
Lepton Flavour Violating Minimal Dark Matter

D. Aristizabal Sierra,
C. Simoes
D. Wegman.
ULg, Liege, Belgium

Meeting of the Belgian Inter-University Attraction Pole network on fundamental interactions.

18 December 2015

University of Antwerp

BSM New Physics

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❖ Neutrino Masses!

BSM New Physics

- ❖ Neutrino Masses!
- ❖ Baryon Asymmetry

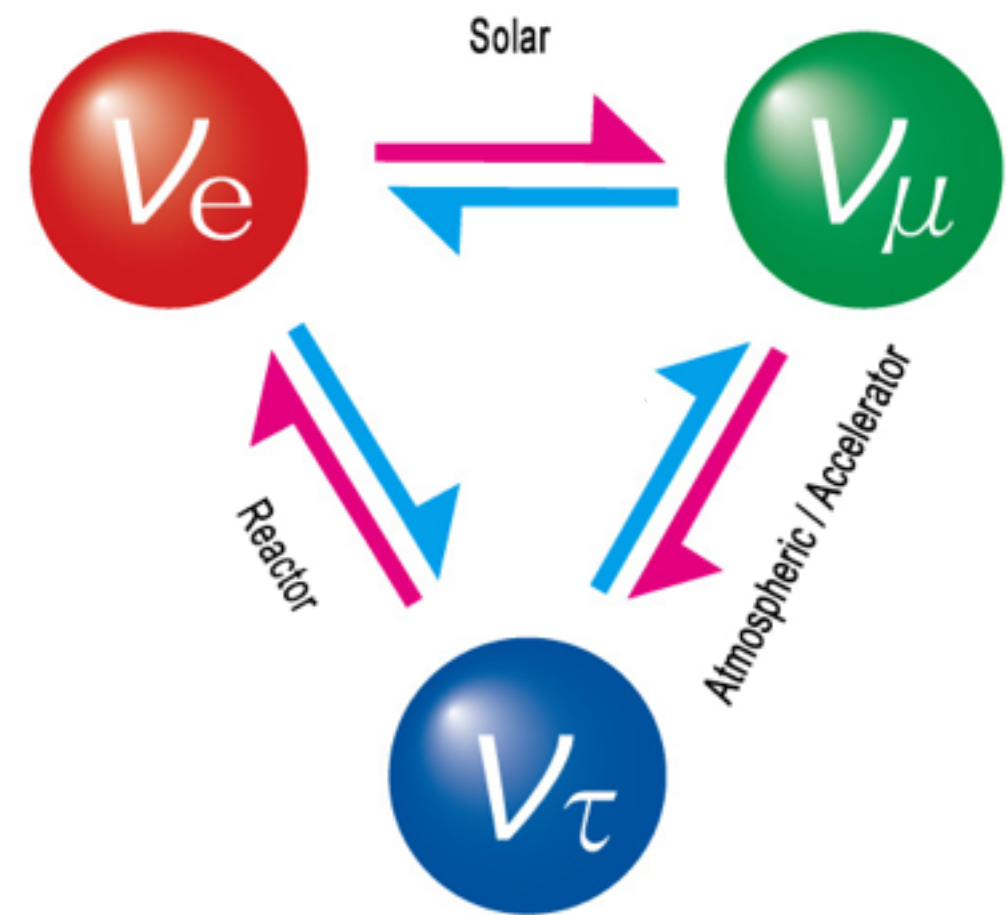
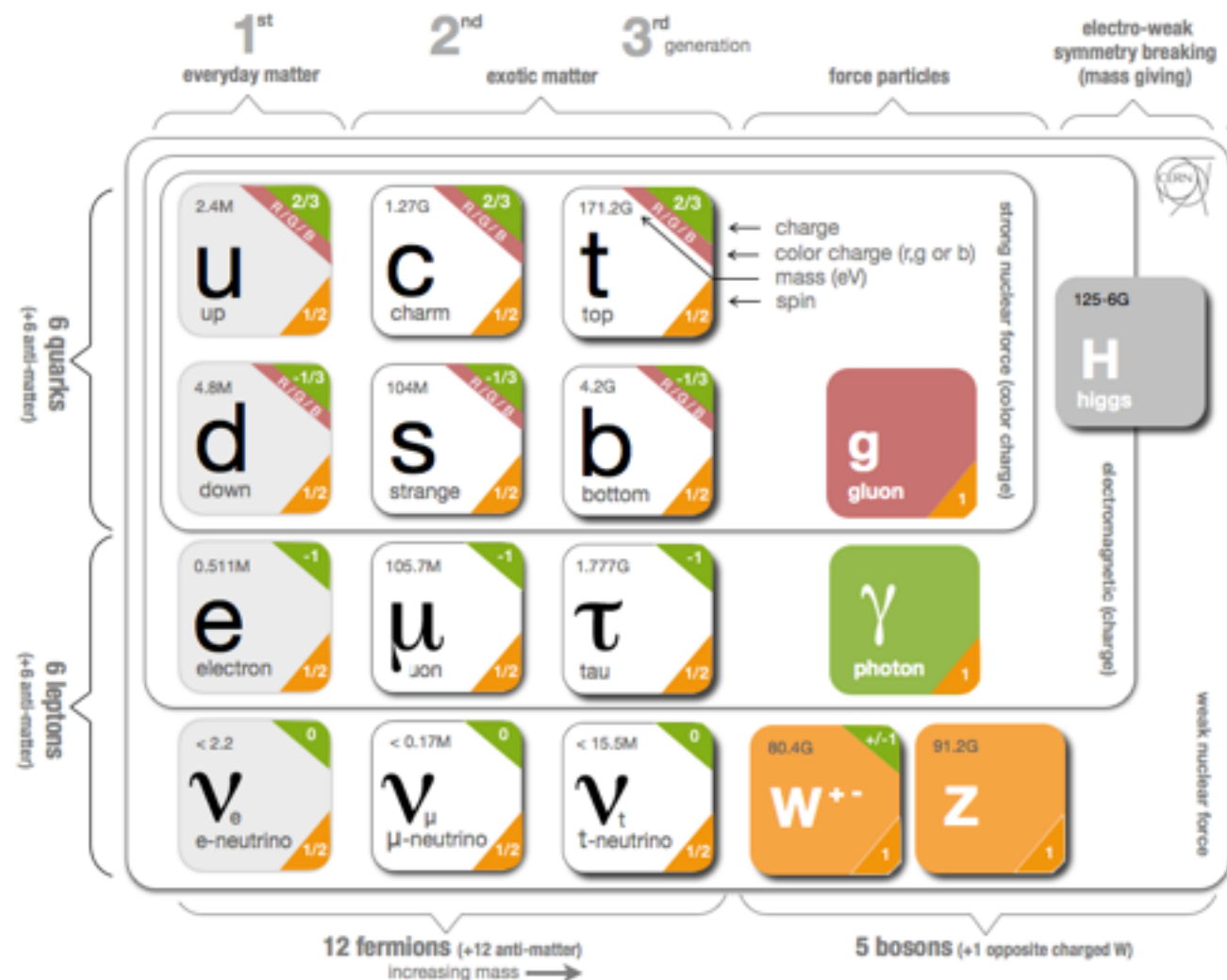
BSM New Physics

- ❖ Neutrino Masses!
- ❖ Baryon Asymmetry
- ❖ Dark Matter?

BSM New Physics

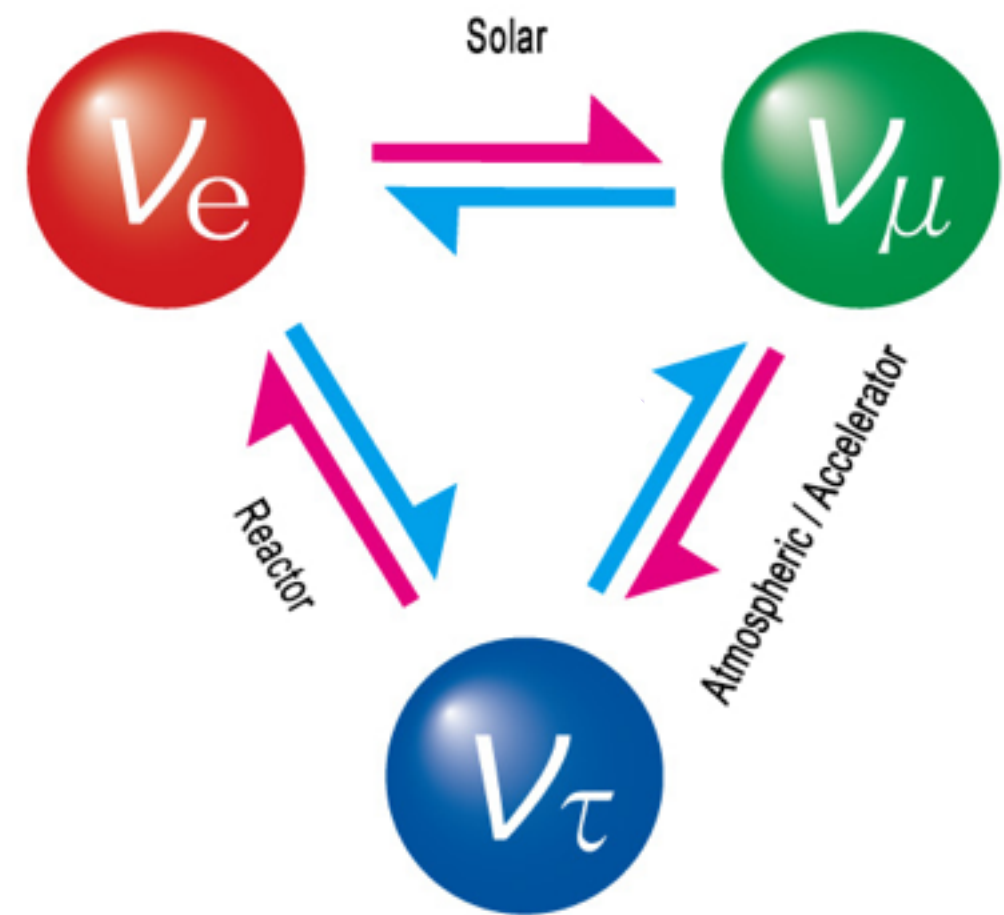
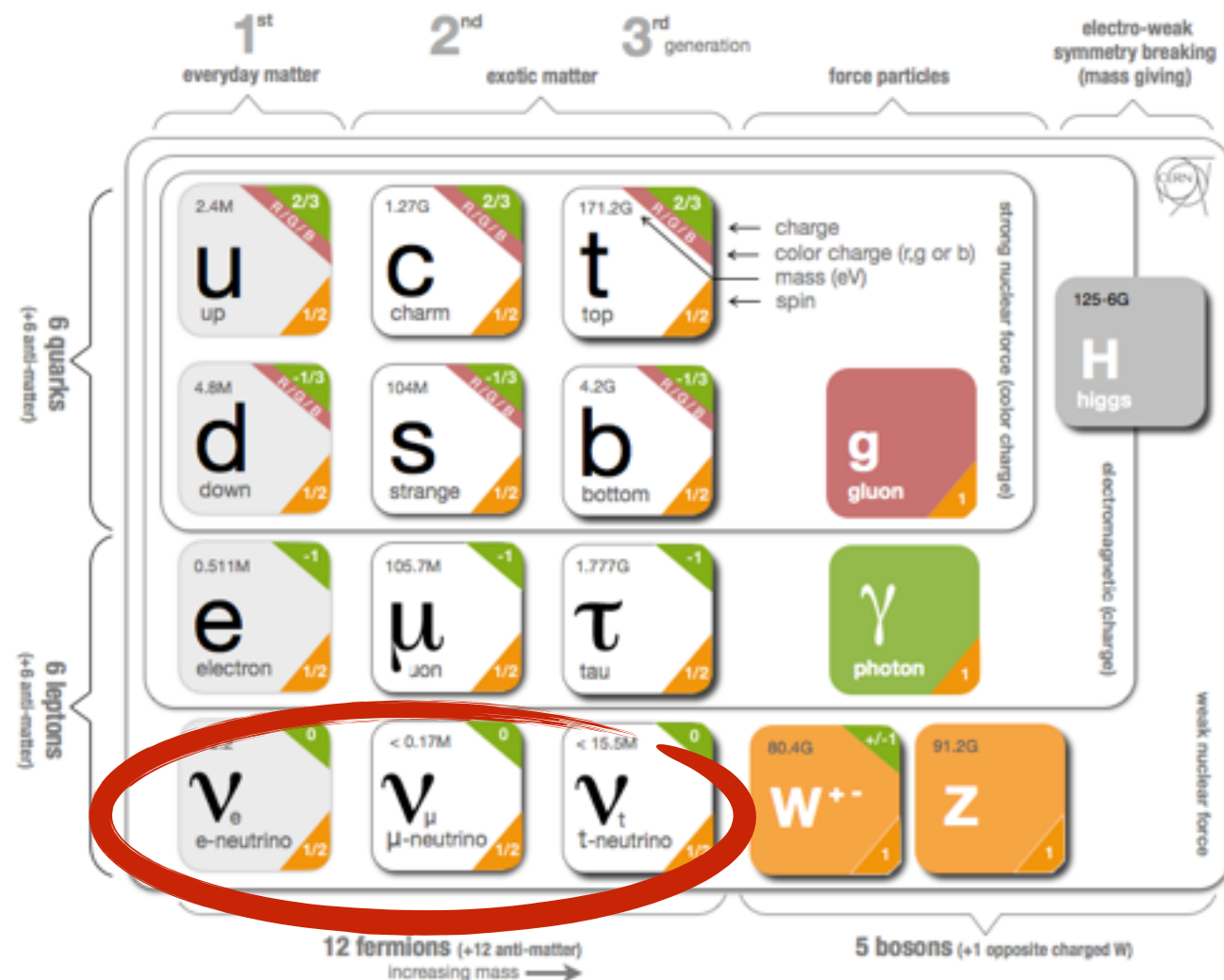
- ❖ Neutrino Masses!
- ❖ Baryon Asymmetry
- ❖ Dark Matter?
- ❖ ???

Neutrino Masses



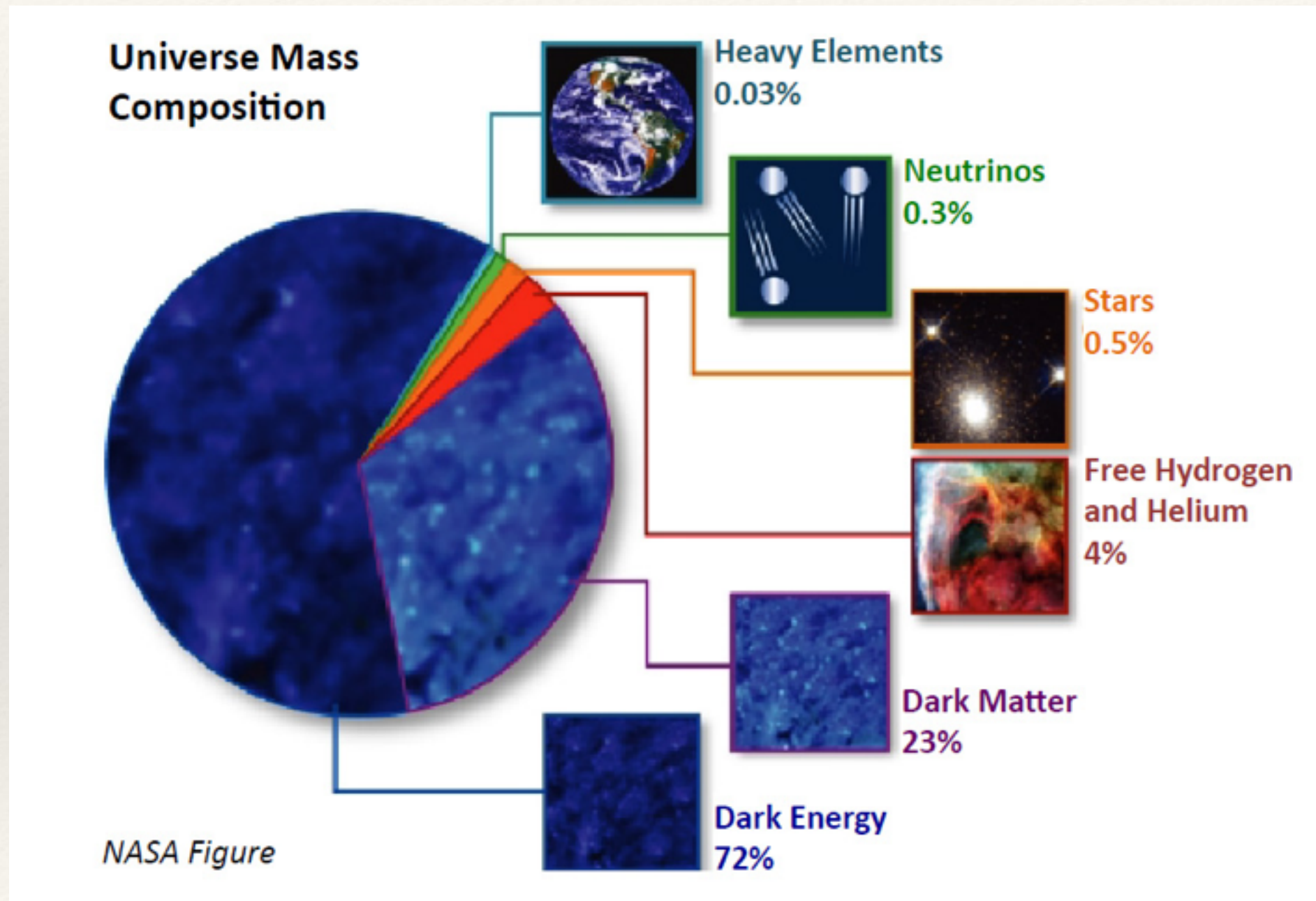
Neutrino oscillation between three generations

Neutrino Masses



Neutrino oscillation between three generations

Dark Matter



“Stable” Dark Matter

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- ❖ No decay

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 - Discrete Symmetry

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 - Accidental Symmetry

“Stable” Dark Matter

- ❖ No decay
 - Discrete Symmetry
 - Accidental Symmetry
- ❖ Long decay

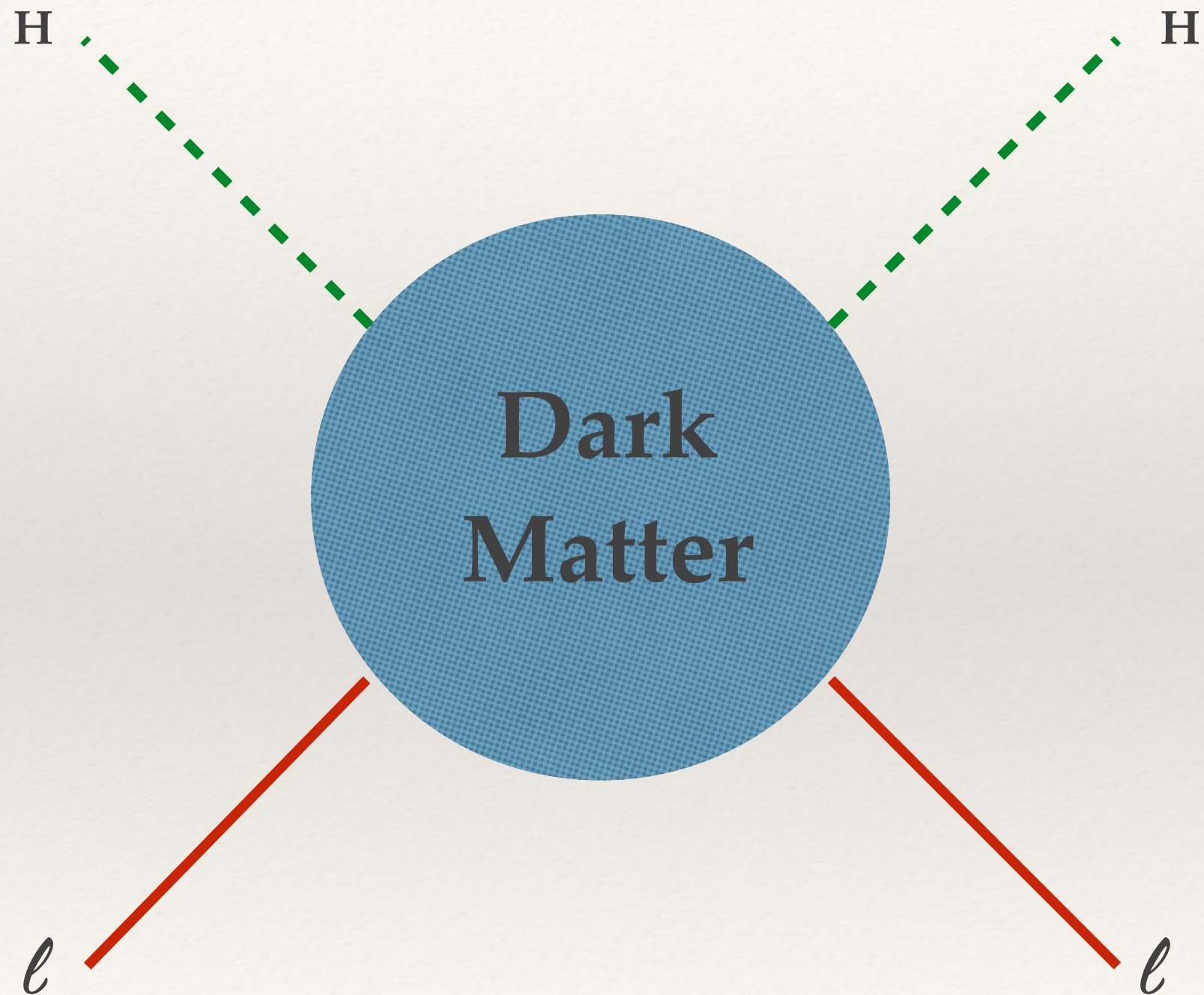
“Stable” Dark Matter

- ❖ No decay
 - Discrete Symmetry
 - Accidental Symmetry
- ❖ Long decay
 - $\tau > 10^{26}$ sec

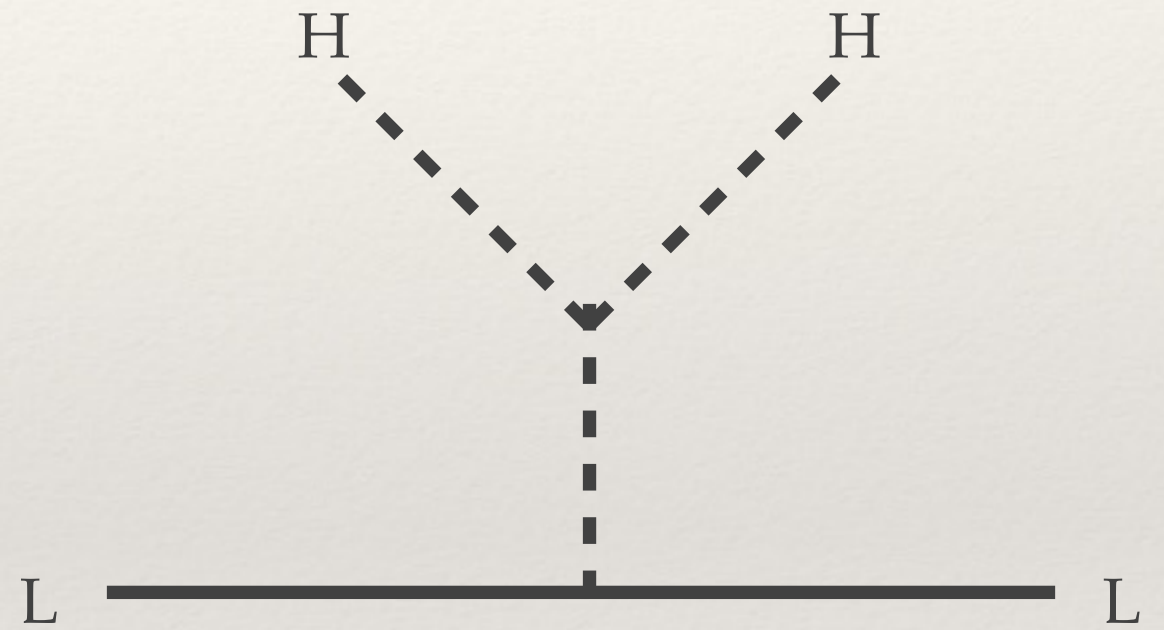
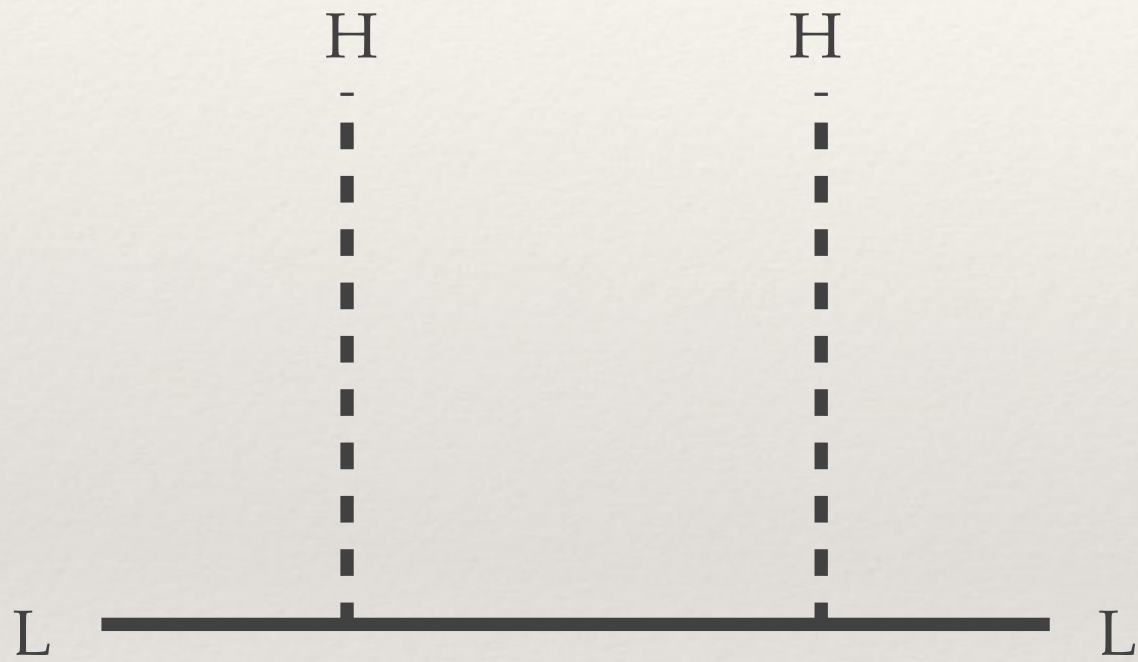
“Stable” Dark Matter

- ❖ No decay
 - Discrete Symmetry
 - Accidental Symmetry
- ❖ Long decay
 - $\tau > 10^{26}$ sec
 - Parameter Space.

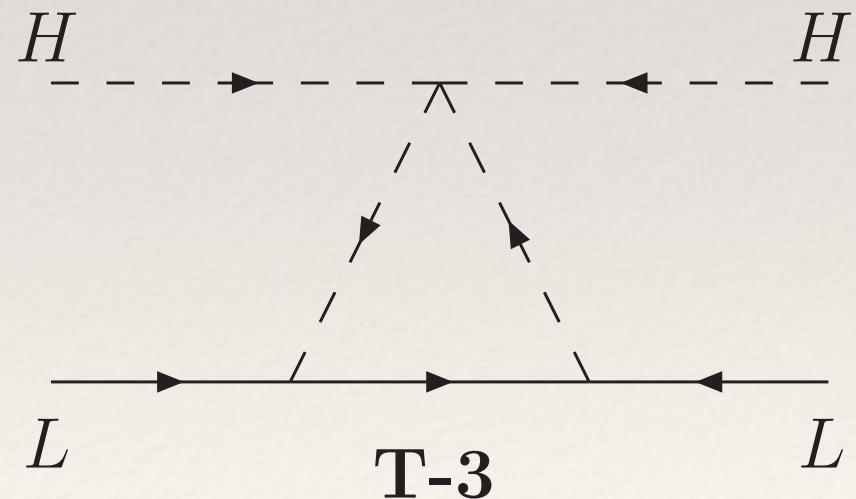
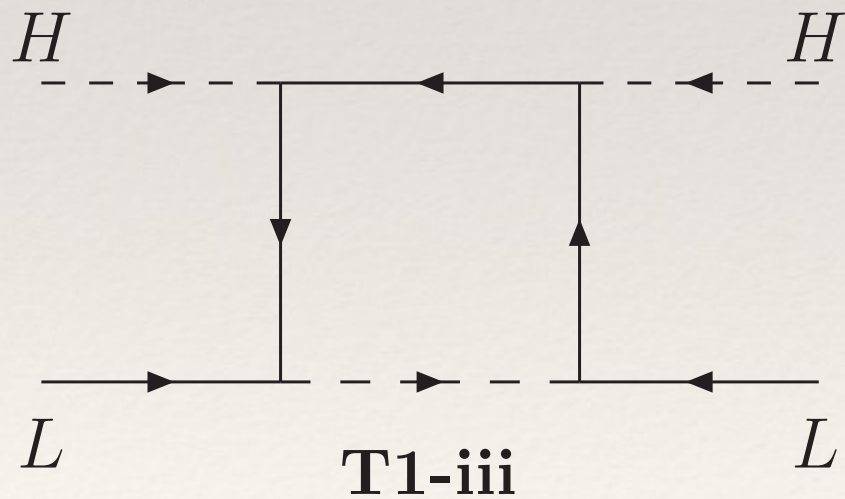
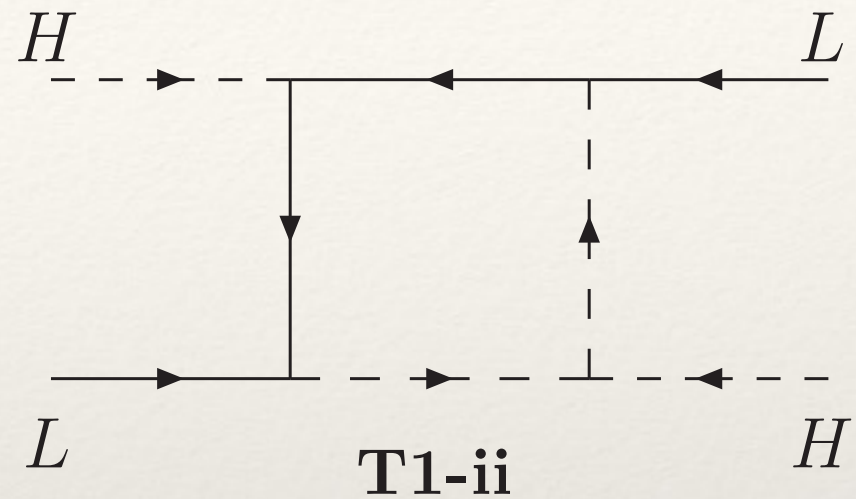
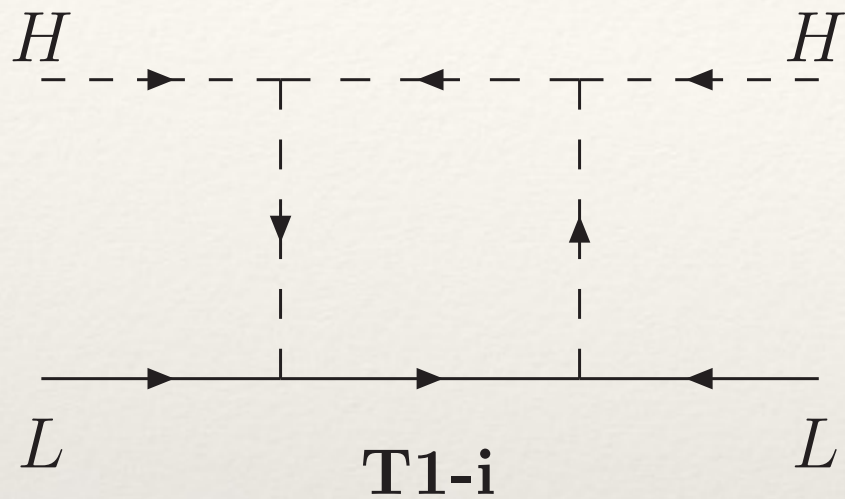
DM \longleftrightarrow Neutrinos



Seesaw Masses



One Loop Neutrino Masses



Minimal Dark Matter

- ❖ Minimal DM rely on the fact that neutral particles belonging to higher-order $SU(2)$ representations, are automatically stable, without the need to add any new symmetry. While still matching DM cosmological constraints.

M. Cirelli and A. Strumia, Minimal Dark Matter: Model and results, New J. Phys. 11, 105005 (2009) [arXiv:0903.3381 [hep-ph]].

SU(2) Multiplication

$$2 \times 2 = 1 + 3$$

$$3 \times 2 = 2 + 4$$

$$3 \times 3 = 1 + 3 + 5$$

$$4 \times 2 = 3 + 5$$

$$4 \times 3 = 2 + 4 + 6$$

$$4 \times 4 = 1 + 3 + 5 + 7$$

$$5 \times 2 = 4 + 6$$

$$5 \times 3 = 3 + 5 + 7$$

$$5 \times 4 = 2 + 4 + 6 + 8$$

$$5 \times 5 = 1 + 3 + 5 + 7 + 9$$

$$6 \times 2 = 5 + 7$$

$$6 \times 3 = 4 + 6 + 8$$

$$6 \times 4 = 3 + 5 + 7 + 9$$

$$6 \times 5 = 2 + 4 + 6 + 8 + 10$$

$$6 \times 6 = 1 + 3 + 5 + 7 + 9 + 11$$

$$7 \times 2 = 6 + 8$$

$$7 \times 3 = 5 + 7 + 9$$

$$7 \times 4 = 4 + 6 + 8 + 10$$

$$7 \times 5 = 3 + 5 + 7 + 9 + 11$$

$$7 \times 6 = 2 + 4 + 6 + 8 + 10 + 12$$

$$7 \times 7 = 1 + 3 + 5 + 7 + 9 + 11 + 13$$

$$8 \times 2 = 7 + 9$$

$$8 \times 3 = 6 + 8 + 10$$

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$$8 \times 5 = 4 + 6 + 8 + 10 + 12$$

$$8 \times 6 = 3 + 5 + 7 + 9 + 11 + 13$$

$$8 \times 7 = 2 + 4 + 6 + 8 + 10 + 12 + 14$$

$$8 \times 8 = 1 + 3 + 5 + 7 + 9 + 11 + 13 + 15$$

$$9 \times 2 = 8 + 10$$

$$9 \times 3 = 7 + 9 + 11$$

$$9 \times 4 = 6 + 8 + 10 + 12$$

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SU(2)~4: $4 \times 2=3, 3 \times 2=2, 2 \times 2=1$

$4 \times 2 \times 2 \times 2=1$

S H H H* ———> Dim 4

F L H H* ———> Dim 5

SU(2) Multiplication

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SU(2)~4: $4 \times 2=3, 3 \times 2=2, 2 \times 2=1$

$$4 \times 2 \times 2 \times 2=1$$

S H H H* \longrightarrow Dim 4

F L H H* \longrightarrow Dim 5

SU(2)~5: $5 \times 2=4, 4 \times 2=3, 3 \times 2=2, 2 \times 2=1$

$$5 \times 2 \times 2 \times 2 \times 2=1$$

S H H H* H* \longrightarrow Dim 5

F L H H H \longrightarrow Dim 6

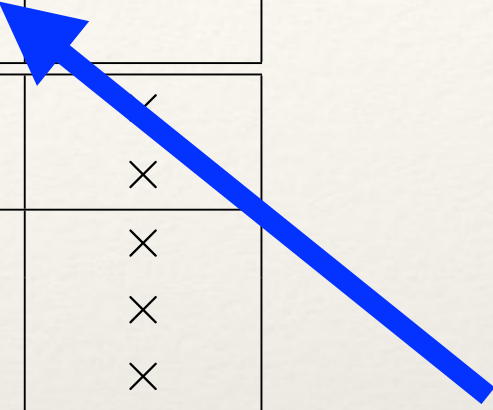
DM Candidates?

Quantum numbers			DM can decay into	DD bound?	Stable?
$SU(2)_L$	$U(1)_Y$	Spin			
2	1/2	S	EL	×	×
2	1/2	F	EH	×	×
3	0	S	HH^*	✓	×
3	0	F	LH	✓	×
3	1	S	HH, LL	×	×
3	1	F	LH	×	×
4	1/2	S	HHH^*	×	×
4	1/2	F	(LHH^*)	×	×
4	3/2	S	HHH	×	×
4	3/2	F	(LHH)	×	×
5	0	S	(HHH^*H^*)	✓	×
5	0	F	—	✓	✓
5	1	S	$(HH^*H^*H^*)$	×	×
5	1	F	—	×	✓
5	2	S	$(H^*H^*H^*H^*)$	×	×
5	2	F	—	×	✓
6	1/2, 3/2, 5/2	S	—	×	✓
7	0	S	—	✓	✓
8	1/2, 3/2 ...	S	—	×	✓

M. Cirelli and A. Strumia, Minimal Dark Matter: Model and results, New J. Phys. 11, 105005 (2009) [arXiv:0903.3381 [hep-ph]].

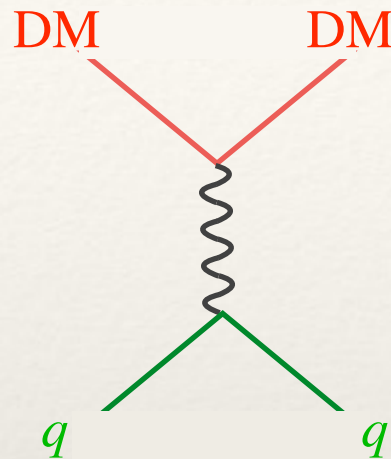
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$SU(2)_L$	$U(1)_Y$	Spin			
2	1/2	S	EL	×	×
2	1/2	F	EH	×	×
3	0	S	HH^*	✓	×
3	0	F	LH	✓	×
3	1	S	HH, LL	×	×
3	1	F	LH	×	×
4	1/2	S	HHH^*	×	×
4	1/2	F	(LHH^*)	×	×
4	3/2	S	HHH	×	×
4	3/2	F	(LHH)	×	×
5	0	S	(HHH^*H^*)	✓	×
5	0	F	—	✓	✓
5	1	S	$(HH^*H^*H^*)$	×	×
5	1	F	—	×	✓
5	2	S	$(H^*H^*H^*H^*)$	×	×
5	2	F	—	×	✓
6	1/2, 3/2, 5/2	S	—	×	✓
7	0	S	—	✓	✓
8	1/2, 3/2 ...	S	—	×	✓



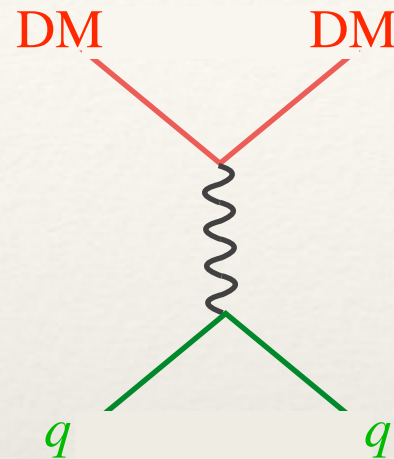
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MDM Direct Detection



$$\sigma(\text{DM } \mathcal{N} \rightarrow \text{DM } \mathcal{N}) = c \frac{G_{\text{F}}^2 M_{\mathcal{N}}^2}{2\pi} Y^2 (N - (1 - 4s_{\text{W}}^2)Z)^2$$

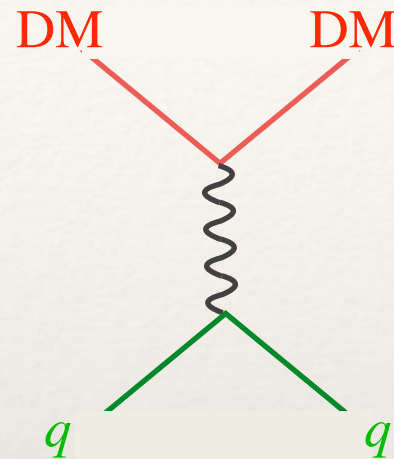
MDM Direct Detection



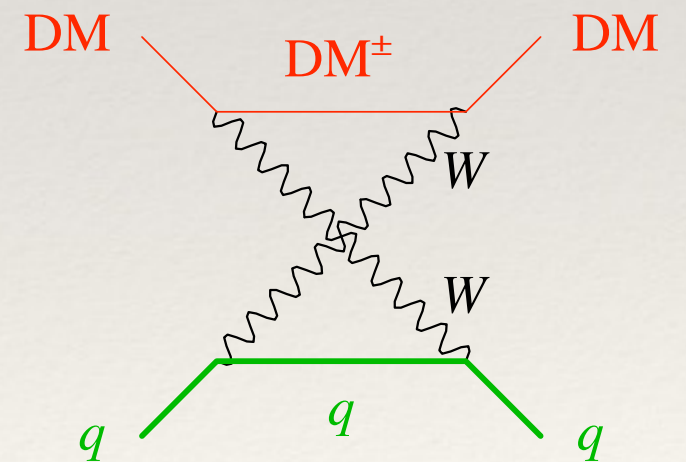
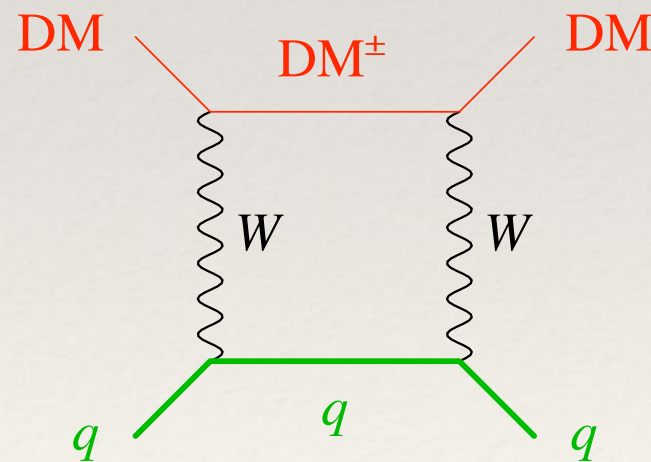
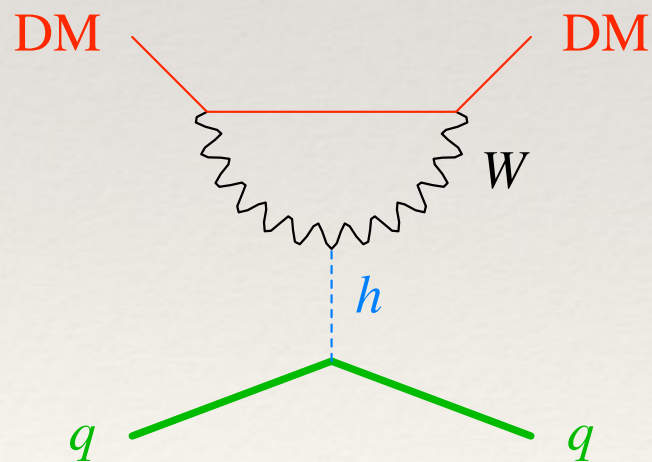
$$\sigma(\text{DM } \mathcal{N} \rightarrow \text{DM } \mathcal{N}) = c \frac{G_{\text{F}}^2 M_{\mathcal{N}}^2}{2\pi} Y^2 (N - (1 - 4s_{\text{W}}^2)Z)^2$$

Y=0

MDM Direct Detection

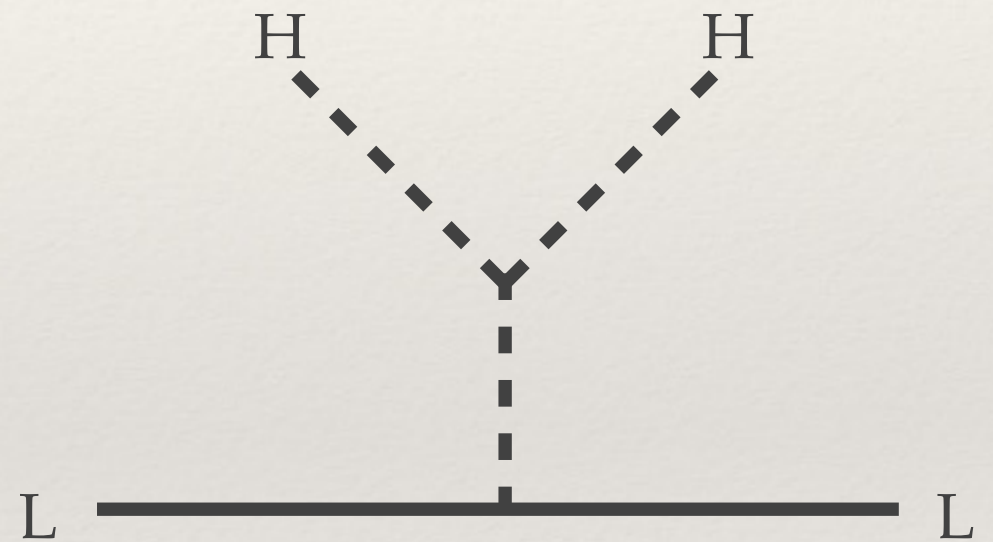
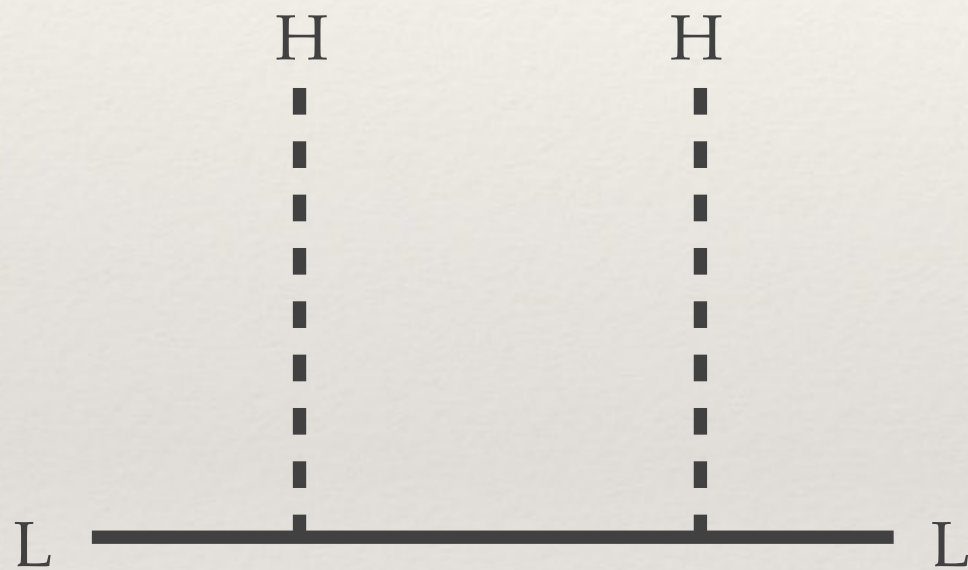


$$\sigma(\text{DM } \mathcal{N} \rightarrow \text{DM } \mathcal{N}) = c \frac{G_F^2 M_{\mathcal{N}}^2}{2\pi} Y^2 (N - (1 - 4s_W^2)Z)^2 \quad \text{with } Y=0$$



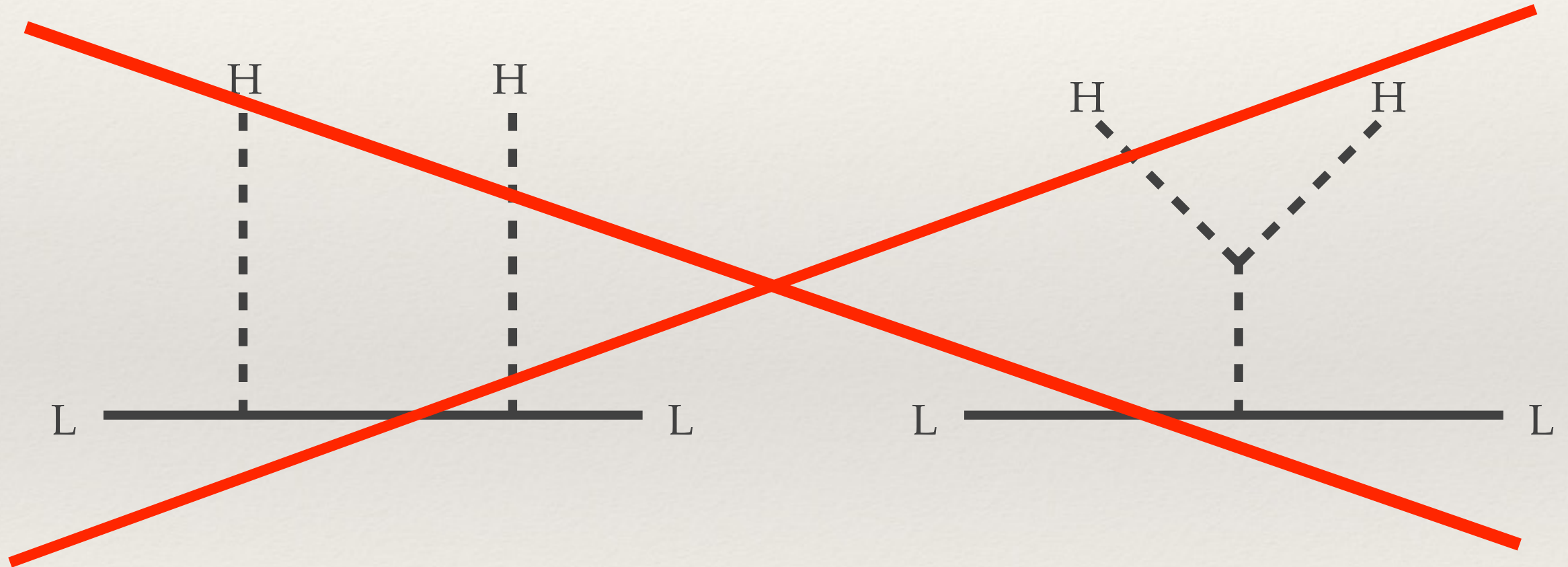
$$\sigma_{\text{SI}}(\text{DM } \mathcal{N} \rightarrow \text{DM } \mathcal{N}) = (n^2 - 1)^2 \frac{\pi \alpha_2^4 M_{\mathcal{N}}^4 f^2}{64 M_W^2} \left(\frac{1}{M_W^2} + \frac{1}{m_h^2} \right)^2.$$

Seesaw Masses



$$2 \times 2 = 1 + 3$$

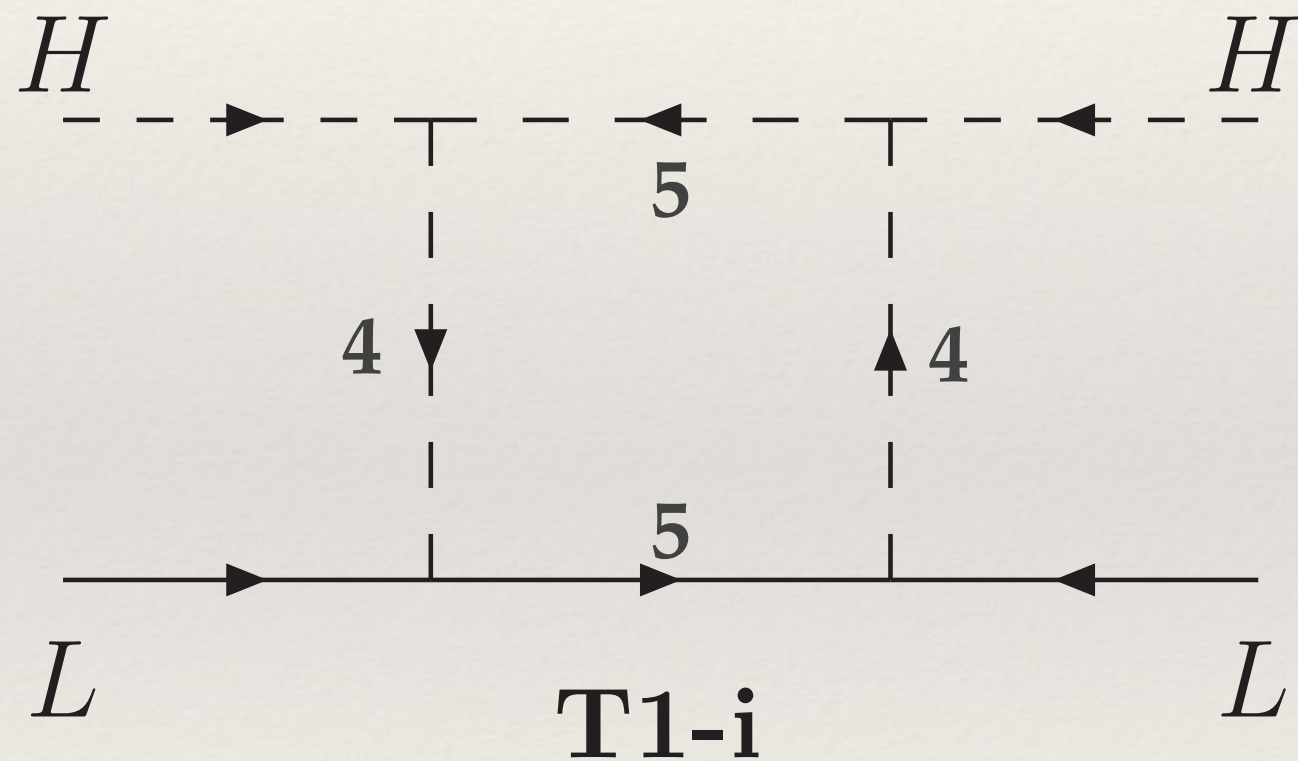
Seesaw Masses



$$2 \times 2 = 1 + 3$$

One Loop Example

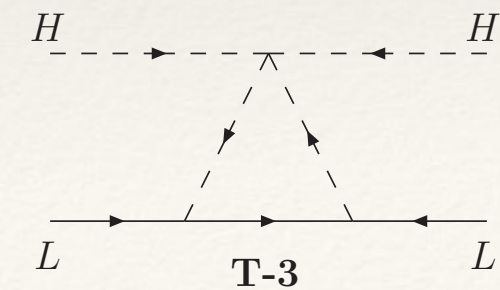
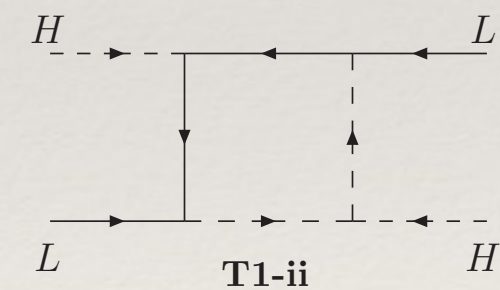
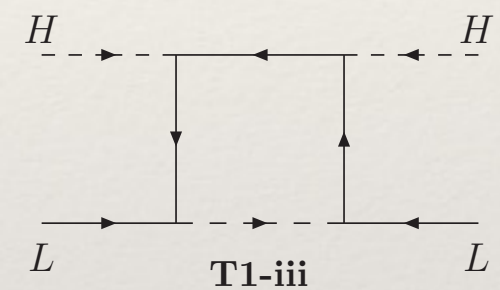
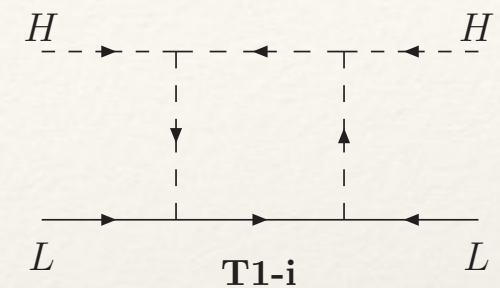
$$5 \times 4 \times 2 = 1$$



Fermonic 5plet

DM~(5,0)

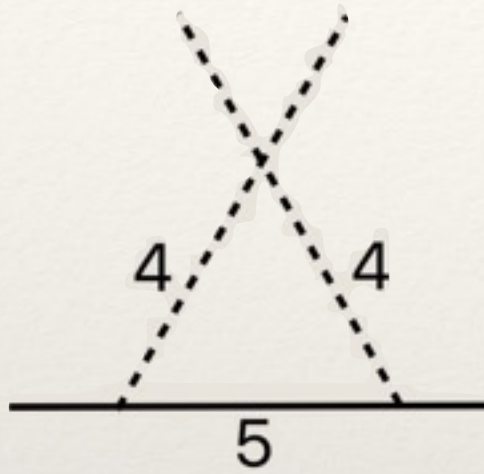
T-3	(4,1)	(6,1)	(4,1) (6,1)			
T3, T1-i	(4,1)(3,0)	(4,1) (5,0)	(4,1)(5,0) (6,1)	(6,1) (5,0)	(6,1) (7,0)	
T3, T1-i, T1-ii	(4,1) (4,1)(3,0)	(4,1) (4,1) (5,0)	(6,1) (4,1)(5,0)	(4,1) (6,1) (5,0)	(6,1) (6,1) (5,0)	(6,1) (6,1) (7,0)
T1-iii	(4,1) (3,0)	(4,1) (5,0)	(6,1) (5,0)	(4,1) (6,1) (5,0)	(6,1) (7,0)	
T3, T1-iii	(4,1) (3,2) (4,1)	(4,1) (5,2) (4,1)	(6,1) (5,2) (4,1)	(4,1) (5,2) (6,1)	(6,1) (5,2) (6,1)	(6,1) (7,2) (6,1)



Fermion Scalar

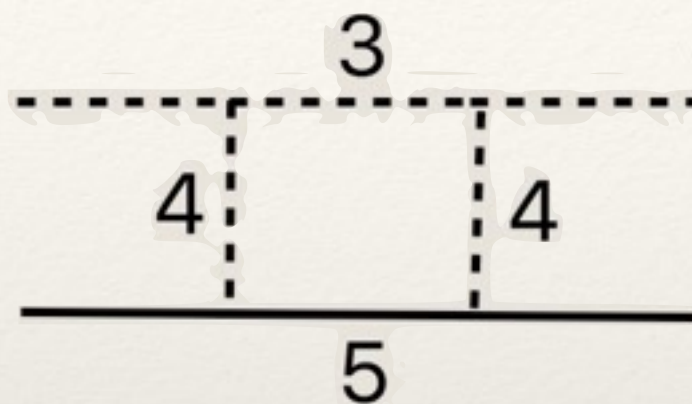
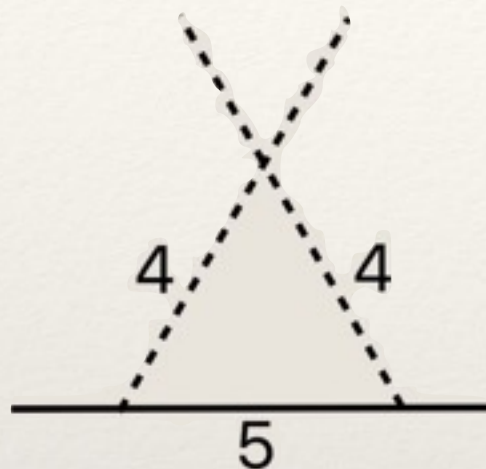
Example

$(5,0)(4,1)$



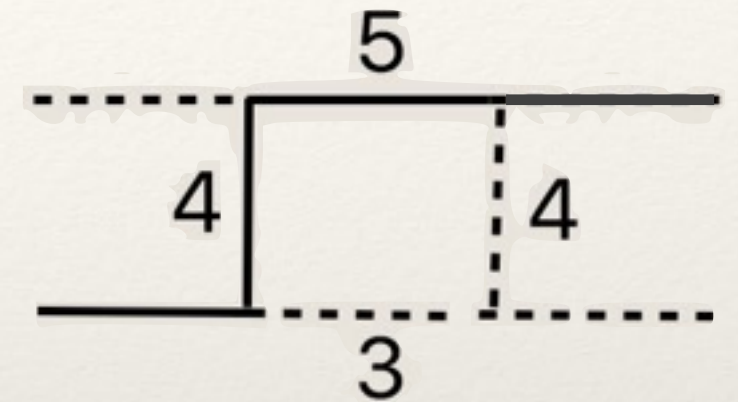
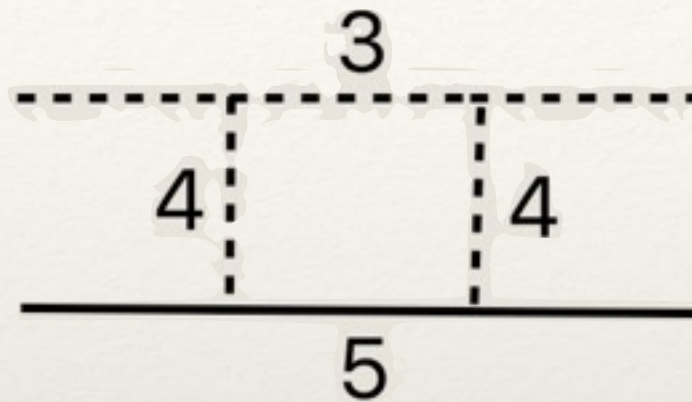
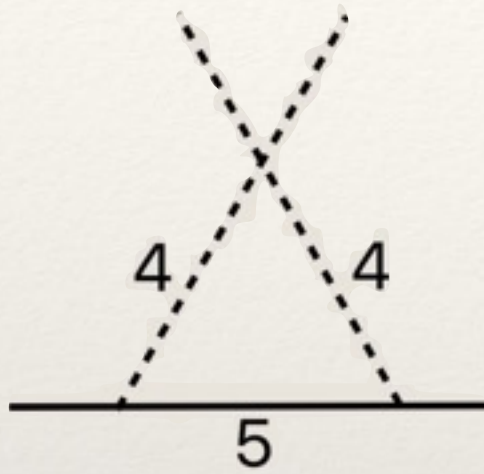
Example

$(5,0)(4,1)(3,0)$



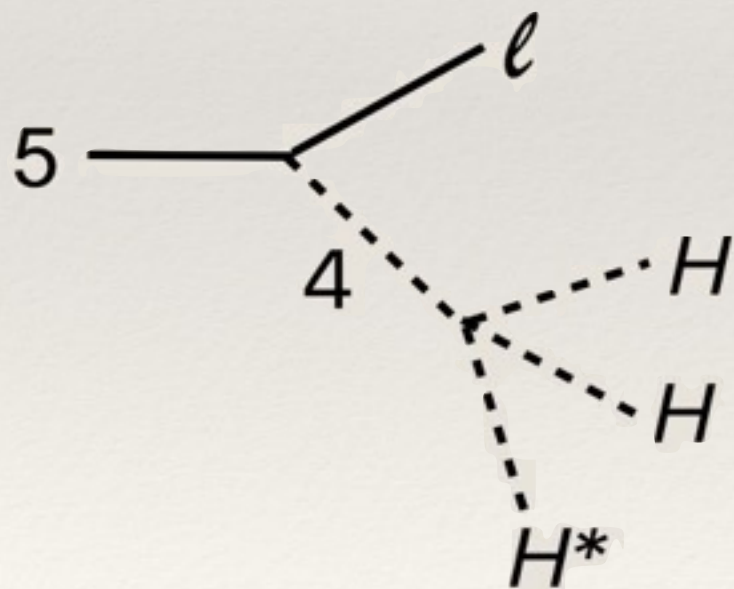
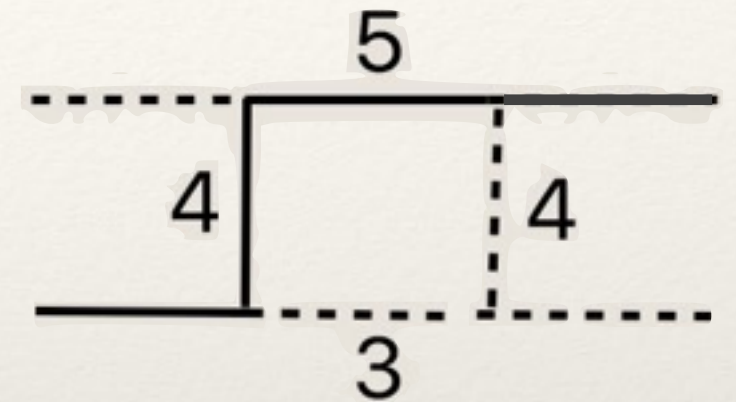
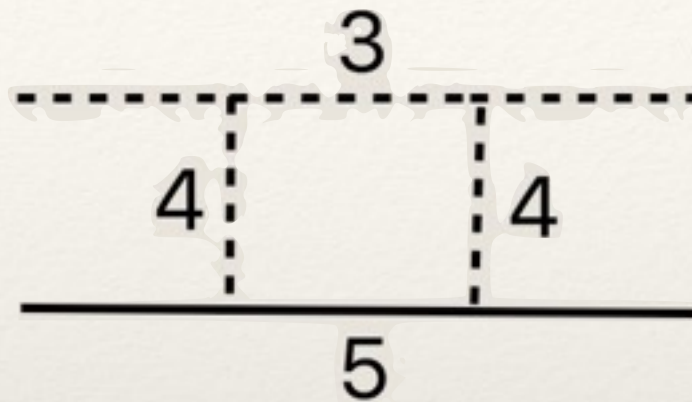
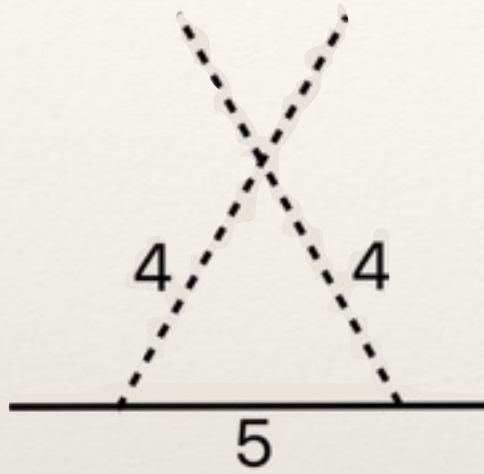
Example

$(5,0)(4,1)(3,0)(4,1)$



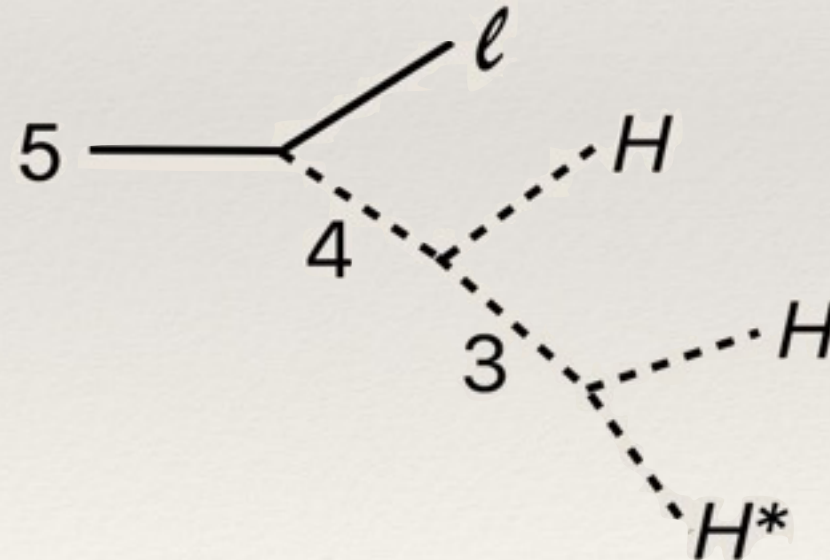
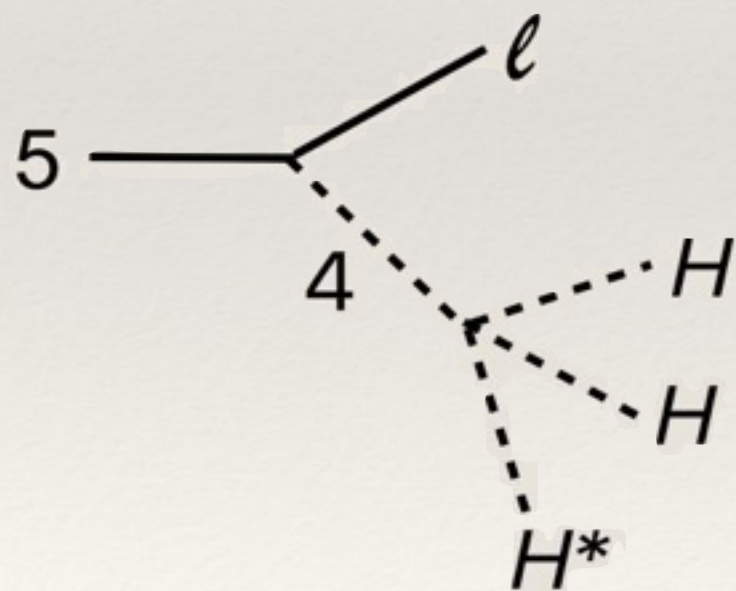
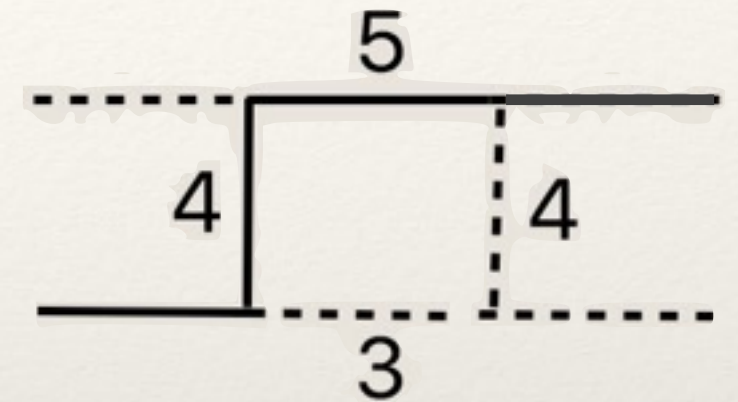
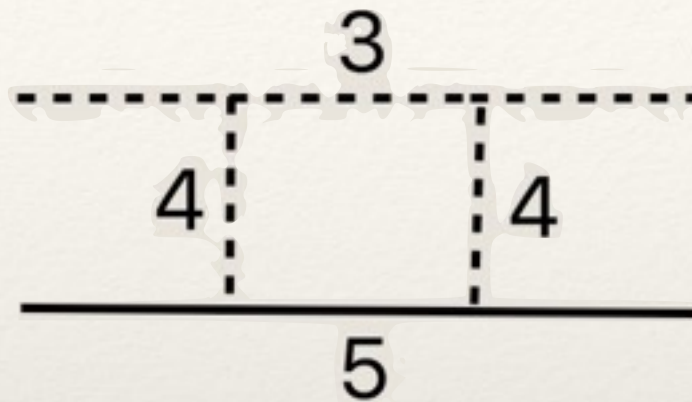
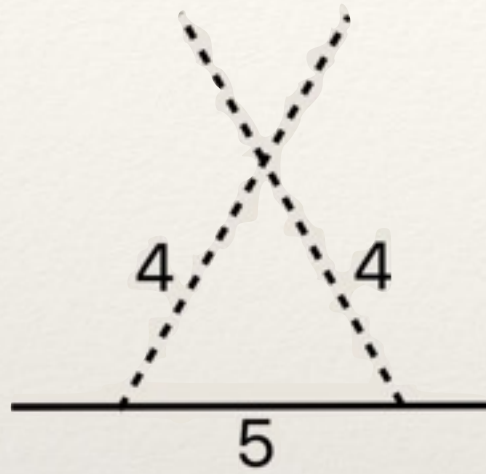
Example

$(5,0)(4,1)(3,0)(4,1)$



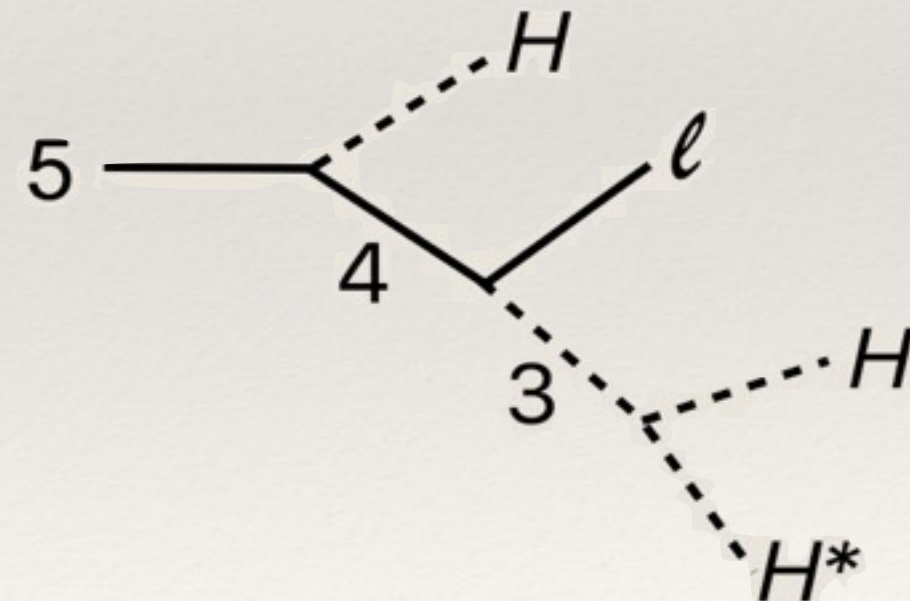
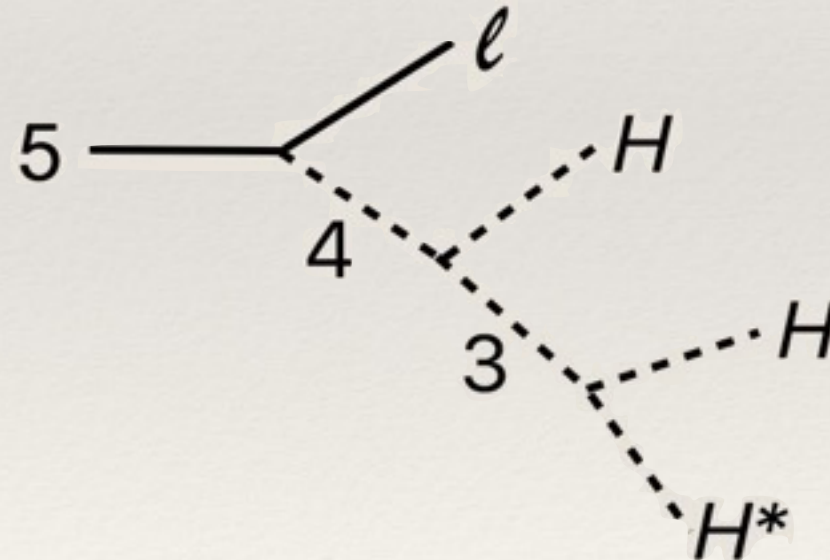
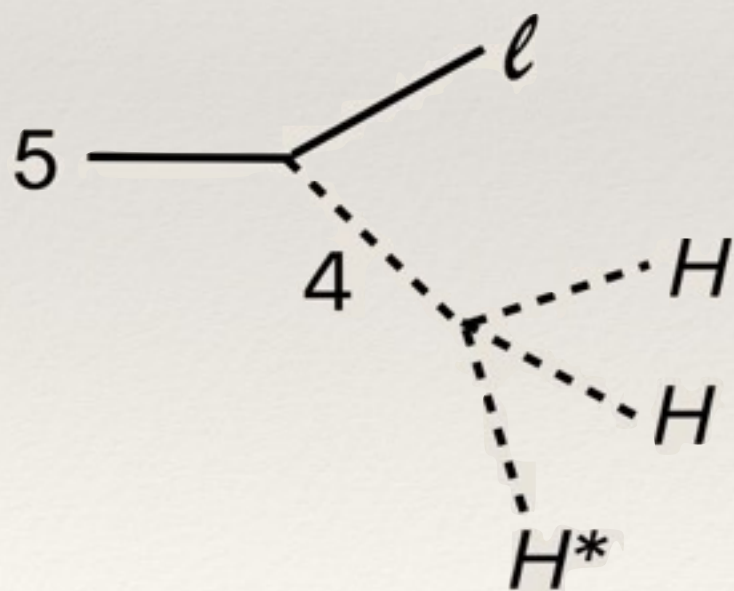
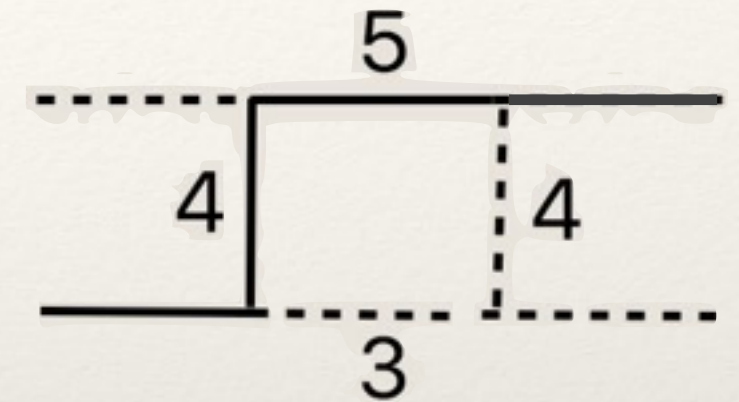
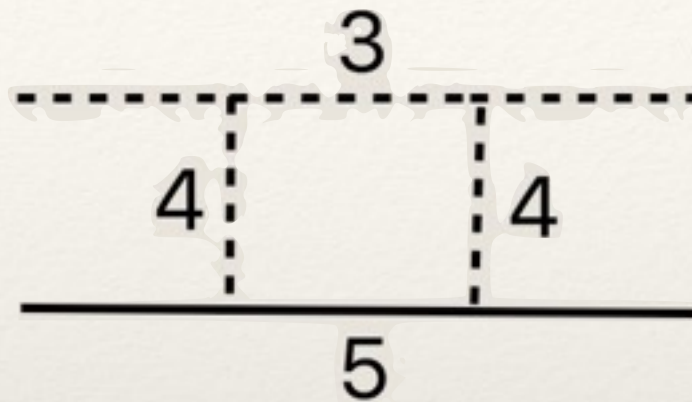
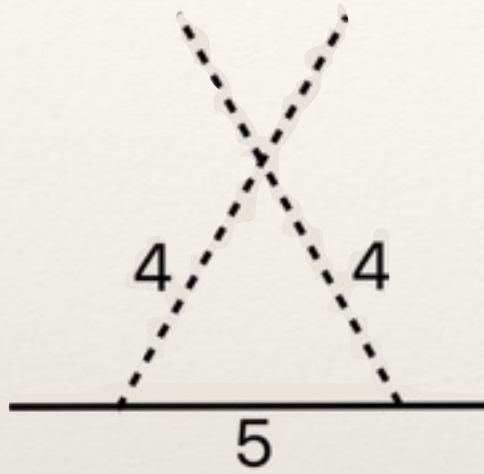
Example

$(5,0)(4,1)(3,0)(4,1)$



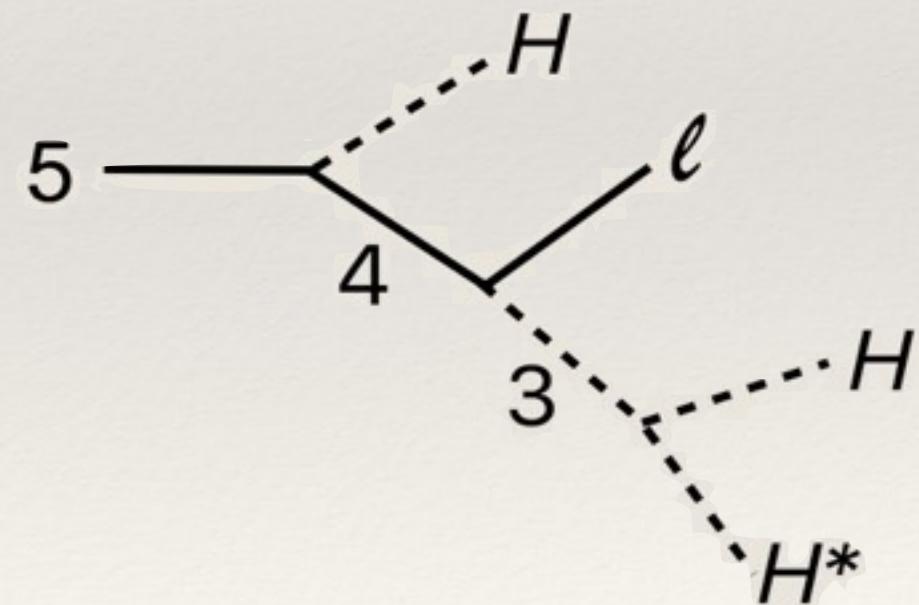
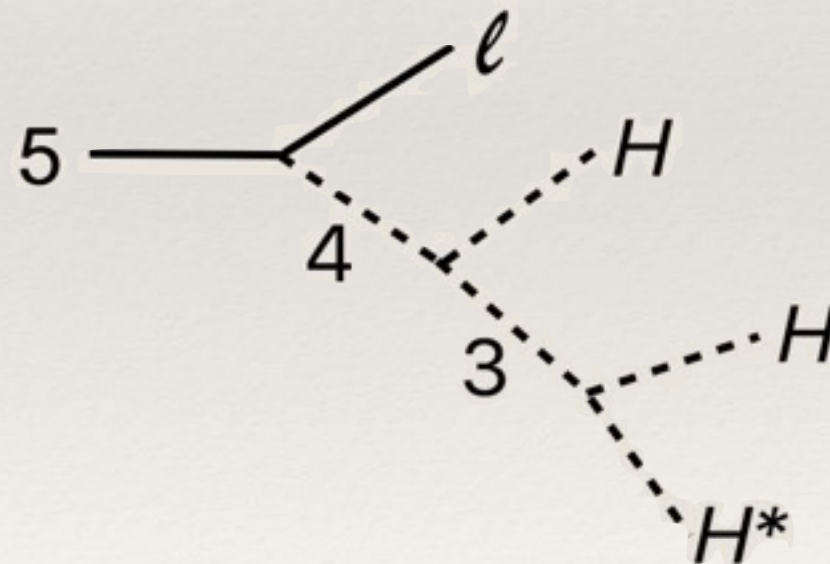
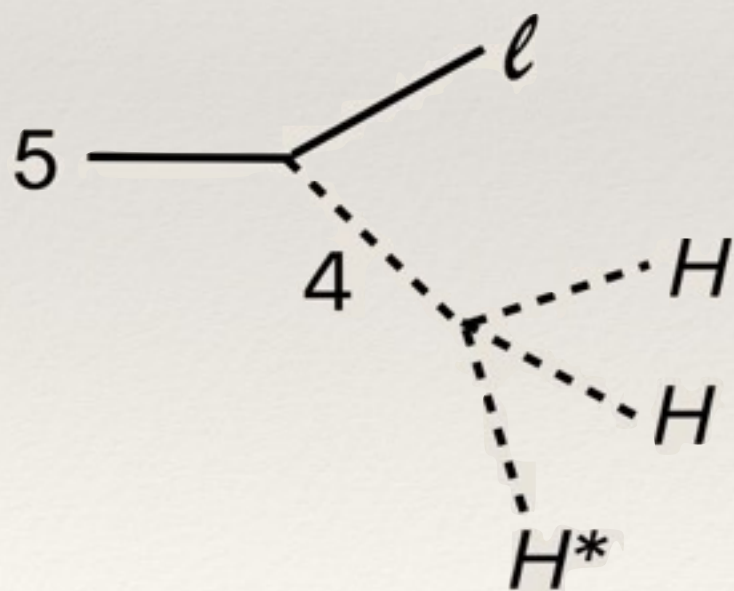
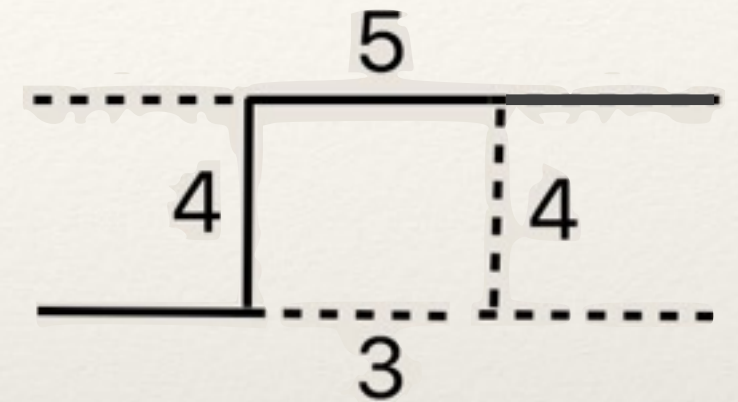
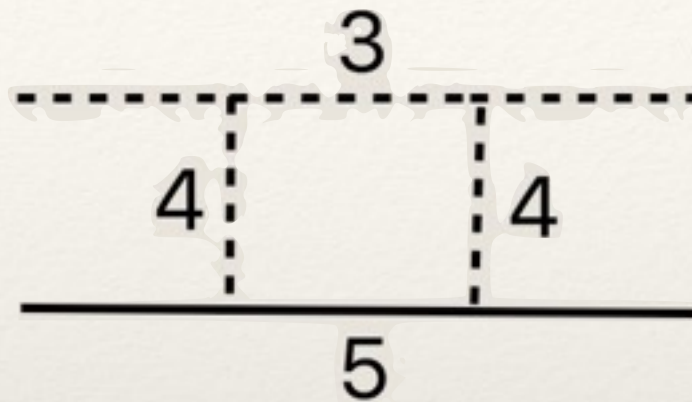
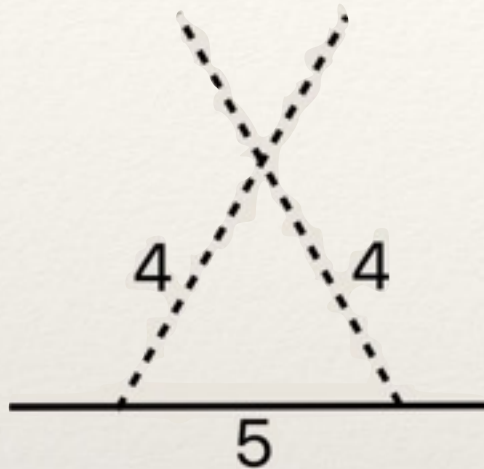
Example

$(5,0)(4,1)(3,0)(4,1)$



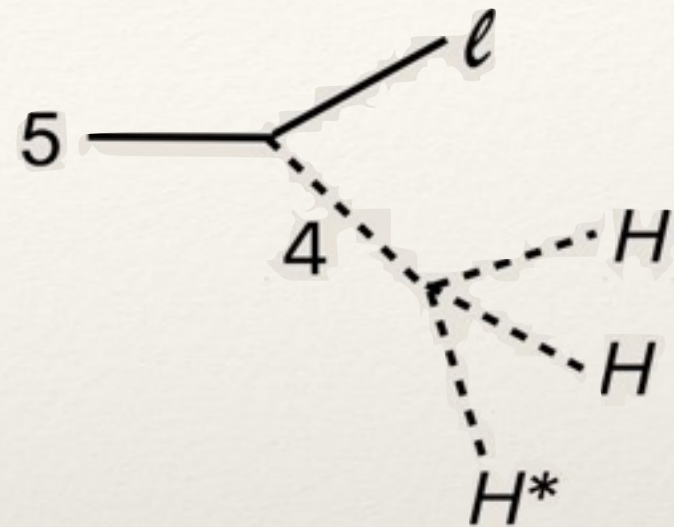
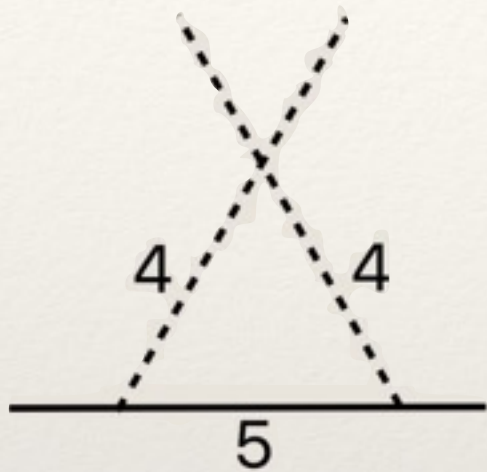
Example

$(5,0)(4,1)(3,0)(4,1)$



Dim 5

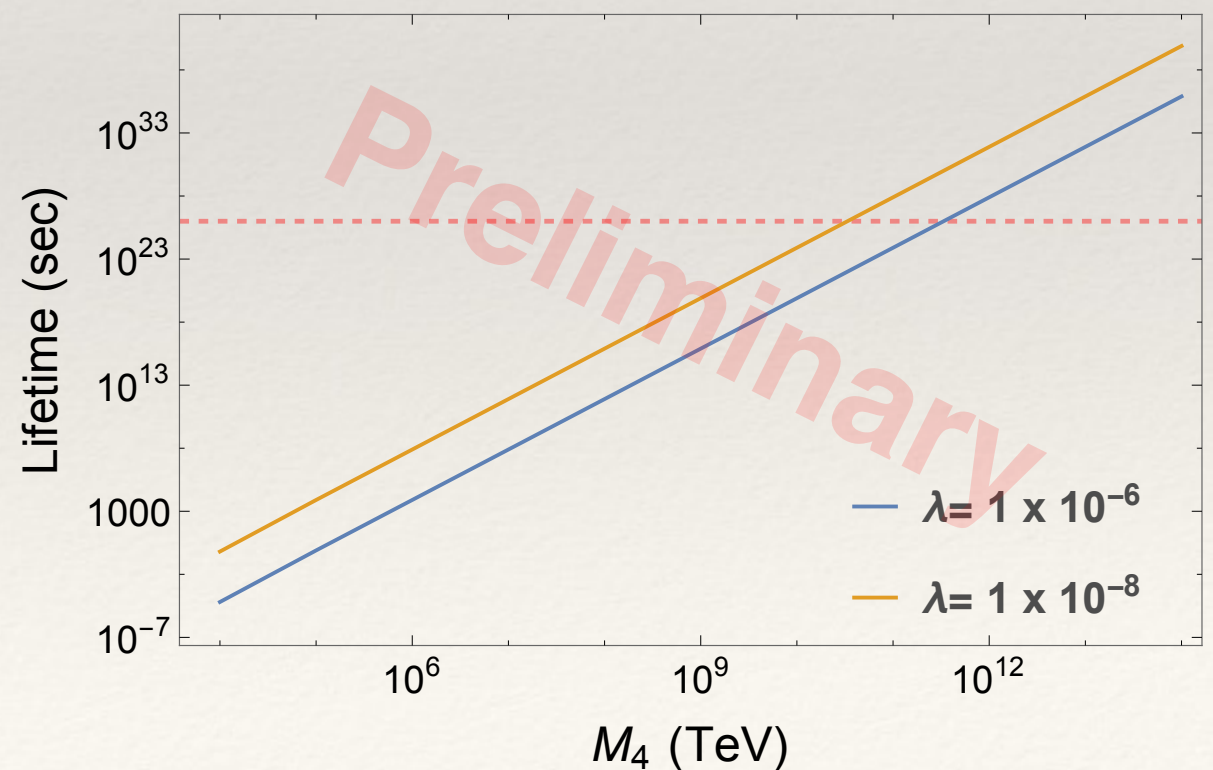
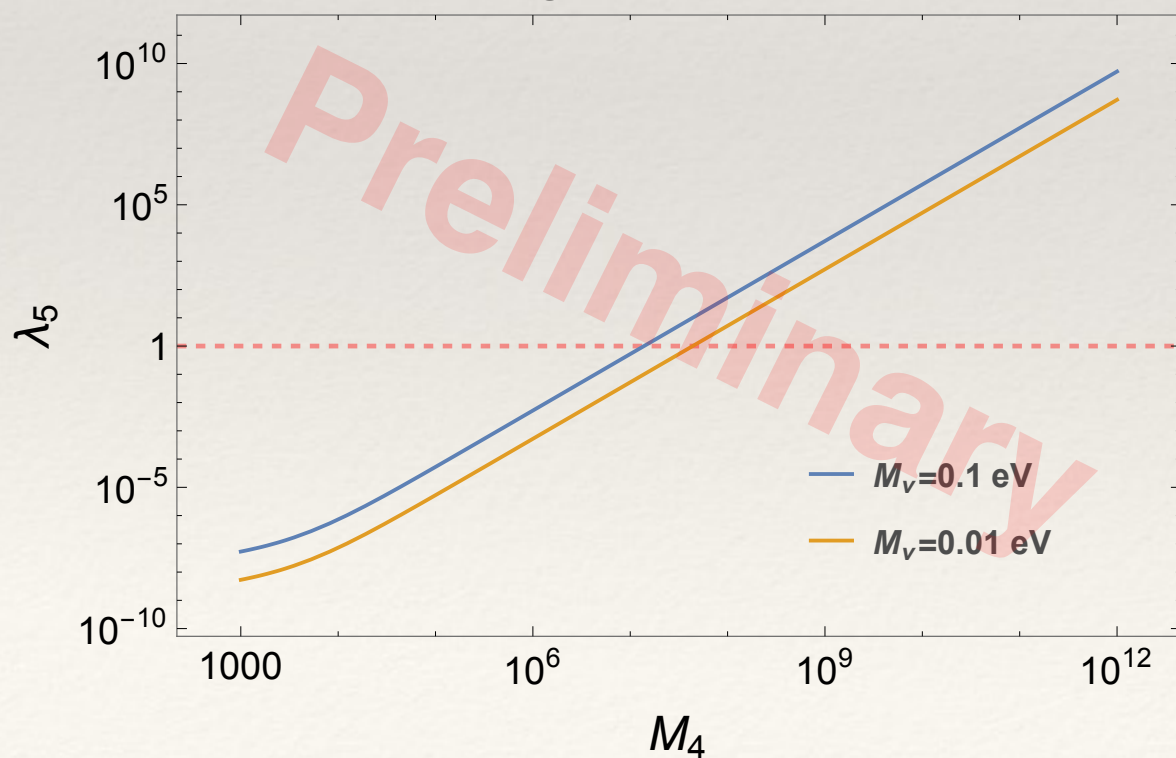
Parameter Space in Decay Cascades



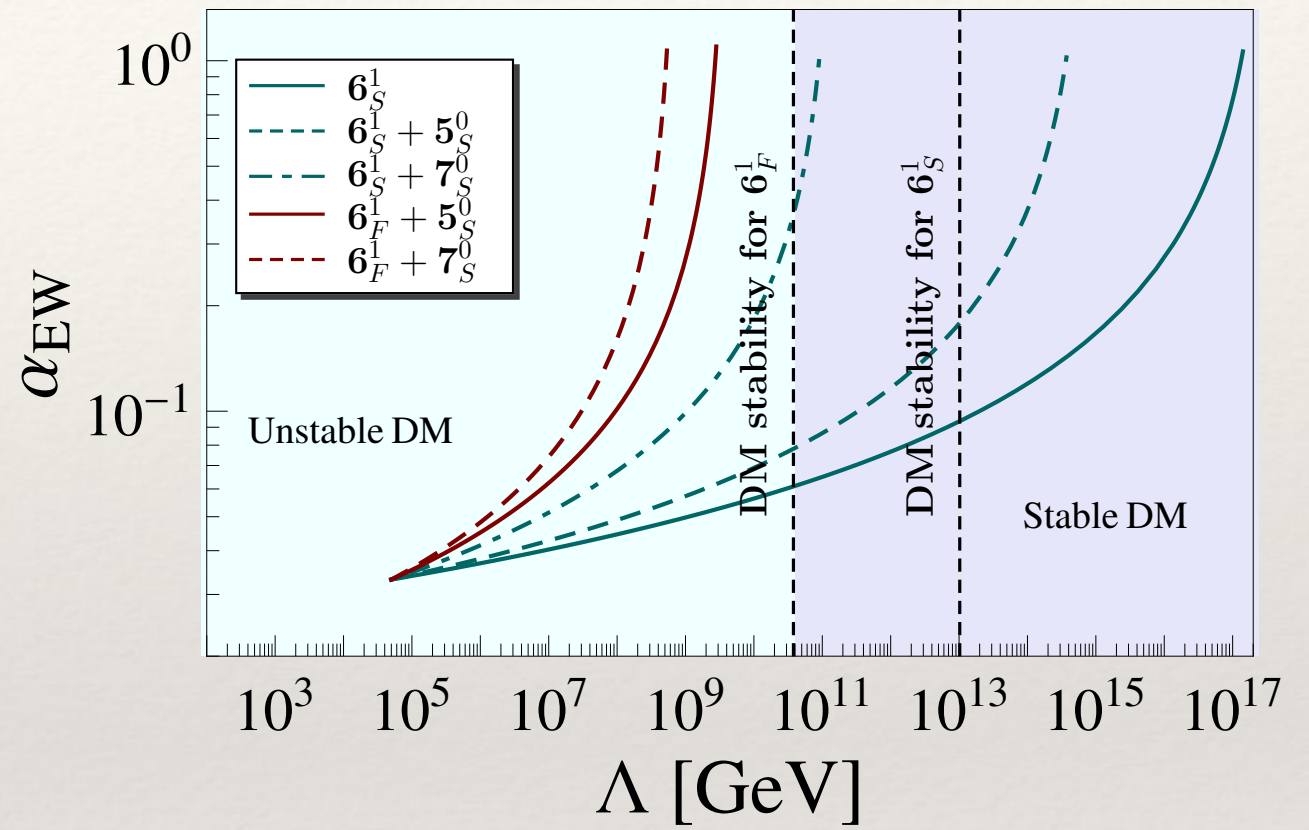
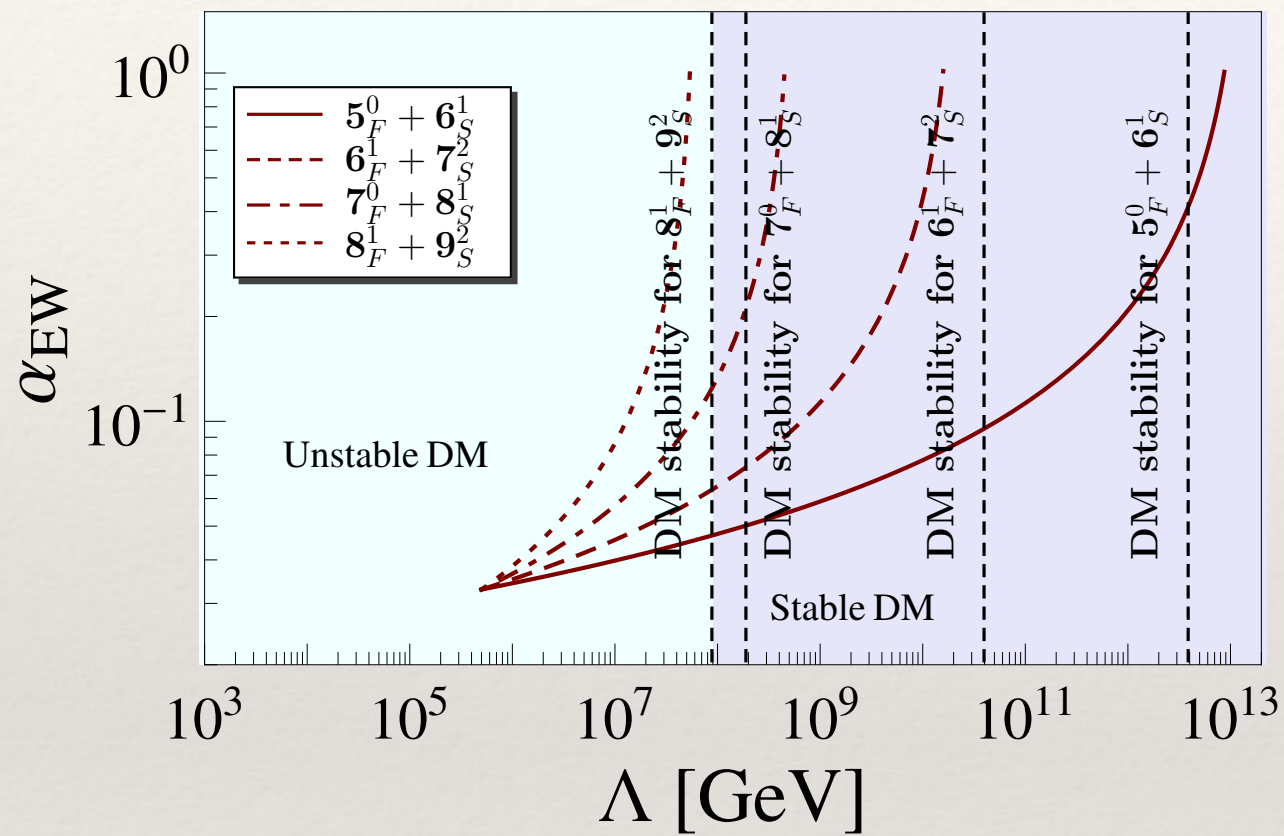
Scotogenic Neutrino Mass

$M_5 = 5 \text{ TeV}, Y=0.1$

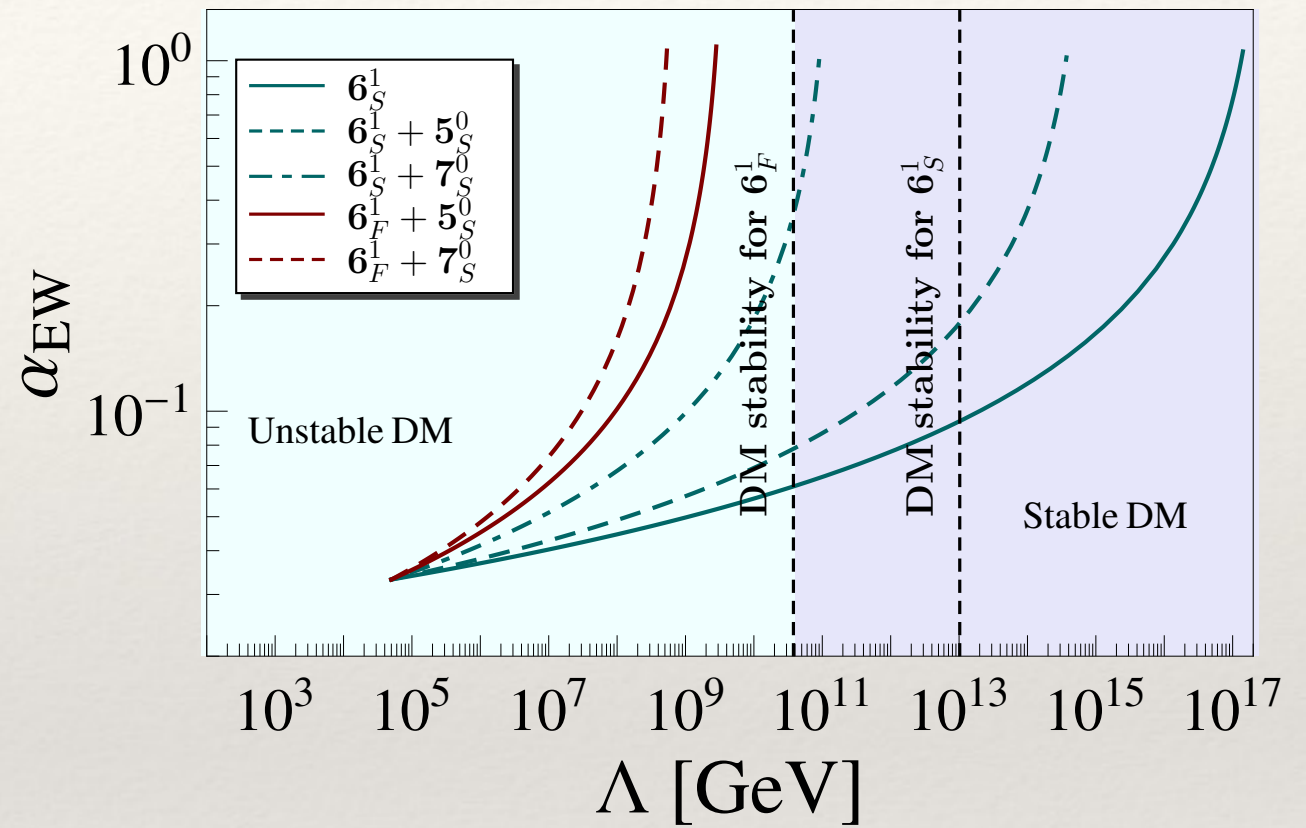
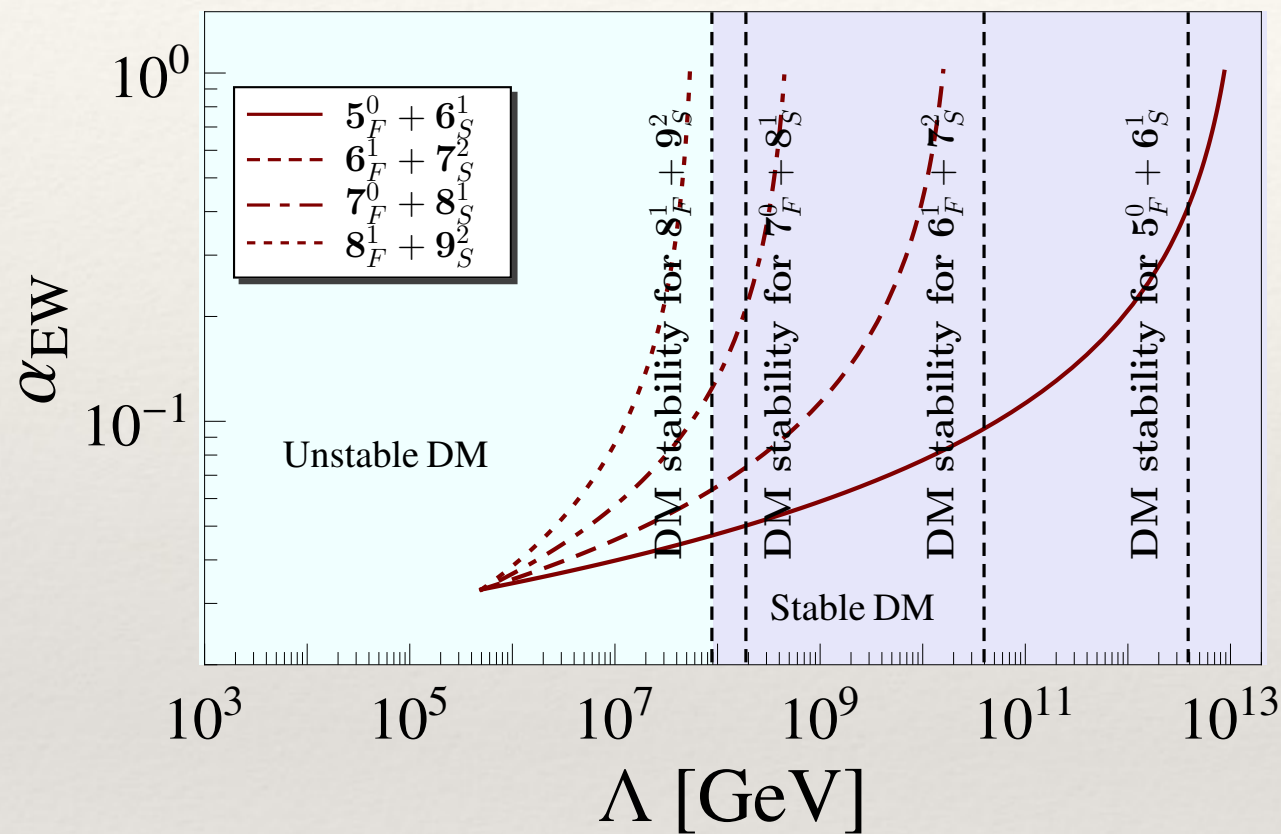
$5_F \rightarrow 1 H H H$



Perturbativity



Perturbativity



Careful: Quartic coupling running
goes faster than α_{EW} .

(Hamada, Kawana, Tsumara. hep-ph 1505.01772)

Scalar 7plet

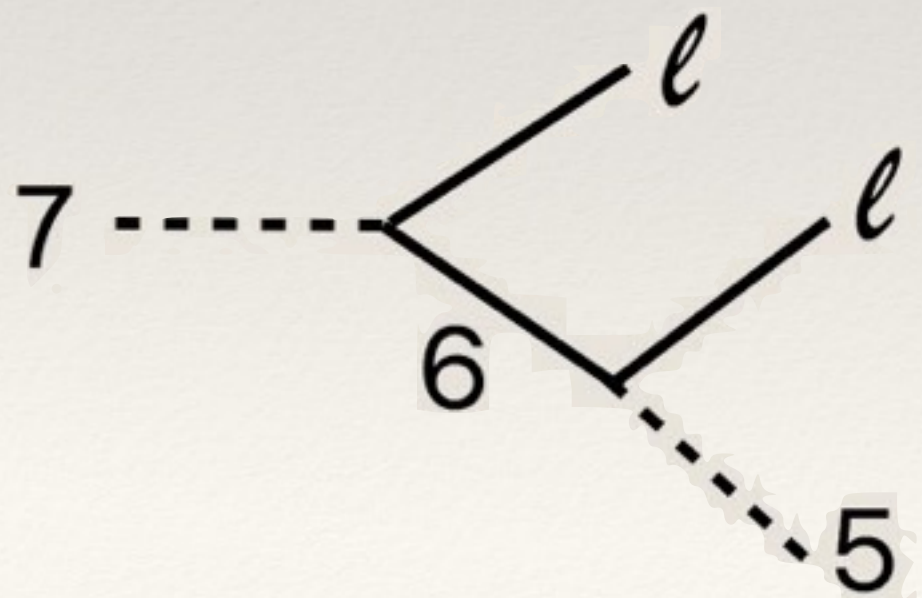
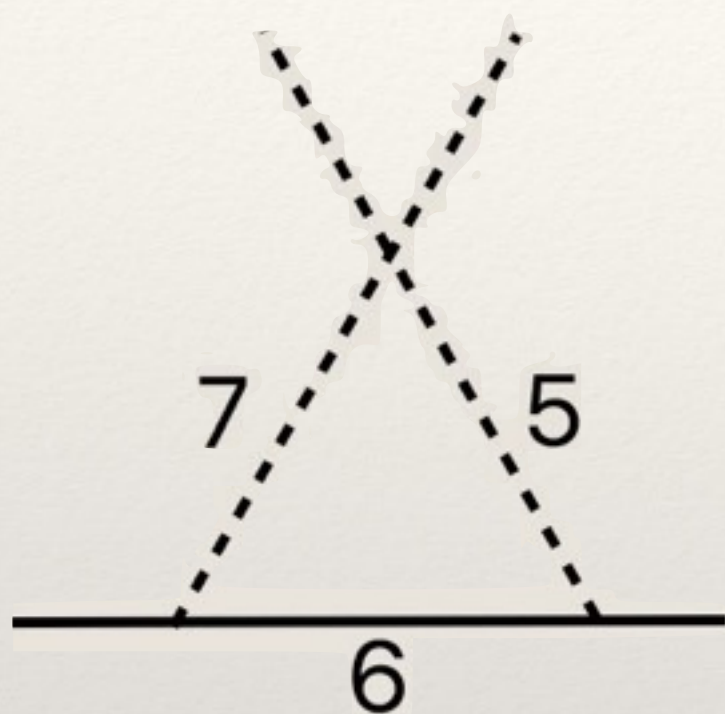
DM~(7,0)

T-3	(6,1) (5,2)	(6,1) (7,2)	(8,1) (7,2)	(8,1) (9,2)			
T1-i	(5,0) (6,1)	(7,0) (6,1)	(7,0) (6,1) (8,1)	(7,0) (8,1)	(9,0) (8,1)		
T3, T1-i	(6,1) (5,2) (6,1)	(6,1) (5,2) (6,1)	(6,1) (7,2) (6,1)	(6,1) (7,2) (8,1)	(8,1) (7,2) (6,1)	(8,1) (7,2) (8,1)	(8,1) (9,2) (8,1)
T1-iii	(6,1) (5,0)	(6,1) (7,0)	(6,1) (7,0) (8,1)	(8,1) (7,0)	(8,1) (9,0)		
T1-i, T2-ii, T3-iii	(6,1) (5,0) (6,1)	(6,1) (7,0) (6,1)	(6,1) (7,0) (8,1)	(8,1) (7,0) (6,1)	(8,1) (7,0) (8,1)	(8,1) (9,0) (8,1)	

Fermion Scalar

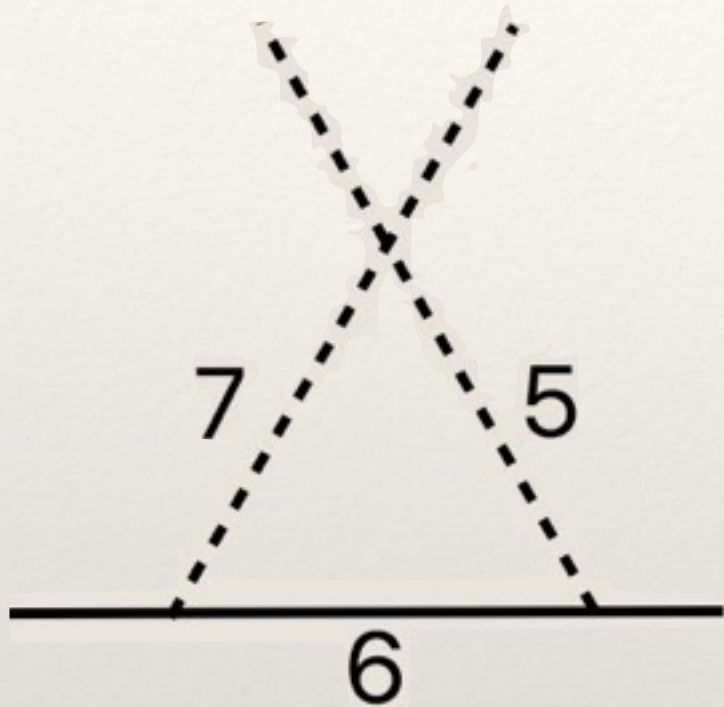
Example 2

$(7,0)(6,1)(5,2)$

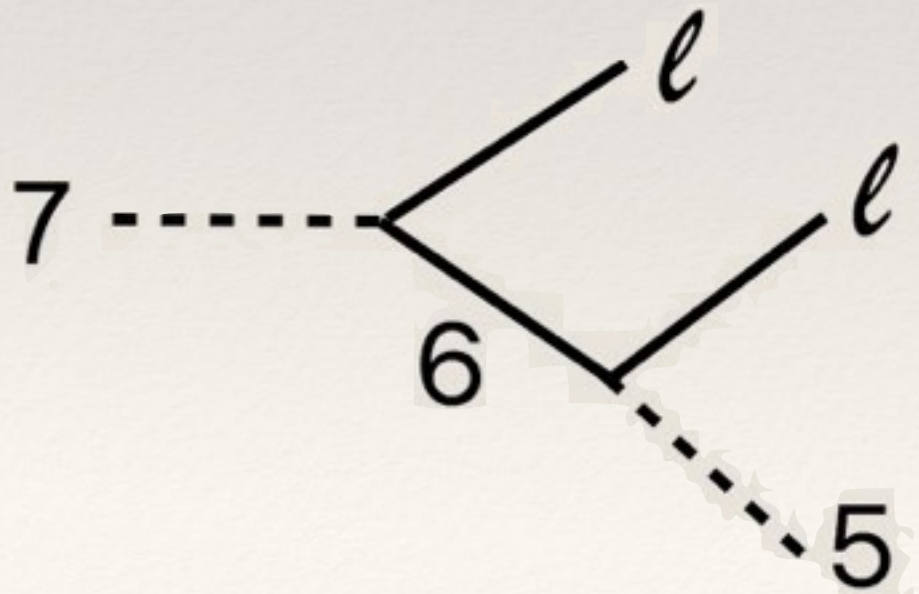


Example 2

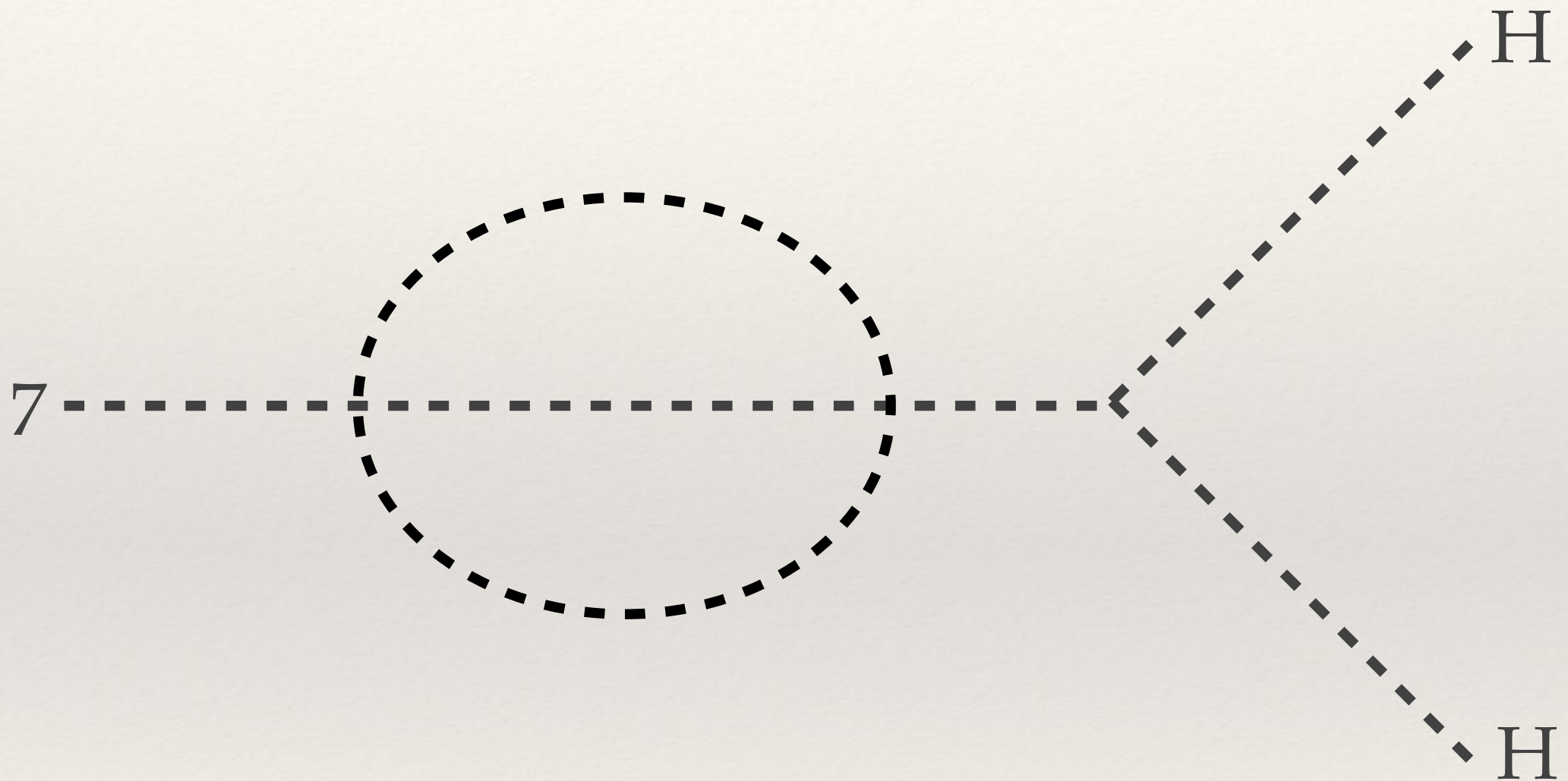
$(7,0)(6,1)(5,2)$



Only models with an $SU(2)_{\sim 3}$ or a ~ 4 can decay into all SM particles.



In Progress: Decays With a Loop



Dim 4

Conclusions

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