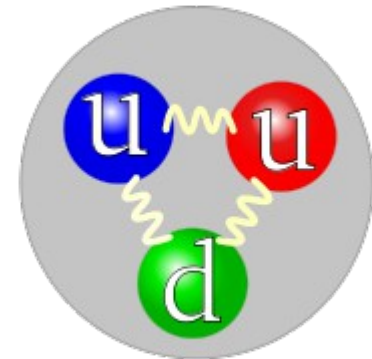
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So far, the knowledge on nuclear force was derived from studies made on **nucleon or / and nuclei**.

Nuclear force between **antinucleons** was not studied so far.

The knowledge of interaction between two anti-protons is **fundamental** to understand the properties of more sophisticated antinuclei.

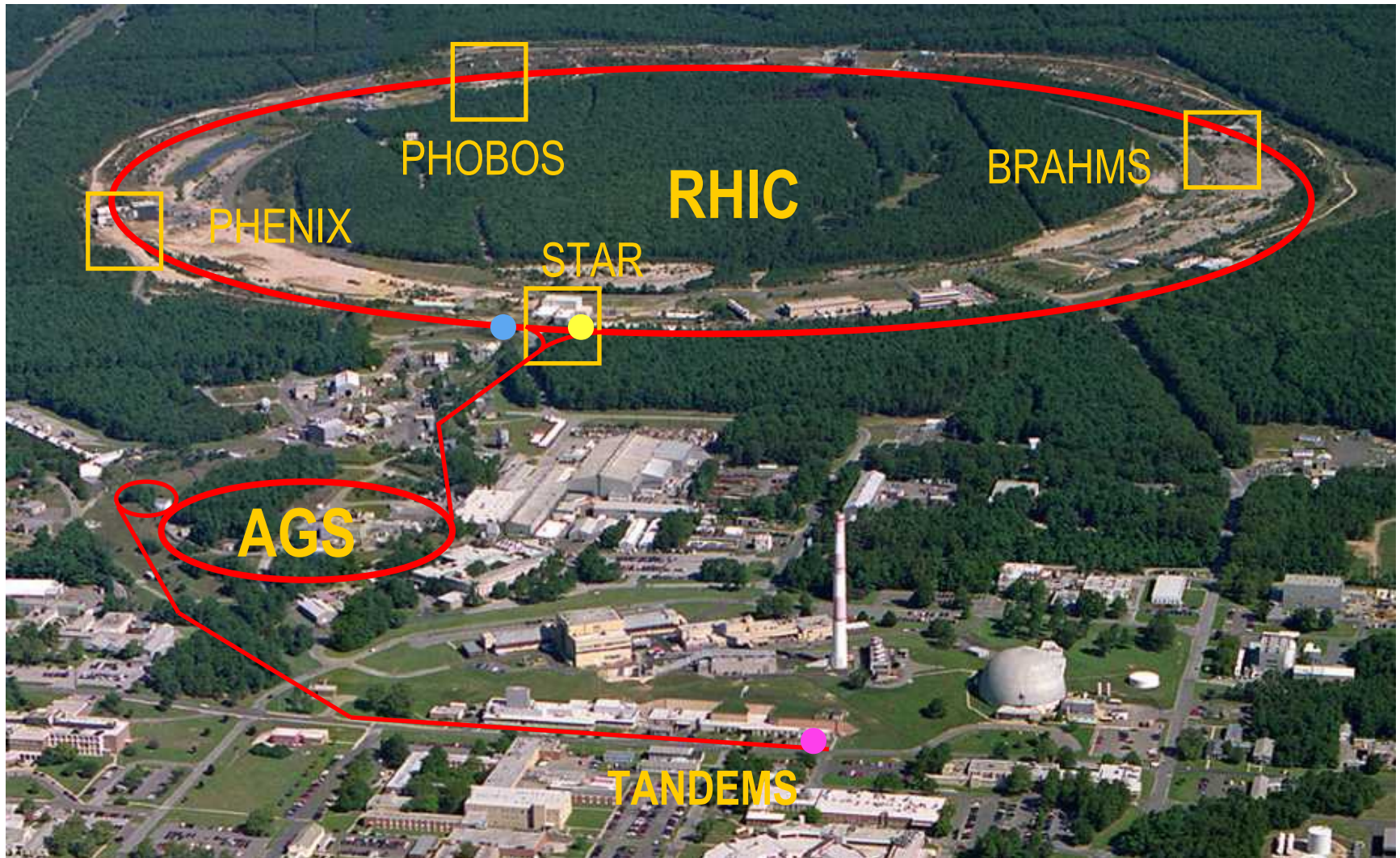
**RHIC** has the excellent capability to conduct such studies.



Nature 527, 345–348(2015)

## 2) Relativistic Heavy Ion Collider (RHIC)

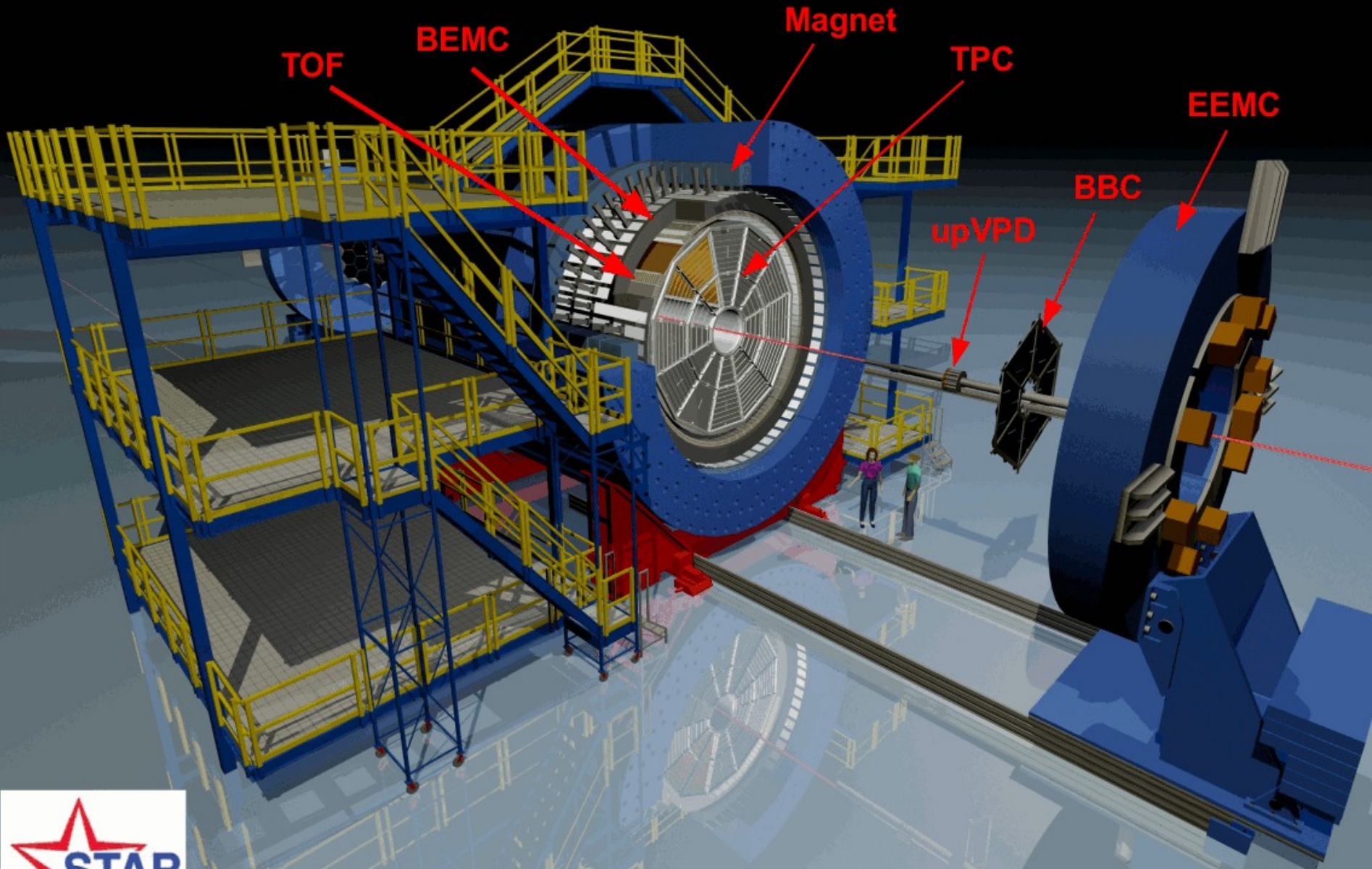
Brookhaven National Laboratory (BNL), New York



- 2 concentric rings of 1740 superconducting magnets
- 3.8 km circumference



# 3) The Solenoidal Tracker At RHIC



# 4) Few words about femtoscopy

## Single- and two- particle distributions

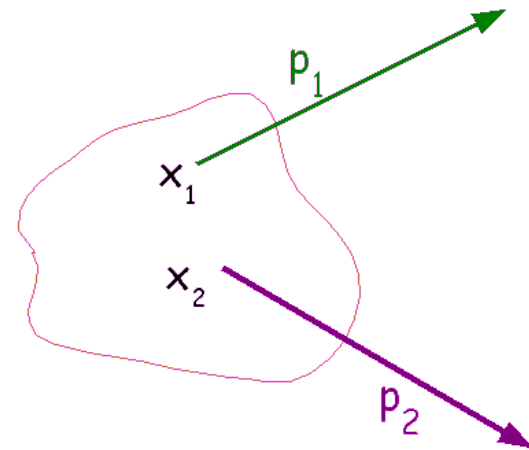
$$P_1(p) = E \frac{dN}{d^3p} = \int d^4x S(x, p)$$

**S(x,p)** – emission function: the distribution of source density probability of finding particle with **x** and **p**

$$P_2(p_1, p_2) = E_1 E_2 \frac{dN}{d^3p_1 d^3p_2} = \int d^4x_1 S(x_1, p_1) d^4x_2 S(x_2, p_2) \Phi(x_2, p_2 | x_1, p_1)$$

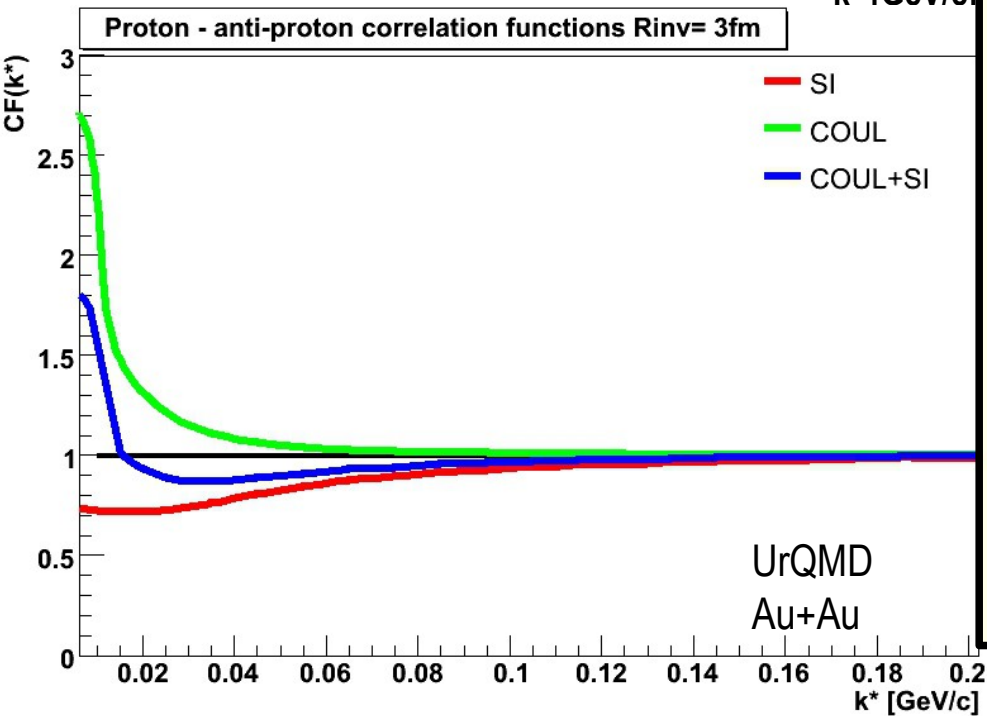
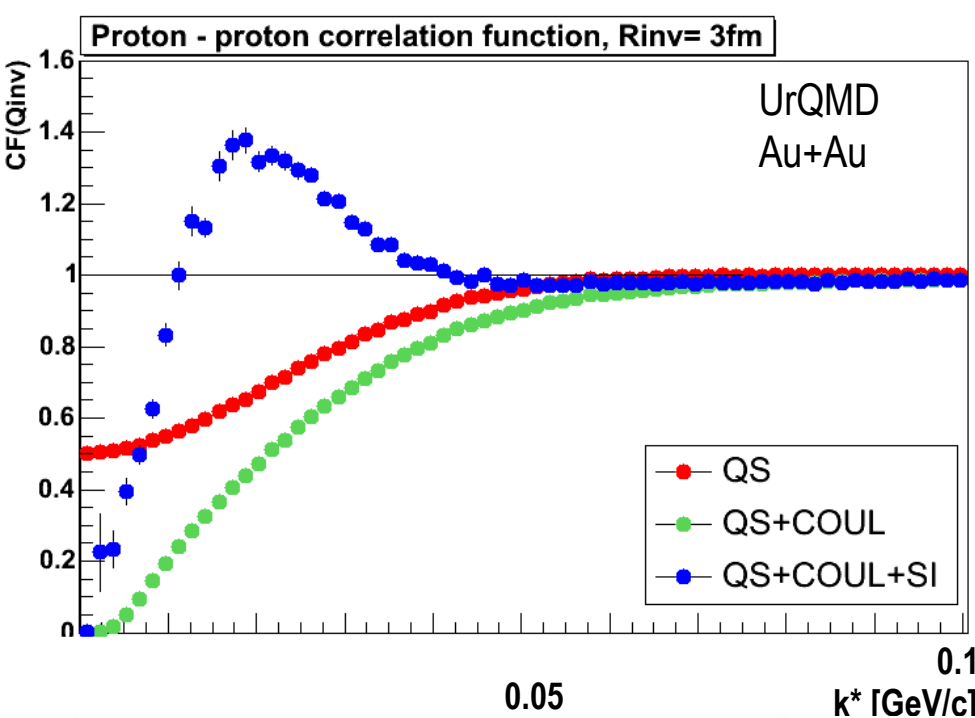
## The correlation function

$$C(p_1, p_2) = \frac{P_2(p_1, p_2)}{P_1(p_1)P_1(p_2)}$$



$$C_{corrected} = \frac{C_{measured}(k^{star}) - 1}{PairPurity(k^{star})} + 1$$

# 5) Proton- (anti)proton correlations



## Identical baryon- baryon

- Quantum Statistics- QS

- Final State Interactions- FSI

- Coulomb

- Strong

## Nonidentical baryon- (anti)baryon

- Final State Interactions- FSI

- Coulomb

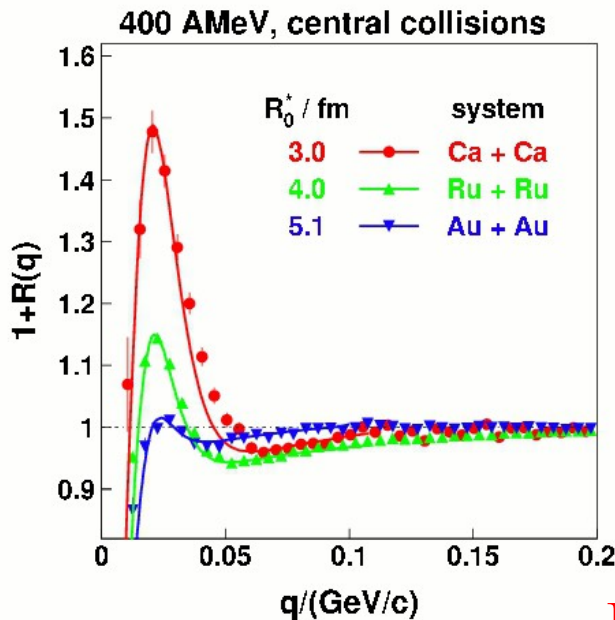
- Strong



# Results

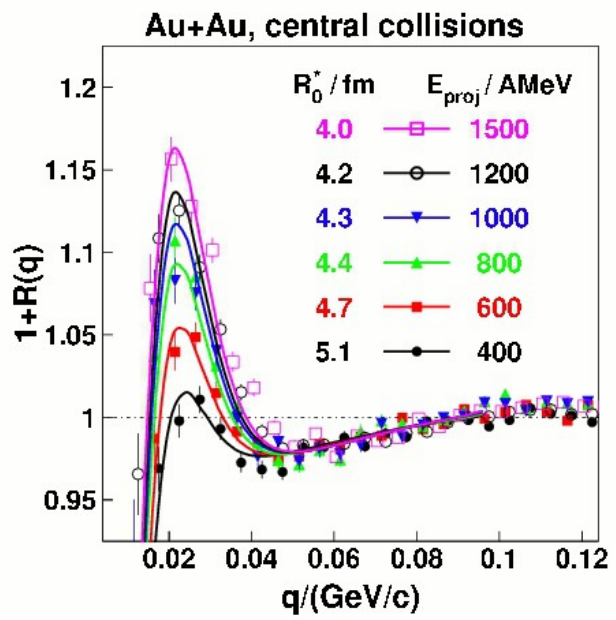
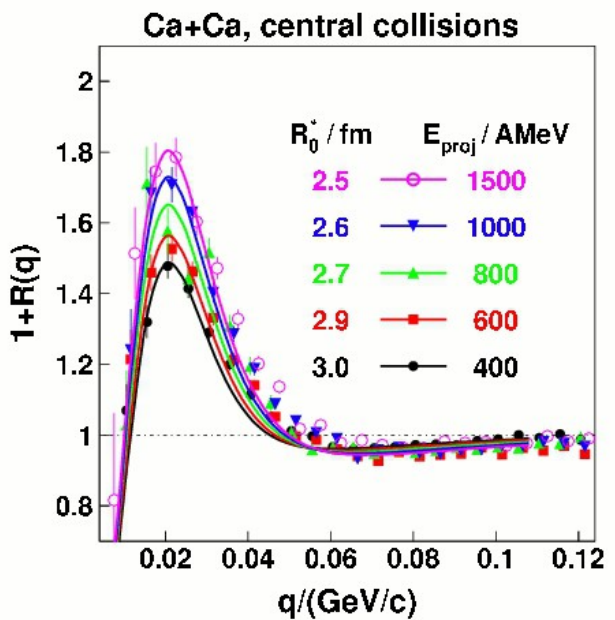


# 1) Results of p-p correlations from lower energies

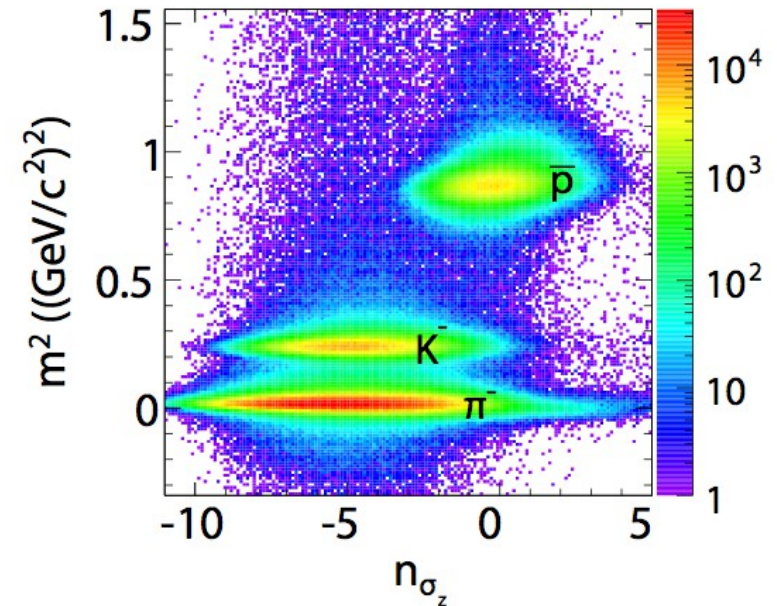
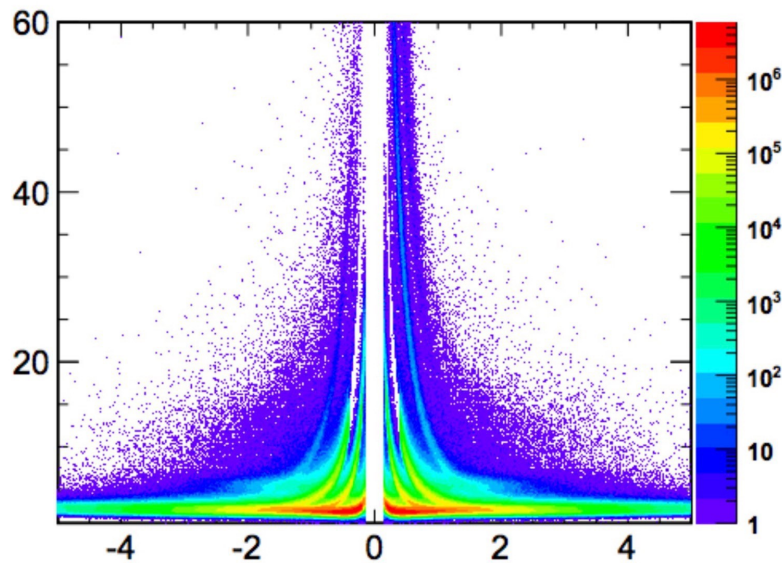


SIS → AGS/SPS → RHIC

Eur.J.Phys.A23:271-278,2005



## 2) Particle Identification

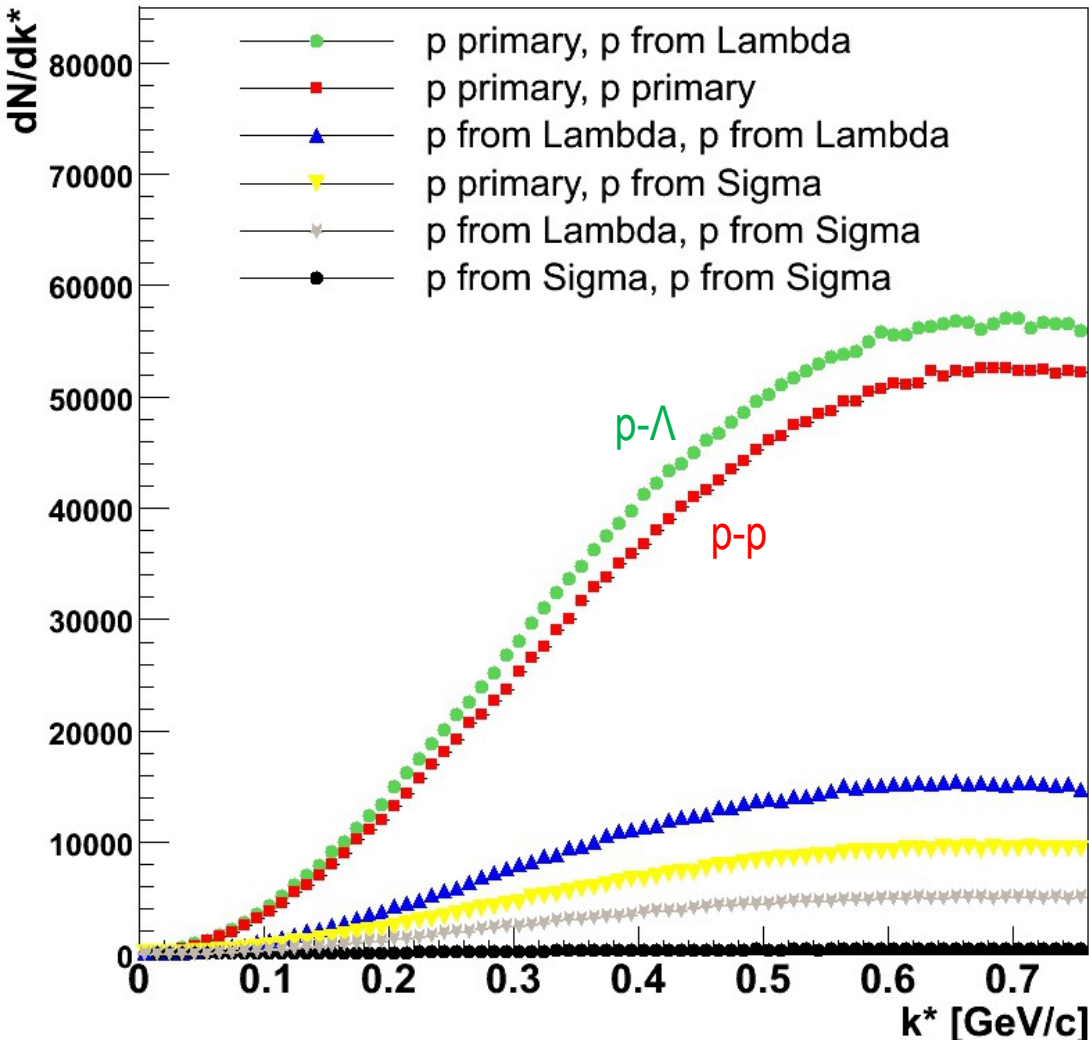


$m^2$  vs  $n_{\sigma_p}$ : Negative Charge

- TPC and TOF for the particle identification.
- The purity for anti-proton over 99%.

# 3) Proton femtoscopy @ 200 GeV – contribution to the measured correlation function

$$CF_{true}(k_{star}) = \sum_{x,y=p,\Lambda,\Sigma} CF_{x-y}(k_{star}) F_{x-y}(k_{star})$$



$$F_{x-y}(k_{star}) = \frac{f_{x-y}(k_{star})}{\sum f_{i,j}(k_{star})}$$

$$x,y = [p,\Lambda,\Sigma]$$

weak decay channels of interest:

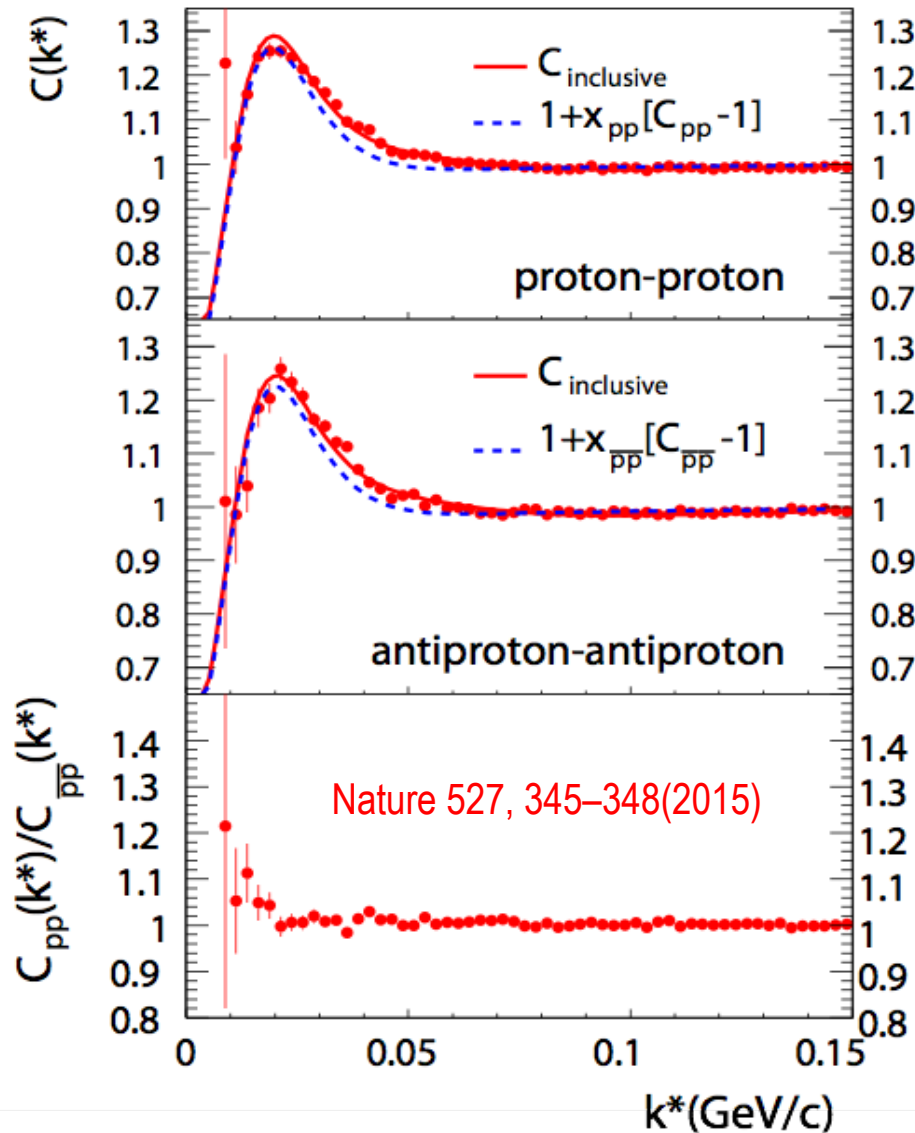
$$\Lambda \rightarrow p + \pi, \Lambda_{bar} \rightarrow p_{bar} + \pi^+$$

$$\Sigma^+ \rightarrow p + \pi^0, \Sigma^+_{bar} \rightarrow p_{bar} + \pi^0$$

**THERMal heavy IoN  
generATOR (Broniowski,  
Florkowski, Kisiel, Tałuc:  
nucl-th/0504047)**

# 4) Correlation functions

Fit



Fit results:

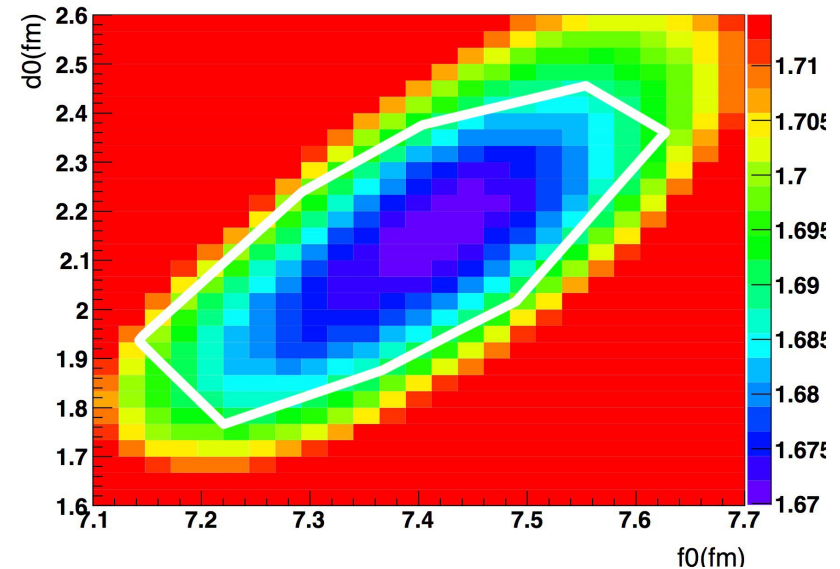
p-p CF,

$R=2.75 \pm 0.01 \text{ fm}$ ; NDF = 1.66;

pbar-pbar CF,

$R=2.80 \pm 0.02 \text{ fm}$ ,  $f_0=7.41 \pm 0.19 \text{ fm}$ ,

$d_0=2.14 \pm 0.27 \text{ fm}$ ; NDF=1.61



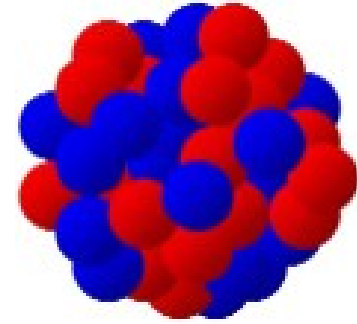


## 5) Parameters: $f_0$ and $d_0$

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The scattering length  $f_0$ : describes low-energy scattering.

The elastic cross section,  $\sigma_e$ , (at low energies) determined solely by the scattering length,  $\lim_{k \rightarrow 0} \sigma_e = 4\pi f_0^2$



$d_0$  - the effective range of strong interaction between two particles.

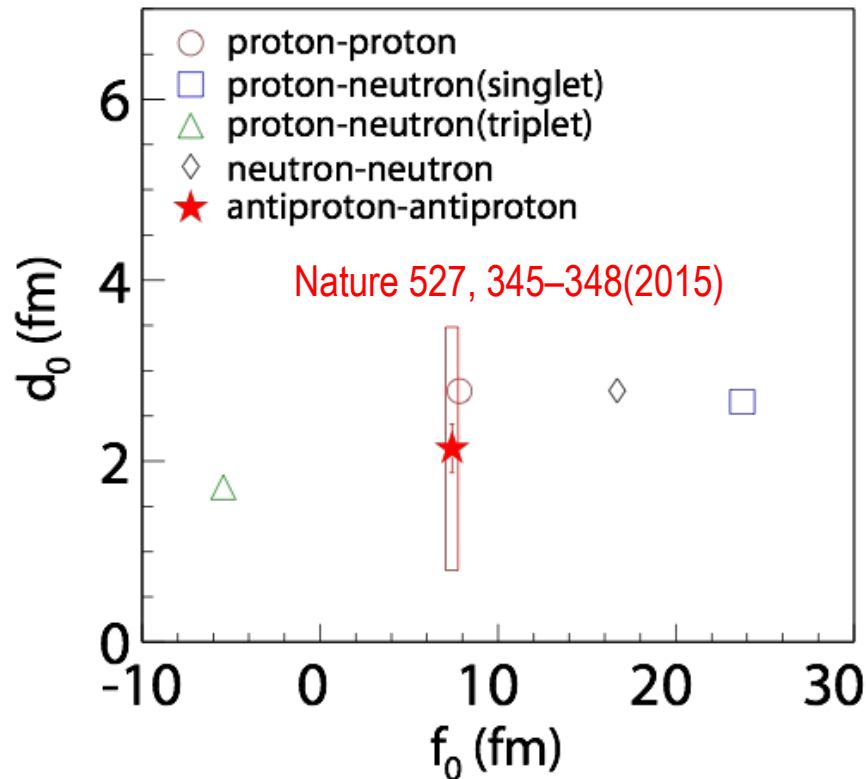
It corresponds to the range of the potential in an extremely simplified scenario the square well potential.

- $f_0$  and  $d_0$  - two important parameters in strong interaction between two particles.

- The part  $C_{pp}(k^*; R_{pp})$  in the equation we used to fit the data is calculated based on  $f_0$  and  $d_0$ .

# 5) $f_0$ and $d_0$ for antiproton-antiproton

•



- $f_0$  and  $d_0$  for the antiproton-antiproton interaction consistent with parameters for the proton-proton interaction.
- Descriptions of the interaction among antimatter (based on the simplest systems of anti-nucleons).
- A quantitative verification of Matter-antimatter symmetry in context of the forces responsible for the binding of (anti)nuclei.

# 6) Strange baryon correlations (including $\Lambda$ hyperons)

p $\Lambda$  correlations:

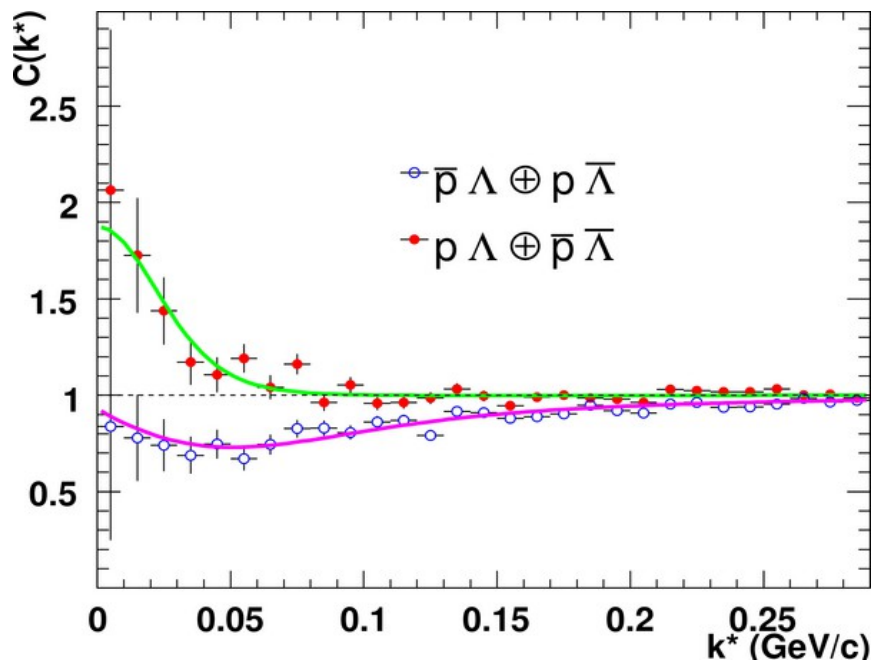
sensitive to the Strong FSI only

$\Lambda\Lambda$  correlations:

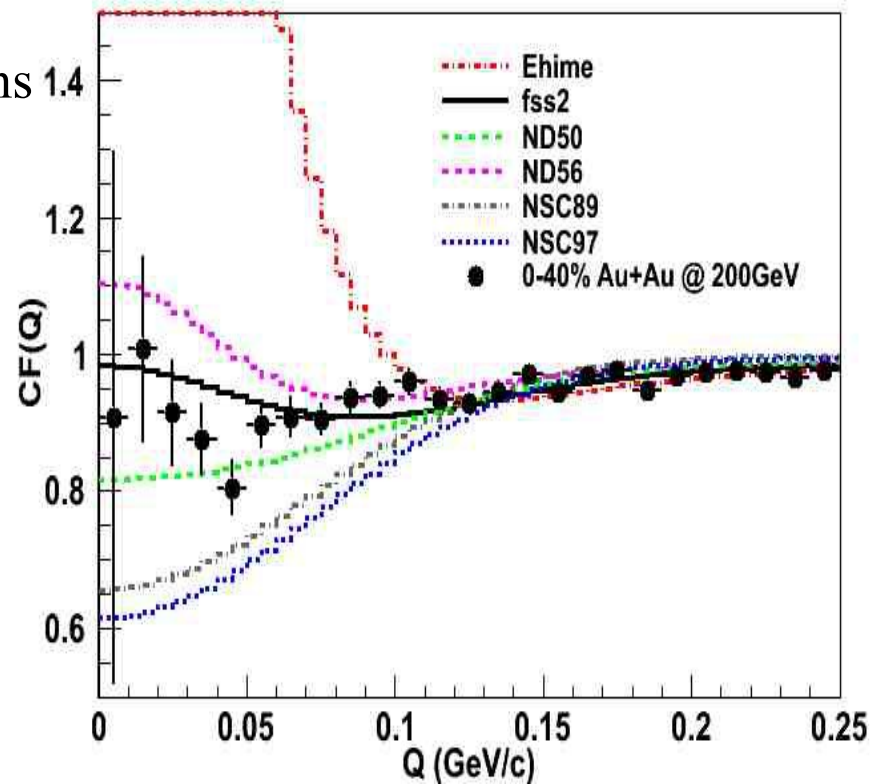
sensitive to the Quantum Statistic effects and Strong FSI

$\Lambda\Lambda$  and p $\Lambda$  correlations:

contain contribution of Residual Correlations



System	$r_0$ (fm)
$p - \Lambda$	$2.97 \pm 0.34_{-0.25}^{+0.19} \pm 0.2$
$\bar{p} - \bar{\Lambda}$	$3.24 \pm 0.59_{-0.14}^{+0.24} \pm 0.2$
$p - \Lambda \oplus \bar{p} - \bar{\Lambda}$	$3.09 \pm 0.30_{-0.25}^{+0.17} \pm 0.2$
$\bar{p} - \Lambda$	$1.56 \pm 0.08_{-0.14}^{+0.10} \pm 0.3$
$p - \bar{\Lambda}$	$1.41 \pm 0.10 \pm 0.11 \pm 0.3$
$\bar{p} - \Lambda \oplus p - \bar{\Lambda}$	$1.50 \pm 0.05_{-0.12}^{+0.10} \pm 0.3$





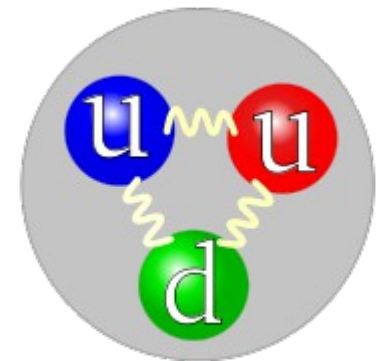
# Conclusions & Summary



# Summary

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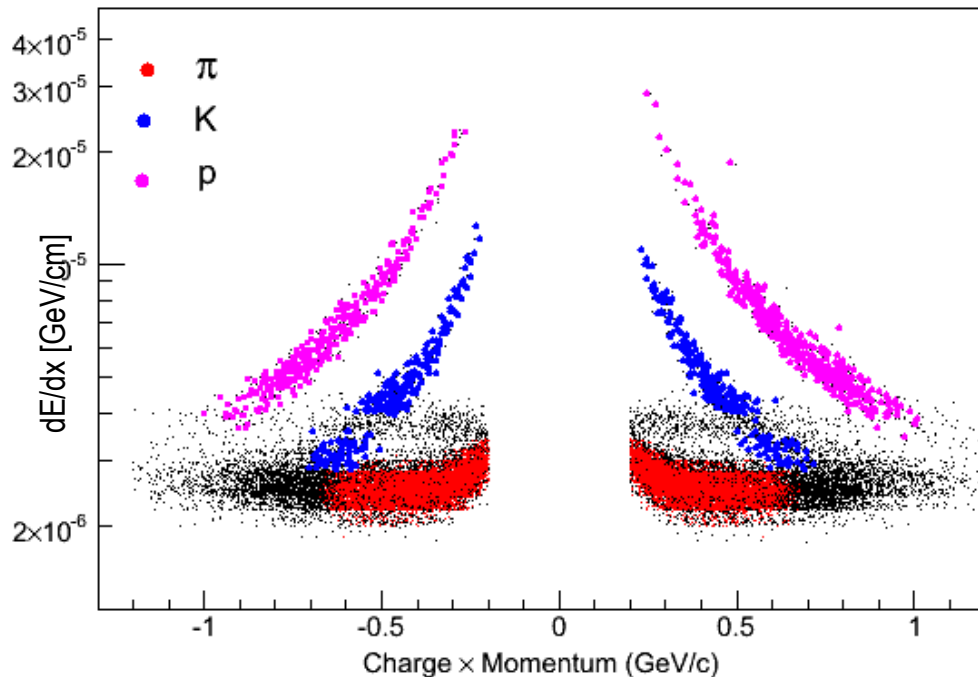
- Result of antiproton-antiproton correlation function from  $\sqrt{s_{NN}} = 200\text{GeV}$  Au+Au collisions shown
- Parameters  $f_0, d_0$  extracted
- The interaction between two antiprotons attractive
- Direct information on interaction between two anti-protons fundamental to understand the structure and properties of more complex antinuclei
- More detailed studies started



**Thank you!**

# Analysed data, particle identification - PID

Au+Au 200 GeV 70-80%



$$\frac{-dE}{dx} = \frac{4\pi}{m_e c^2} \frac{nz^2}{\beta^2} \frac{e^2}{4\pi\epsilon_0} \left[ \ln \frac{2m_e c^2 \beta^2}{I(1-\beta^2)} - \beta^2 \right]$$

E- energy

x- distance

$\beta=v/c$  (v- particle velocity,

c- speed of light)

$m_e$  - electron mass

z- particle charge

n – density of e- inside medium

$n=N_A Z\rho/A$

$N_A$  - Avogadro's number

A, Z- atomic and mass numbers

$\rho$  – medium density

I- ionization potential

Analysed data:

3 centrality classes (the percentage of the total hadronic cross-section of the collision):

0-10%

10-30%

30-80%

$\sqrt{s_{NN}} = 39$  GeV: 96 M

$\sqrt{s_{NN}} = 200$  GeV: 112 M

Selected protons and antiprotons:

$p \in [0.4, 3.0]$  GeV/c

$p_T \in [0.4, 2.5]$  GeV/c

$\eta \in [-0.5, 0.5]$

# Correlation Function

$$CF(k^*) = \frac{\sum_{pair} \delta(k_{pair}^* - k^*) w(k^*, r^*)}{\sum_{pair} \delta(k_{pair}^* - k^*)}$$

$$w(k^*, r^*) = |\psi_{-k^*}^{S(+)}(r^*) + (-1)^S \psi_{k^*}^{S(+)}(r^*)|^2 / 2$$

$$\psi_{-k^*}^{S(+)}(r^*) = e^{i\delta_c} \sqrt{A_c(\eta)} [e^{-ik^* r^*} F(-i\eta, 1, i\xi) + f_c(k^*) \frac{\tilde{G}(\rho, \eta)}{r^*}]$$

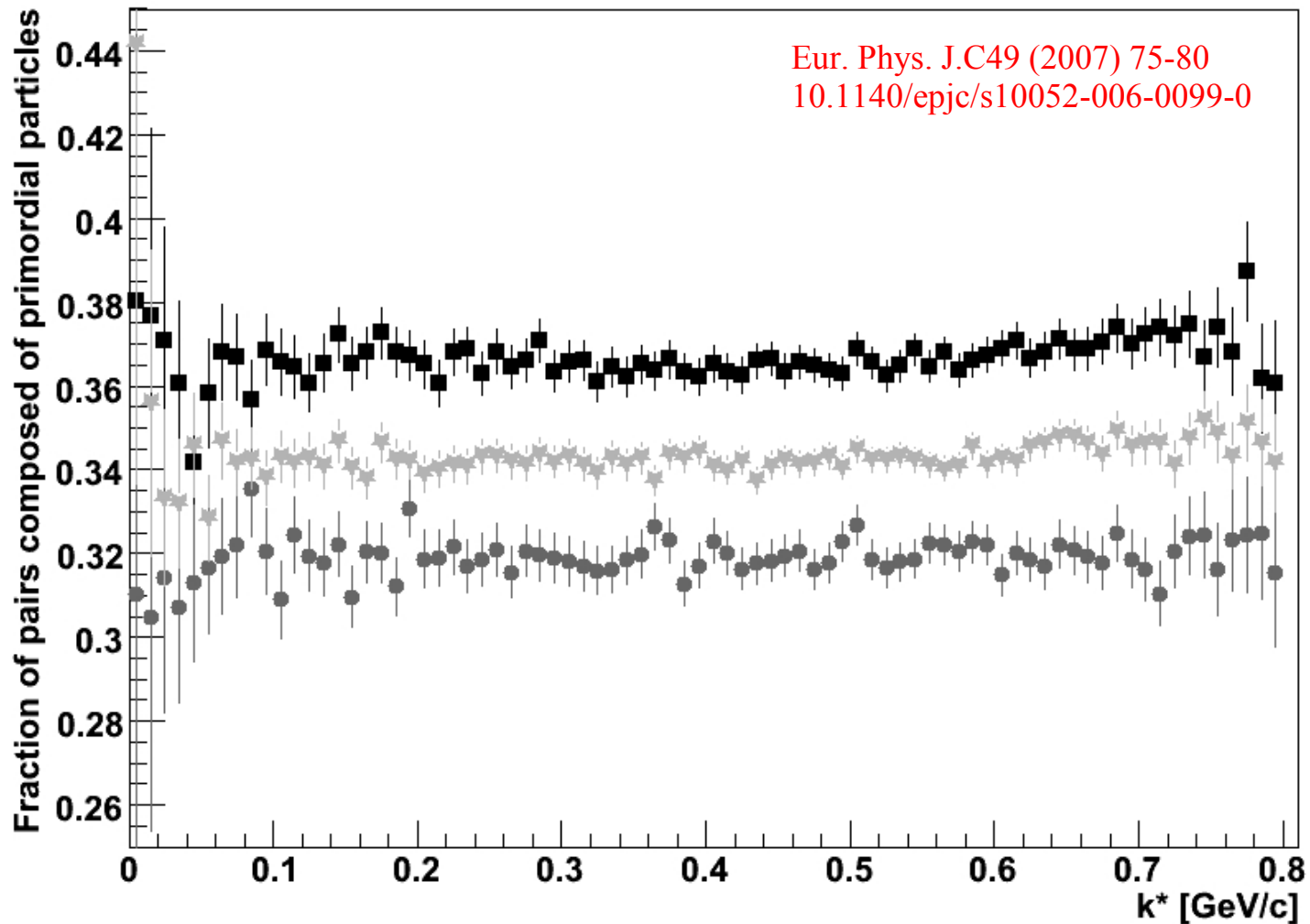
$$f_c(k^*) = \left[ \frac{1}{f_0} + \frac{1}{2} d_0 k^{*2} - \frac{2}{a_c} h(k^* a_c) - ik^* A_c(k^*) \right]^{-1}$$

$$A_C(k^*) = (2\pi/k^* a_c) \frac{1}{\exp(2\pi/k^* a_c) - 1}, \quad h(x) = \frac{1}{x^2} \sum_{n=1}^{\infty} \frac{1}{n(n^2 + x^2)} - C + \ln|x|,$$

and  $\tilde{G}(\rho, \eta) = \sqrt{A_c(k^*)} (G_0(\rho, \eta) + iF_0(\rho, \eta))$  is a combination of regular ( $F_0$ ) and singular ( $G_0$ ) s-wave Coulomb functions.



### 3) Proton femtoscopy @ 200 GeV – - fractions of pure p-p pairs from Therminator



Eur. Phys. J.C49 (2007) 75-80  
10.1140/epjc/s10052-006-0099-0

Therminator,  
Au+Au @ 200 GeV

MEASURED  
 $p$ - $\Lambda$  and  $\bar{p}$ - $\Lambda$

Phys. Rev. C 74  
 (2006) 64906

CF( $k^*$ )

kinematic  
 dependencies  
 of  $\Lambda$  decay

Eur. Phys. J.C49 (2007) 75-80  
 10.1140/epjc/s10052-006-0099-0

$k^*_{p-\Lambda}$  [GeV/c]

The estimation of  $p$ - $\Lambda$   
 residual correlation

$$\sum_{k_{p-\Lambda}^{star}} CF_{p-\Lambda}^{meas}(k_{p-\Lambda}^{star}) W(k_{p-p}^{star}, k_{p-\Lambda}^{star})$$

CF( $k^*$ )

RESIDUAL  
 $p$ - $\Lambda$  and  $\bar{p}$ - $\Lambda$

$k^*_{p-p}$  [GeV/c]

