

# R-axion:

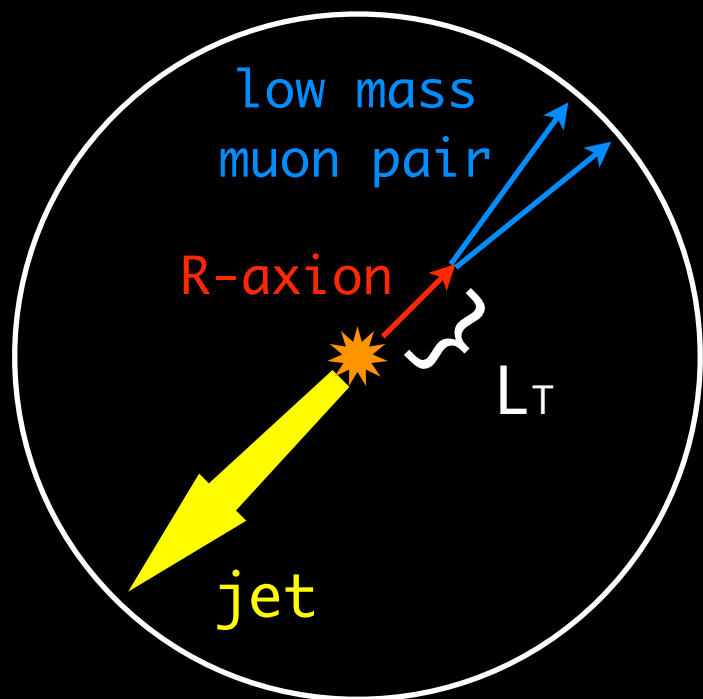
A New LHC physics signature involving muon pairs

Nov.12th Atlas Forum  
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Arxiv:0810.5773

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# Introduction



R-axion:  $m_a = 0(100)\text{MeV}$

$c\tau = 0(1)\text{ps}$

Mainly decays into a muon pair

Production cross section:

$\sigma = 0(10)\text{fb}$  ( $p_T > 100\text{GeV}$ ) at the LHC

Can we detect the R-axion by searching for a displaced vertex at the LHC?

# Outline

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## • Theoretical Background

- ★ R-symmetry and R-axion
- ★ R-axion properties
- ★ Constraints

## • R-axion at LHC

- ★ R-axion production at LHC
- ★ R-axion reconstruction
- ★ Background Estimation

# R-symmetry and R-axion

## • What is R-symmetry?

The R-symmetry is a U(1) symmetry under which fields in the same supermultiplet rotate differently.

ex) If we assign R-charge  $Q_q$  to a quark squark multiplet

$$\Phi_q = (\tilde{q}, q, F_q)$$

$Q_q \qquad Q_q - 1 \qquad Q_q - 2$

The R-charge of the gauginos is uniquely fixed to 1.

$$W_\alpha = (\lambda_\alpha, F_{\mu\nu}, D)$$

$1 \qquad 0 \qquad 0$

# R-symmetry and R-axion

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- How is the R-symmetry important?

We need to break SUSY to realize the Standard Model



SUSY breaking models require R-symmetry  
(or non-generic superpotential) Nelson & Seiberg '93



The model construction beyond the SSM  
often involves the R-symmetry!

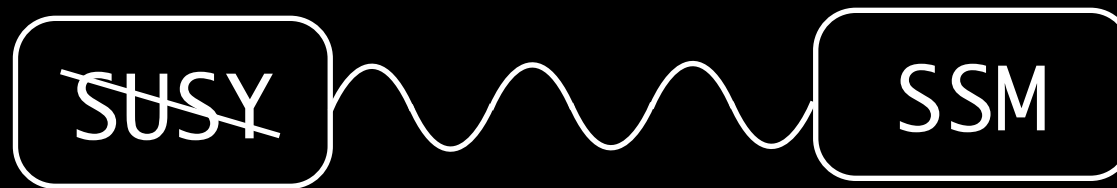
# R-symmetry and R-axion

- R-symmetry must be broken!

$$\mathcal{L} = \frac{1}{2} m_{1/2} \underbrace{\lambda \lambda}$$

R-charge: 2

Gaugino mass terms require an R-symmetry breaking!



R-symmetry is broken at some point

# R-symmetry and R-axion

• How do we break? (Model dependent)

★ Gravity Mediation

Explicit R-breaking

R-symmetry leaves little trace  
for the collider experiments...

★ Gauge Mediation

Spontaneous R-breaking

The model predicts a light NG-boson: **R-axion**

**Can we detect the R-axion at the LHC?**

# Properties of R-axion

- How low can we take the R-symmetry breaking scale?

In generic models with gauge mediation, R-breaking scale is bounded from below,

$$m_{\text{gaugino}} \lesssim \frac{\alpha}{4\pi} f_R \leftarrow \text{R-breaking scale}$$

$$m_{\text{gaugino}} > O(100) \text{ GeV}$$

$$f_R \gtrsim 10^4 \text{ GeV}$$



# Properties of R-axion

## • Mass of R-axion

R-symmetry is slightly broken by

- ★ Anomaly to the SSM gauge symmetry
- ★ In supergravity, the R-symmetry is broken by a constant in the superpotential which is necessary to set the cosmological constant to zero

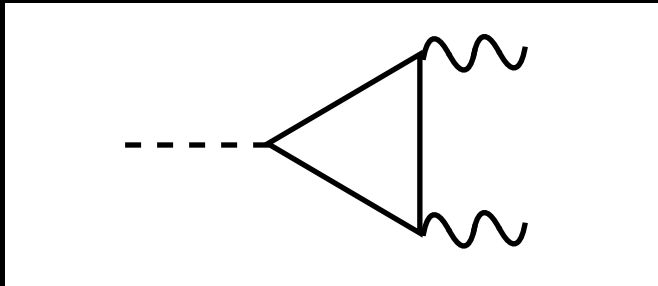
R-axion is massive

$$m_a \simeq 300 \text{ MeV} \times \left( \frac{m_{3/2}}{10 \text{ eV}} \right) \left( \frac{f_R}{10^4 \text{ GeV}} \right)^{-1/2}$$

( $m_{3/2} > 0(1) \text{ eV}$  in Gauge Mediation)

# Properties of R-axion

## R-axion interaction (at messenger scale)

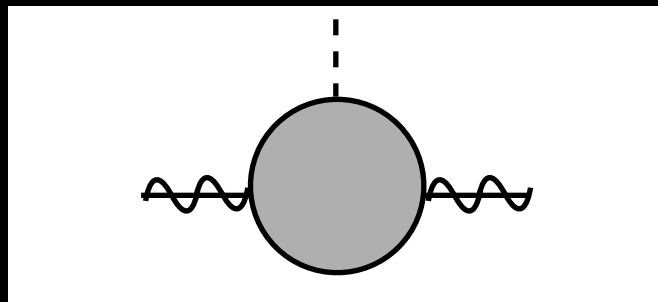


messenger loops

anomaly coupling

$$C_H \frac{g^2}{32\pi^2} \frac{a}{f_R} F \tilde{F}$$

( $C_H=0, -1, \dots, -5$ )



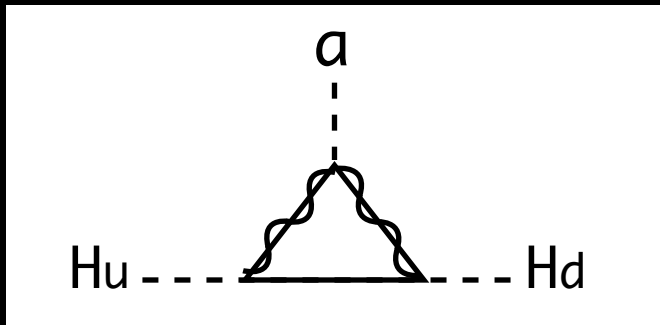
Yukawa coupling

$$\frac{1}{2} m_{1/2} e^{-ia/f_R} \lambda \lambda$$

$$\longrightarrow \frac{1}{2} \frac{m_{1/2}}{f_R} a \lambda \lambda$$

# Properties of R-axion

## R-axion interaction (at lower scale)



Higgsino-Gaugino loop

R-axion-Higgs coupling

$$B_\mu e^{-ia/f_R} H_u H_d$$

(R-charge of  $\mu = 0$ )

R-axion mixes with CP-odd Higgs bosons!

$$H_u \sim \frac{v}{f_R} \cos^2 \beta \sin \beta \times a, \quad H_d \sim \frac{v}{f_R} \sin^2 \beta \cos \beta \times a, \quad (\tan \beta = v_u/v_d)$$

( $v=246\text{GeV}$ )

Yukawa couplings to the SM fermions

$$\lambda_u = i m_u / f_R \cos^2 \beta, \quad \lambda_{d,\ell} = i m_{d,\ell} / f_R \sin^2 \beta$$

# Properties of R-axion

## • Decay of R-axion

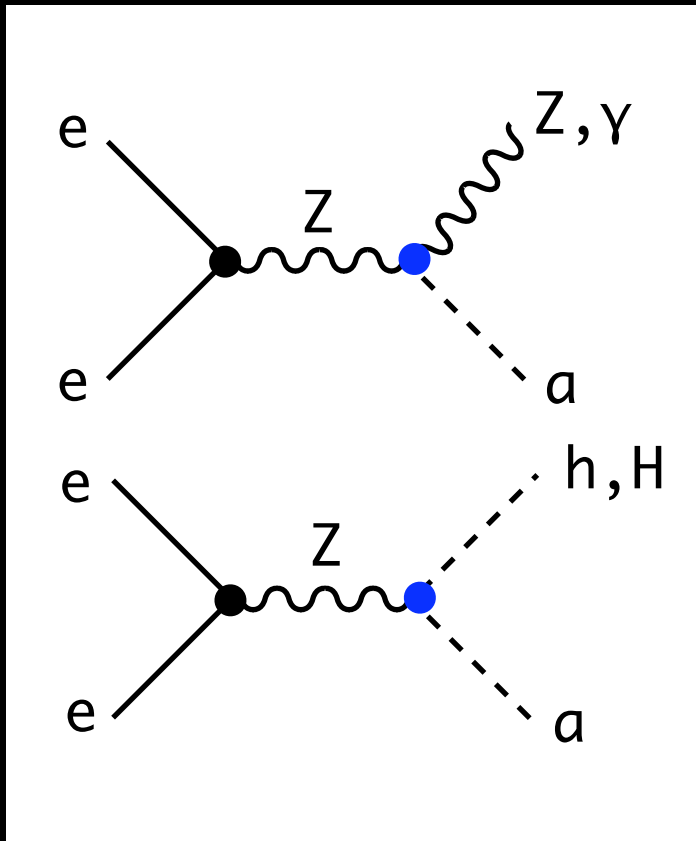
For  $2m_\mu \lesssim m_a \lesssim 1\text{GeV}$

R-axion mainly decays into a muon pair via the Yukawa coupling

$$\Gamma_{\mu\mu} \simeq 1.3 \times 10^{-12} \text{ GeV} \times \sin^4 \beta \left( \frac{m_a}{300 \text{ MeV}} \right) \left( \frac{10^4 \text{ GeV}}{f_R} \right)^2 \left( 1 - \frac{4m_\mu^2}{m_a^2} \right)^{1/2}$$
$$c\tau_{\mu\mu} \simeq \underline{150 \mu\text{m}} \times \frac{1}{\sin^4 \beta} \left( \frac{300 \text{ MeV}}{m_a} \right) \left( \frac{f_R}{10^4 \text{ GeV}} \right)^2 \left( 1 - \frac{4m_\mu^2}{m_a^2} \right)^{-1/2}$$

R-axion leaves a displaced vertex inside the collider!

# R-axion at LEP



$$\frac{g_2^4 C_{L,2} + g_Y^4 C_{L,Y}}{g_2^2 + g_Y^2} \frac{a}{32\pi^2 f_R} F_Z \tilde{F}_Z$$

$$\frac{g_2^2 C_{L,2} + g_Y^2 C_{L,Y}}{g_2^2 + g_Y^2} \frac{\sin 2\theta_W a}{32\pi^2 f_R} F_Z \tilde{F}_A$$

$$g_{\text{MSSM}}^{(A_0)} \times \frac{v}{f_R} \sin \beta \cos \beta$$

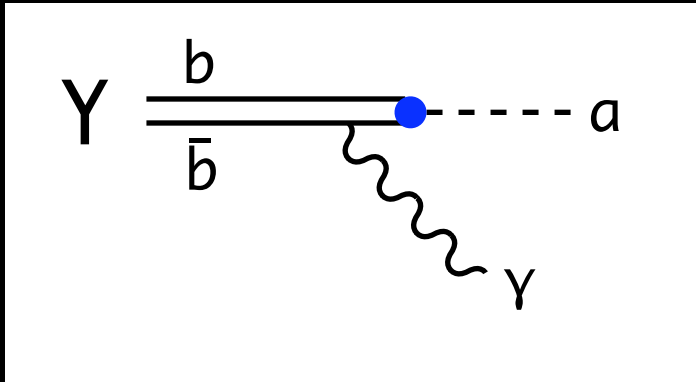
At LEP, for  $f_R \sim 10^4 \text{ GeV}$ :

Cross sections for those processes are well below 1fb

No R-axion at the LEP!

# Constraints on fR

## ★ Rare decay of $\Upsilon(1S)$ and $J/\psi$



$$\frac{Br(\Upsilon \rightarrow a + \gamma)}{Br(\Upsilon \rightarrow \mu^+ \mu^-)} = \frac{\lambda_b^2}{2\pi\alpha}$$

$$\lambda_b = \frac{im_b}{f_R} \sin^2 \beta \quad \text{Wilczek '77}$$

$$Br(\Upsilon \rightarrow a\gamma) < 10^{-(5-6)} \quad \text{CLEO '08} \quad \longrightarrow \quad f_R > 10^3 \text{ GeV}$$

## ★ Astrophysical constraints

R-axion is heavier than the temperatures of most astrophysical events.

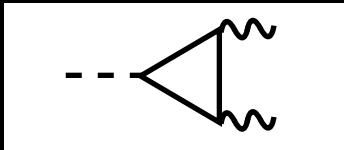
→ No constraints from astrophysics!

# R-axion at LHC

## R-axion production

The dominant processes with a large transverse momentum are:  $gg \rightarrow ga$ ,  $gq \rightarrow qa$ , and  $qq \rightarrow ga$ .

Below gluino and top mass scale, those processes are well described by using effective anomaly coupling



gluino loops  
top loops



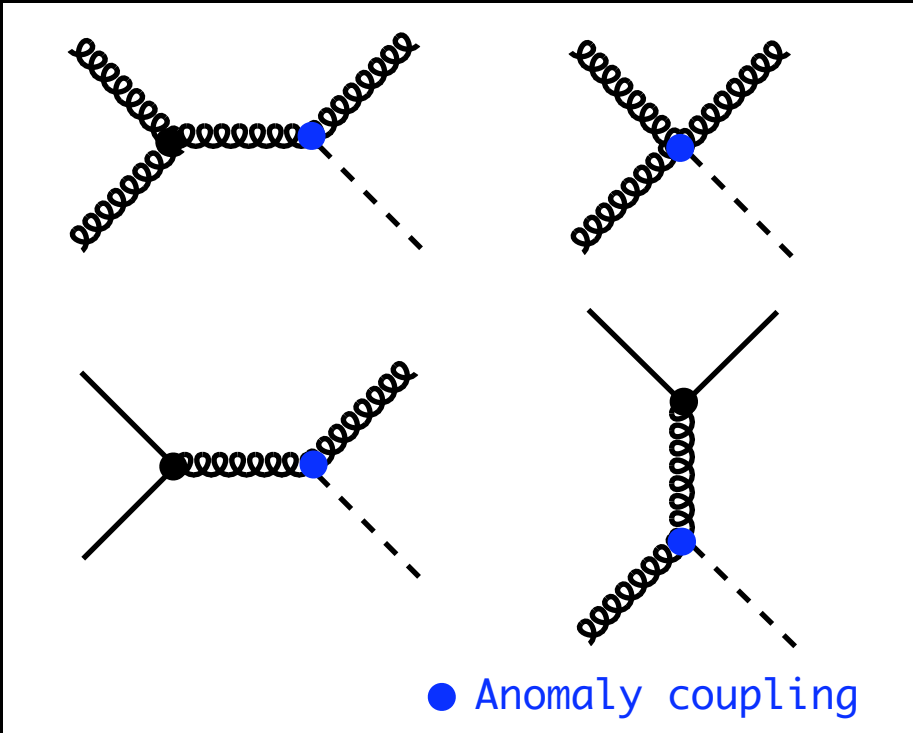
effective anomaly coupling

$$(C_H + 3 - \cos^2\beta) \frac{g^2}{32\pi^2} \frac{a}{f_R} F \tilde{F}$$

$$(C_H = 0, -1, \dots, -5)$$

# R-axion at LHC

## R-axion production



$$|\mathcal{M}(gg \rightarrow ga)|^2 = \frac{3k}{32} \left( \frac{s^4 + t^4 + u^4}{stu} \right)$$

$$|\mathcal{M}(q\bar{q} \rightarrow ga)|^2 = \frac{k}{9} \left( \frac{t^2 + u^2}{s} \right)$$

$$|\mathcal{M}(gq \rightarrow qa)|^2 = -\frac{k}{24} \left( \frac{s^2 + u^2}{t} \right)$$

$$k = \frac{C_L^2 g_s^6}{64\pi^4 f_R^2} \quad C_L = (C_H + 3 - \cos^2\beta)$$

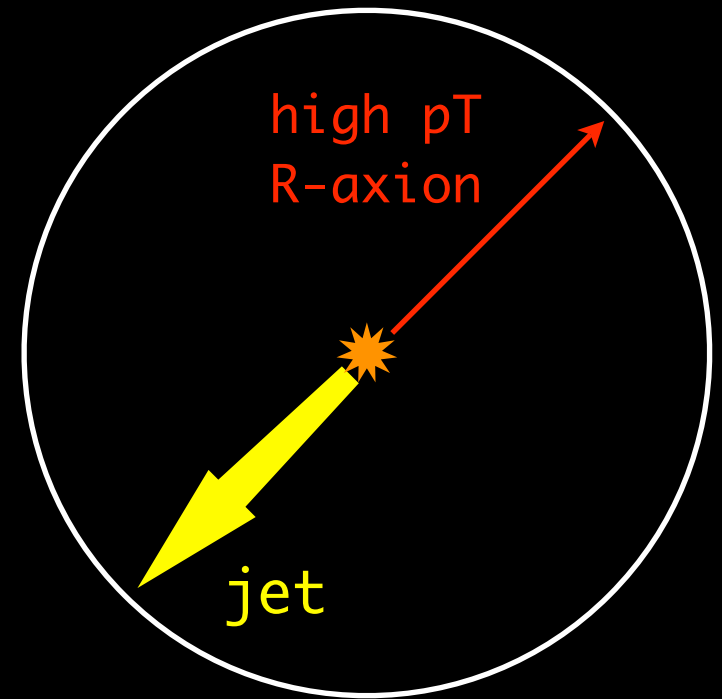
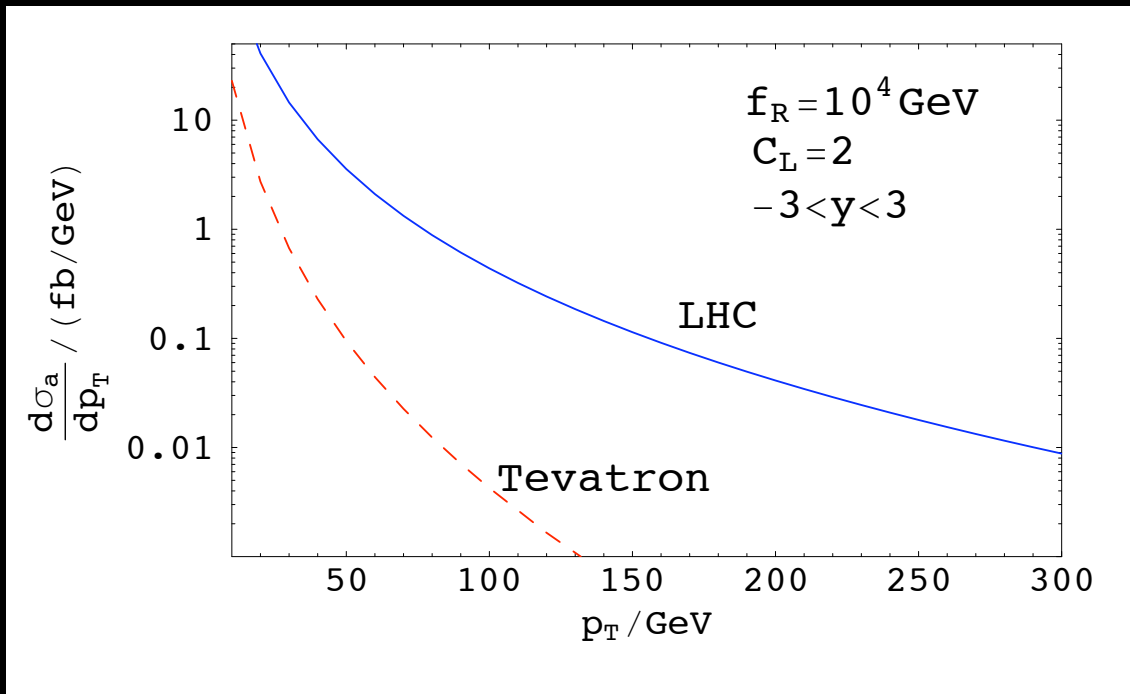
(cf. MSSM CP-odd:  $f_{R=V}, C_L=1$ )

Kao '93



# R-axion at LHC

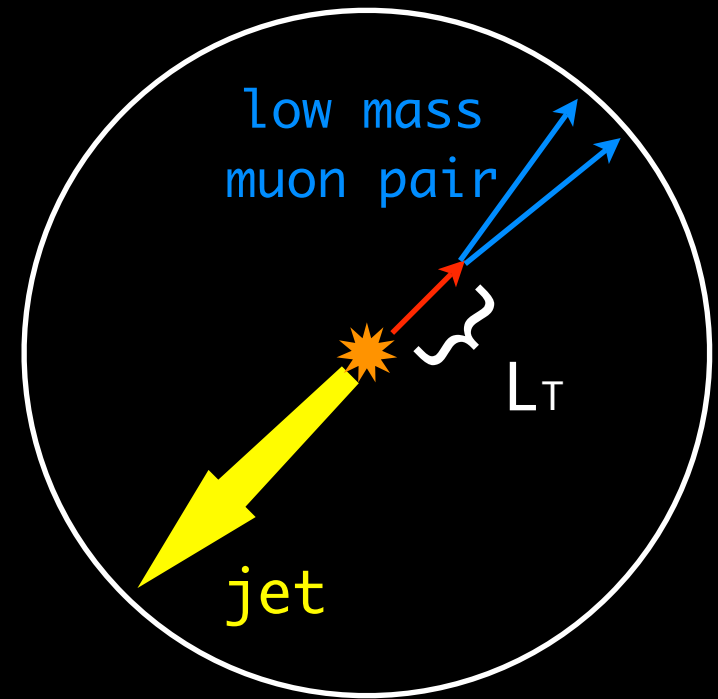
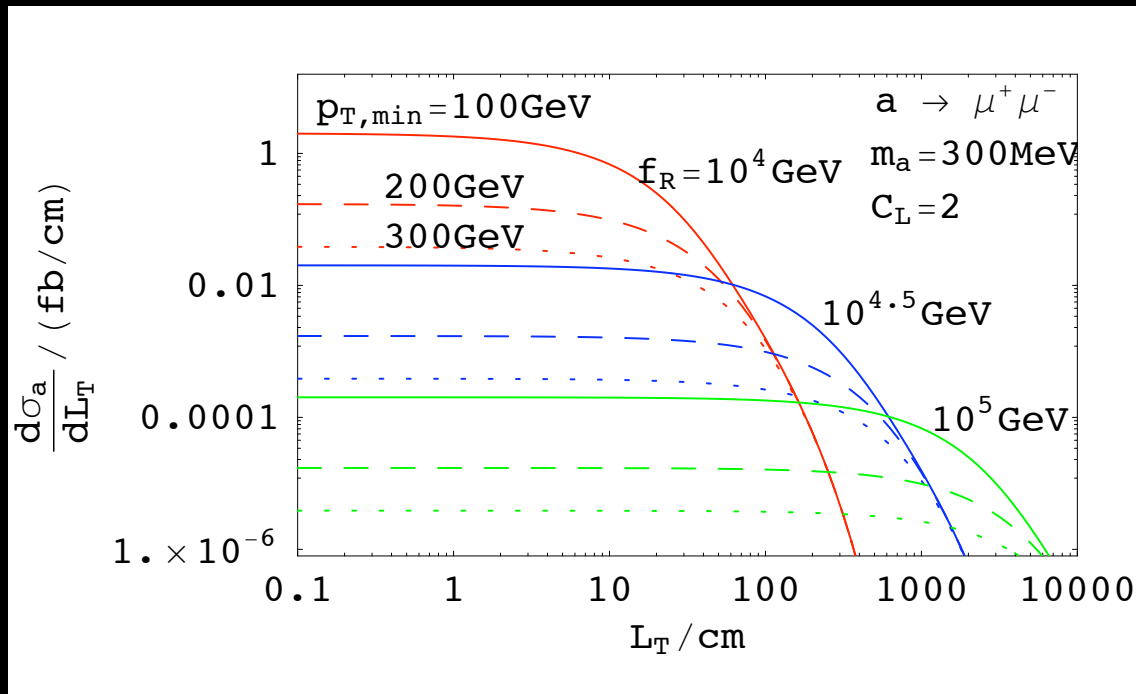
## • Transverse momentum distribution



The R-axion production:  $\sigma = 10-100$  fb for  $p_T > 100$  GeV

# R-axion at LHC

## • Transverse decay length distribution

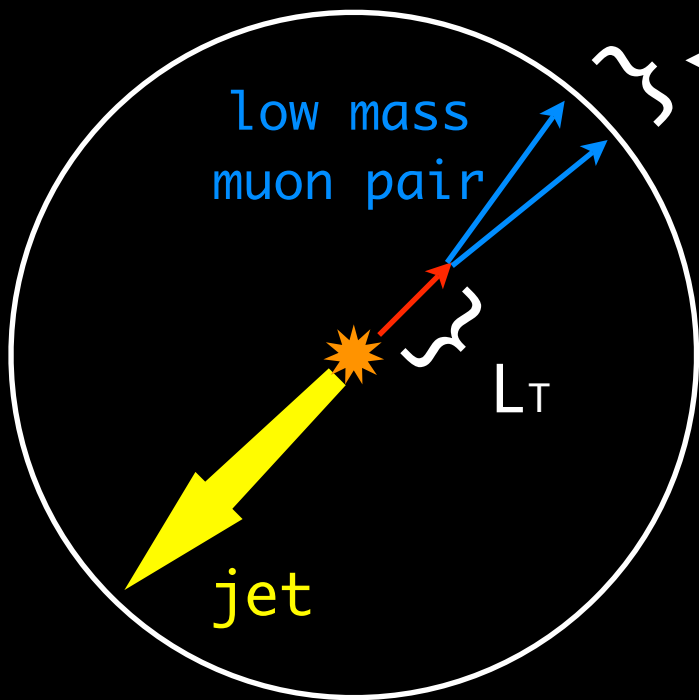


The R-axion leaves a displaced vertex from which a low mass muon pair is produced!

# R-axion at LHC

## R-axion Reconstruction

Typical open angle between two muons are very small:



$$\varphi_{\mu\mu} \sim 2m_a/p_T \sim 1-10 \text{ mrad.}$$

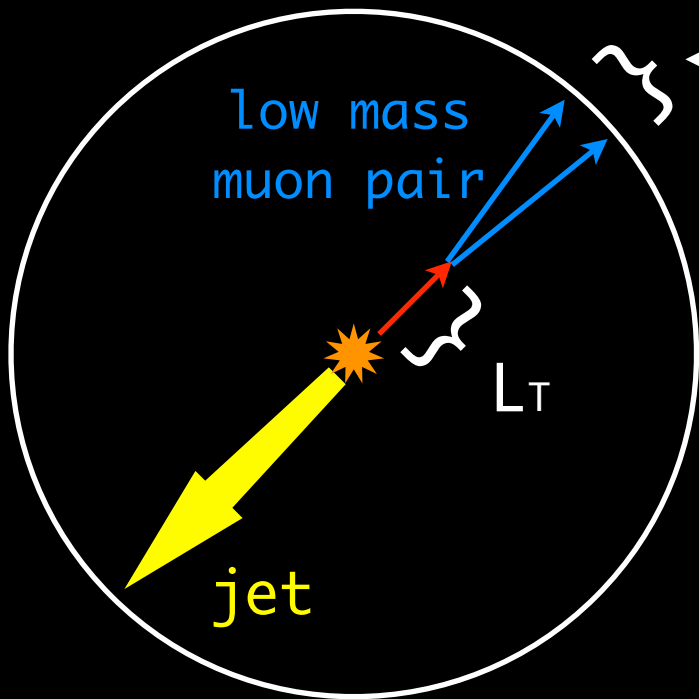
The challenge is to separate the two muon tracks!  
We also need to measure the transverse impact parameters of the two muons!

$$d_0 \sim c\tau = 0(100) \mu\text{m}$$

# R-axion at LHC

## R-axion Reconstruction

Typical open angle between two muons are very small:



$$\varphi_{\mu\mu} \sim 2m_a/p_T \sim 1-10 \text{ mrad}.$$

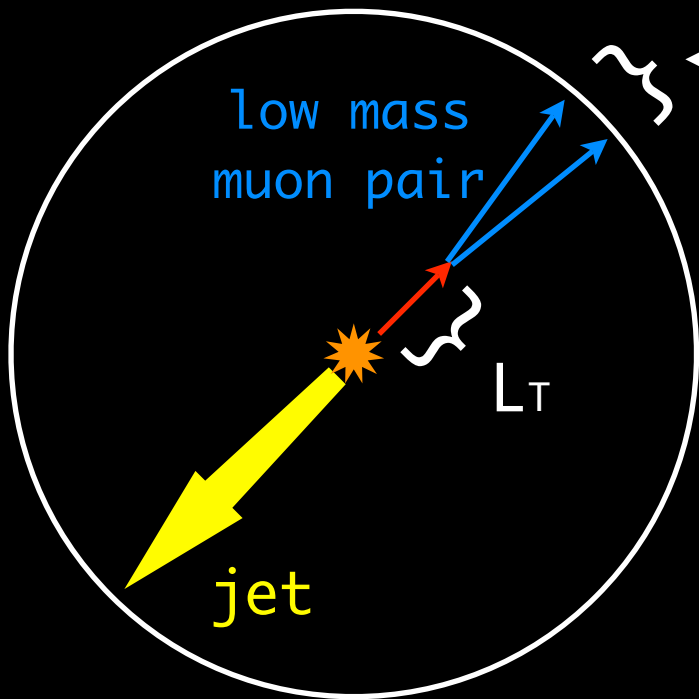
For  $L_T > \text{beam-pipe}$ :

- ★ Muons do not hit the first few layers of the pixel detector  
→ Track-resolutions get worse
- ★ Background from the muon pair photo-production requires careful study

# R-axion at LHC

## R-axion Reconstruction

Typical open angle between two muons are very small:



$$\varphi_{\mu\mu} \sim 2m_a/p_T \sim 1-10 \text{ mrad.}$$

For  $L_T < \text{beam-pipe}$ :

- ★ Distance between two muon tracks at pixel detectors ( $r=4, 10, 13\text{cm}$ )  $\sim O(100)\mu\text{m}$ .

Can we separate them? with pixels;

Atlas:  $50 \times 400 \mu\text{m}^2$

CMS:  $100 \times 100 \mu\text{m}^2$

Does the muon trigger work for “isolated muon pairs”?

# R-axion at LHC

## • R-axion Reconstruction

If the trigger and tracking system work for a muon pair in the same way for an isolated muon;

$$\sigma_{\phi} \simeq 0.075 \oplus \frac{1.8}{p_T/\text{GeV} \sqrt{\sin \theta}} \text{ (mrad)}$$

$$\sigma_{\cot \theta} \simeq 0.70 \times 10^{-3} \oplus \frac{2.0 \times 10^{-3}}{p_T/\text{GeV} \sqrt{\sin \theta}}$$

$$\sigma_{d_0} \simeq 11 \oplus \frac{73}{p_T/\text{GeV} \sqrt{\sin \theta}} \text{ (\mu m)}$$

Atlas TDR

The displaced vertex search will be successful!

# Background Estimation

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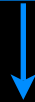
- ★ Prompt muon pairs: light meson decay, Drell-Yan process
  - Suppressed by the impact parameter measurement.
- ★ Muon pairs in heavy meson (B,D) decays
  - They are not suppressed by the impact parameter measurement. We need careful study.
- ★ Fake muon pairs ( $\pi \rightarrow \mu$ ) in K meson decay
  - Fake rate is small enough.
- ★ Muon photo-production at detector material
  - We are safe as long as the R-axion decays inside the beam pipe.

# Background Estimation

- ★ Muon pairs in heavy meson (B,D) decays  
(B,D) meson:  $c\tau = 0(100)\mu\text{m} \sim R\text{-axion}$

Signal:  $\sigma \sim 10\text{fb}$  ( $p_T > 100\text{GeV}$ )

Background:  $\sigma_{B,D} \sim 10\text{nb}$  ( $p_T > 100\text{GeV}$ )



We need a suppression factor better than  $10^{-6}$ .

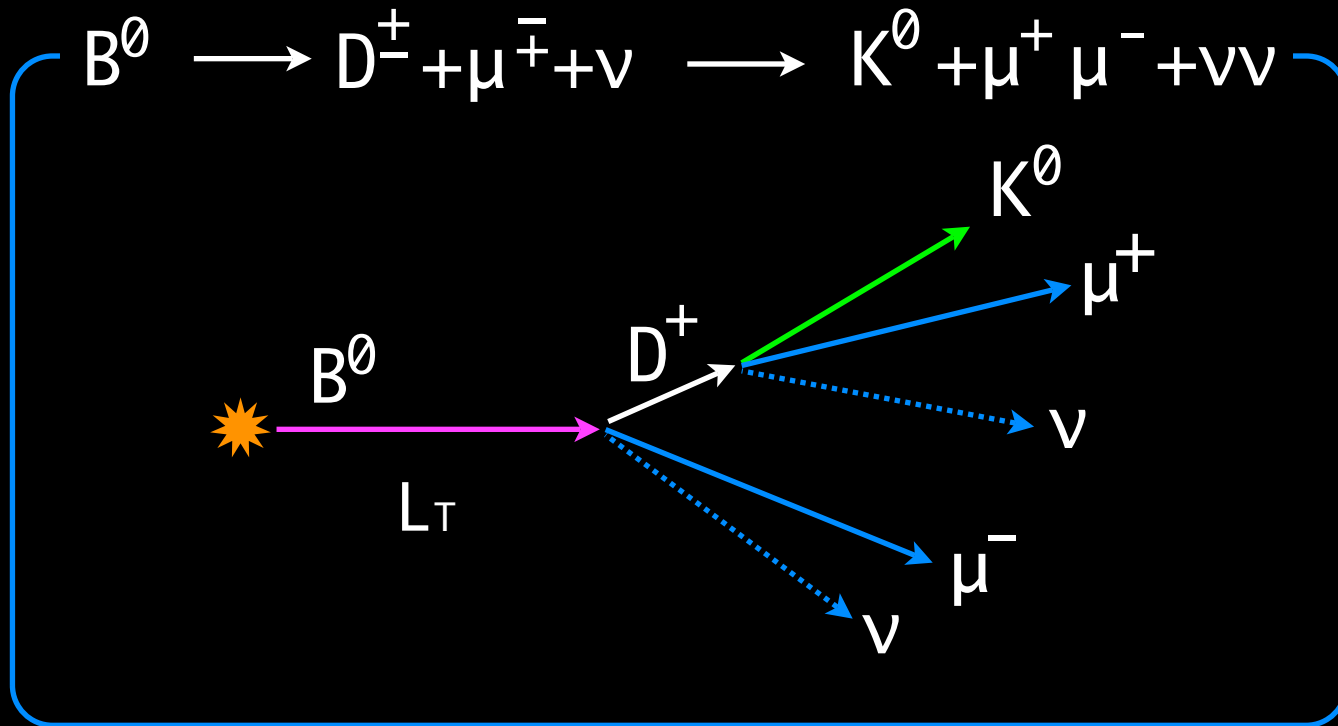
Fortunately, branching ratios of most decay modes involving muon pairs are small.

By combining with muon pair isolation cut, invariant mass cut, most of them are not serious.



# Background Estimation

★ Background from a cascade B decay ( $\text{Br} \sim 10^{-2}$ ):



Although the D meson decay leaves a displaced vertex, the D meson vertex and the muon track is too close to be distinguished!

# Background Estimation

Background

$$\varphi_{\mu\mu}^B \sim 2m_B/p_T \longleftrightarrow \varphi_{\mu\mu}^a \sim 2m_a/p_T$$

impact parameter

$$d_0 \sim L_T \varphi_{\mu\mu}$$



Event Shape Difference  
Suppression

$$\sim (\varphi_{\mu\mu}^B / \varphi_{\mu\mu}^a)^3 \sim (m_a / m_B)^3$$

$$\sim 10^{-(2-3)}$$

Signal

low mass  
muon pair

$L_T$

jet

b-jet veto  $\sim 0.1$

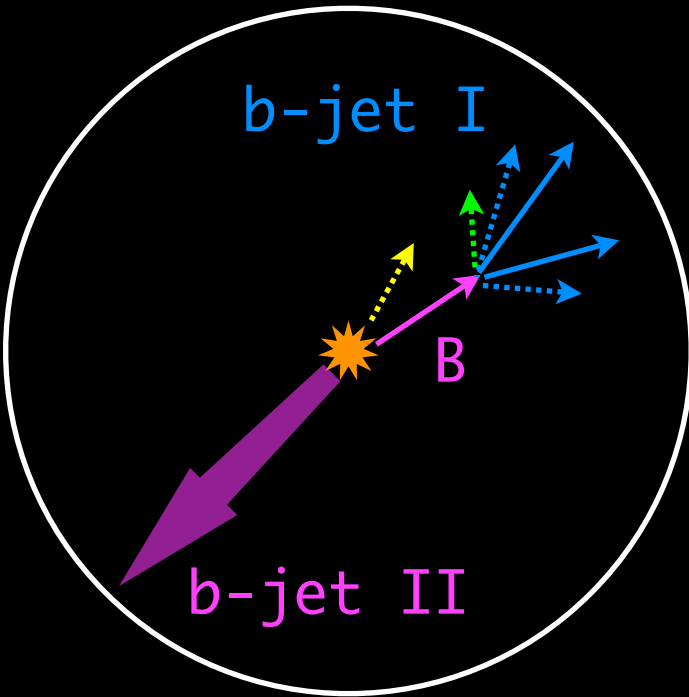
Ill balanced  $p_T$



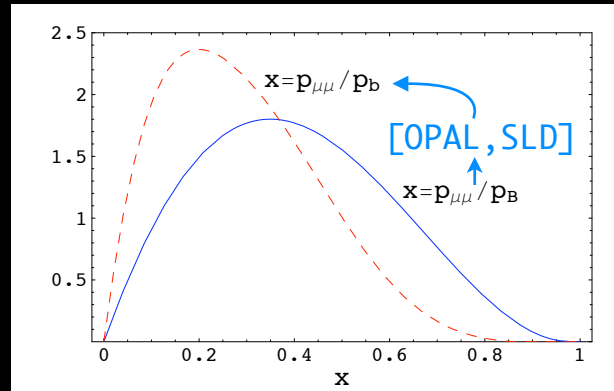
well balanced  $p_T$

# Background Estimation

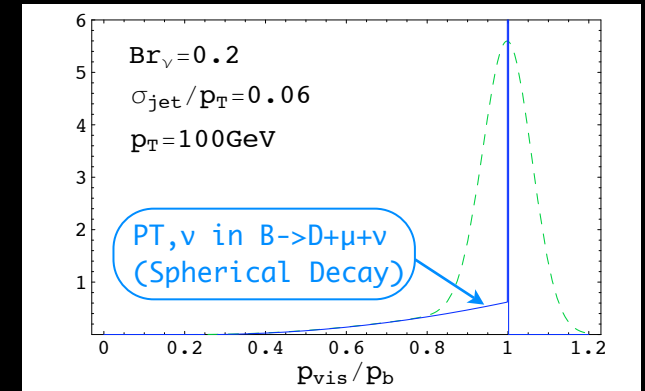
## ★ Missing $p_T$ veto



b-jet I



b-jet II

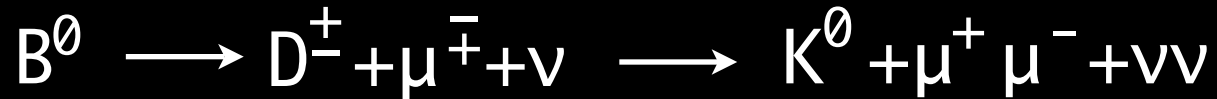


- ★ A Muon pair isn't likely to carry more than 80% of b-jet I.
- ★ Most  $p_T$  of b-jet II is visible.

Missing  $p_T$  veto results in a suppression  $\sim 10^{-2}$   
( $p_T < 0.2 p_T$ )

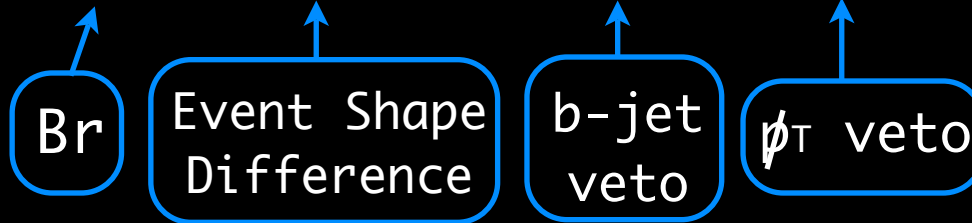
# Background Estimation

★ Background from a cascade B decay ( $\text{Br} \sim 10^{-2}$ ):



Resultant suppression factor

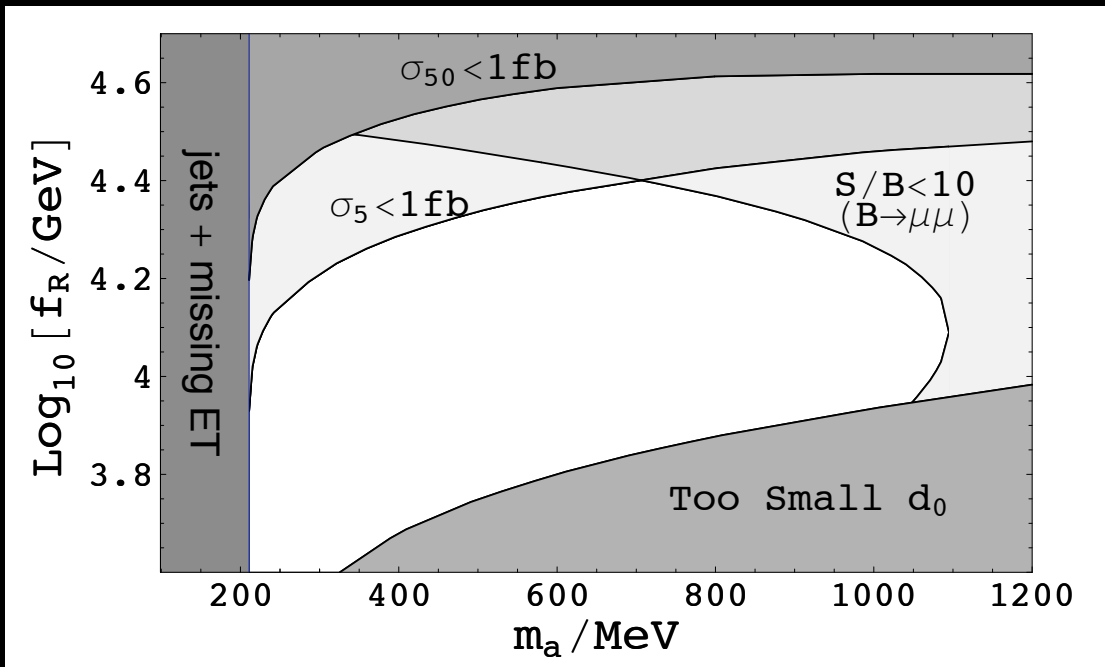
$$\sim 10^{-2} \times 10^{-(2-3)} \times 10^{-1} \times 10^{-2} \sim 10^{-(7-8)}$$



→ Background cross section is below 1 fb

# Parameter Analysis

$[\sigma_5 (L_T < 5\text{cm}) \quad \sigma_{50} (L_T < 50\text{cm})]$



(Efficiency of R-axion detection:100%)

R-axion search at the LHC is possible for  $m_a=200-1000$  MeV and  $f_R=10^4$  GeV!

- R-axion Cross Section: independent of  $m_a$
- Decay length gets shorter for the heavy  $m_a$ , larger  $f_R$



Background from the cascade decay gets severer for the heavy  $m_a$ .

# Summary

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- ★ R-axion: interrelated with the nature of SUSY breaking sector, messenger sector, Higgs sector
- ★ R-axion can be very light with the mass in 100MeV range.
- ★ R-axion produces the striking signature: displaced vertex from which a muon pair is produced.

Challenges are: ★ Is the trigger system OK?

★ Can we separate two muon tracks?

- ★ Background from heavy mesons can be suppressed

# Summary

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## Future works:

- ★ Can we detect R-axion with lighter or heavier mass?
  - ★ lighter mass: looks like missing ET
  - ★ heavier mass: leaves no displaced vertex
- ★ R-axion production associated with heavy quarks or SUSY particle production.
  - ★ Associated production with a fermion pair is suppressed due to the pseudo scalar nature of the R-axion.

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# Backup



# Background Estimation

- Background from prompt muon pairs
  - ★ Muon pairs from light meson decay  
 $\sigma \sim 1 \mu\text{b}$  ( $p_T > 100 \text{ GeV}$ )  $\text{Br} = 10^{-(4-5)}$
  - ★ Muon pairs from Drell-Yan  
 $\sigma \sim 10 \text{ pb}$  ( $p_T > 100 \text{ GeV}$ )

We need a suppression factor better than  $10^{-5}$ .

Mis-measurement probability of the impact parameter

$$P_{d_0} \simeq \text{Erfc} \left( \frac{d_0}{\sqrt{2}\sigma_{d_0}} \right)^2$$

For  $d_0 > 45 \mu\text{m}$ ,  $P_{d_0} \ll 10^{-5}$

# Background Estimation

## Background from (B,D) meson decays

| process   | $Br_{\mu\mu}^{(X)}$         | $P_{geo}$          | $\sigma_{X \rightarrow \mu\mu}(\text{fb})$ |
|---|-----------------------------|--------------------|--|
| $B^0 \rightarrow K^{*0} \mu^+ \mu^-$                                | $1.3 \times 10^{-6}$        | $(m_a/m_B)^3$      | $10^{-4}$                                  |
| $B^0 \rightarrow J/\psi + X \rightarrow \mu^+ \mu^- + X$            | $\simeq 5.9 \times 10^{-5}$ | $\lesssim 10^{-6}$ | $10^{-5}$                                  |
| $B^0 \rightarrow D^0 + X \rightarrow D^0 + \mu^+ \mu^-$             | $< 10^{-8}$                 | $(m_a/m_B)$        | $10^{-4}$                                  |
| $B^0 \rightarrow D^\pm + \mu^\mp + \nu \rightarrow \mu^+ \mu^- + X$ | $10^{-2}$                   | $(m_a/m_B)^3$      | 1  |
| $B^0 \rightarrow \pi^- \mu^+ \nu$                                   | $3 \times 10^{-8}$          | $(m_a/m_B)^3$      | $10^{-5}$                                  |
| $D^0 \rightarrow \rho^0 + \mu^+ \mu^-$                              | $1.5 \times 10^{-7}$        | $(m_a/m_D)^3$      | $10^{-3}$                                  |
| $D^0 \rightarrow \omega + K_S^0 \rightarrow \mu\mu + K_S^0$         | $10^{-6}$                   | $(m_a/m_D)$        | 1  |
| $D^0 \rightarrow \rho^0 + \pi^0 \rightarrow \mu\mu + \pi^0$         | $10^{-7}$                   | $(m_a/m_D)$        | $10^{-1}$                                  |
| $D^0 \rightarrow K^\pm + \mu^\mp + \nu$                             | $10^{-5}$                   | $(m_a/m_D)^3$      | $10^{-1}$                                  |
| $D^0 \rightarrow \pi^\pm + \mu^\mp + \nu$                           | $6 \times 10^{-7}$          | $(m_a/m_D)^3$      | $10^{-2}$                                  |

Fake Muon rate

$$P_{\mu/K} < 10^{-4}$$

$$P_{\mu/\pi} < 10^{-4}$$

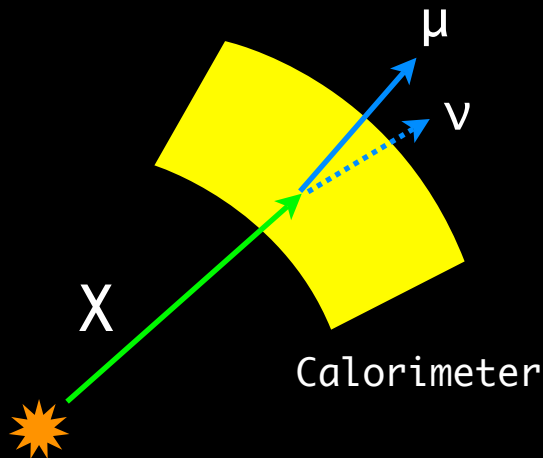
The branching ratios of the modes involving muon pairs are small.

By combining a suppression factors from differences of the event shape, missing pT veto etc, background cross section is well below 1fb.

# Background Estimation

## ★ Fake muon probability ( $X=\pi, K$ )

$$P_{\mu/X} = P_{\text{mis-id}} \times Br_{X \rightarrow \mu + \nu} \times \int_0^{r_{\text{out}}} dL_T \frac{1}{c\tau_X} \frac{m_X}{p_{T,X}} \exp \left[ -\frac{m_X}{p_{T,X}} \frac{L_T}{c\tau_X} \right] \times n_X(L_T)$$



In flight decay rate at  $L_T$

Punch through rate up to  $L_T$

$$n_X(L_T) \simeq 1 - \theta(L_T - r_{\text{in}}) \int_{r_{\text{in}}}^{L_T} dx \frac{11}{\Delta r_{\text{calo}}} \exp \left[ -11 \frac{(x - r_{\text{in}})}{\Delta r_{\text{calo}}} \right]$$

( $r_{\text{in}}=2\text{m}$ ,  $r_{\text{out}}=4\text{m}$ ,  $\Delta r_{\text{calo}} = r_{\text{out}}-r_{\text{in}}$ )

$P_{\text{mis-ID}} = 50\%$  ( $\pi$ ),  $P_{\text{mis-ID}} = 10\%$  (K) **AtlasTDR**

### Resultant Fake Rates

$$P_{\mu/\pi} < 10^{-4} \quad P_{\mu/K} < 10^{-4}$$

# Background Estimation

## Background from K meson decays

### Effective Branching ratios ( $p_T > 100 \text{ GeV}$ )

$$\begin{aligned} Br^{(\text{eff})}(K_L^0 \rightarrow \mu(\pi) + \mu + \nu) &= \left( \frac{m_K}{p_{T,K}} \frac{r_{\text{pipe}}}{c\tau_{K_L}} \right) \times P_{\mu/\pi} \times Br(K_L^0 \rightarrow \pi + \mu + \nu) \simeq 10^{-9}, \\ Br^{(\text{eff})}(K_S^0 \rightarrow \mu(\pi) + \mu + \nu) &= \left( \frac{m_K}{p_{T,K}} \frac{r_{\text{pipe}}}{c\tau_{K_S}} \right) \times P_{\mu/\pi} \times Br(K_S^0 \rightarrow \pi + \mu + \nu) \simeq 10^{-9}, \\ Br^{(\text{eff})}(K_S^0 \rightarrow \mu(\pi) + \mu(\pi)) &= \left( \frac{m_K}{p_{T,K}} \frac{r_{\text{pipe}}}{c\tau_{K_S}} \right) \times P_{\mu/\pi}^2 \times Br(K_S^0 \rightarrow \pi + \pi) \simeq 3 \times 10^{-10}, \end{aligned}$$

$$\begin{aligned} c\tau_{K_L} &= 15.3 \text{ m}, \quad c\tau_{K_S} = 2.68 \text{ cm} \\ Br(K_L \rightarrow \pi \mu \nu) &= 27\%, \quad Br(K_S \rightarrow \pi \mu \nu) = 5 \times 10^{-4}, \quad Br(K_S \rightarrow \pi \pi) = 68\% \end{aligned}$$

**Background is highly suppressed!**

# Background Estimation

- Muon pair from photo-production at material

Background cross section

$$\sigma_{\gamma \rightarrow \mu\mu} = P_{\gamma \rightarrow \mu\mu} \times \sigma_{\gamma} \quad [\sigma_{\gamma} \sim 1\text{nb} \text{ (} p_T > 100\text{GeV)}]$$

$$P_{\gamma \rightarrow \mu\mu} \sim \underline{10^{-30} \text{ cm}} \times (Z/4)^2 \times n \times \Delta L$$

Small momentum transfer  
Tsai '74

|    | Z  | A  | $\rho$ (g·cm <sup>-3</sup> ) | n (10 <sup>22</sup> cm <sup>-3</sup> ) | $P_{\gamma \rightarrow \mu\mu}$ |
|----|----|----|------------------------------|--|---------------------------------|
| Be | 4  | 9  | 1.85                         | 12.3                                   | $4 \times 10^{-8}$              |
| C  | 6  | 12 | 1.9-2.3                      | 9.5-11                                 | $7 \times 10^{-8}$              |
| Si | 14 | 28 | 2.33                         | 4.98                                   | $2 \times 10^{-7}$              |

[1mm thick material]

Background is small for the R-axion decaying inside of the beam-pipe.

Careful study is required for the R-axion decaying outside of the beam-pipe.