

Production of Inert Scalars at e^+e^- Linear Colliders

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- 2 Analysis framework
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 - Charged scalar production
 - Neutral scalar production
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Study done with Majid Hashemi, Maria Krawczyk and Saereh Najjari
Presented at “Scalars 2015” conference in Warsaw (December 2015)
[arXiv:1512.01175](https://arxiv.org/abs/1512.01175)

Inert Doublet Model

One of the simplest extensions of the Standard Model (SM).

The scalar sector consists of two doublets:

- Φ_S is the **SM-like Higgs** doublet,
- Φ_D (**inert doublet**) has four additional scalars H, A, H^\pm .

$$\Phi_S = \begin{pmatrix} G^\pm \\ \frac{v+h+iG^0}{\sqrt{2}} \end{pmatrix} \quad \Phi_D = \begin{pmatrix} H^\pm \\ \frac{H+iA}{\sqrt{2}} \end{pmatrix}$$

The most general scalar potential:

$$V(\Phi_S, \Phi_D) = -\frac{1}{2} \left[m_{11}^2 (\Phi_S^\dagger \Phi_S) + m_{22}^2 (\Phi_D^\dagger \Phi_D) \right] + \frac{\lambda_1}{2} (\Phi_S^\dagger \Phi_S)^2 + \frac{\lambda_2}{2} (\Phi_D^\dagger \Phi_D)^2 \\ + \lambda_3 (\Phi_S^\dagger \Phi_S) (\Phi_D^\dagger \Phi_D) + \lambda_4 (\Phi_S^\dagger \Phi_D) (\Phi_D^\dagger \Phi_S) + \frac{\lambda_5}{2} \left[(\Phi_S^\dagger \Phi_D)^2 + (\Phi_D^\dagger \Phi_S)^2 \right]$$

has **seven** parameters ($m_{11,22}, \lambda_{1,2,3,4,5}$) that are assumed to be real.

Inert Doublet Model

Two parameters fixed from Standard Model (ν , M_h)

⇒ 5 new, free parameters: M_H , M_A , M_{H^\pm} + 2 couplings.

We assume a discrete Z_2 symmetry under which

- SM Higgs doublet Φ_S is *even*: $\Phi_S \rightarrow \Phi_S$ (also other SM→SM)
- inert doublet Φ_D is *odd*: $\Phi_D \rightarrow -\Phi_D$.

⇒ Yukawa-type interactions only for Higgs doublet (Φ_S).

The inert doublet (Φ_D) does not interact with the SM fermions!

⇒ The lightest inert particle is stable: a natural candidate for dark matter!
 We assume the neutral scalar H is the dark matter particle.

Inert scalars couplings to γ , W^\pm and Z determined by SM parameters

⇒ well established predictions for production and decay rates!

Constraints on inert scalar masses and couplings

see: [A. Ilnicka, M. Krawczyk, and T. Robens, arXiv:1508.01671](#)

- Theoretical

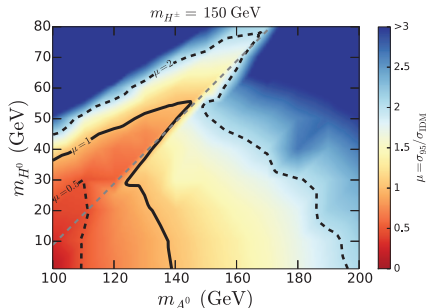
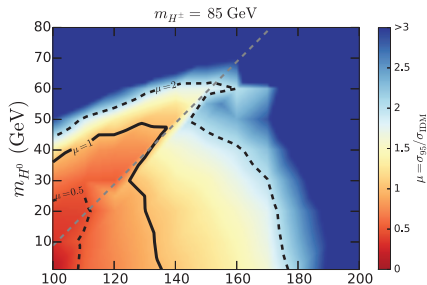
- vacuum stability at tree level
- perturbative unitarity
- global minimum of the potential

- Experimental

- The mass of the SM-like Higgs boson h
- The upper bound on the total width of h
- Total widths of W and Z boson
- A lower bound from LEP on mass of H^\pm
- Exclusion from SUSY searches at LEP and LHC experiments.
- Agreement with electroweak precision observables
- Lower limit on H^\pm width from long-lived charged particle searches
- Direct bound by the dark matter nucleon scattering is by LUX
- Planck limit on relic density

Inert scalars can be pair-produced at LHC via virtual Z or W exchange.
Recasting the results of ATLAS Run I dilepton analyses:

- SUSY-2013-11: Chargino, neutralino and slepton [arXiv:1403.5294]
- HIGG-2013-03: $ZH \rightarrow l^+l^- + \text{inv.}$ [arXiv:1402.3244]



Sabine Kraml, presented at “Scalars 2015”, Warsaw, December 2015
G. Belanger et al., arXiv:1503.07367

Benchmark points (BP) for investigation at LHC Run II [arXiv:1508.01671](https://arxiv.org/abs/1508.01671)

- Benchmark point 1: **low scalar mass**

$$M_H = 57.5 \text{ GeV}, M_A = 113.0 \text{ GeV}, M_{H^\pm} = 123 \text{ GeV}$$

- Benchmark point 2: **low scalar mass**

$$M_H = 85.5 \text{ GeV}, M_A = 111.0 \text{ GeV}, M_{H^\pm} = 140 \text{ GeV}$$

- Benchmark point 3: **intermediate scalar mass**

$$M_H = 128.0 \text{ GeV}, M_A = 134.0 \text{ GeV}, M_{H^\pm} = 176.0 \text{ GeV}$$

- Benchmark point 4: **high scalar mass**, mass degeneracy

$$M_H = 363.0 \text{ GeV}, M_A = 374.0 \text{ GeV}, M_{H^\pm} = 374.0 \text{ GeV}$$

- Benchmark point 5: **high scalar mass**, no mass degeneracy

$$M_H = 311.0 \text{ GeV}, M_A = 415.0 \text{ GeV}, M_{H^\pm} = 447.0 \text{ GeV}$$

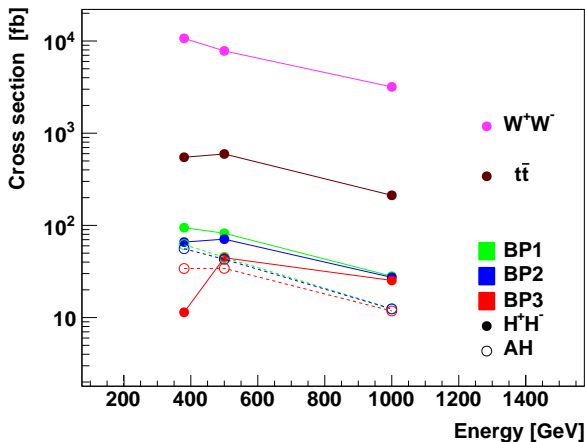
H is DM candidate, A decays always to $Z H$, H^\pm decays mainly to $W^\pm H$

- Signal events generated using CompHEP 4.5.2
 - based on IDM model files prepared using LanHEP 3.2,
 - final state showering and multi-particle interactions in PYTHIA 8.1.53.
- Background events generated with PYTHIA.
- Jet reconstruction with FASTJET 2.4.1
 - anti-kt algorithm with a cone size of 0.4.
- Running scenarios considered
 - $\sqrt{s} = 380, 500, 1000$ GeV
 - luminosity of 500 fb^{-1}
- No simulation of detector effects. Results corrected only for
 - angular acceptance
 - jet energy resolution ($\sigma_E = 50\%/\sqrt{E[\text{GeV}]}$)

CompHEP cross sections for charged and neutral scalar production

$$e^+e^- \rightarrow H^+H^-, \quad e^+e^- \rightarrow AH$$

for three benchmark points considered:

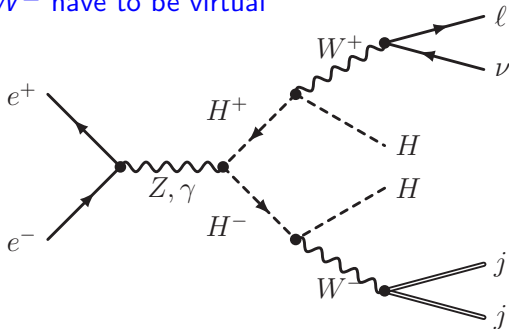


Charged scalar production

For the charged scalar pair production we focus on the decay channel

$$H^\pm \longrightarrow W^{\pm(*)} H$$

For the considered benchmark scenarios $M_{H^\pm} < M_W + M_H$
 \Rightarrow produced W^\pm have to be virtual



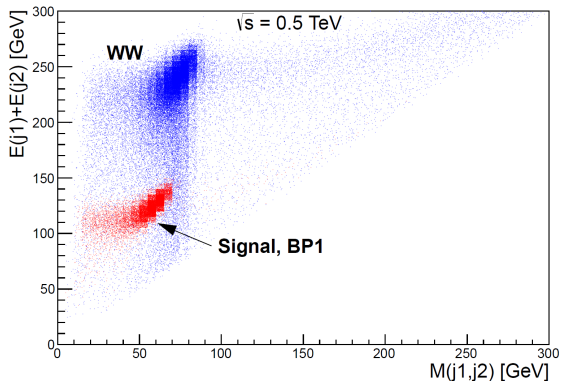
Final state topology depends on the W^\pm decays (as for $t\bar{t}$ events)

Most promising channel: semi-leptonic decay

Charged scalar production

Jet energy sum vs invariant mass distribution for **semi-leptonic channel**:

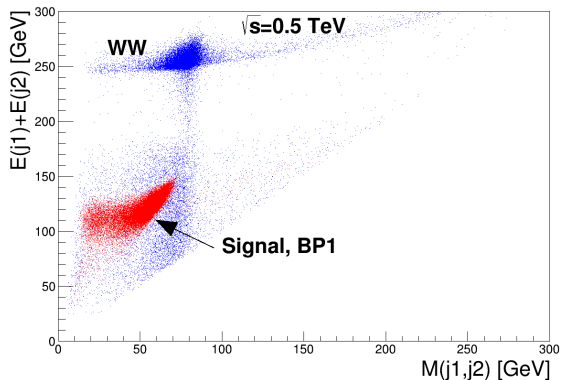
- one lepton ($p_t > 10\text{GeV}$)
- two jets ($E_T > 10\text{GeV}$)
- a missing transverse momentum ($p_T^{\text{miss}} > 20\text{GeV}$)



Charged scalar production

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Dominant W^+W^- background can be further suppressed with cut on missing mass

Plot shown for
 $M_{\text{miss}} > 250\text{GeV}$

Charged scalar production

How to interpret the maximum observed in $E_{j_1} + E_{j_2}$ vs $M_{j_1 j_2}$ distribution

Semi-leptonic channel \Rightarrow two jets come from single off-shell W^\pm decay

- two-jet invariant mass: $M_{j_1 j_2} = M_{W^*}$
- sum of jet energies: $E_{j_1} + E_{j_2} = E_{W^*} = \gamma_{W^*} M_{W^*}$
where γ_{W^*} is the W^* Lorentz boost factor

We expect that W^* production with the highest virtuality is most likely

\Rightarrow expect maximum at $M_{W^*} \approx M_{H^\pm} - M_H$

With maximum virtuality W^* is almost **at rest in the H^\pm reference frame**

\Rightarrow we can approximate W^* boost by that of H^\pm : $\gamma_{W^*} \approx \gamma_{H^\pm}$

Energies of the charged scalars are given by the beam energy

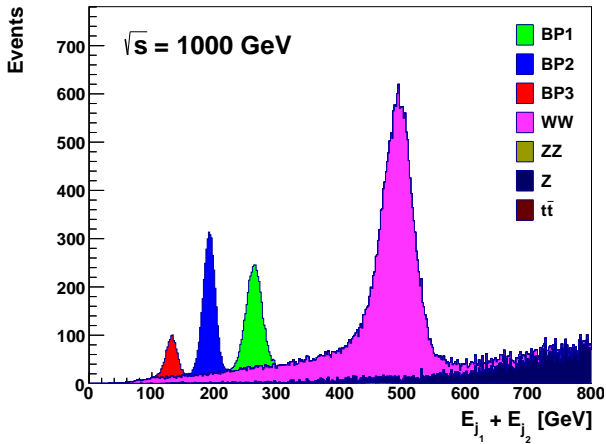
\Rightarrow their Lorentz boost factor: $\gamma_{H^\pm} = E_{beam}/M_{H^\pm}$

Therefore we expect to observe maximum at:

$$M_{j_1 j_2} \approx M_{H^\pm} - M_H \quad E_{j_1} + E_{j_2} = E_{beam} \left(1 - \frac{M_H}{M_{H^\pm}} \right)$$

Charged scalar production

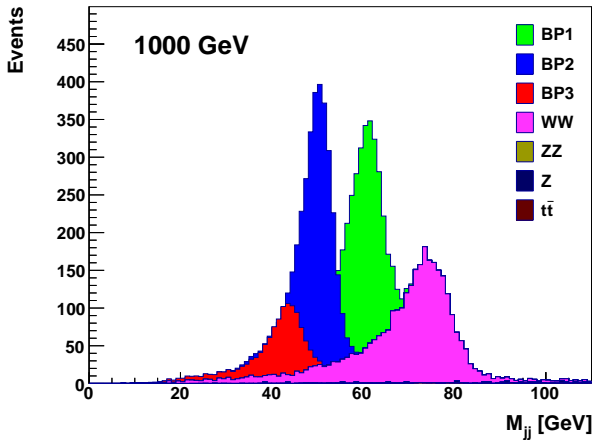
Distribution of the jet energy sum



Clear signal separation for all considered benchmark scenarios

Charged scalar production

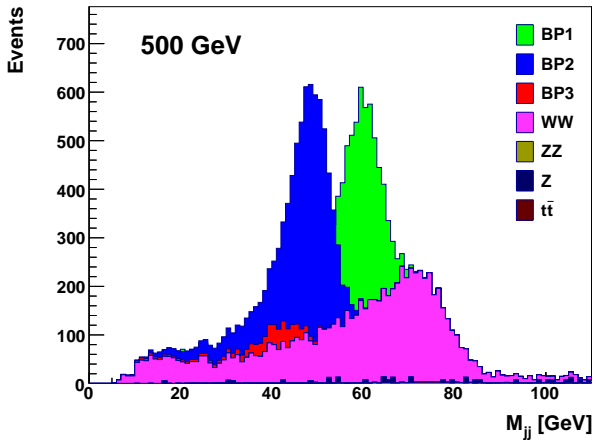
Distribution of the two-jet invariant mass, **after cut on jet energy sum**



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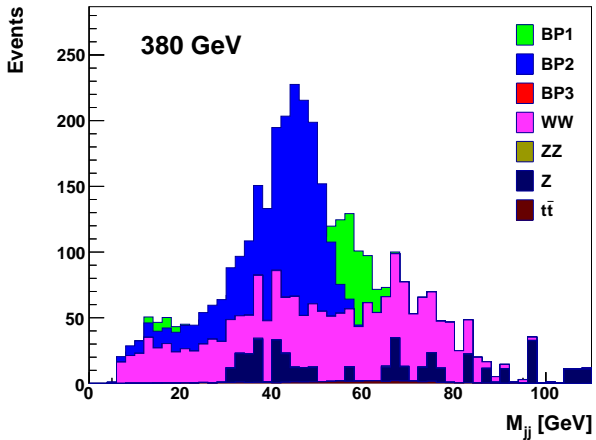
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Clear signal separation for low mass benchmark scenarios

Charged scalar production

Distribution of the two-jet invariant mass, **after cut on jet energy sum**



Clear signal separation for low mass benchmark scenarios

Charged scalar production

Unique kinematic constraints \Rightarrow high signal selection efficiency:

- 12 – 28% for $\sqrt{s}=0.38$ TeV (BP1 and BP2 only)
- 20 – 64% for $\sqrt{s}=0.5$ TeV
- 59 – 86% for $\sqrt{s}=1$ TeV

and good background suppression

\Rightarrow signal to background ratio S/B after mass window cut:

- 1.44 – 3.7 for $\sqrt{s}=0.38$ TeV (BP1 and BP2 only)
- 0.35 – 4 for $\sqrt{s}=0.5$ TeV
- 2.5 – 11 for $\sqrt{s}=1$ TeV

Final statistical significance $S/\sqrt{S+B}$

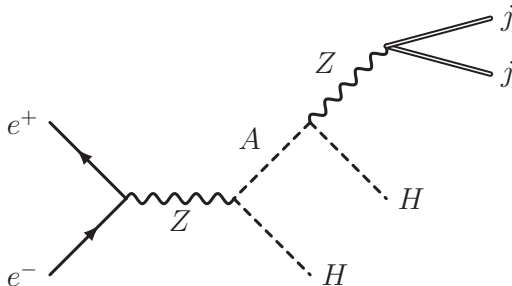
- 25 – 39 for $\sqrt{s}=0.38$ TeV (BP1 and BP2 only)
- 11 – 66 for $\sqrt{s}=0.5$ TeV
- 33 – 87 for $\sqrt{s}=1$ TeV

Neutral scalar production

For the neutral scalar pair production there is only one decay channel:

$$A \longrightarrow Z^* H$$

For the considered benchmark scenarios $M_A < M_Z + M_H$
 \Rightarrow produced Z have to be virtual



Both hadronic and leptonic Z decays can be considered.
 Event statistics much higher in the **hadronic channel**.

Neutral scalar production

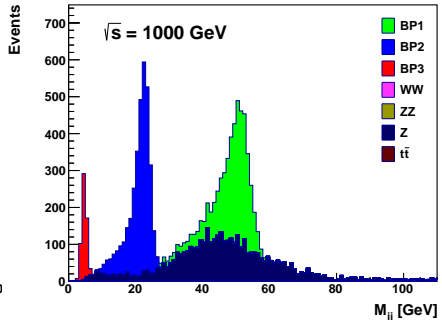
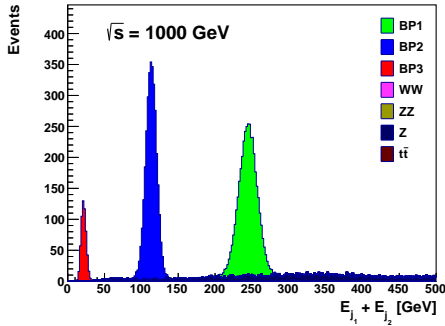
Final state is not symmetric \Rightarrow kinematic relations more complicated

However, we still expect to observe maxima for signal events in

jet energy sum

and

jet invariant mass distributions:



hadronic channel

Neutral scalar production

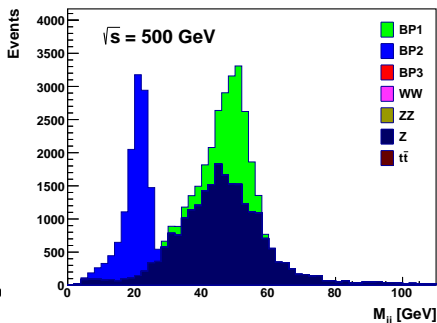
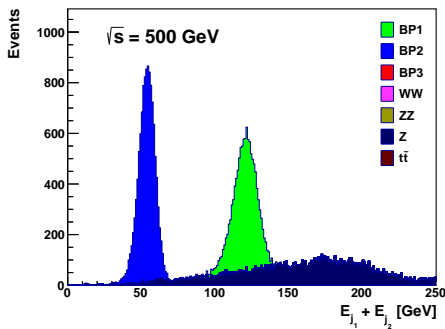
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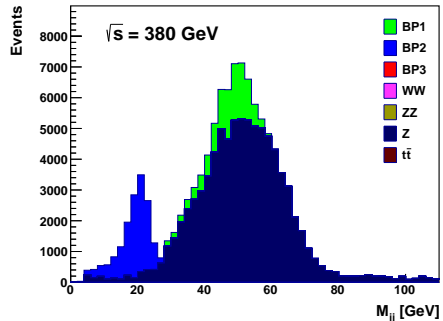
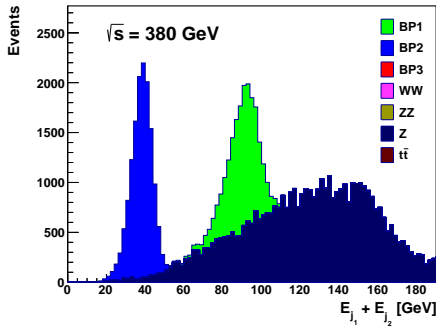
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Clear signal separation for low mass benchmark scenarios

Scalar mass reconstruction

For the charged scalar production $e^+e^- \rightarrow H^+H^-$

- Semi-leptonic channel $e^+e^- \rightarrow l\nu jjHH$
 - two jet invariant mass: $m_{jj} = m_{W^*} \approx m_{H^\pm} - m_H$
 - sum of two jet energies: $E_{jj} = E_{beam} (1 - R)$, where $R = m_H/m_{H^\pm}$
- Fully hadronic channel $e^+e^- \rightarrow jjjjHH$
 As both W^* have the same Lorentz boost, jet with the highest energy (lab) comes from the same W^* as the jet with the lowest energy
 \Rightarrow we can reconstruct both W^* easily
 - two jet invariant masses: $m_{14} = m_{23} = m_{W^*} \approx m_{H^\pm} - m_H$
 - sum of four jet energies: $E_{4j} = 2 E_{beam} (1 - R)$

For the neutral scalar production $e^+e^- \rightarrow HA$

- For leptonic channel $e^+e^- \rightarrow llHH$
 two lepton invariant mass: $m_{ll} = m_{Z^*} \approx m_A - m_H$
- For hadronic channel $e^+e^- \rightarrow jjHH$
 two jet invariant mass: $m_{jj} = m_{Z^*} \approx m_A - m_H$

Expected **statistical precision** of scalar mass determination with 500 fb^{-1}

Scalar	\sqrt{s} [TeV]	BP1	BP2	BP3
m_{H^\pm}	theo.	123	140	176
	0.38	125.85 ± 0.17	136.53 ± 0.25	
	0.5	119.00 ± 0.10	138.43 ± 0.14	170.03 ± 0.38
	1	114.20 ± 0.06	130.45 ± 0.05	164.36 ± 0.23
m_H	theo.	57.5	85.5	128
	0.38	66.70 ± 0.09	92.69 ± 0.17	
	0.5	60.01 ± 0.05	89.78 ± 0.06	129.92 ± 0.30
	1	54.21 ± 0.04	80.72 ± 0.03	121.33 ± 0.17
m_A	theo.	113	111	134
	0.38	121.91 ± 0.10	117.52 ± 0.18	
	0.5	115.02 ± 0.06	114.27 ± 0.07	135.78 ± 0.38
	1	109.02 ± 0.05	105.39 ± 0.04	126.34 ± 0.19

The systematic shifts observed between the assumed (theo.) scalar masses and the fit results are due to the simplified approach used.

Can be corrected for based on the simulation results.

- Inert Doublet Model is one of the simplest extensions of the Standard Model providing a candidate for dark matter.
 - Second scalar doublet is not involved in mass generation and **does not couple to fermions**
 - IDM with inert scalar **masses of the order of M_Z** still in agreement with all existing data

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- LHC signatures similar to some SUSY scenarios, but cross sections small
 - Run 1 limits on m_H extend to ~ 50 GeV only
 - Dedicated **benchmark points** prepared for LHC Run 2
- IDM should be clearly visible at high energy e^+e^- collider for **low and intermediate mass scenarios**
 - Well constrained kinematics allows for efficient selection
 - Scalar masses can be reconstructed with statistical precision of the order of 100 MeV

- Analysis in the current framework
 - Finalize 380 GeV results
 - Consider high mass benchmark points (at 1.5 or 3 TeV)

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- Proceed with detector level analysis