

# Charged Lepton Flavor Violation

SATO, Joe  
(Saitama University)

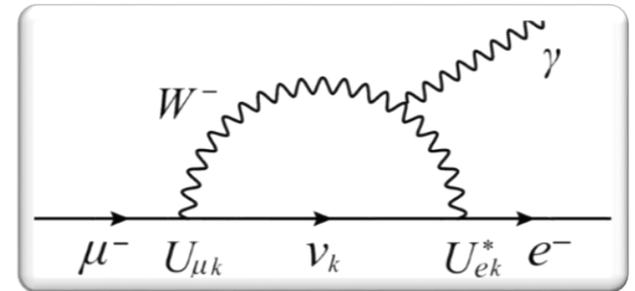
July14 Quy Nhon Vietnam

# 1. Introduction

## Lepton Flavor is exact symmetry in SM

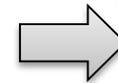
as long as neutrinos are massless

Charged Lepton Flavor Violation  
(cLFV) through Lepton Mixing  
in the neutrino oscillation



But ...

$$\text{BR}(\mu \rightarrow e\gamma) \sim \left( \frac{\delta m_\nu^2}{m_W^2} \right)^2 < 10^{-54}$$



Invisible, eternally

Strong suppression of FCNC by GIM

Detection of the LFV signal



Clear evidence for beyond SM

Indeed, in physics beyond SM,

**Large FCNC** is expected

Particularly Combining with neutrino oscillation

Large FCNC in charged lepton is expected

(must appear ??)

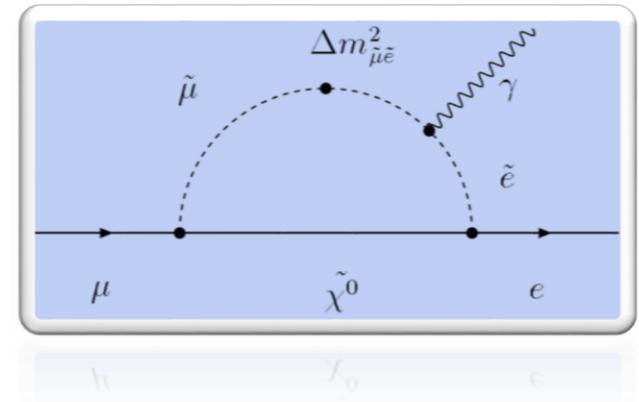
*e.g.* a supersymmetric model

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Enhancement of LFV  
through the slepton mixing

➔ Detectable at future experiments

➔ **Search for LFV with charged lepton  
is inevitable**



# cLFV from muon decay

Upper limit on Br

$$\mu^+ \rightarrow e^+ \gamma < 4.2 \times 10^{-13}$$

$$\mu^+ \rightarrow e^+ e^+ e^- < 1.0 \times 10^{-12}$$

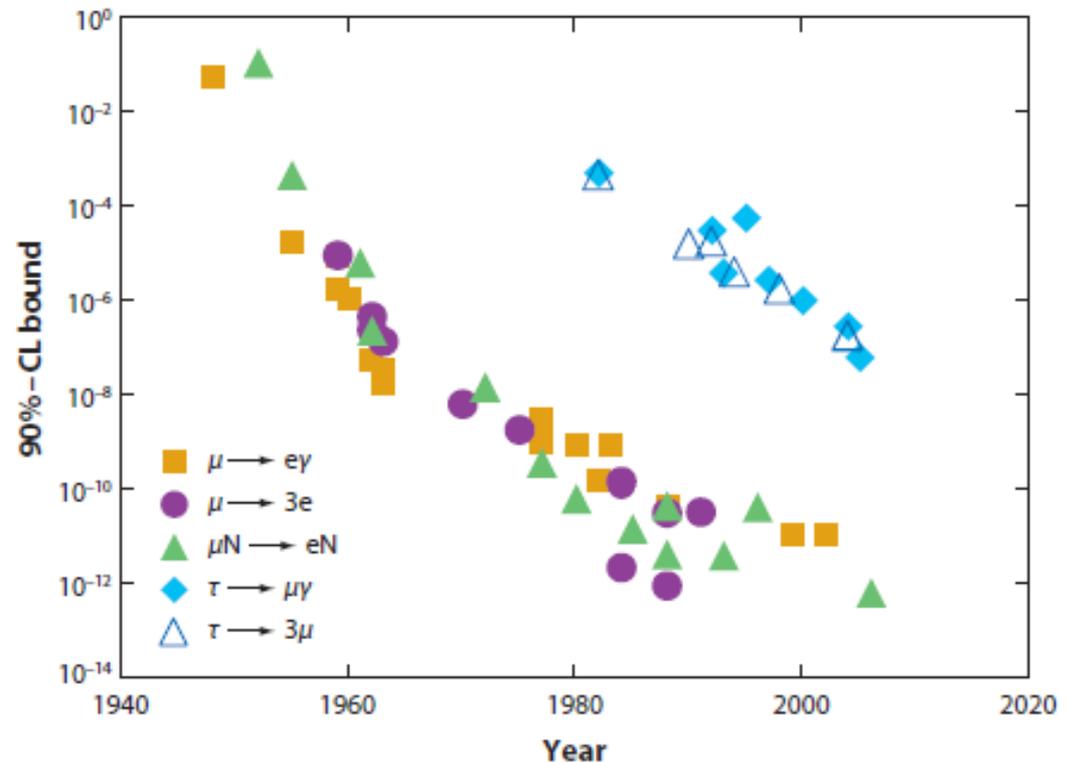
$$\mu^- \text{Ti} \rightarrow e^- \text{Ti} < 6.1 \times 10^{-13}$$

$$\mu^- \text{Au} \rightarrow e^- \text{Au} < 7 \times 10^{-13}$$

$$\mu^+ e^- \rightarrow \mu^- e^+ < 8.3 \times 10^{-11}$$

Annu. Ref. Nucl. Part. Sci. 2008. 58:315-41  
W. J. Marciano, T. Mori, and J. M. Roney

Long history





## (New?) particle with LFV

### SM Particle

$$Z \rightarrow ll' < O(10^{-6}) \text{ for } e\mu, O(10^{-5}) \text{ for } l\tau$$

$$H \rightarrow ll' < O(1\%)$$

or  $\text{Br}(H \rightarrow \mu\tau) = 0.84 \pm 0.39\%$

### New(?) Particle with LFV

$Z'$  from Extra dim/extra U(1) models

Neutral scalar, e.g. scalar neutrino in SSM

**No signals yet even with LHC**

## 2. Effective operators for CLFV

### A) Loop vs Tree

$$\mu^+ \rightarrow e^+ \gamma \quad :: \text{Loop only, dipole}$$

Gauge Symmetry forbids tree contribution

$$\mu^+ \rightarrow e^+ e^- e^+ \quad :: \text{Loop and Tree}$$

$$\mu^- N \rightarrow e^- N$$

e.g. Loop = dipole + quark bilinear =  $\mu^- N \rightarrow e^- N$

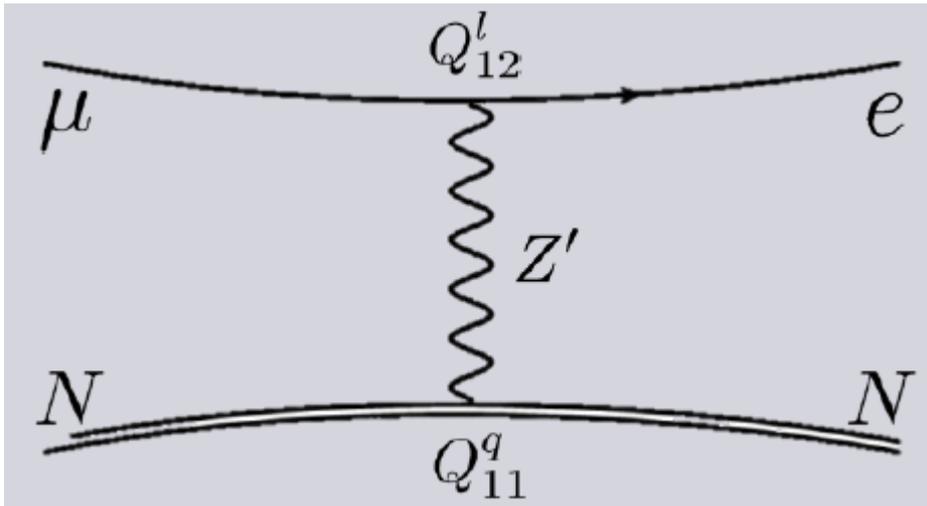
$\sim \alpha$  smaller than  $\mu \rightarrow e \gamma$

Tree :: singlet particle is necessary for conversion!

Charge 2 is OK for  $\mu \rightarrow 3e$

Leptoquark is OK for  $\mu \rightarrow e$

Tree, e.g.



No direct relation with MEG  
NO suppression

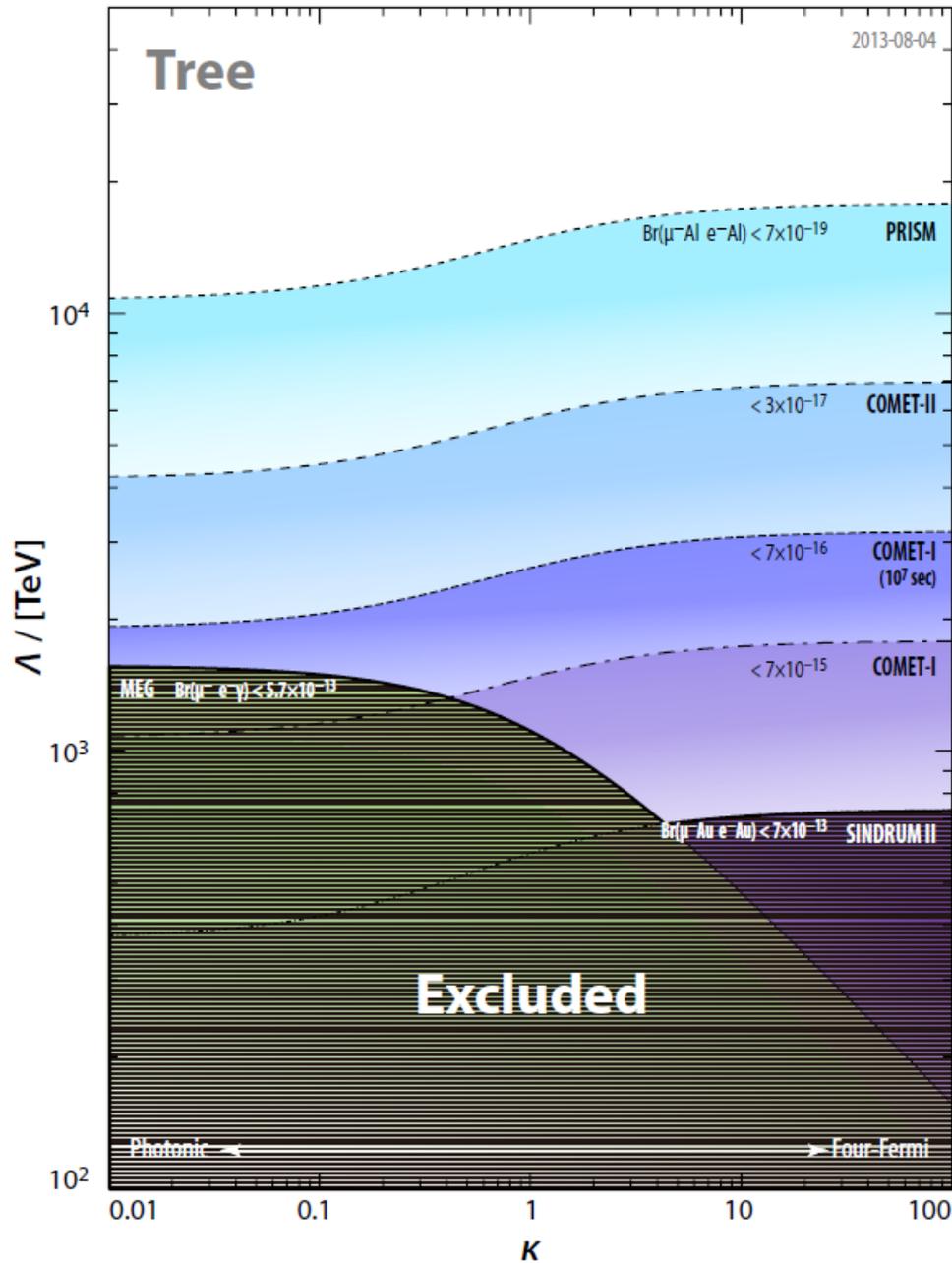
We can parameterize the relative strength

$$\mathcal{L} = \frac{1}{1 + \kappa} \frac{m_\mu}{\Lambda^2} \bar{\mu}_R \sigma^{\mu\nu} e_L F_{\mu\nu} + \frac{\kappa}{1 + \kappa} \frac{1}{\Lambda^2} (\bar{\mu}_L \gamma^\mu e_L) (\bar{q}_L \gamma_\mu q_L)$$

$\kappa \sim \alpha$  :: dipole type, say SUSY with R parity

In general, Model Dependent

MEG



PRISM

COMET Phase-II

COMET Phase-I

## B) Vector vs Scalar

cLFV is mediated by new particle(s)

Vector Boson ::

Boson with broken gauge

So-called  $Z'$  Model, Extra  $U(1)$  from  $SO(10)$  GUT

Kaluza-Klein mode of gauge

Higher dimensional models have massive modes of gauge bosons

Scalar Boson ::

From symmetry = SUSY

Extension of Higgs :: more 2plet, 3plet for nu mass

Explanation for new physics

# Vector type interaction

If Vector boson has no charge

$$\mu^+ \rightarrow e^+ e^- e^+ \text{ and } \mu^- N \rightarrow e^- N$$

can occur at tree level

in a wide sense  $Z'$  model

$$\mu^+ \rightarrow e^+ \gamma \longleftrightarrow \mu^- N \rightarrow e^- N$$

irrelevant

# cLFV Interaction

$$\frac{g_{Z'}}{\sin \theta_W} \bar{l}_i Q_{ij} \gamma^\mu l_j Z'_\mu$$

Different Q's !!

Experiment type	Charges probed
$\mu^- N \rightarrow e^- N$	$Q_{12}$
$\mu^+ \rightarrow e^+ \gamma$	$Q_{13} Q_{23}$ (and all others)
$\mu^+ \rightarrow e^+ e^- e^+$	$Q_{11} Q_{12}$
$e^+ e^- \rightarrow \mu^+ \tau^- (\mu^- \tau^+)$	$Q_{11} Q_{23}$ ( $Q_{12} Q_{13}$ )
$e^+ e^- \rightarrow \mu^+ \mu^-$	$Q_{11} Q_{22}$ ( $Q_{12}$ )
muon $g - 2$	$Q_{23}$ ( $Q_{21} Q_{22}$ )

Table 1: The CFLV experiments and the corresponding  $Z'$  charges probed at lowest order pro-

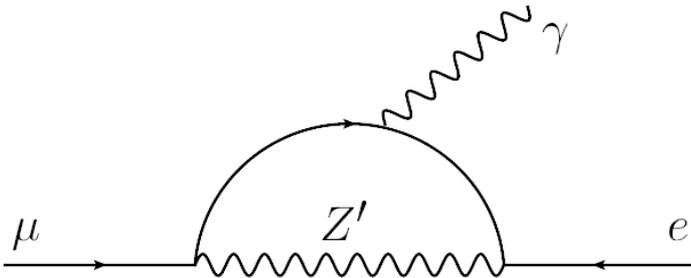


Figure 2:  $\mu^+ \rightarrow e^+ \gamma$  in the  $Z'$  models.

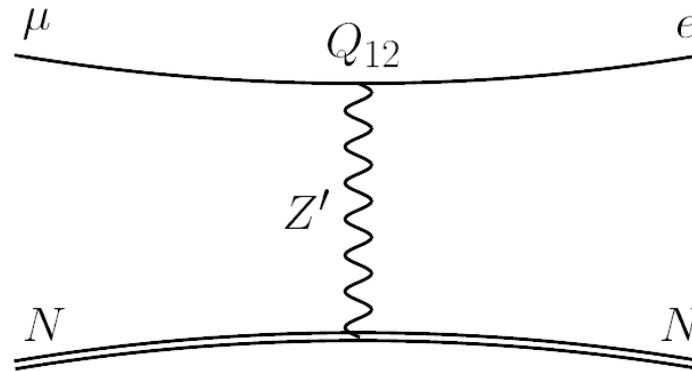
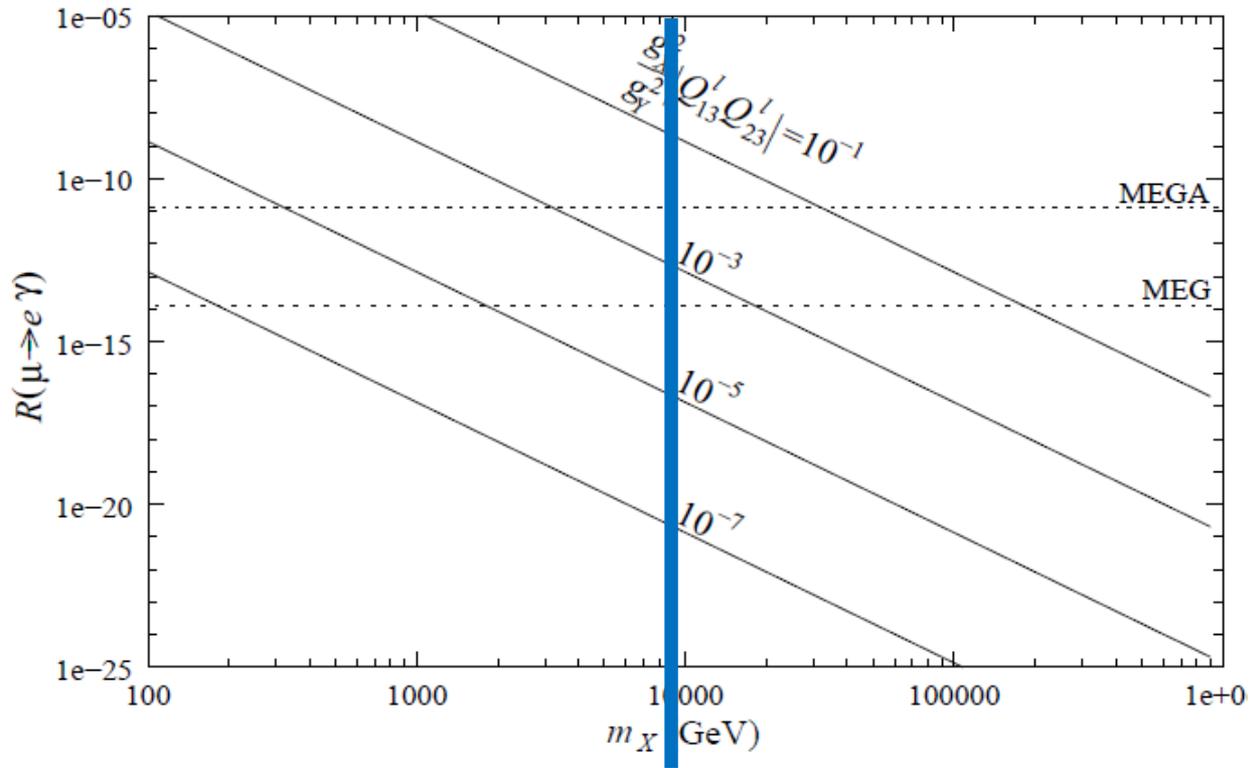


Figure 3: Non-photon diagram of  $\mu^- - e^-$  conversion in the  $Z'$  models.

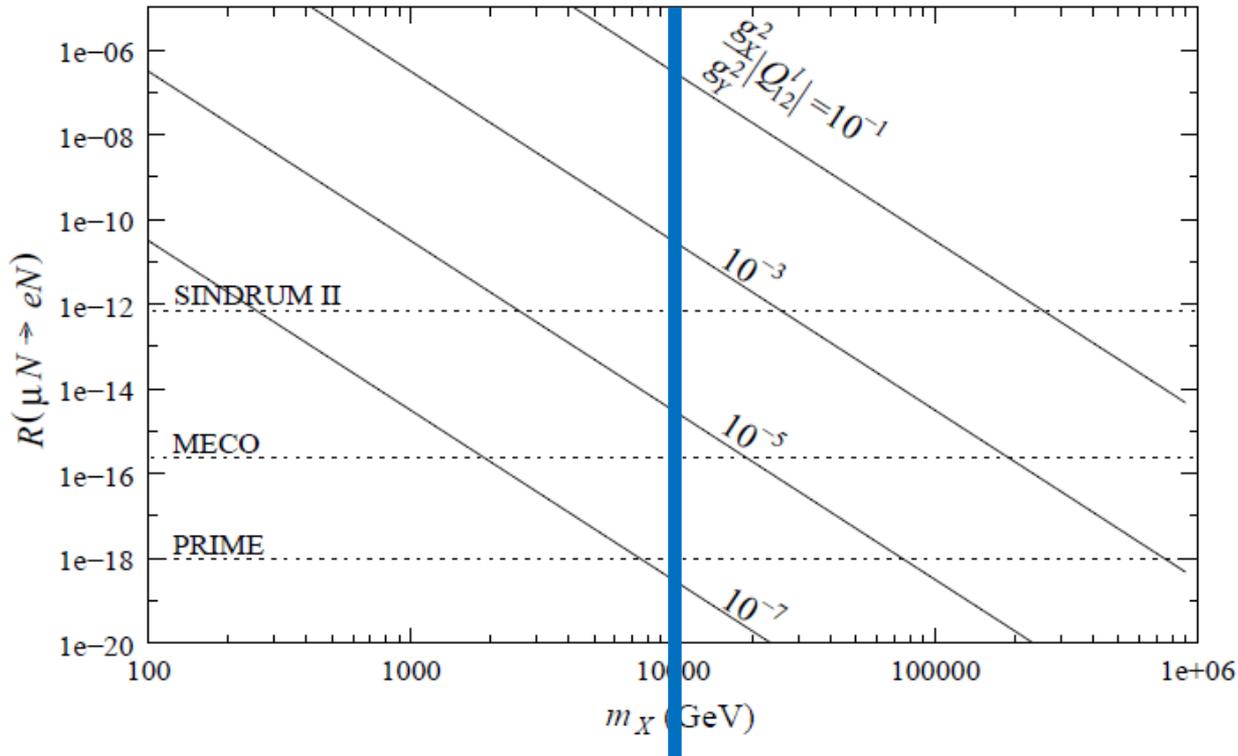


Brandon  
Murakami

10TeV

Figure 4: Constraint of  $Z'$  by the current search for  $\mu^+ \rightarrow e^+ \gamma$ .

$$B(\mu \rightarrow e \gamma) = 1.3 \times 10^{-13} \left( \frac{g_x}{g_Y} \right)^4 \left( \frac{Q_{13} Q_{23}}{10^{-5}} \right)^2 \left( \frac{1 \text{TeV}}{m_{Z'}} \right)^4$$



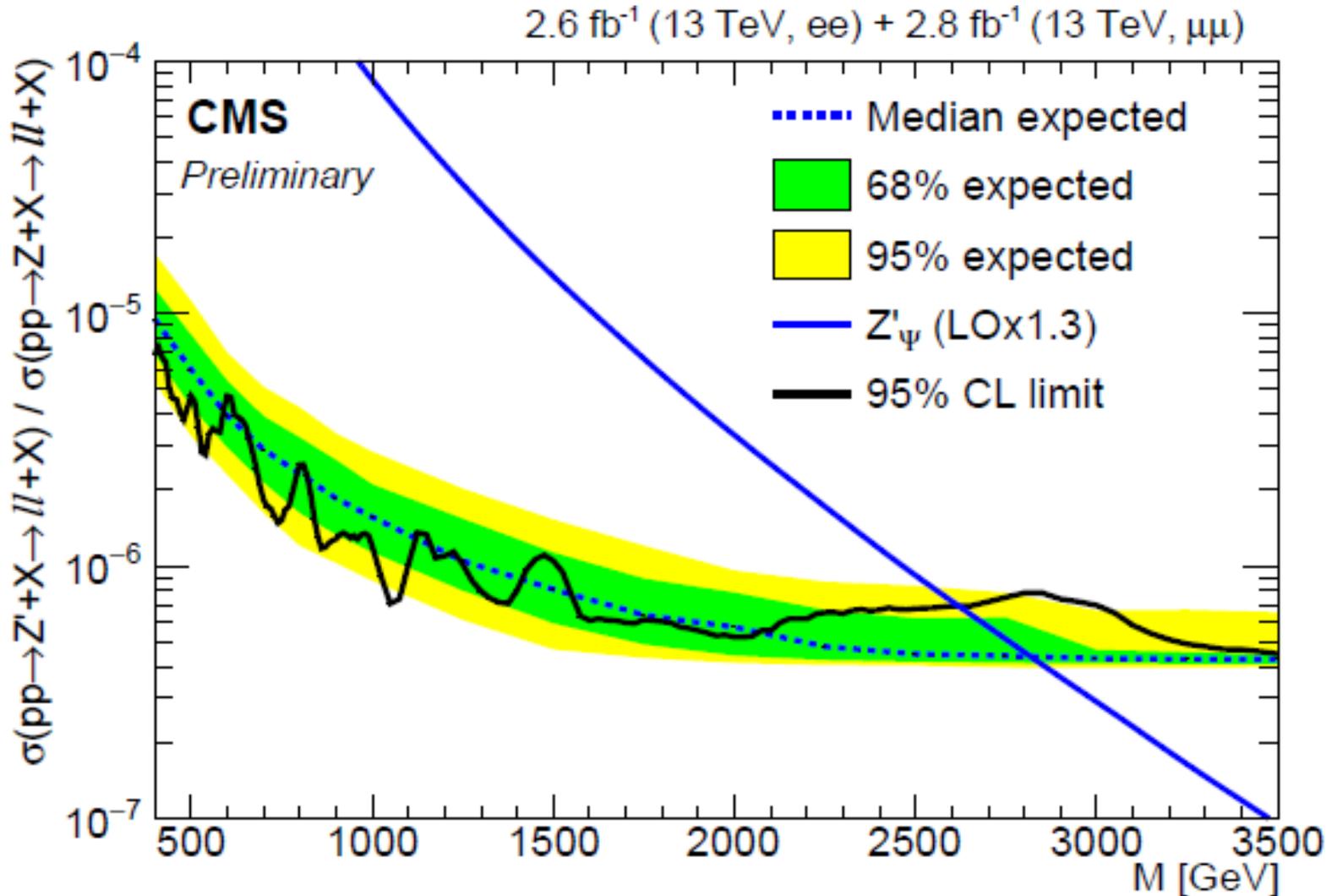
Brandon  
Murakami

10TeV

Figure 5: Constraint of  $Z'$  by the current search for  $\mu^- - e^-$  conversion.

$$B(\mu N \rightarrow e N) = 3.1 \times 10^{-11} \left( \frac{g_{Z'}}{g_Y} \right)^4 \left( \frac{Q_{12}}{10^{-5}} \right)^2 \left( \frac{1 \text{ TeV}}{m_{Z'}} \right)^4$$

# Direct Search at LHC ,excluded < 3TeV



# Scalar type

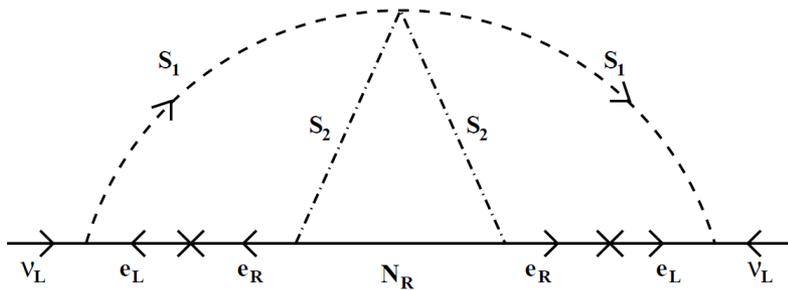
SUSY :: Still main target!?

2 < doublet higgs :: SUSY is restricted version

- Higgs triplet :: doubly charged
- Radiative generation of neutrino masses

*Krauss et al*

sometimes doubly charged



$$\mu^+ \rightarrow e^+ e^- e^+$$

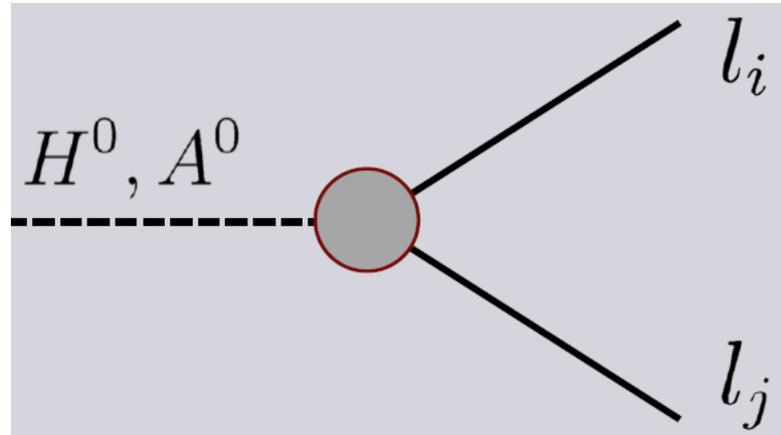
Is more relevant

# SUSY

Neutral scalar : Heavy neutral higgs , sneutrino

**With R-Parity**

Higgs can  
contribute at tree  
level



Naïve  $2 <$  doublets, this coupling can be large, though...

In SUSY , slepton mixing must be contributed , that is, the couplings has same or less magnitude as dipole

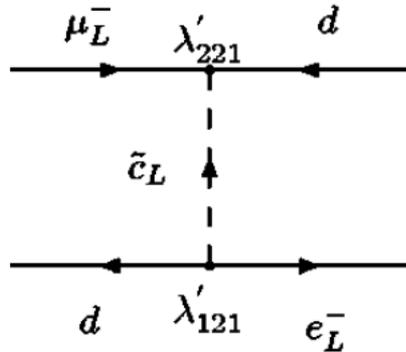
Furthermore, these higgses are probably very heavy

If R parity is broken,

$$W_{RPV} = \frac{\lambda_{ijk}}{2} L_i L_j \bar{E}_k + \lambda'_{ijk} L_i Q_j \bar{D}_k + \lambda''_{ijk} \bar{U}_i \bar{D}_j \bar{D}_k + \mu'_i L_i H_u$$

Tree contribution may dominate for  $\mu - e$  conversion

### Leptoquark



While  $\mu \rightarrow e + \gamma$   
Induced by loop

→ distinction of models

Andre' de Gouvea, Smaragda Lola, and Kazuhiro Tobe

	$\frac{\text{Br}(\mu \rightarrow e \gamma)}{\text{Br}(\mu \rightarrow 3e)}$	$\frac{R(\mu \rightarrow e \text{ in Ti})}{\text{Br}(\mu \rightarrow 3e)}$	$A_P$	$A_{P_1}$	$A_{P_2}$	$A_{P_1}/A_{P_2}$
$\lambda'_{121} \lambda'_{221}$	1.1	$2 \times 10^5$	-100%	-26%	-5%	5.6
MSSM with $\nu_R$	$1.6 \times 10^2$	0.92	-100%	10%	17%	0.6

# Orthodox scenario

Source of LFV  
= Slepton mixing

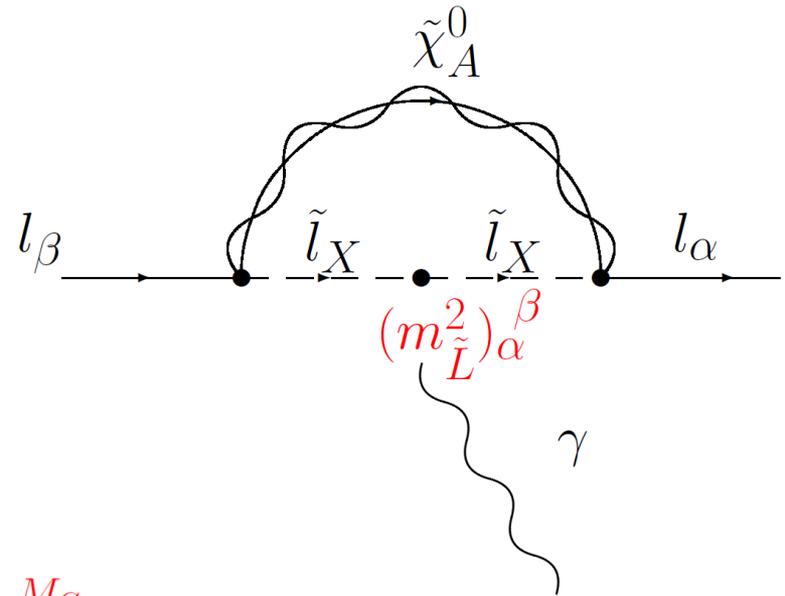
$$m_{\tilde{l}}^2 = \begin{pmatrix} m_{\tilde{e}\tilde{e}}^2 & \Delta m_{\tilde{e}\tilde{\mu}}^2 & \Delta m_{\tilde{e}\tilde{\tau}}^2 \\ \Delta m_{\tilde{\mu}\tilde{e}}^2 & m_{\tilde{\mu}\tilde{\mu}}^2 & \Delta m_{\tilde{\mu}\tilde{\tau}}^2 \\ \Delta m_{\tilde{\tau}\tilde{e}}^2 & \Delta m_{\tilde{\tau}\tilde{\mu}}^2 & m_{\tilde{\tau}\tilde{\tau}}^2 \end{pmatrix}$$

## CMSSM + RH neutrino

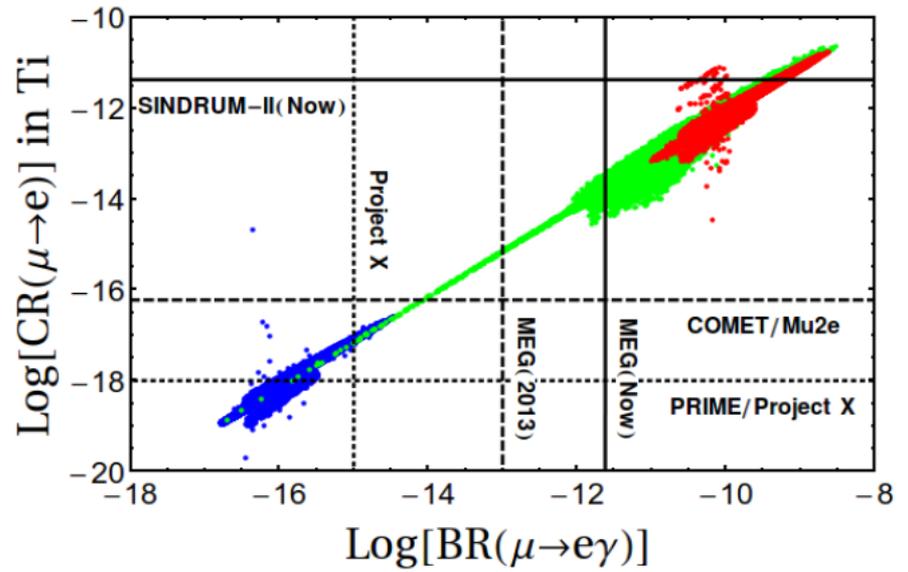
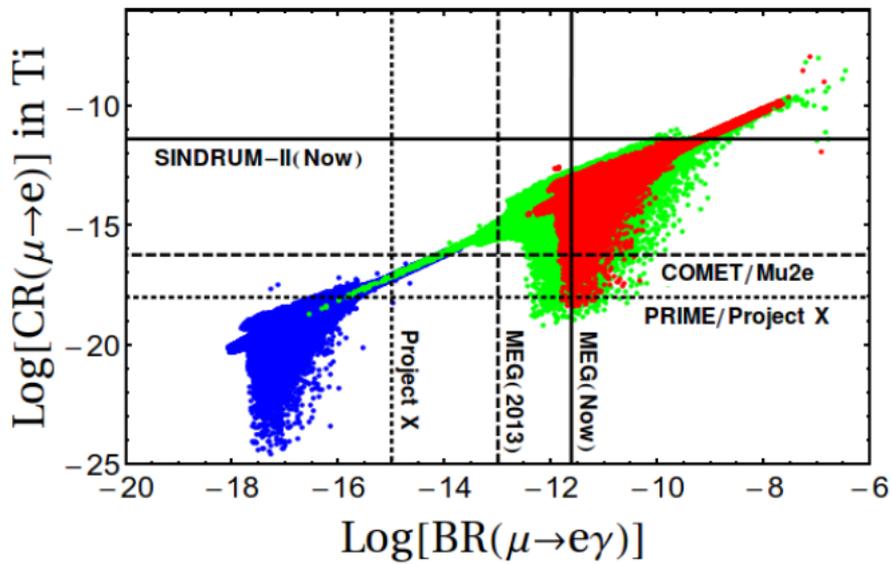
Most exhaustively studied

$$W = f_\nu^{i\beta} \bar{N}_i L_\beta H_u$$

$$\begin{aligned} (m_{\tilde{L}}^2)_\alpha^\beta &\simeq -\frac{(6 + a_0^2)m_0^2}{16\pi^2} (f_\nu^\dagger f_\nu)_\alpha^\beta \log \frac{M_G}{M_R} \\ &\simeq -\frac{(6 + a_0^2)m_0^2}{16\pi^2} U_{\alpha k}^{Dirac} (U^{Dirac*})^{\beta k} |f_{\nu k}|^2 \log \frac{M_G}{M_R} \end{aligned}$$



Dipole dominant



# 3.Connection among CLFVs an Example

J.S & M.Yamanaka

Phys. Rev. D91 055018-1-17, 2015

MEGII experiment updates/discovers(?)



COMET/DeeMe/Mu2E will discover(?)



In near future

Sensitivity is same.

If COMET find CLFV first then ...?

# $\mu$ -e conversion and then ?

If  $\mu$ -e conversion is found, while other cLFV processes will never be found

E.g.

R-parity violating SUSY gives such a situation

Tree contribution for CLFV  
Scalar/Vector with LFV  
Direct coupling with qq and  $\mu$ -e

- ☑ No correlations among cLFVs
- ☑ How to confirm the scenario?

# Aim of this work

To find out distinctive signals to discriminate the scenario and other new physics models

To show the feasibility to determine the parameters in the RPV scenario through observing the signals

**How to confirm a model?**

# R-parity violating SUSY

☑ Candidate of new physics: R-parity violating SUSY

☑ Consistent with experimental/theoretical status

📖 New physics is required to cancel Higgs quadratic divergence

📖 TeV scale SUSY predicts grand unification of interactions

📖 So far no typical SUSY signals have been observed

Omit the term to avoid proton decay

☑ RPV terms in superpotential in SUSY

$$\mathcal{W}_{\mathcal{R}} = \lambda_{ijk} L_i L_j E_k^c + \lambda'_{ijk} L_i Q_j D_k^c + \lambda''_{ijk} U_i^c D_j^c D_k^c$$

**Offers LFV Scalar**

# Framework of our scenario

Naturally realized by RG evolution  
with universal masses@GUT scale

- ☑ Slepton contribution to RPV: only 3rd generation
- ☑ Different generation of left- and right-handed leptons  
 $\lambda_{ijk}$  ( $i \neq k$  and  $j \neq k$ )

Assumption to realize  
the interesting situation

- ☑ RPV terms in superpotential in SUSY

$$\mathcal{W}_{\mathcal{R}} = \lambda_{ijk} L_i L_j E_k^c + \lambda'_{ijk} L_i Q_j D_k^c + \lambda''_{ijk} U_i^c D_j^c D_k^c$$

# Framework of our scenario

Naturally realized unless we introduce additional sources of flavor violation

- ☑ For quarks, flavor diagonal components are much larger than off-diagonal components

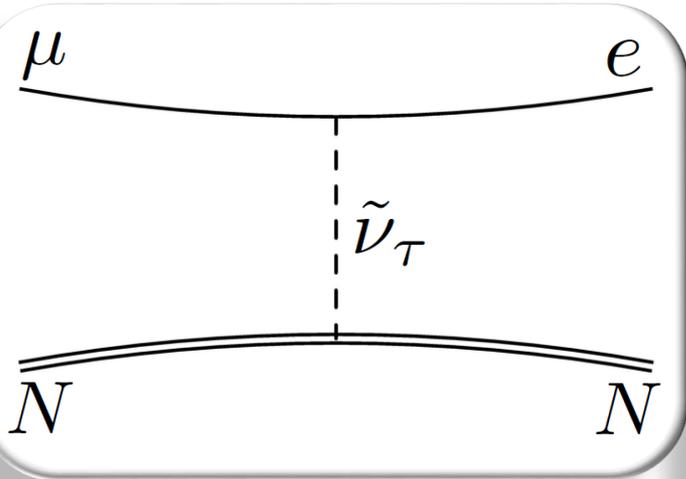
$$\lambda'_{ijj} \gg \lambda'_{ijk} \quad (j \neq k)$$

- ☑ RPV terms in superpotential in SUSY

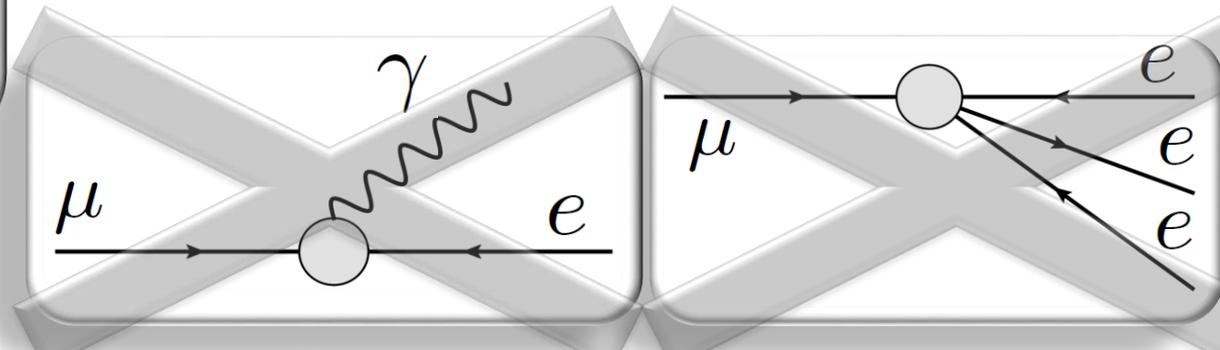
$$\mathcal{W}_{\mathcal{R}} = \lambda_{ijk} L_i L_j E_k^c + \lambda'_{ijk} L_i Q_j D_k^c - \lambda''_{ijk} U_i^c D_j^c D_k^c$$

# Exotic processes in the scenario

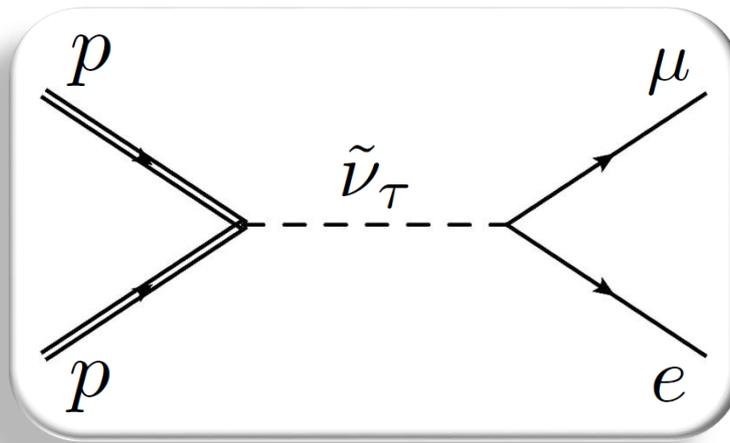
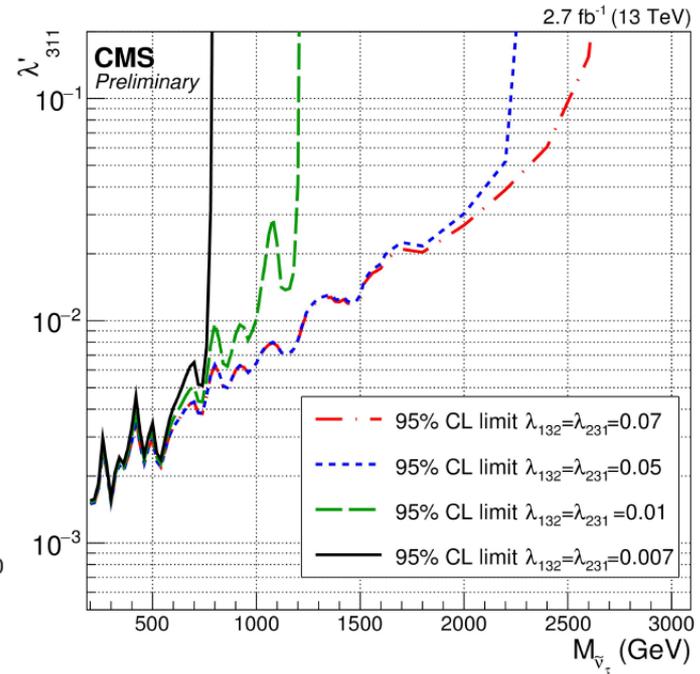
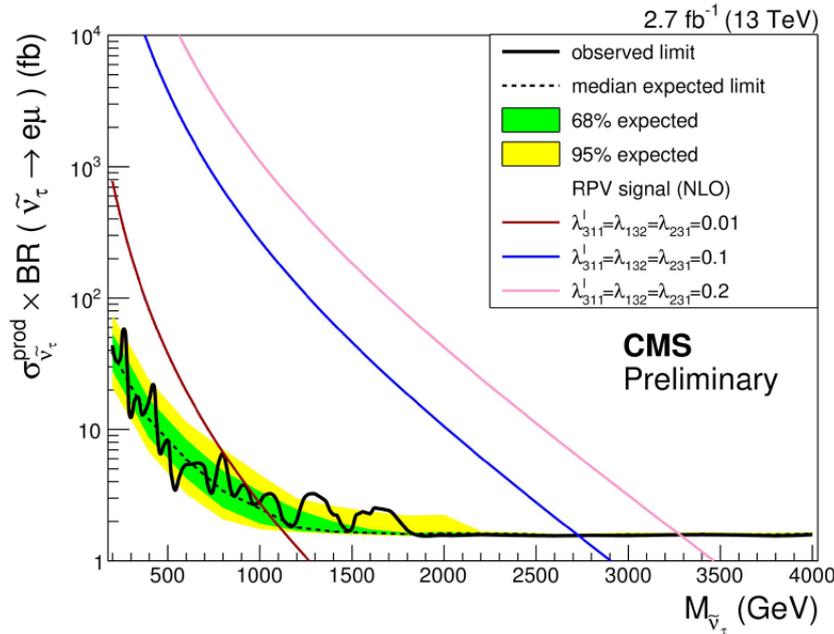
$$\mathcal{L}_{\text{RPV}} = 2 \left\{ \lambda_{312} \tilde{\nu}_\tau \bar{\mu}_R e_L + \lambda_{321} \tilde{\nu}_\tau \bar{e}_R \mu_L + \lambda_{132} \tilde{\tau}_L \bar{\mu}_R \nu_e + \lambda_{231} \tilde{\tau}_L \bar{e}_R \nu_\mu \right\} \\ + \left\{ \lambda'_{311} (\tilde{\nu}_\tau \bar{d}_R d_L - \tilde{\tau}_L \bar{d}_R u_L) + \lambda'_{322} (\tilde{\nu}_\tau \bar{s}_R s_L - \tilde{\tau}_L \bar{s}_R c_L) \right. \\ \left. + \lambda'_{333} (\tilde{\nu}_\tau \bar{b}_R b_L - \tilde{\tau}_L \bar{b}_R t_L) \right\} + \text{h.c.}$$



- ☑ μ-e conversion@tree level
- ☑ Negligible rates of other cLFV processes



# Current bound for the scalar with LFV



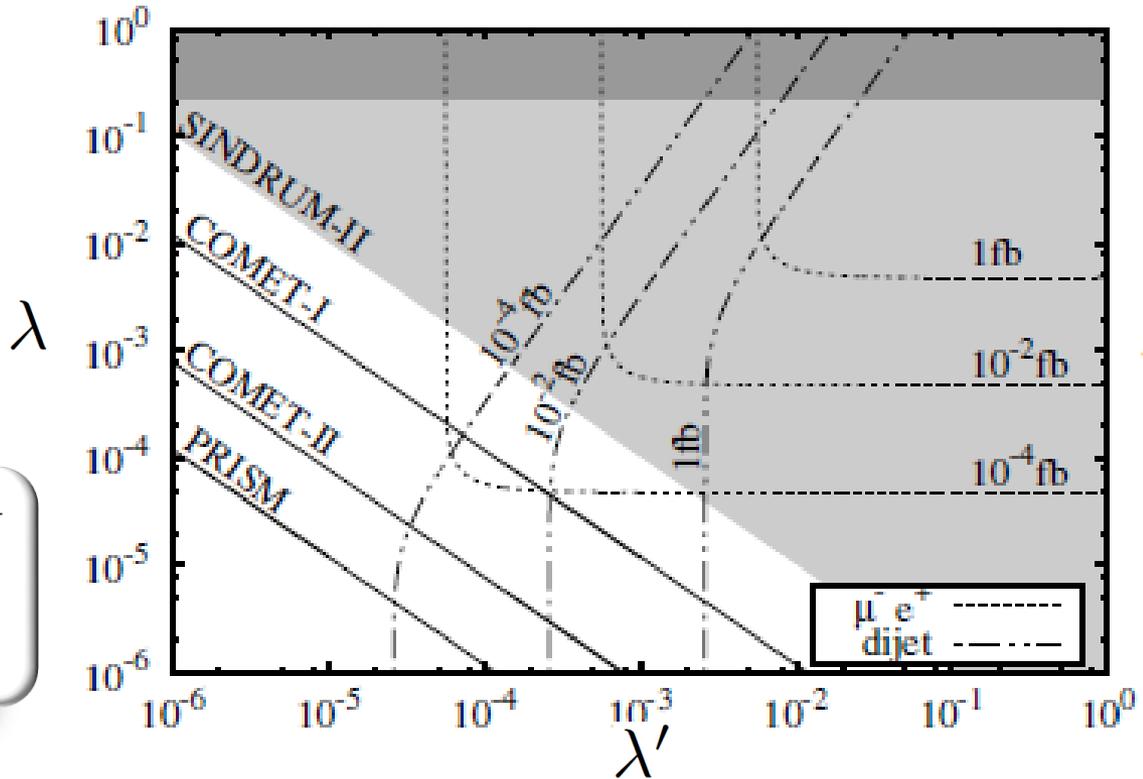
# Correlations of distinctive signals

Contour plot of

- $\text{BR}(\mu^- + N \rightarrow e^- + N)$
- $\sigma(pp \rightarrow \mu e)$
- $\sigma(pp \rightarrow jj)$

■ sneutrino mass  $m_{\tilde{\nu}_\tau} = 1\text{TeV}$

■ collision energy  $\sqrt{s} = 14\text{TeV}$



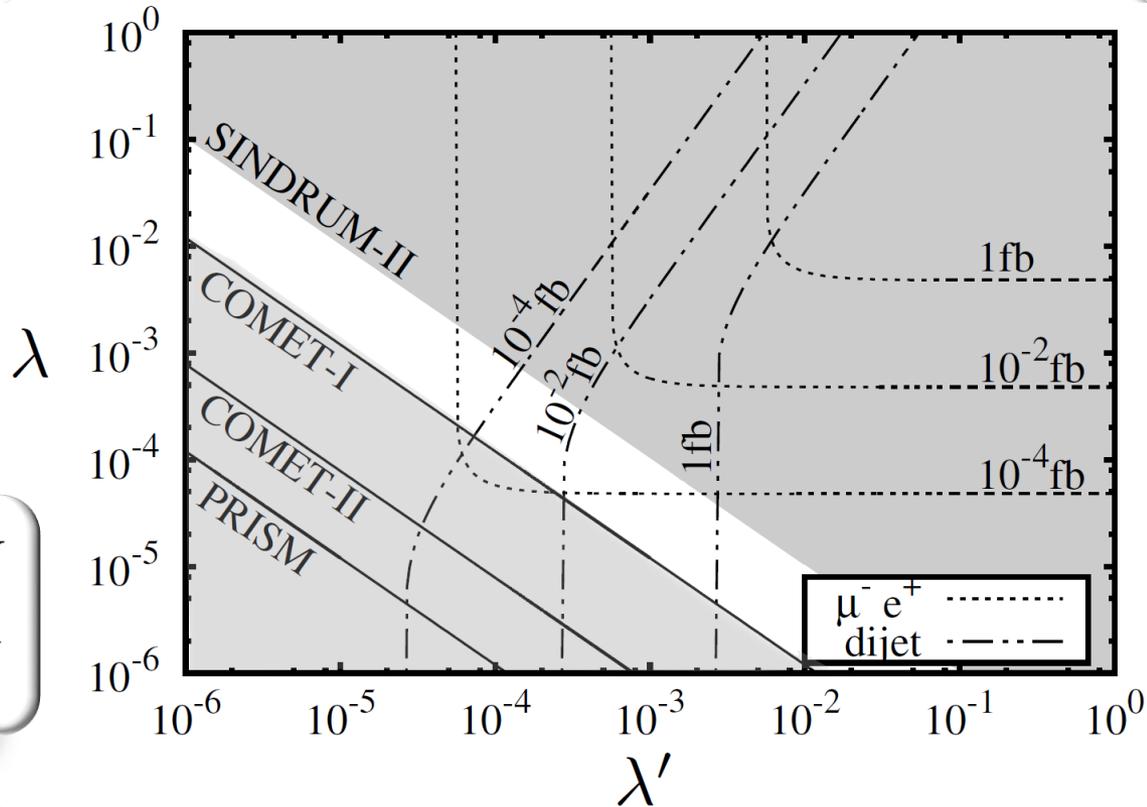
- ☑  $\mu$ -e conversion search is a strong tool for exploring RPV
- ☑ PRISM explores all parameter space wherein LHC can survey

# Correlations of distinctive signals

Contour plot of

- $\text{BR}(\mu^- + N \rightarrow e^- + N)$
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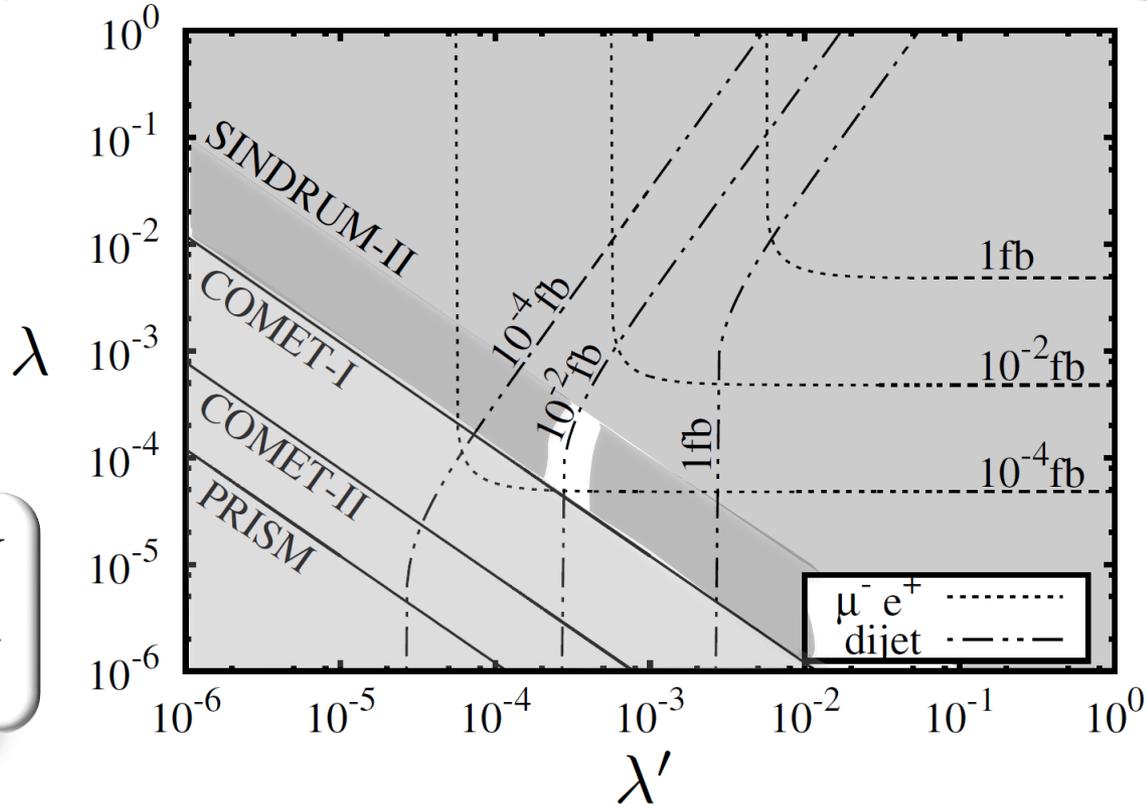
☑ COMET/DeeMe found m-e conversion  $\longrightarrow$  white band

# Correlations of distinctive signals

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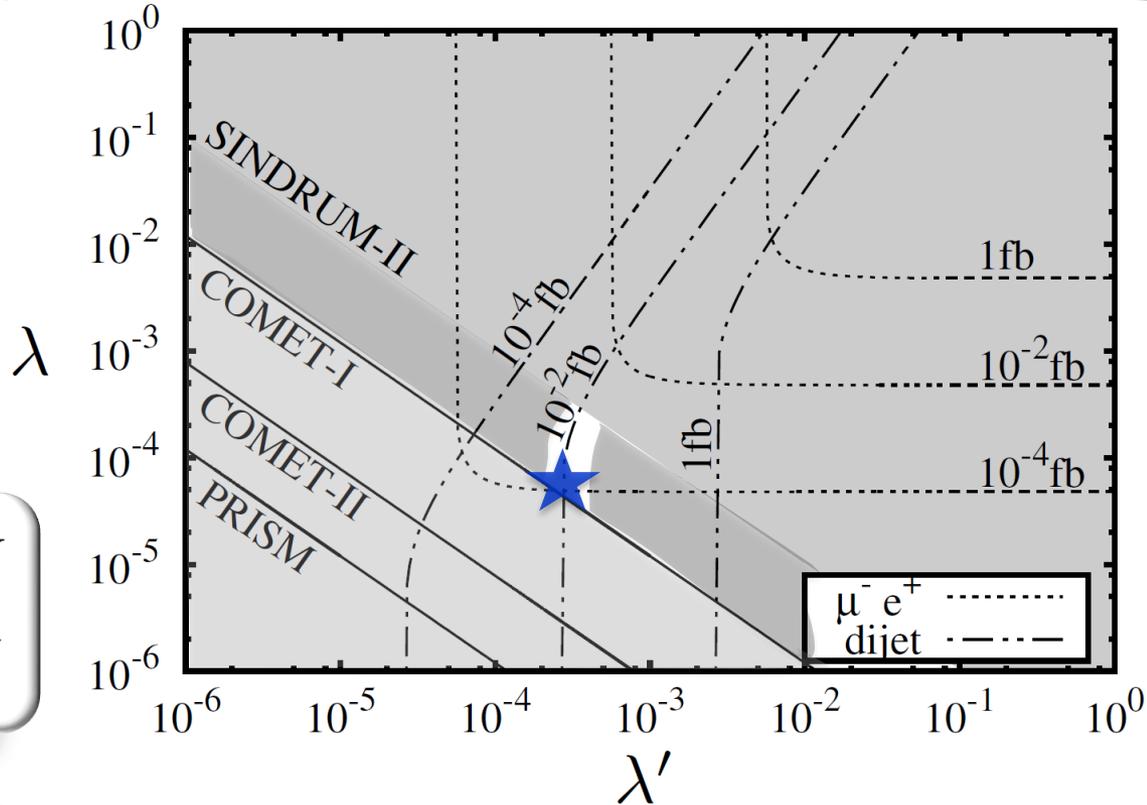
- ☑ COMET/DeeMe found  $m\text{-}e$  conversion  $\longrightarrow$  white band
- ☑ Dijet resonance is found with  $10\text{fb}^{-2}$   $\longrightarrow$  white small region

# Correlations of distinctive signals

Contour plot of

- $\text{BR}(\mu^- + N \rightarrow e^- + N)$
- $\sigma(pp \rightarrow \mu\bar{e})$
- $\sigma(pp \rightarrow jj)$

- sneutrino mass  $m_{\tilde{\nu}_\tau} = 1\text{TeV}$
- collision energy  $\sqrt{s} = 14\text{TeV}$



☑  $\mu\bar{e}$  resonance is found with  $10\text{fb}^{-4}$   $\longrightarrow$  blue star point

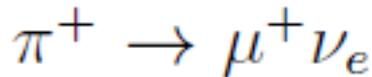
☑ J-PARC and LHC precisely determine the RPV parameters!

# More on coupling discrimination

- Non Standard Interaction

Pion decay in scalar channel – chiral enhancement

Exotic decay



$$\epsilon_{\mu e}^S = \sqrt{2} \frac{m_\pi^2}{m_\mu m} \frac{\lambda_{312}^* \lambda'_{311}}{G_F m_\tau^2}$$

312 : LH electron only

- ILC with polarization

LHC signal is same for 312(LH e) and 321 (RH e)

Can you distinguish them ?

## 4. Another idea for CLFV with muon

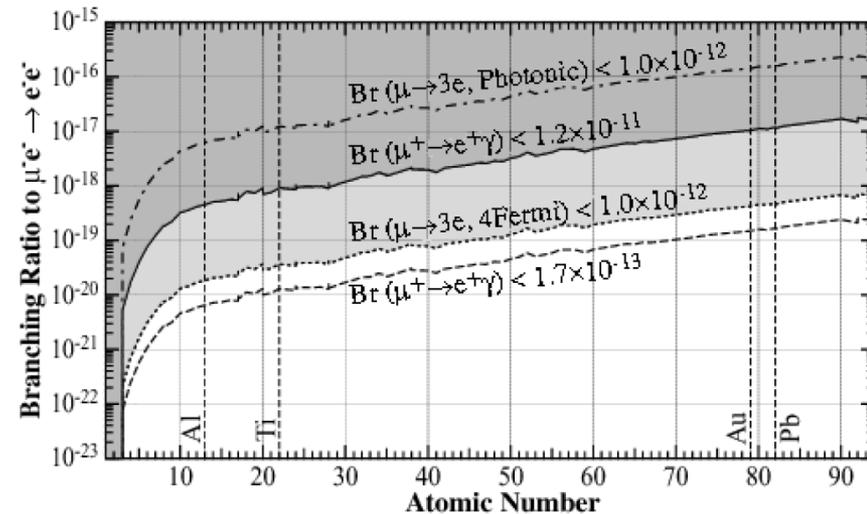
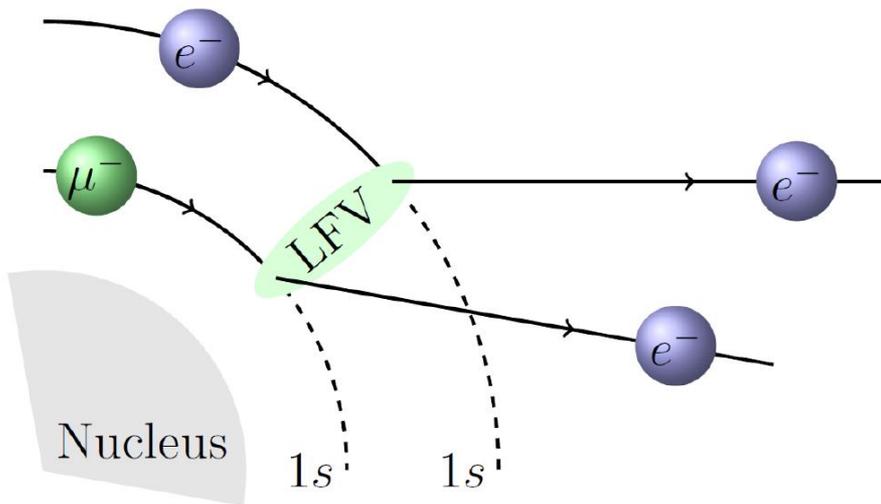
M.Koike, Y.Kuno, J.S., M.Yamanaka, Phys. Rev. Lett. 105, 121601 (2010)

Y.Uesaka, Y.Kuno, J.S., T.Sato, M.Yamanaka, Phys. Rev. D93 076006-1-8, 2016

$\mu^- + e^- \rightarrow e^- + e^-$  in orbits

Same lagrangian for muon LFV

$$\text{Br}(\mu^- e^- \rightarrow e^- e^-) = 3.3 \cdot 10^{-12} \times (Z - 1)^3 \left( \frac{\tilde{T}_\mu}{\tau_\mu} \right) G$$



# 5. Summary

## Charged Lepton Flavor Violation

Clean signal for Physics beyond the Standard Model

Not observed yet though many searches have been done

Muon decay, Tau decay, LFV in final state (decay product)

## Classification of new physics

Tree vs Loop :  $\mu^+ \rightarrow e^+ \gamma$  : always loop effect

Scalar vs Vector

Model dependence

## Most precise measurements with muon

$$\mu^+ \rightarrow e^+ \gamma \quad \text{and} \quad \mu^- \rightarrow e^- \gamma$$

Which one will be observed first?

Example of model dependent analysis with other signals

**New CLFV mode?**  $\mu^- + e^- \rightarrow e^- + e^-$  **in orbits**