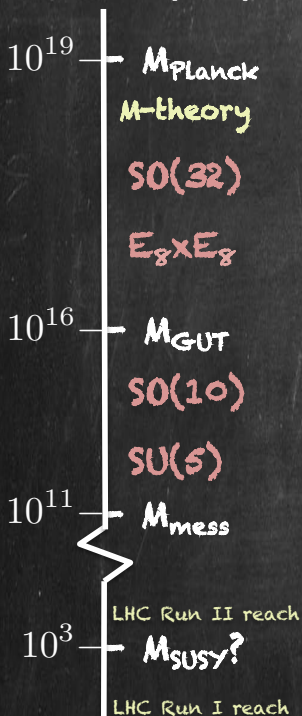




Energy, E [GeV]

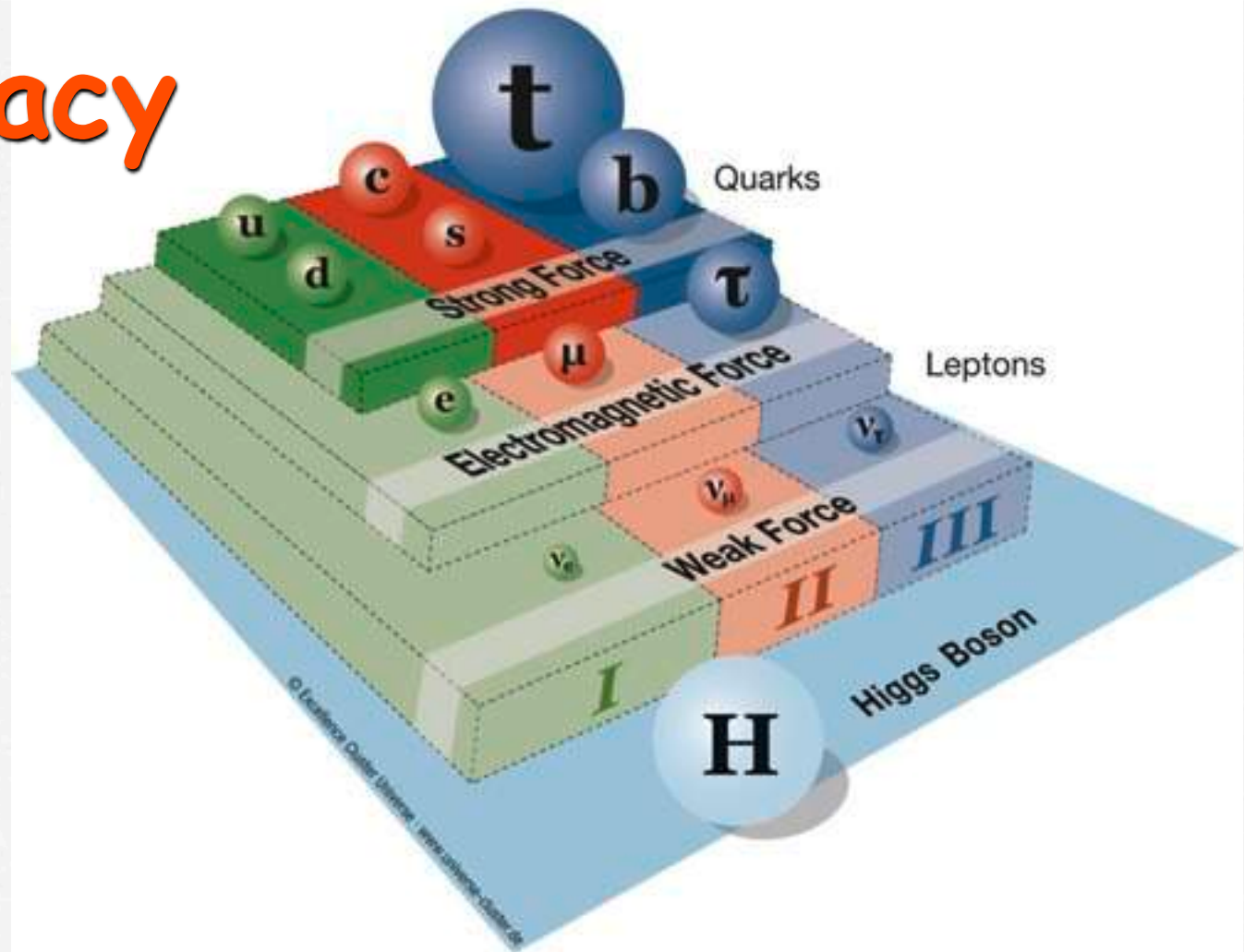


SUSY GUTs & Flavour

Steve King, University of Kent,
Canterbury, 11-12th January 2016

SUPERSYMMETRY: from M-theory to the LHC

The Standard Model and its Legacy



Standard Model Puzzles

1. *The origin of neutrino mass* - and its relation to the weak scale, and the solution to the hierarchy problem
2. *The quest for unification* - the question of whether the three known forces of the standard model may be related into a grand unified theory, and whether such a theory could also include a unification with gravity.
3. *The problem of flavour* - the problem of the undetermined fermion (including neutrino) masses and mixing angles and CP violation, but with suppressed flavour changing neutral currents and strong CP violation.

*We shall discuss all three questions
(apart from strong CP problem)*

See-saw mechanism

P. Minkowski;
T. Yanagida;
M. Gell- Mann,
P. Ramond and
R. Slansky;

$$\begin{pmatrix} \overline{\nu}_L & \overline{\nu}_R^c \end{pmatrix} \begin{pmatrix} 0 & m_{LR} \\ m_{LR}^T & M_{RR} \end{pmatrix} \begin{pmatrix} \nu_L^c \\ \nu_R \end{pmatrix}$$

Dirac mass
↓
 m_{LR}

M_{RR}

$$m^\nu = m_{LR} \cdot \frac{1}{M_{RR}} \cdot m_{LR}^T$$

Light Majorana matrix

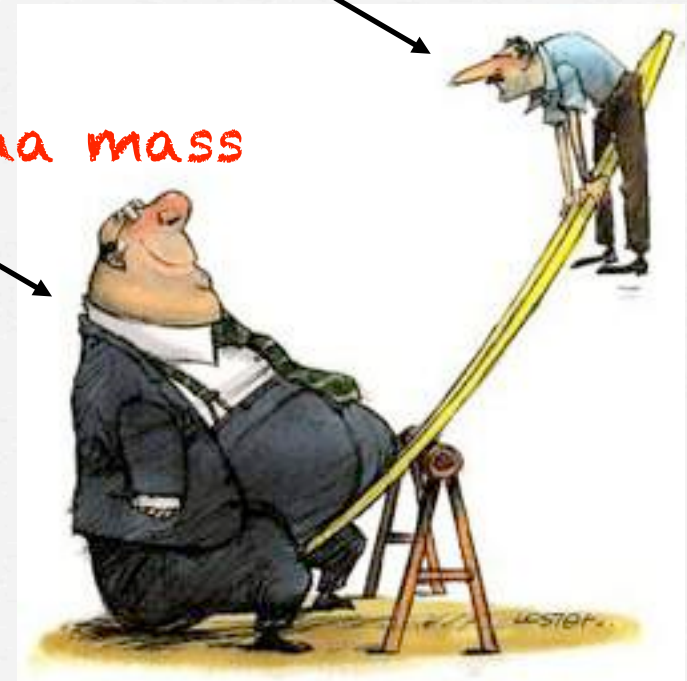
Heavy Majorana mass

Maybe neutrinos are so light

∴ RH neutrinos are so heavy

The minimal seesaw model is:

"Littlest seesaw" 1512.07531

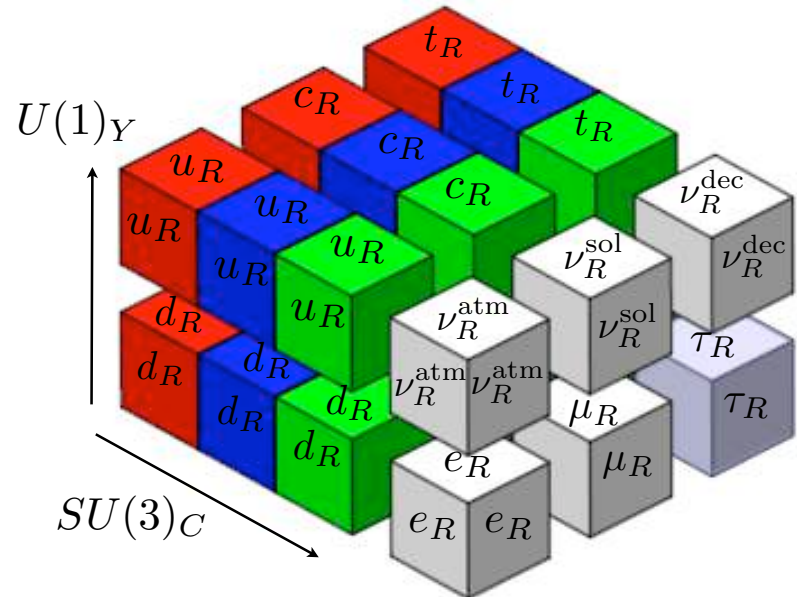
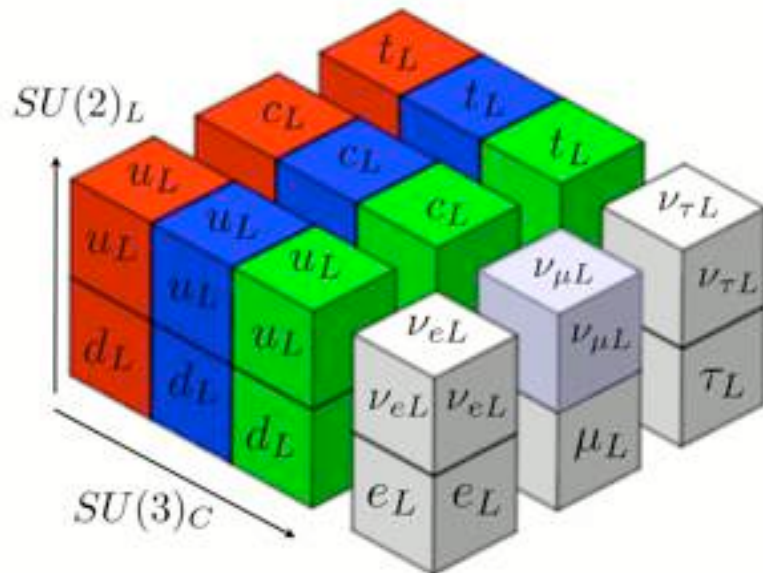


The Standard Model with 3 right-handed neutrinos

$$SU(3)_C \times SU(2)_L \times U(1)_Y$$

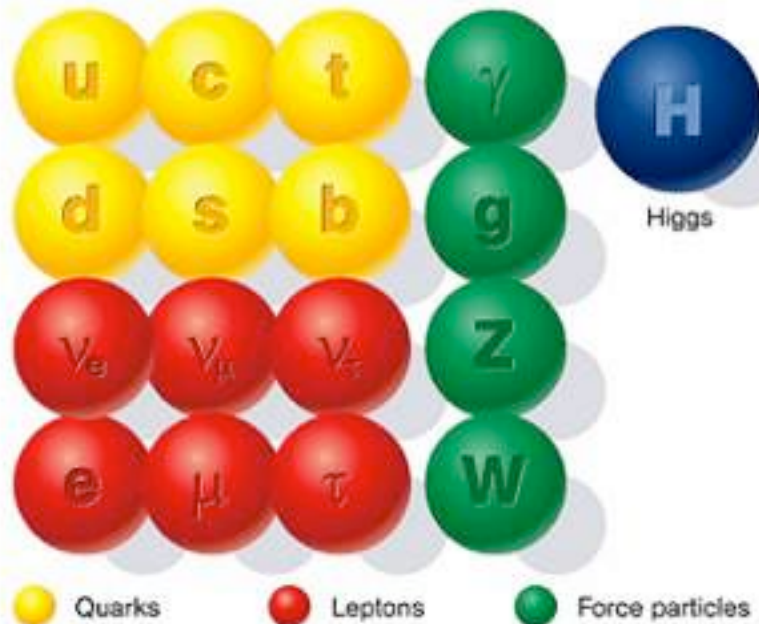
Left-handed quarks and
leptons (active neutrinos)

Right-handed quarks and leptons
(sterile neutrinos)

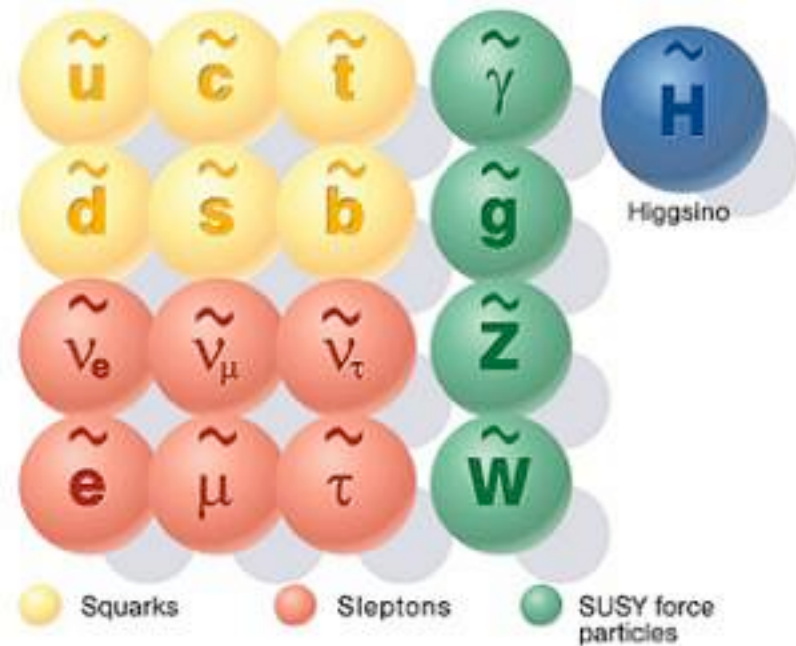


SUSY

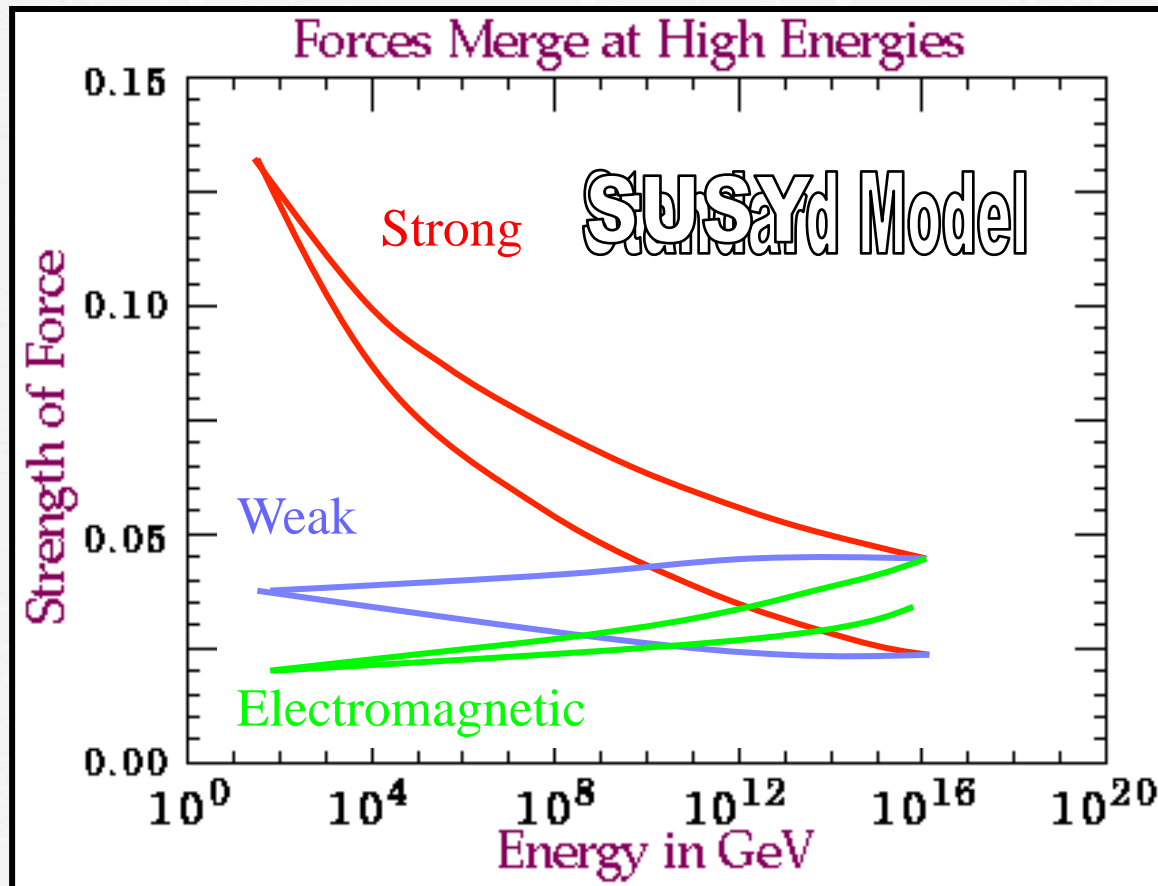
Standard particles



SUSY particles



SUSY facilitates GUTs



Grand Unified Theories (GUTs)

Basic idea is to embed the SM gauge group into a simple gauge group G with a single coupling constant, broken at a high energy scale

$$G \rightarrow SU(3)_c \otimes SU(2)_L \otimes U(1)_Y$$

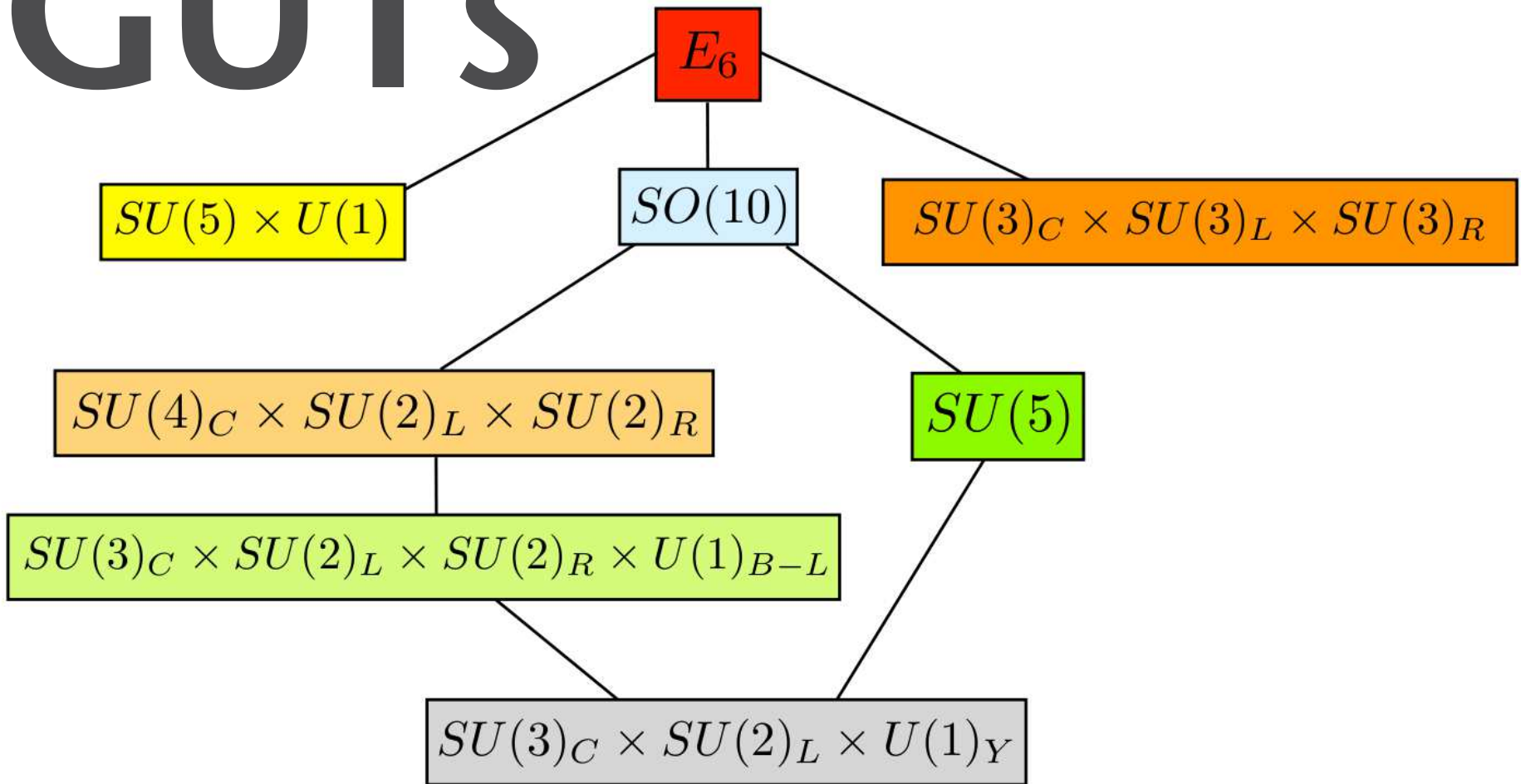
$$u_i^c = (\bar{3}, 1, -\frac{2}{3}), \quad d_i^c = (\bar{3}, 1, \frac{1}{3}), \quad e^c = (1, 1, 1),$$

$$Q^{\alpha i} = (u^i, d^i) = (3, 2, \frac{1}{6}), \quad L^\alpha = (\nu, e) = (1, 2, -\frac{1}{2}),$$

Motivations

1. Continuation of process of unification of physics starting with Maxwell
2. Remarkable fit of SM multiplets into Pati-Salam, $SU(5)$, $SO(10)$, E_6 ...
3. Unification of gauge couplings at high energy scale M_{GUT}
4. Charge quantization: equality of electron and proton charges
5. High energy fermion mass relations e.g. $m_b = m_\tau$

GUTs



SU(5) GUT

Right-handed
neutrino is a singlet

$$(1)_L : \textcircled{\nu^c}$$

$$(\bar{5})_L : \left\{ \begin{array}{c} d^c \\ d^c \\ d^c \\ e \\ \nu_e \end{array} \right\} \begin{array}{l} SU(3) \\ SU(2) \end{array}$$

$$(10)_L : \begin{array}{ccccc} & & u^c & -u^c & u & d \\ & & & u^c & u & d \\ & & & & u & d \\ & & & & & e^c \end{array}$$

SU(5) GUT

Georgi, Glashow

Each family fits nicely into the SU(5) multiplets

$$\bar{5}_i \equiv \begin{pmatrix} d_1^c \\ d_2^c \\ d_3^c \\ e^- \\ -\nu \end{pmatrix}_L \quad 10^{[ij]} \equiv \begin{pmatrix} 0 & u_3^c & -u_2^c & u^1 & d^1 \\ . & 0 & u_1^c & u^2 & d^2 \\ . & . & 0 & u^3 & d^3 \\ . & . & . & 0 & e^c \\ . & . & . & . & 0 \end{pmatrix}_L$$

$$\bar{5} = (\bar{3}, 1, +1/3) \oplus (1, \bar{2}, -1/2) \quad \text{and} \quad 10 = (\bar{3}, 1, -2/3) \oplus (3, 2, +1/6) \oplus (1, 1, +1)$$

N.B in minimal SU(5) neutrino masses are zero.

Right-handed neutrinos may be added to give neutrino masses but
they are not predicted.

Fermion Masses in SU(5)

The Yukawa superpotential for one family

$$\lambda_u H_i 10_{jk} 10_{lm} \epsilon^{ijklm} + \lambda_d \bar{H}^i 10_{ij} \bar{5}^j$$

$$\lambda_u H_u Q u^c + \lambda_d (H_d Q d^c + H_d e^c L)$$

$$\lambda_d = \lambda_e \text{ at the GUT scale}$$

Assuming this relation holds for all 3 families.

$$\underbrace{\lambda_b = \lambda_\tau}_{\text{good}}, \quad \underbrace{\lambda_s = \lambda_\mu, \quad \lambda_d = \lambda_e^T}_{\text{modify using Georgi-Jarlskog mechanism}} \text{ at } M_{GUT}$$

good

modify using Georgi-Jarlskog mechanism

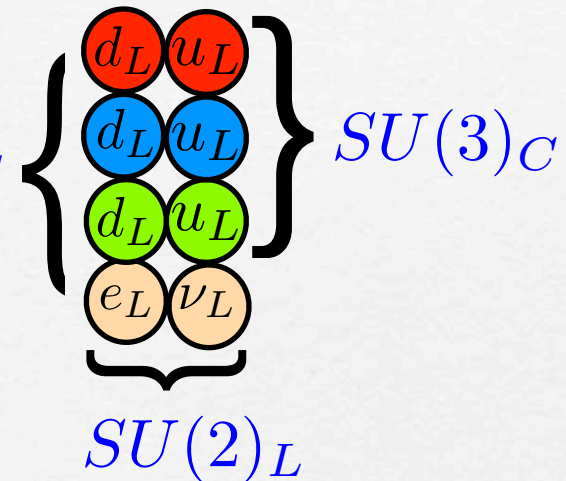
$$\lambda_b = \lambda_\tau, \quad \lambda_s = \frac{\lambda_\mu}{3}, \quad \lambda_d = 3\lambda_e$$

Pati-Salam

Talk by
Patrick

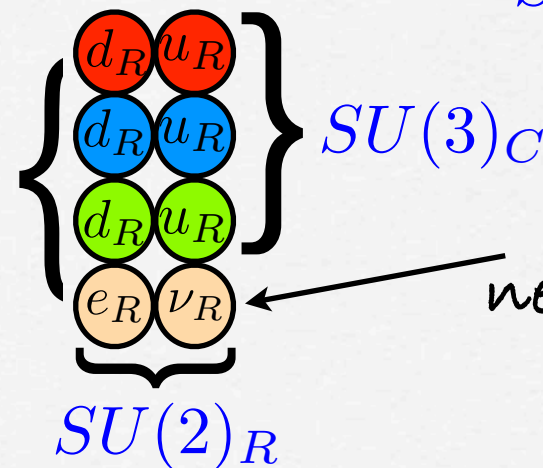
$$SU(4)_C \times SU(2)_L \times SU(2)_R$$

$$(4, 2, 1)_L : SU(4)_C$$



"Lepton number as the
fourth colour"

$$(4, 1, 2)_R : SU(4)_C$$



Right-handed
neutrino is predicted

Pati-Salam

$$SU(4)_{PS} \times SU(2)_L \times SU(2)_R$$

$$(4, 2, 1) = \begin{pmatrix} u & u & u & \nu \\ d & d & d & e^- \end{pmatrix}_L \quad (4, 1, 2) = \begin{pmatrix} u & u & u & \nu \\ d & d & d & e^- \end{pmatrix}_R$$

- Predicts RH neutrinos with lepton number as the "fourth colour"
- Allows the possibility of restoring parity if LR symmetry is imposed
- (Quark-lepton) unification of 16 family into two LR symmetric reps
- B-L as a gauge symmetry
- Quantization of electric charge $\rightarrow Q_e = -Q_p$
- Pati-Salam can be unified into $SO(10)$

$$(4, 2, 1) + (4, 1, 2) \subset 16$$

SO(10) GUT

Georgi; Fritzsch and Minkowski

The 16 of SO(10) contains a single quark and lepton family and also predicts a single right-handed neutrino per family.

The SU(5) reps are unified into SO(10):

$$10 + \bar{5} + \bar{\nu} \subset 16$$

The two Higgs doublets are contained in a 10 of SO(10)

$$5_H, \bar{5}_H \subset 10_H$$

Fermion masses arise from the coupling

$$\lambda 16.16.10_H = \lambda \left(Q h_2 u^c + Q h_1 d^c + L h_1 e^c + L h_2 \nu^c \right)$$

Neutrino Masses in SO(10)

$$16.16.10_H \rightarrow (\bar{\nu} \quad \bar{e})_L \begin{pmatrix} H^0 \\ H^- \end{pmatrix} \nu_R \rightarrow m_{LR} \bar{\nu}_L \nu_R \quad \text{Dirac mass}$$

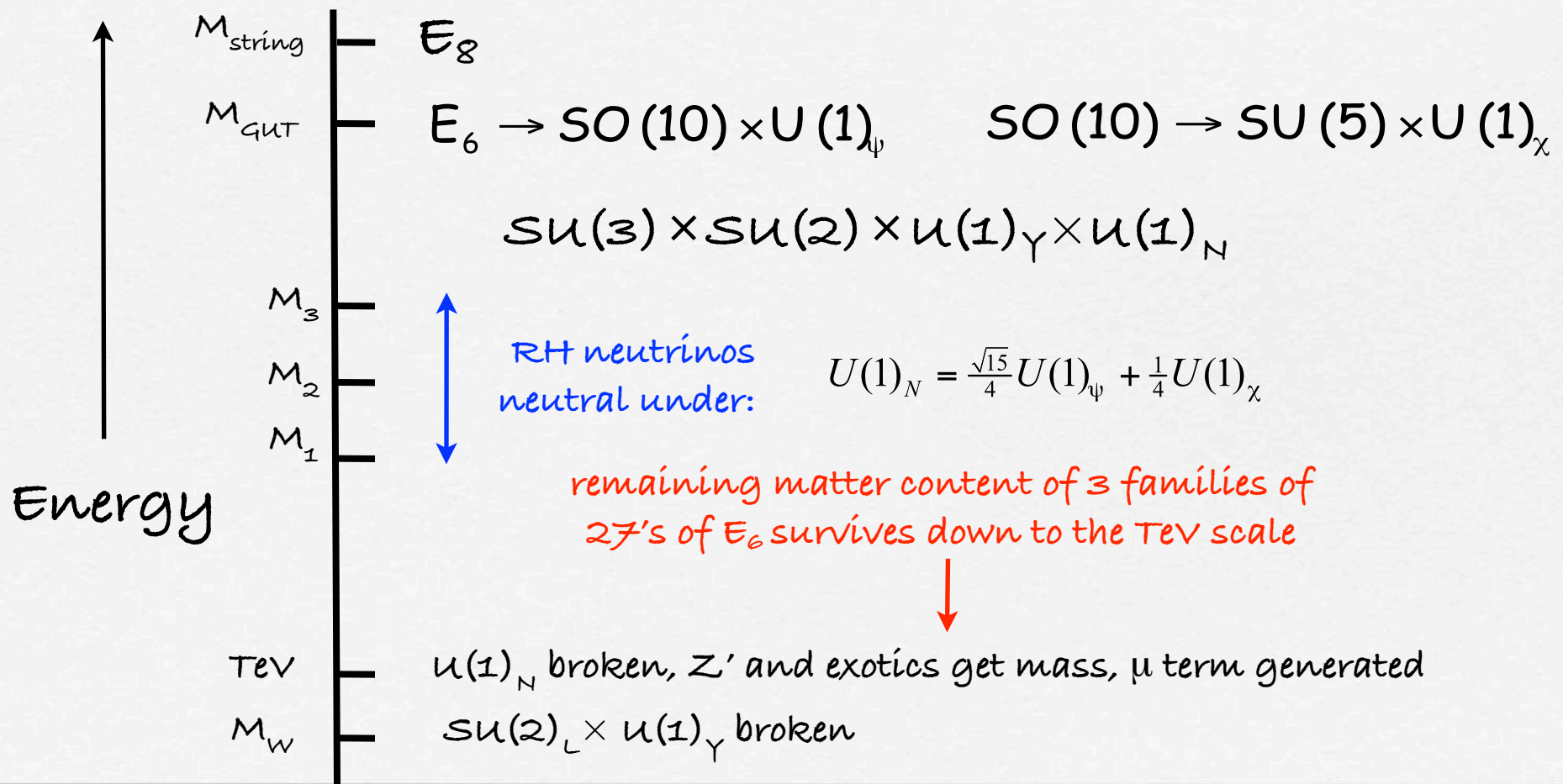
$$16.16.126_H \rightarrow \langle 126_H \rangle \nu_R \nu_R$$

$$\frac{16.16.\overline{16}_H \overline{16}_H}{M} \rightarrow \frac{\langle \overline{16}_H \rangle^2}{M} \nu_R \nu_R$$

Heavy Majorana mass

SO(10) contains all the ingredients for the see-saw mechanism

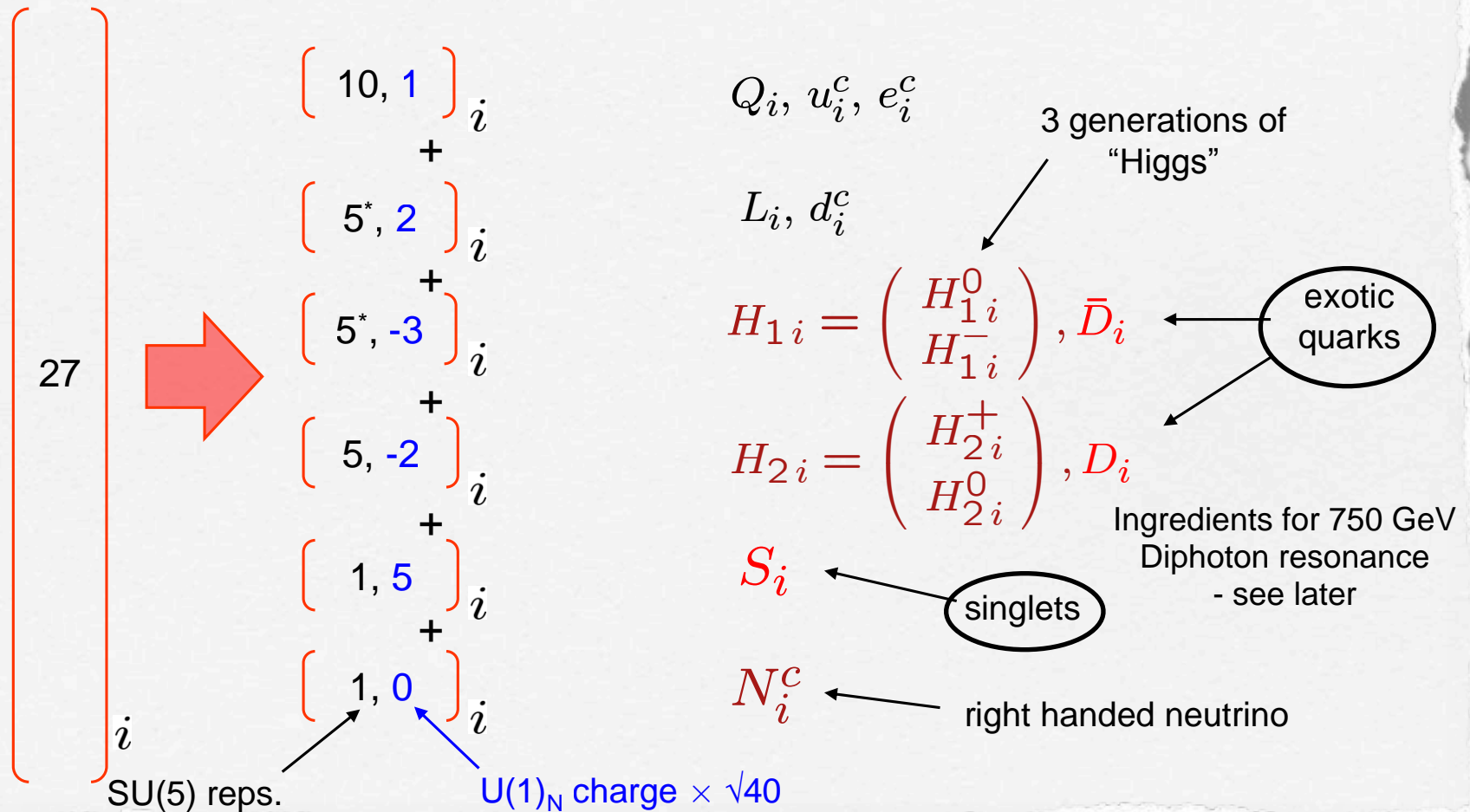
Exceptional SUSY SM (E_6 SSM)



Matter Content of 27's of E_6

All the SM matter fields are contained in one 27-plet of E_6 per generation.

Miller



E₆SSM Couplings

$$S \subset S_i,$$

$$D \subset D_i, \bar{D}_i,$$

$$H \subset H_i^u, H_i^d$$

$$F \subset Q_i, L_i, U_i^c, D_i^c, E_i^c, N_i^c$$

$$W = SHH + SDD + HFF + DFF$$

Singlet-Higgs-Higgs
couplings includes
effective μ term

Singlet-D-D couplings
includes effective D
mass terms

Yukawa couplings
but extra Higgs
give FCNCs

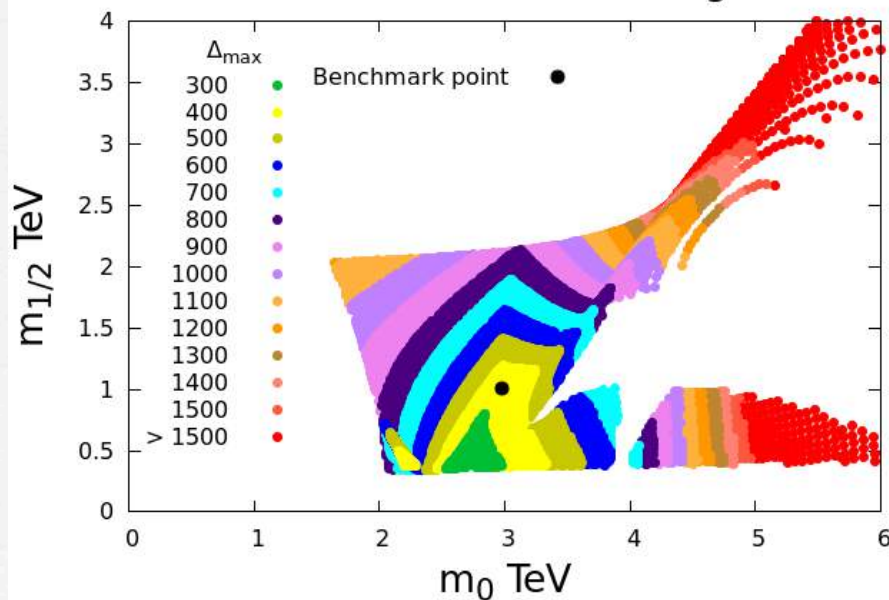
DQQ, DQL allows D
decay but also proton
decay. Need to:
– either forbid one of
DQQ or DQL
– or allow both with
Yukawas $\sim 10^{-12}$

Fine-tuning in the cE6SSM

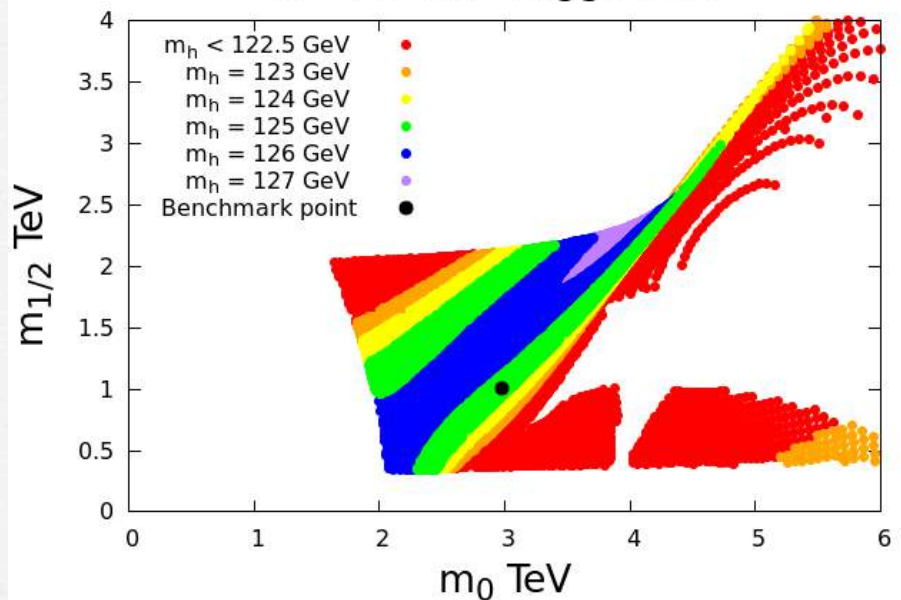
$\tan \beta = 10$, $\lambda_{12} = 0.1$, $s = 10$ TeV,

Athron, Binjonaïd, SFK

$s = 10$ TeV - Fine Tuning



$s = 10$ TeV - Higgs Mass

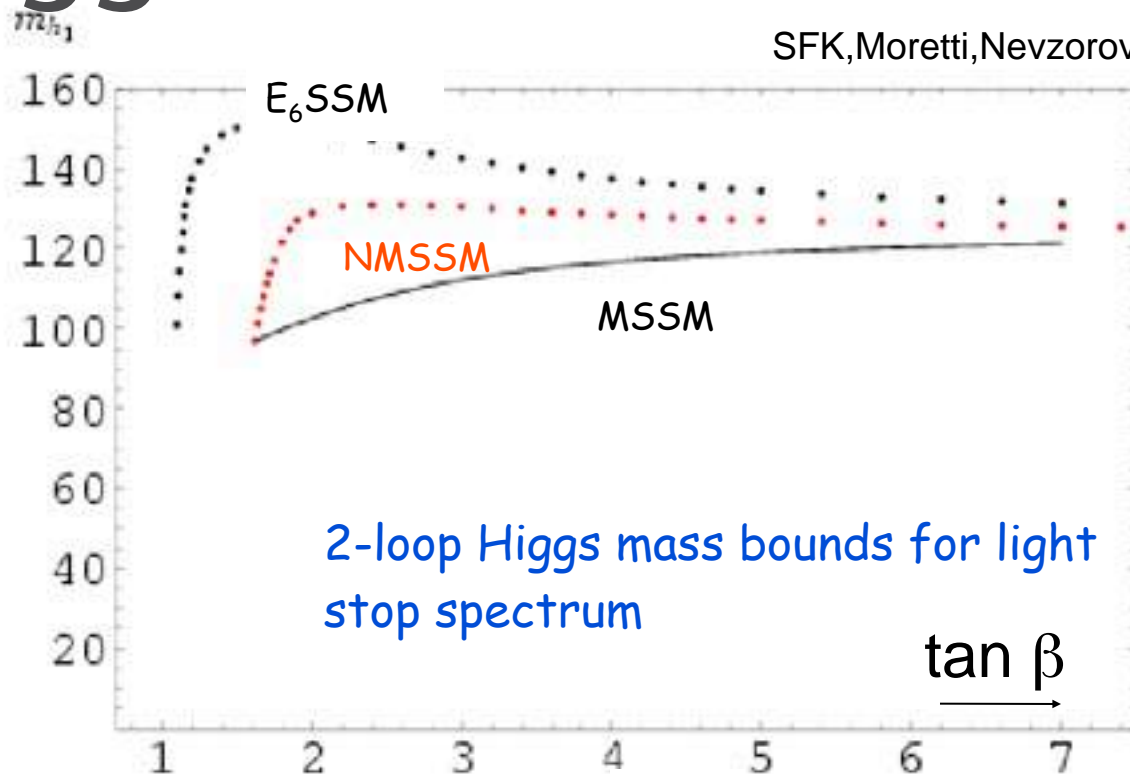


Lower fine-tuning than cMSSM

Higgs mass bounds in SSM's

SFK, Moretti, Nevzorov hep-ph/0510419

m_h



Extra terms in non-minimal models allow

$$\Delta m_h < M_Z$$

Hence allow lighter stops and lower fine-tuning

$$m_h^2 \approx \underbrace{M_Z^2 \cos^2 2\beta}_{MSSM} + \underbrace{\frac{\lambda^2}{2} v^2 \sin^2 2\beta + \frac{M_Z^2}{4} \left(1 + \frac{1}{4} \cos 2\beta\right)^2}_{NMSSM} + \Delta m_h^2$$

E_6SSM

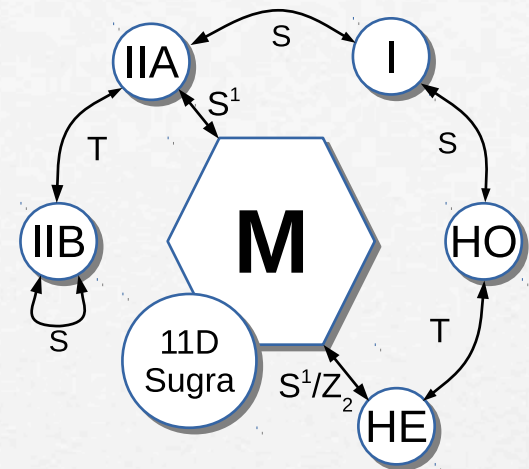
LHC phenomenology of E_6 SSM

- **SUSY** - typical spectrum has heavier squarks and lighter gluinos, with gluinos having longer decay chains than MSSM, due to extra neutralinos and charginos, giving less missing energy and more soft leptons and jets
- **Higgs** - Richer Higgs spectrum than MSSM or NMSSM, incl. inert + singlet Higgs (Diphoton)
- **Exotics** - Z' , D-leptoquarks/diquarks (maybe long lived)

M-theory

GUTs (gravity)

Talk by Miguel Romao



- M-theory \rightarrow 11d SUGRA \rightarrow 4d $N=1$ SUGRA
- Compactified 7d $\rightarrow G_2$ manifold
- Gauge fields on dominant volume 3d submanifold
- $SU(5)$ GUT
- $SO(10)$ GUT
- main prediction: extra 16+16bar at TeV scale



Witten,
Acharya,
Kane, ...

Acharya, Bozek, M.C.Romao,
S.F.K. and Pongkitivanichkul
1502.01727

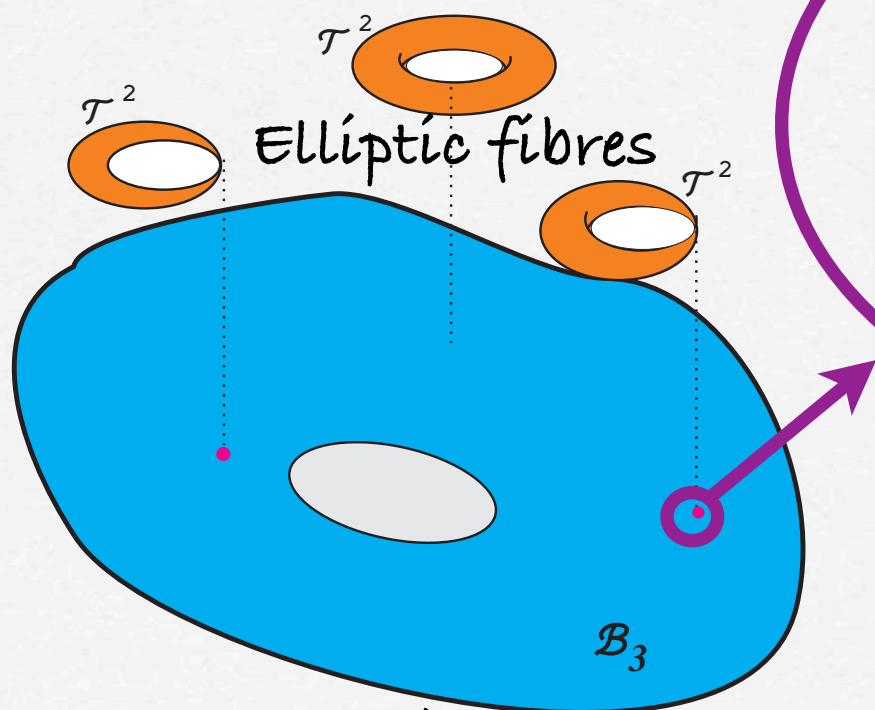
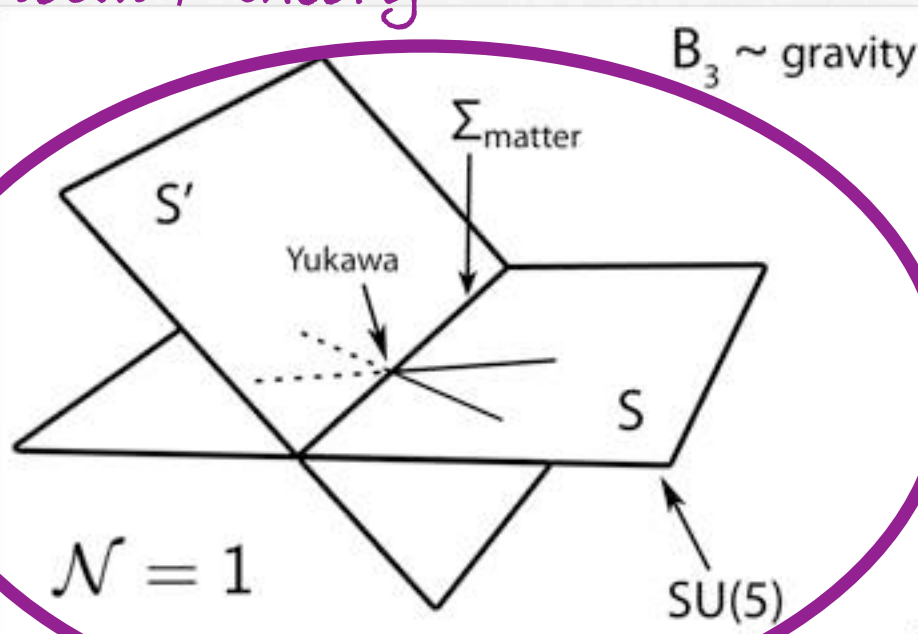
Talk by Andrew Meadowcroft

F-theory

GUTs

G.K. Leontaris,
 ``Aspects of F-Theory GUTs,``
 PoS CORFU {\bf 2011} (2011) 095
 [arXiv:1203.6277 [hep-th]].

Local F-theory



Type IIB string theory

dim.	internal dim.	feature
10	$6 = \dim(B_3)$	gravity
8	$4 = \dim(S)$	gauge fields
6	$2 = \dim(S \cap S')$	matter
4	$0 = \dim(S \cap S' \cap S'')$	interactions

E₆SSM from F-theory

Callaghan, SFK

E_6	$SO(10)$	$SU(5)$	Weight vector	Q_N	N_Y	$M_{U(1)}$	SM particle content	Low energy spectrum
$27_{t'_1}$	16	$\bar{5}_3$	$t_1 + t_5$	$\frac{1}{\sqrt{10}}$	1	4	$4d^c + 5L$	$3d^c + 3L$
$27_{t'_1}$	16	10_M	t_1	$\frac{1}{2\sqrt{10}}$	-1	4	$4Q + 5u^c + 3e^c$	$3Q + 3u^c + 3e^c$
$27_{t'_1}$	16	θ_{15}	$t_1 - t_5$	0	0	n_{15}	$3\nu^c$	-
$27_{t'_1}$	10	5_1	$-t_1 - t_3$	$-\frac{1}{\sqrt{10}}$	-1	3	$3D + 2H_u$	$3D + 2H_u$
$27_{t'_1}$	10	$\bar{5}_2$	$t_1 + t_4$	$-\frac{3}{2\sqrt{10}}$	1	3	$3\bar{D} + 4H_d$	$3\bar{D} + 3H_d$
$27_{t'_1}$	1	θ_{14}	$t_1 - t_4$	$\frac{5}{2\sqrt{10}}$	0	n_{14}	θ_{14}	θ_{14}
$27_{t'_3}$	16	$\bar{5}_5$	$t_3 + t_5$	$\frac{1}{\sqrt{10}}$	-1	-1	$\bar{d}^c + 2\bar{L}$	-
$27_{t'_3}$	16	10_2	t_3	$\frac{1}{2\sqrt{10}}$	1	-1	$\bar{Q} + 2\bar{u}^c$	-
$27_{t'_3}$	16	θ_{35}	$t_3 - t_5$	0	0	n_{35}	-	-
$27_{t'_3}$	10	5_{H_u}	$-2t_1$	$-\frac{1}{2\sqrt{10}}$	1	0	H_u	H_u
$27_{t'_3}$	10	$\bar{5}_4$	$t_3 + t_4$	$-\frac{3}{2\sqrt{10}}$	-1	0	\bar{H}_d	-
$27_{t'_3}$	1	θ_{34}	$t_3 - t_4$	$\frac{5}{2\sqrt{10}}$	0	n_{34}	θ_{34}	θ_{34}
-	1	θ_{31}	$t_3 - t_1$	0	0	n_{31}	θ_{31}	-
-	1	θ_{53}	$t_5 - t_3$	0	0	n_{53}	θ_{53}	-
-	1	θ_{54}	$t_5 - t_4$	$\frac{5}{2\sqrt{10}}$	0	n_{54}	θ_{54}	-
-	1	θ_{45}	$t_4 - t_5$	$-\frac{5}{2\sqrt{10}}$	0	n_{45}	θ_{45}	-

$$W \sim \lambda \theta_{14} H_d H_u + \lambda_{\alpha\beta\gamma} \theta_{34}^\alpha H_d^\beta H_u^\gamma + \kappa_{\alpha jk} \theta_{34}^\alpha \bar{D}_j D_k$$

Singlets couple to the extra vector-like fermions (see later)

Bulk exotics

Theorem: flux breaking of E_6 always accompanied by bulk exotics

$$E_8 \supset E_6 \times SU(3)_\perp$$

$$248 \rightarrow (78, 1) + (27, 3) + (\overline{27}, \overline{3}) + (1, 8)$$



Bulk exotics

$$78 \rightarrow (1, 1)_{0,0,0} + \{ (1, 1)_{0,0,0} + (1, 1)_{0,0,0} + (8, 1)_{0,0,0} + (1, 3)_{0,0,0} + (3, 2)_{-5,0,0} + (\overline{3}, 2)_{5,0,0} \\ + (3, 2)_{1,4,0} + (\overline{3}, 2)_{-1,-4,0} + (\overline{3}, 1)_{-4,4,0} + (3, 1)_{4,-4,0} + (1, 1)_{6,4,0} + (1, 1)_{-6,-4,0} \} \\ + \{ (1, 1)_{0,-5,-3} + (\overline{3}, 1)_{2,3,-3} + (1, 2)_{-3,3,-3} + (1, 1)_{6,-1,-3} + (3, 2)_{1,-1,-3} + (\overline{3}, 1)_{-4,-1,-3} \} \\ + \{ (1, 1)_{0,5,3} + (3, 1)_{-2,-3,3} + (1, 2)_{3,-3,3} + (1, 1)_{-6,1,3} + (\overline{3}, 2)_{-1,1,3} + (3, 1)_{4,1,3} \}$$

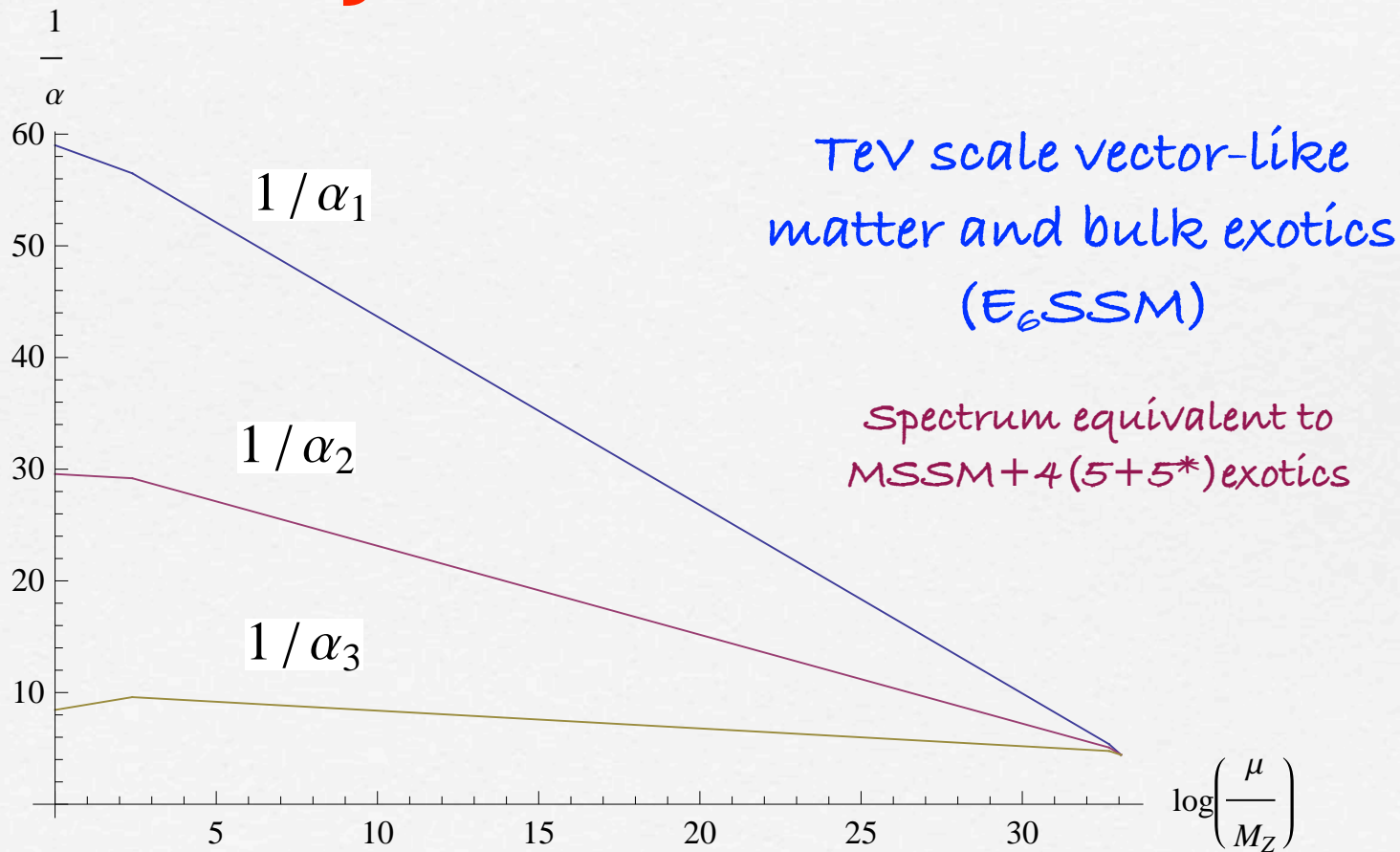
E_6 origin	$SU(5)$ origin	TeV scale spectrum	$U(1)_N$
$27_{t'_1}$	$\overline{5}$	$3d^c + 3L$	$\frac{1}{\sqrt{10}}$
$27_{t'_1}$	10	$3Q + 3u^c + 3e^c$	$\frac{1}{2\sqrt{10}}$
$27_{t'_1}$	5	$3D + 2H_u$	$-\frac{1}{\sqrt{10}}$
$27_{t'_1}$	$\overline{5}$	$3\overline{D} + 3H_d$	$-\frac{3}{2\sqrt{10}}$
$27_{t'_1}$	1	θ_{14}	$\frac{5}{2\sqrt{10}}$
$27_{t'_3}$	5	H_u	$-\frac{1}{2\sqrt{10}}$
$27_{t'_3}$	1	$2\theta_{34}$	$\frac{5}{2\sqrt{10}}$
78	$\overline{5}$	$2X_{H_d} + X_{d^c}$	$-\frac{3}{2\sqrt{10}}$
78	5	$2\overline{X}_{\overline{H}_d} + \overline{X}_{\overline{d^c}}$	$\frac{3}{2\sqrt{10}}$

Minimal allowed set of bulk exotics can restore gauge coupling unification in E_6 SSM

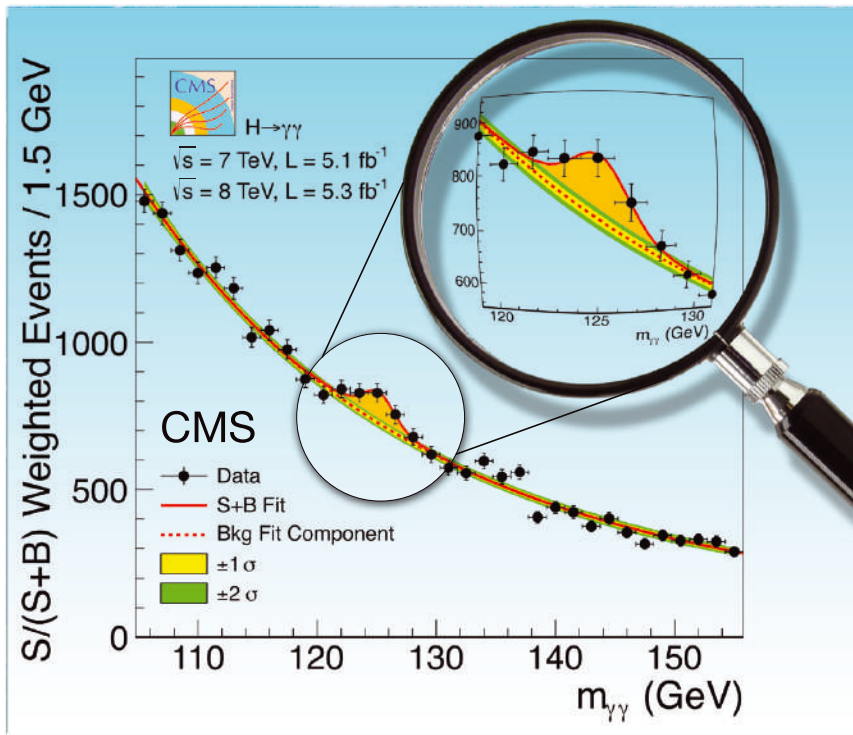
TeV spectrum equivalent to MSSM + 4(5+5*) exotics

Callaghan, SFK, Leontaris

Gauge coupling unification in F-theory model with bulk exotics



Diphoton resonance at 125 GeV



4th July, 2012

Congratulations to both
Atlas and CMS Collaborations
and to the builders of the LHC
on a magnificent achievement!

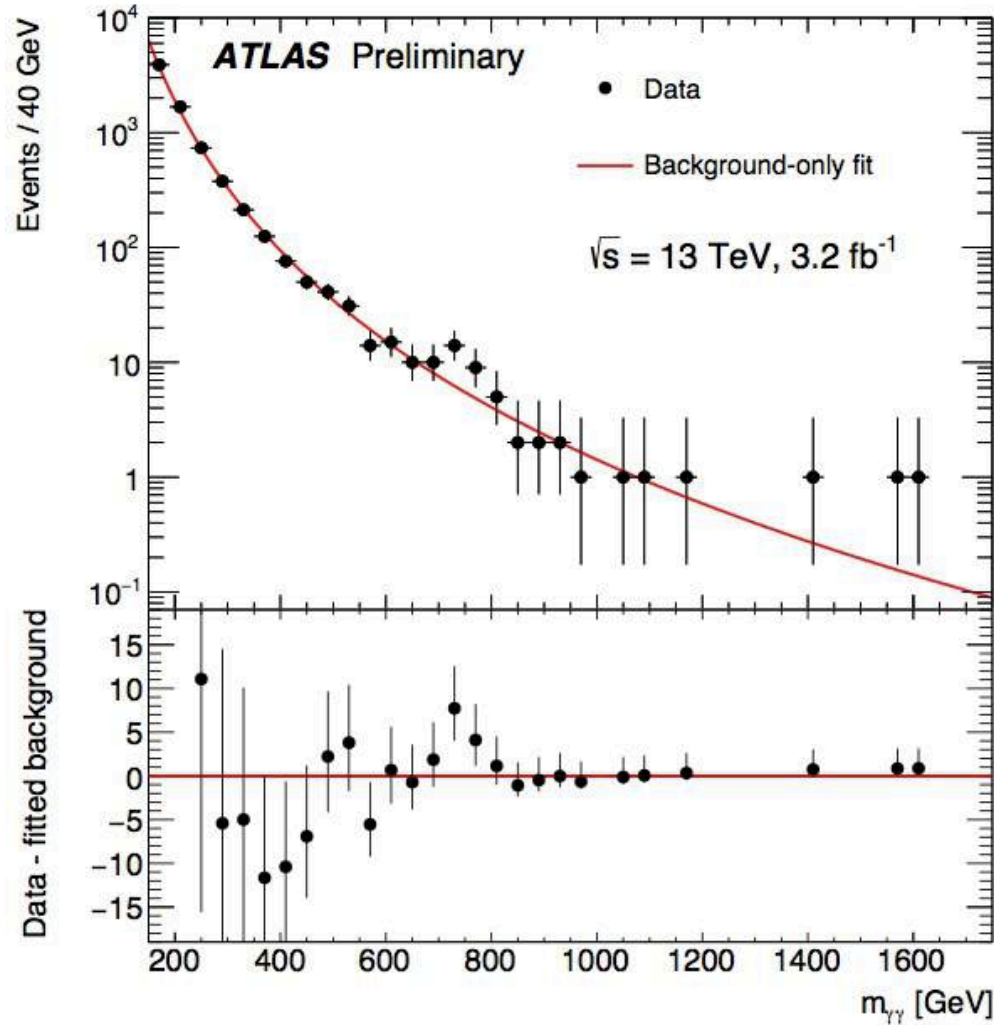


Peter Higgs
30 August 2012

"... The decay to two photons indicates that the new particle is a boson with spin different from one. The results presented here are consistent, ... with expectations for a standard model Higgs boson."

- CMS Collaboration

Diphoton resonance at 750 GeV



“Who ordered that?”

ATLAS

$$M \simeq 750 \text{ GeV}$$

$$\Gamma \sim 45 \text{ GeV}$$

avored

~ 14 events

3.9σ local

2.3σ including LEE

CMS

$$M \simeq 760 \text{ GeV}$$

narrow width favored

~ 10 events

2.6σ local

1.2σ including LEE

- No significant E_{Tmiss} , leptons or jets in the events
- No $\gamma \gamma$ resonance at 8 TeV but small upward fluctuation

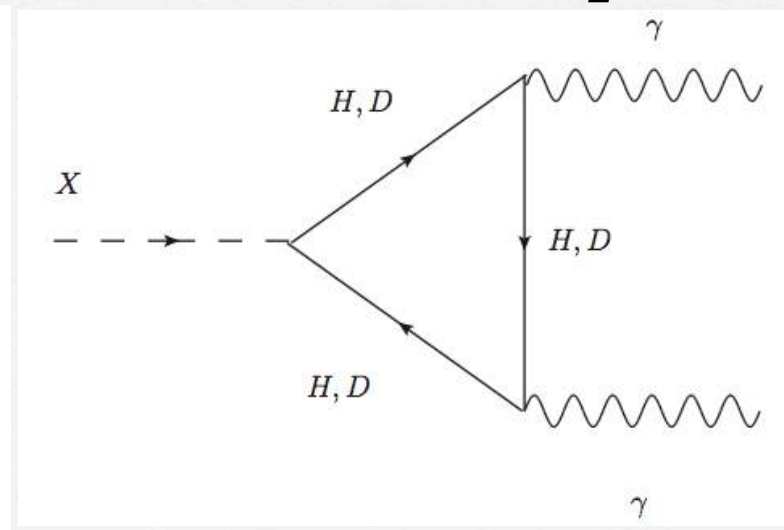
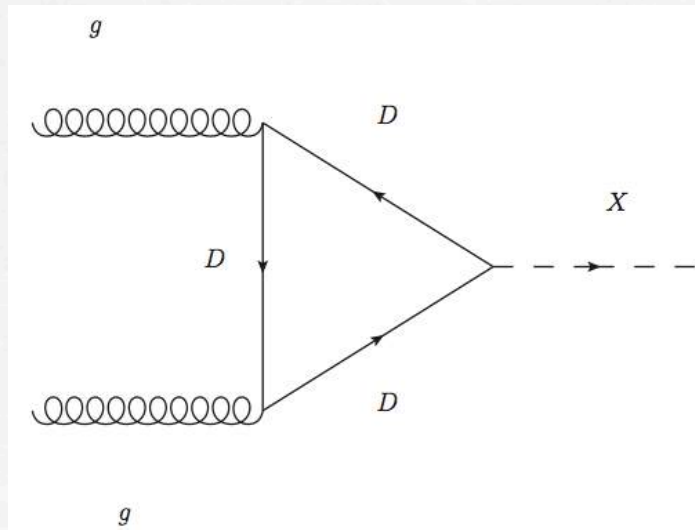
$$\sigma(pp \rightarrow \gamma\gamma) \approx \begin{cases} (0.5 \pm 0.6) \text{ fb} & \text{CMS [2]} & \sqrt{s} = 8 \text{ TeV}, \\ (0.4 \pm 0.8) \text{ fb} & \text{ATLAS [3]} & \sqrt{s} = 8 \text{ TeV}, \\ (6 \pm 3) \text{ fb} & \text{CMS [1]} & \sqrt{s} = 13 \text{ TeV}, \\ (10 \pm 3) \text{ fb} & \text{ATLAS [1]} & \sqrt{s} = 13 \text{ TeV}. \end{cases}$$

Diphoton resonance at 750 GeV

Over 100 theoretical papers with various interpretations

We propose that it is an E_6 SSM F-theory singlet X coupling to vector-like Higgsino and D fermions

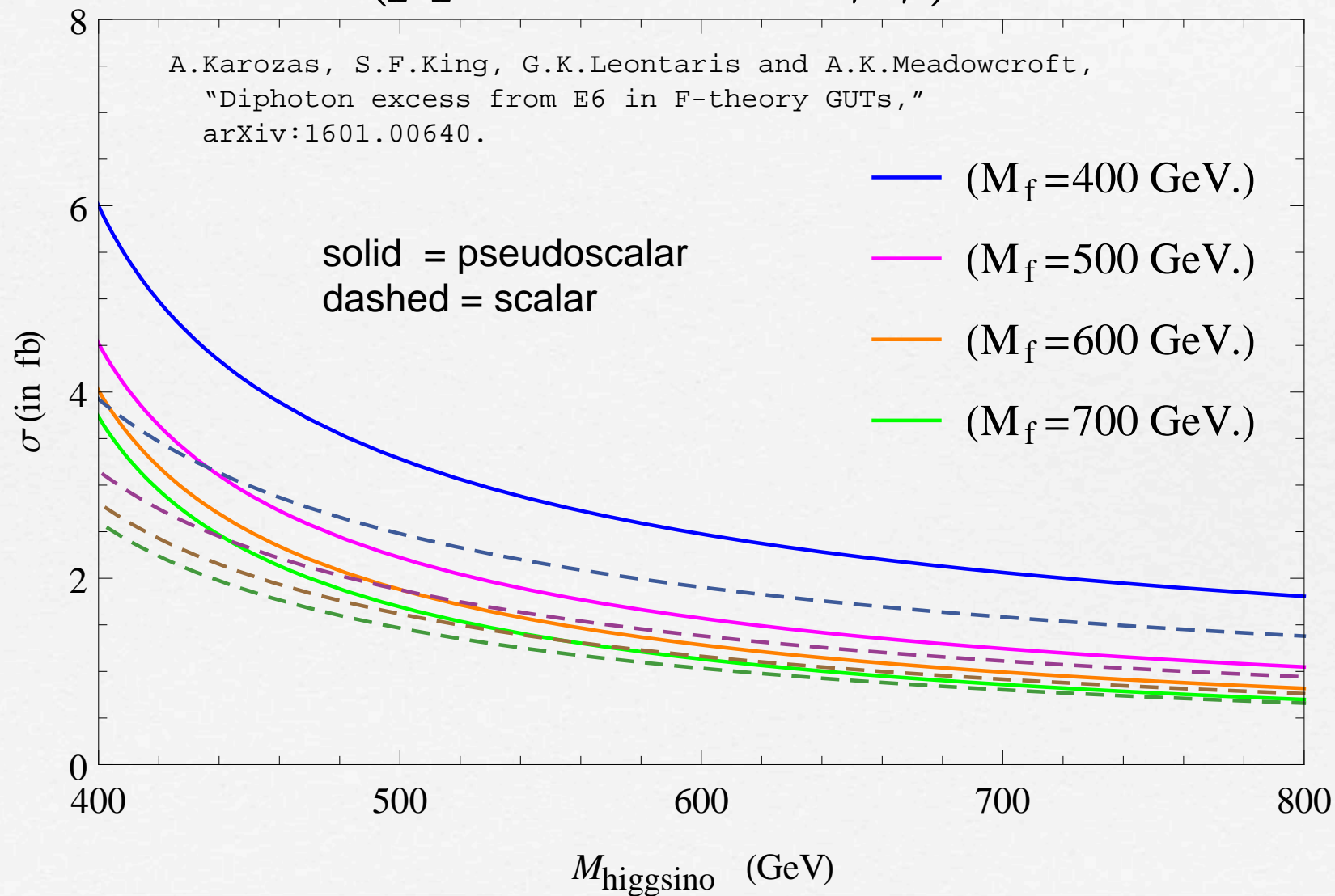
$$\mathcal{L} \sim \kappa_i X \bar{D}_i D_i + \lambda_\alpha X H_u^\alpha H_d^\alpha + M_i \bar{D}_i D_i + M_{H_\alpha} H_u^\alpha H_d^\alpha + \frac{1}{2} M^2 X^2 + \dots$$



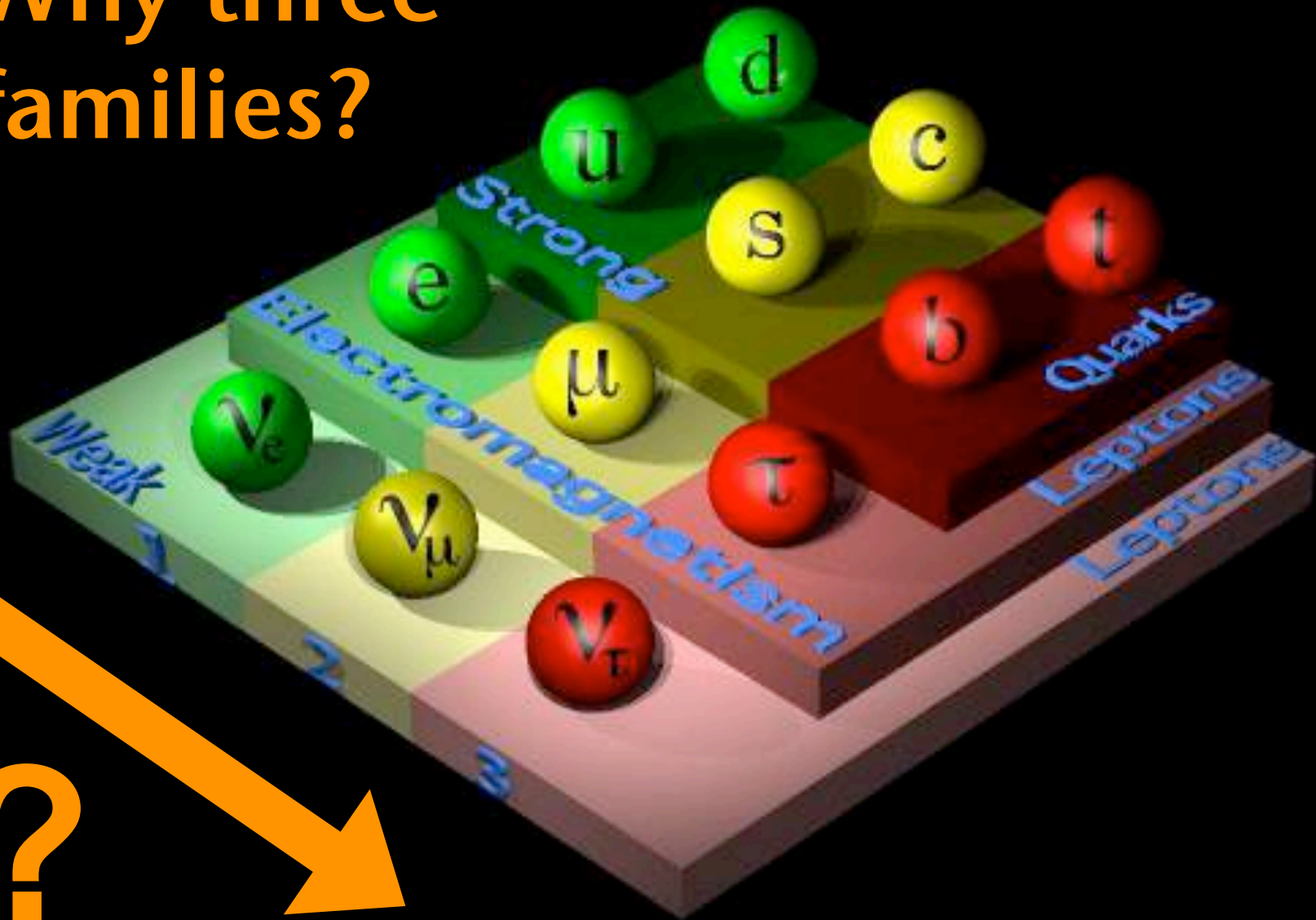
$$\sigma(pp \rightarrow X \rightarrow \gamma\gamma) = \frac{1}{M\Gamma_S} C_{gg} \Gamma(X \rightarrow gg) \Gamma(X \rightarrow \gamma\gamma)$$

$$\sigma(pp \rightarrow X \rightarrow \gamma\gamma)$$

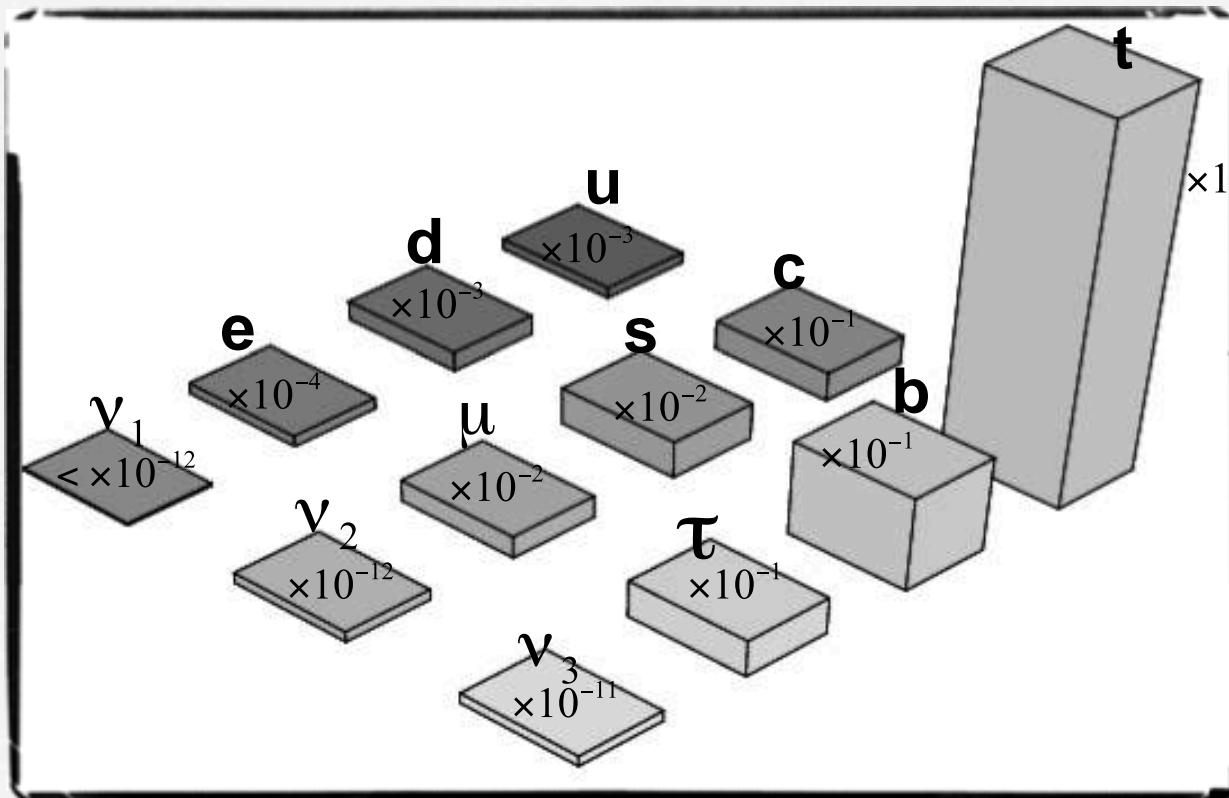
A.Karozas, S.F.King, G.K.Leontaris and A.K.Meadowcroft,
"Diphoton excess from E6 in F-theory GUTs,"
arXiv:1601.00640.



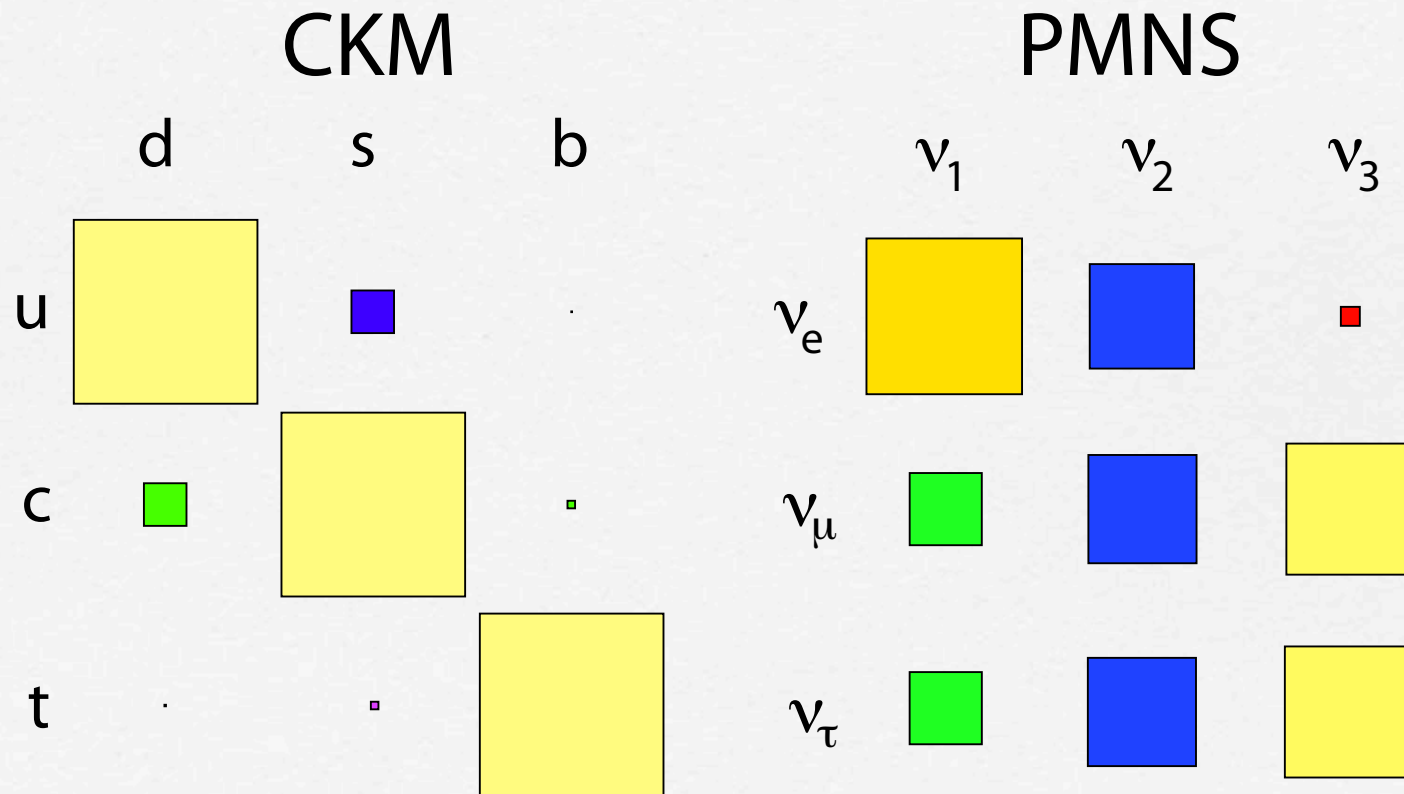
Why three families?



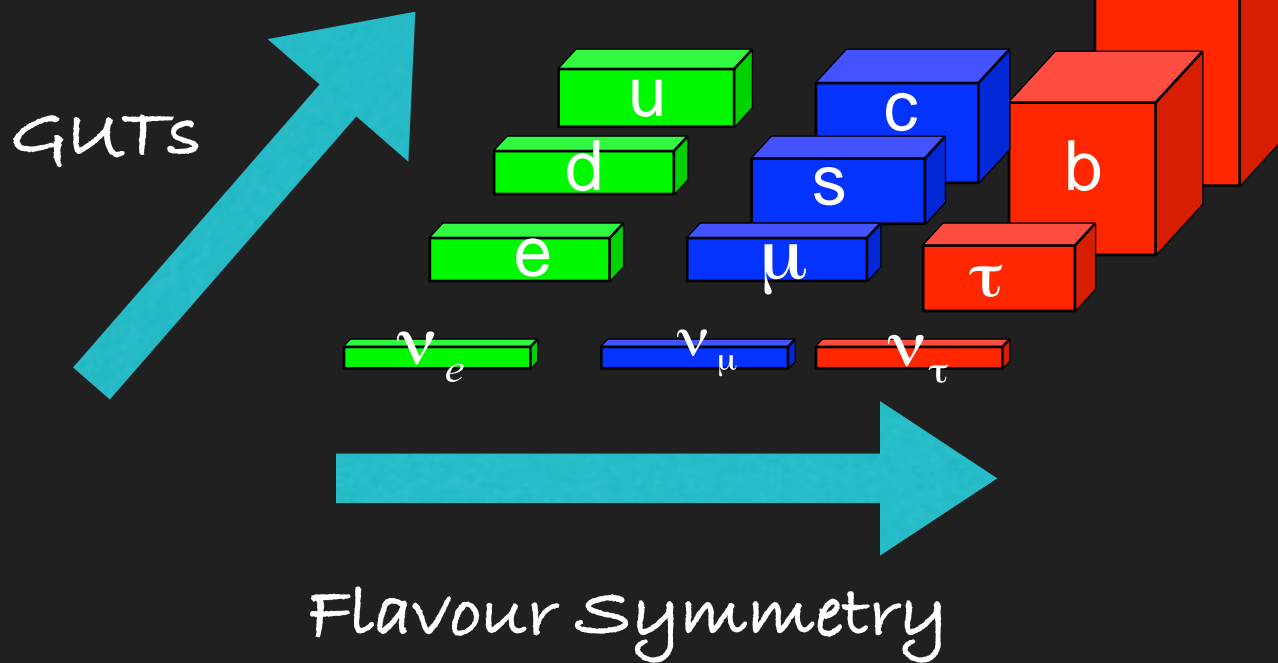
What is the origin of Quark and Lepton Masses?



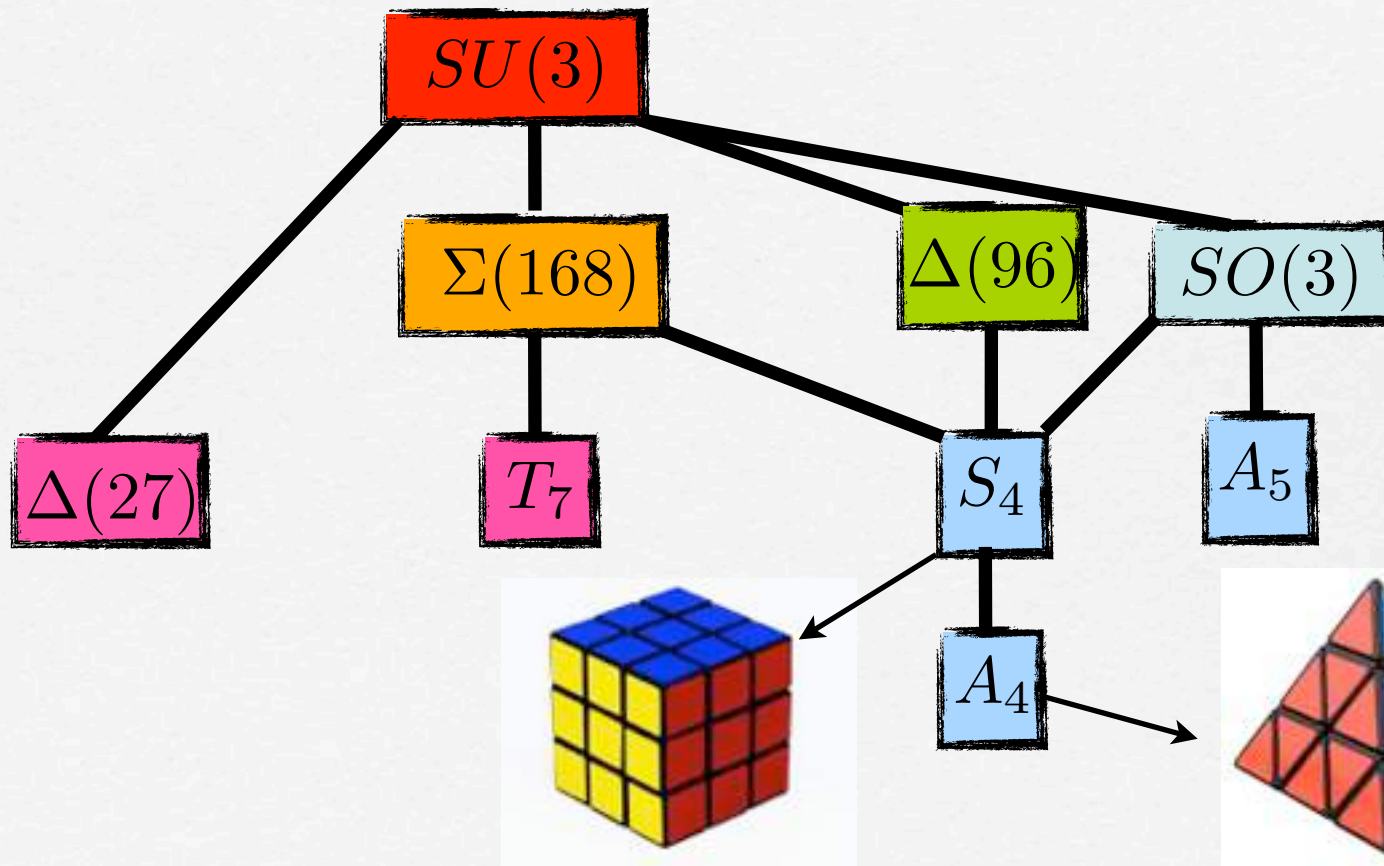
What is the origin of Quark and Lepton Mixing?



GUTs and Flavour



Flavour Symmetry



Hagedorn, SFK, Luhn

$$S_4 \times SU(5) \times U(1) \quad m_\nu^{\text{eff}} \approx \frac{y_D^2 v_u^2}{\lambda^4 M} \left[\begin{pmatrix} b^\nu + c^\nu - a^\nu & a^\nu & a^\nu \\ a^\nu & b^\nu & c^\nu \\ a^\nu & c^\nu & b^\nu \end{pmatrix} e^{-i\theta_A} + \begin{pmatrix} 0 & 0 & d^\nu \\ 0 & d^\nu & 0 \\ d^\nu & 0 & 0 \end{pmatrix} \lambda e^{i(\theta_D - 2\theta_A)} \right]$$

	Matter fields				Higgs fields			Flavon fields								
	T_3	T	F	ν^c	H_5	$H_{\bar{5}}$	$H_{\overline{45}}$	ϕ_2^u	$\tilde{\phi}_2^u$	ϕ_3^d	$\tilde{\phi}_3^d$	ϕ_2^d	$\phi_{3'}^\nu$	ϕ_2^ν	ϕ_1^ν	η
$SU(5)$	10	10	$\bar{5}$	1	5	$\bar{5}$	$\overline{45}$	1	1	1	1	1	1	1	1	1
S_4	1	2	3	3	1	1	1	2	2	3	3	2	3'	2	1	1
$U(1)$	0	5	4	-4	0	0	1	-10	0	-4	-11	1	8	8	8	7

Yukawa
couplings

$$Y^u = \begin{pmatrix} y_1^u \lambda^8 & 0 & 0 \\ 0 & y_2^u \lambda^4 & 0 \\ 0 & 0 & y_3^u \end{pmatrix},$$

$$\lambda \approx 0.22$$

$$\frac{A^u}{A_0} = \begin{pmatrix} a_1^u \lambda^8 & 0 & 0 \\ 0 & a_2^u \lambda^4 & 0 \\ 0 & 0 & a_3^u \end{pmatrix},$$

soft SUSY
breaking
trilinears

$$Y^d = \begin{pmatrix} 0 & y_3^d \lambda^5 & -y_3^d \lambda^5 \\ -y_3^d \lambda^5 & y_1^d \lambda^4 & (y_3^d - y_1^d) \lambda^4 \\ 0 & 0 & y_2^d \lambda^2 \end{pmatrix},$$

$$\frac{A^d}{A_0} = \begin{pmatrix} 0 & a_3^d \lambda^5 & -a_3^d \lambda^5 \\ -a_3^d \lambda^5 & a_1^d \lambda^4 & (a_3^d - a_1^d) \lambda^4 \\ 0 & 0 & a_2^d \lambda^2 \end{pmatrix}$$

$$Y^e = \begin{pmatrix} 0 & -y_3^e \lambda^5 & 0 \\ y_3^e \lambda^5 & -3y_1^e \lambda^4 & 0 \\ -y_3^e \lambda^5 & (3y_1^e + y_3^e) \lambda^4 & y_2^e \lambda^2 \end{pmatrix},$$

$$\frac{A^e}{A_0} = \begin{pmatrix} 0 & -a_3^e \lambda^5 & 0 \\ a_3^e \lambda^5 & -3a_1^e \lambda^4 & 0 \\ -a_3^e \lambda^5 & (3a_1^e + a_3^e) \lambda^4 & a_2^e \lambda^2 \end{pmatrix},$$

Mass insertion parameters

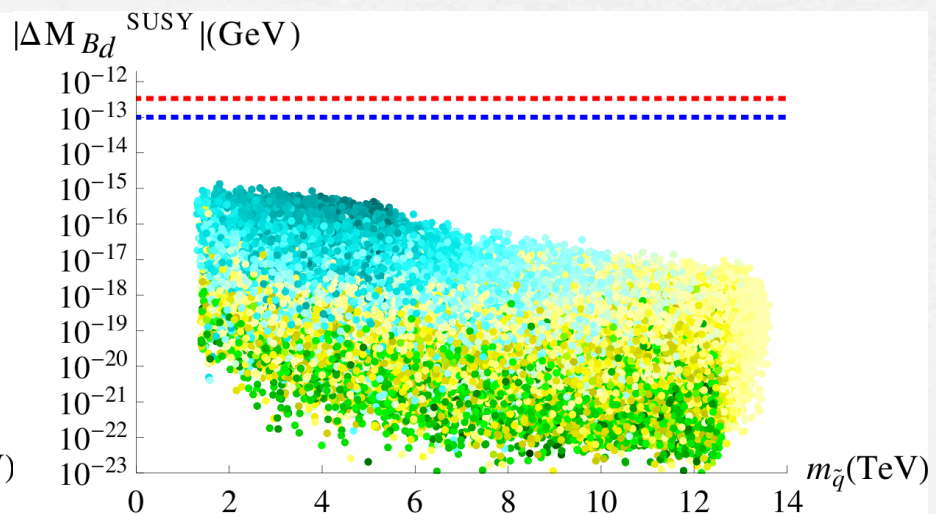
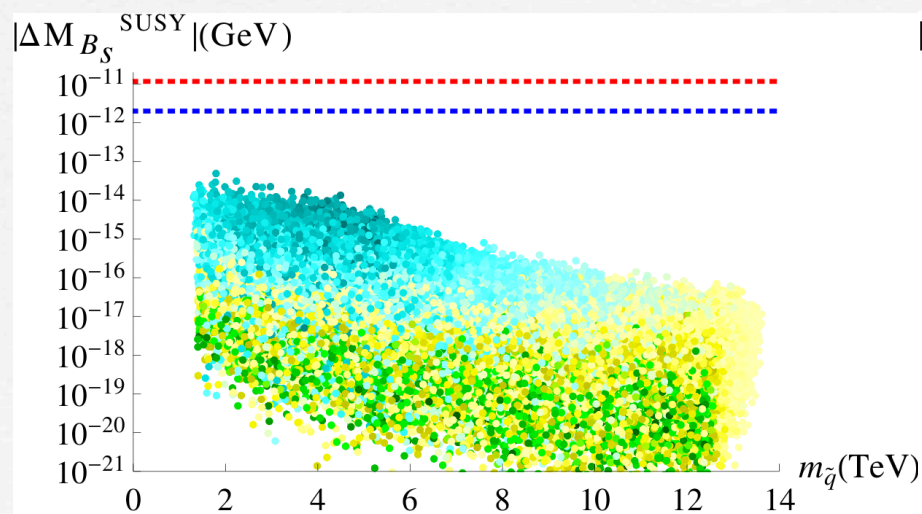
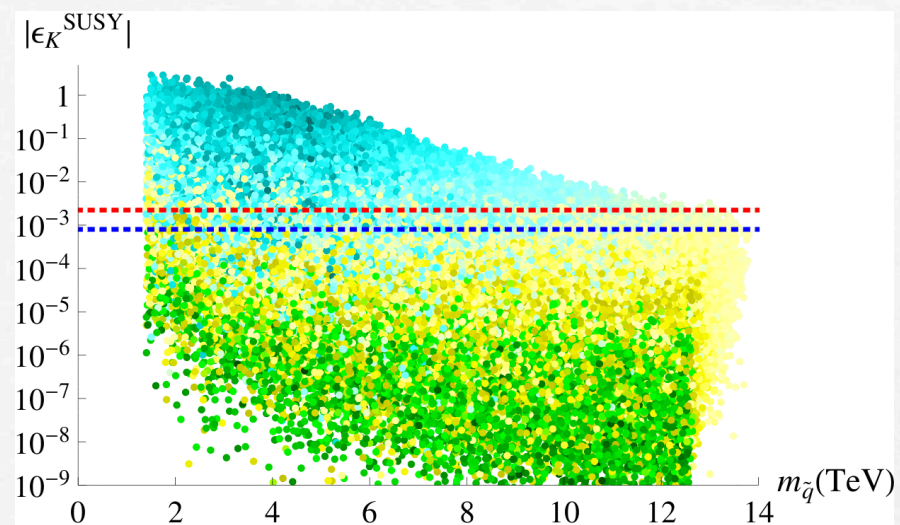
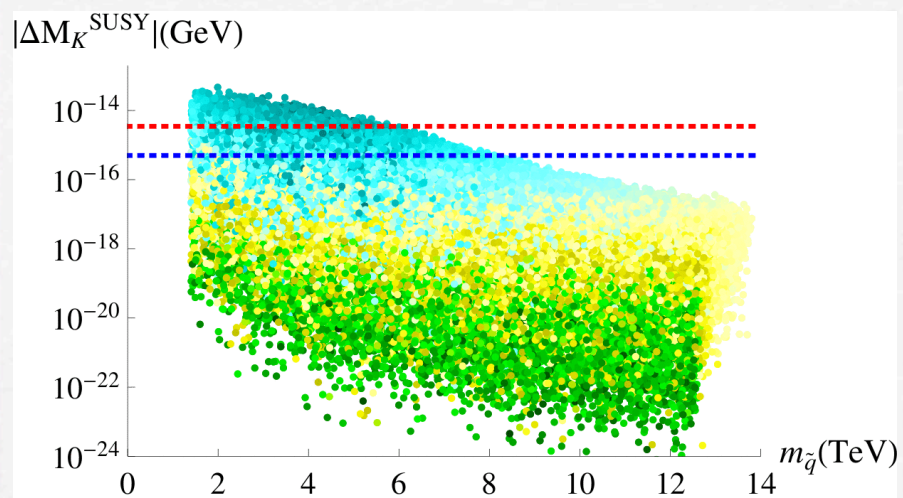
Closely resemble Minimal Flavour Violation $\lambda \approx 0.22$

$$\delta_{LL}^u \sim \begin{pmatrix} 1 & \lambda^4 & \lambda^6 \\ \cdot & 1 & \lambda^5 \\ \cdot & \cdot & 1 \end{pmatrix}, \quad \delta_{RR}^u \sim \begin{pmatrix} 1 & \lambda^4 & \lambda^6 \\ \cdot & 1 & \lambda^5 \\ \cdot & \cdot & 1 \end{pmatrix}, \quad \delta_{LR}^u \sim \begin{pmatrix} \lambda^8 & 0 & \lambda^7 \\ 0 & \lambda^4 & \lambda^6 \\ 0 & \lambda^7 & 1 \end{pmatrix},$$

$$\delta_{LL}^d \sim \begin{pmatrix} 1 & \lambda^3 & \lambda^4 \\ \cdot & 1 & \lambda^2 \\ \cdot & \cdot & 1 \end{pmatrix}, \quad \delta_{RR}^d \sim \begin{pmatrix} 1 & \lambda^4 & \lambda^4 \\ \cdot & 1 & \lambda^4 \\ \cdot & \cdot & 1 \end{pmatrix}, \quad \delta_{LR}^d \sim \begin{pmatrix} \lambda^6 & \lambda^5 & \lambda^5 \\ \lambda^5 & \lambda^4 & \lambda^4 \\ \lambda^6 & \lambda^6 & \lambda^2 \end{pmatrix},$$

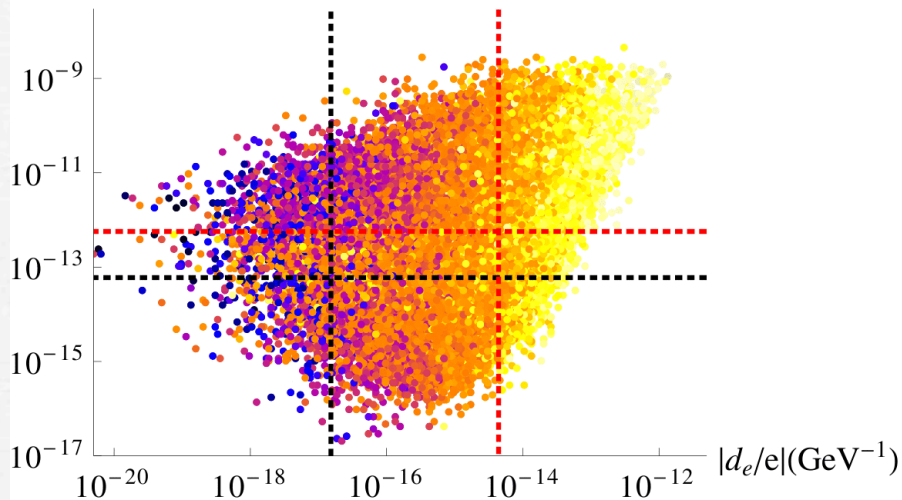
$$\delta_{LL}^e \sim \begin{pmatrix} 1 & \lambda^4 & \lambda^4 \\ \cdot & 1 & \lambda^4 \\ \cdot & \cdot & 1 \end{pmatrix}, \quad \delta_{RR}^e \sim \begin{pmatrix} 1 & \lambda^3 & \lambda^4 \\ \cdot & 1 & \lambda^2 \\ \cdot & \cdot & 1 \end{pmatrix}, \quad \delta_{LR}^e \sim \begin{pmatrix} \lambda^6 & \lambda^5 & \lambda^6 \\ \lambda^5 & \lambda^4 & \lambda^6 \\ \lambda^5 & \lambda^4 & \lambda^2 \end{pmatrix}.$$

Poster by María Dímon

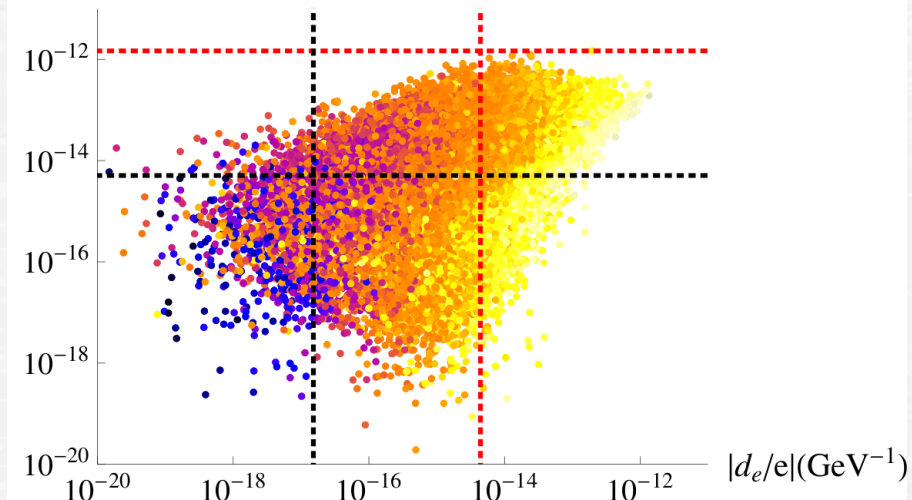


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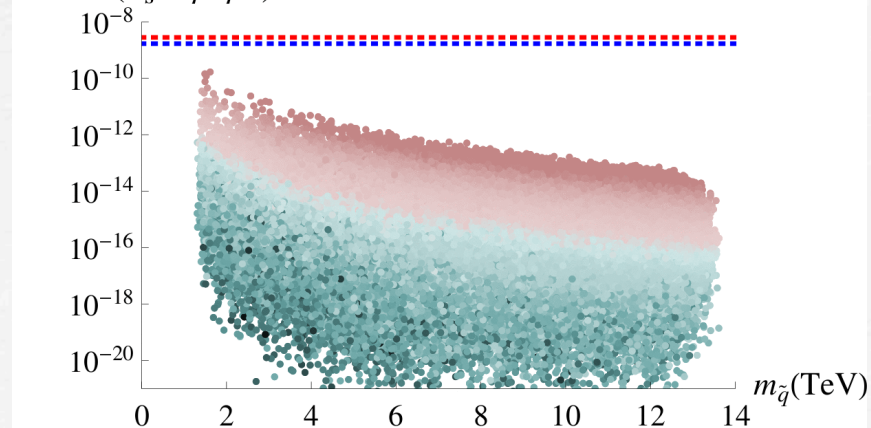
$\text{BR}(\mu \rightarrow e \gamma)$



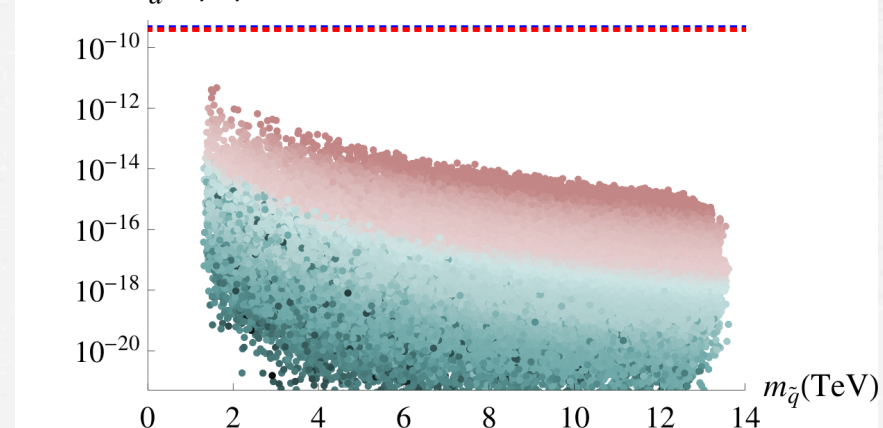
$|d_n/e|(\text{GeV}^{-1})$



$\text{BR}^{\text{SUSY}}(B_s \rightarrow \mu^+ \mu^-)$



$\text{BR}^{\text{SUSY}}(B_d \rightarrow \mu^+ \mu^-)$



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Conclusion

- The Standard Model is highly successful but leaves three questions: nu mass, unification, flavour
- Nu mass motivates RH neutrinos
- SUSY facilitates unification: $SU(5)$, $SO(10)$, E_6
- E_6 SSM allows seesaw, predicts singlet+extra matter
- We discussed E_6 SSM from F-theory to the LHC
- It has all the ingredients for 750 GeV Diphotons
- Flavour problem necessitates flavour symmetry
- We discussed $S_4 \times SU(5) \times U(1)$ with flavour predictions