Particle Detection: Trackers

Lecture I

Gregor Herten

University of Freiburg, Germany

09. June 2009

CERN-FNAL HCP School 2009

Outline

Lecture 1

- 1. Interaction of charged particle with matter
- 2. Momentum measurement
- 3. Drift and Diffusion in Gases
- 4. History of Tracking Detectors (not shown)
- 5. Proportional Chambers

Lecture 2

- 6. Drift Chambers
- 7. Micro Pattern Gas Chambers
- 8. Limitations of Gaseous Detectors

Lecture 3

- 9. Vertex Reconstruction
- **10. Semiconductor Detectors**
- 11. Silicon Strip and Pixel Detectors
- 12. Radiation Damage of Silicon Detectors
- 13. New Semiconductor Detector Concepts
- 14. Tracking Systems: ATLAS, CMS

I. Interaction of Particle with Matter



Challenge in Tracking

e+ e- collision in the ALEPH Experiment/LEP.

ALEPH DAL

Au+ Au+ collision in the STAR Experiment/RHIC Up to 2000 tracks Pb+ Pb+ Kollision in the ALICE Experiment/LHC Simulation for Angle Θ=60 to 62° Up to 40 000 tracks/collision







Gregor Herten / 4. History of Tracking Detectors

I. Energy Loss of Charged Particle by Atomic Collisions

- A charged particle passing through matter suffers
- 1. energy loss
- 2. deflection from incident direction

Main type of reactions:

- 1. Inelastic collisions with atomic electrons of the material.
- 2. Elastic scattering from nuclei.

Less important reactions are:

- 3. Emission of Cherenkov radiation
- 4. Nuclear reactions
- 5. Bremsstrahlung

Classification of charged particles with respect to interaction with matter:

- 1. Low mass: electrons and positrons
- 2. High mass: muons, pions, protons, light nuclei.

Energy loss:

- mainly due to inelastic collisions with atomic electrons.
- cross section $\sigma \approx 10^{-17} 10^{-16} \text{ cm}^2 !$
- small energy loss in each collision, but many collisions in dense material. Thus one can work with average energy loss.
- Example: a proton with E_{kin}=10 MeV looses all its energy after 0.25 mm of copper.

Two groups of inelastic atomic collisions:

- soft collisions: only excitation of atom.
- hard collisions: ionization of atom. In some of the hard collisions the atomic electron get such a large energy that it causes secondary ionisation (δelectrons).

Elastic collisions from nuclei cause very small energy loss. They are the main cause for deflection.

I. Bethe-Bloch Formula

Bethe-Bloch formula gives the mean rate of energy loss (stopping power) of a heavy charged particle.

$$-\frac{dE}{dx} = Kz^2 \frac{Z}{A} \frac{1}{\beta^2} \left[\frac{1}{2} \ln \frac{2m_e c^2 \beta^2 \gamma^2 T_{max}}{I^2} - \beta^2 - \frac{\delta(\beta\gamma)}{2}\right]$$

with

A : atomic mass of absorber

$$\frac{K}{A} = 4\pi N_A r_e^2 m_e c^2 / A = 0.307075 \text{ MeV g}^{-1} \text{cm}^2$$
, for A = 1g mol⁻¹

z: atomic number of incident particle

Z: atomic number of absorber

 $T_{
m max}$: Maximum energy transfer in a single collision T_m

$$aax = \frac{2m_e c^2 \beta^2 \gamma^2}{1 + 2\gamma m_e/M + (m_e/M)^2}$$

 $\delta(\beta\gamma)$: density effect correction to ionization loss.

 $x = \rho s$, surface density or mass thickness, with unit g/cm², where s is the length.

dE/dx has the units MeV cm²/g

PDG 2008

I. History of Energy Loss Calculations: dE/dx

1915: Niels Bohr, classical formula, Nobel prize 1922.1930: Non-relativistic formula found by Hans Bethe1932: Relativistic formula by Hans Bethe

Bethe's calculation is leading order in pertubation theory, thus only z^2 terms are included.

Additional corrections:

- z³ corrections calculated by Barkas-Andersen
- z⁴ correction calculated by Felix Bloch (Nobel prize 1952, for nuclear magnetic resonance). Although the formula is called Bethe-Bloch formula the z⁴ term is usually not included.
- Shell corrections: atomic electrons are not stationary
- Density corrections: by Enrico Fermi (Nobel prize 1938, for discovery of nuclear reaction induced by slow neutrons).



(not shown)

Hans Bethe 1906-2005

Born in Strasbourg, emigrated to US in 1933. Professor at Cornell U. Nobel prize 1967 for theory of nuclear processes in stars.

I. Examples of Mean Energy Loss





PDG 2008

I. Particle Identification from dE/dx and p Measurements



A simultaneous measurement of dE/dx and momentum can provide particle identification.



I. Fluctuations in Energy Loss



I. Bremsstrahlung

High energy electrons loose their energy predominantly through radiation (bremsstrahlung).



The electron is decelerated (accelerated) in the field of the nucleus. Accelerated charges radiate photons. Thus the bremsstrahlung is strong for light charged particles (electrons), because its acceleration is large for a given force. For heavier particles like muons bremsstrahlung effects are only important at energies of a few hundred GeV.

The presence of a nucleus is required to restore energy-momentum conservation. Thus the cross section is proportional to Z^2 and α^3 (α = fine structure constant).

The characteristic length which a electron travels in material until a bremsstrahlung happens is the radiation length X_0 .

I. Radiation Length X₀

The radiation length is the characteristic length scale to describe electromagnetic showers in material. It is usually measured in g/cm².

The radiation length is:

- the mean distance over which a high energy electron looses all but 1/e of its energy.
- 7/9 of the mean free path for pair production by a high energy photon.

The radiation length is give by:

$$\frac{1}{X_0} = 4\alpha r_e^2 \frac{N_A}{A} \left\{ Z^2 \left[L_{\text{rad}} - f(Z) \right] + Z L_{\text{rad}}' \right\}$$

For
$$A = 1$$
 g mol⁻¹, $4\alpha r_e^2 N_A / A = (716.408 \text{ g cm}^{-2})^{-1}$.

$$f(Z) = a^{2} [(1 + a^{2})^{-1} + 0.20206$$
$$-0.0369 a^{2} + 0.0083 a^{4} - 0.002 a^{6}]$$

where $a = \alpha Z$

Element	Z	L _{rad}	$L'_{\rm rad}$
Н	1	5.31	6.144
He	2	4.79	5.621
Li	3	4.74	5.805
Be	4	4.71	5.924
Others	> 4	$\ln(184.15 Z^{-1/3})$	$\ln(1194Z^{-2/3})$

I. High Energy Muon Bremsstrahlung



Bremsstrahlung off muons starts to be important for momenta of a few hundred GeV.

Cosmic muon bremsstrahlung event in the ALEPH detector at LEP.

I. Multiple Coulomb Scattering





Figure 27.9: Quantities used to describe multiple Coulomb scattering. The particle is incident in the plane of the figure.

A particle which traverses a medium is deflected by small angle Coulomb scattering from nuclei. For hadronic particles also the strong interaction contributes.

The angular deflection after traversing a distance x is described by the Molière theory. The angle has roughly a Gauss distribution, but with larger tails due to Coulomb scattering.

Defining:
$$\theta_0 = \theta_{\text{plane}}^{\text{rms}} = \frac{1}{\sqrt{2}} \theta_{\text{space}}^{\text{rms}}$$

Gaussian approximation:

$$\theta_0 = \frac{13.6 \text{ MeV}}{\beta cp} \ z \ \sqrt{x/X_0} \Big[1 + 0.038 \ln(x/X_0) \Big]$$

 x/X_0 is the thickness of the material in radiation length.

2. Momentum measurement in B-Fields

The momentum is measured from the sagitta s, which gives the curvature ρ of the track in the magnetic field.



Transverse momentum:

$$p_T = qB\rho$$

$$p_T[GeV] = 0.3 \ B[T] \ \rho[m]$$

$$\frac{L/2}{\rho} = \sin\frac{\theta}{2} \approx \frac{\theta}{2} \ (\text{for small } \theta) \Rightarrow \theta \approx \frac{L}{\rho} = \frac{0.3BL}{p_T}$$

$$s = \rho(1 - \cos\frac{\theta}{2}) \approx \rho\left(1 - (1 - \frac{1}{2}\frac{\theta^2}{4})\right) = \rho\frac{\theta^2}{8} \approx \frac{0.3BL^2}{8p_T}$$
Example: 3 measurements
$$s = x_2 - (x_1 + x_3)/2 \rightarrow ds = dx_2 - dx_1/2 - dx_3/2$$
assume uncorrelated errors: $\sigma(x) \approx dx_i$

$$\sigma_s^2 = \sigma^2(x) + 2\frac{\sigma^2(x)}{4} = \frac{3}{2}\sigma^2(x)$$

Gregor Herten / 2. Momentum Measurement

2. Relative Momentum Error

For 3 points the relative momentum resolution is given by: $\frac{\sigma(p_T)}{p_T} = \frac{\sigma_s}{s} = \sqrt{\frac{3}{2}}\sigma(x) \cdot \frac{8p_T}{0.3BL^2}$

- degrades linearly with transverse momentum
- improves linearly with increasing B field
- improves quadratically with radial extension of detector

In the case of N equidistant measurements according to Gluckstern [NIM 24 (1963) 381]:

 $\frac{\sigma(p_T)}{p_T} = \frac{\sigma(\kappa)}{\kappa} = \frac{\sigma(x) \cdot p_T}{0.3BL^2} \sqrt{\frac{720}{(N+4)}}$

(for
$$N \ge 10$$
 , curvature $\kappa = 1/\rho$)

Example: For $p_T = 1$ GeV, L = 1m, B = 1T, $\sigma(x) = 200 \mu$ m and N = 10 one obtains:



Gregor Herten / 2. Momentum Measurement

2. Contributions from Multiple Scattering

The contribution to the momentum error from MS is given by:



3 Drift and Diffusion in Gases : Ionization



Fast charged particles ionize atoms of gas. Often resulting primary electron will have enough kinetic energy to ionize other atoms.

$$\begin{split} n_{total} &= \frac{\Delta E}{W_i} = \frac{\frac{dE}{dx}\Delta x}{W_i} & n_{total} \text{-number of created} \\ n_{total} &\approx 3 \dots 4 \cdot n_{primary} & \Delta_E &= \text{total energy loss} \\ W_i &= \text{effective /pair} \end{split}$$

Number of primary electron/ion pairs in frequently used gases.

Lohse and Witzeling, Instrumentation In High Energy Physics, World Scientific, 1992

from L. Ropelewski



3. Primary Ionization in Gases

The actual number **m** of primary electron/ion pairs is Poisson distributed.

$$P(m) = \frac{\bar{n}^m e^{-\bar{n}}}{m!}$$

, where the average number of electron/ion pairs is $\ \, ar{n} = rac{L}{\lambda} = L N \sigma_i$

Detection efficiency ε: Depends on the minimum number of measurable electron/ion pairs

Example: m > 0 $\epsilon = 1 - P(0) = 1 - e^{-\bar{n}}$

For thin detector layers the efficiency can be significantly smaller then 1. Example: 1 mm of Ar ; $\bar{n} = 2.5 \rightarrow \epsilon = 0.92$

Considering: Electronic noise in amplifier is typically 1000 e⁻ (ENC):

Conclusion: signal amplification in gas is needed!

3. Diffusion in Gases

Electrons and ions, produced by the ionization process, loose their energy by multiple collisions and thermalize with the temperature of the gas.

At room temperature: $\epsilon = (3/2) \text{ kT} \approx 0.04 \text{ eV}$

The energy distribution follows a Maxwell-Boltzmann-Distribution

$$F(\epsilon) = const \cdot \sqrt{\epsilon} \exp(-\epsilon/kT)$$



Due to multiple collisions (diffusion) there is a statistical distribution of charge, which is found in the length interval dx at distance x at a time t according to :

 $\frac{dN}{N} = \frac{1}{\sqrt{4\pi Dt}} \exp\left(-\frac{x^2}{4Dt}\right) dx$ Linear diffusion: $\sigma_x = \sqrt{2Dt}$ Volume diffusion: $\sigma_{vol} = \sqrt{3} \sigma_x = \sqrt{6Dt}$ Average mean free path $\lambda = \frac{1}{N\sigma(\epsilon)}$

Gregor Herten / 3. Drift and Diffusion in Gas

3. Drift and Diffusion in Gases

Average mean free path in diffusion:

$$\lambda = \frac{1}{N\sigma(\epsilon)}$$

where $\sigma(\epsilon)$ is energy dependent collision cross section

 $N = (N_A / A) \rho$: number of molecules per unit volume.

If charge carriers are in an electric field the ordered drift due to the E-field is superimposed by the statistical disordered movement due to diffusion.

The **drift velocity** of the charge carriers inside the gas can be defined as:

$$\vec{v}_{drift} = \mu(E) \ \vec{E} \ \frac{p_0}{p}$$

 $\mu(E)$ energy dependent charge-carrier mobility

 \vec{E} electric field

 p/p_0 pressure normalized to standard pressure

Note that the drift velocity scales with E/p (if μ is constant).

Gregor Herten / 6. Drift and Diffusion in Gas

3. Drift and Diffusion in Gases



Gregor Herten / 3. Drift and Diffusion in Gas



4. History of Tracking Detectors: Cloud Chamber (not shown)



Fast electron in a magnetic field at the Bevatron, 1940



α-particles in air.

In cloud chambers a charged particle causes condensation of a supersaturated gas.

The picture (left) shows and electron with 16.9 MeV initial energy.

It spirals about 36 times in the magnetic field.

Nobel prizes related to cloud chamber development: C. T. R. Wilson, 1927 P.M.S. Blackett, 1948 (triggered chambers)

Gregor Herten / 4. History of Tracking Detectors

4. History of Tracking Detectors: Nuclear Emulsion (not shown)





Discovery of muon and pion

Emulsion detectors are still used today: Opera experiment at Gran Sasso for the identification of tau decays.

(not shown)

Cloud chamber: supersaturating a gas with a vapor.

Bubble chamber: superheated liquid. Invented by Donald A. Glazer, Nobel Prize 1960. A particle depositing energy along it's path makes the liquid boil and forms bubbles.



The 80-inch Bubble Chamber

BNL, First Pictures 1963, 0.03s cycle



4. Bubble Chamber : BEBC

(not shown)



Can be seen outside the Microcosm Exhibition

3.7 meter hydrogen bubble chamber at CERN, equipped with the largest superconducting magnet in the world at that time.

During its working life from 1973 to 1984, the "Big European Bubble Chamber" (BEBC) took over 6 million photographs.



The excellent position $(5\mu m)$ resolution and the fact that target and detecting volume are the same (H chambers) makes the Bubble chamber almost unbeatable for reconstruction of complex decay modes.

The drawback of the bubble chamber is the low rate capability (a few tens/ second). E.g. LHC 10⁹ collisions/s.

The fact that it cannot be triggered selectively means that every interaction must be photographed.

Analyzing the millions of images by 'operators' was a quite laborious task.

That's why electronics detectors took over in the 70ties.

4. Spark Chamber

(not shown)



A charged particle traverses the detector and leaves an ionization trail.

The scintillators trigger an HV pulse between the metal plates and sparks form in the place where the ionization took place.

The Spark Chamber was developed in the early 60ies.

Schwartz, Steinberger and Lederman used it in discovery of the muon neutrino



4. History: Multi Wire Proportional Chambers (not shown)

Tube, Geiger- Müller, 1928



Multi Wire Geometry, in H. Friedmann 1949



G. Charpak 1968, Multi Wire Proportional Chamber, readout of individual wires and proportional mode working point.



5. Proportional Chamber : Single Wire



Electrons produced by ionization drift to the anode wire.

Avalanche:

- Close to the wire (Ø about few tens of μm) the E-field is very large (> 10 kV/cm).
- Between collisions electrons gain enough energy to ionize gas.
- Exponential increase of number of electron/ion pairs (gas amplification)

$$n = n_0 \ e^{\alpha(E)x}$$

a is the first Townsend coefficient.



5. Single Wire Proportional Chamber

ionization mode





5. Single Wire Proportional Chamber



Time for ion signal is very long due to the long drift path. Need to differentiate signal with time constant τ =RC. Avalanche formation happens near the wire within time < 1 ns.

Signal induced on anode and cathode due to moving charges (electrons and ions).

Work to move charge q by dr:

$$dW = lCV_0 \ dV = q \frac{dV(r)}{dr} dr$$
 Induced voltage:
$$dV = \frac{q}{lCV_0} \frac{dV(r)}{dr} dr$$

Total voltage induced in a cylindrical tube (a < r < b) for gas multiplication at distance d from anode, from electrons (V⁻) and ions (V⁺):

$$V^{-} = \frac{-q}{lCV_{0}} \int_{a+d}^{a} \frac{dV(r)}{dr} dr = -\frac{q}{2\pi\epsilon l} \ln\left(\frac{a+d}{a}\right)$$
$$V^{+} = \frac{q}{lCV_{0}} \int_{a+d}^{b} \frac{dV(r)}{dr} dr = -\frac{q}{2\pi\epsilon l} \ln\left(\frac{b}{a+d}\right)$$
$$\text{Ratio:} \quad \frac{V^{-}}{V^{+}} = \frac{\ln[(a+d)/a]}{\ln[b/(a+d)]} < 1\% \qquad \begin{array}{c} \text{for} \\ a=10 \ \mu\text{m} \\ b=10 \ \text{mm} \\ d=1 \ \mu\text{m} \end{array}$$

5. Multi Wire Proportional Chamber (MWPC)



Simple idea to multiply SWPC cell : Nobel Prize 1992

First electronic device allowing high statistics experiments !!

Typical geometry 5mm, 1mm, 20 μm

Normally digital readout : spatial resolution limited to



First large size MWPC



G. Charpak, F. Sauli and J.C. Santiard ,1970

Gregor Herten / 5. Proportional Chamber

from L. Ropelewski

5. MWPC: Two Dimensional Readout



5. MWPC: Typical experimental set up



With this experimental set-up based on MWPC an event rate of about 100 000 Hz can be processed. The position resolution in each layer is about 1 mm.

5. MWPC: Many Wire Planes

MWPC with many wire planes.

1985



5. Cathode Strip Chamber



5. CMS Muon System





Muon Englandie Strip Efficiency

Cosmic Ray At Four Tesla

Average measured efficiencies for each station/ring.



Endcap Muon CSC chambers performed well during cosmics run.





F. Cavallari, Elba 2009

5. Resistive Plate Chamber



5. CMS Muon Barrel RPC Efficiency



The ATLAS Muon Spectrometer

Monitored drift tubes	MDT	
- Coverage	$ \eta < 2.7$ (innermost layer: $ \eta < 2.0$)	
- Number of chambers	1088 (1150)	
- Number of channels	339 000 (354 000)	
- Function	Precision tracking	
Cathode strip chambers	CSC	
- Coverage	$2.0 < \eta < 2.7$	
- Number of chambers	32	
- Number of channels	31 000	
- Function	Precision tracking	
Resistive plate chambers	RPC	
- Coverage	$ \eta < 1.05$	
- Number of chambers	544	
- Number of channels	359 000	
- Function	Triggering, second coordinate	
Thin gap chambers	TGC	
- Coverage	$1.05 < \eta < 2.7$ (2.4 for triggering)	
- Number of chambers	3588	
- Number of channels	318 000	
- Function	Triggering, second coordinate	

A complex system:

4 different technologies (MDT,CSC,RPC,TGC)

Large area (10,000 m²)

Many channels (IM)



The ATLAS Muon Spectrometer

Difficult environment: Large magnetic field variations in toroid.



ATLAS Commissioning with Cosmics



High statistics collected in autumn 2008 (full ATLAS)
Few high statistics runs studied in great detail

- •Subdetectors runs in 2009: RPC runs in January
- •"muon slice" runs at the end of April

5. ATLAS Resistive Plate Chamber Efficiency

Dead strips < 2% Noisy channels < 1%

In 2008 problems with •Synchronzation

•Gas

•Temperature (reduced HV in top sectors) Affected the overall efficiency (70% of trigger coverage)

Most of the problems were fixed during the winter shutdown, current trigger coverage is 95.5%





Access shaft of ATLAS cavern reconstructed in measurement.

5. ATLAS RPC Trigger Coverage



Hit maps of the strips involved in Low and High Pt triggers

• Commisioning ongoing

- Trigger coverage increased from 70% in 2008 to current 95.5% (better timing)
- Full detector for 2009

run.