



27<sup>th</sup> RD50 workshop, CERN

# IV-characterization of silicon sensors irradiated up to $2E16n_{eq}/cm^2$

Sven Wonsak<sup>a</sup>, A. Affolder<sup>a</sup>, G. Casse<sup>a</sup>, P. Dervan<sup>a</sup>, S. Kuehn<sup>b</sup>, R. Mori<sup>b</sup>, U. Parzefall<sup>b</sup>, I. Tsurin<sup>a</sup>, M. Wiehe<sup>b</sup>, M. Wormald<sup>a</sup>

<sup>a</sup>: University of Liverpool

<sup>b</sup>: Albert-Ludwigs-Universität Freiburg



- Current scaling:

$$\frac{I(T_2)}{I(T_1)} = \left(\frac{T_2}{T_1}\right)^2 \exp\left(\frac{-E_{eff}}{2k_B} \frac{T_1 - T_2}{T_1 T_2}\right)$$

$E_{eff}$ : effective energy (1.214±0.014eV [1]);  $T_1$ : measurement temperature,  $T_2$ : scaling temperature;  $k_B$ : Boltzmann constant

Use for scaling of current to different temperatures, determination of  $E_{eff}$  from measurement

- Investigate behaviour of current for irradiated sensors

$$\frac{I(\Phi_{eq}) - I(\Phi_0)}{V} = \alpha \Phi_{eq}$$

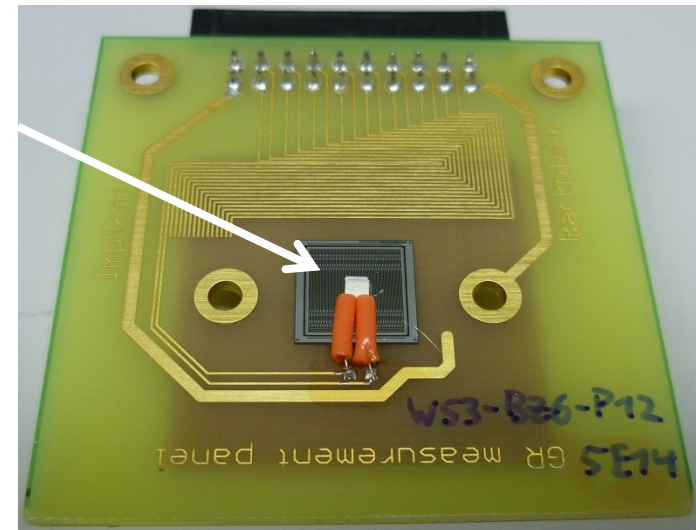
$V$ : depleted volume;  $\Phi_{eq}$ : equivalent fluence;  $I(\Phi_0)$ : nonirradiated current ;  $\alpha$ : current related damage rate

Determination of  $\alpha$  from measurements,  
 $\alpha$  depends on the sensor annealing time

[1]: A. Chilingarov; *Temperature dependence of the current generated in Si bulk*; 2013\_JINST\_8\_P10003

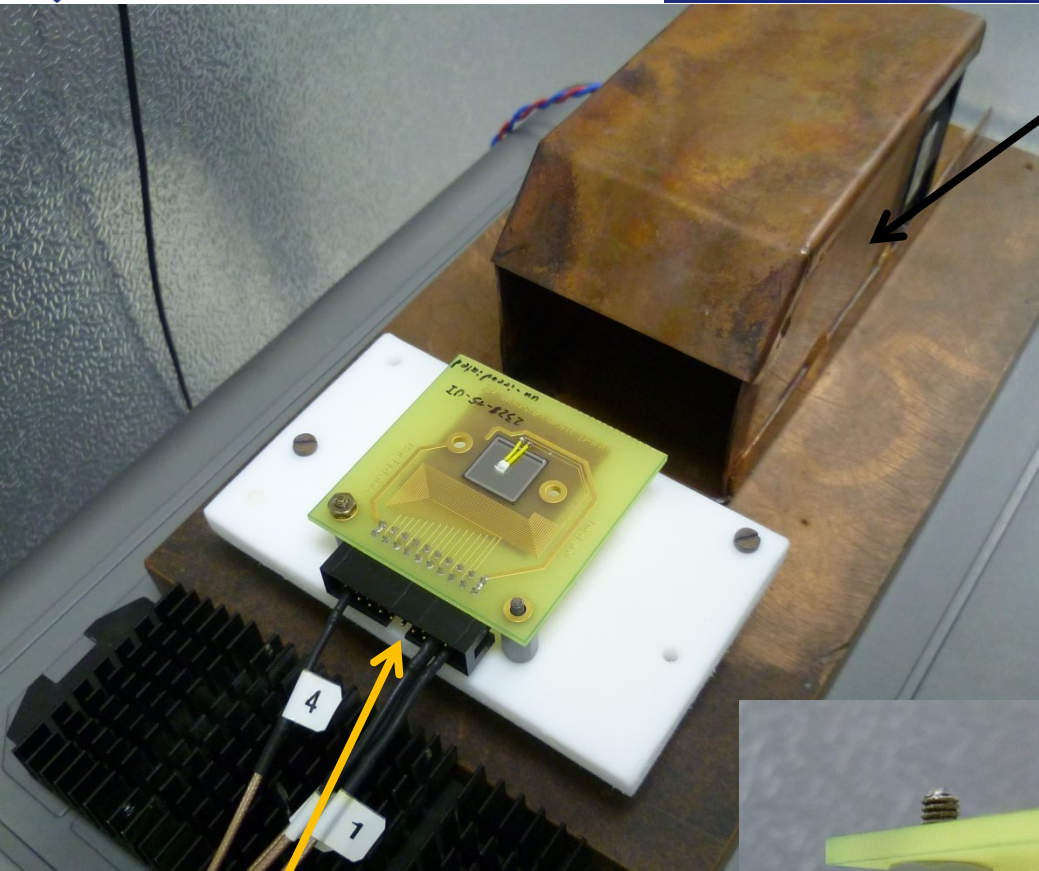


- Irradiate silicon sensors to different fluences
  - Protons (Birmingham):
    - ATLAS07 MINI (293 $\mu\text{m}$ ):  $1 \times 10^{12}$  to  $1 \times 10^{15}$   $n_{\text{eq}}/\text{cm}^2$
  - Neutrons (Ljubljana):
    - ATLAS07 MINI (293 $\mu\text{m}$ ):  $5 \times 10^{15}$  to  $2 \times 10^{16}$   $n_{\text{eq}}/\text{cm}^2$
    - Micron 2437 (143 $\mu\text{m}$ ):  $5 \times 10^{15}$  to  $2 \times 10^{16}$   $n_{\text{eq}}/\text{cm}^2$
    - Micron 2923 (108 $\mu\text{m}$ ):  $5 \times 10^{15}$  to  $2 \times 10^{16}$   $n_{\text{eq}}/\text{cm}^2$
    - Micron 2923 (108 $\mu\text{m}$ ):  $5 \times 10^{15}$  to  $2 \times 10^{16}$   $n_{\text{eq}}/\text{cm}^2$  measured at CERN
    - Micron 3107 (50 $\mu\text{m}$ ):  $1 \times 10^{15}$  to  $2 \times 10^{16}$   $n_{\text{eq}}/\text{cm}^2$
- Glued PT1000 temperature sensor on sensor
- Perform IV/CV measurements in a freezer at different temperatures from  $-23^\circ\text{C}$  to  $-15^\circ\text{C}$  (at least 2 per sensor)
- Room temperature annealing in nitrogen cabinet to total annealing times of 10d and 30d





# Old Liverpool Setup



Fan for air flow

PCB just placed in freezer

Fan for air circulation

Limited by freezer:

If freezer is constantly running a

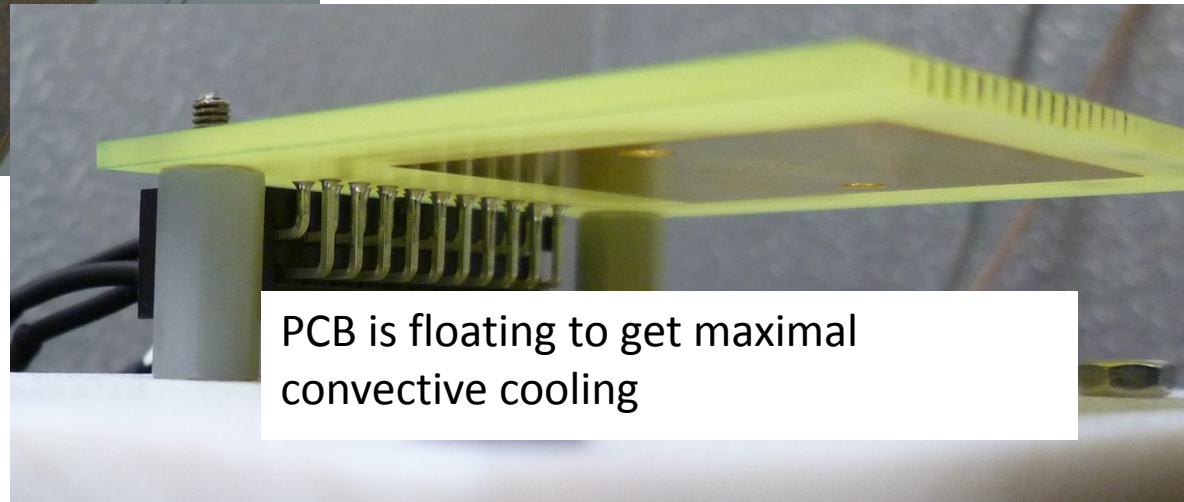
temperature of  $-23^{\circ}\text{C}$  can be reached

For higher temperatures a oscillation

can be observed due to the freezer not

being constantly on

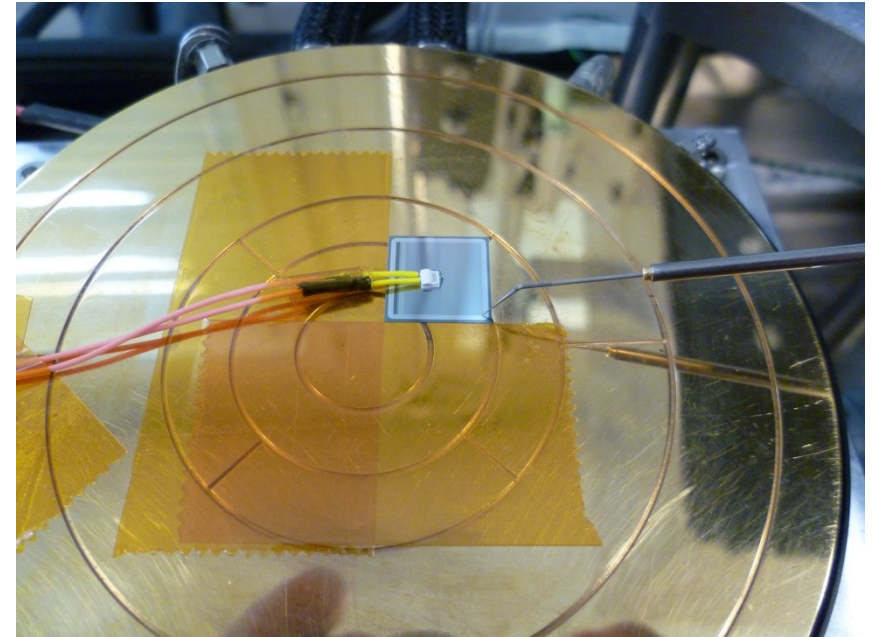
HV and PT1000 read out



PCB is floating to get maximal convective cooling

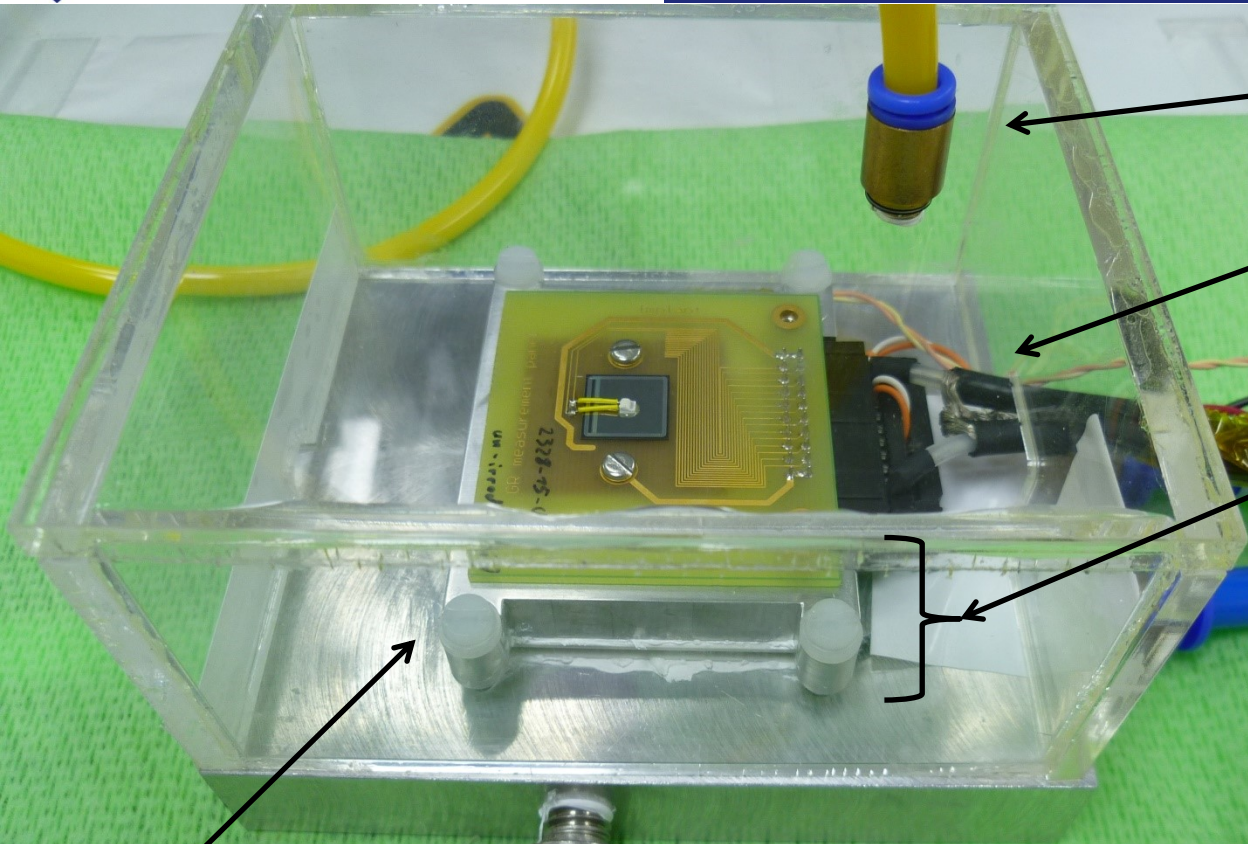


- Cold chuck, cooled by chiller and peltier
- PT1000 glued onto sensor for temperature measurement





# New Liverpool setup



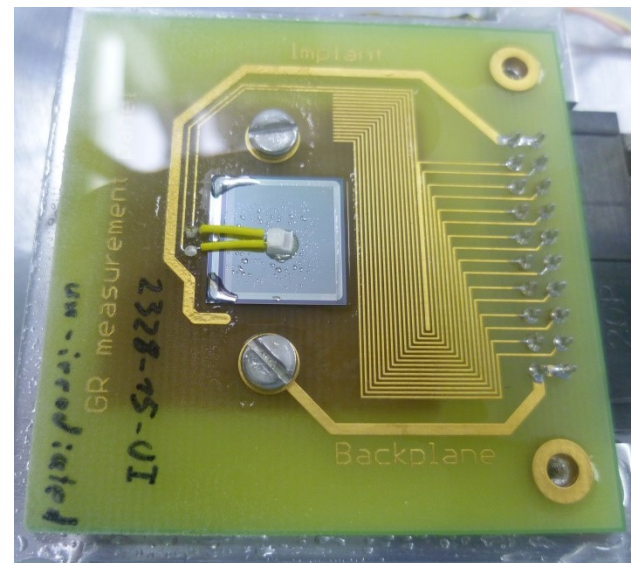
Perspex cover with Nitrogen inlet

HV and PT1000 connector

PCB
Mounting Plate
Peltier
Chuck cooled to chiller

Use Nylon screws to prevent heat loop

Sufficient flow of dry air / nitrogen is very important to prevent ice on sensor

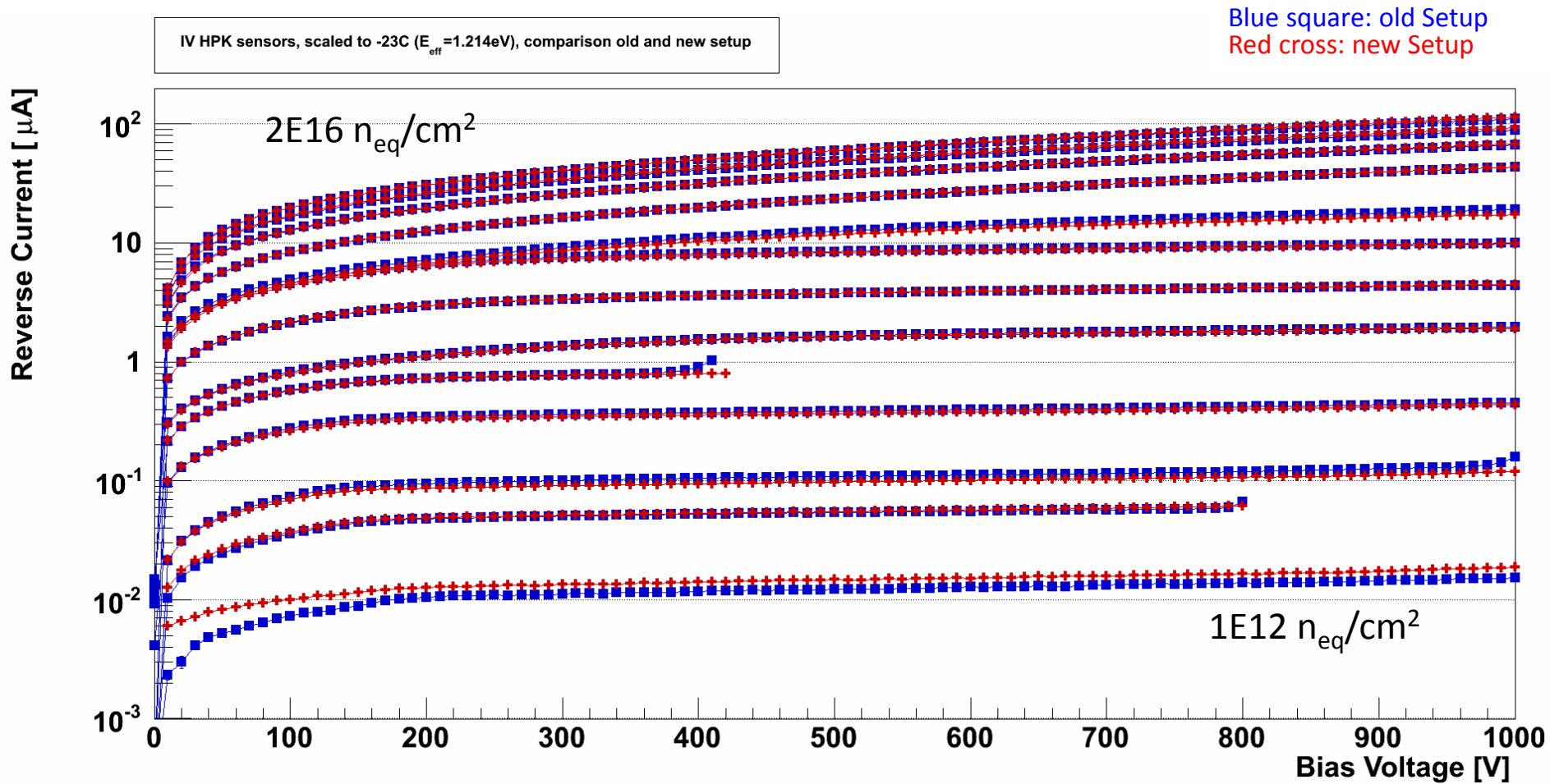




- Same method used in Freiburg
  - Start at highest voltage and ramp down
  - Measurements at  $-25^{\circ}\text{C}$  and  $-20^{\circ}\text{C}$  (PT1000 at chuck)
  - Setup not in freezer
  - Chiller set to  $+5^{\circ}\text{C}$  to prevent ice at tubes; Peltier power set to 15V (3A)
    - At  $-25^{\circ}\text{C}$  use 90% of Peltier power
    - Peltier can cope with higher voltage (up to 29.8V, 6A), but this require a modification of the PID controller
- Cooling with new setup much faster
- PID parameters not optimal, but for first measurements they are acceptable



293 $\mu\text{m}$  sensors (HPK),  $1\text{E}12 \rightarrow 2\text{E}16 \text{ n}_{\text{eq}}/\text{cm}^2$







$$R_t = R_0[1 + AT + BT^2 + C(T - 100^\circ\text{C})T^3]$$

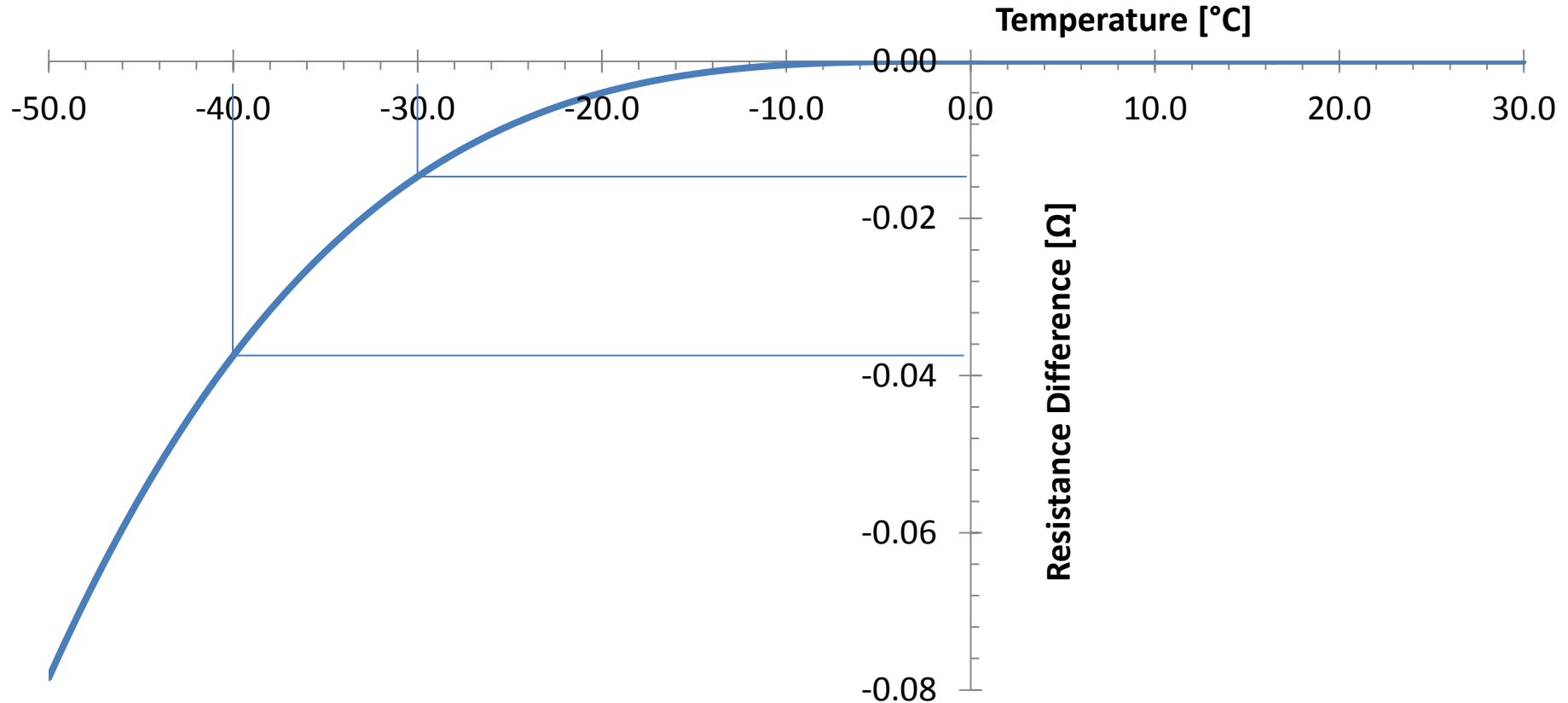
- $T$ : temperature
- $R_0 = 1000\Omega$
- $A = 3.9083 \cdot 10^{-3}^\circ\text{C}^{-1}$
- $B = -5.775 \cdot 10^{-7}^\circ\text{C}^{-2}$
- $C = \begin{cases} -4.183 \cdot 10^{-12}^\circ\text{C}^{-4} & -200^\circ\text{C} \leq T \leq 0^\circ\text{C} \\ 0 & 0^\circ\text{C} \leq T \leq 850^\circ\text{C} \end{cases}$

For temperatures  $< 0^\circ\text{C}$  there is no analytical solution for this equation

- Possible to use a numerical method: calculate resistance for small temperature steps and compare with measured resistance. If values agree within a certain margin, use this temperature
- Use same format as for temperatures  $> 0^\circ\text{C}$  (up to quadratic term), but there is a small deviation



## PT1000 difference quadratic to total



Temperature difference between full equation and “quadratic” approximation  
Up to  $-40^{\circ}\text{C}$  the difference is less than  $0.04\Omega$

- Measurement by hand:  $\sigma_R = 0.1\Omega$
- Automatic measurement:  $\sigma_R \leq 0.02\Omega$



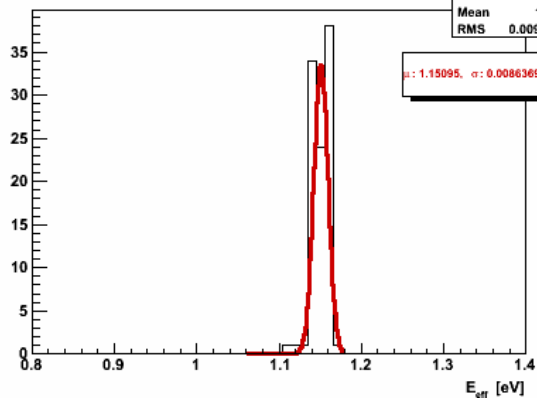
# $E_{\text{eff}}$ and $\alpha$ determination



- Calculate  $E_{\text{eff}}$  for IV measurements
  - $E_{\text{eff}}$  value for each measured voltage
    - Fill data in Histogram
    - Fit with Gauss function
  - Calculate average value
- Fit  $E_{\text{eff}}$  vs Fluence with straight lines
  - Low energy (no slope):  $f(x) = a$
  - High energy:  $f(x) = a - b \log_{10}(x)$

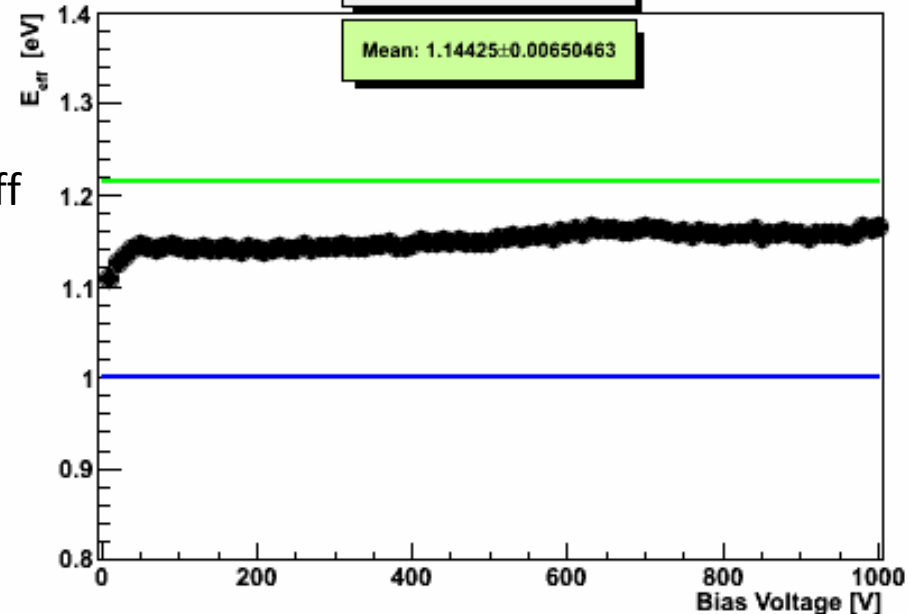


Calculated  $E_{\text{eff}}$

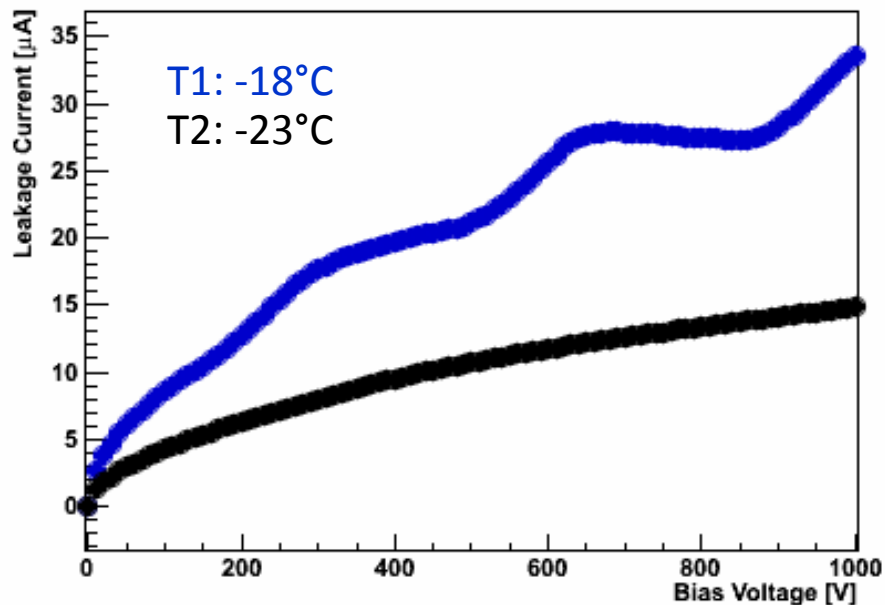


Fairly constant  $E_{\text{eff}}$   
for all voltages  
 $\Rightarrow$  Good Gauss fit

$E_{\text{eff}}$  vs Voltage

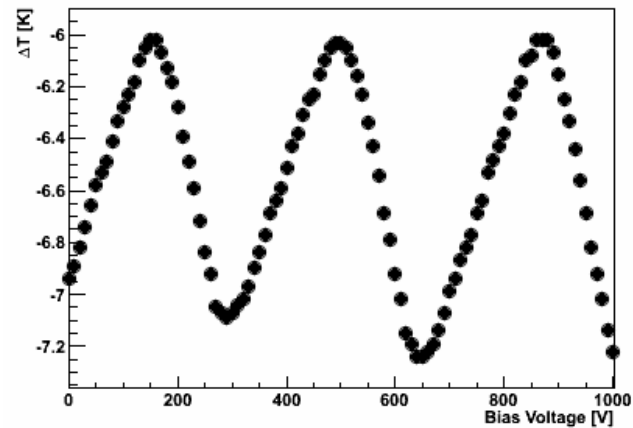


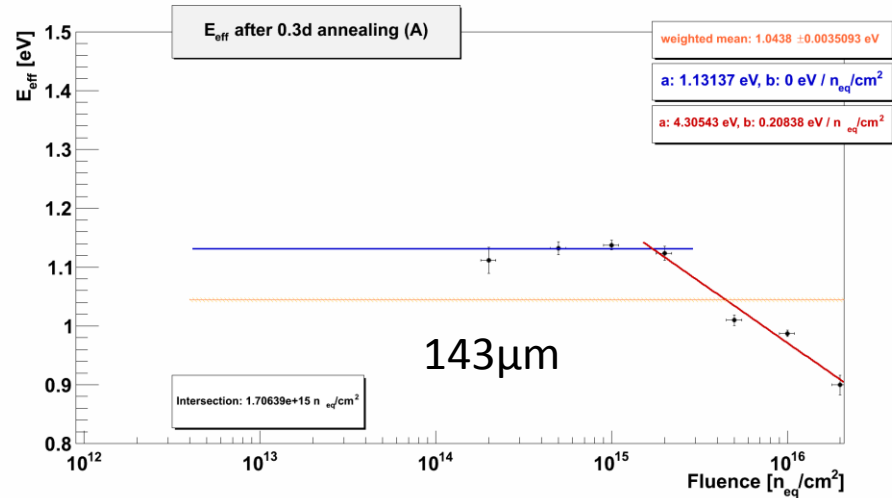
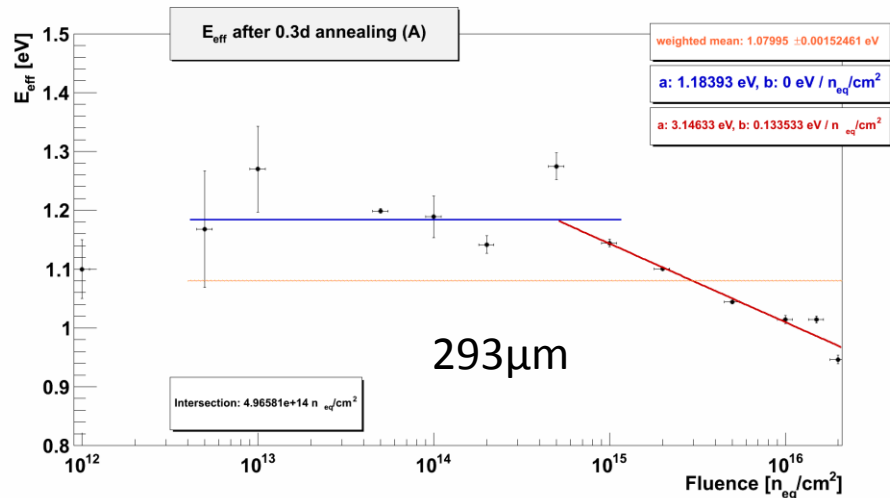
IV Curves



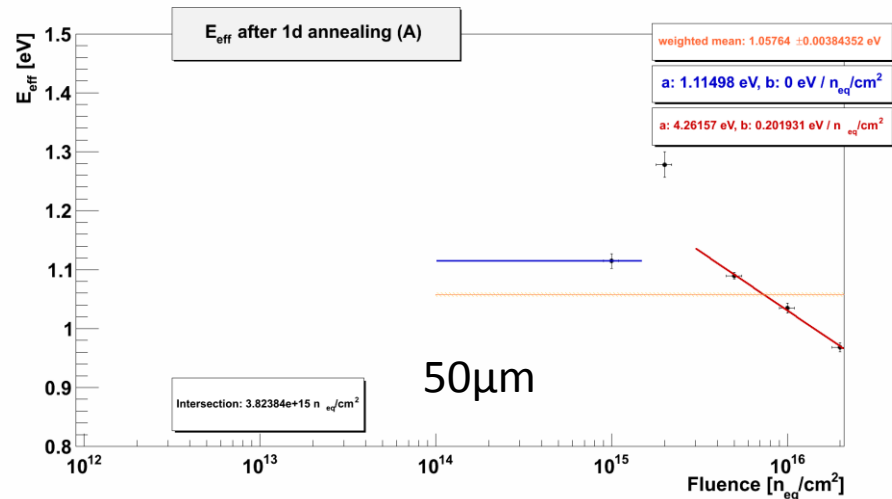
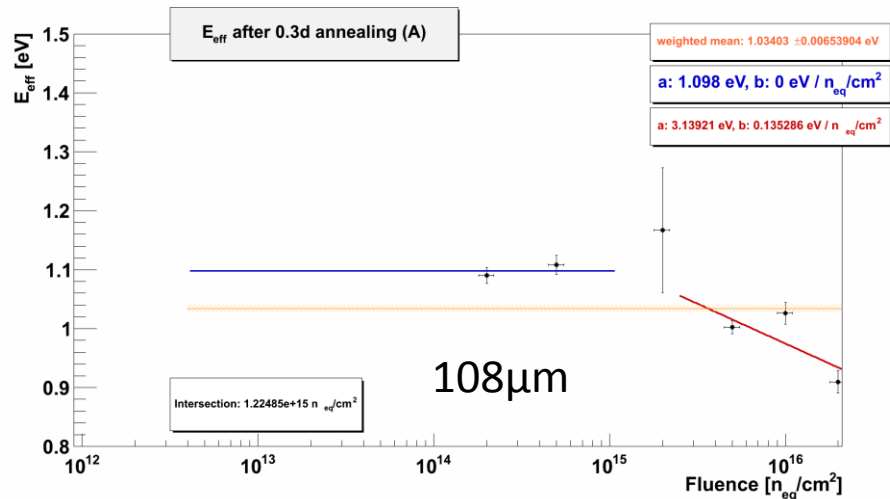
Temperature  
oscillations due  
to freezer  $\rightarrow$  can  
be seen as well  
in current

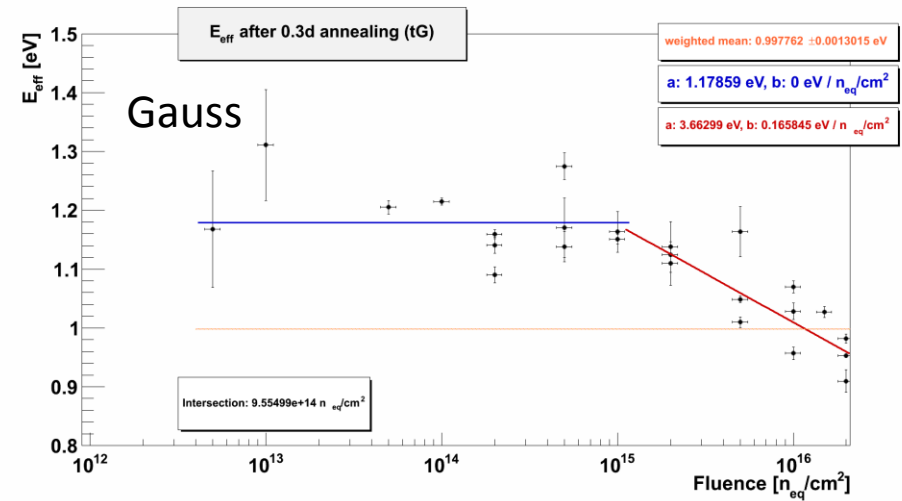
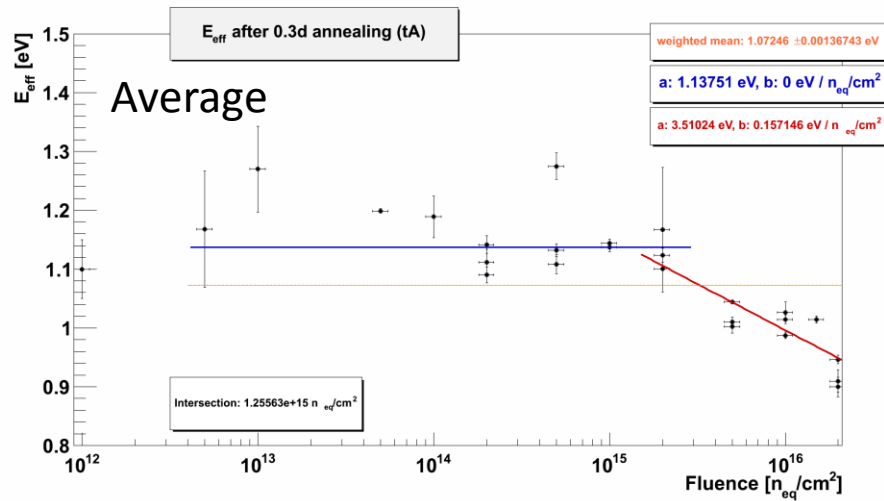
Temperature Difference (T1-T2)





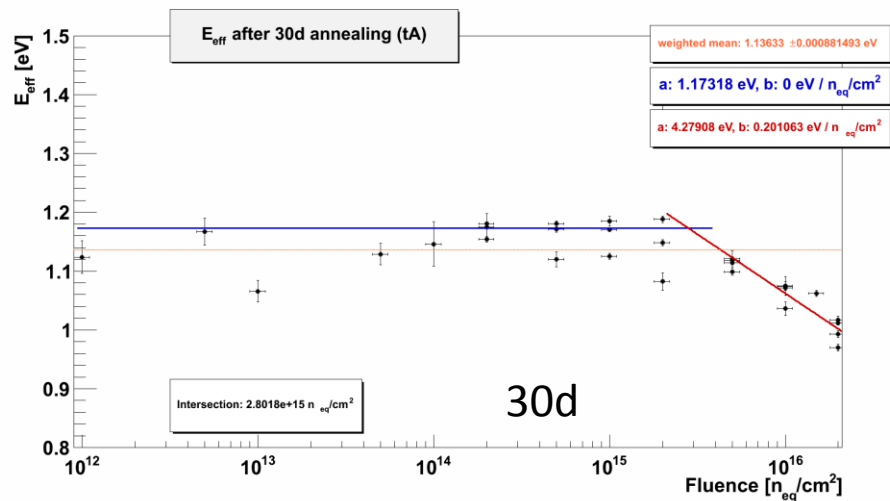
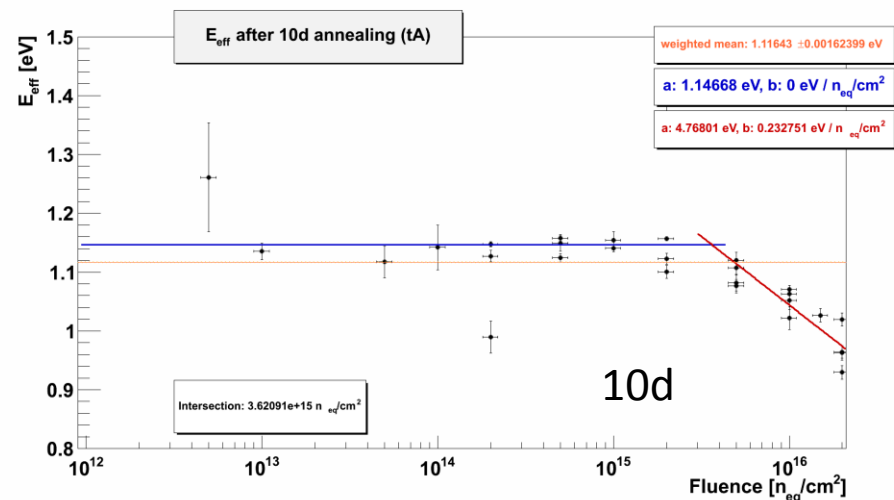
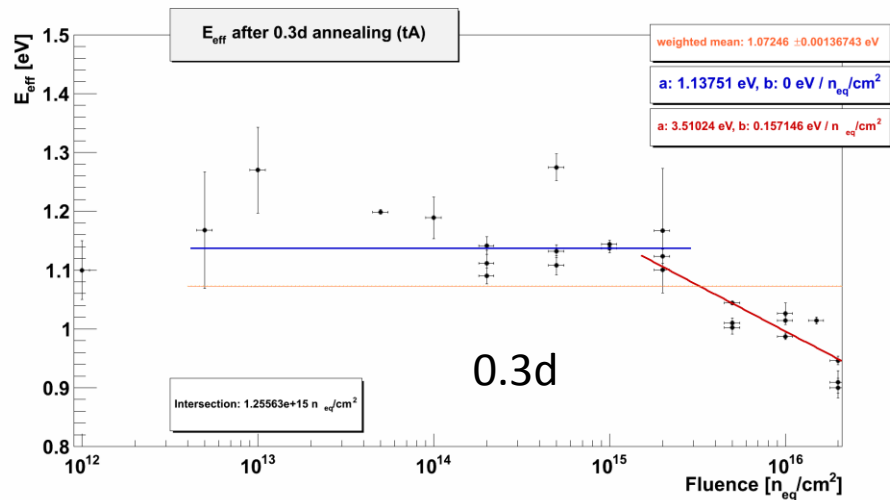
For high fluences ( $>1\text{E}15 / 2\text{E}15$   $n_{\text{eq}}/\text{cm}^2$ )  $E_{\text{eff}}$  decreases with increasing fluence





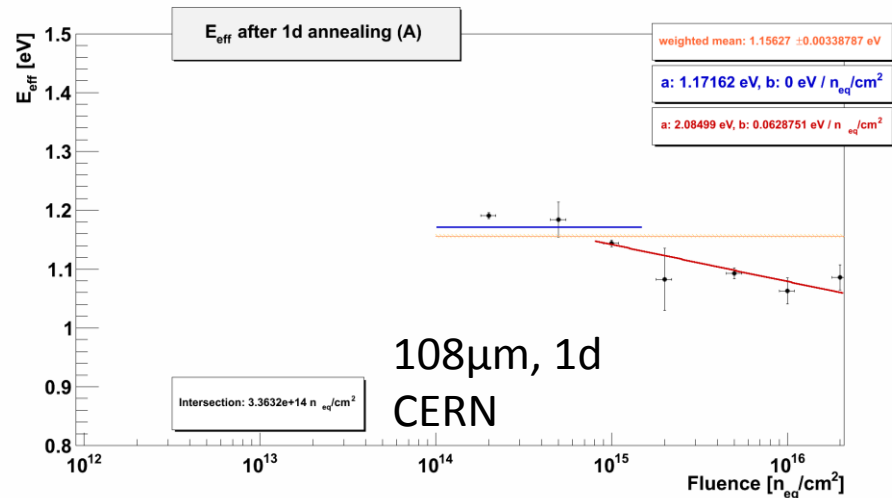
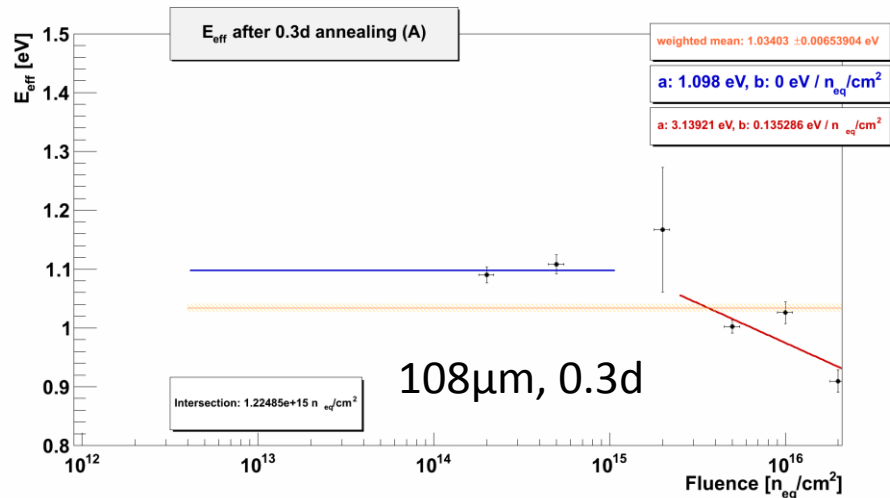
- Small difference between gauss and average  $E_{\text{eff}}$  determination
  - Fit of gauss distribution not always possible

		a	$\sigma_a$	b	$\sigma_b$
Low fluence	Average	1.138	0.002		
	Gauss	1.179	0.003		
High fluence	Average	3.51	0.16	0.16	0.01
	Gauss	3.7	0.2	0.166	0.013

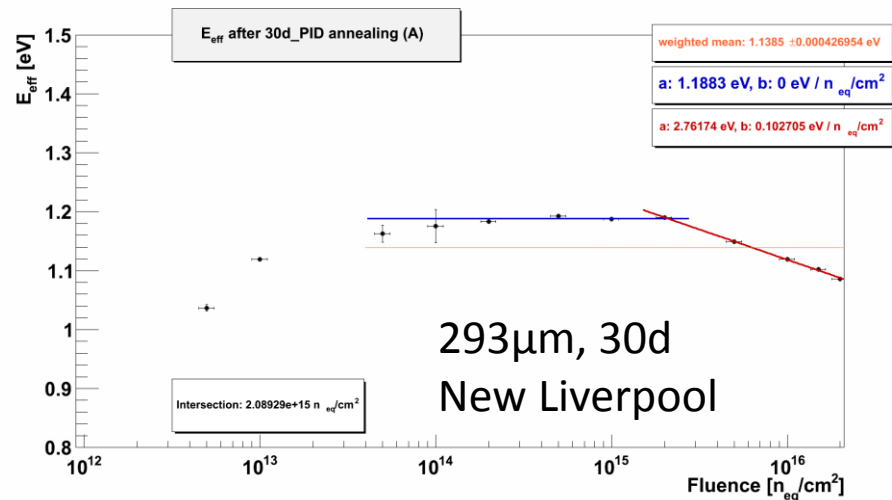
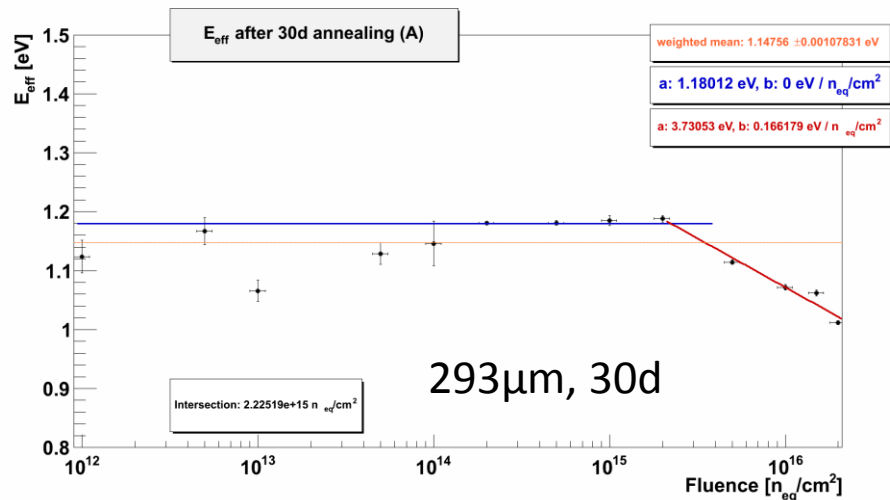


- Small increase of  $E_{\text{eff}}$  values with increasing room temperature annealing time





- Cold chuck method reduces  $E_{\text{eff}}$  decrease at high fluences a bit



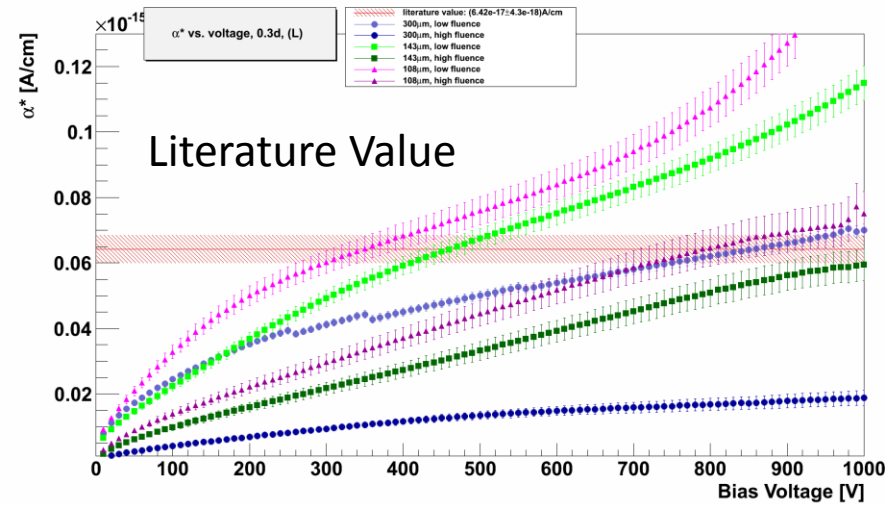


- Scale current to 21°C
  - Use different  $E_{\text{eff}}$  values
    - Literature value
    - For each sensor
      - Gauss value (from measurement of that sensor or from fit)
      - Average value (from measurement of that sensor or from fit)
      - Total Gauss / Average (fit using  $E_{\text{eff}}$  values from all sensors)
  - Fit straight line in  $\Delta I/V$  vs  $\Phi$  plot
    - low irradiation fluence ( $\leq 1E15 n_{\text{eq}}/\text{cm}^2$ )
    - high irradiation fluence ( $\geq 5E15 n_{\text{eq}}/\text{cm}^2$ )
- But: sensors not fully depleted (particularly at high fluences)
  - Geometric current related damage rate  $\alpha^*$ :
    - Instead of unknown depleted volume use the geometric volume
    - For fully depleted volume it is equal to the standard definition of  $\alpha$

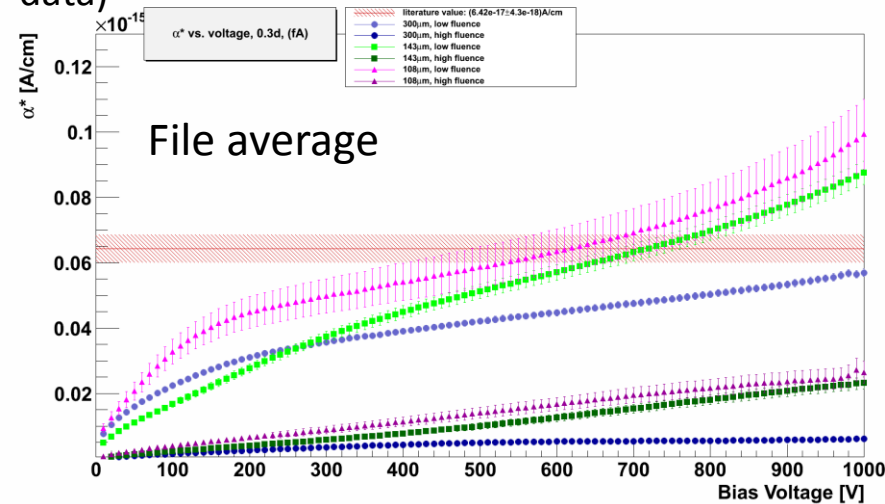


# Which $E_{eff}$ value to use

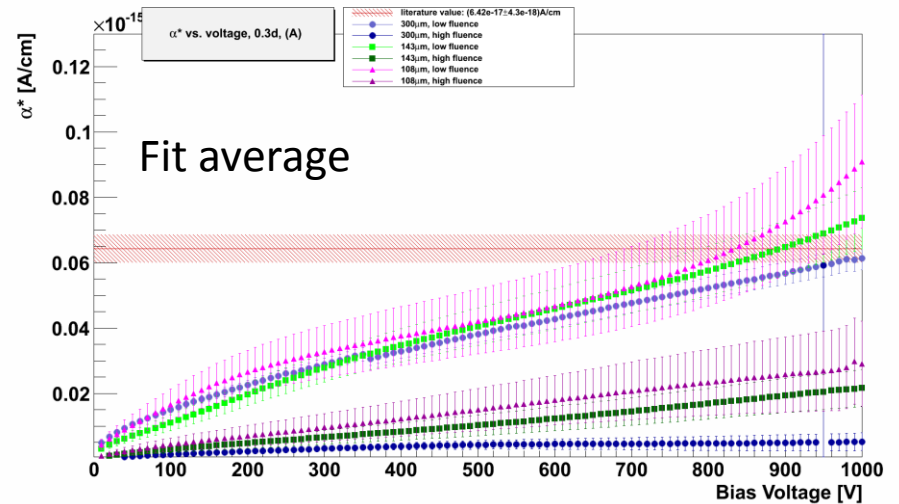
- Using literature value for scaling results in too high  $\alpha^*$  values
- Using the determined values improves this
  - Using the fit data of all sensors the error bars increase due to the high spread of the values



Using separate  $E_{eff}$  values for each sensor (from IV data)

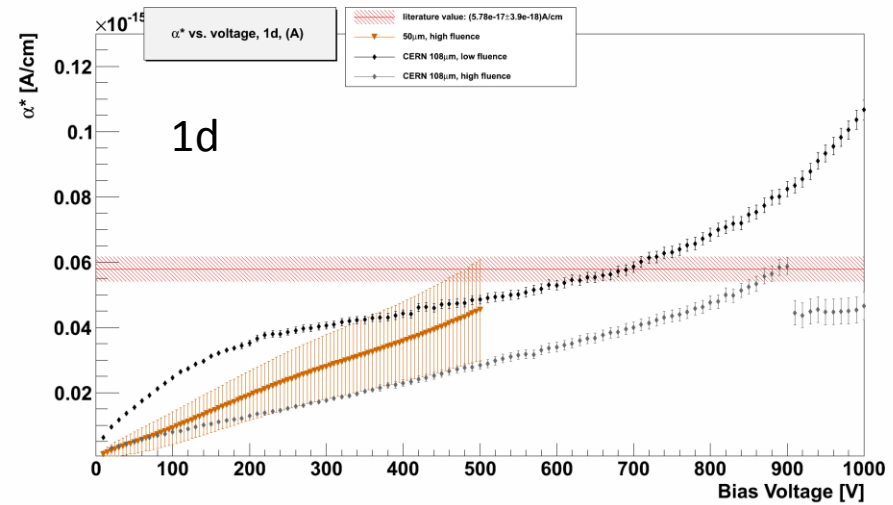
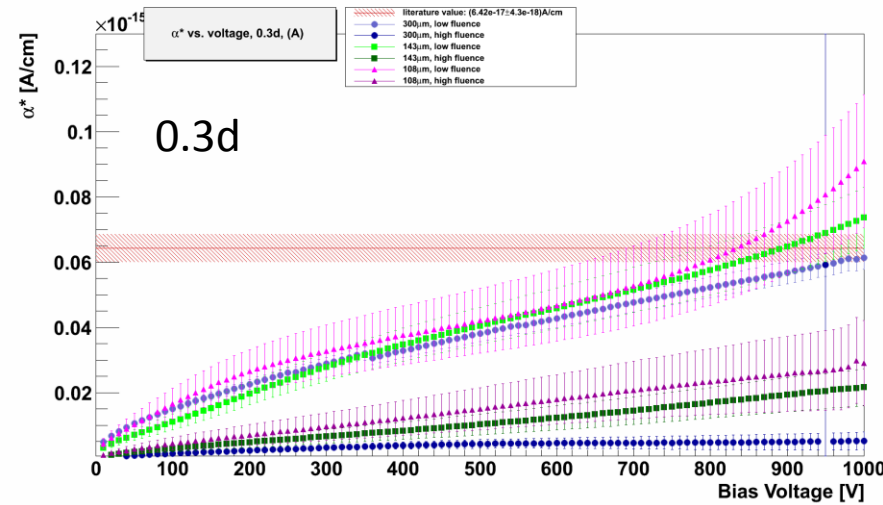


Using function from fit of all average  $E_{eff}$  values

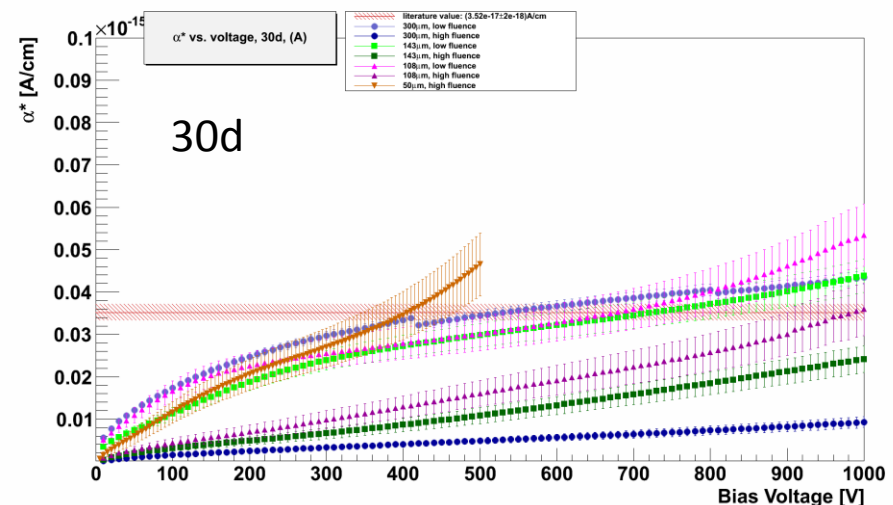
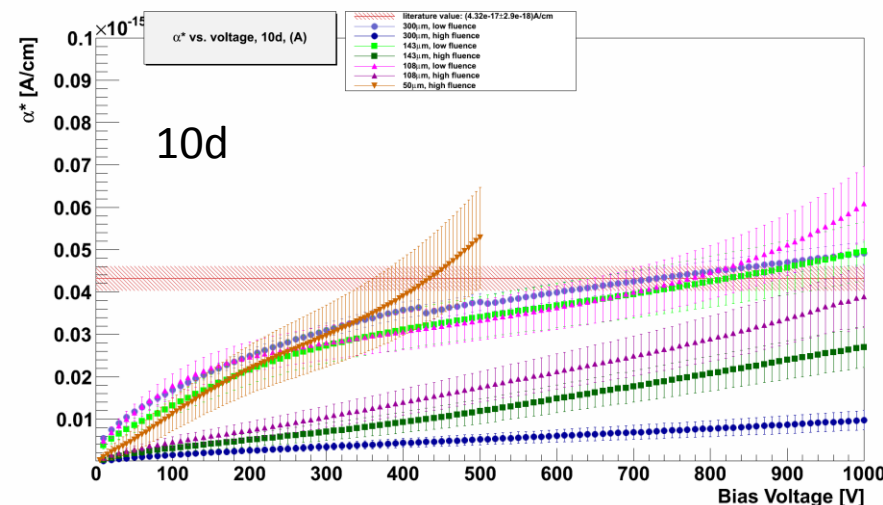


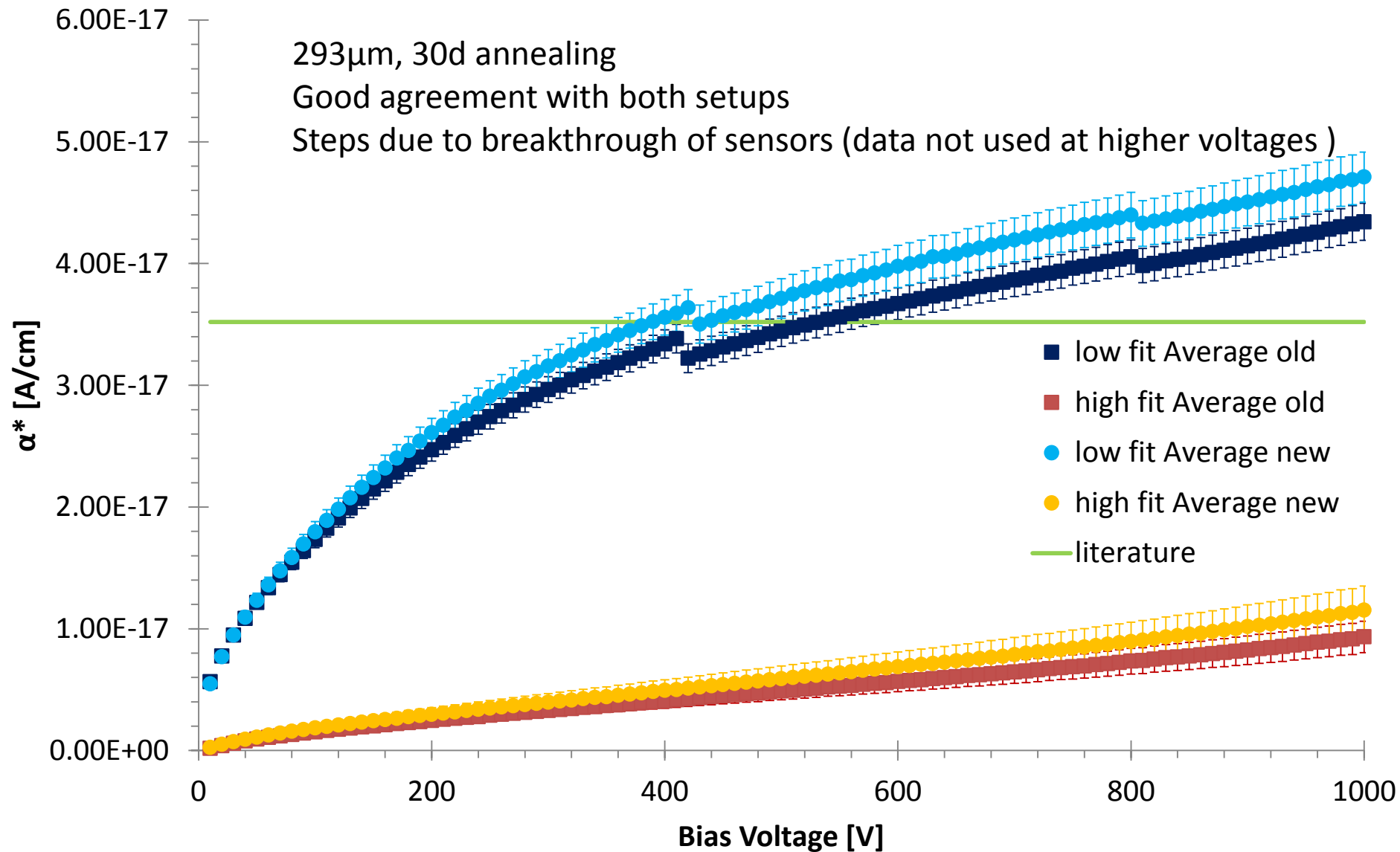


# $\alpha^*$ after annealing



Large error bars due to large uncertainties for  $E_{eff}$  value from fit (high fluence scaled by factor 0.2 for better overview)  
 With increasing annealing time the high fluence values increase further towards literature value







- Computing  $E_{\text{eff}}$  from IV measurements it can be seen that at fluences  $> 2E15n_{\text{eq}}/\text{cm}^2$  the value decrease with increasing fluence
  - Same behaviour after room temperature annealing up to 30d
- Measurements with a cold chuck
  - Fast reach of target temperature
  - Can actively counter self heating
- For  $\alpha^*$  determination the appropriate  $E_{\text{eff}}$  has to be used
  - For high fluences the literature value is not reached, but  $\alpha^*$  is still increasing with increasing voltage => sensor not fully depleted



# Backup



## Short term annealing

$$\alpha(t, T_a) = \alpha_{\infty} \sum_i \frac{b_i}{b_{\infty}} \exp\left(-\frac{t}{\tau_i(T_a)}\right)$$

$t$ : annealing time;  $T_a$ : annealing temperature

← [2,3]  
↓

	$i = 1$	$i = 2$	$i = 3$	$i = 4$	$i = 5$	$i = \infty$
$\tau_i$ [min]	$(1.78 \pm 0.10) \times 10^1$	$(1.19 \pm 0.03) \times 10^2$	$(1.09 \pm 0.01) \times 10^3$	$(1.48 \pm 0.01) \times 10^4$	$(8.92 \pm 0.59) \times 10^4$	$\infty$
$b_i$	$0.156 \pm 0.038$	$0.116 \pm 0.003$	$0.131 \pm 0.002$	$0.201 \pm 0.002$	$0.093 \pm 0.007$	$0.303 \pm 0.006$

$$\alpha_{\infty} = (2.86 \pm 0.18) \times 10^{-17} \text{ A/cm} \quad [4]$$

[2]: M. Moll; *Radiation Damage in Silicon Particle Detectors*; **PHD Thesis**

[3]: R. Wunstorf; *Systematische Untersuchung zur Strahlenresistenz von Silizium-Detektoren für die Verwendung in Hochenergiephysik-Experimenten*; **PHD Thesis**

[4]: A. Chilingarov; *Radiation studies and operational projections for silicon in the ATLAS inner detector*; **NIM A 360 (1995) 432-437**





## Long term annealing

$$\alpha(t) = \alpha_I \exp\left(-\frac{t}{\tau_I}\right) + \alpha_0 - \beta \ln\left(\frac{t}{t_0}\right)$$

$t$ : annealing time

Parameter for annealing at 21°C from fit

$$\alpha_I = 1.23 \times 10^{-17} \text{ A/cm}, \quad \alpha_0 = 7.07 \times 10^{-17} \text{ A/cm}$$

$$\tau_I = 1.4 \times 10^4 \text{ min}, \quad t_0 = 1 \text{ min}$$

$$\beta = 3.29 \times 10^{-18} \text{ A/cm}$$

$\alpha_I$  and  $\beta$  vary slightly with annealing temperature, average values:

$$\langle \alpha_I \rangle = (1.23 \pm 0.06) \times 10^{-17} \text{ A/cm}, \quad \langle \beta \rangle = (3.07 \pm 0.18) \times 10^{-18} \text{ A/cm}$$

$\alpha_0$  depend on annealing temperature => value from parameterization:

$$\alpha_0 = (6.74 \pm 0.06) \times 10^{-17} \text{ A/cm}$$

[2]: M. Moll; *Radiation Damage in Silicon Particle Detectors*; **PHD Thesis**



- Using equations to calculate theoretical alpha values
- Annealing temperature of 20°C (room temperature)
- Sample preparation: ~470min (0.3d) for all sensors
- Room temperature annealing of sensors in Nitrogen box

Annealing time	Short term annealing	Long term annealing	Long term annealing (average)
t [min]	$\alpha$ [ $10^{-17}$ A/cm]		
0.3d (=470 min)	<b>6.40±0.43</b>	6.24	6.04±0.14
10d (=14400min)	<b>4.32±0.29</b>	4.36	4.24±0.18
30d (=43220min)	<b>3.50±0.23</b>	3.61	3.52±0.20



**bold:** “theoretical value” for comparison



$$\sigma_{I(T_2)}^2 = I(T_2)^2 \left[ \left( \frac{\sigma_{I(T_1)}}{I(T_1)} \right)^2 + \left( 2 + \frac{E_{eff}}{2k_B T_1} \right)^2 \left( \frac{\sigma_{T_1}}{T_1} \right)^2 + \left( 2 + \frac{E_{eff}}{2k_B T_2} \right)^2 \left( \frac{\sigma_{T_2}}{T_2} \right)^2 + \left( \frac{1}{2k_B} \left( \frac{1}{T_2} - \frac{1}{T_1} \right) \right)^2 \sigma_{E_{eff}}^2 \right]$$

- Major source for uncertainty:  $E_{eff}$  fit for high fluences
  - $\frac{\sigma_{E_{eff}}}{E_{eff}}$  is up to 10% for high fluences, which results in large uncertainties of the scaled current and therefore large uncertainties of the straight line fit
  - Had to scale  $\sigma_{E_{eff}}$  down by factor 0.2 to get a reasonable size of the error bars in the graph



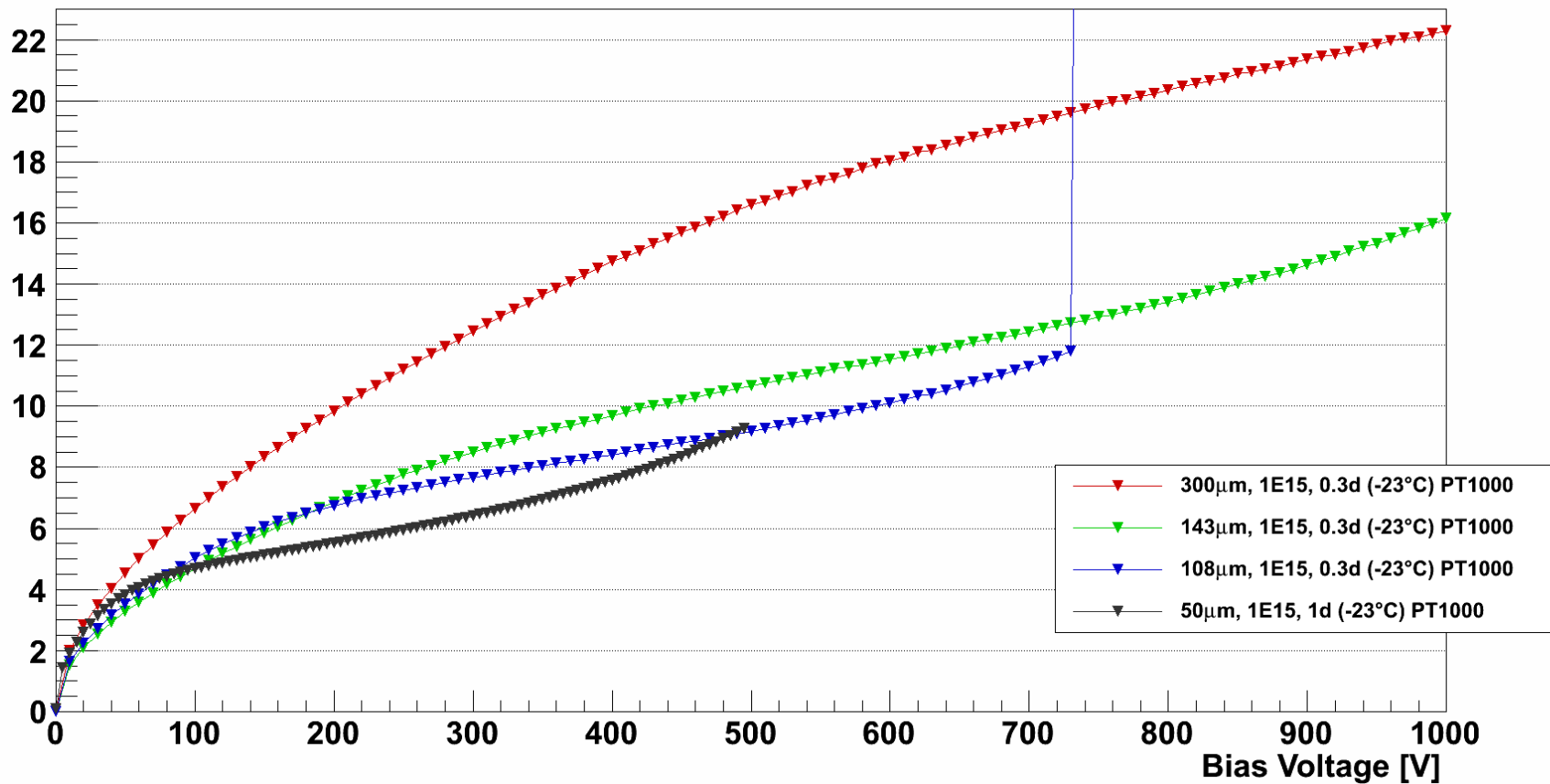
# Leakage Current at different fluences

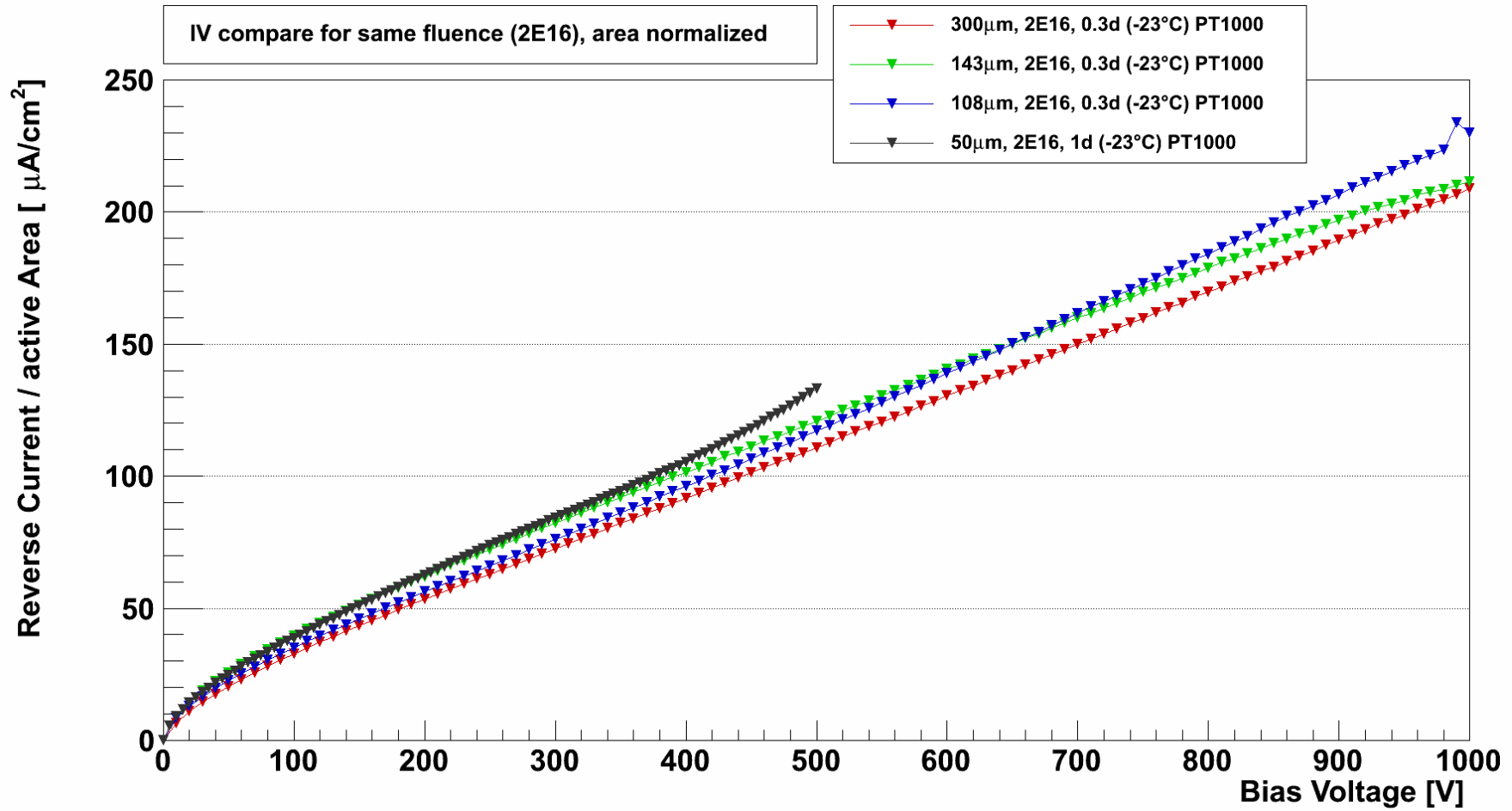
**FOR SENSORS WITH DIFFERENT THICKNESS**

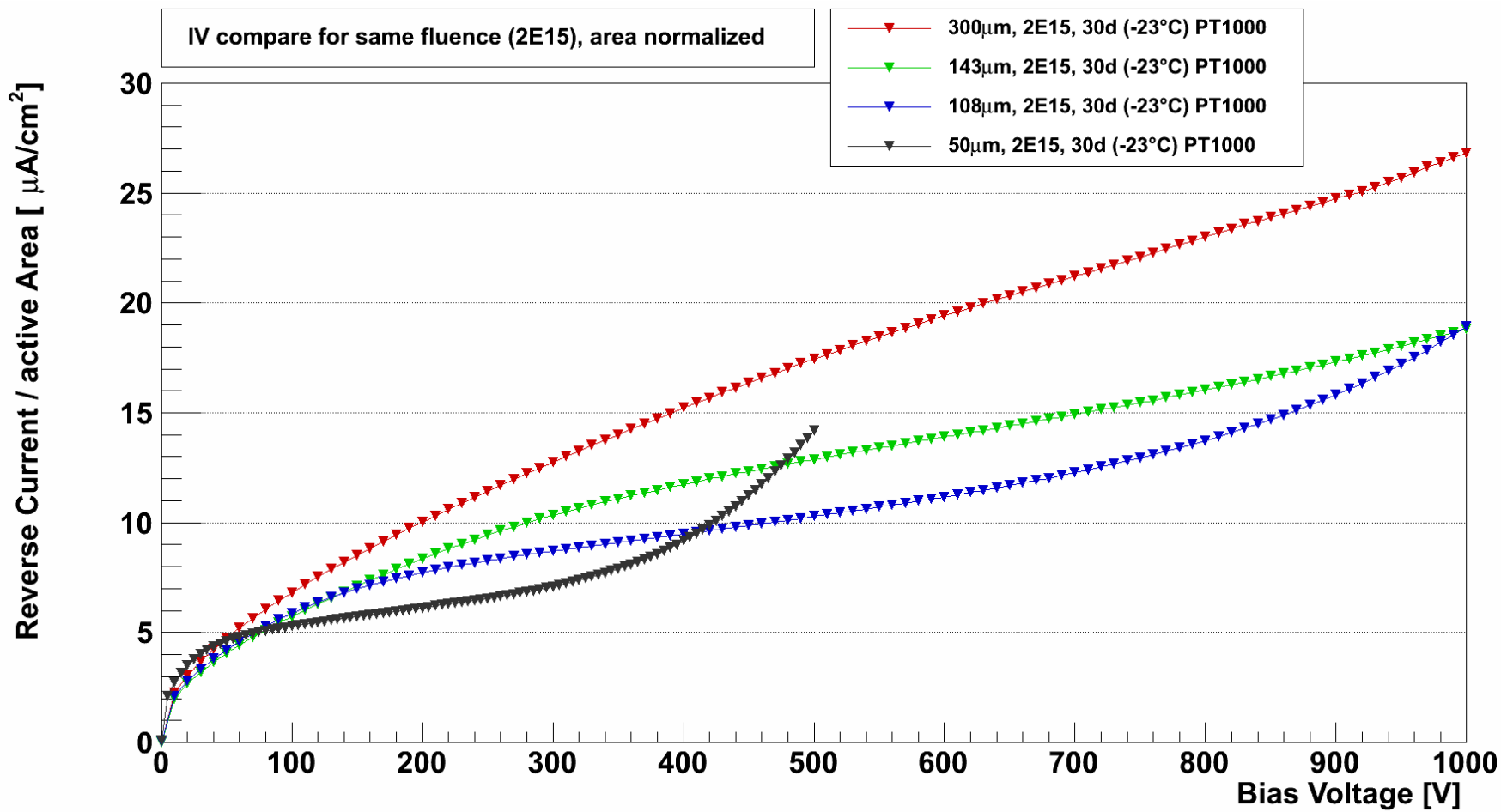


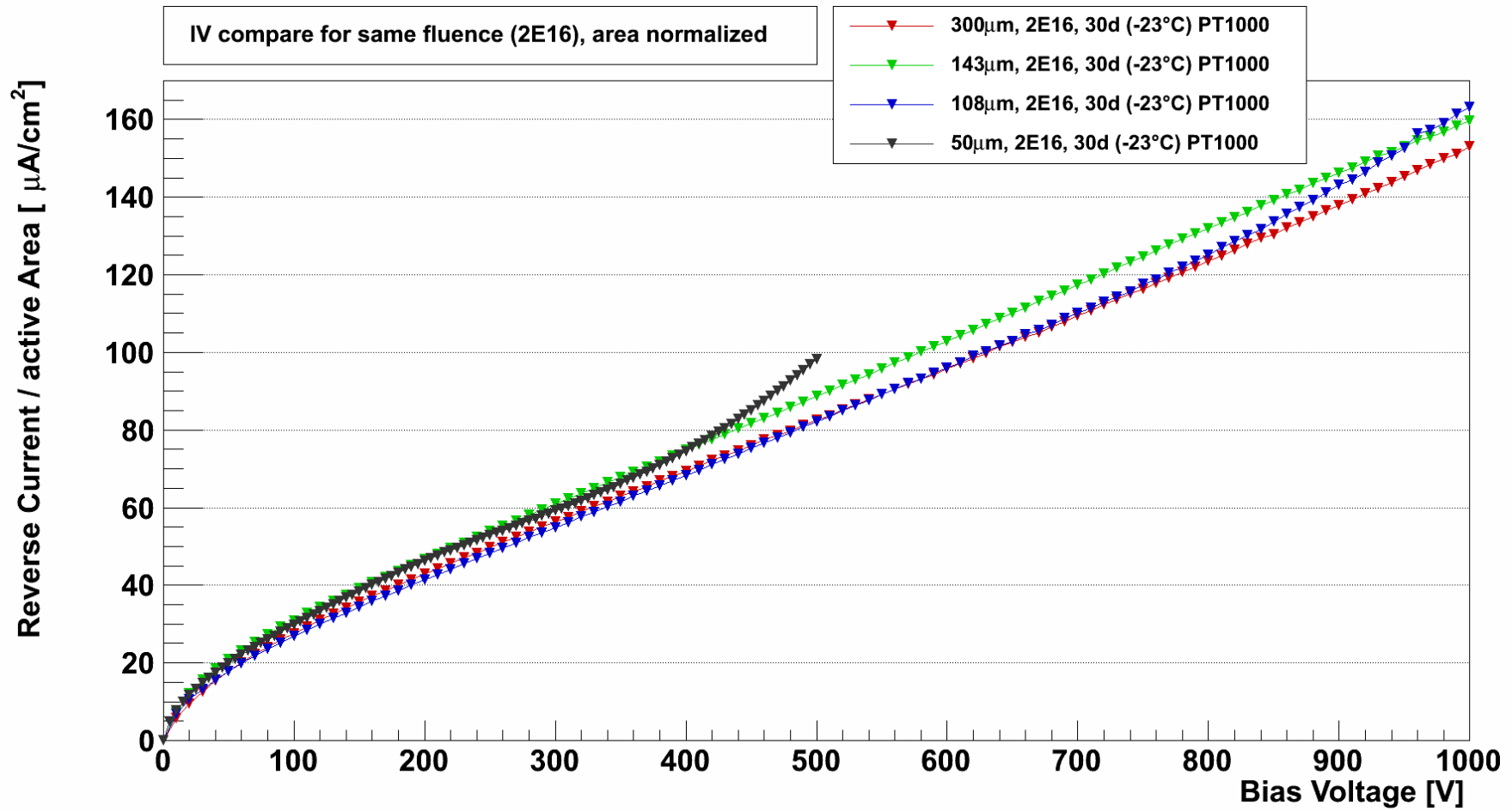
IV compare for same fluence ( $1E15$ ), area normalized

Reverse Current / active Area [ $\mu A/cm^2$ ]











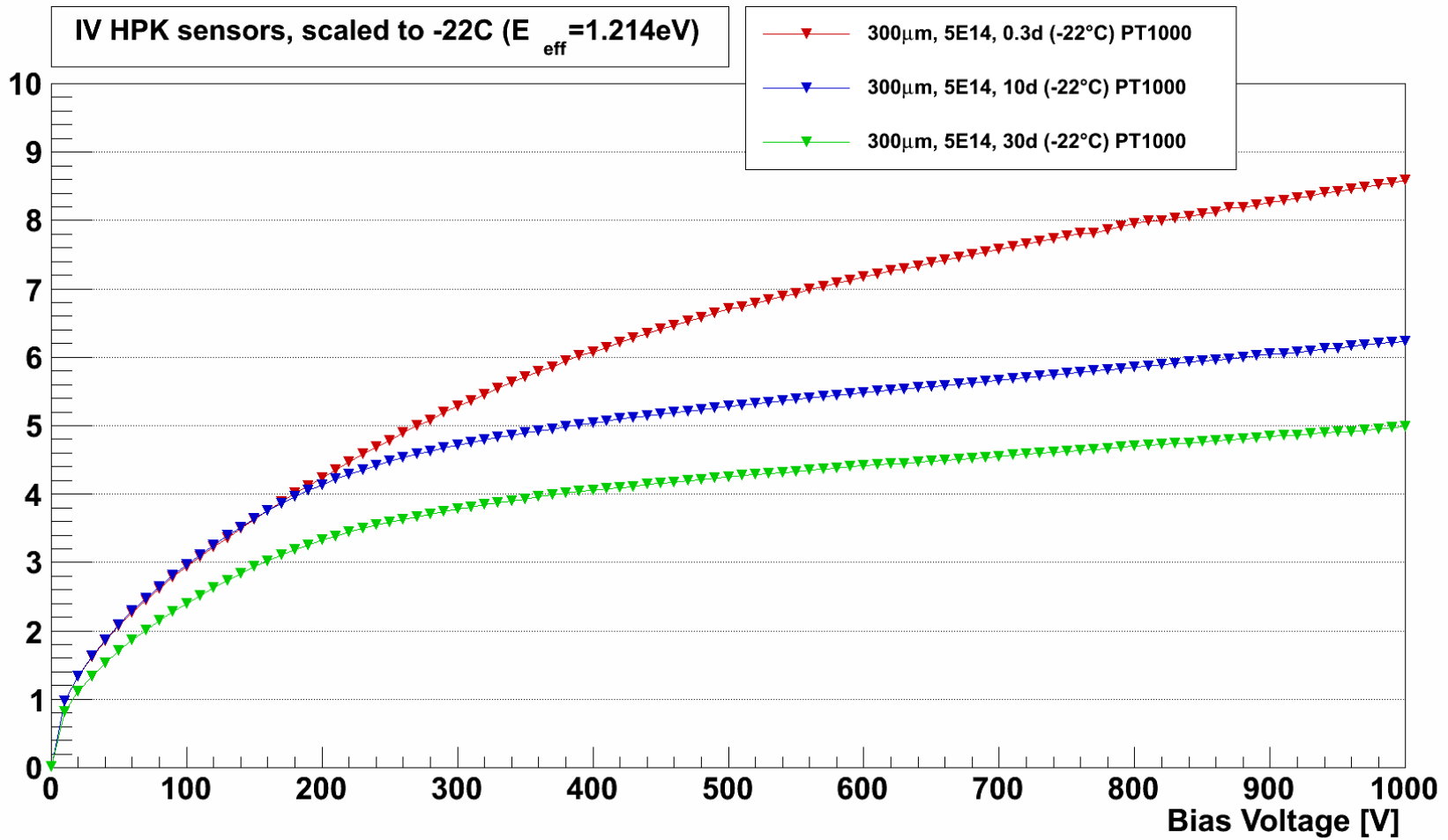


# Leakage Current at different annealing steps

**FOR SAME SENSOR**

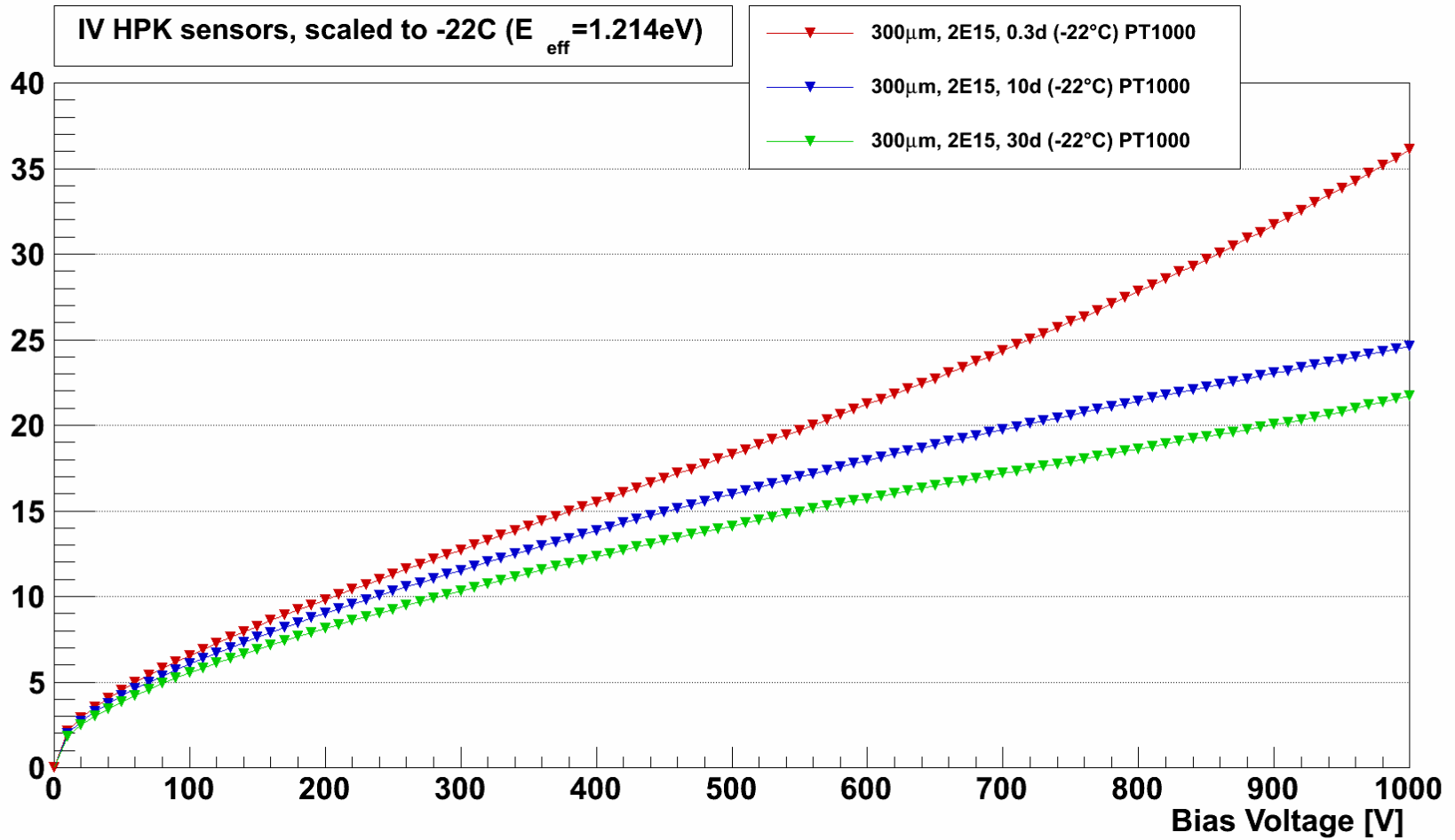


Reverse Current [ $\mu A$ ]





Reverse Current [ $\mu A$ ]

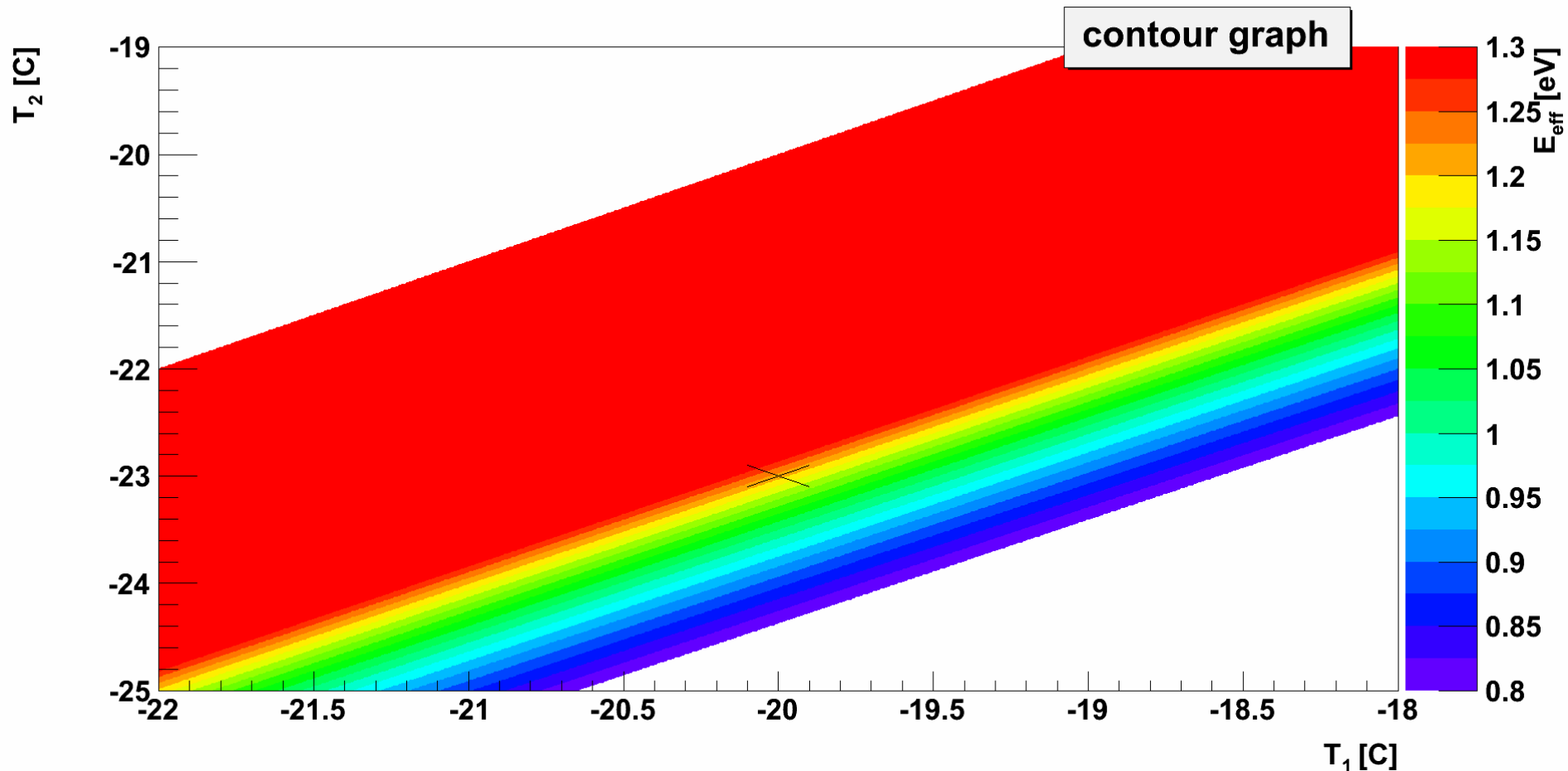




# Simulations and Error reflection



- In formula two possible causes of variation in  $E_{\text{eff}}$ :
  - Wrong temperature measurement (not only temperature of sensor, also temperature of freezer => temperature measured too cold)
  - Wrong current measurement
- Simulation of influence from both effects on  $E_{\text{eff}}$  with:
  - Current measurement correct, only temperature variation
  - Temperature measurement correct, only current variation
- Chosen parameters:
  - $T_1 = -20.0^\circ\text{C}$ ,  $T_2 = -23.0^\circ\text{C}$
  - $I_1 = 20.0\mu\text{A}$ ,  $I_2 = 13.99\mu\text{A}$ 
    - Value of  $I_2$  calculated from other parameters with  $E_{\text{eff}} = 1.214\text{eV}$



Temperature measurement on the sensor could be affected by environment. The environment can be warmer than the sensor due to PID cooling, or the sensor can be warmer than the environment due to self heating. Either way the measured temperature is not the actual silicon temperature.