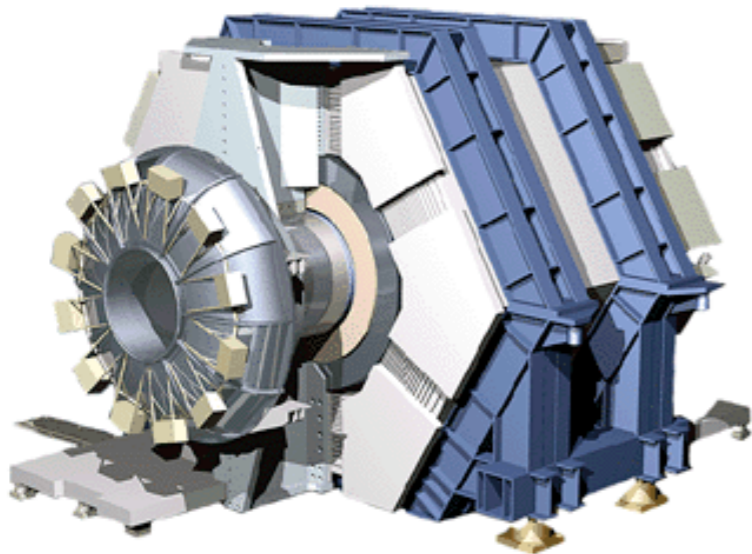


# SemiLeptonic B decays at BaBar

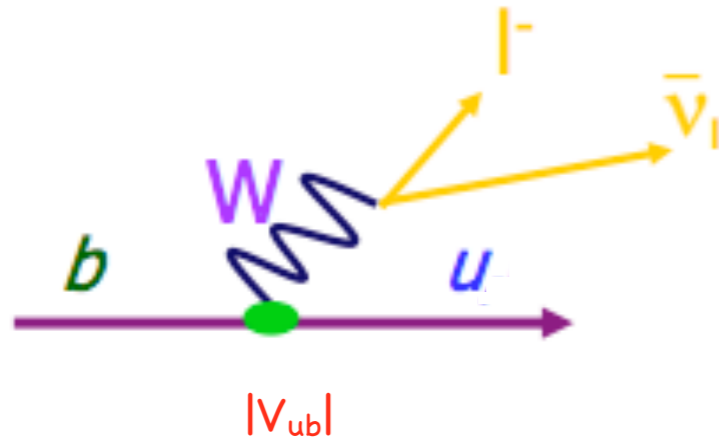
Roberto Sacco

BaBar Symposium, April 1st 2009, London



Queen Mary  
University of London

# The CKM matrix



In the SM, mixing between quark generations is modeled with the CKM matrix

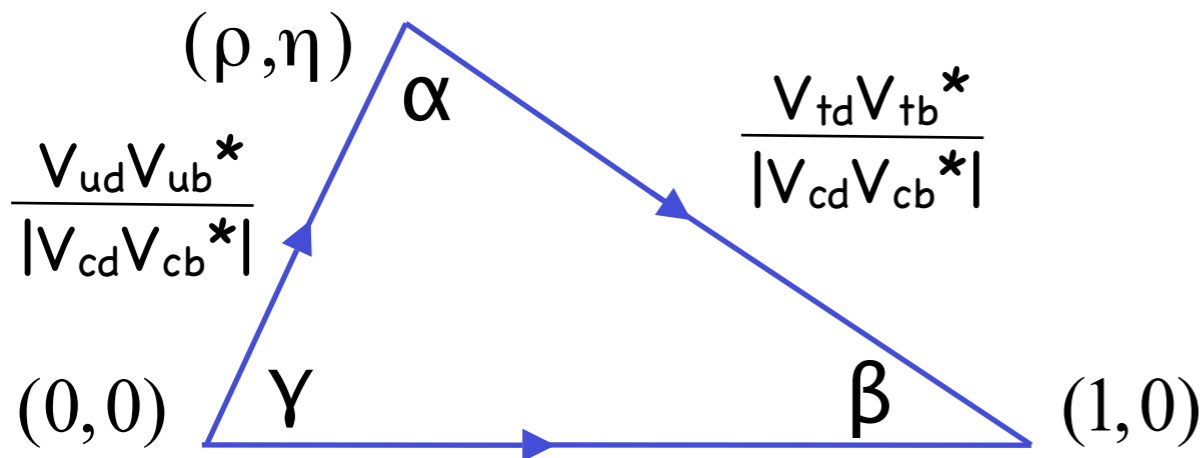
$$\mathbf{V} = \begin{vmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{vmatrix} = \begin{vmatrix} 1 - \lambda^2/2 & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \lambda^2/2 & A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{vmatrix} + O(\lambda^4)$$

CP violation comes from the presence of phase factors in some of the  $V$ 's, a non-vanishing value of  $\eta$

Unitarity of the CKM matrix implies relations such as

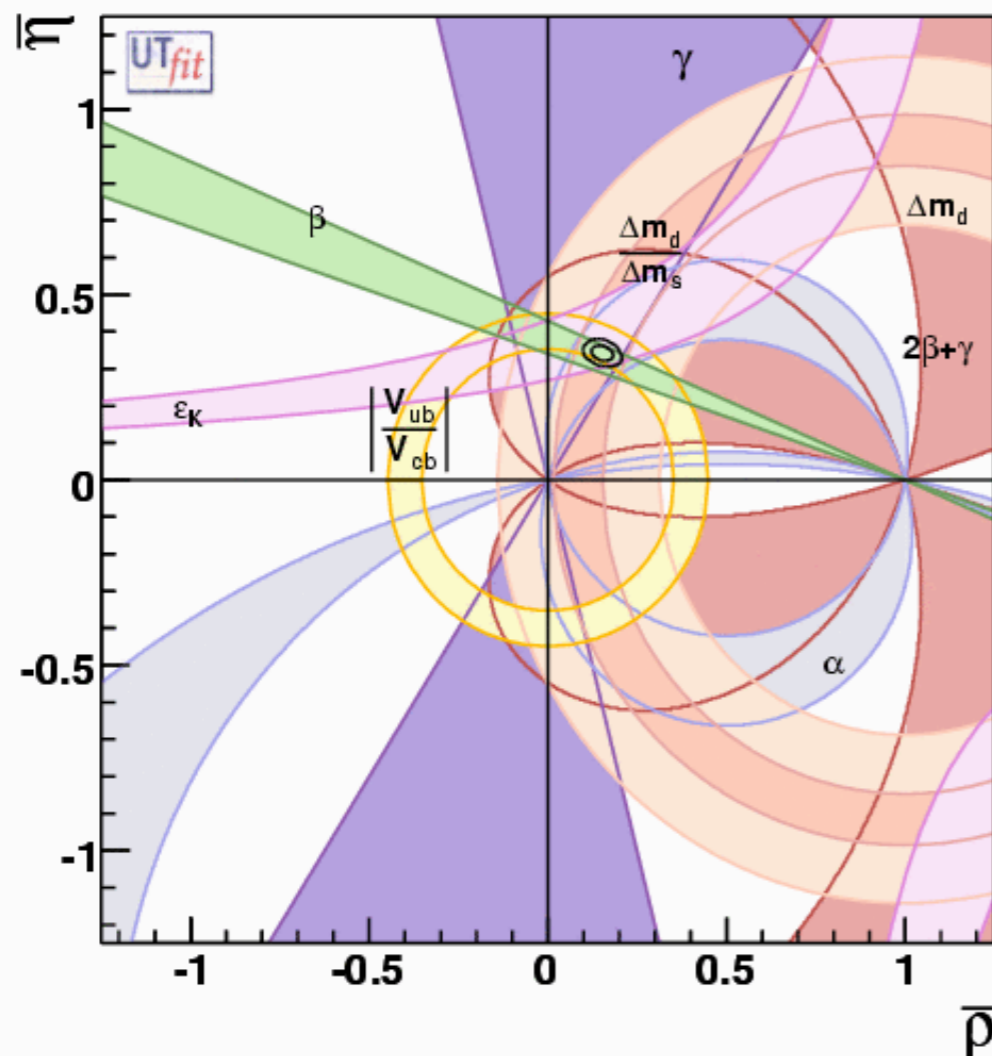
$$V_{ud}V_{ub}^* + V_{cd}V_{cb}^* + V_{td}V_{tb}^* = 0 \quad \text{Unitarity Triangle}$$

# The Unitarity Triangle



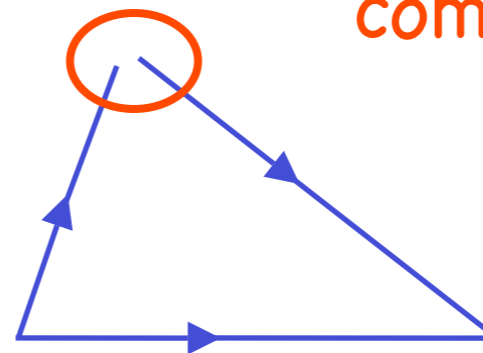
We measure angles and sides

Within errors, agreement with SM predictions



Is there room for **new physics**?  
Need to overconstrain the UT

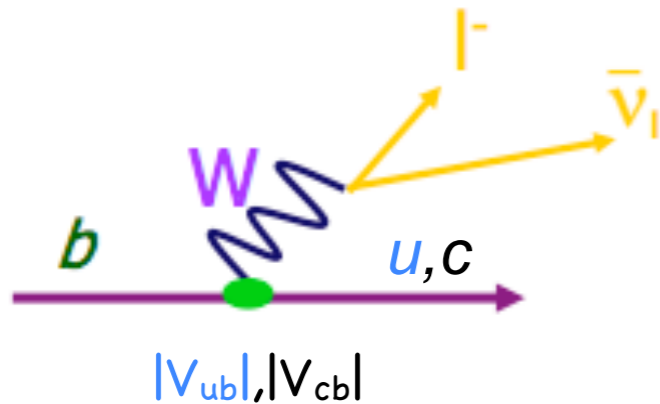
Measurement of  $|V_{ub}|/|V_{cb}|$   
**complementary to  $\sin 2\beta$**



Do they agree with each other?

# Semileptonic B Decays

Semileptonic B decays give us a clear view of the b quark inside the B meson



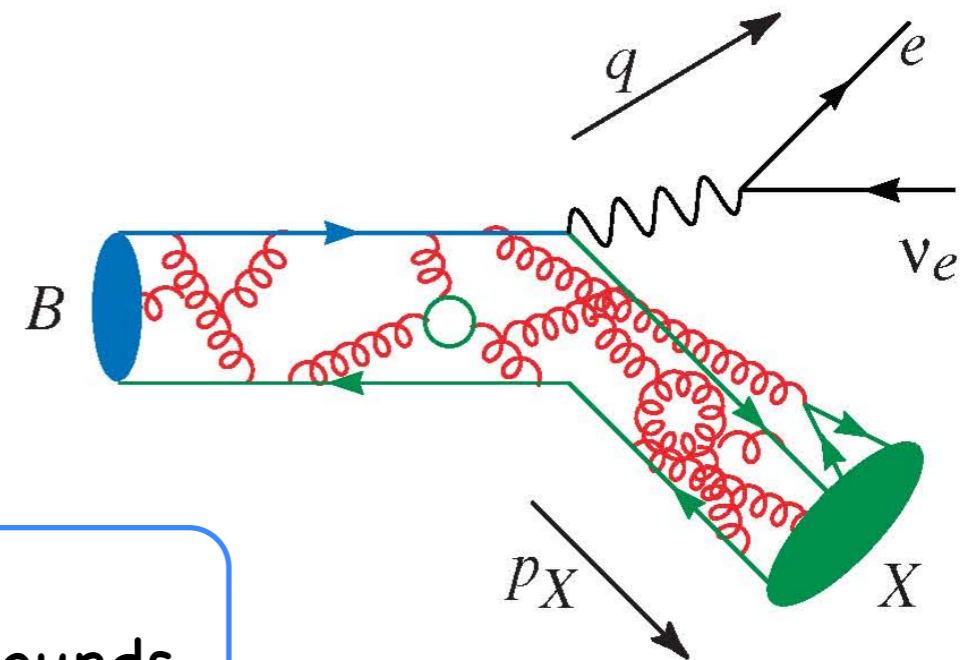
- ⇒ decay rate depends on  $|V_{ub}|$  and  $|V_{cb}|$
- ⇒ Leptonic and hadronic currents can be disentangled
- ⇒ **Tree level decays** ⇒ independent of new physics

## Inclusive decays

Large signal rate, high backgrounds

Total rate calculated with HQE

Need to account for **non perturbative QCD** effects!



## Exclusive decays

Lower signal rate, lower backgrounds

Need **Form Factors** to describe the hadronization process

# A bit of history...

1 graduate student lifetime ago (~20 years)  
we didn't know that  $|V_{ub}| \neq 0$

Experimental status in 1999:

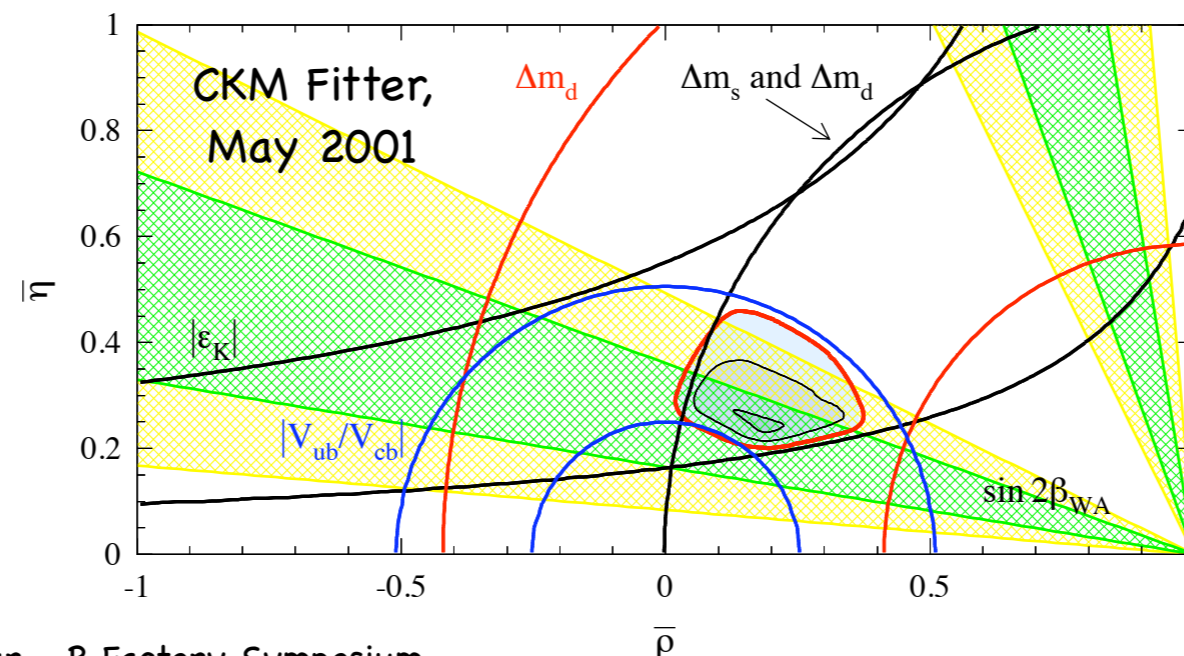
$$|V_{cb}| = 0.0402 \pm 0.0019$$

(combining all LEP data for both inclusive and exclusive decays)

$$|V_{ub}/V_{cb}| = 0.090 \pm 0.025$$

(from CLEO, LEP and assuming conservative  
theoretical uncertainties)

PDG 1999



# A bit of history... $|V_{cb}|$

From the BaBar workbook:

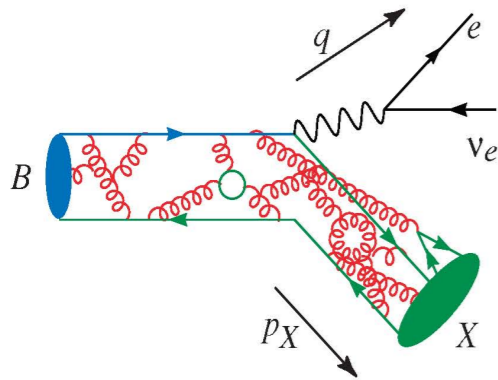
Large data sets will be obtained at BaBar that can be used for the determination of  $|V_{cb}|$  and  $|V_{ub}|$ . With  $30 \text{ fb}^{-1}$ , the experimental errors on  $|V_{cb}|$  are estimated to be  $\pm 0.0006$  (1.5%) and  $\pm 0.0004$  (1.0%) from exclusive  $B \rightarrow D^* \ell \nu$  and inclusive  $B \rightarrow \ell \nu X$  decays, respectively. The theoretical uncertainties are of comparable size for both methods and are of the order of a few percent. If the two results agree, a realistic estimate of the combined theoretical uncertainty is  $\pm 0.0012$  (3%), leading to a BaBar result of

$$|V_{cb}| = \dots \pm 0.0004 \pm 0.0012 (\pm 1\% \pm 3\%) \quad (8.63)$$

after a few years of running, where the first error is experimental (statistical and systematic) and the second is from theory. The estimate of the theoretical uncertainty is based on present theoretical tools. A decrease in this uncertainty to a level of 1% will require new theoretical ideas.

**HQET/OPE approaches** were being studied among many difficulties - the extraction of HQET parameters from the analysis of mass and lepton energy moments did not give consistent results

# HQE parameters determination



fit to hadronic  
mass moments in  
 $B \rightarrow X_c l \nu$

fit to lepton  
energy moments in  
 $B \rightarrow X_c l \nu$

$$\Gamma_{cl\nu} = \frac{G_F m_b^5}{192\pi^3} |V_{cb}|^2 (1 + A_{ew}) A_{\text{pert}} A_{\text{nonpert}} \simeq |V_{cb}|^2 f_{\text{OPE}}(m_b, m_c, a_i)$$

fit to photon  
energy moments in  
 $B \rightarrow X_s \gamma$

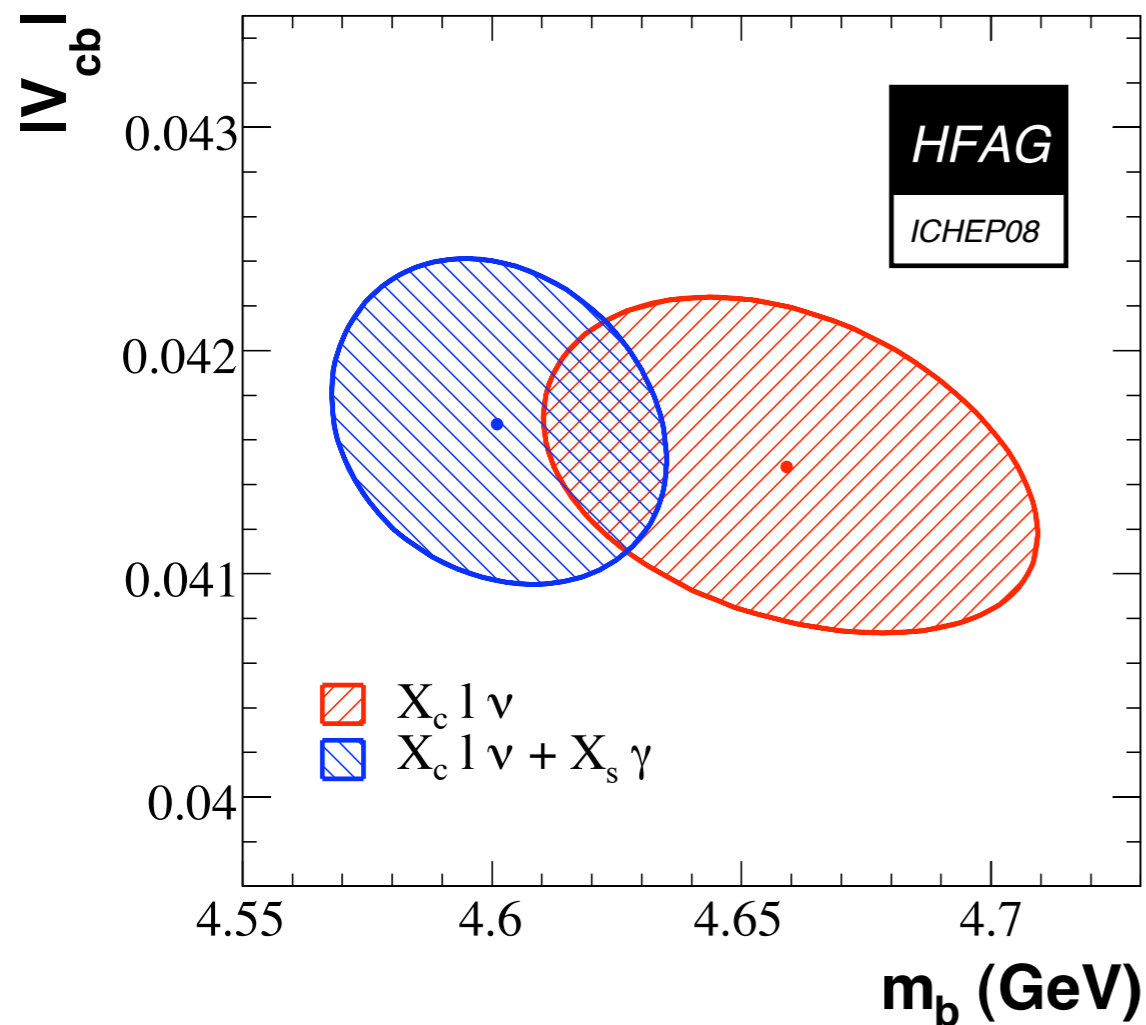
## Kinetic Scheme

P. Gambino and N.Uraltsev, Eur. Phys.  
J. C34, 181 (2004)

## 1S Scheme

C.Bauer, Z.Ligeti, M.Luke, A.Manohar,  
M.Trott PRD 70 094017 (2004)

# Inclusive $|V_{cb}|$ determination



$$|V_{cb}| = (41.67 \pm 0.43_{\text{fit}} \pm 0.08_{\text{TB}} \pm 0.58_{\text{th}}) 10^{-3}$$

$$m_b = 4.601 \pm 0.034$$

$$m_c = 1.165 \pm 0.050$$

$$\mu_\pi^2 = 0.440 \pm 0.040$$

$$|V_{cb}| = (41.48 \pm 0.47_{\text{fit}} \pm 0.08_{\text{TB}} \pm 0.58_{\text{th}}) 10^{-3}$$

$$m_b = 4.659 \pm 0.049$$

$$m_c = 1.285 \pm 0.078$$

$$\mu_\pi^2 = 0.428 \pm 0.044$$

Using  $\sim 60$  moments, fitting 7 parameters

1.7% total error

work in progress to estimate theoretical correlations used in the fit

may shift  $|V_{cb}|$  value closer to exclusive determination



# Exclusive $|V_{cb}|$ determination

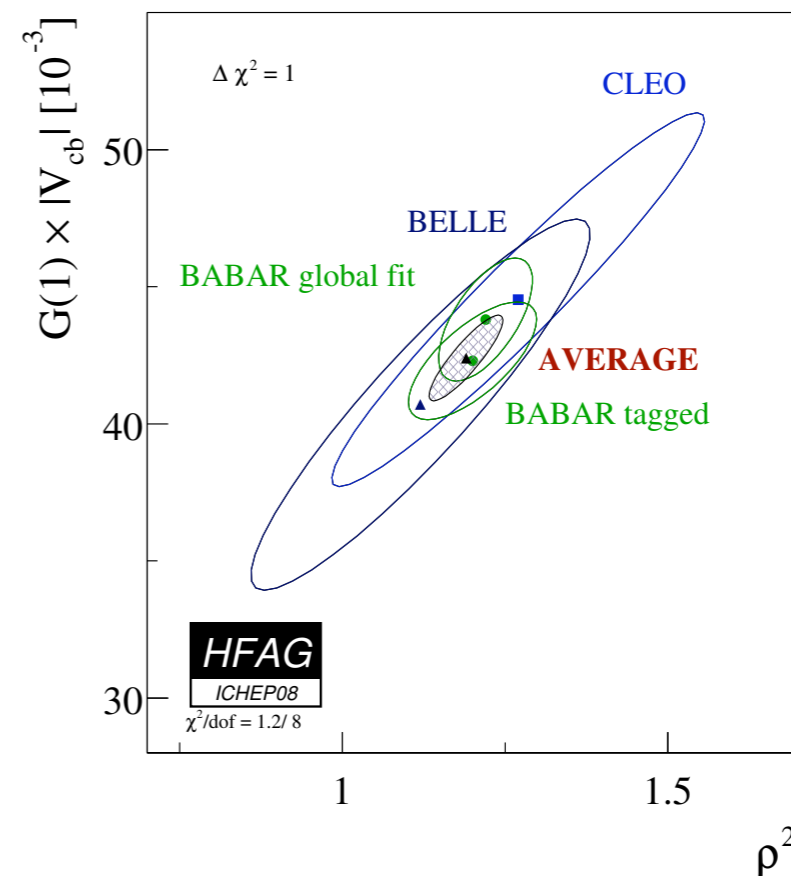
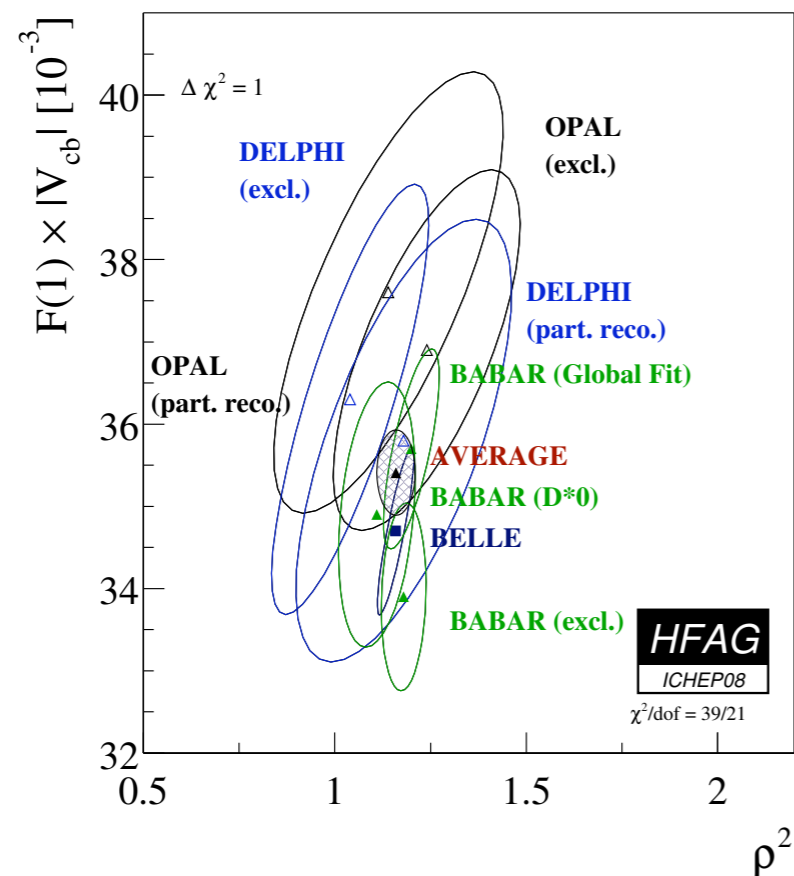
BaBar has recently measured  $|V_{cb}|$  and FF parameters

$F(1)|V_{cb}|$  and  $\rho_F^2$  from untagged  $B \rightarrow D^{*0} \ell \nu$

$G(1)|V_{cb}|$  and  $\rho_G^2$  from tagged  $B \rightarrow D \ell \nu$

$F(1)|V_{cb}|$ ,  $\rho_F^2$ ,  $G(1)|V_{cb}|$  and  $\rho_G^2$  from  $B \rightarrow D^{*0} \ell \nu X$

All the B factories measurements provide precise and consistent results both for  $|V_{cb}|$  and FF parameters



Using Unquenched LQCD calculations:

$$|V_{cb}| = (38.1 \pm 0.6_{\text{exp}} \pm 0.9_{\text{th}}) 10^{-3} (D^*)$$

$$|V_{cb}| = (39.7 \pm 1.4_{\text{exp}} \pm 0.9_{\text{th}}) 10^{-3} (D)$$

# A bit of history... $|V_{ub}|$

Again, from the BaBar workbook:

For  $|V_{ub}|$ , expectations are more modest. With 30 events/fb, BaBar will be able to determine the decay fractions of  $B \rightarrow \pi l \nu$ ,  $B \rightarrow \rho l \nu$ , and  $B \rightarrow \omega l \nu$  with statistical errors around 6%, giving  $|V_{ub}|$  with statistical errors around 3%. Systematic errors should be of the same order, and averaging the three decay modes leads to an estimate of  $\pm 2.5\%$  for the experimental error on  $|V_{ub}|$ . Inclusive decays will not reach the same precision experimentally. They will, however, be extremely important because they have completely different theoretical uncertainties. These are estimated to be about 10% for both methods, based on present theoretical technology. Thus, BaBar could reach

$$|V_{ub}| = \dots \pm 0.0001 \pm 0.0004 (\pm 2.5\% \pm 10\%) \quad (8.64)$$

after a few years of running. Again, new theoretical approaches could decrease the theoretical uncertainties to a level of 5%.

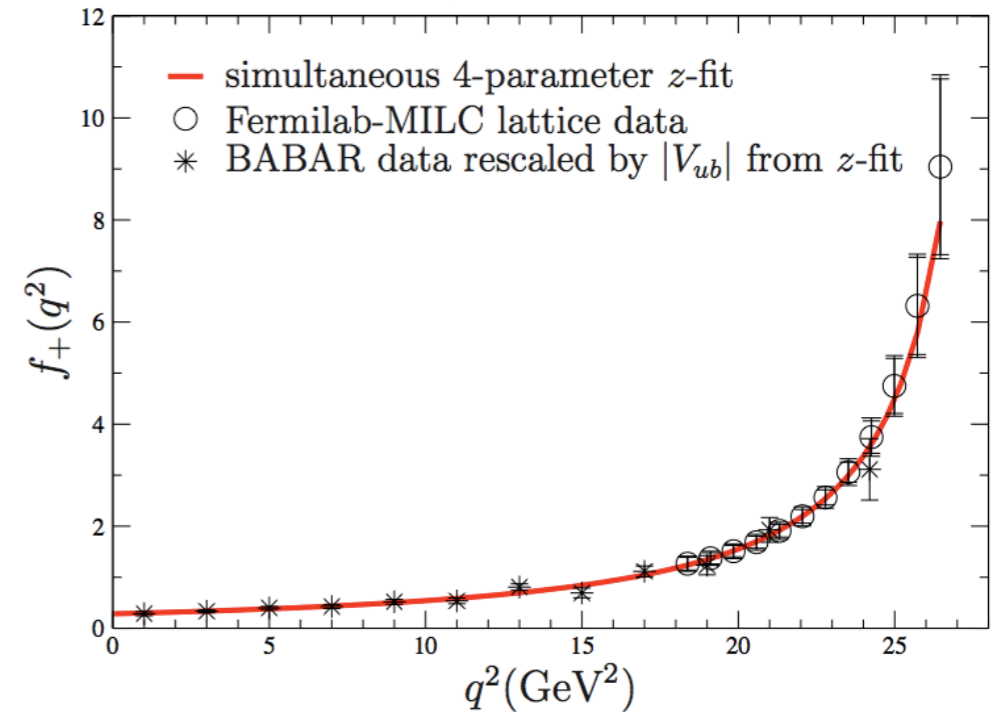
# $|V_{ub}|$ in exclusive B decays

New result from FNAL/MILC collaboration:

$$|V_{ub}| = (3.38 \pm 0.36) 10^{-3}$$

arXiv:0811.3640v3 [hep-lat] (2009)

$\chi^2/\text{d.o.f.} = 0.59$



BABAR SL tag:  $B^+ \rightarrow \pi^0 l^+ \nu \times 2\tau_0/\tau_+$

$$1.81 \pm 0.28 \pm 0.13$$

BABAR  $B_{\text{reco}}$  tag:  $B^+ \rightarrow \pi^0 l^+ \nu \times 2\tau_0/\tau_+$

$$1.54 \pm 0.41 \pm 0.21$$

BELLE SL tag:  $B^+ \rightarrow \pi^0 l^+ \nu \times 2\tau_0/\tau_+$

$$1.45 \pm 0.26 \pm 0.15$$

BELLE  $B_{\text{reco}}$  tag:  $B^+ \rightarrow \pi^0 l^+ \nu \times 2\tau_0/\tau_+$

$$1.24 \pm 0.23 \pm 0.06$$

BABAR SL tag:  $B^0 \rightarrow \pi^- l^+ \nu$

$$1.38 \pm 0.21 \pm 0.07$$

BELLE SL tag:  $B^0 \rightarrow \pi^- l^+ \nu$

$$1.38 \pm 0.19 \pm 0.14$$

BABAR  $B_{\text{reco}}$  tag:  $B^0 \rightarrow \pi^- l^+ \nu$

$$1.07 \pm 0.27 \pm 0.15$$

CLEO untagged:  $B \rightarrow \pi l^+ \nu$

$$1.37 \pm 0.15 \pm 0.11$$

BABAR untagged:  $B \rightarrow \pi l^+ \nu$

$$1.46 \pm 0.07 \pm 0.08$$

BELLE  $B_{\text{reco}}$  tag:  $B^0 \rightarrow \pi^- l^+ \nu$

$$1.12 \pm 0.18 \pm 0.05$$

Average:  $B^0 \rightarrow \pi^- l^+ \nu$

$$1.34 \pm 0.06 \pm 0.05$$

$\chi^2/\text{dof} = 3.5/9$  (CL = 94 %)

HFAG  
ICHEP08

$B(B^0 \rightarrow \pi^- l^+ \nu) [\times 10^{-4}]$

227M BB

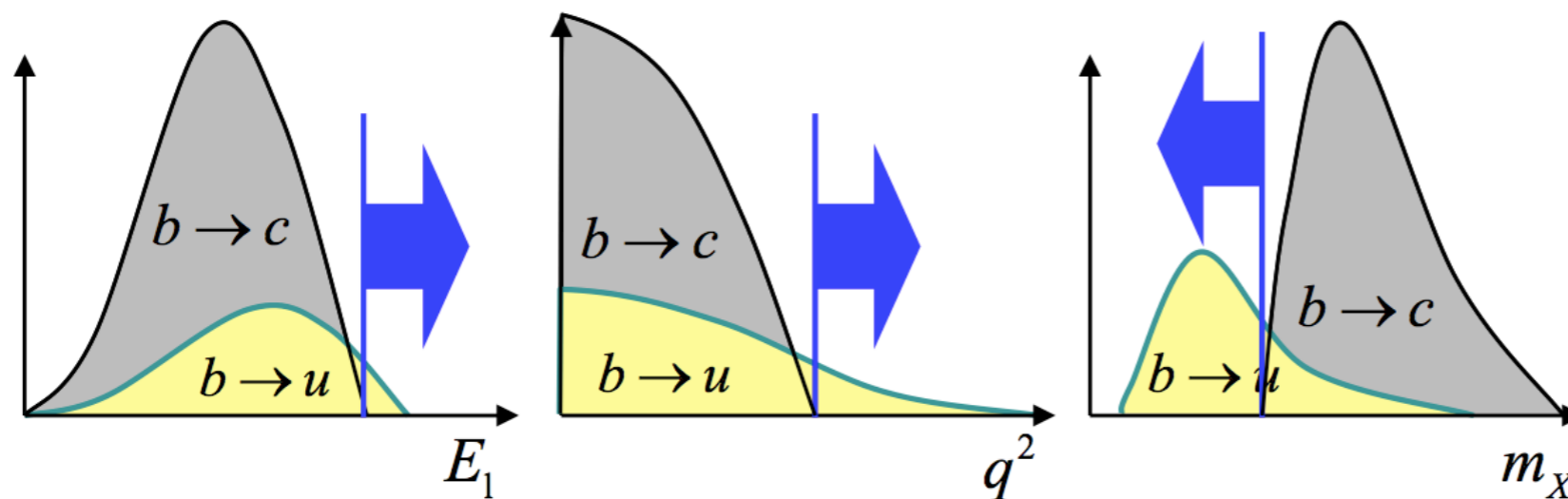
4.8% statistical  
5.5% systematic

Work in progress: new BaBar analyses on  $B \rightarrow \pi/\rho/\omega/\eta/\eta' l \nu$

# $|V_{ub}|$ in inclusive B decays

$$|V_{ub}| = \sqrt{\frac{\Delta\mathcal{B}(\bar{B} \rightarrow X_u \ell \bar{\nu})}{\tau_B \Delta\zeta}}$$

$|V_{ub}|$  is proportional to  
 $B \rightarrow X_u \ell \nu$  branching fraction  
 in limited region of phase space



$E_l$  = lepton energy  
 $q^2$  = dilepton mass squared  
 $m_X$  = hadron system mass

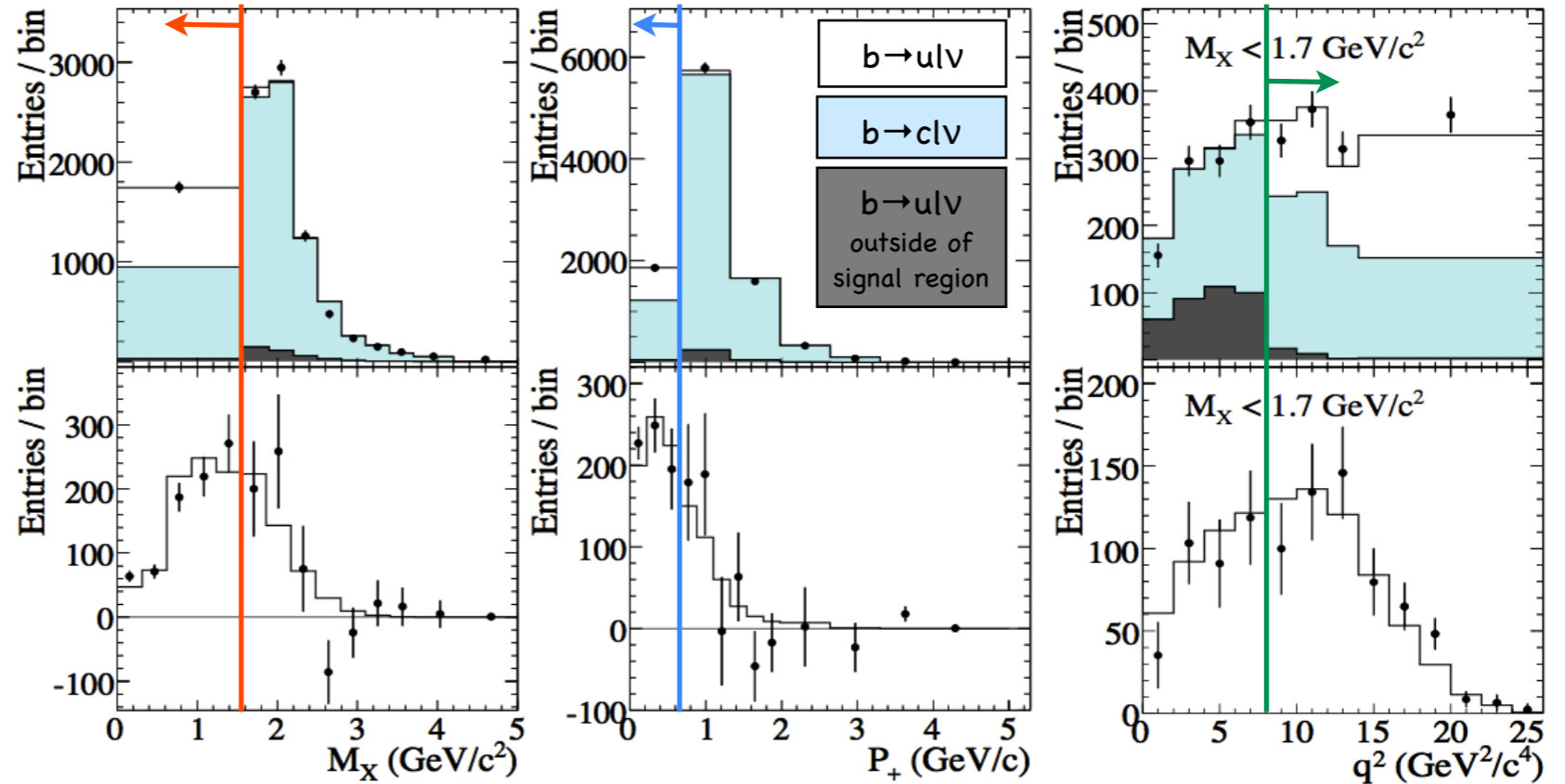
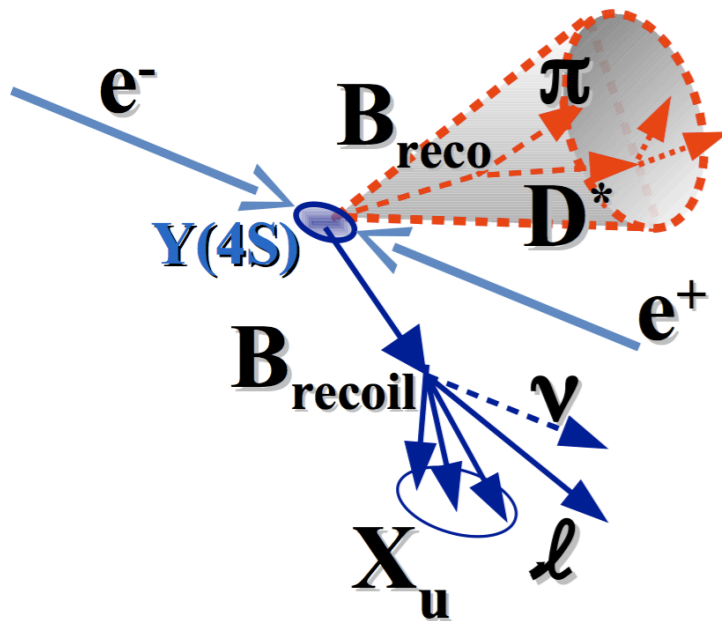
In these regions the **theory (OPE) breaks down**, acceptance sensitive to **Fermi motion** of b quark inside B meson

$\Rightarrow$  **smart choice of phase space**

$\Rightarrow$  **non perturbative QCD computation**, where the effects of the Fermi motion need to be taken into account  
 Several theoretical frameworks address this problem, many advances in recent years

# $|V_{ub}|$ in inclusive B decays

383M BB: PRL 100, 171802 (2008)



Signal regions:

$$m_X < 1.55 \text{ GeV}/c^2$$

$$P_+ = E_X - P_X < 0.66 \text{ GeV}/c$$

$$m_X < 1.7 \text{ GeV}/c^2, \quad q^2 > 8 \text{ GeV}^2/c^4$$

$m_X$

$$|V_{ub}| = (4.27 \pm 0.16_{\text{stat}} \pm 0.13_{\text{syst}} \pm 0.30_{\text{th}}) 10^{-3}$$

BLNP, PRL93, 221801 (2004)

$$|V_{ub}| = (4.56 \pm 0.17_{\text{stat}} \pm 0.14_{\text{syst}} \pm 0.32_{\text{th}}) 10^{-3}$$

DGE, JHEP0601, 097 (2006)

$P_+$

$$|V_{ub}| = (3.88 \pm 0.19_{\text{stat}} \pm 0.16_{\text{syst}} \pm 0.28_{\text{th}}) 10^{-3}$$

BLNP

$$|V_{ub}| = (3.99 \pm 0.20_{\text{stat}} \pm 0.16_{\text{syst}} \pm 0.24_{\text{th}}) 10^{-3}$$

DGE

$m_X, q^2$

$$|V_{ub}| = (4.57 \pm 0.22_{\text{stat}} \pm 0.19_{\text{syst}} \pm 0.30_{\text{th}}) 10^{-3}$$

BLNP

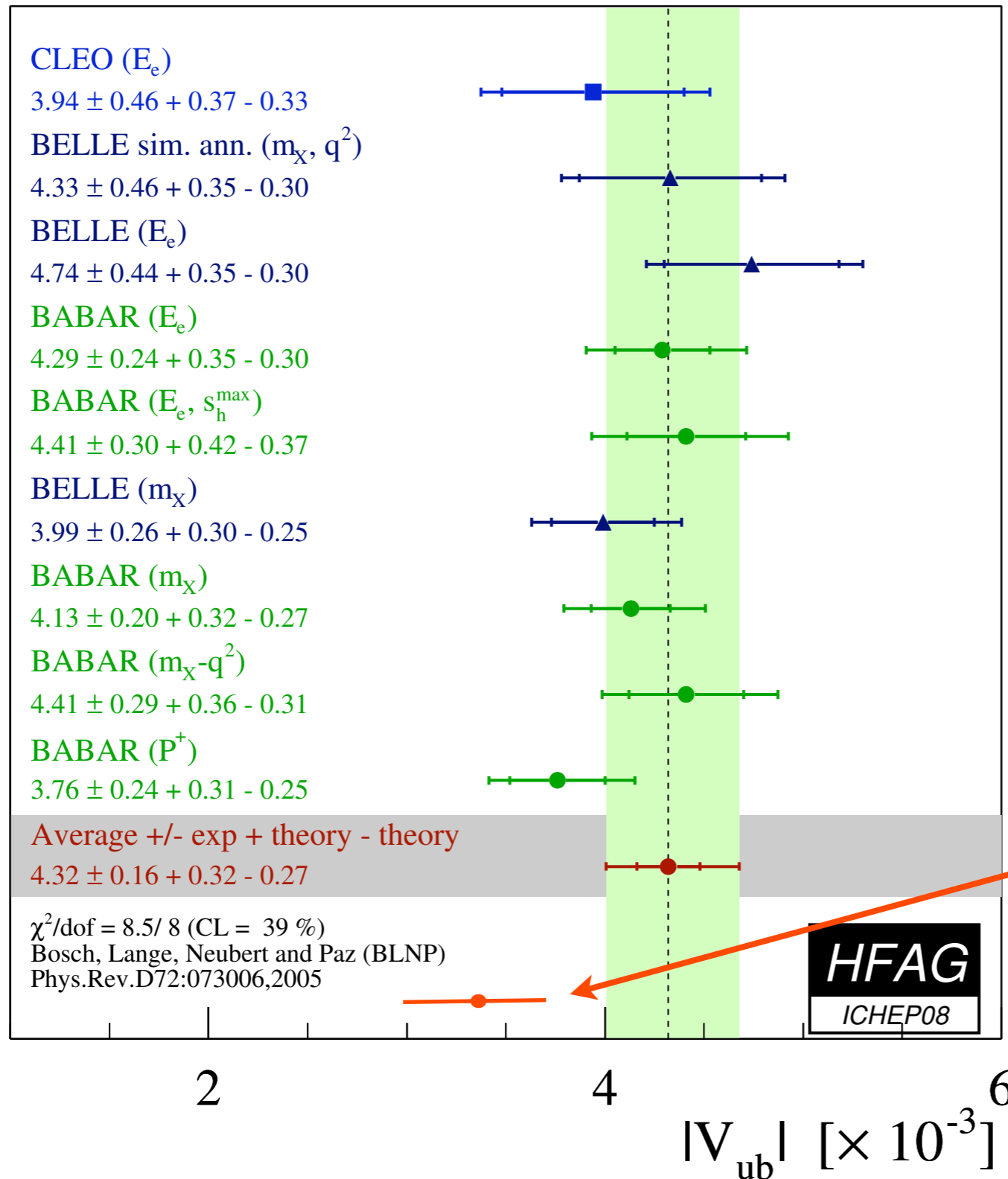
$$|V_{ub}| = (4.64 \pm 0.23_{\text{stat}} \pm 0.19_{\text{syst}} \pm 0.25_{\text{th}}) 10^{-3}$$

DGE

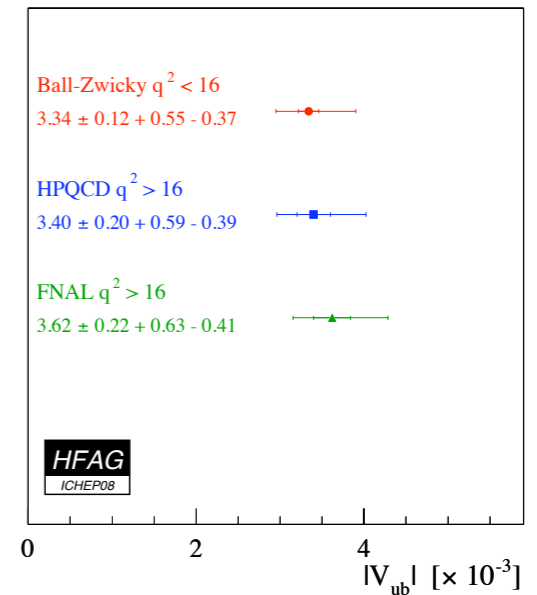
$$|V_{ub}| = (4.93 \pm 0.24_{\text{stat}} \pm 0.20_{\text{syst}} \pm 0.36_{\text{th}}) 10^{-3}$$

BLL, PRD64, 11304 (2001)

# $|V_{ub}|$ in inclusive B decays



Exclusive determination in the range  $3-3.5 \times 10^{-3}$



FNAL/MILC result

# Conclusions

BaBar and PEP-II have gone beyond expectations in the analysis of semileptonic B decays and the measurement of the CKM matrix elements  $|V_{cb}|$  and  $|V_{ub}|$

We now know  $|V_{cb}|$  at the 1.7% level from inclusive decays and 3-4% from exclusive decays

We now know  $|V_{ub}|$  at the 7-8% level from inclusive charmless decays

Precision has brought discrepancy into the picture: inclusive and exclusive determinations of  $|V_{cb}|$  and  $|V_{ub}|$  are, for now, marginally consistent