

# $M$ Theory and the LHC

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Supersymmetry: From  $M$  Theory to the LHC  
Phys.Rev. D92 (2015) 5, 055011 [arXiv:1502.01727]  
and other work in progress  
MCR is supported by FCT under the grant SFRH/BD/84234/2012.

- 1 Introduction and Motivation
  - Motivation
  - Introduction to  $M$  Theory Model Building
- 2  $SO(10)$  SUSY GUTs from  $M$  Theory
- 3 Recent developments and current work [to appear]
- 4 Conclusions and future work

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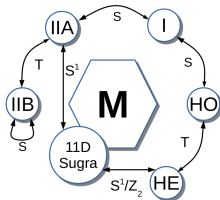
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- In the last two decades things have changed: non-perturbative regimes were found, and new corners of String/ $M$  Theory have been opened to phenomenology.

- In 1995, Witten proposed that non-perturbative limits of Type-IIA and Heterotic-E could be identified as being compactifications of a maximal  $d = 11$  Supergravity (SUGRA) Theory: **M Theory**.

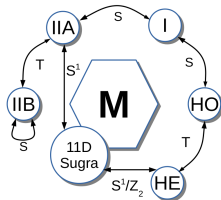
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- In  $d = 11$ ,  $M$  Theory is a maximal SUSY theory with 32 real supersymmetric charges. In order to have  $\mathcal{N} = 1$  in  $d = 4$  we have to compactify on a manifold with  $G_2$  holonomy.

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- Moduli fields are generically charged under discrete symmetries of  $K$  and acquire vevs  $\Rightarrow$  Kahler interactions with matter will generate effective superpotential terms.

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- All possible  $\mathcal{W}$  commute between them  $\Rightarrow$  each  $\mathcal{W}$  is a diagonal element of the GUT group and the breaking pattern is rank preserving.

- A convenient way of representing  $\mathcal{W}$  is

$$\mathcal{W} = \sum_m \frac{1}{m!} \left( \frac{i2\pi}{n} \sum_j a_j Q_j \right)^m ,$$

with  $Q_i$  generators of the surviving  $U(1)$  factors,  $a_j$  s.t.  $\mathcal{W}^n = 1$ .

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- Doublet-triplet problem solution for  $SU(5)$  (hep-ph/1102.0556):  
 $\mathcal{W} = \text{diag}(\eta^\delta, \eta^\delta, \eta^\delta, \eta^\gamma, \eta^\gamma), \eta^n = 1, 3\delta + 2\gamma = 0 \pmod n$

$$\bar{5} = \bar{D} \oplus H_d \rightarrow \eta^\delta \bar{D} \oplus \eta^\gamma H_d$$

with  $\mu H_u H_d$  being effectively generated by Kahler potential interactions with moduli, Giudice-Masiero mechanism

$$K \supset \frac{s}{m_{Pl}} H_u H_d + \text{h.c.} \rightarrow \mu_{\text{eff}} \sim \frac{\langle s \rangle m_{3/2}}{m_{Pl}} \sim \mathcal{O}(\text{TeV}),$$

as, in  $M$  theory,  $m_{3/2} \sim \mathcal{O}(10\text{TeV})$ ,  $\langle s \rangle \sim 0.1 m_{Pl}$ .

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- Furthermore, from usual SUGRA expressions, soft scalar masses are  $\mathcal{O}(m_{3/2}) \sim \mathcal{O}(10 \text{ TeV})$ , while  $m_{1/2} \ll \mu$  (hep-ph/0801.0478).

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- In minimal  $SO(10)$  the  $\mu$ -term is contained in

$$W \supset \mu \mathbf{10}^w \mathbf{10}^w = \mu (H_u H_d + D \bar{D}),$$

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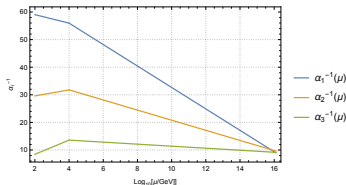
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  - The presence of light coloured states will ruin unification *as they do not form a full GUT multiplet*.
  - Moduli vevs break the discrete symmetry, leading to proton-decay interactions from Kahler interactions (c.f. Giudice-Masiero for  $\mu$  terms).

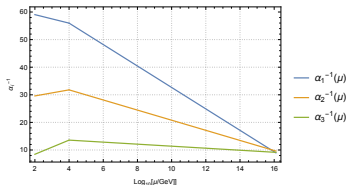
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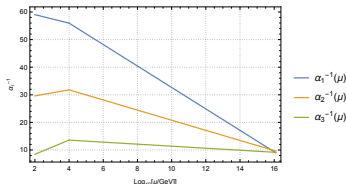


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- The addition of an extra family has other benefits for model building:  $N_X, \bar{N}_X$  vevs ( $v_X, \bar{v}_X$ ) **break the rank of the gauge group** and **generate Right-handed neutrinos Majorana masses**.

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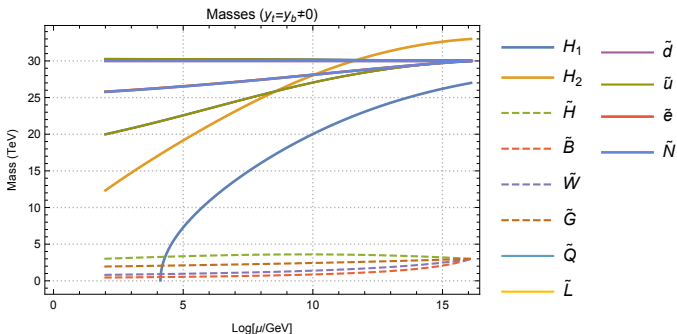
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- A (generic) RGE analysis of the spectrum with universal soft terms



- Moduli vevs generate effective terms which were otherwise forbidden by discrete symmetry

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- On the other hand, due to  $v_X \neq 0$ , relevant RPV terms are also generated, and one can find that LSP is too unstable to be a good dark matter candidate,  $\tau_{LSP} \sim 10^{-9}$  sec.
- Furthermore there is a problematic bilinear RPV contribution:

$$K \supset \frac{s}{m_{Pl}^2} N_X L H_u + \text{h.c.},$$

as see-saw requirements  $v_X \sim 10^{16}$  GeV this leads to an effective term  $\mathcal{O}(100 \text{ GeV})$  while the upper bound  $\lesssim \mathcal{O}(\text{GeV})$  (hep-ph/0004115)  $\Rightarrow$  appeal for non-generic moduli discrete charges configurations that further suppress the Kahler potential term.

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- Employ a consistent  $U(1)$  symmetry breaking mechanism.
  - We need to break the extra  $U(1)$  at the field theory level, which is a challenge task on its own.
  - How can we consolidate a high-scale vev with B-RPV bounds?

- Realistic Yukawa textures: if we consider that the UV spectrum has  $n$  **16** and  $m$   $\overline{\mathbf{16}}$ , so for  $n - m = 3$  the mass matrix

$$\mathbf{16}_i M_{ij} \overline{\mathbf{16}}_j \quad (1)$$

has at most rank= 3. Furthermore, if some of the UV states absorb Wilson line phases then the matrix will generally *not* be  $SO(10) \Rightarrow$  the light spectrum will be composed of 3 effective **16** which will not have  $SO(10)$  textures.

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- Symmetry breaking: we can employ a variation of a Kolda-Martin mechanism (Phys.Rev. D53 (1996) 3871-3883 , [hep-ph/9503445]) where  $(N_X, \overline{N}_X)$  system is aligned in the D-flat direction of the potential. In conjugation with the above solution,  $v_X$  needs not to be  $\mathcal{O}(10^{16})$  GeV any more, hence evading the dangerous B-RPV operators.

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  - Collider signatures and phenomenology of the new light-sates.

# Thank you!

# Backup slides: Hierarchy $M$ Theory

- In  $M$  Theory, moduli are stabilised and SUSY is broken by a confining hidden sector (hep-th/0701034).
- The hidden sector allows for a two chiral supermultiplets that originate a condensate,  $\phi$ , due to two gauge groups  $SU(P) \times SU(Q)$ .
- Due to axionic PQ symmetry, the hidden sector superpotential is non-perturbative

$$W_{hidd} \sim c_1 \phi^{-2/P} e^{-\sum N_i s_i 2\pi/P} + c_2 e^{-\sum N_i s_i 2\pi/Q}$$

$c_i$  are complex numbers with order 1 module,  $N_i$  are determined by the homologies of the hidden 3-cycles.

- The above construction *formally* fixes all moduli and, since

$$m_{3/2} \propto e^K |W_{hidd}|$$

hierarchy for the visible sector.

- Numerical studies with reasonable, expectable, values for parameters return  $m_{3/2} \sim \mathcal{O}(10 \text{ TeV})$ .
- Through usual SUGRA formulae, one can find the order of the values for soft terms and  $\mu$  term (Giudice-Masiero) as hidden (moduli and mesonic) fields acquire vevs.
- The gaugino GUT-scale mass is suppressed as it is (to leading order) set by the  $F$ -term of the hidden mesonic field, which can be found in  $M$  Theory to be suppressed in comparison with other vevs.

# Backup slides: Multiplet $\mathbf{10}$ don't save naive doublet-triplet splitting solution

- Consider an additional  $\mathbf{10}^h$  multiplet, without Wilson line phases:  $\mathbf{10}^h \rightarrow \eta^\xi \mathbf{10}^h$ .
- All the possible gauge invariant couplings between  $\mathbf{10}^w$  and  $\mathbf{10}^h$  are

$$W \supset \mathbf{H}_d^T \cdot \mu_H \cdot \mathbf{H}_u + \overline{\mathbf{D}}^T \cdot M_D \cdot \mathbf{D},$$

where  $\mu_H$  and  $M_D$  are two  $2 \times 2$  superpotential mass parameters matrices,  $\mathbf{H}_{u,d}^T = (H_{u,d}^w, H_{u,d}^h)$ ,  $\overline{\mathbf{D}}^T = (\overline{D}^w, \overline{D}^h)$ , and  $\mathbf{D}^T = (D^w, D^h)$ .

- **There is no choice of vanishing constraints that leaves one eigenvalue of  $\mu_H$  light while keeping both masses of  $M_D$  heavy.**

# Backup slides: RPV violating terms from the Kahler potential

- Consider the relevant Kahler potential operators

$$K \supset \frac{s}{M_{Pl}^2} DQQ + \frac{s}{M_{Pl}^2} De^c u^c + \frac{s}{M_{Pl}^2} DNd^c + \\ + \frac{s}{M_{Pl}^2} \bar{D}d^c u^c + \frac{s}{M_{Pl}^2} \bar{D}QL.$$

- The effective potential may be calculated a la Giudice-Masiero to be

$$W_{eff} \supset \lambda DQQ + \lambda De^c u^c + \lambda DNd^c + \\ + \lambda \bar{D}d^c u^c + \lambda \bar{D}QL,$$

where

$$\lambda \approx \frac{1}{M_{Pl}^2} (\langle s \rangle m_{3/2} + \langle F_s \rangle) \sim 10^{-14}.$$

- The proton-decay rate can be estimated by

$$\Gamma_p \approx \frac{|\lambda^2|^2}{16\pi^2} \frac{m_p^5}{m_D^4}.$$

- $m_D \sim \mathcal{O}(10)$  TeV, so the proton lifetime is

$$\tau_p = \Gamma_p^{-1} \sim 10^{38} \text{ yrs.}$$

- The  $D$  triplet decay rate can also be estimated

$$\tau_D = \Gamma_D^{-1} \sim (\lambda^2 m_D)^{-1} \sim 0.1 \text{ sec,}$$

which is consistent with BBN constraint.

# Backup slides: The vector-like family splitting and unification

- Such solution exists if either  $\mathbf{16}_X$  or  $\overline{\mathbf{16}}_X$  absorb Wilson line phases. Considering

$$\mathbf{16}_X \rightarrow \eta^x \left( \eta^{-3\gamma} L \oplus \eta^{3\gamma+\delta} e^c \oplus \eta^{3\gamma-\delta} N \oplus \eta^{-\gamma-\delta} u^c \oplus \right. \\ \left. \oplus \eta^{-\gamma+\delta} d^c \oplus \eta^\gamma Q \right).$$

and  $\overline{\mathbf{16}}_X \rightarrow \eta^{\bar{x}} \overline{\mathbf{16}}_X$ , the splitting condition is given by

$$\overline{d^c}_X d^c_X : x - \gamma + \delta + \bar{x} = 0 \pmod n,$$

while forbidding all the other self couplings from  $\mathbf{16}_X \overline{\mathbf{16}}_X$ .

- The remaining states of  $\mathbf{16}_X, \overline{\mathbf{16}}_X$  get a TeV scale  $\mu$ -term from moduli vevs.
- Unification scale is found to be  $M_{\text{GUT}} \sim 10^{16}$  GeV, with  $\alpha_u^{-1} \sim 9.6$ .



## Backup slides: On the extra $\mathbf{16}_X, \overline{\mathbf{16}}_X$ family

- $N_X, \overline{N}_X$  vevs ( $v_X$ ) generate Right-handed neutrinos Majorana masses that then generate a see-saw mechanism

$$\frac{1}{M_{Pl}} \overline{N}_X \overline{N}_X N^m N^m : M_{\text{Majorana}} \sim \frac{v_X^2}{M_{Pl}}$$

- There are other consequences one has to study.
  - Potential mixing with regular matter through the effective  $\mu$ -terms

$$\mu \mathbf{16}^m \overline{\mathbf{16}}_X.$$

- R-Parity violating (RPV) interactions through the Kahler terms

$$K_{RPV} \supset \frac{S}{M_{Pl}^3} \mathbf{16}_X \mathbf{16}^m \mathbf{16}^m \mathbf{16}^m + \frac{S}{M_{Pl}^2} \mathbf{10}^w \mathbf{16}_X \mathbf{16}^m.$$

## Backup slides: On the extra $\mathbf{16}_X, \overline{\mathbf{16}}_X$ family

- To study the potential mixing consider up-type quarks mass matrix.
- Schematically,  $W \supset \overline{U} \cdot M_U \cdot U$ , where  $U^T = (u_i, \overline{u}_X^c, u_X)$ ,  $\overline{U}^T = (u_i^c, \overline{u}_X, u_X^c)$ , with  $i = 1, 2, 3$ , and

$$M_U \sim \begin{pmatrix} y_u^{ij} \langle H_u \rangle & \mu_X^i & \lambda_X^i \langle H_u \rangle \\ \mu_X^j & \lambda_{\overline{X}\overline{X}} \langle H_d \rangle & \mu_{XX} \\ \lambda_X^j \langle H_u \rangle & \mu_{XX} & \lambda_{XX} \langle H_u \rangle \end{pmatrix}$$

where  $y_u$  are EWS Yukawas,  $\mu$ -terms  $\sim \mathcal{O}(\text{TeV})$ , and  $\lambda \sim \mathcal{O}(10^{-14})$ .

- In the limit  $\lambda_X^i, \lambda_X^j, \lambda_{XX}, \lambda_{\overline{X}\overline{X}} \rightarrow 0$  and  $y\nu/\mu \ll 1$ , one can find that the light states are composed of states from  $\overline{\mathbf{16}}$ , which are the ones that couple *differently* to  $Z$  and  $W^\pm$ . Therefore, neutral current and CKM unitarity are safe.
- **To leading order in  $\lambda$ s ordinary matter eigenstates do not mix matter with extra matter.**

## Backup slides: $N_X, \bar{N}_X$ vevs and RPV

- RPV interactions arise from the Kahler potential terms and are effectively described by the superpotential

$$W_{RPV} \supset \lambda \frac{v_X}{M_{Pl}} LLe^c + \lambda \frac{v_X}{M_{Pl}} QLe^c + \lambda \frac{v_X}{M_{Pl}} u^c d^c d^c + \lambda v_X LH_u.$$

which after a small rotation  $\mathcal{O}(v_X/m_{pl})$  in  $(H_d, L)$  space reads

$$W_{RPV} \supset y_e \frac{v_X}{m_{pl}} LLe^c + y_d \frac{v_X}{m_{pl}} LQd^c + \lambda \frac{v_X}{m_{pl}} u^c d^c d^c.$$

- In  $SO(10)$ , neutrinos have the same Dirac mass as the up-type quarks. A realistic  $\tau$ -neutrino physical mass requires

$$M_{\text{Majorana}} \gtrsim 10^{14} \text{ GeV} \Rightarrow v_X \sim 10^{16} \text{ GeV}.$$

- Bilinear RPV coupling is constrained by neutrino mass limits to be  $\lambda v_X \lesssim \mathcal{O}(1 \text{ GeV}) \Rightarrow v_X \lesssim 10^{14} \text{ GeV}$ , therefore we must appeal to non-generic geometrical suppression for the respective Kahler potential term.

- There is decay channel for the LSP, and its lifetime can be estimated as

$$\tau_{LSP} \simeq \frac{10^{-13} \text{ sec}}{(v_X/m_{pl})^2} \left( \frac{m_0}{10 \text{ TeV}} \right)^4 \left( \frac{100 \text{ GeV}}{m_{LSP}} \right)^5,$$

for  $m_0 \sim 10 \text{ TeV}$ ,  $m_{LSP} \sim 100 \text{ GeV}$ ,  $v_X/m_{pl} \sim 10^{-2}$  for realistic neutrino masses, one finds  $\tau_{LSP} \sim 10^{-9} \text{ sec}$ .

- **The LSP is not a good dark matter (DM) candidate. Fortunately  $M$ -theory provides axions as DM.**