Theory and Phenomenology of Higgs Bosons of the Standard Model and its SUSY extension



Howard E. Haber 29 June—1 July 2016 Pre-SUSY 2016 Melbourne, Australia



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A brief bibliography

- J.F. Gunion, H.E. Haber, G.L. Kane and S. Dawson, *The Higgs Hunter's Guide* (Westview Press, Boulder CO, 1990).
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- G.C. Branco, P.M. Ferreira, L. Lavoura, M.N. Rebelo, M. Sher and J.P. Silva, "Theory and phenomenology of two-Higgs-doublet models," Phys. Rept. 516, 1 (2012) [arXiv:1106.0034 [hep-ph]].

Lecture I

The Standard Model Higgs Boson

<u>Outline</u>

- The Standard Model before 4 July 2012—what was missing?
- mass generation and the Goldstone boson
- The significance of the TeV scale—Part 1
- Electroweak symmetry breaking dynamics of the Standard Model (SM)
- Discovery of the Higgs boson
- Observed properties of the Higgs boson

FERMIONS matter constituents spin = 1/2, 3/2, 5/2,					
Leptons spin =1/2 Quarks spin =1/2				=1/2	
Flavor	Mass GeV/c ²	Electric charge	Flavor	Approx. Mass GeV/c ²	Electric charge
𝒫 lightest neutrino*	(0-0.13)×10 ⁻⁹	0	up up	0.002	2/3
e electron	0.000511	-1	d down	0.005	-1/3
𝔥 middle neutrino*	(0.009-0.13)×10 ⁻⁹	0	C charm	1.3	2/3
μ muon	0.106	-1	S strange	0.1	-1/3
\mathcal{V}_{H} heaviest neutrino*	(0.04-0.14)×10 ⁻⁹	0	t top	173	2/3
τ tau	1.777	-1	bottom	4.2	-1/3

Particle content of the Standard Model

force carriers

Something is missing...

Unified Electroweak spin = 1		
Name	Mass GeV/c ²	Electric charge
Y photon	0	0
W	80.39	-1
W ⁺	80.39	+1
W bosons	91.188	0
Z boson		

BOSONS

Spin = 0, 1, 2, Strong (color) spin =1			
Name	Mass Electric GeV/c ² charge		
g	0	0	
gluon			

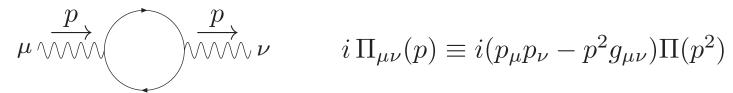
What was missing?

The theory of W^{\pm} and Z gauge bosons must be *gauge invariant*; otherwise the theory is mathematically inconsistent. You may have heard that "gauge invariance implies that the gauge boson mass must be zero," since a mass term of the form $m^2 A^a_{\mu} A^{\mu a}$ is not gauge invariant.

So, what is the origin of the W^{\pm} and Z boson masses? Gauge bosons are massless at tree-level, but perhaps a mass may be generated when quantum corrections are included. The tree-level gauge boson propagator $G^0_{\mu\nu}$ (in the Landau gauge) is:

$$G^{0}_{\mu\nu}(p) = \frac{-i}{p^2} \left(g_{\mu\nu} - \frac{p_{\mu}p_{\nu}}{p^2} \right) \,.$$

The pole at $p^2 = 0$ indicates that the tree-level gauge boson mass is zero. Let's now include the radiative corrections. The polarization tensor $\Pi_{\mu\nu}(p)$ is defined as:



where the form of $\Pi_{\mu\nu}(p)$ is governed by covariance with respect to Lorentz transformations, and is constrained by gauge invariance, i.e. it satisfies $p^{\mu}\Pi_{\mu\nu}(p) = p^{\nu}\Pi_{\mu\nu}(p) = 0.$

The renormalized propagator is the sum of a geometric series

$$\cdots + \cdots + \cdots + \cdots + \cdots + \cdots = \frac{-i(g_{\mu\nu} - \frac{p_{\mu}p_{\nu}}{p^2})}{p^2[1 + \Pi(p^2)]}$$

mm

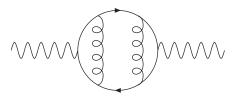
The pole at $p^2 = 0$ is shifted to a non-zero value if:

$$\Pi(p^2) \underset{p^2 \to 0}{\simeq} \frac{-g^2 v^2}{p^2}.$$

Then $p^2[1 + \Pi(p^2)] = p^2 - g^2 v^2$, yielding a gauge boson mass of gv.

Interpretation of the $p^2=0$ pole of $\Pi(p^2)$

The pole at $p^2 = 0$ corresponds to a propagating massless scalar. For example, the sum over intermediate states includes a quark-antiquark pair with many gluon exchanges, e.g.,



This is a strongly-interacting system—it is possible that one of the contributing intermediate states is a massless spin-0 state (due to the strong binding of the quark/antiquark pair).

We know that the Z and W^{\pm} couple to neutral and charged weak currents

$$\mathcal{L}_{\rm int} = g_Z j_{\mu}^Z Z^{\mu} + g_W (j_{\mu}^W W^{+\mu} + \text{h.c.}) \,,$$

which are known to create neutral and charged pions from the vacuum, e.g.,

$$\langle 0|j^Z_\mu(0)|\pi^0\rangle = if_\pi p_\mu \,.$$

Here, $f_{\pi} = 93$ MeV is the amplitude for creating a pion from the vacuum. In the absence of quark masses, the pions are massless bound states of $q\bar{q}$ [they are Goldstone bosons of chiral symmetry which is spontaneously broken by the strong interactions]. Thus, the diagram:

$$Z^0 \quad \swarrow \quad Z^0$$

yields the leading contribution as $p^2 \to 0$ [shown in red] to the $p_\mu p_\nu$ of $\Pi_{\mu\nu}$,

$$i\Pi_{\mu\nu}(p) = ig_Z^2 f_\pi^2 \left(g_{\mu\nu} - \frac{p_\mu p_\nu}{p^2}\right)$$

Remarkably, the latter is enough to fix the corresponding $g_{\mu\nu}$ part of $\Pi_{\mu\nu}$ [thank you, Lorentz invariance and gauge invariance!]. It immediately follows that

$$\Pi(p^2) = -\frac{g_Z^2 f_\pi^2}{p^2},$$

and therefore $m_Z = g_Z f_{\pi}$. Similarly $m_W = g_W f_{\pi}$.

Gauge boson mass generation and the Goldstone boson

We have demonstrated a mass generation mechanism for gauge bosons that is both Lorentz-invariant and gauge-invariant! This is the essence of the *Higgs mechanism*. The $p^2 = 0$ pole of $\Pi(p^2)$ corresponds to a propagating massless scalar state called the Goldstone boson. We showed that the W and Z are massive in the Standard Model (without Higgs bosons!!). Moreover, the ratio $\frac{m_W}{m_Z} = \frac{g_W}{g_Z} \equiv \cos \theta_W \simeq 0.88$

is remarkably close to the measured ratio. Unfortunately, since $g_Z \simeq 0.37$ we find $m_Z = g_Z f_{\pi} = 35$ MeV, which is too small by a factor of 2600.

There must be another source for the gauge boson masses, i.e. new fundamental dynamics that generates the Goldstone bosons that are the main sources of mass for the W^{\pm} and Z.

How do Goldstone bosons arise?

Suppose a Lagrangian exhibits a continuous global symmetry. If the vacuum state of the theory breaks the global symmetry, then the spectrum contains a massless scalar state—the Goldstone boson. This is a rigorous result of quantum field theory.

Goldstone's theorem can be exhibited in a model of elementary scalar dynamics. Suppose I have a multiplet of real scalar fields ϕ_i with Lagrangian

$$\mathscr{L} = \frac{1}{2} \partial_{\mu} \phi_i \partial^{\mu} \phi^i - V(\phi_i) \,,$$

which is invariant under an orthogonal transformation, $\phi_i \to \mathcal{O}_{ij}\phi_j$. Working infinitesimally, $\phi_i \to \phi_i + \delta \phi_i$, where

$$\delta\phi_i = -i\theta^a T^a_{ij}\phi_j \,.$$

The generators iT^a are real antisymmetric matrices and the θ^a are real parameters.

Note that the kinetic energy term is automatically invariant under $\phi_i \rightarrow O_{ij}\phi_j$. The the Lagrangian is invariant under the global symmetry transformation if $\delta V = 0$ when $\phi_i \rightarrow \phi_i + \delta \phi_i$. Using $\delta \phi_i = -i\theta^a T^a_{ij}\phi_j$,

$$\delta V = \frac{\partial V}{\partial \phi_i} \delta \phi_i = 0 \qquad \Longrightarrow \qquad \frac{\partial V}{\partial \phi_i} T^a_{ij} \phi_j = 0 \,.$$

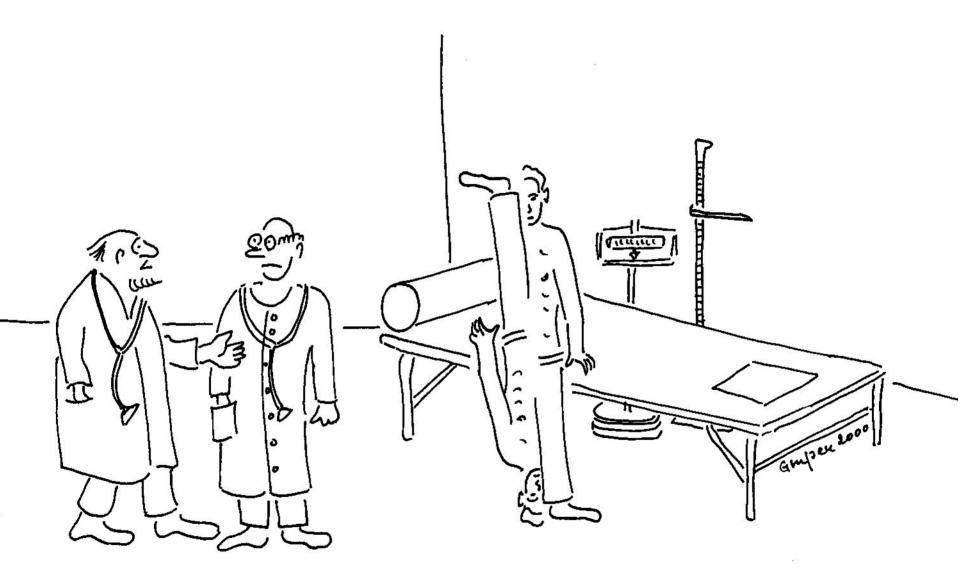
The global symmetry is spontaneously broken if the vacuum state does not respect the symmetry. That is, the potential minimum occurs at $\phi_i = v_i$ where $\exp(-i\theta^a T^a)v \neq v$ [or equivalently, $T^a v \neq 0$].

Define new fields $\widetilde{\phi}_i \equiv \phi_i - v_i$, in which case

$$\mathscr{L} = \frac{1}{2} \partial_{\mu} \widetilde{\phi}_{i} \partial^{\mu} \widetilde{\phi}^{i} - \frac{1}{2} M_{ij}^{2} \widetilde{\phi}_{i} \widetilde{\phi}_{j} + \text{interactions},$$

where M^2 is a non-negative symmetric matrix,

$$M_{ij}^2 \equiv \frac{\partial V}{\partial \phi_i \partial \phi_j} \bigg|_{\phi_i = v_i}$$



"A severe case of symmetry breaking!"

Recall the condition for the global symmetry,

$$\frac{\partial V}{\partial \phi_i} T^a_{ij} \phi_j = 0 \,.$$

Differentiating the above with respect to ϕ_j and setting $\phi_i = v_i$ and $(\partial V / \partial \phi_i)_{\phi_i = v_i} = 0$ then yields

$$M_{ik}^2 T_{ij}^a v_j = 0.$$

That is, $\phi_i T_{ij}^a v_j$ is an eigenvector of M^2 with zero eigenvalue. There is one Goldstone boson for each broken generator $T^a v \neq 0$.

The Higgs mechanism can be exhibited in our simple model of elementary scalar dynamics by promoting the global symmetry to a local symmetry. This is accomplished by introducing a gauge field A^a_{μ} corresponding to each symmetry generator T^a . The Lagrangian is now

$$\mathscr{L} = \mathscr{L}_{\rm YM} + \frac{1}{2} (D_{\mu}\phi)^T (D^{\mu}\phi) - V(\phi) ,$$

where \mathscr{L}_{YM} is the Yang-Mills Lagrangian and D is the covariant derivative

$$D_{\mu} \equiv \partial_{\mu} + igT^a A^a_{\mu}$$

Assuming that the scalar potential is minimized at $\phi_i = v_i$ as before, we again define shifted fields, $\tilde{\phi}_i \equiv \phi_i - v_i$. Then,

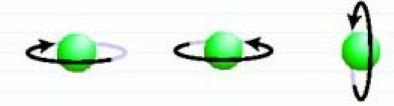
$$(D_{\mu}\phi)^{T}(D^{\mu}\phi) = M_{ab}^{2}A_{\mu}^{a}A^{\mu b} + \cdots,$$

with $M_{ab}^2 = g^2 v^T T^a T^b v$. For each unbroken generator (i.e., $T^a v = 0$), the corresponding vector boson remains massless. The remaining vector bosons acquire mass. One can show that the corresponding Goldstone bosons are no longer physical states of the theory. Instead, they are "absorbed" by the corresponding gauge bosons and are realized as the longitudinal spin component of the massive gauge bosons.

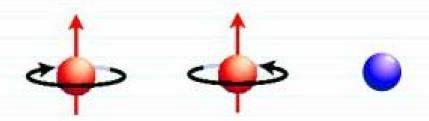
Massless and heavy spin 1 particles

 $\hat{\mathcal{T}}$

Heavy spin 1 particles can spin in 3 directions:



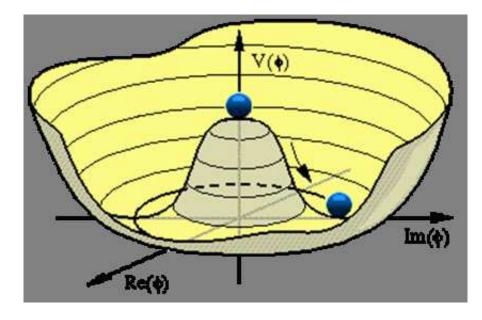
Massless particles must have their spin-axis either parallel or anti-parallel to their direction of motion:



They can only spin in 2 directions.

Possible choices for electroweak-symmetry-breaking (EWSB) dynamics

• weakly-interacting self-coupled elementary (Higgs) scalar dynamics



 strong-interaction dynamics involving new fermions and gauge fields [technicolor, dynamical EWSB, little Higgs models, composite Higgs models, extra-dimensional EWSB, ...]

Both mechanisms generate new phenomena with significant experimental consequences.

Fate of the pion

Let us designate by ω^a the triplet of Goldstone bosons that is generated by the additional electroweak symmetry-breaking dynamics. For example, if ω^a is a consequence of elementary scalar dynamics, then the total axial vector current that creates the ω^a and the pion fields π^a from the vacuum is given by $j^a_\mu = j^a_{\mu,\rm QCD} + v \partial_\mu \omega_a$, where v = 246 GeV and

$$\langle 0|j^a_{\mu}(0)|\pi^b\rangle = if_{\pi}p_{\mu}\delta^{ab}, \qquad \langle 0|j^a_{\mu}(0)|\omega^b\rangle = ivp_{\mu}\delta^{ab}$$

In this case, the "true" Goldstone bosons of electroweak symmetry breaking are:

$$|G^a\rangle = \frac{1}{\sqrt{f_\pi^2 + v^2}} \left[f_\pi |\pi^a\rangle + v |\omega^a\rangle \right],$$

which are absorbed by the W^{\pm} and Z as a result of the Higgs mechanism, and the physical pions are the states orthogonal to the $|G^a\rangle$,

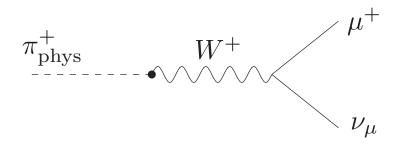
$$|\pi^a\rangle_{\rm phys} = \frac{1}{\sqrt{f_\pi^2 + v^2}} \left[v |\pi^a\rangle - f_\pi |\omega^a\rangle \right].$$

One can check that

$$\langle 0|j^a_{\mu}|G^b\rangle = i(f^2_{\pi} + v^2)^{1/2}p_{\mu}\delta^{ab},$$

$$\langle 0|j^a_{\mu}|\pi^b\rangle_{\rm phys} = 0.$$

So far so good. But, if you look at old textbooks on the weak interactions, they will insist that the (physical) charged pion decays via



But, the π -W vertex above is proportional to $\langle 0|j_{\mu}^{-}|\pi^{+}\rangle_{\text{phys}} = 0$. So how does the charged pion decay?

I learned about this paradox from Marvin Weinstein many years ago. The answer will be given at the beginning of Lecture 2.

Significance of the TeV Scale—Part 1

Let $\Lambda_{\rm EW}$ be energy scale of EWSB dynamics. For example:

- Elementary Higgs scalar $(\Lambda_{\rm EW} = m_H)$.
- Strong EWSB dynamics (e.g., $\Lambda_{\rm EW}^{-1}$ is the characteristic scale of bound states arising from new strong dynamics).

Consider $W_L^+W_L^- \to W_L^+W_L^-$ (L = longitudinal or equivalently, zero helicity) for $m_W^2 \ll s \ll \Lambda_{\rm EW}^2$. The corresponding amplitude, to leading order in g^2 , but to all orders in the couplings that control the EWSB dynamics, is equal to the amplitude for $G^+G^- \to G^+G^-$ (where G^{\pm} are the charged Goldstone bosons). The latter is universal, independent of the EWSB dynamics. This is a rigorous low-energy theorem.

Applying unitarity constraints to this amplitude yields a critical energy $\sqrt{s_c}$, above which unitarity is violated. This unitarity violation must be repaired by EWSB dynamics and implies that $\Lambda_{\rm EW} \lesssim \mathcal{O}\left(\sqrt{s_c}\right)$.

Unitarity of scattering amplitudes

Unitarity is equivalent to the conservation of probability in quantum mechanics. A violation of unitarity is tantamount to a violation of the principles of quantum mechanics—this is too sacred a principle to give up!

Consider the helicity amplitude $\mathcal{M}(\lambda_3\lambda_4; \lambda_1\lambda_2)$ for a $2 \to 2$ scattering process with initial [final] helicities λ_1 , λ_2 [λ_3 , λ_4]. The Jacob-Wick partial wave expansion is:

$$\mathcal{M}(\lambda_3\lambda_4;\,\lambda_1\lambda_2) = \frac{8\pi\sqrt{s}}{(p_i p_f)^{1/2}} e^{i(\lambda_i - \lambda_f)\phi} \sum_{J=J_0}^{\infty} (2J+1)\mathcal{M}^J_{\lambda}(s) d^J_{\lambda_i\lambda_f}(\theta) \,,$$

where p_i $[p_f]$ is the incoming [outgoing] center-of-mass momentum, \sqrt{s} is the center-of-mass energy, $\lambda \equiv \{\lambda_3 \lambda_4; \lambda_1 \lambda_2\}$ and

$$J_0 \equiv \max\{\lambda_i, \lambda_f\}, \text{ where } \lambda_i \equiv \lambda_1 - \lambda_2, \text{ and } \lambda_f \equiv \lambda_3 - \lambda_4.$$

Orthogonality of the *d*-functions allows one to project out a given partial wave amplitude. For example, for $W_L^+W_L^- \to W_L^+W_L^-$ (*L* stands for *longitudinal* and corresponds to $\lambda = 0$),

$$\mathcal{M}^{J=0} = \frac{1}{16\pi s} \int_{-s}^{0} dt \,\mathcal{M}(L,L\,;\,L,L)\,,$$

where $t=-\frac{1}{2}s(1-\cos\theta)$ in the limit where $m_W^2\ll s.$

In the limit of $m_W^2 \ll s \ll \Lambda_{\rm EW}^2$, the J = 0 partial wave amplitude for $W_L^+ W_L^- \to W_L^+ W_L^-$ is equal to the amplitude for $G^+ G^- \to G^+ G^-$: $\mathcal{M}^{J=0} = \frac{G_F s}{16\pi\sqrt{2}}.$

^{*}The amplitude for the scattering of Goldstone bosons is evaluated using the scalar sector of the symmetrybreaking Lagrangian in the absence of gauge bosons.

Partial wave unitarity implies that:

$$|\mathcal{M}^J|^2 \le |\mathrm{Im} \ \mathcal{M}^J| \le 1$$
,

which gives

$$(\operatorname{Re} \mathcal{M}^J)^2 \leq |\operatorname{Im} \mathcal{M}^J| (1 - |\operatorname{Im} \mathcal{M}^J|) \leq \frac{1}{4}.$$

Setting $|\text{Re } \mathcal{M}^{J=0}| \leq \frac{1}{2}$ yields $\sqrt{s_c}$. The most restrictive bound arises from the isospin zero channel $\sqrt{\frac{1}{6}}(2W_L^+W_L^- + Z_LZ_L)$:

$$s_c = \frac{4\pi\sqrt{2}}{G_F} = (1.2 \text{ TeV})^2.$$

Since unitarity cannot be violated, we conclude that $\Lambda_{\rm EW} \lesssim \sqrt{s_c}$. That is,

The dynamics of electroweak symmetry breaking must be exposed at or below the 1 TeV energy scale.

EWSB Dynamics of the Standard Model (SM)

• Add a new sector of "matter" consisting of a complex SU(2) doublet, hypercharge-one self-interacting scalar fields, $\Phi \equiv (\Phi^+ \Phi^0)$ with four real degrees of freedom. The scalar potential is:

$$V(\Phi) = \frac{1}{2}\lambda(\Phi^{\dagger}\Phi - \frac{1}{2}v^2)^2,$$

so that in the ground state, the neutral scalar field takes on a constant non-zero value $\langle \Phi^0 \rangle = v/\sqrt{2}$, where v = 246 GeV. It is convenient to write:

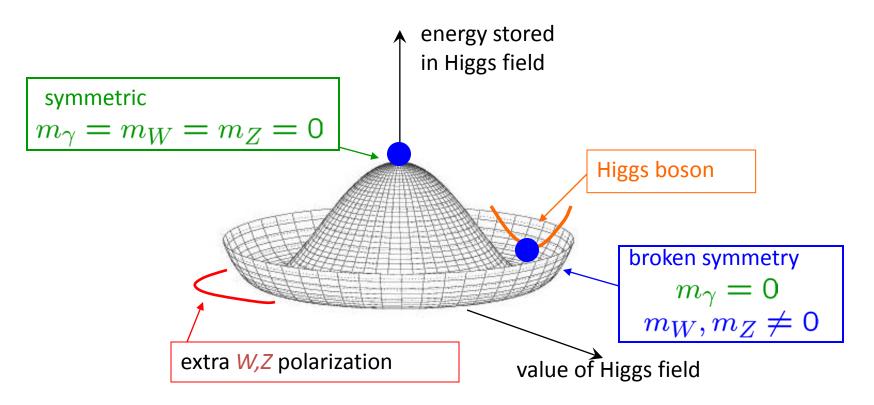
$$\Phi = \begin{pmatrix} \omega^+ \\ \frac{1}{\sqrt{2}} \left(v + H + i \omega^0 \right) \end{pmatrix},$$
$$\omega^{\pm} \equiv (\omega^1 \mp i \omega^2) / \sqrt{2}.$$

where

• The non-zero scalar vacuum expectation value breaks the electroweak symmetry, thereby generating three Goldstone bosons, ω^a (a = 1, 2, 3).

Breaking the Electroweak Symmetry

Higgs imagined a field filling all of space, with a "weak charge". Energy forces it to be **nonzero** at bottom of the "Mexican hat".



• The couplings of the gauge bosons to the $SU(2)_L \times U(1)_Y$ currents are

$$\mathscr{L}_{int} = \frac{1}{2}gW^{\mu a}T^{a}_{\mu L} + \frac{1}{2}g'B^{\mu}Y_{\mu}.$$

Decomposing $T_L = \frac{1}{2}(j_V - j_A)$ into vector and axial vector currents and noting that the electric current, $j_Q = T^3 + \frac{1}{2}Y$ is purely vector,

$$\mathscr{L}_{
m int}=-rac{1}{2}gW^{\mu a}j^a_{A\mu}+rac{1}{2}g'B^{\mu}j^3_{A\mu}+$$
 vector current couplings .

As previously noted, $\langle 0|j_{A\mu}^{a}|\omega^{b}\rangle = ivp_{\mu}\delta^{ab}$. The δ^{ab} factor is a consequence of the global *custodial* SU(2)_L×SU(2)_R symmetry of the scalar potential. Computing the vector boson masses as before yields a 4 × 4 squared-mass matrix,

$$\frac{v^2}{4} \begin{pmatrix} g^2 & 0 & 0 & 0 \\ 0 & g^2 & 0 & 0 \\ 0 & 0 & g^2 & -gg' \\ 0 & 0 & -gg' & g'^2 \end{pmatrix}$$

Diagonalizing this matrix yields

$$m_W^2 = \frac{1}{4}g^2v^2$$
, $m_Z^2 = \frac{1}{4}(g^2 + g'^2)v^2 = \frac{m_W^2}{\cos^2\theta_W}$,

and it follows that (at tree-level), the rho-parameter is

$$\rho \equiv \frac{m_W^2}{m_Z^2 \cos^2 \theta_W} = 1 \,.$$

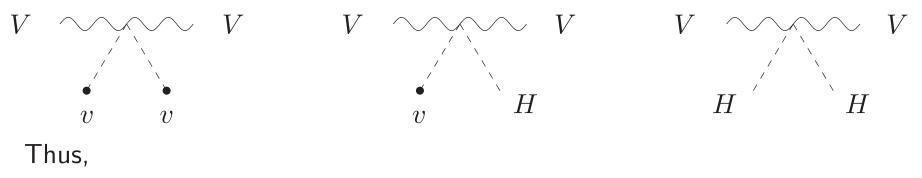
• One scalar degree of freedom is left over—the Higgs boson, *H*, with self-interactions,

$$V(H) = \frac{1}{2}\lambda \left[\left(\frac{H+v}{\sqrt{2}} \right)^2 - \frac{v^2}{2} \right]^2 = \frac{1}{8}\lambda \left[H^4 + 4H^3v + 4H^2v^2 \right]$$

H is a neutral CP-even scalar, whose interactions are precisely predicted, but whose squared-mass, $m_H^2 = \lambda v^2$, depends on the unknown strength of the scalar self-coupling—the only unknown parameter of the model.

Mass generation and Higgs couplings in the SM

Gauge bosons ($V = W^{\pm}$ or Z) acquire mass via interaction with the Higgs vacuum condensate.



 $g_{HVV} = 2m_V^2/v$, and $g_{HHVV} = 2m_V^2/v^2$,

i.e., the Higgs couplings to vector bosons are proportional to the corresponding boson squared-mass.

Likewise, by replacing V with the Higgs boson H in the above diagrams, the Higgs self-couplings are also proportional to the square of the Higgs mass:

$$g_{HHH} = 3\lambda v = \frac{3m_H^2}{v}$$
, and $g_{HHHH} = 3\lambda = \frac{3m_H^2}{v^2}$.

Fermions in the Standard Model

Given a four-component fermion f, we can project out the right and left-handed parts:

$$f_R \equiv P_R f$$
, $f_L \equiv P_L f$, where $P_{R,L} = \frac{1}{2}(1 \pm \gamma_5)$.

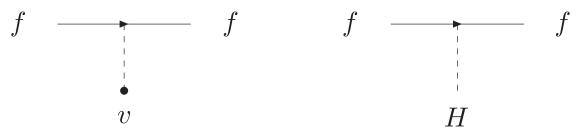
Under the electroweak gauge group, the right and left-handed components of each fermion has different $SU(2) \times U(1)_Y$ quantum numbers:

fermions	SU(2)	$U(1)_{\rm Y}$
$(u,e^-)_L$	2	-1
e_R^-	1	-2
$(u,d)_L$	2	1/3
u_R	1	4/3
d_R	1	-2/3

where the electric charge is related to the U(1)_Y hypercharge by $Q = T_3 + \frac{1}{2}Y$.

Before electroweak symmetry breaking, Standard Model fermions are massless, since the fermion mass term $\mathcal{L}_m = -m(\bar{f}_R f_L + \bar{f}_L f_R)$ is not gauge invariant.

The generation of masses for quarks and leptons is especially elegant in the SM. The fermions couple to the Higgs field through the gauge invariant Yukawa couplings (see below). The quarks and charged leptons acquire mass when Φ^0 acquires a vacuum expectation value:



Thus, $g_{Hf\bar{f}} = m_f/v$, *i.e.*, Higgs couplings to fermions are proportional to the corresponding fermion mass.

It is remarkable that the neutral Higgs boson coupling to fermions is flavordiagonal. This is a consequence of the Higgs-fermion Yukawa couplings:

$$\mathcal{L}_{\text{Yukawa}} = -h_u^{ij} (\bar{u}_R^i u_L^j \Phi^0 - \bar{u}_R^i d_L^j \Phi^+) - h_d^{ij} (\bar{d}_R^i d_L^j \Phi^0^* + \bar{d}_R^i u_L^j \Phi^-) + \text{h.c.} ,$$

where i, j are generation labels and h_u and h_d are arbitrary complex 3×3 matrices. Writing $\Phi^0 = (v + H)/\sqrt{2}$, we identify the quark mass matrices,

$$M_u^{ij} \equiv h_u^{ij} \frac{v}{\sqrt{2}}, \qquad \qquad M_d^{ij} \equiv h_d^{ij} \frac{v}{\sqrt{2}}$$

One is free to redefine the quark fields:

$$u_L \to V_L^U u_L$$
, $u_R \to V_R^U u_R$, $d_L \to V_L^D d_L$, $d_R \to V_R^D d_R$,

where V_L^U , V_R^U , V_L^D , and V_R^D are unitary matrices chosen such that

$$V_R^{U\dagger} M_u V_L^U = \text{diag}(m_u, m_c, m_t), \qquad V_R^{D\dagger} M_d V_L^D = \text{diag}(m_d, m_s, m_b),$$

such that the m_i are the positive quark masses (this is the *singular value* decomposition of linear algebra).

Having diagonalized the quark mass matrices, the neutral Higgs Yukawa couplings are automatically flavor-diagonal.[†] Hence the SM possesses no flavor-changing neutral currents (FCNCs) mediated by neutral Higgs boson (or gauge boson) exchange at tree-level.

[†]Independently of the Higgs sector, the quark couplings to Z and γ are automatically flavor diagonal. Flavor dependence only enters the quark couplings to the W^{\pm} via the Cabibbo-Kobayashi-Maskawa (CKM) matrix, $K \equiv V_L^{U \dagger} V_L^D$.

Phenomenology of the SM Higgs Boson

Once the mass of the SM Higgs boson is fixed, its phenomenological profile is completely determined. At tree level (where $V = W^{\pm}$ or Z),

Vertex	Coupling
HVV	$2m_V^2/v$
HHVV	$2m_V^2/v^2$
HHH	$3m_H^2/v$
HHHH	$3m_H^2/v^2$
$Hf\bar{f}$	m_f/v

At one-loop, the Higgs boson can couple to gluons and photons. Only particles in the loop with mass $\gtrsim O(m_H)$ contribute appreciably.

One-loop Vertex	identity of particles in the loop	
Hgg	quarks	
$H\gamma\gamma$	W^\pm , quarks and charged leptons	
$HZ\gamma$	W^\pm , quarks and charged leptons	

Loop induced Higgs boson couplings

Higgs boson coupling to gluons

At one-loop, the Higgs boson couples to gluons via a loop of quarks:

$$H = \frac{q}{\bar{q}} \xrightarrow{00000} g$$

This diagram leads to an effective Lagrangian

$$\mathcal{L}_{Hgg}^{\text{eff}} = \frac{g\alpha_s N_g}{24\pi m_W} H G^a_{\mu\nu} G^{\mu\nu a} \,,$$

where N_g is roughly the number of quarks heavier than H. More precisely,

$$N_g = \sum_i F_{1/2}(x_i), \qquad x_i \equiv \frac{m_{q_i}^2}{m_H^2},$$

where the loop function $F_{1/2}(x) \to 1$ for $x \gg 1$.

Note that heavy quark loops do *not* decouple. Light quark loops are negligible, as $F_{1/2}(x) \rightarrow \frac{3}{2}x^2 \ln x$ for $x \ll 1$.

The dominant mechanism for Higgs production at the LHC is gluon-gluon fusion. At leading order,

$$\frac{d\sigma}{dy}(pp \to H + X) = \frac{\pi^2 \Gamma(H \to gg)}{8m_H^3} g(x_+, m_H^2) g(x_-, m_H^2) \,,$$

where $g(\boldsymbol{x},Q^2)$ is the gluon distribution function at the scale Q^2 and

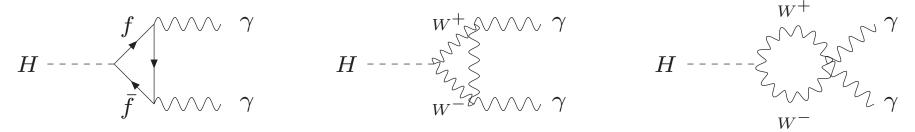
$$x_{\pm} \equiv \frac{m_H e^{\pm y}}{\sqrt{s}}, \qquad y = \frac{1}{2} \ln \left(\frac{E + p_{||}}{E - p_{||}} \right)$$

The rapidity y is defined in terms of the Higgs boson energy and longitudinal momentum in the pp center-of-mass frame.

In practice, one needs a much more precise computation of the gluon fusion cross-section (NLO, NNLO, ...).

Higgs boson coupling to photons

At one-loop, the Higgs boson couples to photons via a loop of charged particles:



If charged scalars exist, they would contribute as well. These diagrams lead to an effective Lagrangian $a \sim N$

$$\mathcal{L}_{H\gamma\gamma}^{\text{eff}} = \frac{g\alpha N_{\gamma}}{12\pi m_W} H F_{\mu\nu} F^{\mu\nu} \,,$$

where

$$N_{\gamma} = \sum_{i} N_{ci} e_i^2 F_j(x_i) , \qquad x_i \equiv \frac{m_i^2}{m_H^2}$$

In the sum over loop particles i of mass m_i , $N_{ci} = 3$ for quarks and 1 for color singlets, e_i is the electric charge in units of e and $F_j(x_i)$ is the loop function corresponding to ith particle (with spin j). In the limit of $x \gg 1$,

$$F_j(x) \longrightarrow \begin{cases} 1/4, & j = 0, \\ 1, & j = 1/2, \\ -21/4, & j = 1. \end{cases}$$

Higgs production at hadron colliders

At hadron colliders, the relevant processes are

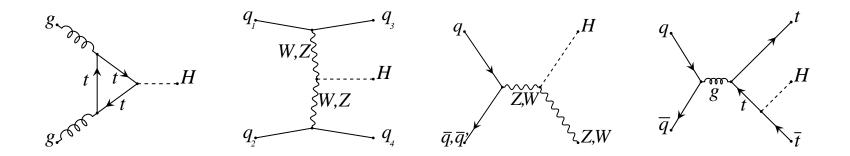
$$gg \to H, \quad H \to \gamma\gamma, \, VV^{(*)},$$

$$qq \to qqV^{(*)}V^{(*)} \to qqH, \quad H \to \gamma\gamma, \, \tau^+\tau^-, \, VV^{(*)},$$

$$q\bar{q}^{(\prime)} \to V^{(*)} \to VH, \quad H \to b\bar{b}, WW^{(*)},$$

$$gg, q\bar{q} \to t\bar{t}H, \quad H \to b\bar{b}, \, \gamma\gamma, \, WW^{(*)}.$$

where V = W or Z.

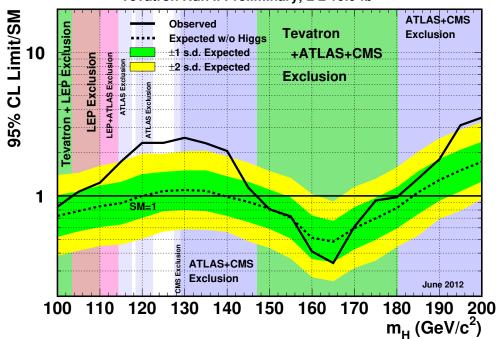


Pre-LHC Expectations for the SM Higgs mass

1. Higgs mass bounds from searches at LEP and the Tevatron.

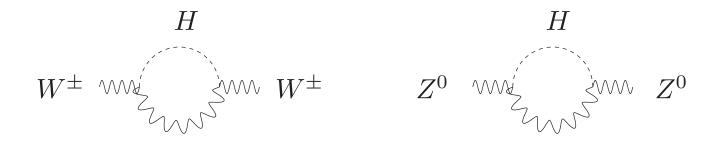
From 1989–2000, experiments at LEP searched for $e^+e^- \rightarrow Z \rightarrow HZ$ (where one of the Z-bosons is on-shell and one is off-shell). A bound was obtained on the SM Higgs mass, $m_H > 114.4 \text{ GeVat} 95\% \text{ CL}$.

Tevatron data extended the Higgs mass exclusion region to $147~{
m GeV} < m_H < 180~{
m GeV}$ at 95% CL. Tevatron Run II Preliminary, L \leq 10.0 fb⁻¹

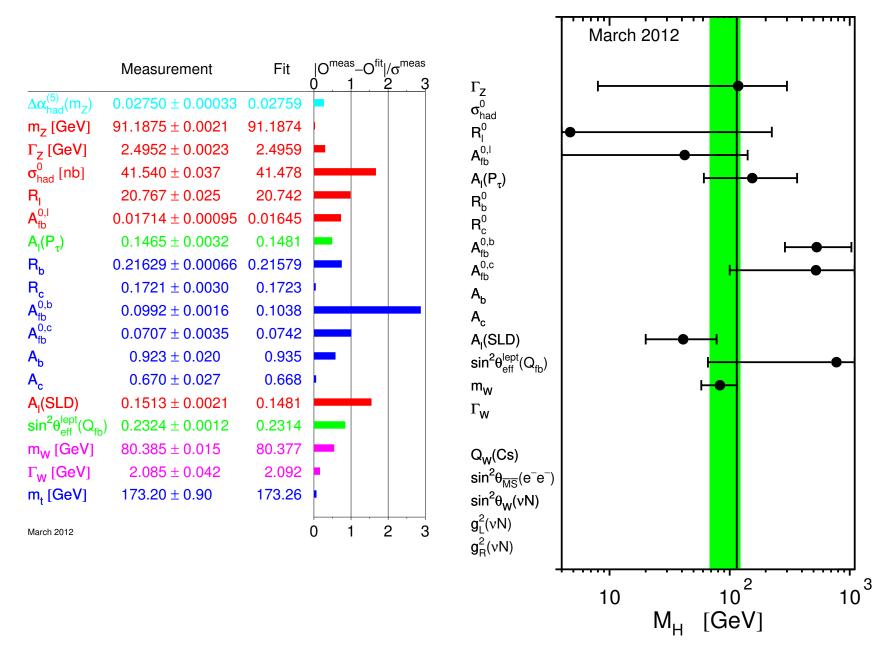


2. Consequences of precision electroweak data.

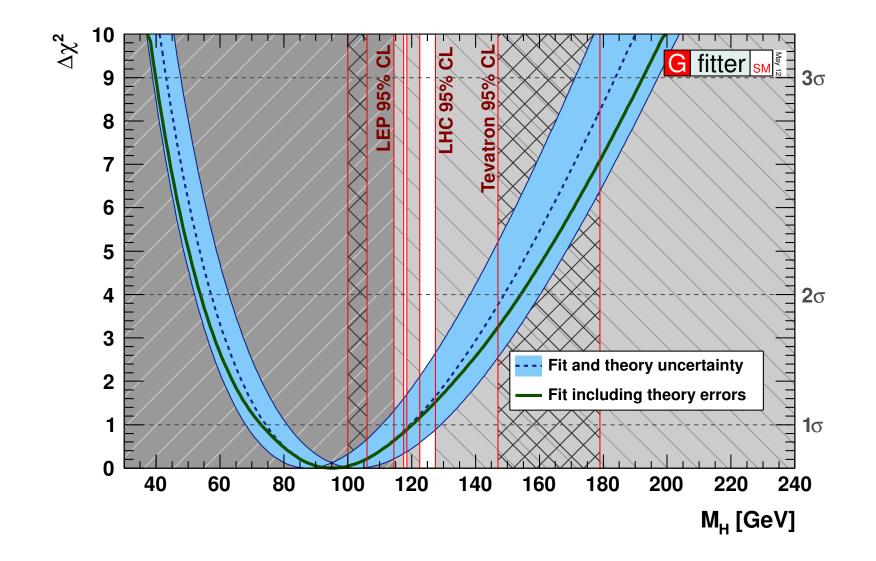
Very precise tests of the Standard Model are possible given the large sample of electroweak data from LEP, SLC and the Tevatron. Although the Higgs boson mass (m_H) is unknown, electroweak observables are sensitive to m_H through quantum corrections. For example, the W and Z masses are shifted slightly due to:



The m_H dependence of the above radiative corrections is logarithmic. Nevertheless, a global fit of many electroweak observables can determine the preferred value of m_H (assuming that the Standard Model is the correct description of the data).



from the LEP, Tevatron and SLD Electroweak Working Groups



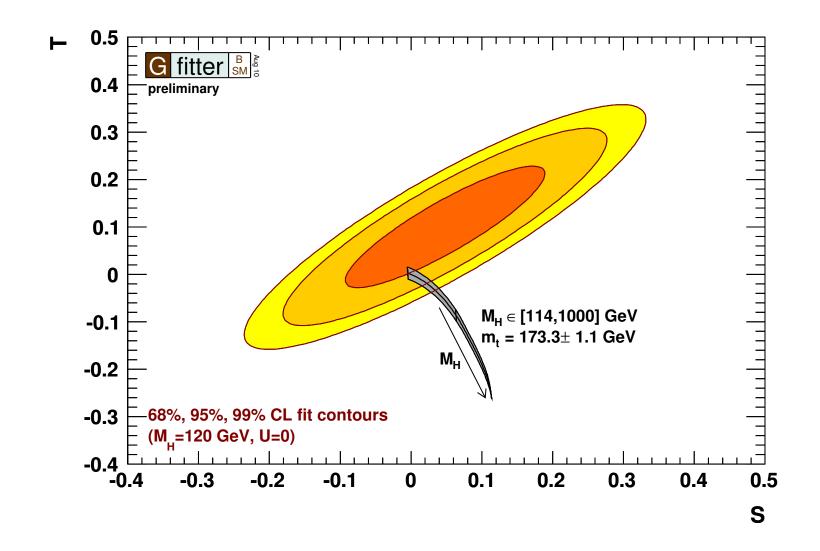
As of May, 2012, the blue band, which does *not* employ the direct Higgs search limits, corresponds to a upper bound of $m_H < 153$ GeV at 95% CL. A similar result of the LEP Electroweak Working group quotes $m_H < 152$ GeV at 95% CL.

Could the Higgs Boson have been significantly heavier?

If new physics beyond the Standard Model (SM) exists, it almost certainly couples to W and Z bosons. Then, there will be additional shifts in the W and Z mass due to the appearance of new particles in loops. In many cases, these effects can be parameterized in terms of two quantities, S and T [Peskin and Takeuchi]:

$$\begin{split} \overline{\alpha} T &\equiv \frac{\Pi_{WW}^{\text{new}}(0)}{m_W^2} - \frac{\Pi_{ZZ}^{\text{new}}(0)}{m_Z^2}, \\ \frac{\overline{\alpha}}{4\overline{s}_Z^2 \overline{c}_Z^2} S &\equiv \frac{\Pi_{ZZ}^{\text{new}}(m_Z^2) - \Pi_{ZZ}^{\text{new}}(0)}{m_Z^2} - \left(\frac{\overline{c}_Z^2 - \overline{s}_Z^2}{\overline{c}_Z \overline{s}_Z}\right) \frac{\Pi_{Z\gamma}^{\text{new}}(m_Z^2)}{m_Z^2} - \frac{\Pi_{\gamma\gamma}^{\text{new}}(m_Z^2)}{m_Z^2}, \end{split}$$

where $s \equiv \sin \theta_W$, $c \equiv \cos \theta_W$, and barred quantities are defined in the MS scheme evaluated at m_Z . The $\Pi_{V_aV_b}^{\text{new}}$ are the new physics contributions to the one-loop V_a — V_b vacuum polarization functions.



In order to avoid the conclusion of a light Higgs boson, new physics beyond the SM must be accompanied by a variety of new phenomena at an energy scale between 100 GeV and 1 TeV.

A theoretical upper bound for the Higgs boson mass?

A Higgs boson with a mass greater than 200 GeV requires additional new physics beyond the Standard Model. A SM-like Higgs boson with mass above 600 GeV is not yet excluded by LHC data. But, how heavy can this Higgs boson be?

Let us return to the unitarity argument. Consider the scattering process $W_L^+(p_1)W_L^-(p_2) \rightarrow W_L^+(p_3)W_L^-(p_4)$ at center-of-mass energies $\sqrt{s} \gg m_W$. Each contribution to the tree-level amplitude is proportional to

$$\left[arepsilon_L(p_1) \cdot arepsilon_L(p_2)
ight] \left[arepsilon_L(p_3) \cdot arepsilon_L(p_4)
ight] \sim rac{s^2}{m_W^4}\,,$$

after using the fact that the helicity-zero polarization vector at high energies behaves as $\varepsilon_L^{\mu}(p) \sim p^{\mu}/m_W$. Due to the magic of gauge invariance and the presence of Higgs-exchange contributions, the bad high-energy behavior is removed, and one finds for s, $m_H^2 \gg m_W^2$:

$$\mathcal{M} = -\sqrt{2}G_F m_H^2 \left(\frac{s}{s - m_H^2} + \frac{t}{t - m_H^2}\right)$$

Projecting out the J=0 partial wave and taking $s\gg m_{H}^{2}$,

$$\mathcal{M}^{J=0} = -\frac{G_F m_H^2}{4\pi\sqrt{2}}$$

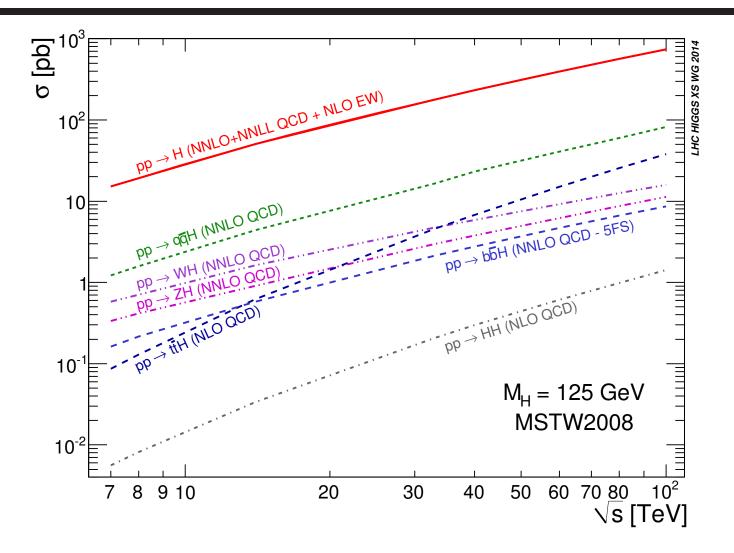
Imposing $|\text{Re } \mathcal{M}^J| \leq \frac{1}{2}$ yields an upper bound on m_h . The most stringent bound is obtained by all considering other possible final states such as $Z_L Z_L$, $Z_L H$ and HH. The end result is:

$$m_H^2 \le \frac{4\pi\sqrt{2}}{3G_F} \simeq (700 \text{ GeV})^2.$$

However, in contrast to our previous analysis of the unitarity bound, the above computation relies on the validity of a tree-level computation. That is, we are implicitly assuming that perturbation theory is valid. If $m_H \gtrsim 700$ GeV, then the Higgs-self coupling parameter, $\lambda = 2m_H^2/v^2$ is becoming large and our perturbative analysis is becoming suspect.

Nevertheless, lattice studies suggest that an upper Higgs mass bound below 1 TeV remains valid even in the strong Higgs self-coupling regime.

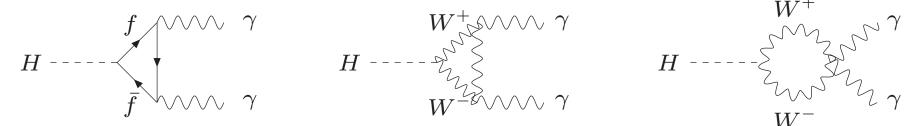
SM Higgs boson production cross-sections at the LHC



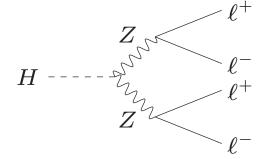
Taken from the LHC Higgs Cross Section Working Group TWiki, https://twiki.cern.ch/twiki/bin/view/LHCPhysics/HiggsEuropeanStrategy

SM Higgs decays at the LHC for $m_H = 125$ GeV

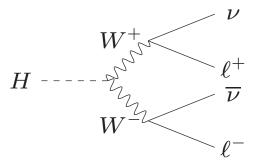
1. The rare decay $H \rightarrow \gamma \gamma$ is the most promising signal.



2. The so-called golden channel, $H \to ZZ \to \ell^+ \ell^- \ell^+ \ell^-$ (where one or both Z bosons are off-shell) is a rare decay for $m_H = 125$ GeV, but is nevertheless visible.



3. The channel, $H \to WW^* \to \ell^+ \nu \ell^- \overline{\nu}$ is also useful, although it does not provide a good Higgs mass determination.



SM Higgs branching ratios for $m_H = 125 \,\, { m GeV}$

Decay mode	Branching fraction [%]
H ightarrow bb	57.5 ± 1.9
$H \to WW$	21.6 ± 0.9
$H \rightarrow gg$	$8.56\ \pm 0.86$
$H \to \tau \tau$	6.30 ± 0.36
$H \to cc$	$2.90\ \pm 0.35$
$H \rightarrow ZZ$	2.67 ± 0.11
$H ightarrow \gamma \gamma$	0.228 ± 0.011
$H \to Z\gamma$	$0.155 \ \pm 0.014$
$H \to \mu \mu$	0.022 ± 0.001

The Discovery of the Higgs boson is announced on July 4, 2012

The CERN update of the search for the Higgs boson, simulcast at ICHEP-2012 in Melbourne, Australia



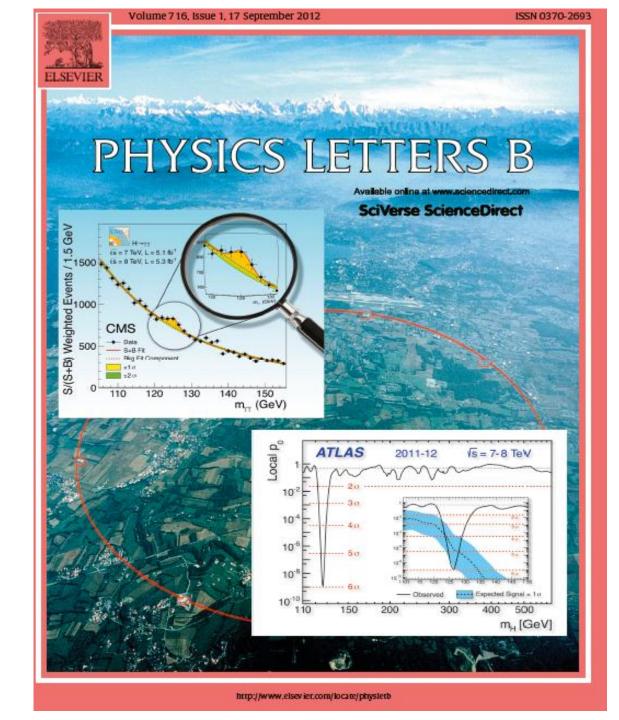
The discovery of the new boson is published in Physics Letters B.

ATLAS Collaboration:

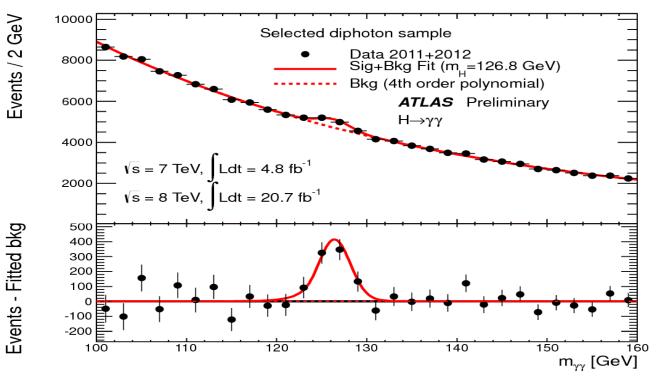
Physics Letters B716 (2012) 1-29

CMS Collaboration:

Physics Letters B716 (2012) 30-61

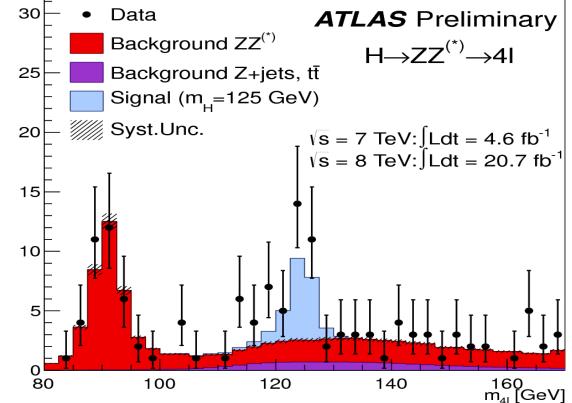


A boson is discovered at the LHC by the ATLAS Collaboration



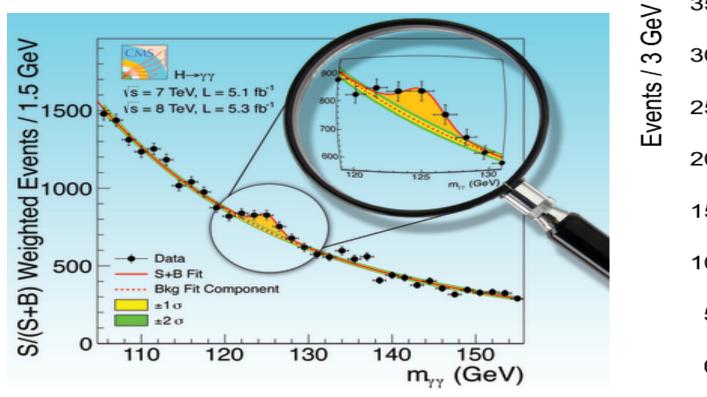
Invariant mass distribution of diphoton candidates for the combined 7 TeV and 8 TeV data samples. The result of a fit to the data of the sum of a signal component fixed to

 m_{H} = 126.8 GeV and a background component described by a fourth-order Bernstein polynomial is superimposed. The bottom inset displays the residuals of the data with respect to the fitted background component. Taken from ATLAS-CONF-2013-012 (March, 2013).

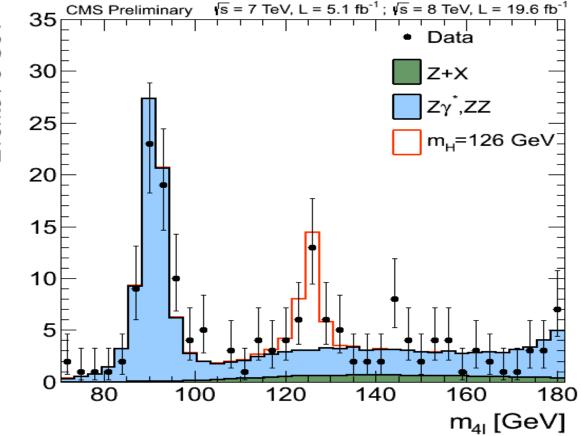


The distribution of the four-lepton invariant mass for the selected candidates, compared to the background expectation in the 80 to 170 GeV mass range, for the combination of the 7 TeV 8 TeV data. The signal expectation for a Higgs boson with m_{H} =125 GeV is also shown. Taken from ATLAS-CONF-2013-013 (March, 2013).

A boson is discovered at the LHC by the CMS Collaboration



The diphoton invariant mass distribution with each event weighted by the S/(S+B) value of its category. The lines represent the fitted background and signal, and the colored bands represent the ±1 and ±2 standard deviation uncertainties in the background estimate. The inset shows the central part of the unweighted invariant mass distribution. Taken from Physics Letters **B716** (2012) 30—61.



Distribution of the four-lepton reconstructed mass in full mass range for the sum of the 4e, 4 μ , and 2e2 μ channels. Points represent the data, shaded histograms represent the background and unshaded histogram the signal expectations. The expected distributions are presented as stacked histograms. The measurements are presented for the sum of the data collected at Vs = 7 TeV and Vs = 8 TeV. [70-180] GeV range - 3 GeV bin width. Taken from CMS-PAS-HIG-13-002 (March, 2013).



Observed Higgs properties vs. SM expectations

At the LHC, what is measured is the cross section for Higgs production times the branching ratio into a particular final state. For the process $i \to H \to f$, define the signal strengths for the production, μ_i and for the decay, μ^f , by

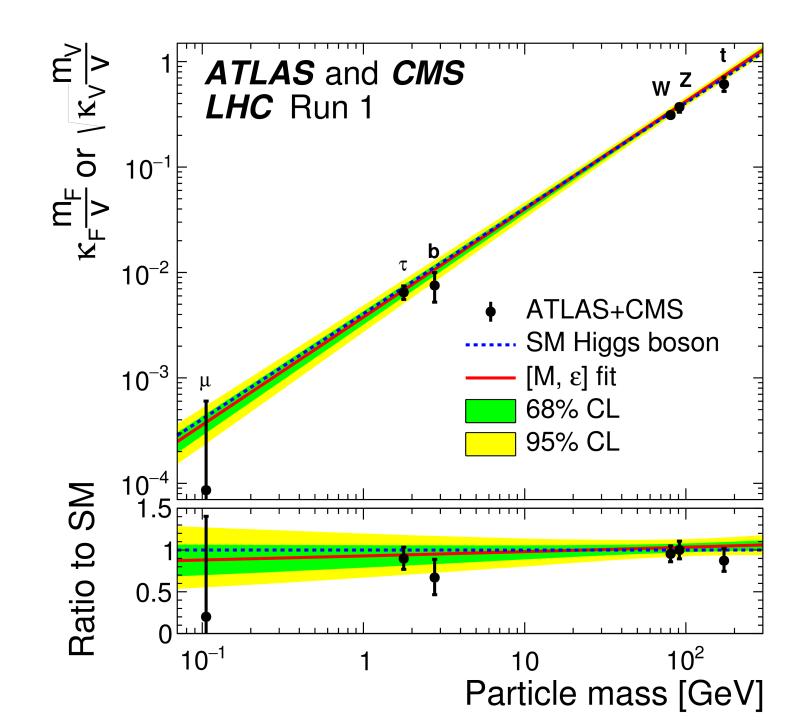
$$\mu_i \equiv \frac{\sigma_i}{(\sigma_i)_{\rm SM}}, \qquad \mu^f \equiv \frac{{\rm B}^f}{({\rm B}^f)_{\rm SM}},$$

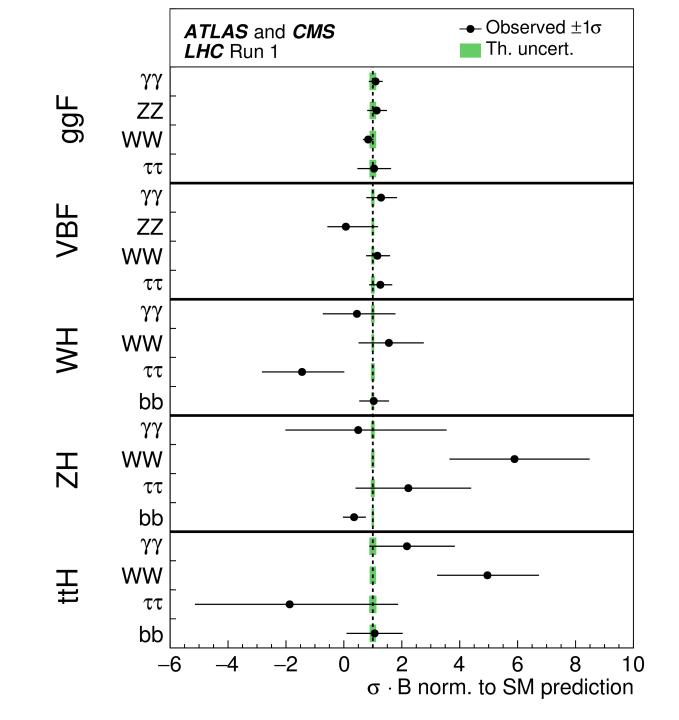
where i = gg fusion, vector boson fusion (VBF), WH, ZH and $t\bar{t}H$ associated production, and B^f is the branching ratio for H to decay into f = ZZ, WW, $\gamma\gamma$, $\tau^+\tau^-$ and $b\bar{b}$ (and eventually, $\mu^+\mu^-$ and $Z\gamma$).

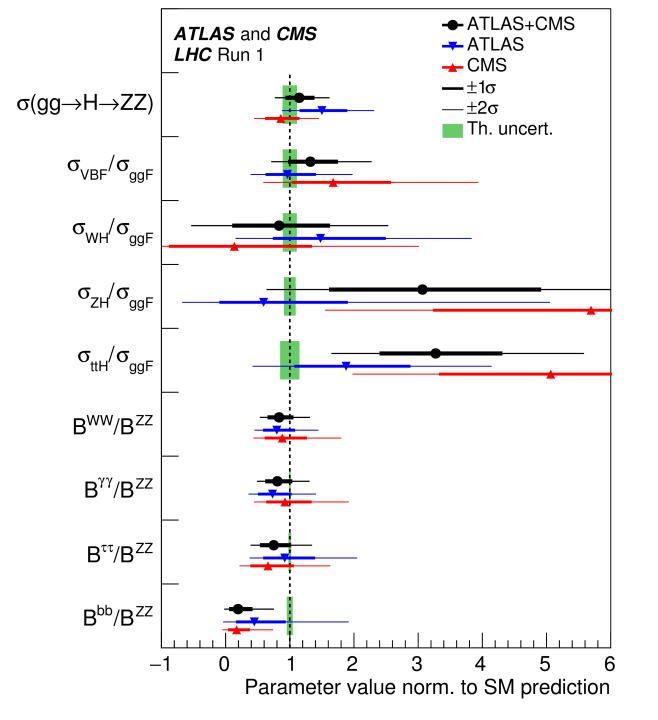
The actual experimental observable is the signal strength μ_i^f for the combined production and decay,

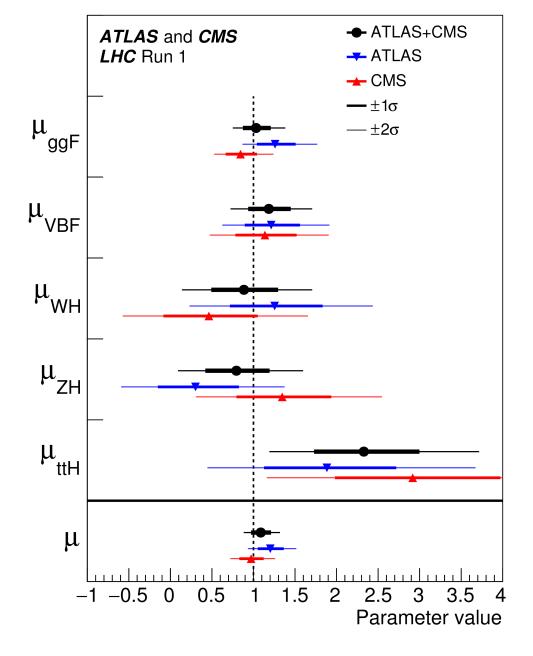
$$\mu_i^f \equiv \frac{\sigma_i \cdot \mathbf{B}^f}{(\sigma_i)_{\mathrm{SM}} \cdot (\mathbf{B}^f)_{\mathrm{SM}}}$$

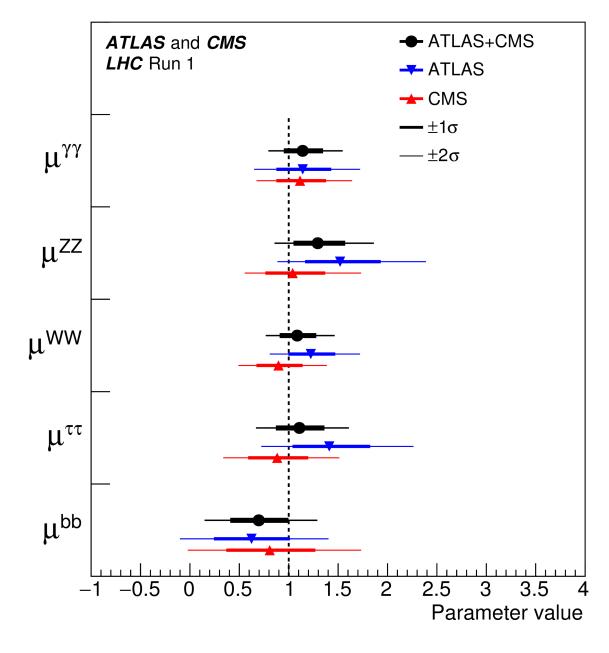
The combined ATLAS and CMS Higgs data from Run-I of the LHC has recently been presented in arXiv:1606.02266.











Assumes that Higgs production modes are according to the SM

Assumes that Higgs decays are according to the SM