# Quarkonium dissociation and regeneration 

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## Quarkonium in a thermal bath



## Colour deconfinement



Transition from hadronic matter to a plasma of deconfined quarks and gluons happening at some critical temperature $T_{c}=154 \pm 9 \mathrm{MeV}$ as studied in finite temperature lattice QCD.

- Wuppertal-Budapest JHEP 1009 (2010) 073, HotQCD PRD 90 (2014) 094503


## Heavy-ion experiments



High energy densities and temperatures $>T_{c}$ as explored by the heavy-ion experiments at RHIC and LHC.

## Quarkonium as a quark-gluon plasma probe

In 1986, Matsui and Satz suggested quarkonium as an ideal quark-gluon plasma probe.

- Heavy quarks are formed early in heavy-ion collisions: $1 / M \sim 0.1 \mathrm{fm}<0.6 \mathrm{fm}$.
- Heavy quarkonium formation will be sensitive to the medium.
- The dilepton signal makes the quarkonium a clean experimental probe.



## Scales

Quarkonium being a composite system is characterized by several energy scales, these in turn may be sensitive to thermodynamical scales smaller than the temperature:

- the scales of a non-relativistic bound state
( $v$ is the relative heavy-quark velocity; $v \sim \alpha_{\mathrm{s}}$ for a Coulombic bound state):
$M$ (mass),
$M v$ (momentum transfer, inverse distance),
$M v^{2}$ (kinetic energy, binding energy, potential $V$ ), $\ldots$
- the thermodynamical scales:
$\pi T$ (temperature),
$m_{D}$ (Debye mass, i.e. screening of the chromoelectric interactions), $\ldots$

The non-relativistic scales are hierarchically ordered: $M \gg M v \gg M v^{2}$ We assume this to be also the case for the thermodynamical scales: $\pi T \gg m_{D}$

## $\Upsilon(1 S)$ scales

A weakly coupled quarkonium possibly produced in a weakly coupled plasma is the bottomonium ground state $\Upsilon(1 S)$ produced in heavy-ion experiments at the LHC:

$$
M_{b} \approx 5 \mathrm{GeV}>M_{b} \alpha_{\mathrm{s}} \approx 1.5 \mathrm{GeV}>\pi T \approx 1 \mathrm{GeV}>M_{b} \alpha_{\mathrm{s}}^{2} \approx 0.5 \mathrm{GeV} \sim m_{D} \gtrsim \Lambda_{\mathrm{QCD}}
$$

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O Brambilla Escobedo Ghiglieri Soto Vairo JHEP 1009 (2010) 038
    Vairo AIP CP 1317 (2011) 241
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## $\Upsilon$ suppression at CMS




- CMS PRL 109 (2012) 222301


## Non-relativistic EFTs of QCD

The existence of a hierarchy of energy scales calls for a description of the system (quarkonium at rest in a thermal bath) in terms of a hierarchy of EFTs.


## Real-time formalism

Temperature is introduced via the partition function.
Sometimes it is useful to work in the real-time formalism.


In real time, the degrees of freedom double (" 1 " and " 2 "), however, the advantages are

- the framework becomes very close to the one for $T=0$ EFTs;
- in the heavy-particle sector, the second degrees of freedom, labeled " 2 ", decouple from the physical degrees of freedom, labeled " 1 ".
This usually leads to a simpler treatment with respect to alternative calculations in imaginary time formalism.


## Real-time gauge boson propagator

- Gauge boson propagator (in Coulomb gauge):

$$
\begin{aligned}
\mathbf{D}_{00}^{(0)}(\vec{k})= & \frac{i}{\vec{k}^{2}}\left(\begin{array}{cc}
1 & 0 \\
0 & -1
\end{array}\right) \\
\mathbf{D}_{i j}^{(0)}(k)= & \left(\delta_{i j}-\frac{k^{i} k^{j}}{\vec{k}^{2}}\right)\left\{\left(\begin{array}{cc}
\frac{i}{k^{2}+i \epsilon} & \theta\left(-k^{0}\right) 2 \pi \delta\left(k^{2}\right) \\
\theta\left(k^{0}\right) 2 \pi \delta\left(k^{2}\right) & -\frac{i}{k^{2}-i \epsilon}
\end{array}\right)\right. \\
& \left.+2 \pi \delta\left(k^{2}\right) n_{\mathrm{B}}\left(\left|k^{0}\right|\right)\left(\begin{array}{cc}
1 & 1 \\
1 & 1
\end{array}\right)\right\}
\end{aligned}
$$

where

$$
n_{\mathrm{B}}\left(k^{0}\right)=\frac{1}{e^{k^{0} / T}-1}
$$

## Real-time heavy-particle propagator

- The free heavy-particle propagator is proportional to

$$
\mathbf{S}^{(0)}(p)=\left(\begin{array}{cc}
\frac{i}{p^{0}+i \epsilon} & 0 \\
2 \pi \delta\left(p^{0}\right) & \frac{-i}{p^{0}-i \epsilon}
\end{array}\right)
$$

Since $\left[\mathbf{S}^{(0)}(p)\right]_{12}=0$, the static quark fields labeled " 2 " never enter in any physical amplitude, i.e. any amplitude that has the physical fields, labeled " 1 ", as initial and final states.

These properties hold also for interacting heavy particle(s): interactions do not change the nature (" 1 " or " 2 ") of the interacting fields.

## Dissociation mechanisms at LO

A key quantity for describing the observed quarkonium dilepton signal suppression is the quarkonium thermal dissociation width.

Two distinct dissociation mechanisms may be identified at leading order:

- gluodissociation, which is the dominant mechanism for $M v^{2} \gg m_{D}$;
- dissociation by inelastic parton scattering, which is the dominant mechanism for $M v^{2} \ll m_{D}$.

Beyond leading order the two mechanisms are intertwined and distinguishing between them becomes unphysical, whereas the physical quantity is the total decay width.

## Gluodissociation

based on
O Brambilla Escobedo Ghiglieri Vairo JHEP 1112 (2011) 116

## Gluodissociation

Gluodissociation is the dissociation of quarkonium by absorption of a gluon from the medium.


- The exchanged gluon is lightlike or timelike.
- The process happens when the gluon has an energy of order $M v^{2}$.
- Kharzeev Satz PLB 334 (1994) 155

Xu Kharzeev Satz Wang PRC 53 (1996) 3051

## Gluodissociation

From the optical theorem, the gluodissociation width follows from cutting the gluon propagator in the following pNRQCD diagram


For a quarkonium at rest with respect to the medium, the width has the form

$$
\Gamma_{n l}=\int_{q_{\min }} \frac{d^{3} q}{(2 \pi)^{3}} n_{\mathrm{B}}(q) \sigma_{\mathrm{gluo}}^{n l}(q) .
$$

- $\sigma_{\text {gluo }}^{n l}$ is the in-vacuum cross section $(Q \bar{Q})_{n l}+g \rightarrow Q+\bar{Q}$.
- Gluodissociation is also known as singlet-to-octet break up.
- Brambilla Ghiglieri Vairo Petreczky PRD 78 (2008) 014017


## $1 S$ gluodissociation at LO



The LO gluodissociation cross section for $1 S$ Coulombic states is

$$
\sigma_{\text {gluo LO }}^{1 S}(q)=\frac{\alpha_{\mathrm{s}} C_{F}}{3} 2^{10} \pi^{2} \rho(\rho+2)^{2} \frac{E_{1}^{4}}{M q^{5}}\left(t(q)^{2}+\rho^{2}\right) \frac{\exp \left(\frac{4 \rho}{t(q)} \arctan (t(q))\right)}{e^{\frac{2 \pi \rho}{t(q)}}-1}
$$

where $\rho \equiv 1 /\left(N_{c}^{2}-1\right), t(q) \equiv \sqrt{q /\left|E_{1}\right|-1}$ and $E_{1}=-M C_{F}^{2} \alpha_{\mathrm{s}}^{2} / 4$.

- Brambilla Escobedo Ghiglieri Vairo JHEP 1112 (2011) 116

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    Brezinski Wolschin PLB 707 (2012) 534
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The Bhanot-Peskin approximation corresponds to the large $N_{c}$ limit, i.e. to neglecting final state interactions (the rescattering of a $Q \bar{Q}$ pair in a color octet configuration).

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O Peskin NPB 156 (1979) 365, Bhanot Peskin NPB 156 (1979) }39
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Gluodissociation width vs Bhanot-Peskin width


## Dissociation by inelastic parton scattering

## based on

O Brambilla Escobedo Ghiglieri Vairo JHEP 05 (2013) 130

## Dissociation by inelastic parton scattering

Dissociation by inelastic parton scattering is the dissociation of quarkonium by scattering with gluons and light-quarks in the medium.


- Grandchamp Rapp PLB 523 (2001) 60, NPA 709 (2002) 415
- The exchanged gluon is spacelike.
- External thermal gluons are transverse.
- In the NRQCD power counting, each external transverse gluon is suppressed by $T / M$.


## Dissociation by inelastic parton scattering

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## Dissociation by inelastic parton scattering

From the optical theorem, the thermal width follows from cutting the gluon self-energy in the following NRQCD diagrams (momentum of the gluon $\gtrsim M v$ )

and/or pNRQCD diagram (momentum of the gluon $\ll M v$ )


- Dissociation by inelastic parton scattering is also known as Landau damping.


## Dissociation by inelastic parton scattering

For a quarkonium at rest with respect to the medium, the thermal width has the form

$$
\Gamma_{n l}=\sum_{p} \int_{q_{\min }} \frac{d^{3} q}{(2 \pi)^{3}} f_{p}(q)\left[1 \pm f_{p}(q)\right] \sigma_{p}^{n l}(q)
$$

where the sum runs over the different incoming light partons and $f_{g}=n_{\mathrm{B}}$ or $f_{q}=n_{\mathrm{F}}$.

- $\sigma_{p}^{n l}$ is the in-medium cross section $(Q \bar{Q})_{n l}+p \rightarrow Q+\bar{Q}+p$.
- The convolution formula correctly accounts for Pauli blocking in the fermionic case (minus sign).
- The formula differs from the gluodissociation formula.
- The formula differs from the one used for long in the literature, which has been inspired by the gluodissociation formula.

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- Grandchamp Rapp PLB 523 (2001)
    Park Kim Song Lee Wong PRC 76 (2007) 044907, ...
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## Dissociation by quark inelastic scattering



## Dissociation by gluon inelastic scattering



## Dissociation width


oVairo EPJ Web Conf 71 (2014) 00135

## Quarkonium in a fireball

## based on

O Brambilla Escobedo Soto Vairo, in preparation

## Quarkonium in a fireball

- After the heavy-ion collisions, quarkonium propagates freely up to 0.6 fm .
- From 0.6 fm to the freeze-out time $t$ it propagates in the medium.
- We assume the medium infinite, homogeneous, isotropic and in thermal equilibrium.
- The temperature $T$ of the medium changes with time:

$$
T=T_{0}\left(\frac{t_{0}}{t}\right)^{v_{s}^{2}}, \quad t_{0}=0.6 \mathrm{fm}, v_{s}^{2}=\frac{1}{3} \text { (sound velocity) }
$$

- Bjorken PRD 27 (1983) 140

The initial temperature $T_{0}$ may account for different centralities

| centrality (\%) | $\langle b\rangle(\mathrm{fm})$ | $T_{0}(\mathrm{MeV}) @$ LHC |
| :---: | :---: | :---: |
| $0-10$ | 3.4 | 471 |
| $10-20$ | 6.0 | 461 |
| $20-30$ | 7.8 | 449 |
| $30-50$ | 9.9 | 425 |
| $50-100$ | 13.6 | 304 |

- We assume the heavy quarks comoving with the medium.


## Quarkonium evolution equations

Quarkonium is not in equilibrium, as it can be created (in a color singlet state) or dissociated (in a color octet state) through emission of gluons. The singlet and octet density matrices can be defined in the close-time path formalism:

$$
\rho_{s}\left(t_{1}, t_{2}\right)=\left\langle\mathcal{P} S_{1}\left(t_{1}\right) S_{2}^{\dagger}\left(t_{2}\right)\right\rangle, \quad \rho_{o}\left(t_{1}, t_{2}\right)=\left\langle\mathcal{P} O_{1}^{a}\left(t_{1}\right) O_{2}^{a \dagger}\left(t_{2}\right)\right\rangle
$$

By resumming self-energy contributions,

they satisfy the evolution equations

$$
\begin{aligned}
& \frac{d \rho_{s}(t ; t)}{d t}=-i h_{s, e f f}(t) \rho_{s}(t ; t)+i \rho_{s}(t ; t) h_{s, e f f}^{\dagger}(t)+\mathcal{F}\left(\rho_{o}, t\right) \\
& \frac{d \rho_{o}(t ; t)}{d t}=-h_{o, e f f}(t) \rho_{o}(t ; t)+i \rho_{o}(t ; t) h_{o, e f f}^{\dagger}(t)+\mathcal{F}_{1}\left(\rho_{s}, t\right)+\mathcal{F}_{2}\left(\rho_{o}, t\right)
\end{aligned}
$$

## Lindblad equations

If $(1 / T) d T / d t \ll E$ the evolution equations can be written in the Lindblad form

$$
\begin{aligned}
& \frac{d \rho}{d t}=-i[H, \rho]+\sum_{i}\left(C_{i} \rho C_{i}^{\dagger}-\frac{1}{2}\left\{C_{i}^{\dagger} C_{i}, \rho\right\}\right) \\
& \rho=\left(\begin{array}{cc}
\rho_{s} & 0 \\
0 & \rho_{o}
\end{array}\right) \\
& C_{i}^{0}=\sqrt{\frac{4 T_{F} \alpha_{s}(\nu) T}{3 N_{c}}}\left(\frac{2 i p_{i}}{M_{b}}+\frac{N_{c} \alpha_{s}\left(1 / a_{o}\right) r_{i}}{2 N_{c} r}\right)\left(\begin{array}{cc}
0 & 1 \\
0 & 0
\end{array}\right), E \gg m_{D} \\
& C_{i}^{1}=\sqrt{\frac{4 C_{F} \alpha_{s}(\nu) T}{3}}\left(-\frac{2 i p_{i}}{M_{b}}+\frac{N_{c} \alpha_{s}\left(1 / a_{o}\right) r_{i}}{2 N_{c} r}\right)\left(\begin{array}{ll}
0 & 0 \\
1 & 0
\end{array}\right), E \gg m_{D} \\
& C_{i}^{2}=\frac{2}{M_{b}} \sqrt{\frac{\left(N_{c}^{2}-4\right) \alpha_{s}(\nu) T}{N_{c}}} p_{i}\left(\begin{array}{cc}
0 & 0 \\
0 & 1
\end{array}\right), E \gg m_{D}
\end{aligned}
$$

$H$ is an effective Hermitian Hamiltonian and $C$ 's are called collapse operators.

## Initial conditions

The production of singlets is $\alpha_{s}$ suppressed compared to that of octets.

- Cho Leibovich PRD 53 (1996) 6203

Our choice at $t=0$ is

$$
\rho_{s}=A|\mathbf{0}\rangle\langle\mathbf{0}|, \quad \rho_{o}=\frac{\delta}{\alpha_{s}\left(M_{b}\right)} \rho_{s}
$$

$A$ is fixed by $\operatorname{Tr}\left(\rho_{s}\right)+\operatorname{Tr}\left(\rho_{o}\right)=1$
$\delta$ fixes the octet fraction with respect to the singlet: $\delta=1,0.1,10$.

## Dilepton suppression rate

We compute the dilepton suppression rate $R_{A A}$ :

$$
R_{A A} \sim \frac{\left.\rho_{S}\right|_{1 S 1 S} ^{A A}}{\left.\rho_{S}\right|_{1 S 1 S} ^{p p}}
$$

If $R_{A A}$ is due only to screening for $M_{b} \alpha_{\mathrm{s}} \gg T \gg m_{D} \gg E$, then


## $R_{A A}$ for $M_{b} \alpha_{\mathrm{s}} \gg T \gg E \gg m_{D}, \delta=1$ and $\nu=372 \mathrm{MeV}$



## $R_{A A}$ for $M_{b} \alpha_{\mathrm{s}} \gg T \gg E \gg m_{D}, \delta=1$ and $\nu=2 \pi T$



## $R_{A A}$ for $M_{b} \alpha_{\mathrm{s}} \gg T \gg E \gg m_{D}, \delta=0.1$ and $\nu=2 \pi T$



## $R_{A A}$ for $M_{b} \alpha_{\mathrm{s}} \gg T \gg E \gg m_{D}, \delta=10$ and $\nu=2 \pi T$



## Conclusions

In a framework that makes close contact with modern effective field theories for non relativistic bound states at zero temperature, one can study the dissociation of a quarkonium in a thermal bath of gluons and light quarks.

In a weakly-coupled framework, the situation is the following.

- For $E>m_{D}$ quarkonium decays dominantly via gluodissociation (aka singlet-to-octet break up).
- For $m_{D}>E$ quarkonium decays dominantly via inelastic parton scattering (aka Landau damping).

In the same framework we have studied dissociation and ricombination of quarkonium out of thermal equilibrium.

- The results depends stronly on the initial conditions and on the renormalization scale.
- Under some reasonable choice of parameters it may come close to the experimental findings.

