

Exploring minimally flavor violating Higgs decays

Jusak Tandean

National Taiwan University

Based on

S Baek & JT, [arXiv:1604.08935](#)

XG He, JT, YJ ZHeng, [JHEP 09 \(2015\) 093 \[arXiv:1507.02673\]](#)

PASCOS 2016: 22nd International Symposium on Particles, Strings and Cosmology
XII Rencontres du Vietnam, ICISE, Quy Nhon, Vietnam

12 July 2016

Outline

- Introduction
 - Data on Higgs decays into a pair of leptons
 - Minimal flavor violation hypothesis
- Minimally flavor violating Higgs dilepton decays
- Higgs dilepton decays in GUT framework with MFV
- Conclusions

Higgs flavor-conserving dilepton decays

- Data on the flavor-conserving channels

- $\mathcal{B}(h \rightarrow e^+e^-) < 1.9 \times 10^{-3}$ at 95% CL from CMS

1410.6679

- $\mathcal{B}(h \rightarrow \mu^+\mu^-) < \begin{cases} 1.5 \times 10^{-3} & \text{at 95\% CL from ATLAS} \\ 1.6 \times 10^{-3} & \text{at 95\% CL from CMS} \end{cases}$

1406.7663, 1410.6679

- $\frac{\mathcal{B}(h \rightarrow \tau^+\tau^-)}{\mathcal{B}(h \rightarrow \tau^+\tau^-)_{\text{SM}}} = 1.12^{+0.25}_{-0.23}$ from ATLAS+CMS

ATLAS-CONF-2015-044
CMS-PAS-HIG-15-002

- For comparison, the SM predicts

- $\mathcal{B}(h \rightarrow e^+e^-) \approx 5.3 \times 10^{-9}$

- $\mathcal{B}(h \rightarrow \mu^+\mu^-) \approx 2.19 \times 10^{-4}$

- $\mathcal{B}(h \rightarrow \tau^+\tau^-) \approx 6.3\%$

- The SM predictions are consistent with the data.

Higgs flavor-changing dilepton decays

• CMS results

- $\mathcal{B}(h \rightarrow \mu\tau) = \mathcal{B}(h \rightarrow \mu^+\tau^-) + \mathcal{B}(h \rightarrow \mu^-\tau^+) = (0.84_{-0.37}^{+0.39})\%$

- $\mathcal{B}(h \rightarrow \mu\tau) < 1.51\%$ at 95% CL

1502.07400

- $\mathcal{B}(h \rightarrow e\tau) < 0.7\%$ at 95% CL

CMS PAS HIG-14-040

- $\mathcal{B}(h \rightarrow e\mu) < 0.036\%$ at 95% CL

• ATLAS results

- $\mathcal{B}(h \rightarrow \mu\tau) = (0.53 \pm 0.51)\%$

1604.07730

- $\mathcal{B}(h \rightarrow \mu\tau) < 1.43\%$ at 95% CL

- $\mathcal{B}(h \rightarrow e\tau) < 1.04\%$ at 95% CL

• A naive combination of ATLAS & CMS numbers yields $\mathcal{B}(h \rightarrow \mu\tau) = (0.73 \pm 0.31)\%$

• The minimal SM predicts no lepton flavor violation

- The tentative $h \rightarrow \mu\tau$ hint would be new physics evidence if confirmed by upcoming data.

Minimal flavor violation

- The standard model has been successful in describing the current data on flavor-changing neutral currents & CP violation in the quark sector.
- This motivates the hypothesis of minimal flavor violation for quarks: Yukawa couplings are the only sources for the breaking of flavor & CP symmetries.
 - Effective field theory approach with MFV.
- It's interesting to extend the MFV idea to the lepton sector
 - This may offer extra insights into the origin of neutrino mass
 - But there are ambiguities in implementing leptonic MFV.
- We consider an effective MFV scenario involving the type-I seesaw mechanism with degenerate heavy right-handed neutrinos.
 - MFV is imposed in both the lepton and/or quark sectors.
 - This could also work with the type-III seesaw case.

Chivukula & Georgi
Hall & Randall

Buras *et al.*
D'Ambrosio *et al.*

Cirigliano *et al.*

Davidson & Palorini
Gavela *et al.*, 2009
He, Lee, JT, Zheng

.....

Flavor symmetry in scenario with right-handed neutrinos

- ◆ The kinetic Lagrangian for SM fermions plus 3 right-handed neutrinos

$$\mathcal{L} \supset i\bar{Q}_{kL}\not{\partial}Q_{kL} + i\bar{U}_{kR}\not{\partial}U_{kR} + i\bar{D}_{kR}\not{\partial}D_{kR} + i\bar{L}_{kL}\not{\partial}L_{kL} + i\bar{\nu}_{kR}\not{\partial}\nu_{kR} + i\bar{E}_{kR}\not{\partial}E_{kR}$$

$$k = 1, 2, 3 \text{ is summed over, } \quad Q_{jL} = \begin{pmatrix} U_{jL} \\ D_{jL} \end{pmatrix}, \quad L_{jL} = \begin{pmatrix} \nu_{jL} \\ \ell_{jL} \end{pmatrix}, \quad j = 1, 2, 3$$

$$(U_1, U_2, U_3) = (u, c, t), \quad (D_1, D_2, D_3) = (d, s, b), \quad (E_1, E_2, E_3) = (\ell_1, \ell_2, \ell_3) = (e, \mu, \tau)$$

- ◆ It's **invariant** under the global flavor rotations

$$\begin{aligned} Q_{jL} &\rightarrow (V_Q)_{jk} Q_{kL}, & U_{jR} &\rightarrow (V_U)_{jk} U_{kR}, & D_{jR} &\rightarrow (V_D)_{jk} D_{kR} \\ L_{jL} &\rightarrow (V_L)_{jk} L_{kL}, & \nu_{jR} &\rightarrow (V_\nu)_{jk} \nu_{kR}, & E_{jR} &\rightarrow (V_E)_{jk} E_{kR}, & V_X &\in \text{SU}(3)_X \end{aligned}$$

- ◆ The flavor symmetry of the theory is explicitly broken by fermion mass terms

$$\begin{aligned} \mathcal{L} \supset & -(Y_u)_{jk} \bar{Q}_{jL} U_{kR} \tilde{H} - (Y_d)_{jk} \bar{Q}_{jL} D_{kR} H - (Y_e)_{jk} \bar{L}_{jL} E_{kR} H \\ & - (Y_\nu)_{jk} \bar{L}_{jL} \nu_{kR} \tilde{H} - \frac{1}{2} (M_\nu)_{jk} \bar{\nu}_{jR}^c \nu_{kR} + \text{H.c.} \end{aligned}$$

$Y_{u,d,\nu,e}$ are Yukawa matrices, H is the Higgs doublet, $\tilde{H} = i\tau_2 H^*$

$M_\nu = \mathcal{M} \text{diag}(1, 1, 1)$ is the Majorana mass matrix of degenerate ν_{kR}

- ◆ \mathcal{L} is formally flavor-symmetric if the Yukawas are spurions transforming as

$$Y_u \rightarrow V_Q Y_u V_U^\dagger, \quad Y_d \rightarrow V_Q Y_d V_D^\dagger, \quad Y_e \rightarrow V_L Y_e V_E^\dagger, \quad Y_\nu \rightarrow V_L Y_\nu \mathcal{O}_\nu^T$$

Flavor spurion combinations for MFV operators

★ We work in the basis where Y_d and Y_e are diagonal

$$Y_d = \text{diag}(y_d, y_s, y_b), \quad Y_e = \text{diag}(y_e, y_\mu, y_\tau), \quad y_f \equiv \sqrt{2} m_f / v, \quad v = 246 \text{ GeV}$$

and U_k , D_k , and E_k refer to the mass eigenstates. Thus

$$Q_{j,L} = \begin{pmatrix} (V_{\text{CKM}}^\dagger)_{jk} U_{k,L} \\ D_{j,L} \end{pmatrix}, \quad Y_u = V_{\text{CKM}}^\dagger \text{diag}(y_u, y_c, y_t), \quad L_{j,L} = \begin{pmatrix} (U_{\text{PMNS}})_{jk} \nu_{k,L} \\ E_{j,L} \end{pmatrix}$$

$$Y_\nu = \frac{i\sqrt{2}}{v} U_{\text{PMNS}} \hat{m}_\nu^{1/2} O M_\nu^{1/2} \quad \text{with } OO^T = \mathbb{1} \text{ and } M_\nu = \mathcal{M} \text{diag}(1, 1, 1)$$

Casas & Ibarra

$m_\nu = \text{diag}(m_1, m_2, m_3)$ is the mass matrix of light ν s

★ The Yukawa combinations of interest

$$\mathbf{A}_q = Y_u Y_u^\dagger = V_{\text{CKM}}^\dagger \text{diag}(y_u^2, y_c^2, y_t^2) V_{\text{CKM}}, \quad \mathbf{B}_q = Y_d Y_d^\dagger = \text{diag}(y_d^2, y_s^2, y_b^2)$$

$$\mathbf{A}_\ell = Y_\nu Y_\nu^\dagger = \frac{2\mathcal{M}}{v^2} U_{\text{PMNS}} \hat{m}_\nu^{1/2} O O^\dagger \hat{m}_\nu^{1/2} U_{\text{PMNS}}^\dagger, \quad \mathbf{B}_\ell = Y_e Y_e^\dagger = \text{diag}(y_e^2, y_\mu^2, y_\tau^2)$$

★ Since $y_t^2 \gg y_b^2$, and sufficiently large \mathcal{M} is chosen so that $|(\mathbf{B}_\ell)_{jk}| \ll |(\mathbf{A}_\ell)_{jk}| \lesssim 1$, in our model-independent approach the pertinent spurion building blocks are

$$\Delta_q = \zeta_1 \mathbb{1} + \zeta_2 \mathbf{A}_q + \zeta_4 \mathbf{A}_q^2, \quad \Delta_\ell = \xi_1 \mathbb{1} + \xi_2 \mathbf{A}_\ell + \xi_4 \mathbf{A}_\ell^2$$

Colangelo, Mercolli, Smith

$\zeta_{1,2,4}$ and $\xi_{1,2,4}$ are free parameters at most of $\mathcal{O}(1)$ with negligible imaginary parts.

Hence $\Delta_q \rightarrow V_Q \Delta_q V_Q^\dagger$, $\Delta_\ell \rightarrow V_L \Delta_\ell V_L^\dagger$

Effective Lagrangian with MFV

- The effective operators need to be invariant under the flavor rotations and SM gauge symmetry.

- Effective dimension-6 MFV operators involving leptons & H

$$\mathcal{L}_{\text{MFV}} \supset \frac{1}{\Lambda^2} \left(O_{RL}^{(e1)} + O_{RL}^{(e2)} + O_{RL}^{(e3)} + O_{RL}^{(e4)} + O_{LL}^{(1)} + O_{LL}^{(2)} + \text{H.c.} \right) + \dots$$

Λ is the scale of MFV,

$$O_{RL}^{(e1)} = g' \bar{E}_R Y_e^\dagger \Delta_{RL}^{(1)} \sigma_{\rho\omega} H^\dagger L_L B^{\rho\omega}$$

$$O_{RL}^{(e2)} = g \bar{E}_R Y_e^\dagger \Delta_{RL}^{(2)} \sigma_{\rho\omega} H^\dagger \tau_a L_L W_a^{\rho\omega}$$

$$O_{RL}^{(e3)} = (\mathcal{D}^\rho H)^\dagger \bar{E}_R Y_e^\dagger \Delta_{RL}^{(3)} \mathcal{D}_\rho L_L$$

$$O_{LL}^{(1)} = \frac{i}{4} [H^\dagger (\mathcal{D}_\rho H) - (\mathcal{D}_\rho H)^\dagger H] \bar{L}_L \gamma^\rho \Delta_{LL}^{(1)} L_L,$$

$$O_{LL}^{(2)} = \frac{i}{4} [H^\dagger \tau_a (\mathcal{D}_\rho H) - (\mathcal{D}_\rho H)^\dagger \tau_a H] \bar{L}_L \gamma^\rho \tau_a \Delta_{LL}^{(2)} L_L$$

generalized from
D'Ambrosio *et al.*
Cirigliano *et al.*

- $\Delta_{RL}^{(1,2,3)}$ and $\Delta_{LL}^{(1,2)}$ are the same in form as Δ_ℓ , but have their own coefficients ξ_r

- If MFV is also imposed in the quark sector, it has an analogous Lagrangian.

$$\star \mathcal{L}_{\text{MFV}} \supset \frac{O_{RL}^{(e3)}}{\Lambda^2} + \text{H.c.}, \quad O_{RL}^{(e3)} = (\mathcal{D}^\rho H)^\dagger \bar{E}_R Y_e^\dagger \Delta \mathcal{D}_\rho L_L$$

$$\star \text{Alternative } h \rightarrow \ell \bar{\ell}' \text{ operator: } H^\dagger H \bar{E}_{jR} H^\dagger L_{kL}$$

★ They are related

$$\begin{aligned} O_{RL}^{(e3)} + \text{H.c.} = & \frac{i}{8} \left[H^\dagger \mathcal{D}_\rho H - (\mathcal{D}_\rho H)^\dagger H \right] \left(\bar{L}_L \gamma^\rho \{ \Delta, Y_e Y_e^\dagger \} L_L + 4 \bar{E}_R \gamma^\rho Y_e^\dagger \Delta Y_e E_R \right) \\ & + \frac{i}{8} \left[H^\dagger \tau_a \mathcal{D}_\rho H - (\mathcal{D}_\rho H)^\dagger \tau_a H \right] \bar{L}_L \gamma^\rho \{ \Delta, Y_e Y_e^\dagger \} \tau_a L_L \\ & + \frac{i}{8} \left[H^\dagger \mathcal{D}_\rho H + (\mathcal{D}_\rho H)^\dagger H \right] \bar{L}_L \gamma^\rho [\Delta, Y_e Y_e^\dagger] L_L \\ & + \frac{i}{8} \left[H^\dagger \tau_a \mathcal{D}_\rho H + (\mathcal{D}_\rho H)^\dagger \tau_a H \right] \bar{L}_L \gamma^\rho [\Delta, Y_e Y_e^\dagger] \tau_a L_L \\ & + \frac{1}{8} \left[\left(\frac{4H^\dagger H}{v^2} - 2 \right) m_h^2 \bar{E}_R Y_e^\dagger \Delta H^\dagger L_L + 4 \bar{L}_L Y_e E_R \bar{E}_R Y_e^\dagger \Delta L_L \right. \\ & \quad \left. + \bar{E}_R Y_e^\dagger \Delta \sigma_{\rho\omega} H^\dagger (g' B^{\rho\omega} + g \tau_a W_a^{\rho\omega}) L_L + \text{H.c.} \right] \\ & + (\text{quark terms}) \end{aligned}$$

- ◆ Effective Lagrangian satisfying MFV criterion

$$\mathcal{L}_{\text{MFV}} \supset \frac{1}{\Lambda^2} (\mathcal{D}^\alpha H)^\dagger \bar{E}_R Y_e^\dagger \Delta_\ell \mathcal{D}_\alpha L_L$$

Λ is the MFV scale, $\Delta_\ell = \xi_1 \mathbb{1} + \xi_2 \mathbf{A}_\ell + \xi_4 \mathbf{A}_\ell^2$

$\xi_{1,2,4}$ are free parameters at most of $\mathcal{O}(1)$

- ◆ Effective Lagrangian describing $h \rightarrow f \bar{f}'$

$$\mathcal{L}_{h f \bar{f}'} = -\bar{f} (\mathcal{Y}_{f' f}^* P_L + \mathcal{Y}_{f f'} P_R) f' h$$

Decay rate $\Gamma_{h \rightarrow f \bar{f}'} = \frac{m_h}{16\pi} (|\mathcal{Y}_{f f'}|^2 + |\mathcal{Y}_{f' f}|^2)$

- ◆ Combined SM and \mathcal{L}_{MFV} contribution to $h \rightarrow E_k^- E_l^+$

$$\mathcal{Y}_{E_k E_l} = \delta_{kl} \mathcal{Y}_{E_k E_k}^{\text{SM}} - \frac{m_{E_l} m_h^2}{2\Lambda^2 v} (\Delta_\ell)_{kl}, \quad \mathcal{Y}_{E_k E_k}^{\text{SM}} = \frac{m_{E_k}}{v}$$

Constraints on leptonic Yukawa couplings

- Indirect limit from new MEG data $\mathcal{B}(\mu \rightarrow e\gamma) < 4.2 \times 10^{-13}$

1605.05081

$$\sqrt{|(\mathcal{Y}_{\mu\mu} + r_\mu)\mathcal{Y}_{\mu e} + 9.19\mathcal{Y}_{\mu\tau}\mathcal{Y}_{\tau e}|^2 + |(\mathcal{Y}_{\mu\mu} + r_\mu)\mathcal{Y}_{e\mu} + 9.19\mathcal{Y}_{e\tau}\mathcal{Y}_{\tau\mu}|^2} < 4.4 \times 10^{-7}$$

$$r_\mu = 0.29$$

Goudelis, Lebedev, Park
Blankenburg, Ellis, Isidori
Harnik, Kopp, Zupan
Dery *et al.*

- From LHC data on $h \rightarrow \mu^+\mu^-, \tau^+\tau^-$

$$|\mathcal{Y}_{\mu\mu}/\mathcal{Y}_{\mu\mu}^{\text{SM}}|^2 < 6.5, \quad 0.9 < |\mathcal{Y}_{\tau\tau}/\mathcal{Y}_{\tau\tau}^{\text{SM}}|^2 < 1.4$$

- CMS data on $h \rightarrow \mu\tau$

$$2.0 \times 10^{-3} < \sqrt{|\mathcal{Y}_{\tau\mu}|^2 + |\mathcal{Y}_{\mu\tau}|^2} < 3.3 \times 10^{-3}$$

1502.07400

- CMS data on $h \rightarrow e\mu, e\tau$

$$\sqrt{|\mathcal{Y}_{e\mu}|^2 + |\mathcal{Y}_{\mu e}|^2} < 5.43 \times 10^{-4}, \quad \sqrt{|\mathcal{Y}_{e\tau}|^2 + |\mathcal{Y}_{\tau e}|^2} < 2.41 \times 10^{-3}$$

CMS PAS HIG-14-040

- ★ In the SM plus 3 degenerate heavy right-handed neutrinos

$$\Delta_\ell = \xi_1 \mathbb{1} + \xi_2 \mathbf{A}_\ell + \xi_4 \mathbf{A}_\ell^2, \quad \mathbf{A}_\ell = Y_\nu Y_\nu^\dagger = \frac{2\mathcal{M}}{v^2} U_{\text{PMNS}} \hat{m}_\nu^{1/2} \mathbf{O} \mathbf{O}^\dagger \hat{m}_\nu^{1/2} U_{\text{PMNS}}^\dagger$$

$$M_\nu = \mathcal{M} \text{diag}(1, 1, 1)$$

- ★ If \mathbf{O} in Y_ν is real, $|\mathcal{Y}_{\mu\tau}|$ can only reach $\sim 2 \times 10^{-4} \ll |\mathcal{Y}_{\mu\tau}^{\text{CMS}}| \sim 3 \times 10^{-3}$

- ★ To attain $|\mathcal{Y}_{\mu\tau}^{\text{CMS}}|$, less simple structure of Y_ν is needed, particularly with

complex \mathbf{O} so that $\mathbf{O} \mathbf{O}^\dagger = e^{2i\mathbf{R}}$ with $\mathbf{R} = \begin{pmatrix} 0 & r_1 & r_2 \\ -r_1 & 0 & r_3 \\ -r_2 & -r_3 & 0 \end{pmatrix}$ and real $r_{1,2,3}$

	$\frac{\alpha_1}{\pi}$	$\frac{\alpha_2}{\pi}$	r_1	r_2	r_3	$10^5 \xi_1 / \Lambda^2$ (GeV ⁻²)	$10^5 \xi_2 / \Lambda^2$ (GeV ⁻²)	$10^5 \xi_4 / \Lambda^2$ (GeV ⁻²)	$\frac{\mathcal{Y}_{ee}}{\mathcal{Y}_{ee}^{\text{SM}}}$	$\frac{\mathcal{Y}_{\mu\mu}}{\mathcal{Y}_{\mu\mu}^{\text{SM}}}$	$\frac{\mathcal{Y}_{\tau\tau}}{\mathcal{Y}_{\tau\tau}^{\text{SM}}}$	$\frac{ \mathcal{Y}_{e\mu} }{10^{-6}}$	$\frac{ \mathcal{Y}_{e\tau} }{10^{-4}}$	$\frac{ \mathcal{Y}_{\mu\tau} }{10^{-3}}$
NH	0	0	0.81	-1.6	-0.89	-7.5	6.4	5.8	1.6	1.3	0.95	1.0	0.1	3.2
	0	0	-0.90	1.8	-0.92	-8.4	6.0	7.1	1.7	1.3	0.97	1.4	0.4	3.5
	0	0.23	0.74	-0.80	-0.23	7.0	-5.3	-7.5	0.46	0.77	1.15	1.5	1.7	3.3
IH	0	0	0.04	0.63	-0.93	-7.9	8.8	3.0	1.5	1.2	1.08	2.3	2.9	3.3
	0	0	0.02	-0.75	1.1	-6.2	3.7	7.7	1.4	1.1	0.97	2.2	1.2	3.2
	0.79	1.3	-0.61	-0.79	1.4	-6.8	5.0	7.6	1.5	1.0	0.96	1.2	0.4	3.5

Leptonic Yukawa couplings for sample values of the Majorana phases $\alpha_{1,2}$, parameters $r_{1,2,3}$ of the complex O matrix, and coefficients $\xi_{1,2,4}$ in the MFV matrix Δ which can yield $|\mathcal{Y}_{\mu\tau}| \gtrsim 3 \times 10^{-3}$, corresponding to measured neutrino mixing parameters for the normal (NH) or inverted (IH) hierarchy of neutrino masses.

★ In these instances $\mathcal{B}(\mu \rightarrow e\gamma) = (1.8 - 4.3) \times 10^{-13}$, $\mathcal{B}(\mu\text{Al} \rightarrow e\text{Al}) = (2.3 - 8.2) \times 10^{-15}$

- $|\mathcal{Y}_{\mu\tau}|/|\mathcal{Y}_{e\tau}| \sim 10$ or more, consistent with CMS $h \rightarrow e\tau, \mu\tau$ results
- The $\mathcal{Y}_{\mu\mu}$ and $\mathcal{Y}_{\tau\tau}$ predictions are testable with future collider data
- MEG II may probe the $\mu \rightarrow e\gamma$ predictions more stringently

Grand unification with MFV

- In grand unified theories, quarks & leptons appear in the same representations.
- In the Georgi-Glashow GUT based on the SU(5) gauge group

$$\bar{5} : \psi_k = \begin{pmatrix} (D_{k,R}^1)^c \\ (D_{k,R}^2)^c \\ (D_{k,R}^3)^c \\ E_{k,L} \\ -\nu_{k,L} \end{pmatrix}, \quad 10 : \chi_k = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 & (U_{k,R}^3)^c & -(U_{k,R}^2)^c & -U_{k,L}^1 & -D_{k,L}^1 \\ -(U_{k,R}^3)^c & 0 & (U_{k,R}^1)^c & -U_{k,L}^2 & -D_{k,L}^2 \\ (U_{k,R}^2)^c & -(U_{k,R}^1)^c & 0 & -U_{k,L}^3 & -D_{k,L}^3 \\ U_{k,L}^1 & U_{k,L}^2 & U_{k,L}^3 & 0 & -(E_{k,R})^c \\ D_{k,L}^1 & D_{k,L}^2 & D_{k,L}^3 & (E_{k,R})^c & 0 \end{pmatrix}, \quad k = 1, 2, 3$$

◆ Fermion mass Lagrangian

$$\begin{aligned} \mathcal{L}_m^{\text{GUT}} = & (\lambda_5)_{kl} \psi_k^T \chi_l H_5^* + (\lambda_{10})_{kl} \chi_k^T \chi_l H_5 + \frac{(\lambda'_5)_{kl}}{M_P} \psi_k^T \Sigma_{24} \chi_l H_5^* \\ & + (\lambda_1)_{kl} \nu_{k,R}^T \psi_l H_5 - \frac{1}{2} (M_\nu)_{kl} \nu_{k,R}^T \nu_{l,R} + \text{H.c.} \end{aligned}$$

Ellis & Gaillard

the λ s are Yukawa matrices

$$Y_u^\dagger \propto \lambda_{10}, \quad Y_d^\dagger \propto \lambda_5 + \epsilon \lambda'_5, \quad Y_e^* \propto \lambda_5 - \frac{3}{2} \epsilon \lambda'_5, \quad Y_\nu^\dagger = \lambda_1, \quad \epsilon = \frac{M_{\text{GUT}}}{M_P} \ll 1$$

H_5 and Σ_{24} are Higgses in the 5 and 24 of SU(5), the Planck scale $M_P \gg M_{\text{GUT}}$

- $\mathcal{L}_m^{\text{GUT}}$ is formally flavor-symmetric if the fields & Yukawas transform as

Grinstein *et al.*

$$\begin{aligned} \psi &\rightarrow V_{\bar{5}} \psi, & \chi &\rightarrow V_{10} \chi, & \nu_R &\rightarrow \mathcal{O}_1 \nu_R, & V_{\bar{5},10} &\in \text{SU}(3)_{\bar{5},10} \\ \lambda_5^{(\prime)} &\rightarrow V_{\bar{5}}^* \lambda_5^{(\prime)} V_{10}^\dagger, & \lambda_{10} &\rightarrow V_{10}^* \lambda_{10} V_{10}^\dagger, & \lambda_1 &\rightarrow \mathcal{O}_1 \lambda_1 V_{\bar{5}}^\dagger, & \mathcal{O}_1 &\in \text{O}(3)_1 \end{aligned}$$

SU(5) GUT with MFV

- The effective new-physics Lagrangian contributing to $h \rightarrow f'f$ need to be symmetric under the flavor group $SU(3)_5 \otimes SU(3)_{10} \otimes O(3)_1$ and also SM gauge invariant.

- Flavor rotation properties of fermion fields and Yukawa spurions in $\mathcal{L}_m^{\text{GUT}}$

$$\begin{aligned}
 Q_L &\rightarrow V_{10} Q_L, & U_R &\rightarrow V_{10}^* U_R, & D_R &\rightarrow V_{\bar{5}}^* D_R, & L_L &\rightarrow V_{\bar{5}} L_L, & E_R &\rightarrow V_{10}^* E_R \\
 Y_u &\rightarrow V_{10} Y_u V_{10}^T, & Y_d &\rightarrow V_{10} Y_d V_{\bar{5}}^T, & Y_e &\rightarrow V_{\bar{5}} Y_e V_{10}^T, & Y_\nu &\rightarrow V_{\bar{5}} Y_\nu \mathcal{O}_1^T
 \end{aligned}$$

Grinstein et al.

- Effective Lagrangian satisfying MFV criterion $\mathcal{L}_{\text{MFV}}^{\text{GUT}} \supset \frac{\tilde{\mathcal{O}}}{\Lambda^2} + \text{H.c.}$

$$\tilde{\mathcal{O}} = (\mathcal{D}^\eta H)^\dagger \bar{E}_R \left(Y_e^\dagger \Delta_{\ell 1} + Y_d^* \Delta_{\ell 2} + \Delta_{q1}^T Y_d^* + \Delta_{q2}^T Y_e^\dagger + \Delta_{q3}^T Y_e^\dagger \Delta_{\ell 3} + \Delta_{q4}^T Y_d^* \Delta_{\ell 4} \right) \mathcal{D}_\eta L_L$$

$$\Delta_{qj} \sim \Delta_q = \zeta_1 \mathbb{1} + \zeta_2 \mathbf{A}_q + \zeta_4 \mathbf{A}_q^2 \rightarrow V_{10} \Delta_q V_{10}^\dagger, \quad \mathbf{A}_q = Y_u Y_u^\dagger$$

$$\Delta_{\ell j} \sim \Delta_\ell = \xi_1 \mathbb{1} + \xi_2 \mathbf{A}_\ell + \xi_4 \mathbf{A}_\ell^2 \rightarrow V_{\bar{5}} \Delta_\ell V_{\bar{5}}^\dagger, \quad \mathbf{A}_\ell = Y_\nu Y_\nu^\dagger$$

Yukawa couplings

★ In the mass-eigenstate basis

$$\tilde{\mathcal{O}} \supset \frac{\partial^n h}{\sqrt{2} \Lambda^2} \bar{E}_R \left(Y_e \Delta_{\ell 1} + \mathbf{C}^* Y_d \mathbf{G}^T \Delta_{\ell 2} + \mathbf{C}^* \Delta_{q 1}^T Y_d \mathbf{G}^T + \mathbf{C}^* \Delta_{q 2}^T \mathbf{C}^T Y_e \right. \\ \left. + \mathbf{C}^* \Delta_{q 3}^T \mathbf{C}^T Y_e \Delta_{\ell 3} + \mathbf{C}^* \Delta_{q 4}^T Y_d \mathbf{G}^T \Delta_{\ell 4} \right) \partial_\eta E_L$$

now $Y_d = \text{diag}(y_d, y_s, y_b)$, $Y_e = \text{diag}(y_e, y_\mu, y_\tau)$, $\mathbf{C} = \mathbf{V}_{eR}^T \mathbf{V}_{dL}$, $\mathbf{G} = \mathbf{V}_{eL}^T \mathbf{V}_{dR}$

$\mathbf{V}_{dL,dR}$ ($\mathbf{V}_{eL,eR}$) diagonalize Y_d (Y_e)

★ \mathbf{C} & \mathbf{G} appear because the nondiagonal $Y_d \propto (\lambda_5 + \epsilon \lambda'_5)^\dagger \not\propto Y_e^T \propto (\lambda_5 - \frac{3}{2} \epsilon \lambda'_5)^\dagger$

★ Since \mathbf{C} & \mathbf{G} are unknown, for simplicity one may roughly adopt $\mathbf{C} = \mathbf{G} = \mathbf{1}$ Grinstein et al.

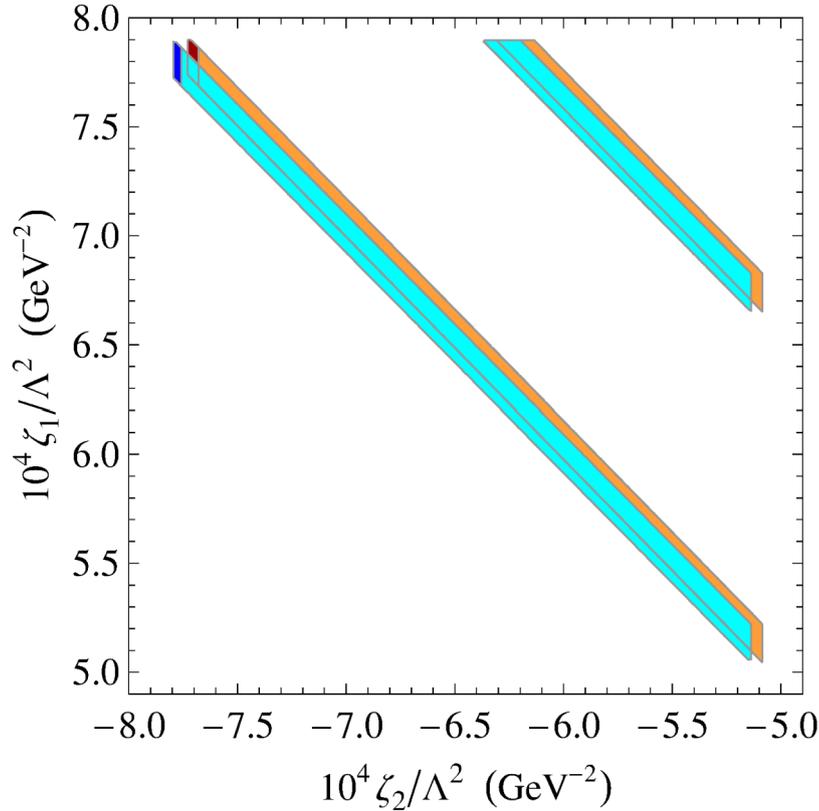
in which case the $\mathcal{L}_{\text{MFV}}^{\text{GUT}}$ contributions to $h \rightarrow E_k^- E_l^+$ are

$$\mathcal{Y}_{E_k E_l} - \delta_{kl} \mathcal{Y}_{E_k E_k}^{\text{SM}} = \frac{-m_h^2}{2\Lambda^2 v} \left[(\Delta_{\ell 1})_{kl} m_{E_l} + (\Delta_{\ell 2})_{kl} m_{D_l} + m_{D_k} (\Delta_{q 1})_{lk} + m_{E_k} (\Delta_{q 2})_{lk} \right. \\ \left. + (\Delta_{\ell 3} \hat{M}_e \Delta_{q 3}^T)_{kl} + (\Delta_{\ell 4} \hat{M}_d \Delta_{q 4}^T)_{kl} \right]$$

An interesting case

- Δ_{q1} contributing, the other Δ s absent

$$\Delta_q = \zeta_1 \mathbb{1} + \zeta_2 \mathbf{A}_q + \zeta_4 \mathbf{A}_q^2$$



Regions of $(\zeta_1, \zeta_2)/\Lambda^2$ (cyan and dark blue) which satisfy the empirical constraints if the Δ_{q1} term is the only new-physics contribution in $\mathcal{Y}_{ff'}$ and $\zeta_4 = 0$. For the orange and dark red regions, the roles of ζ_2 and ζ_4 are interchanged. The dark (blue and red) patches correspond to $|\mathcal{Y}_{\tau\mu}| \simeq 0.003$ and hence $\mathcal{B}(h \rightarrow \mu\tau) \simeq 1\%$.

These contributions are determined mainly by the CKM parameters & quark masses

$\frac{\mathcal{Y}_{ee}}{\mathcal{Y}_{ee}^{\text{SM}}}$	$\frac{\mathcal{Y}_{\mu\mu}}{\mathcal{Y}_{\mu\mu}^{\text{SM}}}$	$\frac{\mathcal{Y}_{\tau\tau}}{\mathcal{Y}_{\tau\tau}^{\text{SM}}}$	$\frac{\mathcal{Y}_{\mu e}}{10^{-7}}$	$\frac{\mathcal{Y}_{\tau e}}{10^{-4}}$	$\frac{\mathcal{Y}_{\tau\mu}}{10^{-3}}$	$\mathcal{B}(\mu \rightarrow e\gamma)$	$\mathcal{B}(\mu\text{Al} \rightarrow e\text{Al})$
-34	-2.5	1.1	$-4.8 - 2.0i$	$5.9 + 2.4i$	$-3.0 + 0.06i$	5.4×10^{-13}	2.6×10^{-15}
-28	-1.9	1.2	$-4.0 - 1.7i$	$4.9 + 2.0i$	$-2.5 + 0.05i$	2.9×10^{-13}	1.5×10^{-15}
-24	-1.5	0.95	$-3.3 - 1.4i$	$4.1 + 1.7i$	$-2.1 + 0.04i$	1.6×10^{-13}	9.1×10^{-16}

Conclusions

- Experimental quests for charged-lepton flavor violation offer excellent probes for many models.
- We have explored the flavor-changing decays of the Higgs boson into charged leptons in the MFV framework based on the SM extended with the addition of right-handed neutrinos plus effective dimension-6 operators and **in its SU(5) GUT counterpart**.
- The non-GUT framework involving the type-I (or type-III) seesaw mechanism can accommodate the recent tentative hint of $h \rightarrow \mu\tau$ from the LHC with $\mathcal{B}(h \rightarrow \mu\tau) \sim 1\%$ if the right-handed neutrinos have nontrivial couplings to the Higgs boson.
- In the SU(5) GUT case, there can be instances in which $\mathcal{B}(h \rightarrow \mu\tau) \sim 1\%$ is **achievable** with contributions depending mainly on known quark parameters and the predictions on other lepton-flavor-violating processes, such as $\mu \rightarrow e\gamma$, are potentially testable by upcoming searches.