Dark Matter Annihilation into Fermions and a Photon

> Debtosh Chowdhury INFN, Rome

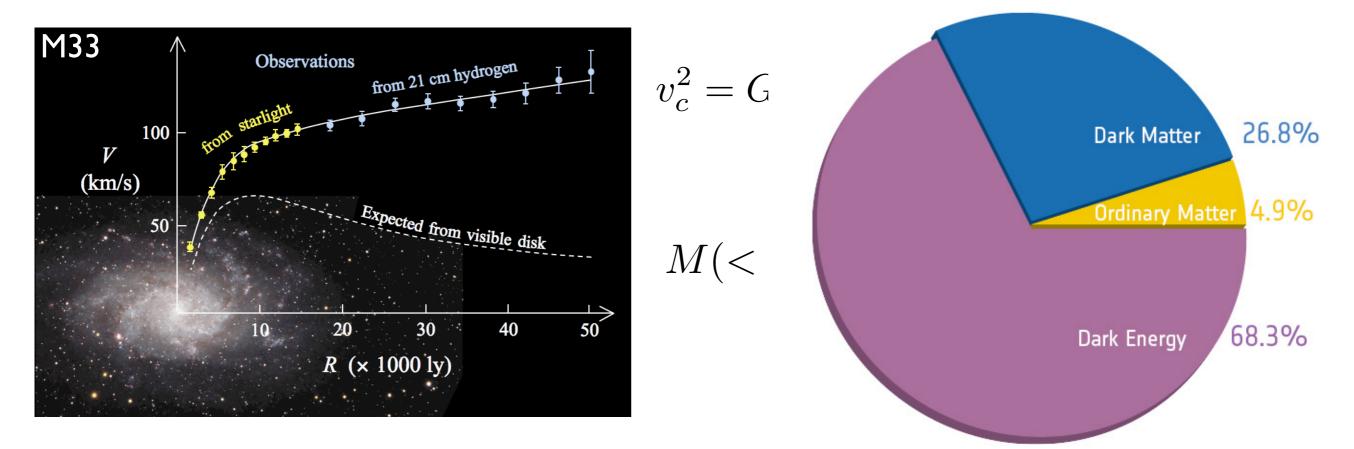
in collaboration w/ A. lyer and R. Laha [arXiv:1601.06140]

> SUSY 2016 Melbourne, Australia July 4, 2016

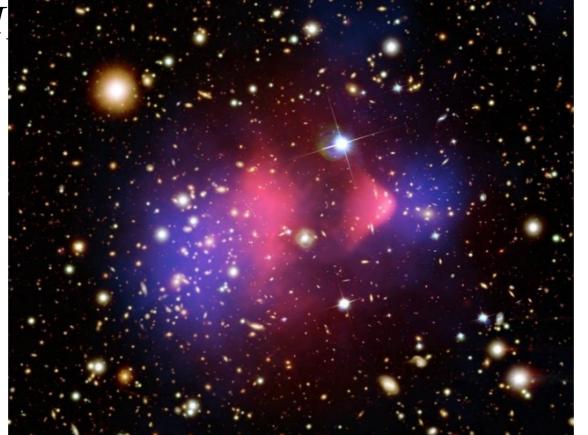
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Evidence of Dark Matter



$$v_c = const. \Rightarrow M$$



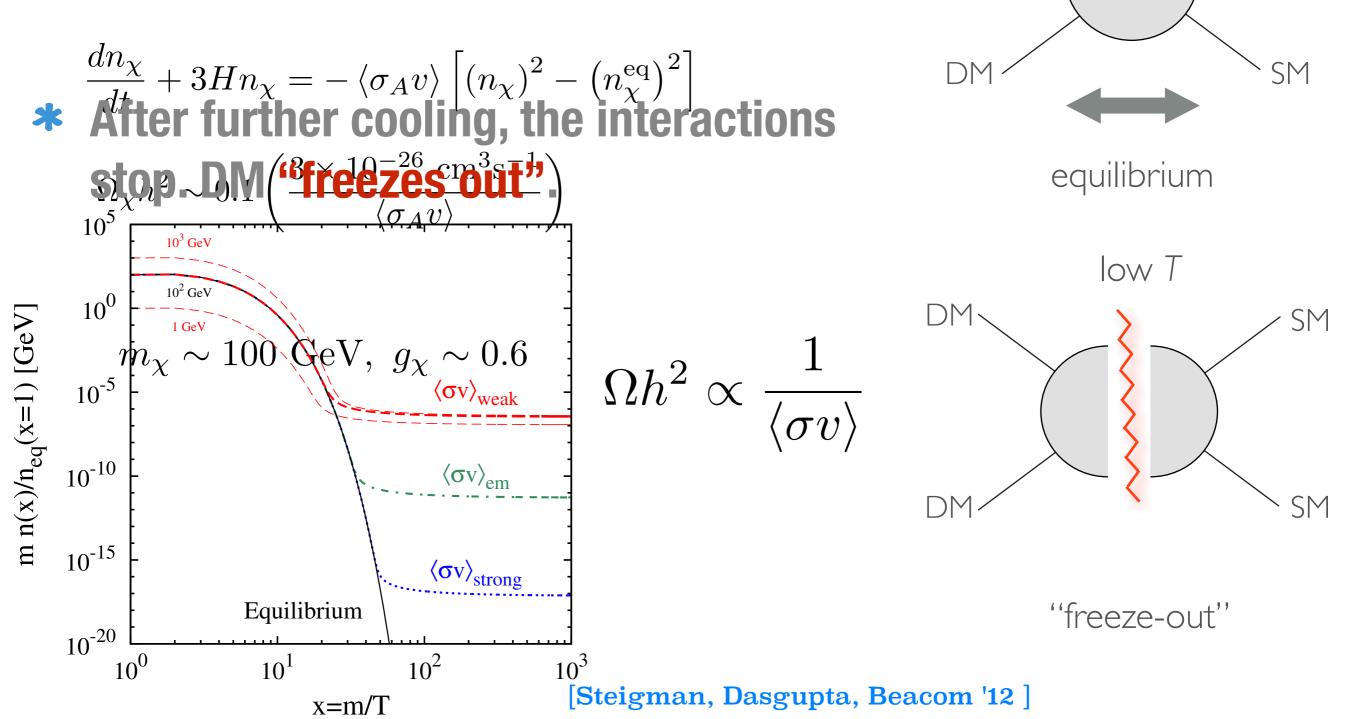
Thermal Relic

high T

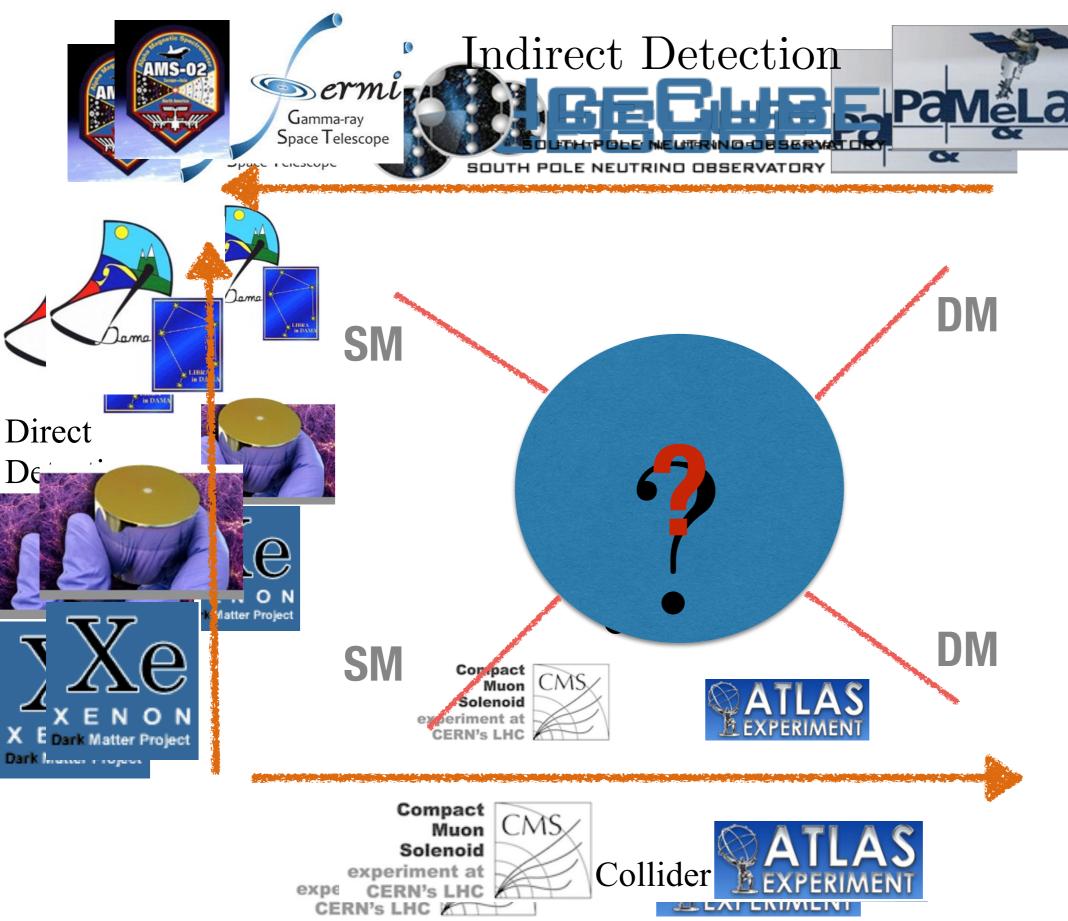
SM

DM

- * In early Universe DM DM \Leftrightarrow SM SM.
- ***** Universe cools down DM DM \Rightarrow SM SM.



Dark Matter Detection



DM Annihilation into Fermions

$$\mathcal{L} = \mathcal{L}_{\rm SM} + \mathcal{L}_{\chi} + \mathcal{L}_{\eta} + \mathcal{L}_{\rm int}$$

$$\mathcal{L}_{\chi} = \frac{1}{2} \bar{\chi}^c i \partial \chi - \frac{1}{2} m_{\chi} \bar{\chi}^c \chi ,$$

$$\mathcal{L}_{\eta} = (D_{\mu} \eta)^{\dagger} (D^{\mu} \eta) - m_{\eta}^2 \eta^{\dagger} \eta$$

$$\mathcal{L}_{\rm int} = -y \bar{\chi} \Psi_R \eta + \text{h.c.}$$

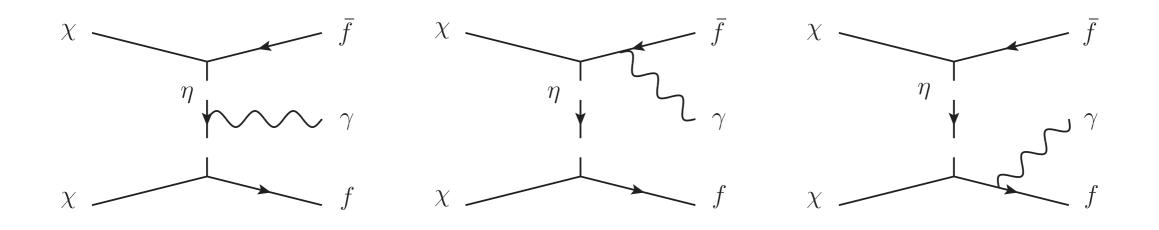
$$\langle \sigma v \rangle = a + bv^2 + \mathcal{O}(v^4) \qquad \qquad \mu \equiv (m_{\eta}/m_{\chi})^2$$

$$(\sigma v)_{2\text{-body}}^{\text{s-wave}} = \frac{y^4 N_c}{32\pi m_{\chi}^2} \frac{m_f^2}{m_{\chi}^2} \frac{1}{(1+\mu)^2} \qquad (\sigma v)_{2\text{-body}}^{p\text{-wave}} = v^2 \frac{y^4 N_c}{48\pi m_{\chi}^2} \frac{1+\mu^2}{(1+\mu)^4}$$

$$v \sim 10^{-3}$$

[Bergstrom '89, ...]

Virtual Internal Bremsstrahlung



$$(\sigma v)_{3\text{-body}} \simeq \frac{\alpha_{\text{em}} y^4 N_c Q_f^2}{64\pi^2 m_\chi^2} \left\{ (\mu+1) \left[\frac{\pi^2}{6} - \ln^2 \left(\frac{\mu+1}{2\mu} \right) - 2\text{Li}_2 \left(\frac{\mu+1}{2\mu} \right) \right] + \frac{4\mu+3}{\mu+1} + \frac{4\mu^2 - 3\mu - 1}{2\mu} \ln \left(\frac{\mu-1}{\mu+1} \right) \right\}$$

VIB lifts the helicity suppression of DM annihilation into pair of fermions [Bergstrom '89, ...]

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G. Jungman et al. / Physics Reports 267 (1996) 195-373

221

(3.4)

 H_u

ets

Using the above relations $(H = 1.66g_*^{1/2} T^2/m_{\text{Pl}})$ and the freezeout condition $\Gamma = n_{\chi} \langle \sigma_A v \rangle = H$, we find

$$(n_{\chi}/s)_{0} = (n_{\chi}/s)_{f} \simeq 100/(m_{\chi}m_{P1}g_{*}^{1/2} \langle \sigma_{A}v \rangle)$$

$$\simeq 10^{-8}/[(m_{\chi}/\text{GeV})(\langle \sigma_{A}v \rangle/10^{-27} \text{ cm}^{3} \text{ s}^{-1})], \qquad (3.3)$$

where the subscript f denotes the value at freezeout and the subscript 0 denotes the value today. The current entropy density is $s_0 \simeq 4000 \text{ cm}^{-3}$, and the critical density today is $\rho_c \simeq 10^{-5} h^2 \text{ GeV cm}^{-3}$, where h is the Hubble constant in units of $100 \text{ km s}^{-1} \text{ Mpc}^{-1}$, so the present mass density in units of the critical density is given by

$$\Omega_{\chi}h^2 = m_{\chi}n_{\chi}/\rho_{\rm c} \simeq (3 \times 10^{-27}\,{\rm cm}^3\,{\rm s}^{-1}/\langle \sigma_{\rm A}v \rangle) \,.$$

The result is independent of the mass of the WIMP (except for logarithmic corrections), and is inversely propertional to its annihilation cross section.

Fig. 4 shows numerical solutions to the Boltzmann equation. The equilibrium (solid line) and actual (dashed lines) abundances per comoving volume are plotted as a function of $x \equiv m_{\chi}/T$

$$y_{R} \stackrel{\text{0.01}}{\underset{10^{-8}}{\overset{1$$

VIB in Effective Operator Model

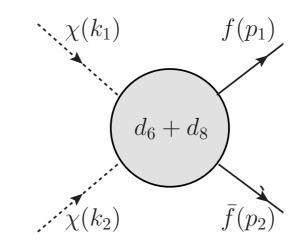
$$\mathcal{L}_{\mathrm{d}=6} = \frac{1}{\Lambda^2} (\bar{\chi}\gamma^5 \gamma^\mu \chi) (\bar{f}\gamma_\mu f)$$

$$\mathcal{L}_{d=8} = \frac{1}{\Lambda^4} (\bar{\chi}\gamma^5 \gamma^\mu \chi) \left[\left(\bar{f}_L \overleftarrow{D_\rho} \right) \gamma_\mu \left(\overrightarrow{D^\rho} f_L \right) + \left(\bar{f}_R \overleftarrow{D_\rho} \right) \gamma_\mu \left(\overrightarrow{D^\rho} f_R \right) \right]$$

$$\begin{split} \bar{f}_L \overleftarrow{D}_\mu &= (\partial_\mu \bar{f}_L) - ig \frac{\sigma^i}{2} W^i_\mu \bar{f}_L - ig' Y_f B_\mu \bar{f}_L \,, \\ \overrightarrow{D}_\mu f_L &= (\partial_\mu f_L) + ig \frac{\sigma^i}{2} W^i_\mu f_L + ig' Y_f B_\mu f_L \,, \\ \bar{f}_R \overleftarrow{D}_\mu &= (\partial_\mu \bar{f}_R) - ig' Y_f B_\mu \bar{f}_R \,, \\ \overrightarrow{D}_\mu f_R &= (\partial_\mu f_R) + ig' Y_f B_\mu f_R \,, \end{split}$$

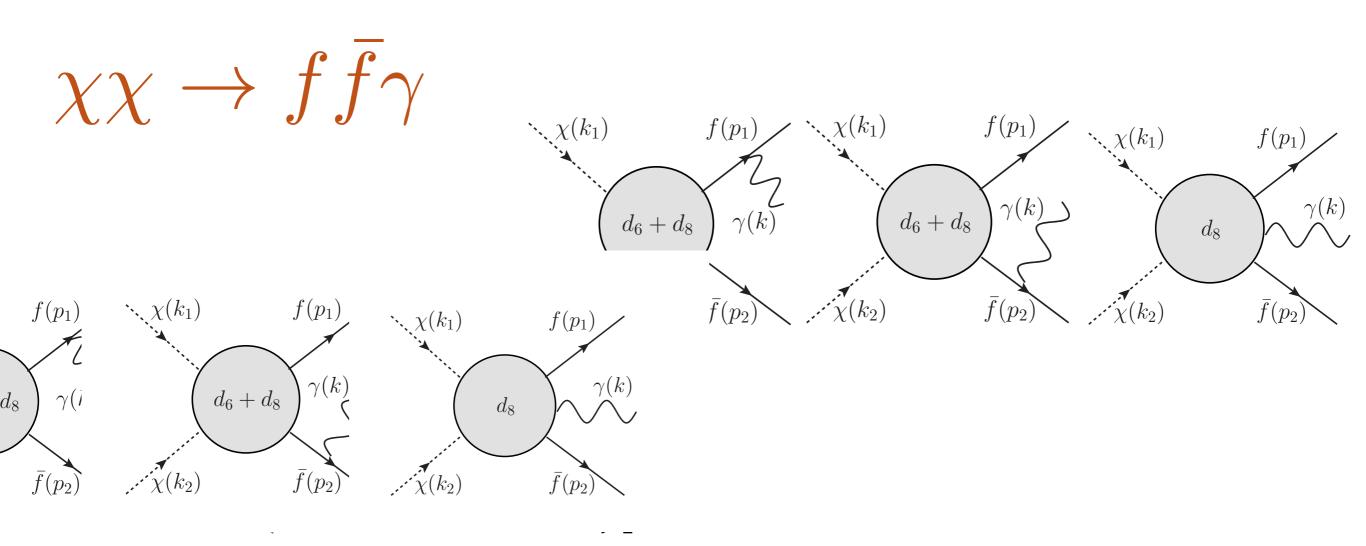
$$\mathcal{L} = d_6 \,\mathcal{L}_{\mathrm{d}=6} + d_8 \,\mathcal{L}_{\mathrm{d}=8}$$

 $\chi\chi\to f\bar{f}$



$$\mathcal{L} = \frac{d_6}{\Lambda^2} (\bar{\chi}\gamma^5 \gamma^\mu \chi) (\bar{f}\gamma_\mu f) + \frac{d_8}{\Lambda^4} (\bar{\chi}\gamma^5 \gamma^\nu \chi) \bigg[\left(\partial_\rho \bar{f} \right) \gamma_\nu \left(\partial^\rho f \right) \bigg]$$

$$\sigma v = \frac{v^2}{3\pi\Lambda^8} \sqrt{1 - \frac{m_f^2}{m_\chi^2}} \left(2m_\chi^2 + m_f^2\right) \left\{ |d_6|^2 \Lambda^4 + |d_8|^2 (2m_\chi^2 + m_f^2)^2 - \Lambda^2 (d_6 d_8^* + d_6^* d_8) (2m_\chi^2 - m_f^2) \right\}$$



$$\mathcal{M} = -i e Q \, \bar{u}(k_1) \gamma^5 \gamma^\mu v(k_2) \left[\left(\frac{d_6}{\Lambda^2} - \frac{d_8}{\Lambda^4} \, p_2 . (p_1 + k) \right) \bar{u}(p_1) \not \in (k) \frac{p_1' + k' + m_f}{(p_1 + k)^2 - m_f^2 + i\epsilon} \gamma_\mu v(p_2) \right. \\ \left. + \left(\frac{d_6}{\Lambda^2} - \frac{d_8}{\Lambda^4} \, p_1 . (p_2 + k) \right) \bar{u}(p_1) \gamma_\mu \frac{-p_2' - k' + m_f}{(p_2 + k)^2 - m_f^2 + i\epsilon} \not \in (k) v(p_2) \right. \\ \left. - \frac{d_8}{\Lambda^4} \bar{u}_{p_1} \epsilon_\rho(k) \gamma_\mu v_{p_2}(p_1^\rho - p_2^\rho) \right]$$

Ratio of the cross-sections

$$d_{6} = 1, d_{8} = 1, v = 10^{-3}$$

$$10^{6}$$

$$10^{6}$$

$$10^{7}$$

$$10^{7}$$

$$10^{7}$$

$$10^{4}$$

$$10^{3}$$

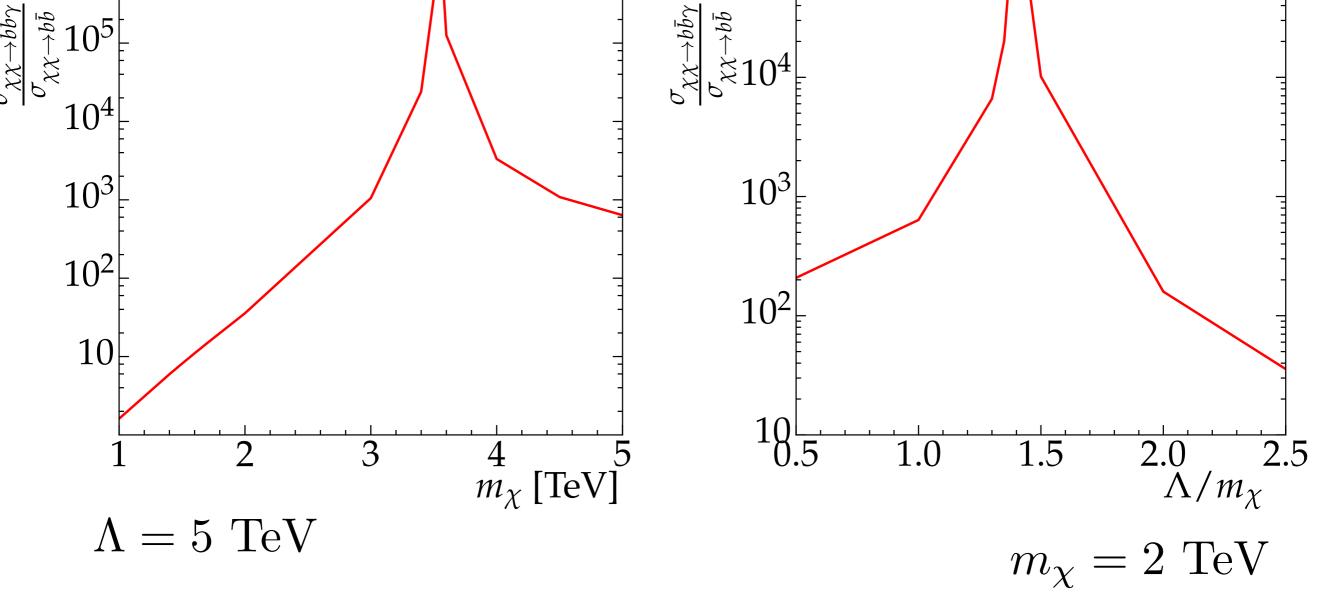
$$10^{3}$$

$$10^{3}$$

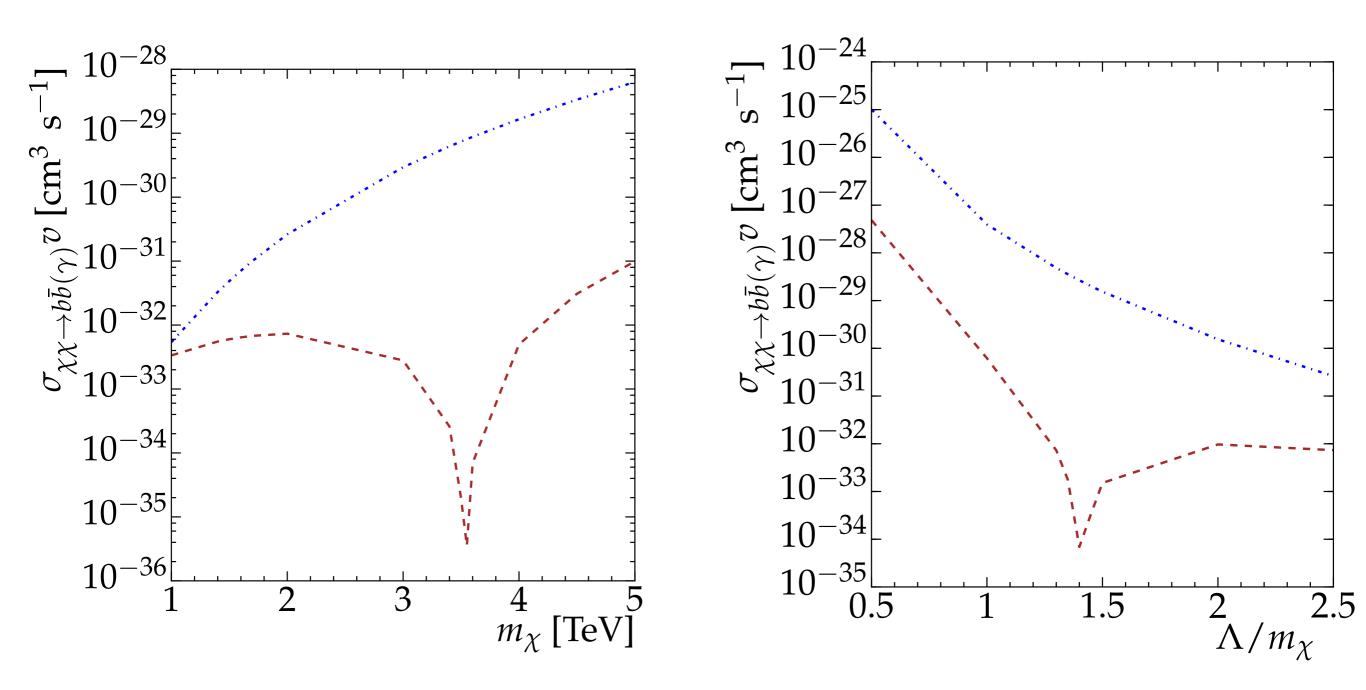
$$10^{3}$$

$$10^{3}$$

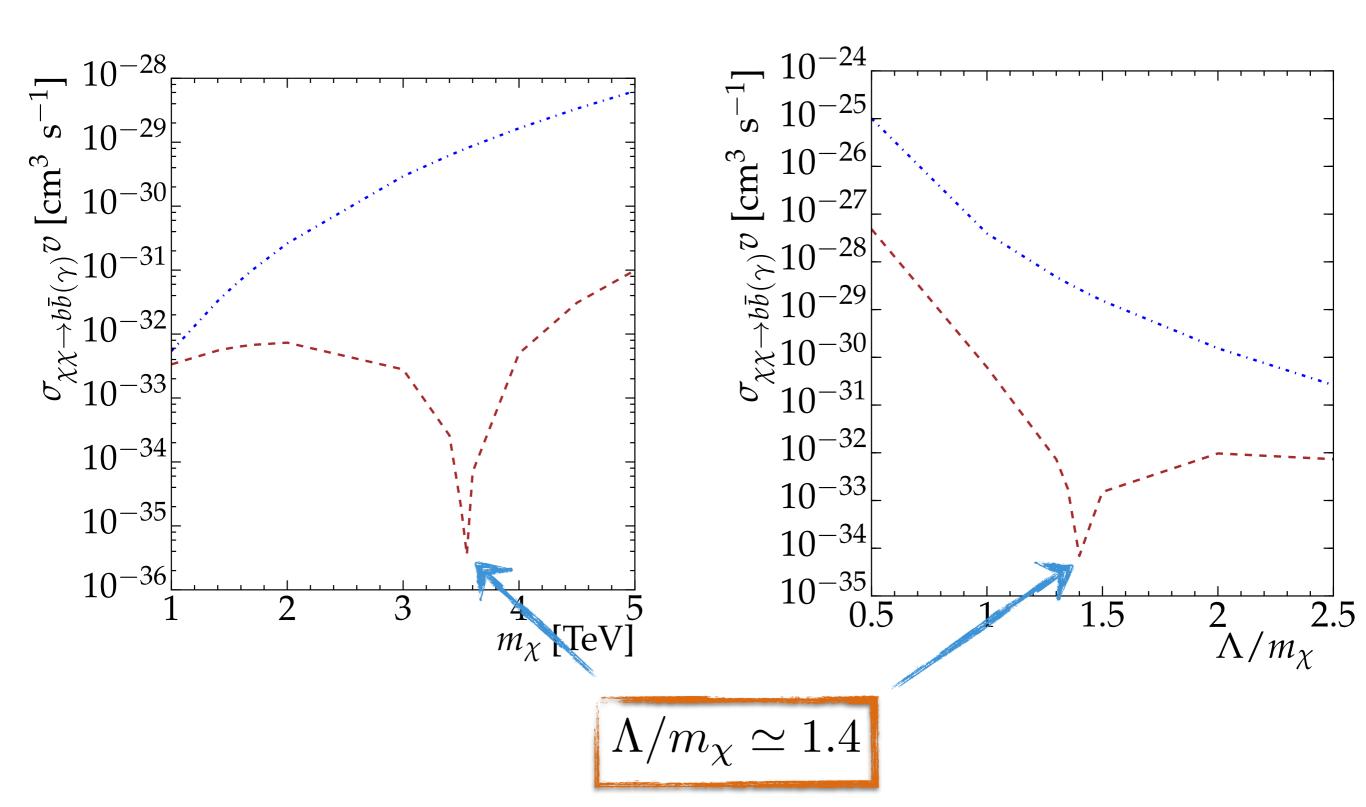
$$10^{3}$$



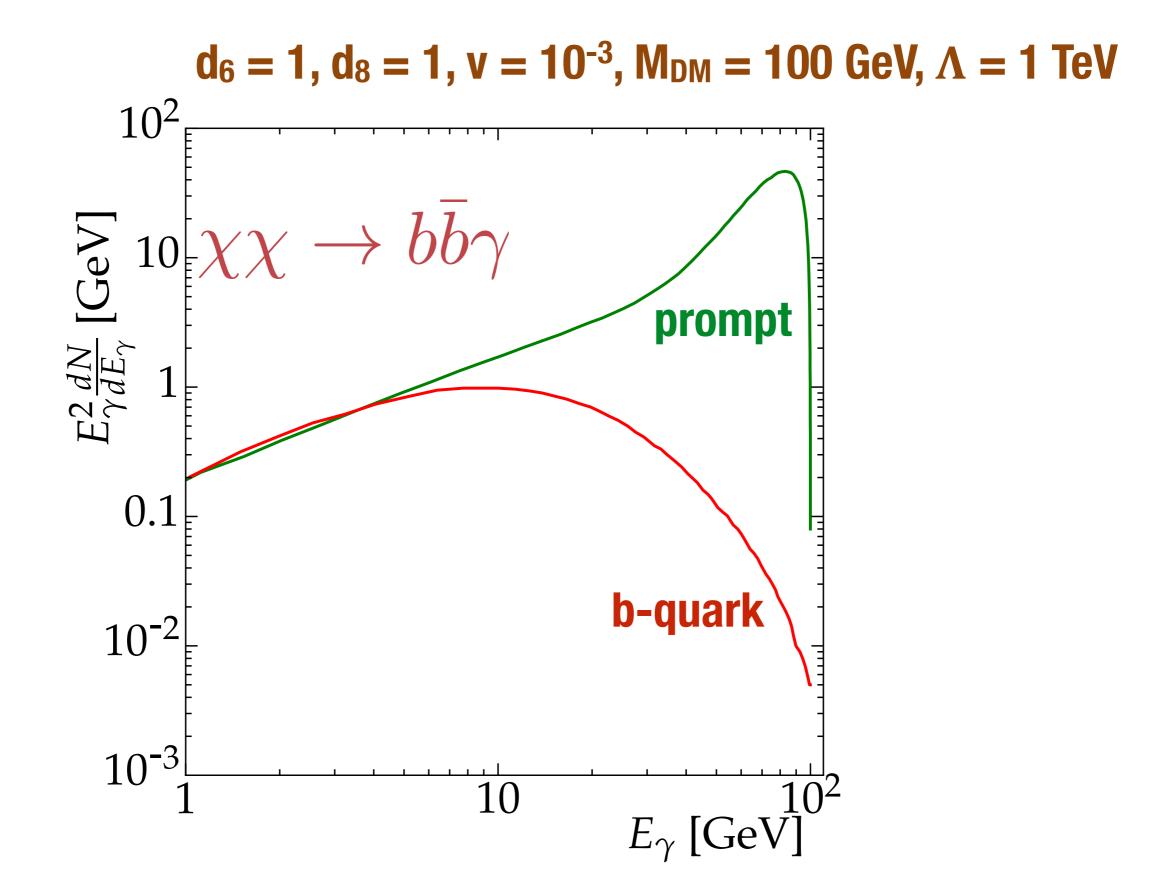
Ratio of the cross-sections



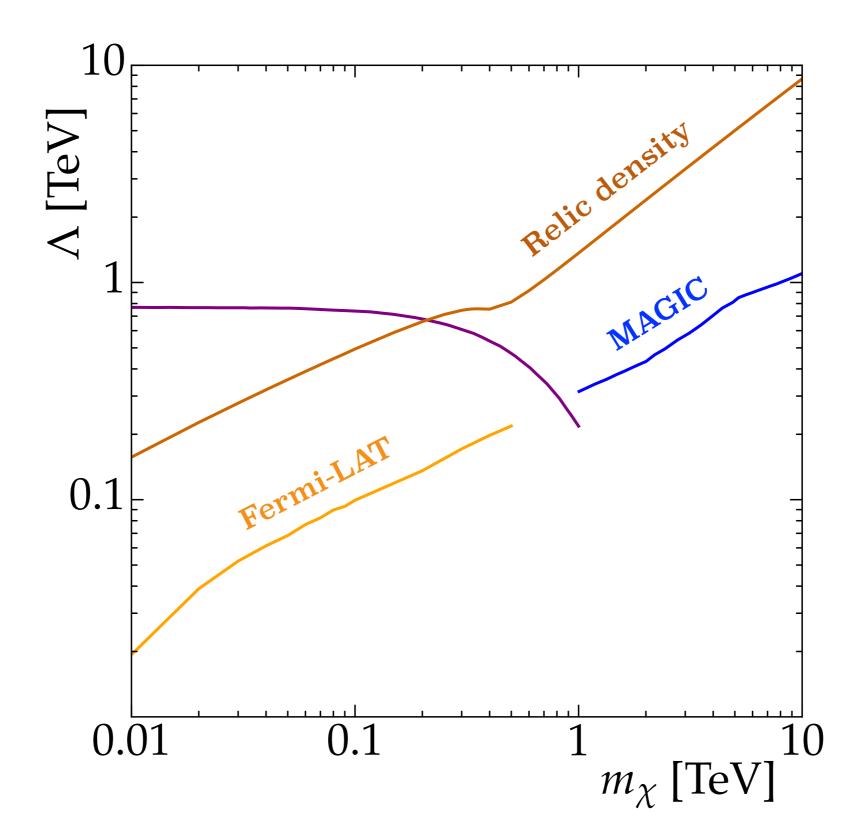
Ratio of the cross-sections



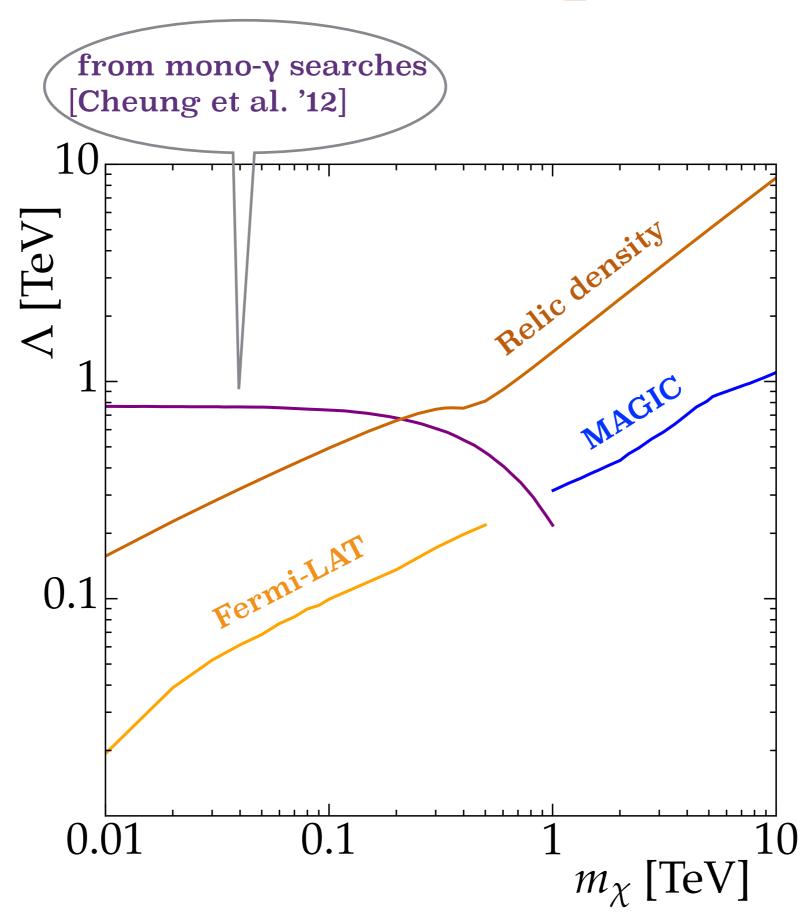
Photon Energy Spectrum



Bound on effective operator scale



Bound on effective operator scale



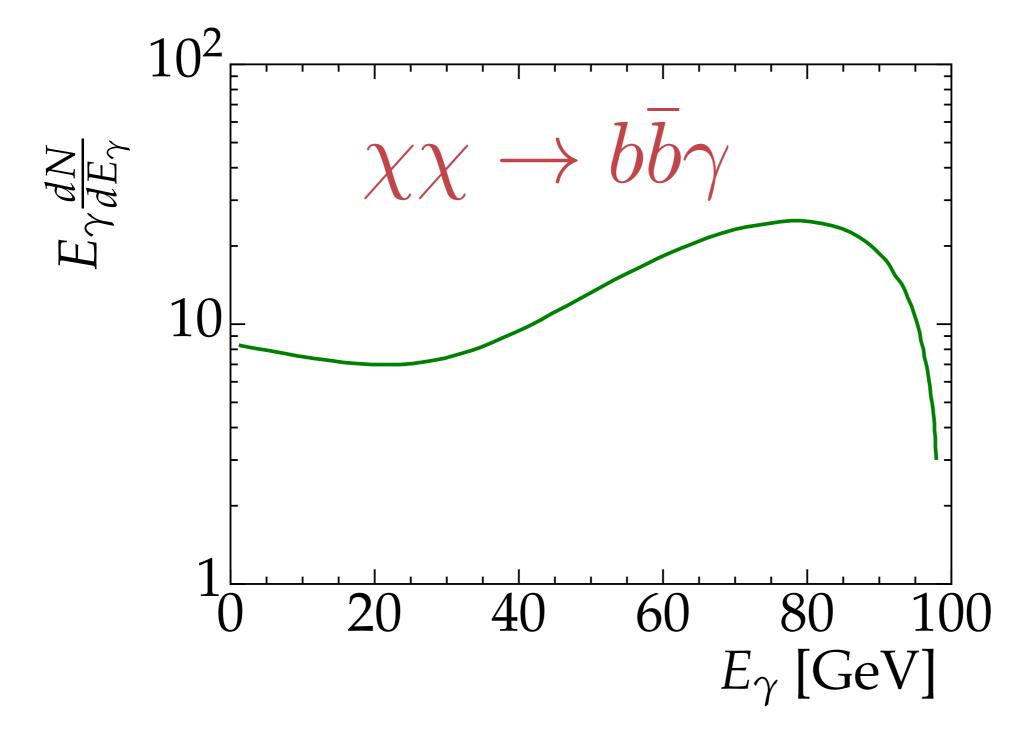
Conclusions

- Electroweak bremsstrahlung lifts the helicity suppression of DM annihilation to fermions.
- ***** dim-8 operator encodes this effect in EFT framework.
- In spite of higher dimensionality of dim-8 operator, it does not suffer any suppression from DM relative velocity.
- Annihilation cross- section from dim 8 operator to the dim 6 operator is always larger at all dark matter mass scales > 1 TeV.
- * Cancellation in the 2-body cross-section between dim 6 and dim 8 for $\Lambda/m_{\chi}\simeq 1.4$
- Bounds on the γ-ray flux and relic density translates into stringent bound on the EFT scale.
- * For high mass DM (> 200 GeV), relic density provides the strongest bound on Λ .

Thank You!!

Photon Energy Spectrum

 $d_6 = 1, d_8 = 1, v = 10^{-3}, M_{DM} = 100 \text{ GeV}, \Lambda = 1 \text{ TeV}$



Photon Energy Spectrum

 $d_6 = 1, d_8 = 1, v = 10^{-3}, M_{DM} = 100 \text{ GeV}, \Lambda = 1 \text{ TeV}$

