

Physics potential and motivations for muon colliders.

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CERN, November 19th, 2015

Little of history

- The idea of muon colliders (MC) goes back to about middle '90s.
- Discovery and study of s-channel Higgs physics in the SM and beyond.

D. Cline, '94, ...

V. Barger, M. Berger, J. Gunion and T. Han,
Phys. Rept. 286 (1997)

- - (i) First MC at low c.m. energy (100-500 GeV) for Higgs discovery, $L \sim 2 \times 10^{33} \text{ cm}^{-2} \text{ s}^{-1}$
 - (ii) Next MC at high c.m. energy (up to 4 TeV), for new phenomena, $L \sim 10^{35} \text{ cm}^{-2} \text{ s}^{-1}$

Neutrino Factories

- Neutrino beams from a high L muon storage ring (with a straight section pointing towards a desired experimental area)

S. Geer, '97

- Precision neutrino physics:
- Neutrino oscillations
- Neutrino mixing, Dirac vs. Majorana phases
- CP violation
-

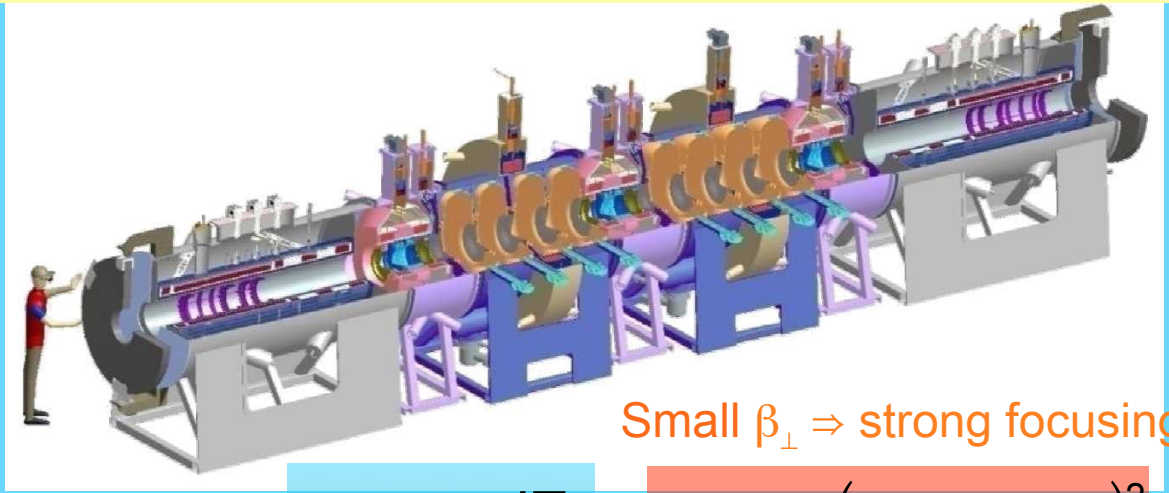
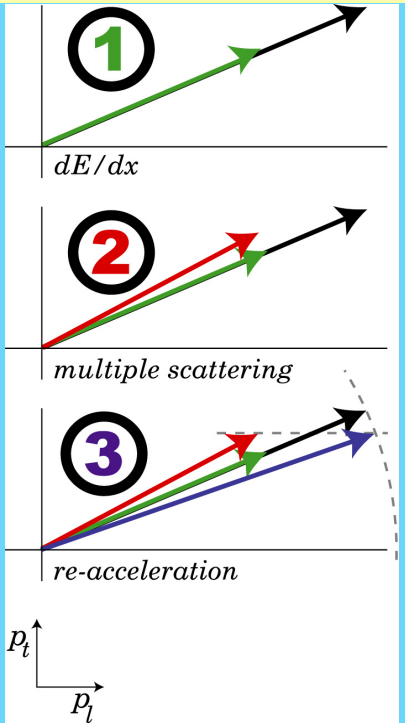
See f. ex. P. Huber, '15

Muon Cooling

□ Muon Ionization Cooling:

- Muon Ionization Cooling is the key technology required to be able to realise a Neutrino Factory and a Muon Collider

Principle **Practice**



Small $\beta_{\perp} \Rightarrow$ strong focusing

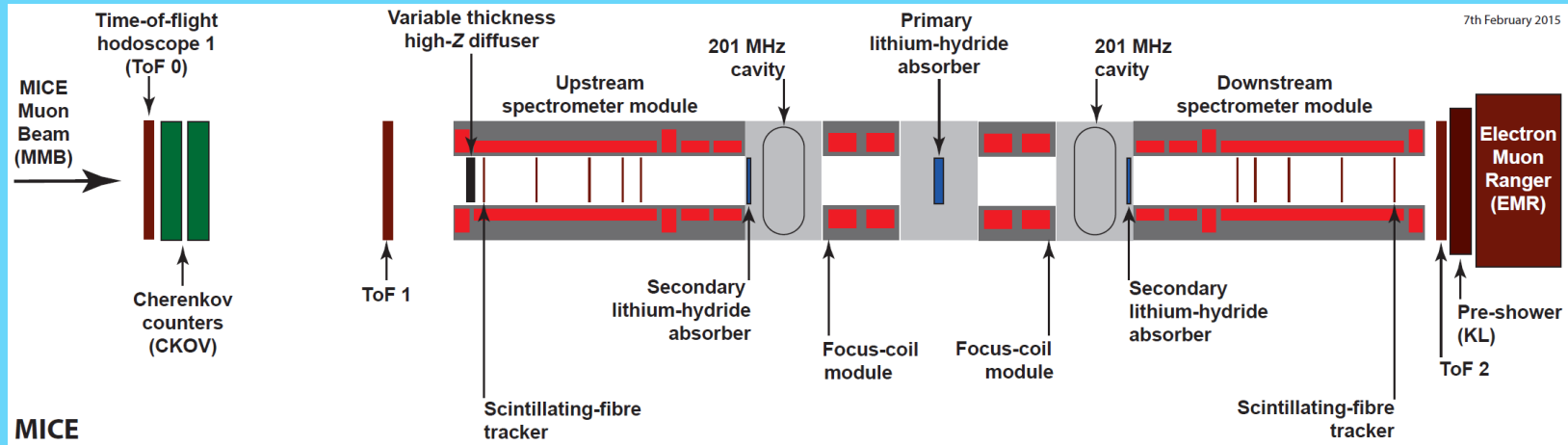
$$\frac{d\varepsilon}{dz} \approx - \frac{\varepsilon}{E_{\mu} \beta^2} \frac{dE_{\mu}}{dz} + \frac{\beta_{\perp}}{2m\beta^3} \frac{(13.6 \text{ MeV})^2}{E_{\mu} X_0}$$

Ionization:
cooling term

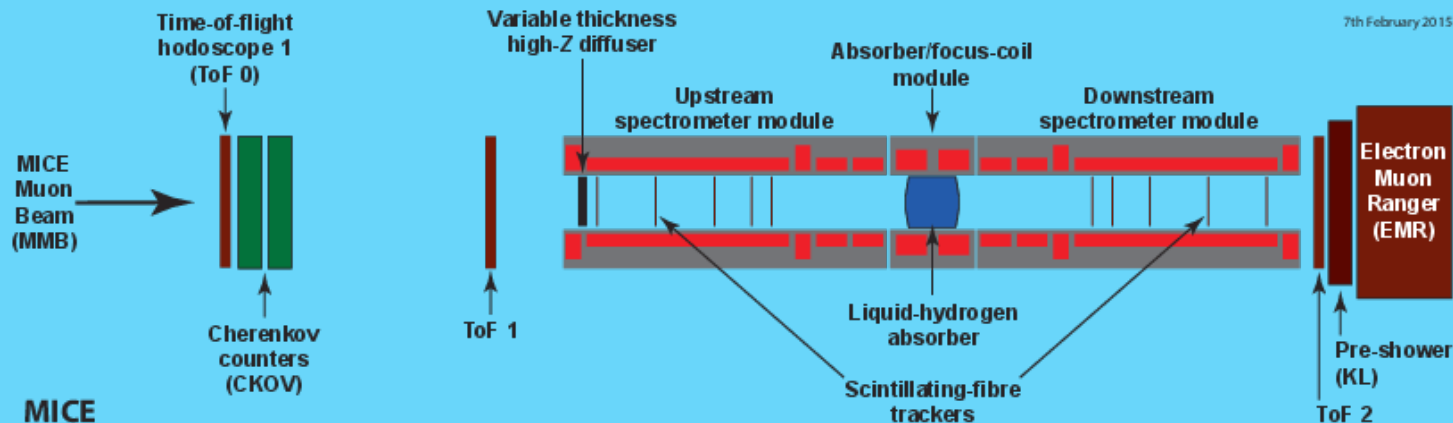
Multiple scattering:
heating term

Muon Ionization Cooling Experiment

- Final MICE demonstration of ionization cooling was recently reconfigured after a detailed project review



- MICE Step IV: first chance to measure normalised transverse emittance reduction and explore ionization cooling parameters



New motivation

- The discovery of the Higgs particle (H) has been a success of the SM, but is also demanding a detailed knowledge of its properties.
- Among the various types of colliders which have been proposed, the muon collider offers the unique opportunity of a precision study of the total and partial widths of H in the various decay channels.
- In addition, all the Higgs bosons of the minimal Susy model (MSSM) are produced in sufficient abundance in s-channel $\mu^+\mu^-$ collisions to allow their detection for most of the model parameter space.

The LHC discovery of the Higgs at 125 GeV

- Atlas and CMS have observed a narrow line of high significance at about 125 GeV mass, compatible with the Standard Model Higgs boson.
- Their data are consistent with fermionic and bosonic couplings expected from a SM Higgs particle. Searches have been performed in several decay modes.
- ATLAS and CMS and CDF also exclude so far other SM-type Higgs bosons up to approximately 600 GeV.
- Experimental energy resolutions have been so far much wider of the expected intrinsic Higgs width of about 4 MeV.

- From the available data it cannot be concluded yet that we have found the SM Higgs and not one of the scalars postulated within the possible extensions of the SM.
- In particular the Higgs width's measurement is essential to determine the couplings to fermions and bosons and their partial widths
- Therefore the detailed study of the properties of this particle is mandatory.
Q: Will LHC (14-Tev) be enough?

“A complete demonstrator of a muon cooled Higgs factory.”

C. Rubbia, arXiv: 1308.6612

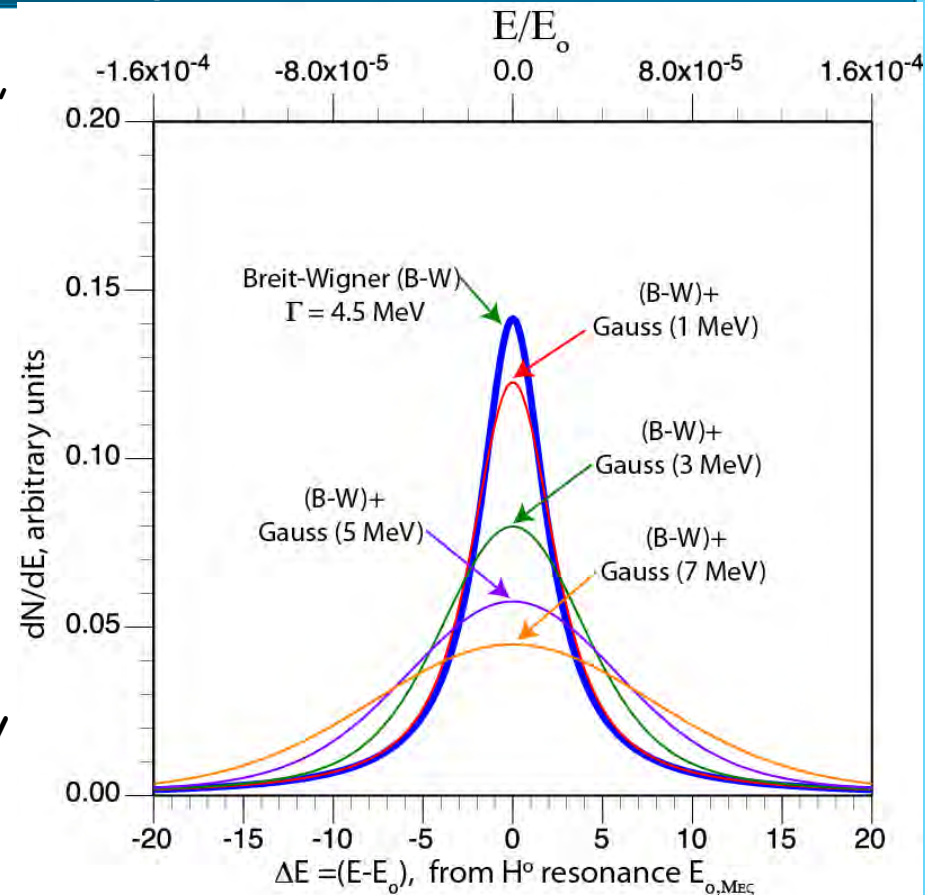
- Muon cooling: a Higgs factory at CERN?

C.Rubbia, Frascati, Dec. '14, Venice, March 2015, Cern, April 2015

--> The issue of muon cooling is essential for the Luminosity and the energy spread of the beams. We need highly mono-chromatic beams.

The Higgs width according to the Standard Model

- Like in the case of the Z_0 , the determination of the H_0 width will be crucial in the determination of the nature of the particle and the underlying theory
- Cross section is shown here, convoluted with a Gaussian beam distribution.
- Signal is not affected only if the rms beam energy width is \leq a few MeV.



4.5 MeV width: A very demanding resolution $R \approx 0.003\%$ is required

Venice, March. 2015

Slide# : 6

C. Rubbia

No radiative corrections are included.

The need of a better precision

- What precision is needed in order to search for possible additional deviations from the SM, even under the assumption that there is no other additional "Higgs" state at the LHC ?
- Predicted ultimate LHC accuracies for "exotic" alternatives

<i>R.S. Gupta et al.</i>	ΔhVV	$\Delta h\bar{t}t$	Δhbb
Mixed-in Singlet	6%	6%	6%
Composite Higgs	8%	tens of %	tens of %
Minimal Supersymmetry	< 1%	3%	10% ^a ,
LHC 14 TeV, 3 ab ⁻¹	8%	10%	15%

Ultimate at LHC
1 ab = 10⁻⁴² cm²

$$\frac{g_{hbb}}{g_{SMbb}} = \frac{g_{h\tau\tau}}{g_{SM\tau\tau}} \simeq 1 + 1.7\% \left(\frac{1 \text{ TeV}}{m_A} \right)^4$$

SUSY tan(β) > 5

$$\frac{g_{hff}}{g_{SMff}} = \frac{g_{hVV}}{g_{SMVV}} \simeq 1 - 3\% \left(\frac{1 \text{ TeV}}{f} \right)^2$$

Composite Higgs

$$\frac{g_{hgg}}{g_{SMgg}} \simeq 1 + 2.9\% \left(\frac{1 \text{ TeV}}{m_T} \right)^2, \quad \frac{g_{h\gamma\gamma}}{g_{SM\gamma\gamma}} \simeq 1 - 0.8\% \left(\frac{1 \text{ TeV}}{m_T} \right)^2$$

Top partners

- Sensitivity to "TeV" new physics for "5 sigma" discoveries may need 1 per-cent to sub 1-per-cent σ accuracies on rates.

Venice, March. 2015

arXiv:1206.3560v3 [hep-ph] 27 Sep 2012

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C. Rubbia

SUSY Extensions of the SM

- MSSM: the Higgs sector contains at least two Higgs doublets and the resulting spectrum of physical Higgs fields includes three neutral Higgs bosons, the CP-even h_0 and H_0 and the CP-odd A_0 .
- The couplings of the MSSM Higgs bosons to fermions and vector bosons are determined by $\tan \beta$ and the mixing angle α between the neutral Higgs states h_0 and H_0 .
- The Higgs boson widths are then crucial parameters, and for this study the muon collider is particularly suitable.
- Tests of lepton universality of Higgs couplings.
 - Crucial role played by the beam energy resolution for study of the widths in the case of muon colliders.
- Non minimal extensions of MSSM → neutral Higgs bosons.

The quest for Higgs Factories

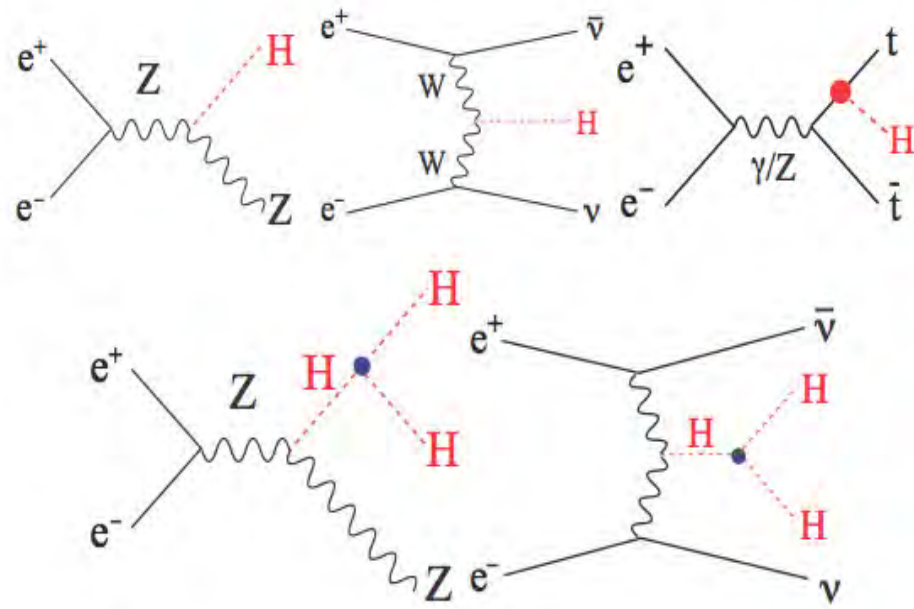
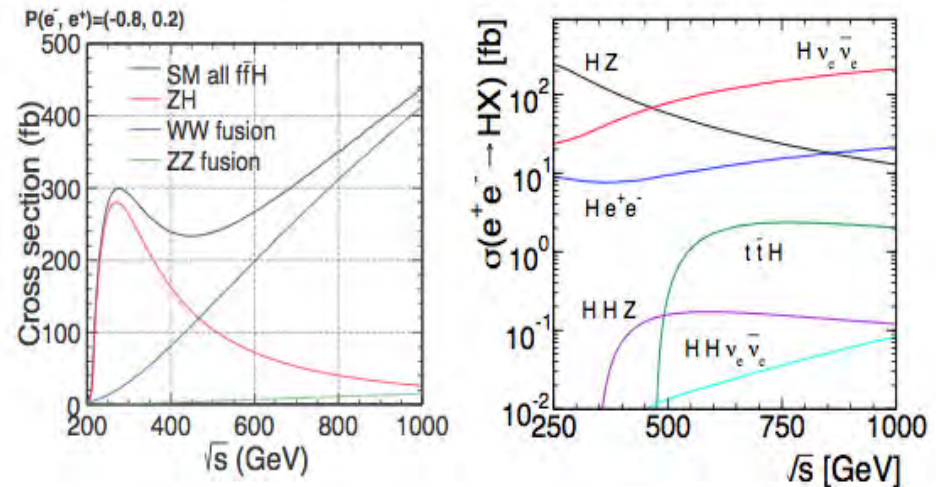
- Two possible future lepton alternatives:

- A e^+e^- collider at $L > 10^{34}$ and a $Z+H_0$ signal of ≈ 200 fb. The circumference of a new, LEP-like ring is of about ≈ 80 km or of a Linear Collider of 31 km.
- A $\mu^+\mu^-$ collider at $L > 10^{32}$ and a H_0 signal in the s -state of $\approx 20'000$ fb. The collider radius is much smaller, only ≈ 50 m, but the novel "muon cooling" facility is required.

C. Rubbia

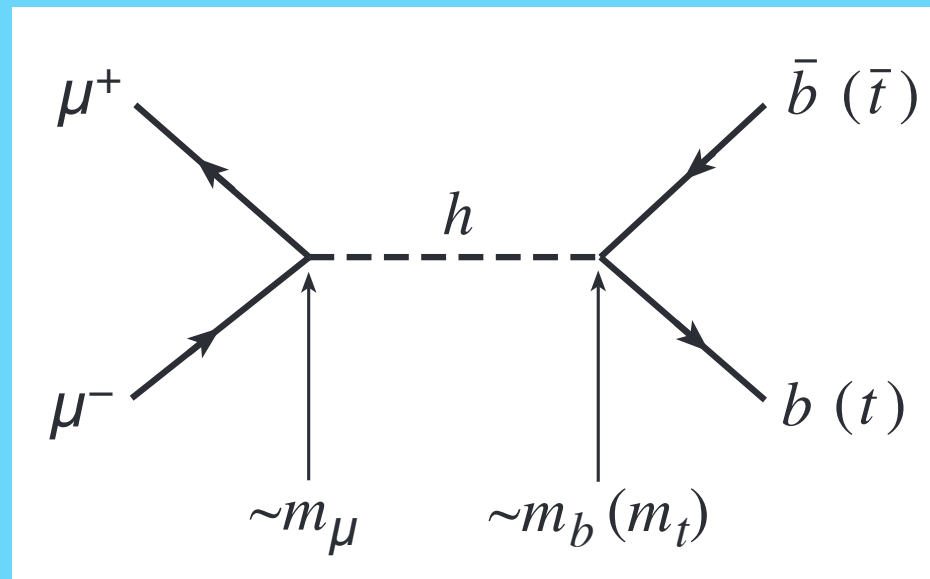
Production cross sections at the $e^+ e^-$ collider

- The production cross sections of the Higgs boson with the mass of 125 GeV for e^+e^- as a function of the energy \sqrt{s} .
- The cross sections of the production processes as a function of the \sqrt{s} collision energy.
- The Higgs-strahlung diagram (Left), the W-boson fusion process (Middle) and the top-quark association (Right).
- Double Higgs boson diagrams via off-shell Higgs-strahlung (Left) and W-boson fusion (Right) processes



Muon Collider

- The s-channel cross section is much higher and allows a direct and very precise measurement of the H total and partial widths. Tests of universality of H couplings.



- Possibility to detect and measure with precision more scalars, if any, and therefore to distinguish among the various extensions of the SM. Scalars close in mass.

Muon Collider

- The s-channel cross section is much higher and allows a direct and very precise measurement of the H total and partial widths. Possibility to detect and measure with precision more scalars, if any, and therefore to distinguish among the various extensions of the SM.

However:

- Key role is played by the beam energy resolution.
- Great importance of QED radiative effects for a precision study of the line-shape and Sign/Backg ratio. Not enough emphasized in the past.

Radiative effects

- In the case of a Higgs factory through a muon collider, sizeable QED radiative effects - of order of 50% - must be carefully taken into account for a precise measurement of the leptonic and total widths of the Higgs particle.
- Those effects do not apply in the case of Higgs production in electron-positron colliders.
- ISR effects similar to J/Psi, Z, ... production in e+e- annihilation, but not accounted for in previous studies.

-

M. G. [arXiv:1503.05046](https://arxiv.org/abs/1503.05046)

S. Jadach, R. Kycia [arXiv:1509.02406](https://arxiv.org/abs/1509.02406)

I S R effect

- Correction factor $\propto (\Gamma/M)^{(4\alpha/\pi) \log(2E/m)}$
modifies the lowest order cross section by o(50%).

- By defining:
$$\beta_i = \frac{4\alpha}{\pi} \left[\log \frac{W}{m_i} - \frac{1}{2} \right], \quad \begin{aligned} y &= W - M \\ \tan \delta_R(W) &= \frac{1}{2} \Gamma / (-y) \end{aligned}$$

Infrared factor modifies

M.G., Pancheri, Srivastava, Nucl. Phys. B101, 1975
and B171, 1980

Born cross section as:

M.C. Codes for LEP (Zfitter,...)

$$C_{infra}^{res} = \left(\frac{y^2 + (\Gamma/2)^2}{(M/2)^2} \right)^{\beta_i/2} \left[1 + \beta_i \frac{y}{\Gamma/2} \delta_R \right]$$

to o(1-2 %) accuracy

- At $W = 2E = M$

$$\beta_i = 0.061$$

$$C_{infra}^{res} = (\Gamma/M)^{\beta_i} = 0.53,$$

- The effect is very similar to the case of J/Psi, Z production in e+e- annihilation. Background situation is different.
- Folding with beam energy resolution:

- Since the resonance is quite narrow, one has to integrate over the machine resolution

$$G(W' - W) = \frac{1}{\sqrt{2\pi}\sigma} e^{-(W' - W)^2 / (2\sigma^2)}$$

$$\tilde{\sigma}(W) = \int G(W' - W) dW' \sigma(W')$$

- Then the observed cross section at the peak is, to o(1%) accuracy:

$$\tilde{\sigma}(M) = \frac{2\pi^2 \Gamma_i \Gamma_f}{\sqrt{2\pi} \sigma M^2 \Gamma} \left(\frac{\Gamma}{M} \right)^{\beta_i} e^{\left(\frac{\Gamma}{2\sqrt{2}\sigma} \right)^2} \left\{ \operatorname{erfcf} \left(\frac{\Gamma}{2\sqrt{2}\sigma} \right) + \frac{1}{2} \beta_i E_1 \left(\frac{\Gamma^2}{8\sigma^2} \right) \right\}$$

--> Numerical results for SM Higgs. The correction factor C is:

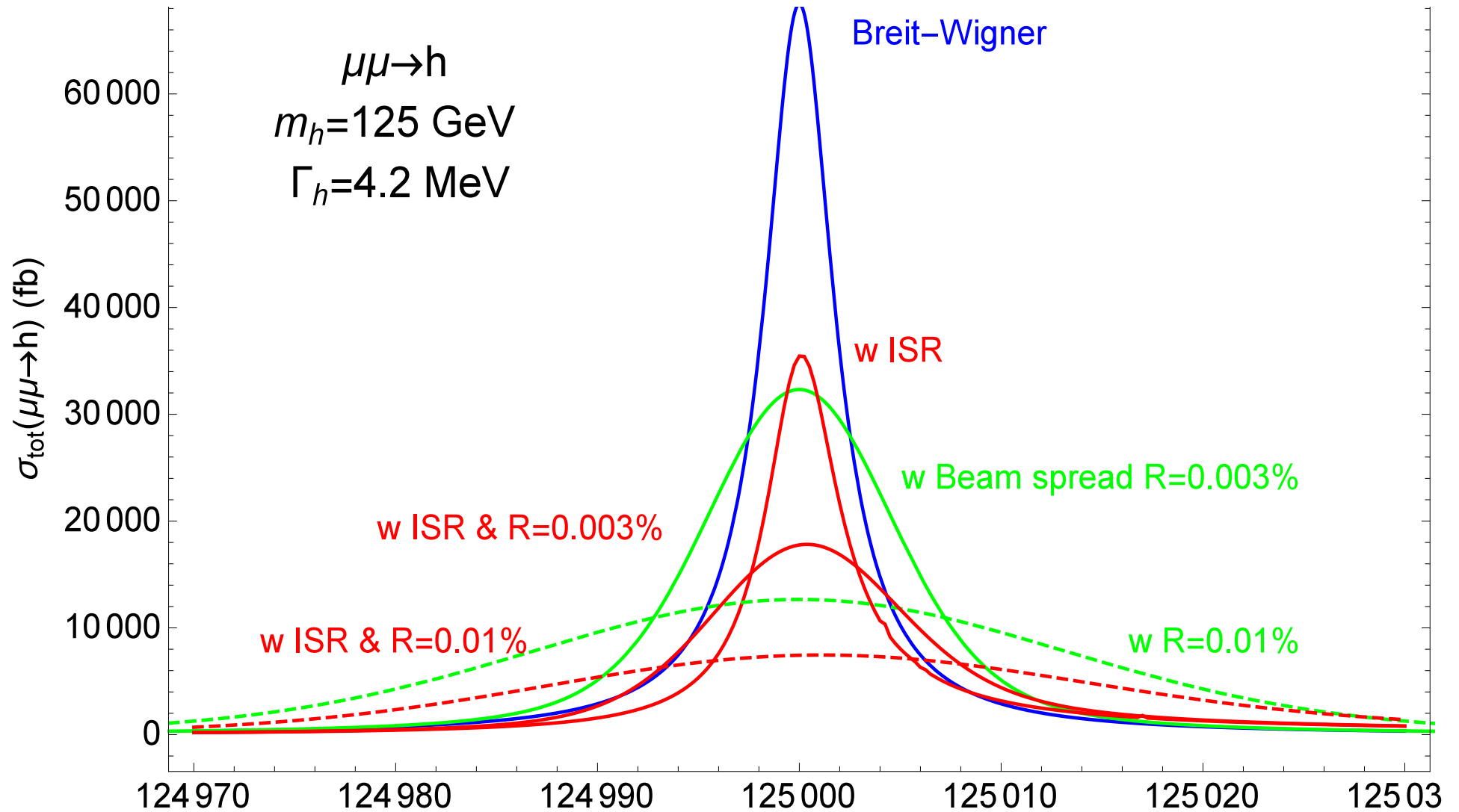
$$C = 0.47, \quad 0.37, \quad 0.30, \quad 0.20$$

for

$$\sigma = 1 \text{ MeV}, 2 \text{ MeV}, 3 \text{ MeV}, 4 \text{ MeV},$$

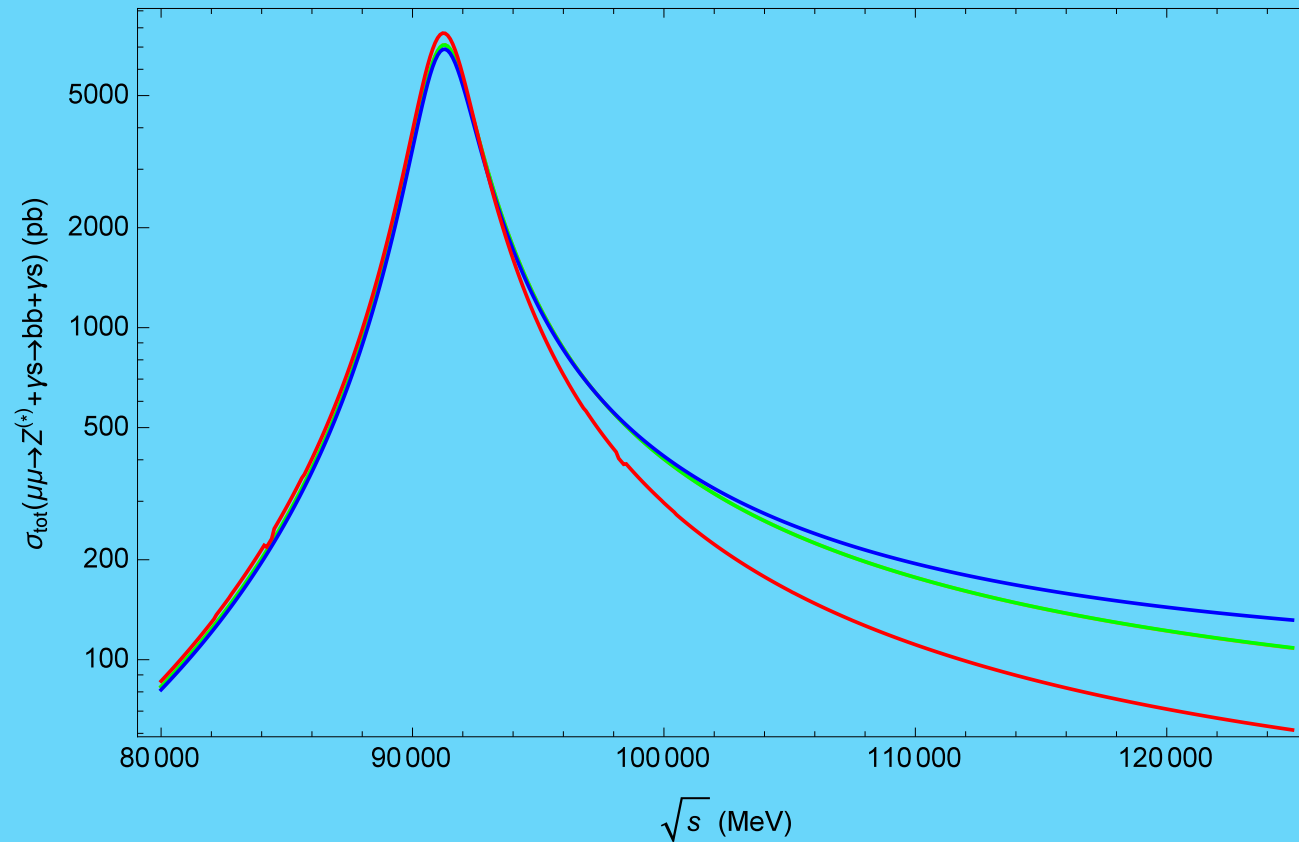
--> Important reduction of the Born Higgs signal.

Higgs line shape



Signal/Backg ratio is affected by r. c. and beam energy spread

- Background coming from Z radiative tail:



← Different accuracy in QED structure functs. of initial beams

M.G., T. Han, Z. Liu

Previous Signal/Background studies:

T. Han and Z. Liu

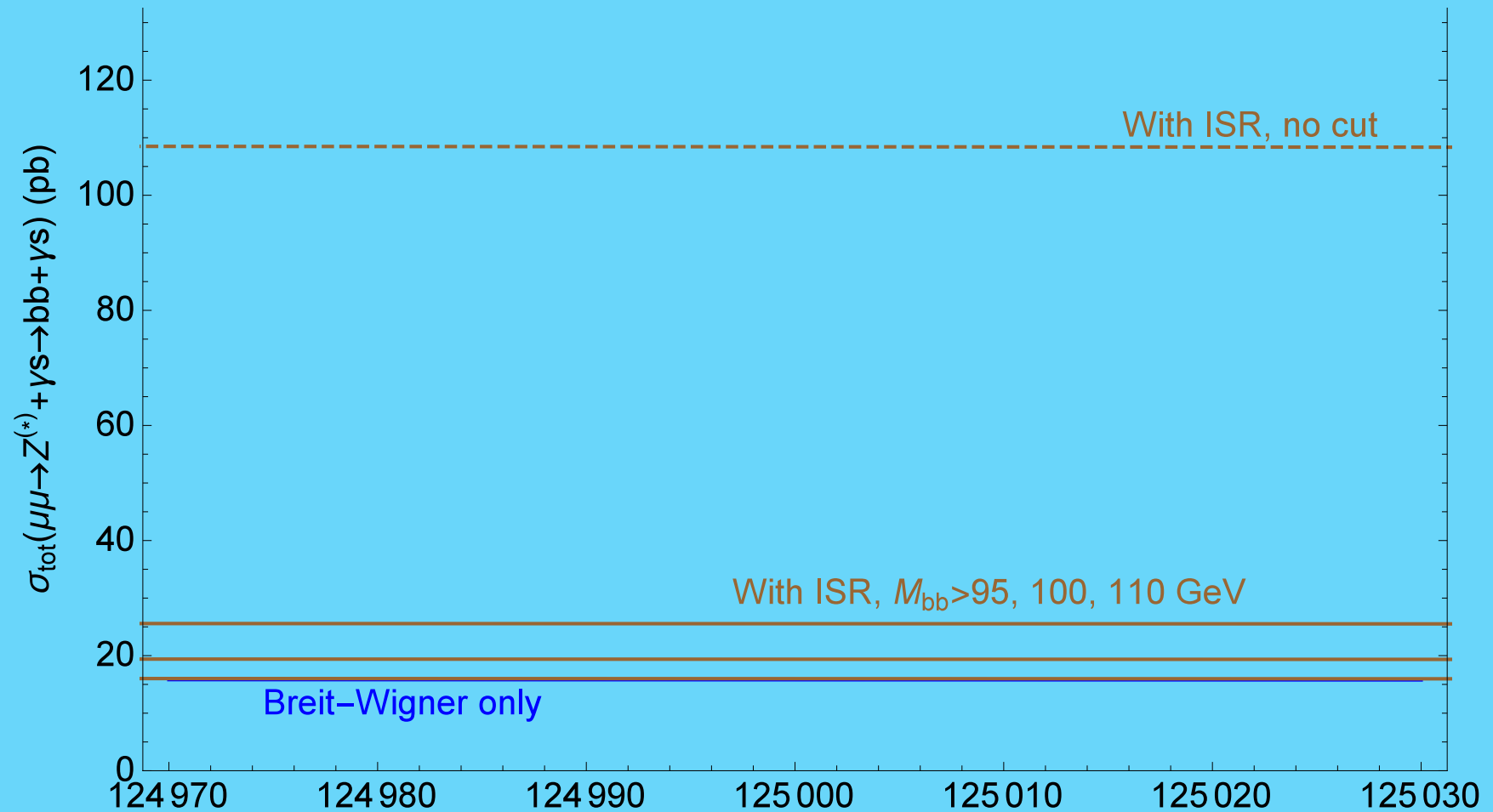
(arXiv:1210.7803v2)

R (%)	$\mu^+ \mu^- \rightarrow h$ σ_{eff} (pb)	$h \rightarrow b\bar{b}$		$h \rightarrow WW^*$	
		σ_{Sig}	σ_{Bkg}	σ_{Sig}	σ_{Bkg}
0.01	16	7.6	15	3.7	0.051
0.003	38	18		5.5	

Effective cross sections (in pb) at the resonance for two choices of beam energy resolutions R and two leading decay channels, with the SM branching fractions.

(No radiative effects included yet)

Backg. cross section vs. M_{bb} cuts



Signal/Background ratio

R (%)	$\mu^+\mu^- \rightarrow h$ σ_{eff} (pb)	$h \rightarrow b\bar{b}$		$h \rightarrow WW^*$	
		σ_{Sig}	σ_{Bkg}	σ_{Sig}	σ_{Bkg}
0.01	7.3	3.4	20	1.7	0.051
0.003	17	8.0		2.5	

The bb background is shown with a 100 GeV m_{bb} cut applied to the signal and background.

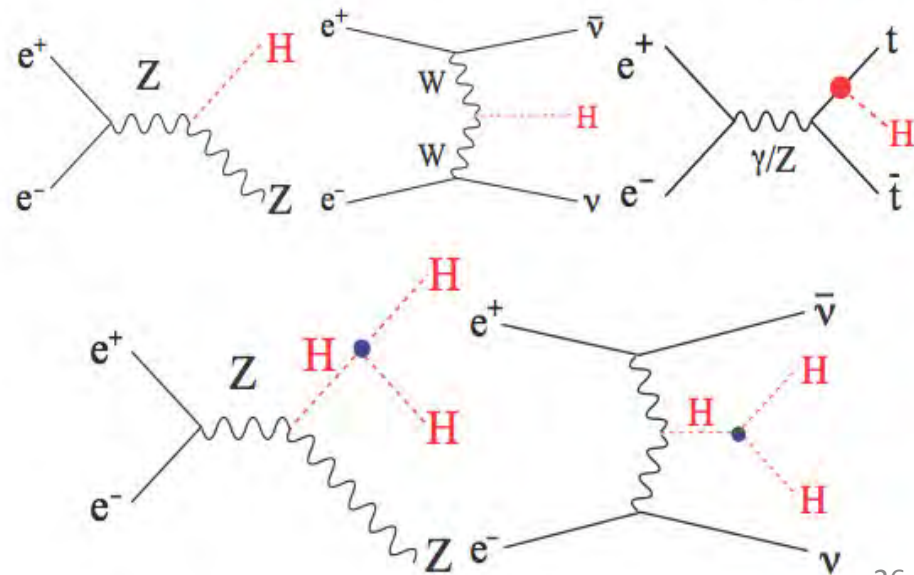
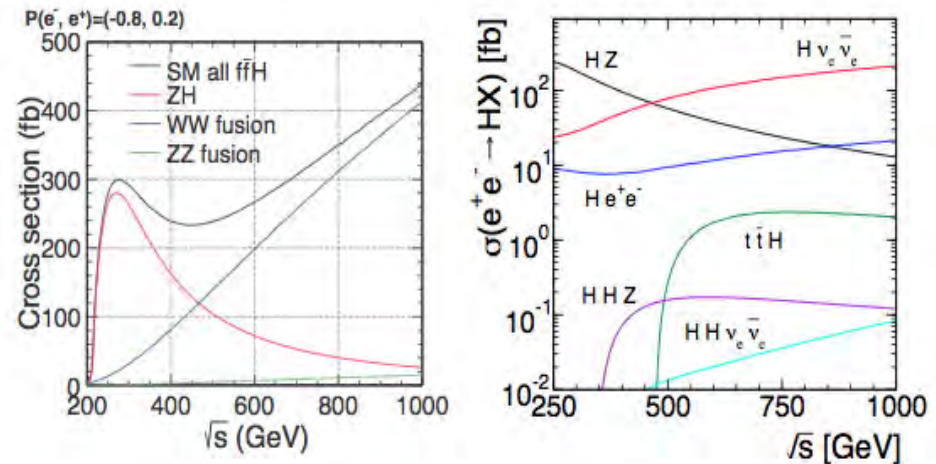
M.G., T. Han, Z. Liu

The energy spread plays a role on the Sign/Backg. ratio

- No similar effects for e+e- colliders

Production cross sections at the e+ e- collider

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Conclusions

- Precision studies of the properties of the Higgs particle are mandatory.
- Various proposals of electron and muon colliders have been suggested.
- Muon collider seems more appropriate for measuring the Higgs width and couplings, checking flavour universality, trying discover and investigate the scalar sector predicted in various extensions of the SM.
- Sizeable radiative effects – of order 50% or larger – must be carefully taken into account for high precision measurements.
- The issue of muon cooling is really crucial. In addition to L the energy spread of beams plays an important role.