



CoEPP

ARC Centre of Excellence for
Particle Physics at the Terascale

Precision Higgs mass prediction in minimal and non-minimal SUSY models

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in collaboration with

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FlexibleSUSY = spectrum generator generator

We can do our calculation in any model because
we implement our algorithm in:

FlexibleSUSY

<https://flexiblesusy.hepforge.org/>

[PA, J.H.Park, D.Stöckinger, A.Voigt CPC 190 (2015) 139-172]



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Model specific details
from:

SARAH

[F.Staub arXiv:0806.0538,
CPC 182 (2011) 808-833,
CPC 181 (2010) 1077-1086]



FlexibleHiggs

The Higgs mass is a very important prediction in SUSY models

Quartic coupling in MSSM is fixed:

$$V_{\phi}^{SM} = \mu^2 |\phi|^2 + \lambda |\phi|^4$$

$$V_{H^0}^{MSSM} = m_1^2 |H_u^0|^2 + m_2^2 |H_d^0|^2 - m_3^2 (H_u^0 H_d^0 + h.c.) + \frac{1}{8} (g'^2 + g^2) v^2$$

$$\Rightarrow m_h \leq M_Z \quad \text{Tree level upperbound on lightest Higgs mass}$$

To test if 125 GeV is possible two-loop corrections are essential!

Furthermore Higgs mass and sparticle limits imply large logs need resummed

Many alternatives (NMSSM, E6SSM, MRSSM) raise the Higgs mass.

But then two-loop corrections are also essential to check you actually resolve the problem.

Fixed Order Calculation in full theory

$$M_H^2 + \Sigma(p^2 = m_{h_i}^2) \xrightarrow[\text{for eigenvalues}]{\text{diagonalise}} m_{h_i}^2$$

In practice this is done with:

$$\Sigma(p^2) = \Sigma^{1\text{-loop}}(p^2) + \Sigma^{2\text{-loop}}(0)$$

$\Sigma^{1\text{-loop}}$: **complete** All models

$\Sigma^{2\text{-loop}}$: $\mathcal{O}(y_t^2 g_s^2, y_b^2 g_s^2)$ MSSM, NMSSM

: $\mathcal{O}(y_t^4, y_t^2 y_b^2, y_b^4, y_\tau^4)$ MSSM

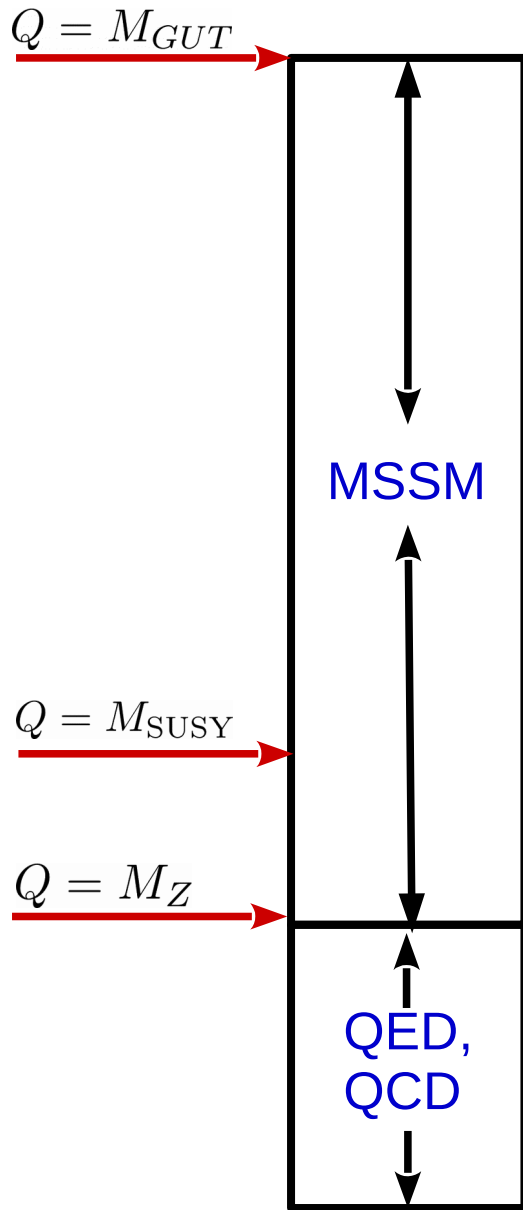
: **complete in gaugeless limit** All models

(SARAH/SPheno only)

$$\Sigma(p^2) = \Sigma(p^2, Q^2)$$

$Q^2 = m_{\tilde{t}_1} m_{\tilde{t}_2}$ - chosen to minimise largest logarithmic corrections

Fixed Order Calculation in full theory



Implemented in a number of public spectrum generators

$$\Sigma(p^2) = \Sigma^{1\text{-loop}}(p^2) + \Sigma^{2\text{-loop}}(0)$$

$$M_H^2 + \Sigma(p^2 = m_{h_i}^2) \xrightarrow[\text{for eigenvalues}]{\text{diagonalise}} m_{h_i}^2$$

$Q = M_{\text{SUSY}}$

Calculate

m_h^{MSSM}

$$Q = M_{\text{SUSY}} = \sqrt{(m_{\tilde{t}_1} m_{\tilde{t}_2})}$$

$Q = M_Z$

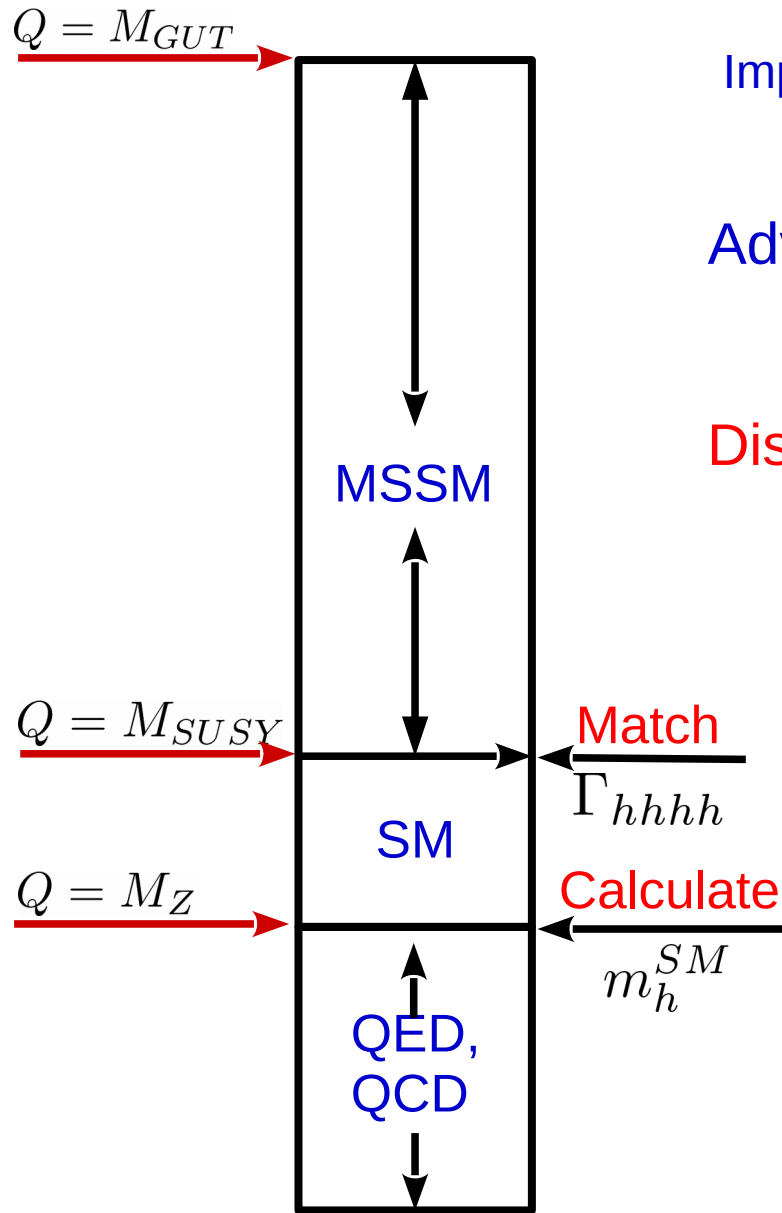
Advantage: includes terms $\mathcal{O}(p^2/M_{\text{SUSY}})$

Disadvantage: no resummed logs

Suffers from large logs when

$$M_{\text{SUSY}} \gg M_Z$$

EFT: match 4-point functions



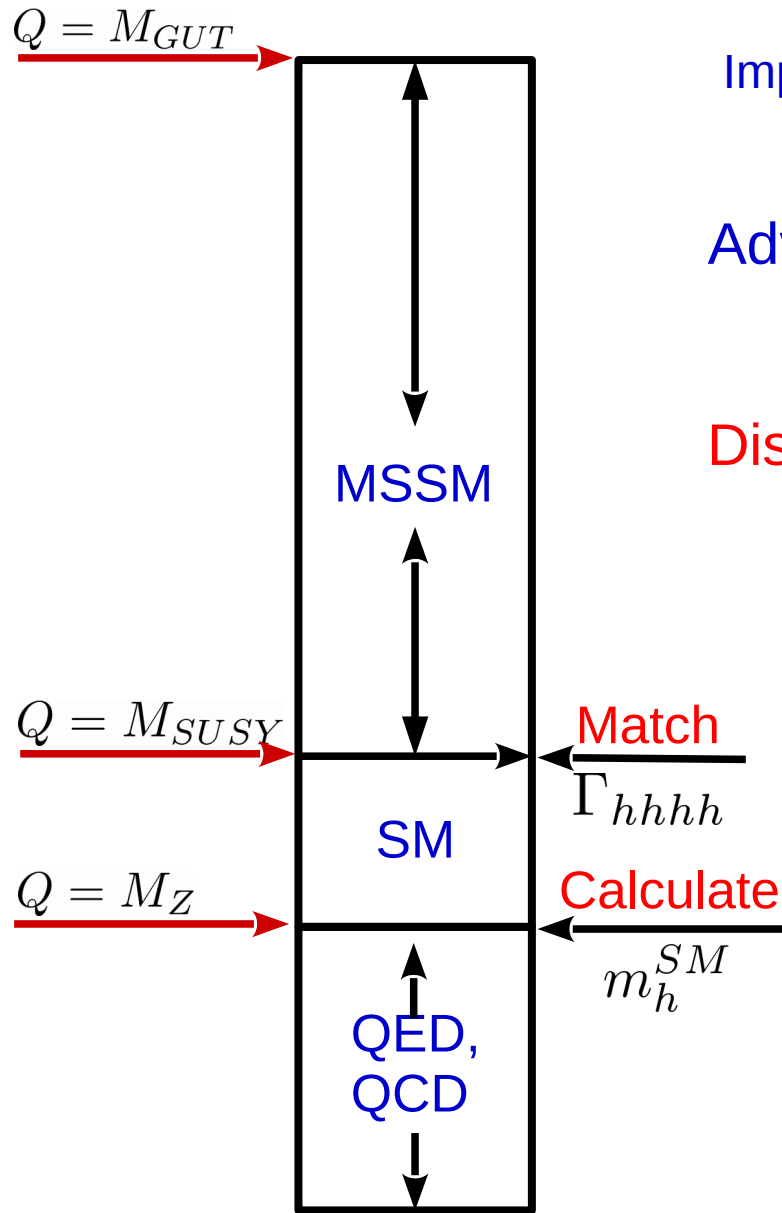
Implemented in SUSYHD and FlexibleSUSY HSSUSY

Advantage: resums large logs
can includes two-loop matching

Disadvantage: Misses p^2/M_{SUSY}^2 terms
Suffers if $M_{SUSY} \approx M_Z$

$$\lambda = \frac{1}{4} (g_Y^2 + g_2^2) \cos^2 2\beta + \Delta\lambda^{(1)} + \Delta\lambda^{(2)}$$

EFT: match 4-point functions



Implemented in SUSYHD and FlexibleSUSY HSSUSY

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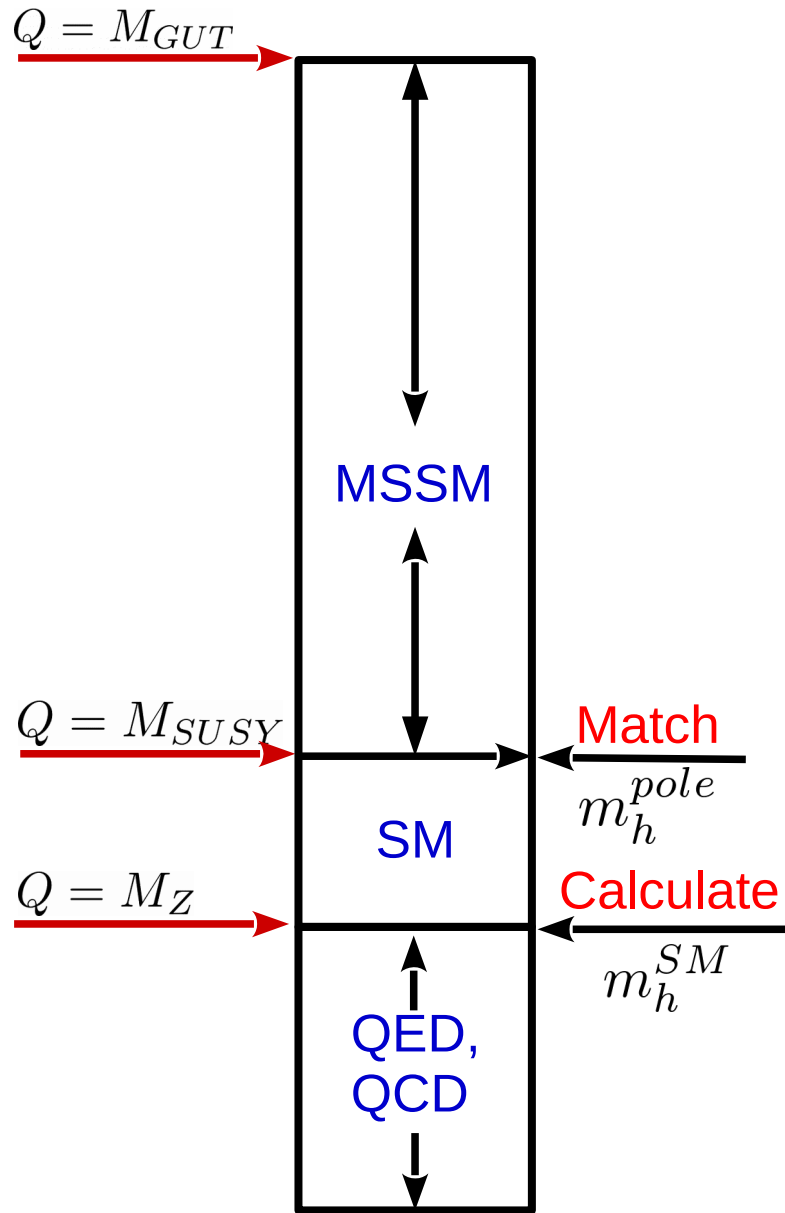
$$\lambda = \frac{1}{4} (g_Y^2 + g_2^2) \cos^2 2\beta + \Delta\lambda^{(1)} + \Delta\lambda^{(2)}$$

EFT: match pole masses



Advantage: Resums logs
Includes p^2/M_{SUSY}^2
Can be used in any model

Disadvantage: two-loop matching not known currently



$$(m_h^{\overline{MS},SM})^2 - \Sigma_h^{SM}(M_h^2) = (m_h^{\overline{DR},SUSY})^2 - \Sigma_h^{SUSY}(M_h^2),$$

$$\lambda(M_{SUSY}) = \frac{1}{v^2} \left[(m_h^{\overline{DR},SUSY})^2 - \Sigma_h^{SUSY}(M_h^2) + \Sigma_h^{SM}(M_h^2) \right]$$

Higgs pole mass calculations

Full theory
fixed order

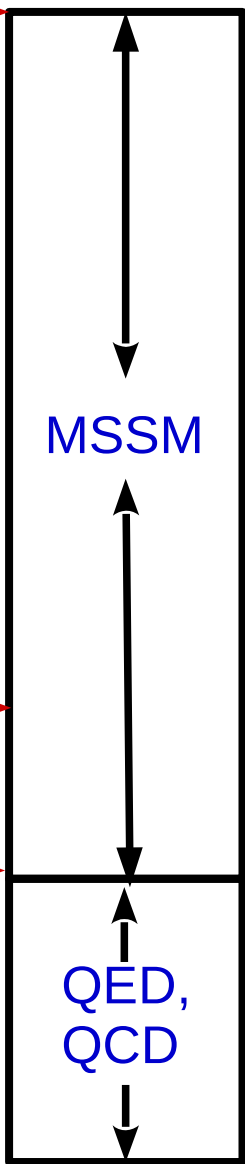
EFT match
4-point functions

EFT match
2-point functions

$$Q = M_{GUT}$$

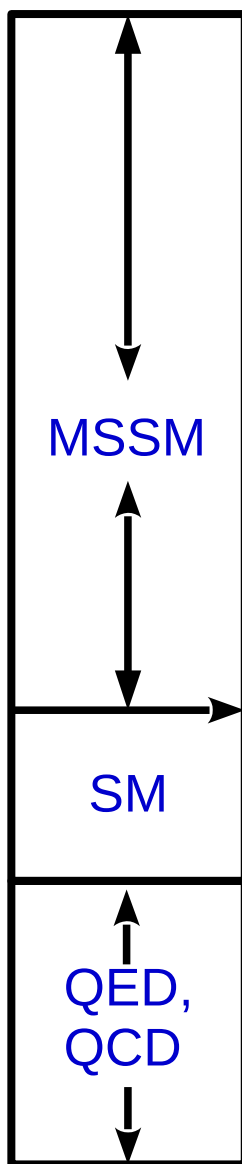
$$Q = M_{SUSY}$$

$$Q = M_Z$$



Calculate

$$m_h^{MSSM}$$

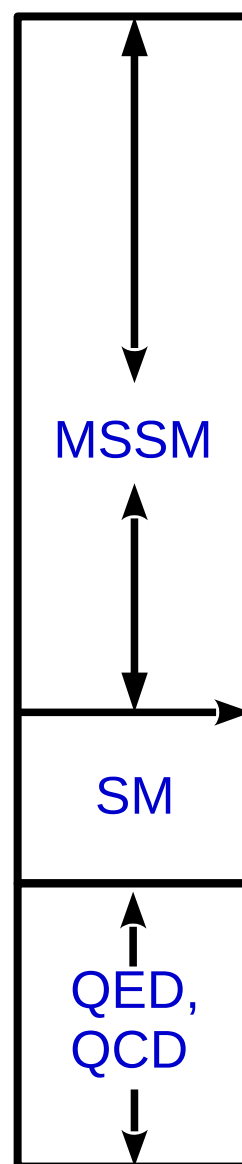


Match

$$\Gamma_{hhhh}$$

Calculate

$$m_h^{SM}$$



Match

$$m_h^{pole}$$

Calculate

$$m_h^{SM}$$

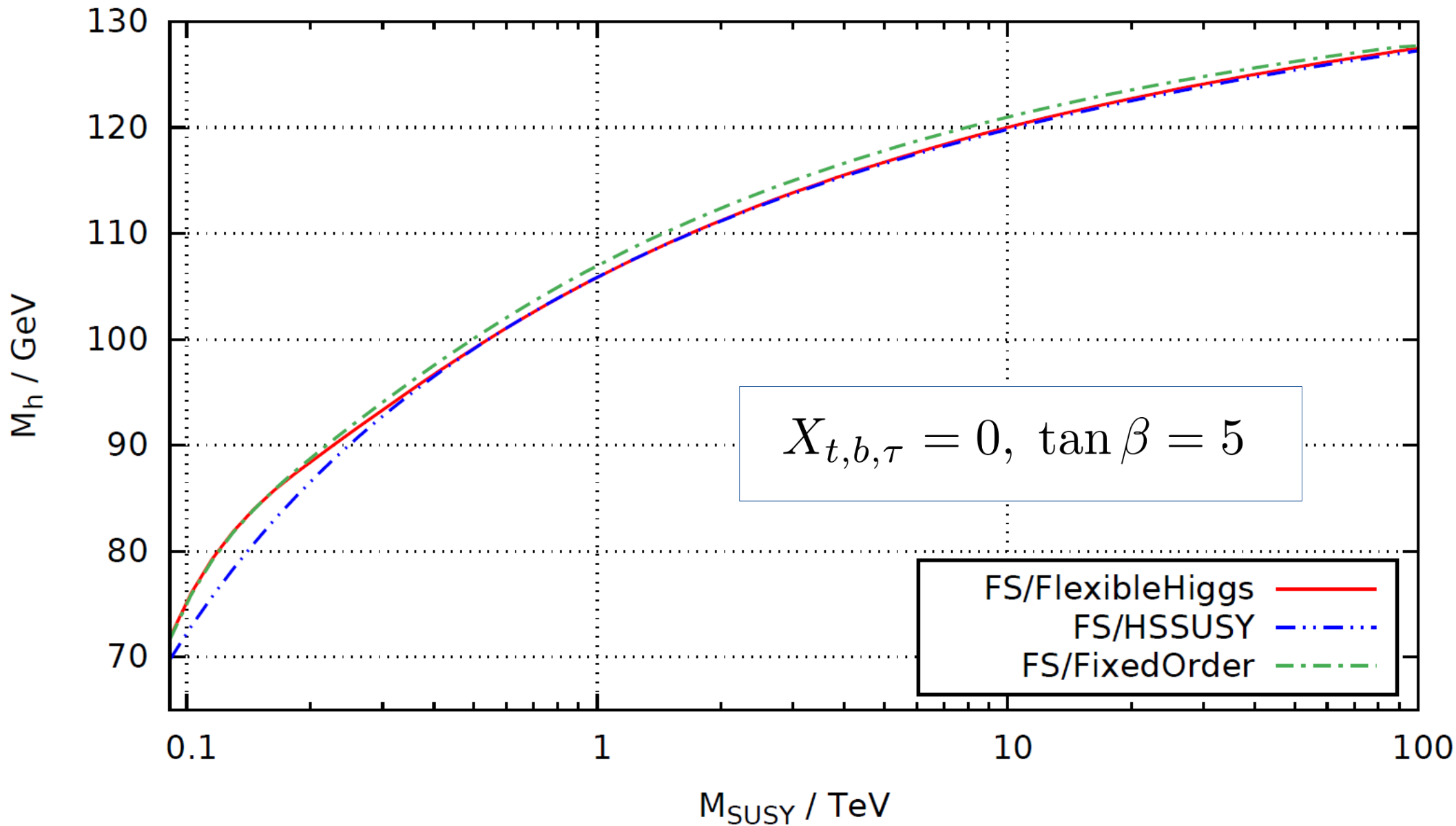
No resummed logs
Suffers if $M_{SUSY} \gg M_Z$

Misses p^2/M_{SUSY}^2 terms
Suffers if $M_{SUSY} \approx M_Z$

Resums logs
Includes p^2/M_{SUSY}^2

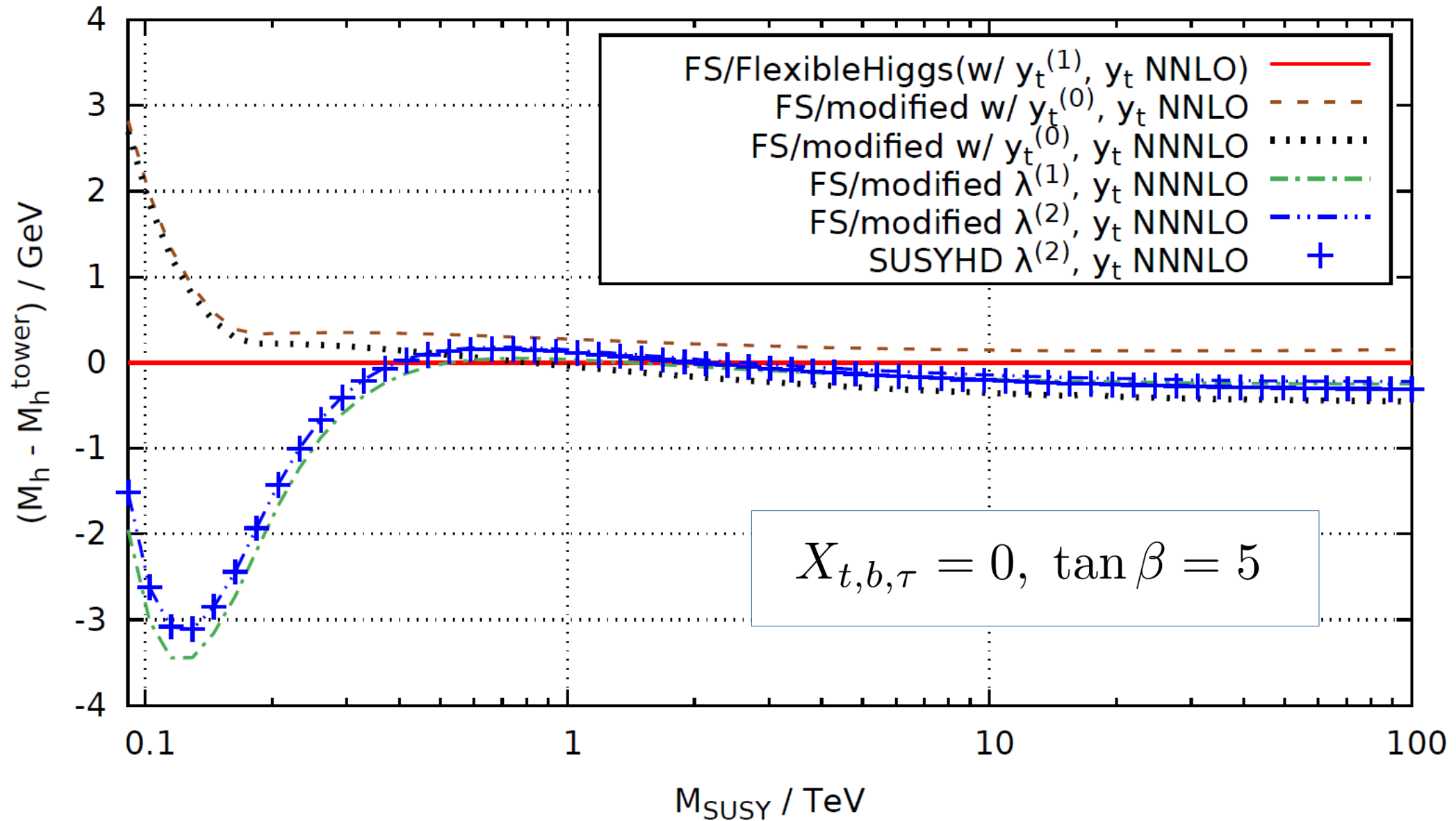
Comparison of FlexibleSUSY EFTs and Fixed order calculations in the MSSM

Note: $\alpha_s \alpha_t$ two-loop matching corrections vanish in these scenarios



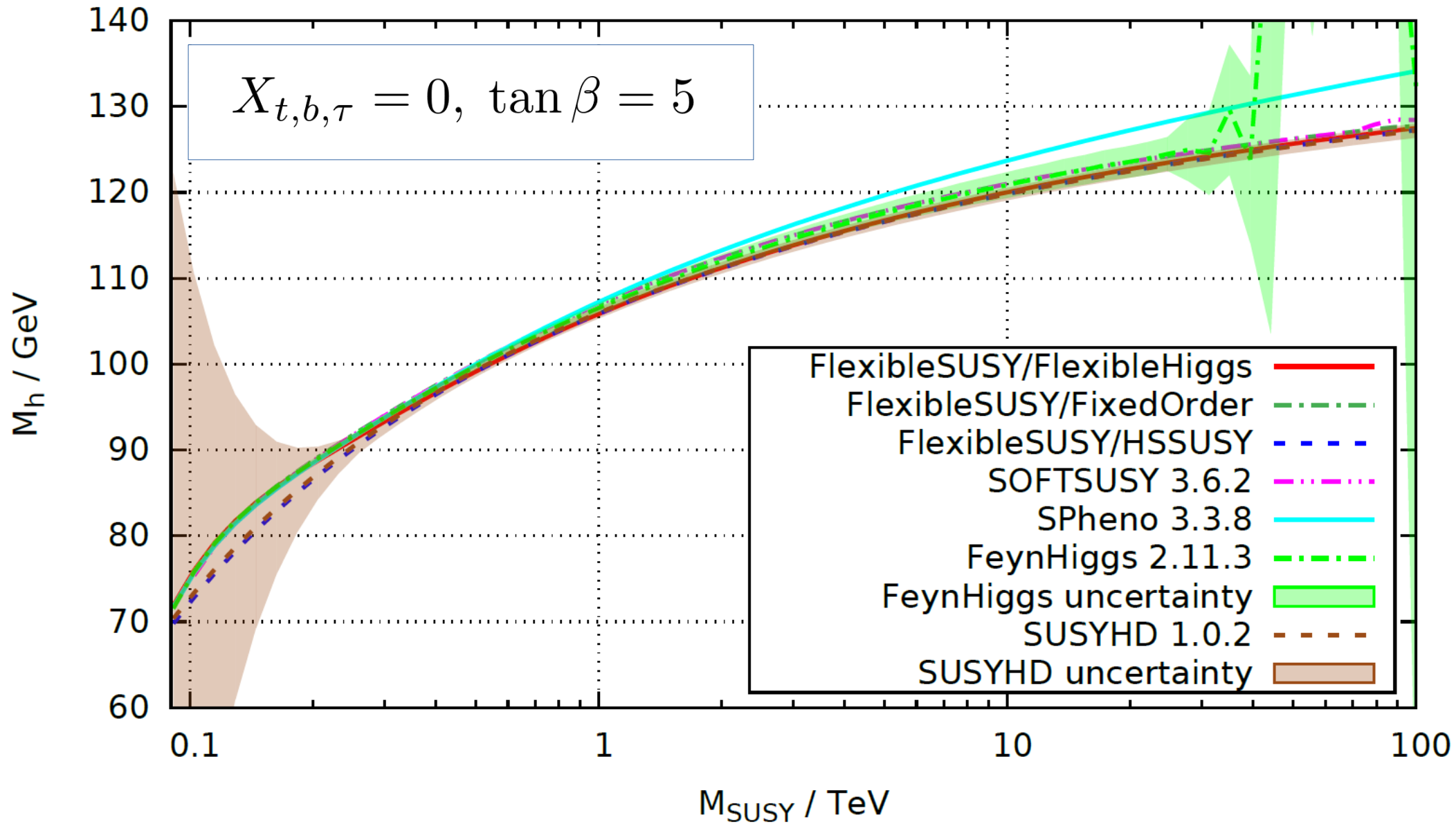
SUSY HD vs FlexibleHiggs ($X_t = 0$)

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Comparison to public codes (Xt = 0)

Note: $\alpha_s \alpha_t$ two-loop matching corrections vanish in these scenarios

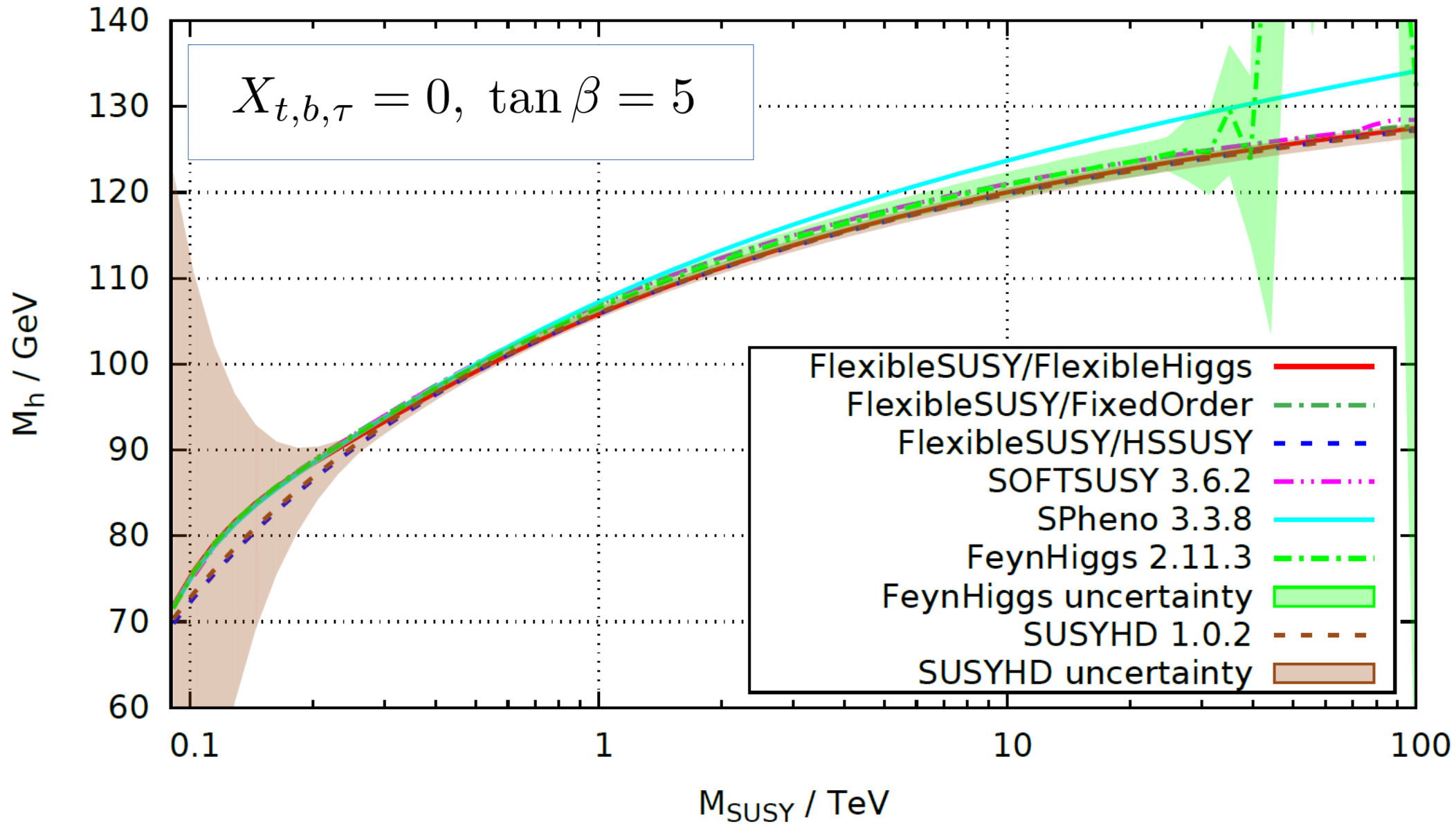


Comparison to public codes

Why is Spheno so different?

Or

Why do FlexibleSUSY and SOFTSUSY agree so well with FlexibleHiggs?



Comparison to public codes

Why is Spheno so different?

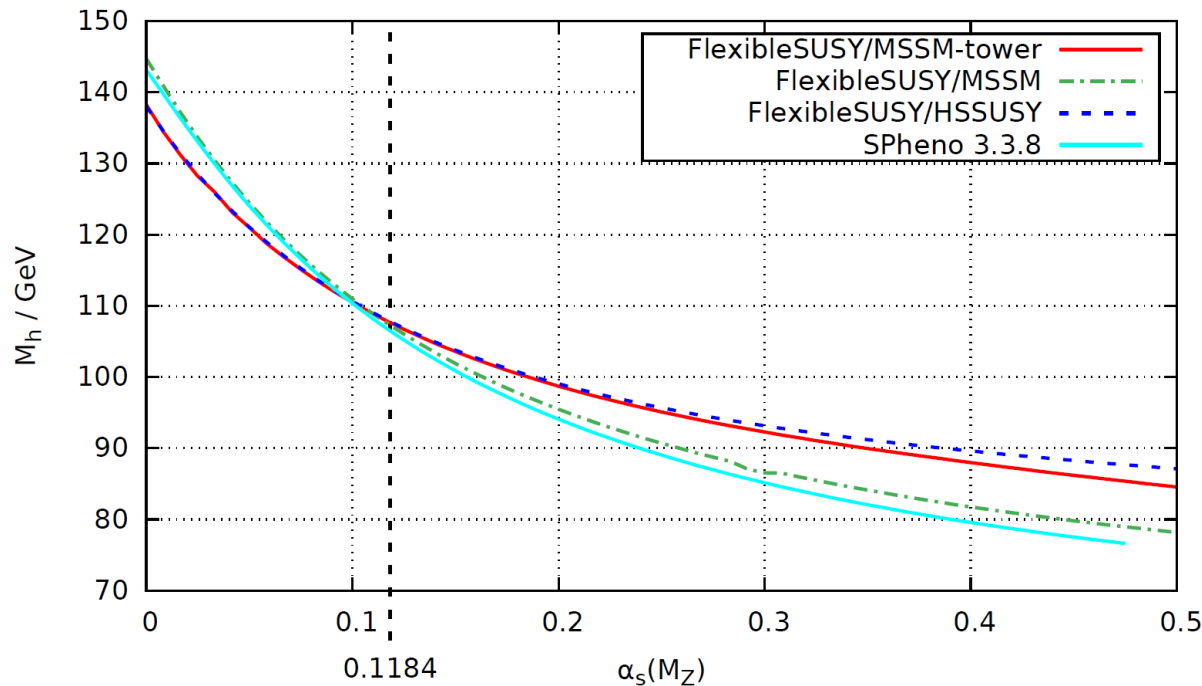
Or

Why do FlexibleSUSY and SOFTSUSY agree so well with FlexibleHiggs?

Cause of difference:
higher order
differences from
calculation of $m_t^{\overline{\text{DR}}}$

$$\text{FS: } m_t^{\overline{\text{DR}}} = M_t + \left[\tilde{\Sigma}_t^{(1),S}(M_t) \right] + M_t \left[\tilde{\Sigma}_t^{(1),L}(M_t) + \tilde{\Sigma}_t^{(1),R}(M_t) \right] \\ + M_t \left[\tilde{\Sigma}_t^{(1),\text{qcd}}(m_t^{\overline{\text{DR}}}) + \left(\tilde{\Sigma}_t^{(1),\text{qcd}}(m_t^{\overline{\text{DR}}}) \right)^2 + \tilde{\Sigma}_t^{(2),\text{qcd}}(m_t^{\overline{\text{DR}}}) \right],$$

$$\text{SP: } m_t^{\overline{\text{DR}}} = M_t + \left[\tilde{\Sigma}_t^{(1),S}(m_t^{\overline{\text{DR}}}) \right] + m_t^{\overline{\text{DR}}} \left[\tilde{\Sigma}_t^{(1),L}(m_t^{\overline{\text{DR}}}) + \tilde{\Sigma}_t^{(1),R}(m_t^{\overline{\text{DR}}}) \right] \\ + m_t^{\overline{\text{DR}}} \left[\tilde{\Sigma}_t^{(1),\text{qcd}}(m_t^{\overline{\text{DR}}}) + \tilde{\Sigma}_t^{(2),\text{qcd}}(m_t^{\overline{\text{DR}}}) \right].$$



Cause of agreement:
must be an accidental cancellation!

Comparison to public codes

Why is Spheno so different?

Or

Why do FlexibleSUSY and SOFTSUSY agree so well with FlexibleHiggs?

Fixed order expansion:

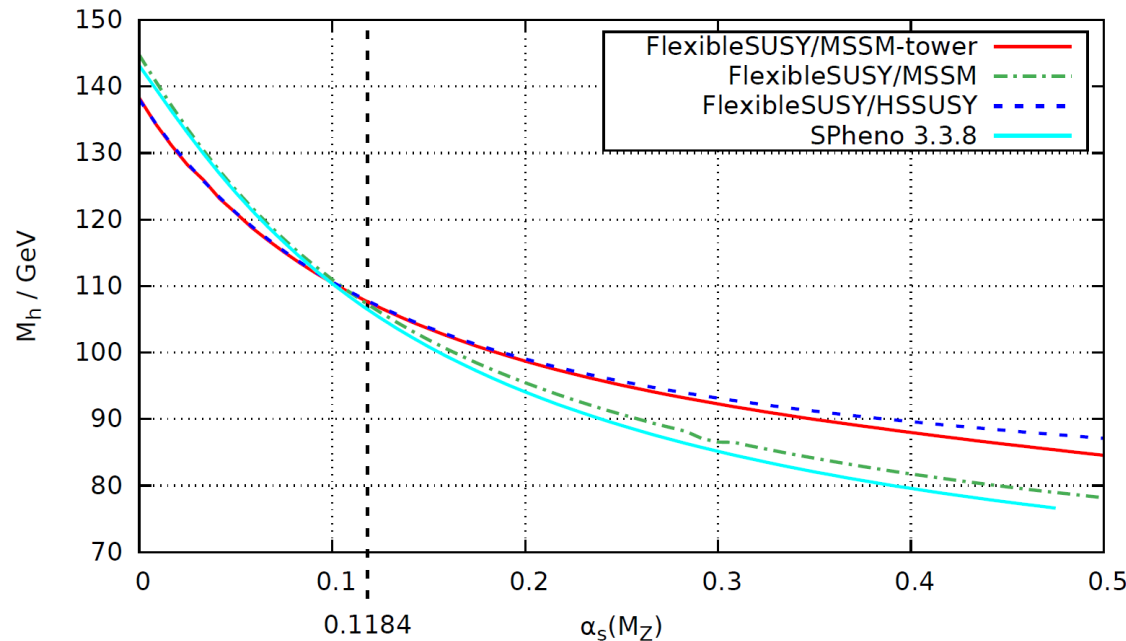
$$(M_h^2)^{\text{EFT}} = m_h^2 + v^2 y_t^4 \left[12t_S \kappa_L + 12t_S^2 \kappa_L^2 (16g_3^2 - 9y_t^2) + 4t_S^3 \kappa_L^3 (736g_3^4 - 672g_3^2 y_t^2 + 90y_t^4) + \dots \right],$$

Large coefficients suggest both FlexibleSUSY and Spheno have a larger uncertainty than the difference between the suggests

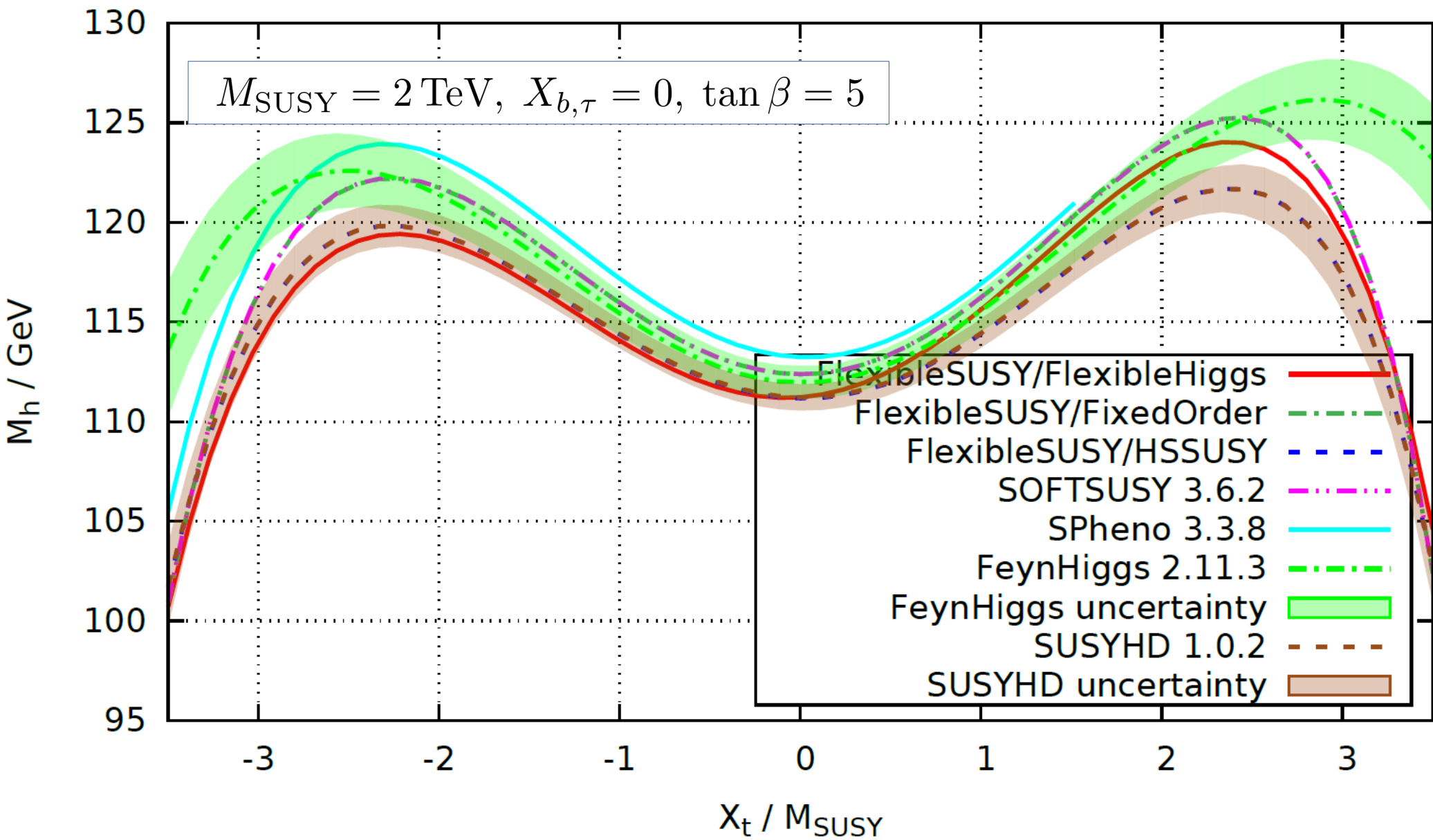
$$(M_h^2)^{\text{FlexibleSUSY}} = m_h^2 + v^2 y_t^4 \left[12t_S \kappa_L + 12t_S^2 \kappa_L^2 (16g_3^2 - 9y_t^2) + 4t_S^3 \kappa_L^3 \left(\frac{736}{3} g_3^4 - 288g_3^2 y_t^2 + \frac{27}{2} y_t^4 \right) + \dots \right],$$

$$(M_h^2)^{\text{SPheno}} = m_h^2 + v^2 y_t^4 \left[12t_S \kappa_L + 12t_S^2 \kappa_L^2 (16g_3^2 - 9y_t^2) + 4t_S^3 \kappa_L^3 \left(\frac{992}{3} g_3^4 - 192g_3^2 y_t^2 + \frac{81}{2} y_t^4 \right) + \dots \right].$$

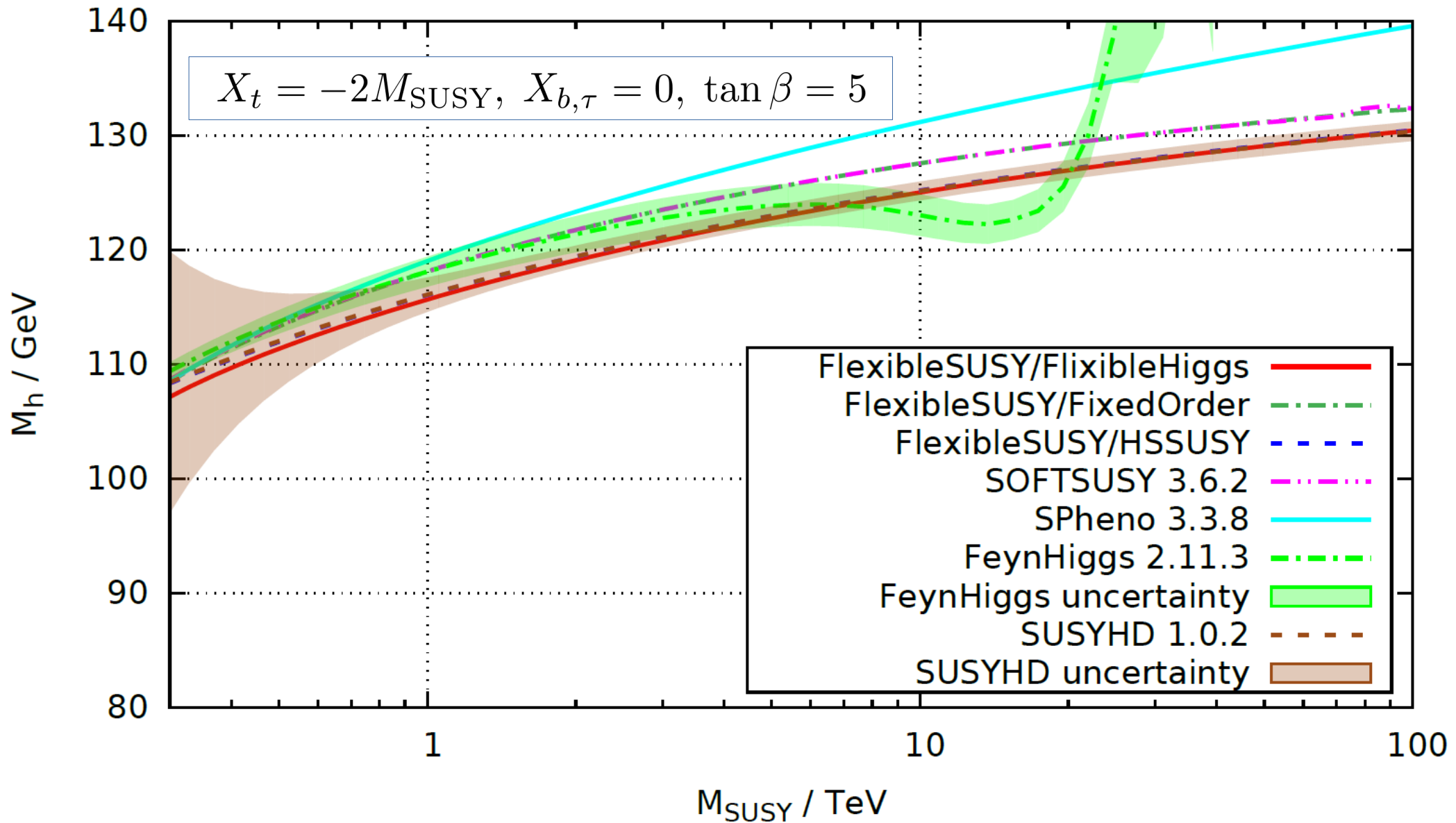
Cause of agreement:
must be an accidental cancellation!



Comparison to public codes ($X_t \neq 0$)



Comparison to public codes ($X_t \neq 0$)



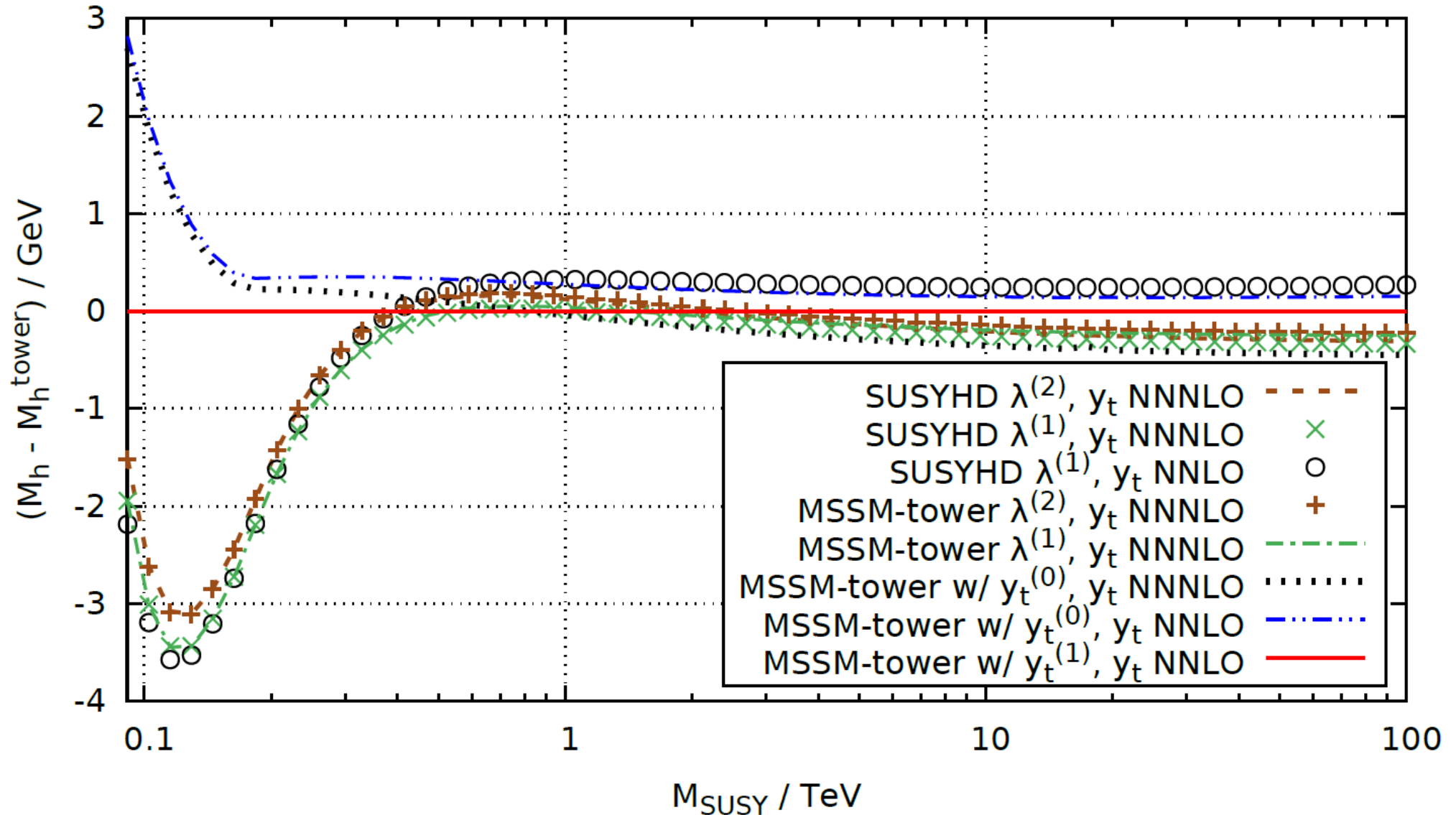
Summary and outlook

- **FlexibleHiggs** uses a new EFT approach to predict Higgs mass in **any SUSY model** with resummed two-loop logarithmic corrections.
- The pole-mass matching approach of **FlexibleHiggs** ensures beautiful agreement with the fixed order calculation when $M_{SUSY} = M_Z$.
- For the MSSM **FlexibleHiggs** agrees very well with the leading calculations when $X_t=0$
- When $X_t \neq 0$ the two-loop matching corrections can be large and introduce **finite shifts** between SUSYHD / HSSUSY and **FlexibleHiggs**
- We also have done a detailed study of error estimation for **FlexibleHiggs**, using methods that are applicable to all models (see forthcoming paper for details)
- **FlexibleHiggs** has already been applied and studied in the NMSSM, E6SSM and MRSSM (see forthcoming paper for details)
- **FlexibleHiggs** will be made publicly available as part of FlexibleSUSY in a new release
- Two-loop matching conditions will be provided and studied in a future update

SUSY HD vs MSSM-tower ($X_t = 0$) (difference)

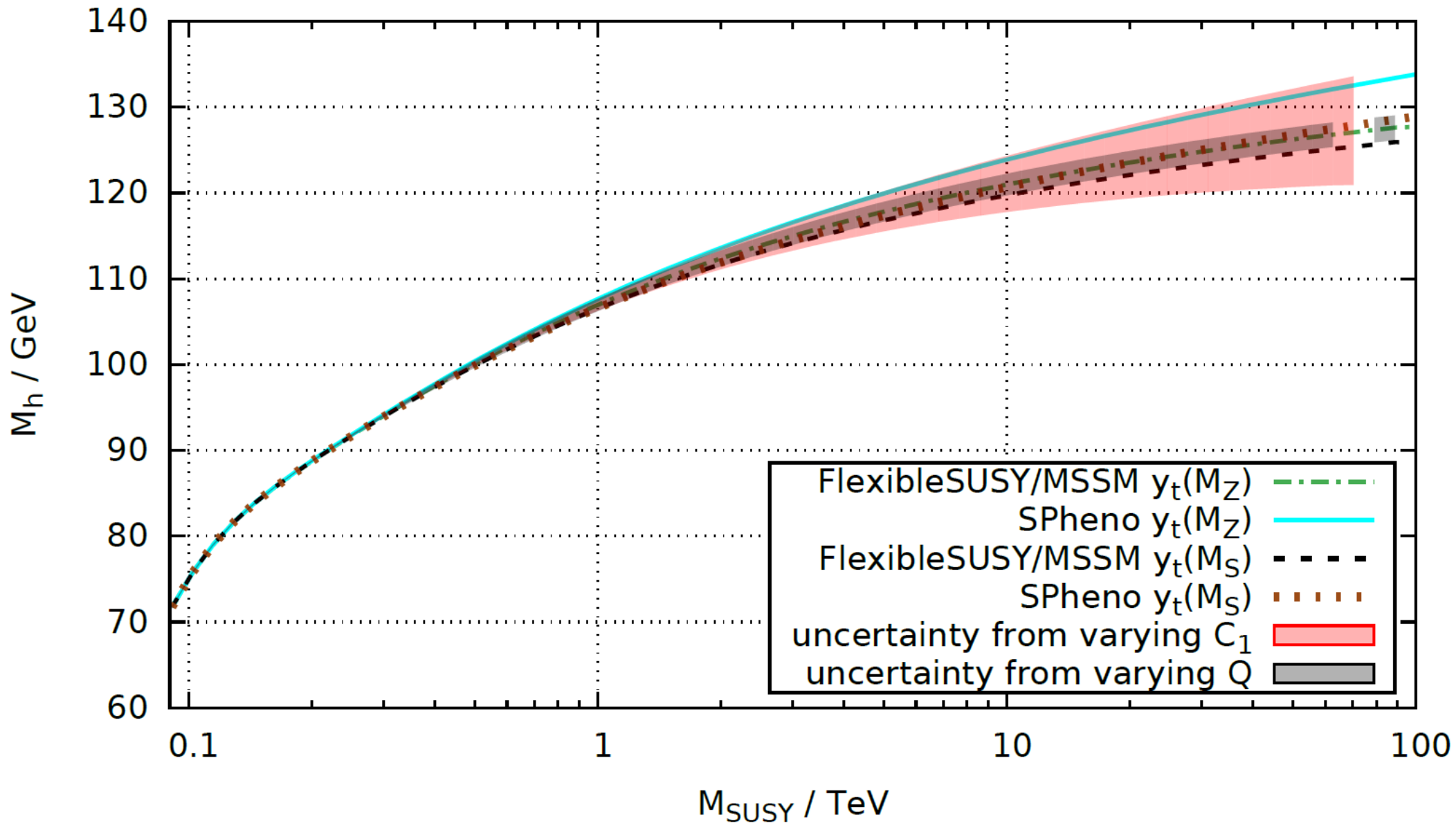
Note: $\alpha_s \alpha_t$ two-loop matching corrections vanish in these scenarios

Alternative version of plot with more steps



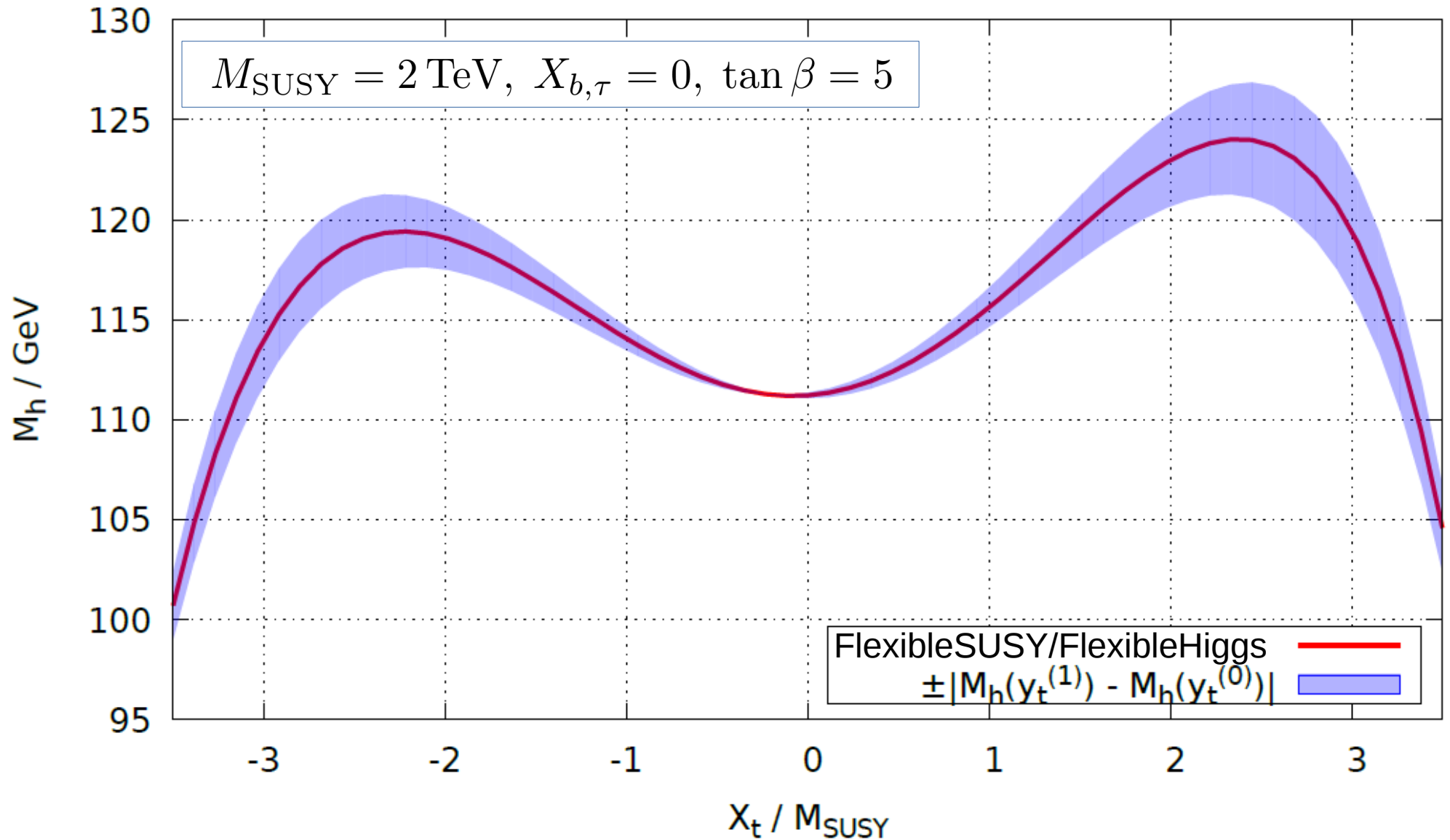
Fixed order MSSM uncertainty estimation

Vary coefficient of g_s^4 $\Delta m_t = \frac{C_1 g_s^4 M_t^4}{4\pi} \log^2 \left(\frac{M_{\text{SUSY}}}{M_Z} \right)$
 $C_1 \in \{-184/9, +184/9\}$



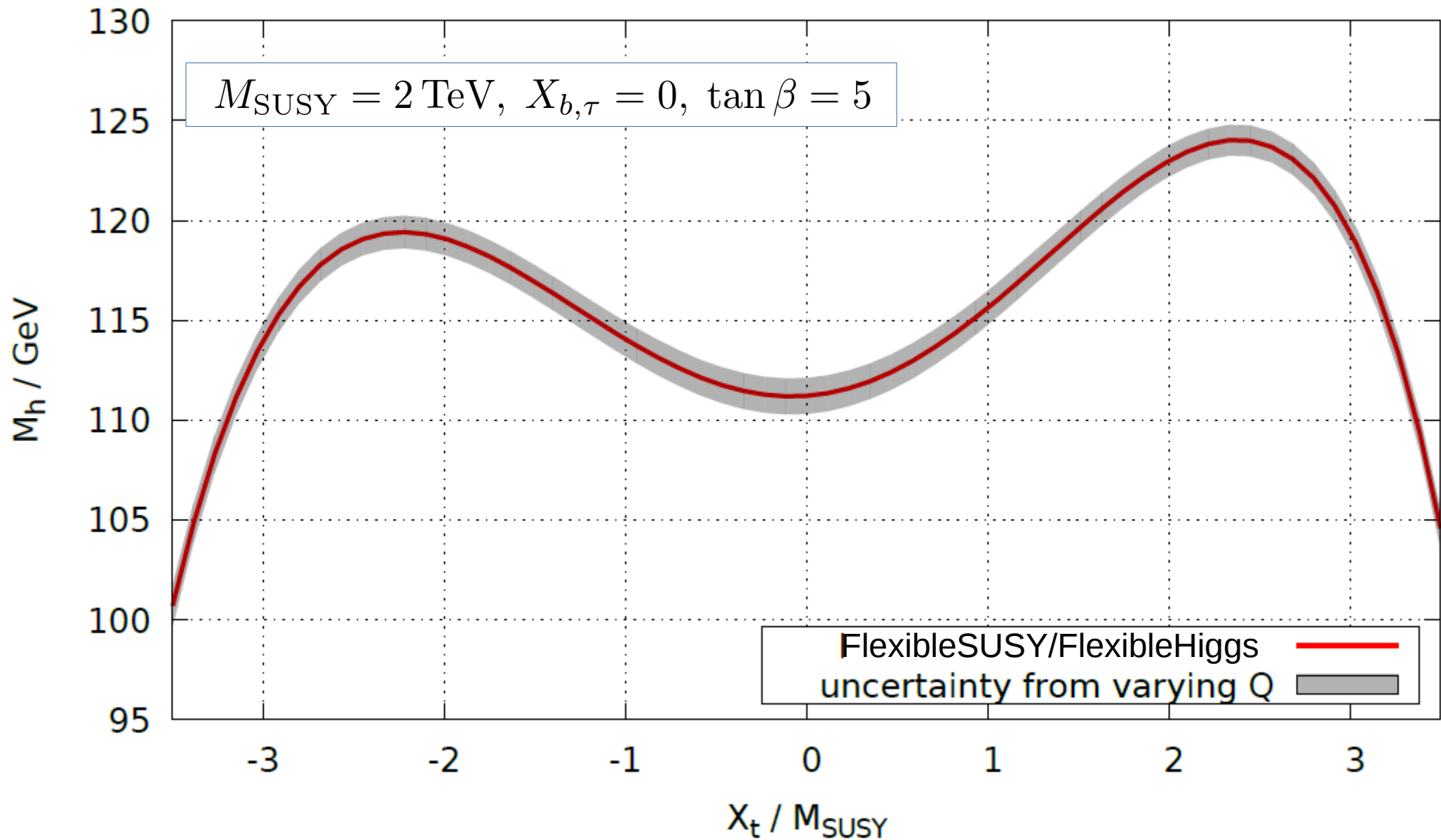
FlexibleHiggs uncertainty estimation

$$y_t^{\text{MSSM},(0)} = \frac{y_t^{\text{SM}}}{s_\beta} \quad y_t^{\text{MSSM},(1)} = \frac{y_t^{\text{SM}}}{s_\beta} + \frac{\sqrt{2}}{s_\beta v} \left[\Sigma_t^{\text{MSSM}} - \Sigma_t^{\text{SM}} \right]$$



FlexibleHiggs uncertainty estimation

Vary renormalisation scale of SM Higgs mass calculation



Comparison of uncertainties

Note: combining errors linearly is quite conservative, so these are likely an overestimate

Full model approach (2L):

(C_3 and Q uncertainties added linearly)

M_S/TeV	X_t/M_S	$\Delta M_h/\text{GeV}$		X_t/M_S	$\Delta M_h/\text{GeV}$
1	0	± 1.3		2	± 2.0
2	0	± 2.1		2	± 3.0
10	0	± 4.5		2	± 5.5

EFT- M_h approach (1L):

($y_t^{(i)}$ and Q uncertainties added linearly)

M_S/TeV	X_t/M_S	$\Delta M_h/\text{GeV}$		X_t/M_S	$\Delta M_h/\text{GeV}$
1	0	± 1.0		2	± 3.1
2	0	± 1.0		2	± 3.1
10	0	± 1.1		2	± 2.8