# Vector Boson Scattering at CLIC: Determination of anomalous gauge couplings 

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## Introduction

- Higgs field is responsible for electroweak symmetry breaking $S U(2)_{L} \times U(1)_{Y} \rightarrow U(1)_{e m}$
- Details of symmetry breaking still unknown
- Vector boson scattering is sensitive to new physics in the Higgs sector
- New physics: additional resonances or anomalous couplings


## Effective field theory and anomalous couplings

- $\mathcal{L}_{\text {eff }}=\mathcal{L}_{S M}+\sum_{i} \mathcal{L}_{i}$
- Relevant longitudinal dimension eight operators:

$$
\begin{aligned}
& \mathcal{L}_{S, 0}=F_{S, 0} \operatorname{Tr}\left[\left(\mathbf{D}_{\mu} \mathbf{H}\right)^{\dagger}\left(\mathbf{D}_{\nu} \mathbf{H}\right)\right] \operatorname{Tr}\left[\left(\mathbf{D}^{\mu} \mathbf{H}\right)^{\dagger}\left(\mathbf{D}^{\nu} \mathbf{H}\right)\right] \\
& \mathcal{L}_{S, 1}=F_{S, 1} \operatorname{Tr}\left[\left(\mathbf{D}_{\mu} \mathbf{H}\right)^{\dagger}\left(\mathbf{D}^{\mu} \mathbf{H}\right)\right] \operatorname{Tr}\left[\left(\mathbf{D}_{\nu} \mathbf{H}\right)^{\dagger}\left(\mathbf{D}^{\nu} \mathbf{H}\right)\right]
\end{aligned}
$$

H linear representation of the Higgs field

- Goal: measure couplings $F_{S, 0}$ and $F_{S, 1}$

$$
\mathbf{H} \equiv \frac{1}{2}\left(\begin{array}{cc}
v+h-i w^{3} & -i \sqrt{2} w^{+} \\
-i \sqrt{2} w^{-} & v+h+i w^{3}
\end{array}\right)
$$

## Vector boson scattering



Figure: Feynman diagram for vector boson scattering in a fermion antifermion collision.

## Signal and background processes in VBS



Figure: Feynman diagrams contributing to the vector boson scattering signal.

## Signal and background processes in VBS



Figure: Feynman diagrams contributing to the vector boson scattering signal.


Figure: Feynman diagrams contributing to the irreducible background.

## Signal and background processes in VBS



Figure: Feynman diagrams contributing to the vector boson scattering signal.


Figure: Feynman diagrams contributing to the partially reducible background.

## CLIC

CLIC energy stages and int. luminosities

- $\left(E_{1}=350 / 375 \mathrm{GeV}, \mathcal{L}_{\text {int }, 1}=500 \mathrm{fb}^{-1}\right)$
- $E_{2}=1400 \mathrm{GeV}, \mathcal{L}_{\text {int }, 2}=1500 \mathrm{fb}^{-1}$
- $E_{3}=3000 \mathrm{GeV}, \mathcal{L}_{\text {int }, 3}=2000 \mathrm{fb}^{-1}$


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## Initial state polarization

$e^{-}: 80 \%$
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Low angle coverage m. Idzik: DOI: 10.5506/APhysPolB.46.1297

- LumiCal: 38-110 mrad
- BeamCal: 15-38 mrad


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W and $Z$ identification J. S. Marshall, A. Mnnich, M. A. Thomson: arxiv:1209.4039

- $\approx 88 \%$ (with photon induced bkg.: 71-79 \%)

- Event generator for collider physics
- Matrix element generator O'Mega
- Efficient phase space and event generation
- Current release: 2.2.8 (November 22nd, 2015)


## Total cross sections without cuts

| Process | 1400 GeV | 3000 GeV | Factor |
| :--- | :---: | :---: | :---: |
| $W^{+} W^{-} \nu \bar{\nu}$ | 47.1 | 132 | 1 |
| $W^{+} W^{-} e^{+} e^{-}$ | 1570 | 3820 | 1 |
| $W^{ \pm} Z e^{\mp} \nu$ | 138 | 408 | 0.136 |
| $Z Z e^{+} e^{-}$ | 3.78 | 4.70 | 0.019 |
| $W^{+} W^{-}(Z \rightarrow \nu \bar{\nu})$ | 11.7 | 9.35 | 1 |
| $Z Z \nu \bar{\nu}$ | 15.7 | 57.5 | 1 |
| $Z Z e^{+} e^{-}$ | 3.78 | 4.70 | 1 |
| $W^{ \pm} Z e^{\mp} \nu$ | 138 | 408 | 0.136 |
| $W^{+} W^{-} e^{+} e^{-}$ | 1570 | 3820 | 0.019 |
| $Z Z(Z \rightarrow \nu \bar{\nu})$ | 0.484 | 0.237 | 1 |

Table: Total cross sections in fb without cuts (error $\approx 1 \%$ ).

## Differential cross sections



Figure: Differential cross sections depending on the transverse momentum of the $W$ boson pair at $\sqrt{s}=3000 \mathrm{GeV}$.

## Used cuts

(1) $M_{\text {inv }}(\bar{\nu} \nu)>230(175) \mathrm{GeV}$ (neutrinos originate from Z decay, backgrounds from $W^{+} W^{-}$and QCD four-jet production)
(2) $|\cos \theta(W / Z)|<0.8$ and $p_{\perp}(W / Z)>300(180) \mathrm{GeV}$ (backgrounds which result from t-channel exchange in the subprocess)
(3) $\theta(e)>15 \mathrm{mrad}$ and $p_{\perp}(W W)>100(50) \mathrm{GeV}, p_{\perp}(Z Z)>60(40) \mathrm{GeV}$ (background resulting from $\gamma \gamma$ fusion)
(9) $900(800) \mathrm{GeV}<M_{\text {inv }}(W W)<1900(1175) \mathrm{GeV}$, 850(800) $\mathrm{GeV}<M_{\text {inv }}(Z Z)<1900(1175) \mathrm{GeV}$ (non scattered vector bosons)

## Cross sections with cuts

| Process | 1400 GeV | 3000 GeV | Factor |
| :--- | :---: | :---: | :---: |
| $W^{+} W^{-} \nu \bar{\nu}$ | 0.119 | 0.790 | 1 |
| $W^{+} W^{-} e^{+} e^{-}$ | 0.000 | 0.000 | 1 |
| $W^{ \pm} Z e^{\mp} \nu$ | 0.269 | 1.200 | 0.136 |
| $Z Z e^{+} e^{-}$ | 0.000 | 0.000 | 0.019 |
| $W^{+} W^{-}(Z \rightarrow \nu \bar{\nu})$ | 0.039 | 0.610 | 1 |
| $Z Z \nu \bar{\nu}$ | 0.084 | 0.790 | 1 |
| $Z Z e^{+} e^{-}$ | 0.000 | 0.000 | 1 |
| $W^{ \pm} Z e^{\mp} \nu$ | 0.288 | 1.593 | 0.136 |
| $W^{+} W^{-} e^{+} e^{-}$ | 0.000 | 0.000 | 0.019 |
| $Z Z(Z \rightarrow \nu \bar{\nu})$ | 0.000 | 0.000 | 1 |

Table: Total cross sections in fb with cuts (error $\approx 1 \%$ ).

## Cross sections at 1400 GeV



Figure: Total cross sections of $e^{+} e^{-} \rightarrow W^{+} W^{-} \nu \bar{\nu}$ depending on $F_{S, 0}$ and $F_{S, 1}$ at $\sqrt{s}=1400 \mathrm{GeV}$ without unitarization.

## Exclusion contours and exclusion sensitivities at 1400 GeV



Figure: $\pm 1 \sigma$ exclusion contours and $90 \%$ exclusion sensitivity in the $F_{S, 0} / F_{S, 1}$ plane at $\sqrt{s}=1400 \mathrm{GeV}$ without unitarization.

## Exclusion contours and exclusion sensitivities at 1400 GeV


$\Rightarrow 90 \%$ exclusion sensitivity $\approx 30-40 \mathrm{TeV}^{-4}$

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## Exclusion contours and exclusion sensitivities at 3000 GeV



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## Exclusion contours and exclusion sensitivities at 3000 GeV


$\Rightarrow 90 \%$ exclusion sensitivity $\approx 5-7 \mathrm{TeV}^{-4}$

Figure: $\pm 1 \sigma$ exclusion contours and $90 \%$ exclusion sensitivity in the $F_{S, 0} / F_{S, 1}$ plane at $\sqrt{s}=3000 \mathrm{GeV}$ with unitarization.

## Actual values

## Theoretical CLIC values

$-40 \mathrm{TeV}^{-4}<F_{S, 0,1}<40 \mathrm{TeV}^{-4}(1400 \mathrm{GeV})$
$-7 \mathrm{TeV}^{-4}<F_{S, 0,1}<7 \mathrm{TeV}^{-4}(3000 \mathrm{GeV})$
Latest ATLAS analysis c. Aad et al:: arxiv: 1405.6241
$-461 \mathrm{TeV}^{-4}<F_{S, 0}<527 \mathrm{TeV}^{-4}$
$-758 \mathrm{TeV}^{-4}<F_{S, 1}<791 \mathrm{TeV}^{-4}$

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$\Rightarrow$ CLIC values up to $15 \times(90 x)$ better
Max. photon induced bkg.: exclusion sensitivities worsen $\approx 15-20 \%$

## Conclusion

- CLIC offers great possibilities for measuring anomalous gauge couplings.
- Exclusion sensitivities can be enhanced.
- Measurements are complementary to the LHC measurements.
- Especially BeamCal and LumiCal detectors important to reduce background.


## Outlook

## Relevant Operators:



- $\mathcal{L}_{S, 0}=F_{S, 0} \operatorname{Tr}\left[\left(\mathbf{D}_{\mu} \mathbf{H}\right)^{\dagger}\left(\mathbf{D}_{\nu} \mathbf{H}\right)\right] \operatorname{Tr}\left[\left(\mathbf{D}^{\mu} \mathbf{H}\right)^{\dagger}\left(\mathbf{D}^{\nu} \mathbf{H}\right)\right]$
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Figure: Scattering
of longitudi-
nal/transverse vector bosons.

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- $\mathcal{L}_{M, 0}=-g^{2} F_{M, 0} \operatorname{Tr}\left[\left(\mathbf{D}_{\mu} \mathbf{H}\right)^{\dagger}\left(\mathbf{D}^{\mu} \mathbf{H}\right)\right] \operatorname{Tr}\left[\mathbf{W}_{\nu \rho} \mathbf{W}^{\nu \rho}\right]$
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Figure: Scattering of longitudinal/transverse vector bosons.

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- $\mathcal{L}_{T, 0}=g^{4} F_{T, 0} \operatorname{Tr}\left[\mathbf{W}_{\mu \nu} \mathbf{W}^{\mu \nu}\right] \operatorname{Tr}\left[\mathbf{W}_{\alpha \beta} \mathbf{W}^{\alpha \beta}\right]$
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- $\mathcal{L}_{T, 2}=g^{4} F_{T, 2} \operatorname{Tr}\left[\mathbf{W}_{\alpha \mu} \mathbf{W}^{\mu \beta}\right] \operatorname{Tr}\left[\mathbf{W}_{\beta \nu} \mathbf{W}^{\nu \alpha}\right]$

Figure: Scattering of longitudinal/transverse vector bosons.

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Unitarization done, now: Implementation in WHIZARD.

## Backup Slides

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## Vector boson scattering



Figure: Feynman diagrams for elastic vector boson scattering with four-point-interaction or a vector boson propagator.

## Vector boson scattering





Figure: Feynman diagrams for elastic vector boson scattering with four-point-interaction or a vector boson propagator.


Figure: Feynman diagrams for elastic vector boson scattering with a Higgs propagator.

## Differential cross sections



Figure: Differential cross section depending on the $W$ boson pair recoil mass at $\sqrt{s}=3000 \mathrm{GeV}$.

## Differential cross sections



Figure: Differential cross sections depending on the invariant mass of the $W$ boson pair at $\sqrt{s}=3000 \mathrm{GeV}$.

## Cross sections at 1400 GeV



Figure: Total cross sections of $e^{+} e^{-} \rightarrow Z Z \nu \bar{\nu}$ depending on $F_{S, 0}$ and $F_{S, 1}$ at $\sqrt{s}=1400 \mathrm{GeV}$ without unitarization.

## Cross sections at 3000 GeV



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