



QCD corrections to SUSY particle production at the LHC

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Aachen Bonn Heidelberg Mainz





- Inclusive cross sections at NLO+NLL
- Differential distributions at NLO with parton shower
- Tools
- Outlook

LHC SUSY cross section working group

https://twiki.cern.ch/twiki/bin/view/LHCPhysics/SUSYCrossSections

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LHC SUSY Cross Section Working Group

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+ LHC SUSY Cross Section Working Group

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Overview



Reference: Squark and gluino production cross sections in pp collisions at \sqrt(s) = 13, 14, 33 and 100 TeV at, C. Borschensky, M. Kramer, A. Kulesza, M. Mangano, S. Padhi, T. Plehn, X. Portell, arXiv:1407.5066, Published in Eur.Phys.J. C74 (20

SUSY Cross Sections using 7 TeV pp collisions

Abstract

We summarise the status of the cross section predictions for various supersymmetric processes in pp collisions at sqrt(s)=7 TeV. This document is based on the agreement between the ATLAS and CMS collaborations, as well as with the LPCC SU working group. Calculations including the resummation of soft gluon emission at the next-to-leading logarithmic accuracy are used whenever available. In all other cases we rely on the next-to-leading order in the strong coupling constant. These or uncertainties are provided for various scale and PDF choices.

The space of SUSY theories...



The minimal supersymmetric model

Field Content of the MSSM					
Super-	Boson	Fermionic			
Multiplets	Fields	Partners	SU(3)	SU(2)	U(1)
gluon/gluino	g	\widetilde{g}	8	1	0
gauge/	W^{\pm},W^0	$\widetilde{W}^{\pm},\widetilde{W}^{0}$	1	3	0
gaugino	B	\widetilde{B}	1	1	0
slepton/	$(\widetilde{\nu}, \widetilde{e}^-)_L$	$(\nu, e^-)_L$	1	2	-1
lepton	\tilde{e}_R^-	e_R^-	1	1	-2
squark/	$(\widetilde{u}_L, \widetilde{d}_L)$	$(u,d)_L$	3	2	1/3
quark	\widetilde{u}_R	u_R	3	1	4/3
	\widetilde{d}_R	d_R	3	1	-2/3
Higgs/	(H_d^0, H_d^-)	$(\widetilde{H}_d^0, \widetilde{H}_d^-)$	1	2	-1
higgsino	(H_u^+, H_u^0)	$(\widetilde{H}_u^+, \widetilde{H}_u^0)$	1	2	1

The minimal supersymmetric model

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Multiplets	Fields	Partners	SU(3)	SU(2)	$\mathrm{U}(1)$
gluon/glu Squark and gluino production				0	
gauge,				0	
gaugin large cross sections 				0	
slepton • largely model-independent				-1	
leptor				-2	
squark • large higher-order QCD effects				1/3	
quark	\widetilde{u}_R	u_R	3	1	4/3
	\widetilde{d}_R	d_R	3	1	-2/3
Higgs/	(H_d^0,H_d^-)	$(\widetilde{H}_d^0, \widetilde{H}_d^-)$	1	2	-1
higgsino	(H_u^+, H_u^0)	$(\widetilde{H}_u^+, \widetilde{H}_u^0)$	1	2	1

$$\mathcal{L}_{\text{SUSY-QCD}} = -\frac{1}{4} F^{a}_{\mu\nu} F^{\mu\nu a} + \frac{i}{2} \bar{\tilde{g}}^{a} \gamma^{\mu} (\partial_{\mu} \delta^{ac} - g_{s} f^{abc} g^{b}_{\mu}) \tilde{g}^{c} + |D^{\mu} \tilde{q}_{jL}|^{2} + |D^{\mu} \tilde{q}_{jR}|^{2} + i \bar{q}_{j} \gamma^{\mu} D_{\mu} q_{j} - \frac{1}{2} m_{\tilde{g}} \bar{\tilde{g}}^{a} \tilde{g}^{a} - m_{\tilde{q}_{jL}}^{2} \tilde{q}^{*}_{jL} \tilde{q}_{jL} - m_{\tilde{q}_{jR}}^{2} \tilde{q}^{*}_{jR} \tilde{q}_{jR} - \frac{1}{2} g^{2}_{s} (\tilde{q}^{*}_{jL} T^{a} \tilde{q}_{jL} - \tilde{q}^{*}_{jR} T^{a} \tilde{q}_{jR})^{2} - \sqrt{2} g_{s} (\bar{q}_{jL} T^{a} \tilde{g}^{a} \tilde{q}_{jL} + \tilde{q}^{*}_{jL} \bar{\tilde{g}}^{a} T^{a} q_{jL} - \tilde{q}^{*}_{jR} \bar{\tilde{g}}^{a} T^{a} q_{jR} - \bar{q}_{jR} \tilde{g}^{a} T^{a} \tilde{q}_{jR})$$



$$\mathcal{L}_{\text{SUSY-QCD}} = -\frac{1}{4} F^{a}_{\mu\nu} F^{\mu\nu a} + \frac{i}{2} \bar{\tilde{g}}^{a} \gamma^{\mu} (\partial_{\mu} \delta^{ac} - g_{s} f^{abc} g^{b}_{\mu}) \tilde{g}^{c} + |D^{\mu} \tilde{q}_{jL}|^{2} + |D^{\mu} \tilde{q}_{jR}|^{2} + i \bar{q}_{j} \gamma^{\mu} D_{\mu} q_{j} - \frac{1}{2} m_{\tilde{g}} \bar{\tilde{g}}^{a} \tilde{g}^{a} - m_{\tilde{q}_{jL}}^{2} \tilde{q}^{*}_{jL} \tilde{q}_{jL} - m_{\tilde{q}_{jR}}^{2} \tilde{q}^{*}_{jR} \tilde{q}_{jR} - \frac{1}{2} g^{2}_{s} (\tilde{q}^{*}_{jL} T^{a} \tilde{q}_{jL} - \tilde{q}^{*}_{jR} T^{a} \tilde{q}_{jR})^{2} - \sqrt{2} g_{s} (\bar{q}_{jL} T^{a} \tilde{g}^{a} \tilde{q}_{jL} + \tilde{q}^{*}_{jL} \bar{\tilde{g}}^{a} T^{a} q_{jL} - \tilde{q}^{*}_{jR} \bar{\tilde{g}}^{a} T^{a} q_{jR} - \bar{q}_{jR} \tilde{g}^{a} T^{a} q_{jR})$$



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We assume R-parity conservation

$$\rightarrow \quad \mathcal{W} = \lambda_{ijk}^{\prime\prime} U_i^c D_j^c D_k^c \qquad \text{etc}$$

→ sparticles are produced in pairs; the LSP is stable

$$\mathcal{L}_{\text{SUSY-QCD}} = -\frac{1}{4} F^{a}_{\mu\nu} F^{\mu\nu a} + \frac{i}{2} \bar{\tilde{g}}^{a} \gamma^{\mu} (\partial_{\mu} \delta^{ac} - g_{s} f^{abc} g^{b}_{\mu}) \tilde{g}^{c} + |D^{\mu} \tilde{q}_{jL}|^{2} + |D^{\mu} \tilde{q}_{jR}|^{2} + i \bar{q}_{j} \gamma^{\mu} D_{\mu} q_{j}$$
$$- \frac{1}{2} m_{\tilde{g}} \bar{\tilde{g}}^{a} \tilde{g}^{a} - m_{\tilde{q}_{jL}}^{2} \tilde{q}^{*}_{jL} \tilde{q}_{jL} - m_{\tilde{q}_{jR}}^{2} \tilde{q}^{*}_{jR} \tilde{q}_{jR} - \frac{1}{2} g^{2}_{s} (\tilde{q}^{*}_{jL} T^{a} \tilde{q}_{jL} - \tilde{q}^{*}_{jR} T^{a} \tilde{q}_{jR})^{2}$$
$$- \sqrt{2} g_{s} (\bar{q}_{jL} T^{a} \tilde{g}^{a} \tilde{q}_{jL} + \tilde{q}^{*}_{jL} \bar{\tilde{g}}^{a} T^{a} q_{jL} - \tilde{q}^{*}_{jR} \bar{\tilde{g}}^{a} T^{a} q_{jR} - \bar{q}_{jR} \tilde{g}^{a} T^{a} q_{jR})$$

Squarks mix to form mass eigenstates

$$\mathcal{M}^2 = \begin{pmatrix} m_Q^2 + m_q^2 + \left(\frac{1}{2} - \frac{2}{3}s_w^2\right)m_z^2\cos(2\beta) & -m_q\left(A_q + \mu\cot\beta\right) \\ -m_q\left(A_q + \mu\cot\beta\right) & m_U^2 + m_q^2 + \frac{2}{3}s_w^2m_z^2\cos(2\beta) \end{pmatrix}$$

- → the mixing is proportional to the quark mass
- → mixing is relevant for the 3rd generation

squark-antisquark

 \vec{q} \vec{q} \vec{q} \vec{q} \vec{q} \vec{q} \vec{q} \vec{q} \vec{q}

 $\tilde{p} = \frac{1}{2} \frac{1}{$

squark-squark









squark-gluino



The cross sections only depend on the SUSY masses

e.g. gluino pair production

$$g_{mn} = \widetilde{g} + \widetilde{g}$$

$$\sigma^B(gg \to \tilde{q}\bar{\tilde{q}}) = \frac{n_f \pi \alpha_s^2}{s} \left[\beta_{\tilde{q}} \left(\frac{5}{24} + \frac{31m_{\tilde{q}}^2}{12s} \right) + \left(\frac{4m_{\tilde{q}}^2}{3s} + \frac{m_{\tilde{q}}^4}{3s^2} \right) \log \left(\frac{1 - \beta_{\tilde{q}}}{1 + \beta_{\tilde{q}}} \right) \right]$$

where
$$\beta_{\tilde{g}} = \sqrt{1 - 4m_{\tilde{g}}^2/s} \to 0$$
 at threshold

Kane, Leveille; Harrison, Llewellyn Smith, Reya, Roy; Dawson, Eichten, Quigg; Baer, Tata ('82-'85)



Borschensky, MK, Kulesza, Mangano, Padhi, Plehn, Portell (1407.5066 [hep-ph])



based on Prospino and NLL-fast

renormalization and factorization scale dependence



Beenakker, Brensing, MK, Kulesza, Laenen, Motyka, Niessen ('09-'11)

renormalization and factorization scale dependence



cf. Langenfeld, Moch, Pfoh; Beneke, Falgari, Schwinn, Wever; Kauth, Kress, Kühn; Broggio et al.

PDF uncertainties

LHC 13 TeV, NLO



Beenakker, Borschensky, MK, Kulesza, Laenen, Marzani, Rojo (1510.00375 [hep-ph])

Beyond Prospino/NNL-fast

NLO-QCD corrections for generic MSSM spectra

→ Effect of O(10%) on σ x BR for generic MSSM benchmark scenarios

Hollik, Lindert, Pagani; Goncalves-Netto, Lopez-Val, Mawatari, Plehn, Wigmore; Gavin, Hangst, MK, Mühlleitner, Pellen, Popenda, Spira

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EWK corrections (EWK loops, EWK x QCD, γ-induced processes)

- → model dependent
- → O(few %) for inclusive cross sections
- \rightarrow more significant for specific processes and large Q²

see e.g. Hollik, Lindert, Mirabella, Pagani (1506.01052 [hep-ph]) and references therein

Squark and gluino production and decay

NLO differential distributions with parton showers



Gavin, Hangst, MK, Mühlleitner, Pellen, Popenda, Spira; cf. Hollik, Lindert, Pagani; Boughezal, Schulze

Squark and gluino production and decay

NLO differential distributions with parton showers



Degrande, Fuks, Hirschi, Proudhom, Shao (1510.00391[hep-ph])

Prospino, NLL-fast, MadGolem, sPOWHEG, MadGraph5_aMC@NLO, ...

Prospino, NLL-fast, MadGolem, sPOWHEG, MadGraph5_aMC@NLO, ...

Prospino: <u>http://www.thphys.uni-heidelberg.de/~plehn/index.php?show=prospino&visible=tools</u>

Our 20 year old warhorse, a bit worn down but still useful

Beenakker, Höpker, Klasen, MK, Plehn, Spira, Zerwas ('94-'??)



Prospino, NLL-fast, MadGolem, sPOWHEG, MadGraph5_aMC@NLO, ...

NLL-fast: http://pauli.uni-muenster.de/~akule_01/nllwiki/index.php/NLL-fast

The current standard tool for inclusive NLO+NLL cross section calculations

Beenakker, Borschensky, MK, Kulesza, Laenen, Motyka, Niessen, Thewes ('09-'14)



Prospino, NLL-fast, MadGolem, sPOWHEG, MadGraph5_aMC@NLO, ...

NLL-fast: http://pauli.uni-muenster.de/~akule_01/nllwiki/index.php/NLL-fast

NNLL-fast is on its way

Beenakker, Borschensky, MK, Kulesza, Laenen Theeuwes, Thewes, in preparation



Prospino, NLL-fast, **MadGolem**, sPOWHEG, MadGraph5_aMC@NLO, ...

MadGolem: code available from authors

NLO squark and gluino production for generic MSSM spectra

Goncalves-Netto, Lopez-Val, Mawatari, Plehn, Wigmore ('13)



Prospino, NLL-fast, MadGolem, **sPOWHEG**, MadGraph5_aMC@NLO, ...

sPOWHEG: <u>http://powhegbox.mib.infn.it</u>

NLO squark production and decay matched to parton showers

POWHEG team + Gavin, Hangst, MK, Mühlleitner, Pellen, Popenda, Spira ('14)



Prospino, NLL-fast, MadGolem, sPOWHEG, MadGraph5_aMC@NLO, ...

MadGraph5_aMC@NLO: https://launchpad.net/mg5amcnlo

NLO squark & gluino production and decay matched to parton showers

Degrande, Fuks, Goncalves Netto, Hirschi, Lopez-Val, Mawatari, Pagani, Proudom, Shao, Zaro, in preparation



The LHC SUSY cross section working group

will

- provide an update of the SUSY cross section recommendation at NNLL, and including recent pdfs;
- quantify the difference between Mellin space ↔ SCET resummation;
- collect benchmark results for EWK corrections;
- provide links to NLO SUSY tools, together with benchmark results for validation.

A lot of effort (> 20 years) went into calculating higher-order QCD corrections for squark and gluino production

The theoretical uncertainty for inclusive cross sections is ≦ 15%, and is now dominated by the pdf error

In the future, we need to work towards automated NLO calculations for more generic models, including NLL resummation

Thank you!



Why do we bother to go beyond NLO?

$$\sigma_{gg \to t\bar{t}\bar{t}}^{(1,\text{thr})} = \frac{\pi \alpha_{\rm s}^2(\mu^2)}{16m^2} \frac{N_c^2 - 2}{N_c(N_c^2 - 1)} \beta \left(1 + 4\pi \alpha_{\rm s}(\mu^2) \left\{ \frac{2C_F - \frac{N_c^2 - 4}{N_c^2 - 2}C_A}{16\beta} - \frac{N_c^2 - 4}{N_c^2 - 2}\frac{C_A}{4\pi^2} \log(8\beta^2) + \frac{2C_A}{4\pi^2} \left[\log^2(8\beta^2) - 4\log(8\beta^2) - \log(8\beta^2) \log\left(\frac{\mu^2}{m^2}\right) \right] \right\} \right).$$

Higher-order corrections introduce large logarithms

These logarithms can be summed to all orders

Threshold resummation



Kidonakis, Sterman; Bonciani, Catani, Mangano, Nason; Kidonakis, Odera, Sterman; Catani, Mangano, Nason, Trentadue ('97-'03)

NLL threshold resummation



LHC recommendation: MK, Kulesza, van der Leeuw, Mangano, Padhi, Plehn, Portell (12)

NNLL threshold resummation



Beenakker, Borschensky, MK, Kulesza, Laenen, Theeuwes, Thewes ('14)

So far, to calculate the SUSY-QCD corrections we have assumed that

 $u_{L/R}, d_{L/R}, s_{L/R}, c_{L/R}, b_{L/R}$ are mass degenerate

and we have summed over a swath of subprocesses

$$q_i \bar{q}_j \to \tilde{q}_k^{c1} \tilde{q}_l^{*c2}$$
 and $gg \to \tilde{q}_i^c \tilde{q}_i^{*c}$.

How good an approximation is that?

Let us look at a random cMSSM scenario with

 $m_0/m_{1/2}/A_0 = 825/550/0$ GeV, $\tan(\beta) = 10$ and $\operatorname{sgn}(\mu) = +1$

corresponding to masses

$m_{\tilde{u}_L} = m_{\tilde{c}_L}$	$m_{\tilde{u}_R} = m_{\tilde{c}_R}$	$m_{\tilde{d}_L} = m_{\tilde{s}_L}$	$m_{\tilde{d}_R} = m_{\tilde{s}_R}$	$m_{\tilde{g}}$
1799.53	1760.21	1801.08	1756.40	1602.96

Taking the average squark mass as an input and summing over all subprocesses for squark-antisquark production one gets

K = 1.39

Looking at the individual channels, we find

Process	$\sigma_{ m LO}[{ m fb}]$	$\sigma_{\rm NLO}[{\rm fb}]$	K-factor
$- ilde{u}_L ar{ ilde{u}}_L$	$9.51 \cdot 10^{-2}$	$1.43 \cdot 10^{-1}$	1.50
$ ilde{u}_R \overline{ ilde{u}}_R$	$1.14 \cdot 10^{-1}$	$1.72 \cdot 10^{-1}$	1.51
$ ilde{d}_L ilde{d}_L$	$5.50 \cdot 10^{-2}$	$8.79 \cdot 10^{-2}$	1.60
$ ilde{d}_R ilde{d}_R$	$6.89\cdot10^{-2}$	$1.11 \cdot 10^{-1}$	1.61
$ ilde{u}_L ar{ ilde{u}}_R$	$3.75 \cdot 10^{-1}$	$5.12 \cdot 10^{-1}$	1.37
$ ilde{d}_L ar{d}_R$	$1.41 \cdot 10^{-1}$	$1.70 \cdot 10^{-1}$	1.21
$ ilde{u}_L ilde{d}_L$	$6.98 \cdot 10^{-2}$	$7.89 \cdot 10^{-2}$	1.13
$ ilde{u}_L ilde{d}_R$	$2.98 \cdot 10^{-1}$	$3.54 \cdot 10^{-1}$	1.19
$ ilde{u}_R ilde{d}_L$	$2.94 \cdot 10^{-1}$	$3.49 \cdot 10^{-1}$	1.19
$ ilde{u}_R ilde{d}_R$	$8.36 \cdot 10^{-2}$	$9.54 \cdot 10^{-2}$	1.14
Sum	1.59	2.07	1.30

Gavin, Hangst, MK, Mühlleitner, Pellen, Popenda, Spira ('14)

Looking at the cross section x decay we find

$$\sum_{\text{channels}} \sigma_{\text{NLO}} \cdot \text{BR}^{\text{LO}} \left(\tilde{q} \to \tilde{\chi}_0 q \right) \cdot \text{BR}^{\text{LO}} \left(\tilde{q}^* \to \tilde{\chi}_0 \bar{q} \right) = 0.139 \,\text{fb}.$$

compared to the approximate (Prospino) calculation

 $\sum_{\text{channels}} \sigma_{\text{LO}} \cdot K^{\text{avg}} \cdot \text{BR}^{\text{LO}} \left(\tilde{q} \to \tilde{\chi}_0 q \right) \cdot \text{BR}^{\text{LO}} \left(\tilde{q}^* \to \tilde{\chi}_0 \bar{q} \right) = 0.126 \,\text{fb}.$

Gavin, Hangst, MK, Mühlleitner, Pellen, Popenda, Spira ('14)

Squark & gluino production and decay

NLO differential distributions with parton showers

ATLAS analysis

ATLAS-CONF-2013-047

$$\begin{split} p_T^{j_1} &> 130 \,\text{GeV}, \quad p_T^{j_2} > 60 \,\text{GeV}, \quad E_T > 160 \,\text{GeV}, \\ \frac{E_T}{m_{\text{eff}}} &> 0.2, \quad m_{\text{eff}}^{\text{incl}} > 1 \,\text{TeV}, \quad \Delta \phi(j_{1/2}, \vec{E}_T) > 0.4, \\ &\text{and} \ \Delta \phi(j_3, \vec{E}_T) > 0.4 \quad \text{if} \quad p_T^{j_3} > 40 \,\text{GeV}. \end{split}$$

	ilde q ilde q	$ ilde q ar { ilde q}$
NLO	0.871 fb	0.0781 fb
Pythia	0.883 fb	0.0797 fb
Herwig++	0.895 fb	0.0807 fb

Gavin, Hangst, MK, Mühlleitner, Pellen, Popenda, Spira ('14)