

# Measurements of the effective bandgap and current related damage rate of highly irradiated silicon sensors

**Moritz Wiehe**<sup>a</sup>

**Tony Affolder**<sup>b</sup>

**Gianluigi Casse**<sup>b</sup>

**Paul Dervan**<sup>b</sup>

**Susanne Kühn**<sup>a</sup>

**Riccardo Mori**<sup>a</sup>

**Ulrich Parzefall**<sup>a</sup>

**Sven Wonsak**<sup>b</sup>

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Albert-Ludwigs-Universität Freiburg

a) Albert-Ludwigs-Universität Freiburg

b) University of Liverpool



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# Outline



- Introduction: Leakage Current
- Setup
- Results for effective bandgap  $E_{g,eff}$
- Results for current related damage rate  $\alpha^*$
- Conclusion

# Introduction: Leakage Current

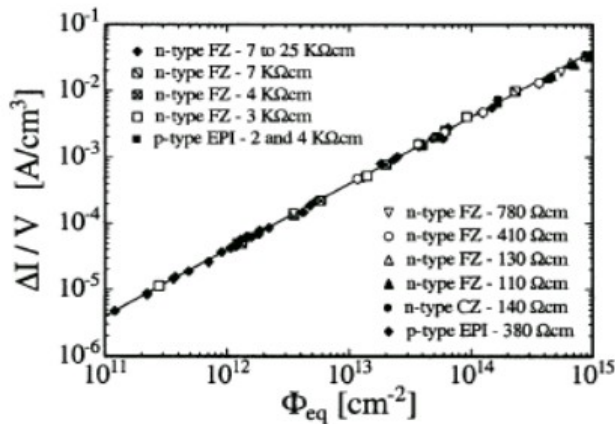


Leakage current after irradiation is proportional to irradiation fluence by **Current-Related-Damage-Rate  $\alpha$** :

$$I(\Phi_{eq}) - I_0 = \Delta I = \alpha \Phi_{eq} V$$

Calculation of temperature dependence with **scaling parameter  $E_{g,eff}$**  :

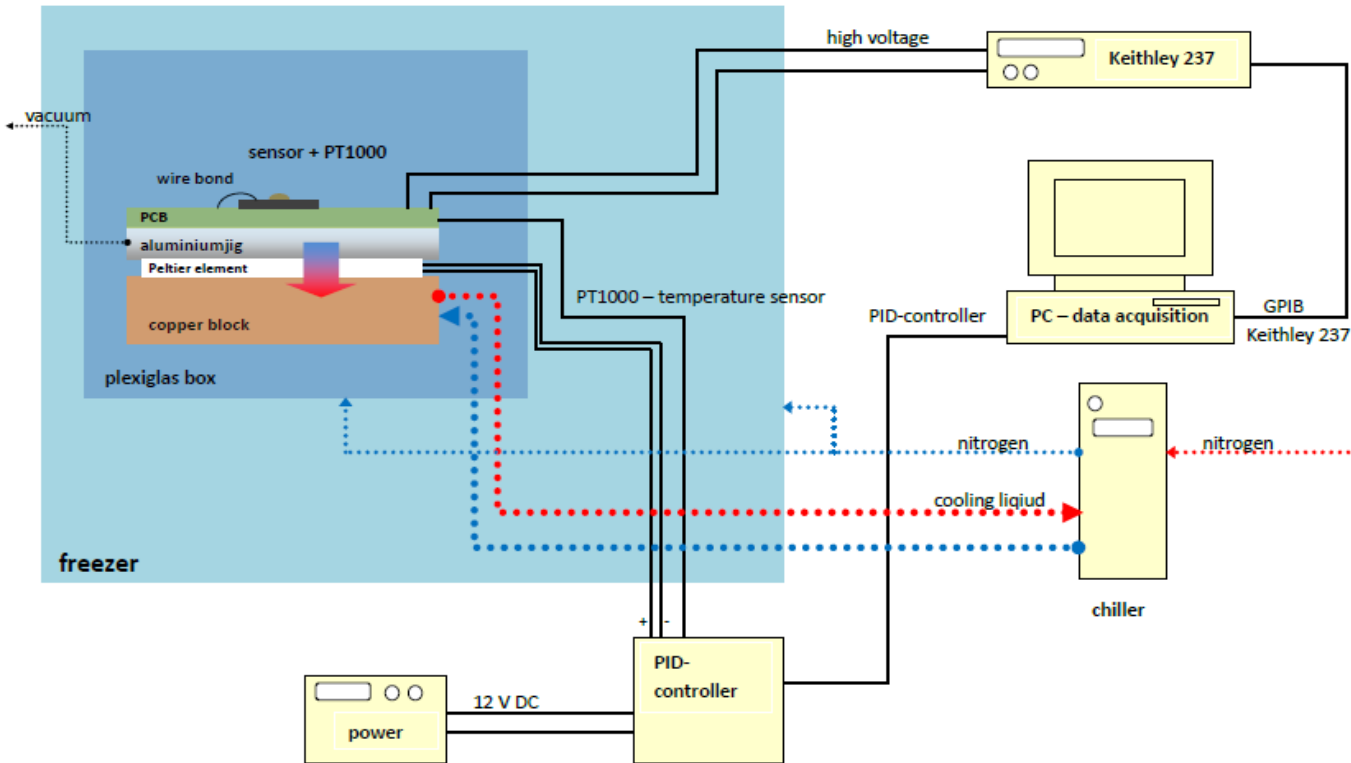
$$I(T_2) = I(T_1) \cdot \left(\frac{T_2}{T_1}\right)^2 e^{-\frac{E_{g,eff}}{2k_B} \left(\frac{1}{T_2} - \frac{1}{T_1}\right)}$$



IV-measurements were performed at low temperatures (-23°C, -27°C, -32°C) for different sensors to estimate  $E_{g,eff}$  and  $\alpha^*$ .

Depleted volume is unknown  
 → physical volume is used for calculation  
 (see also: Sven Wonsak et al. Measurements of the reverse current of highly irradiated silicon sensors)

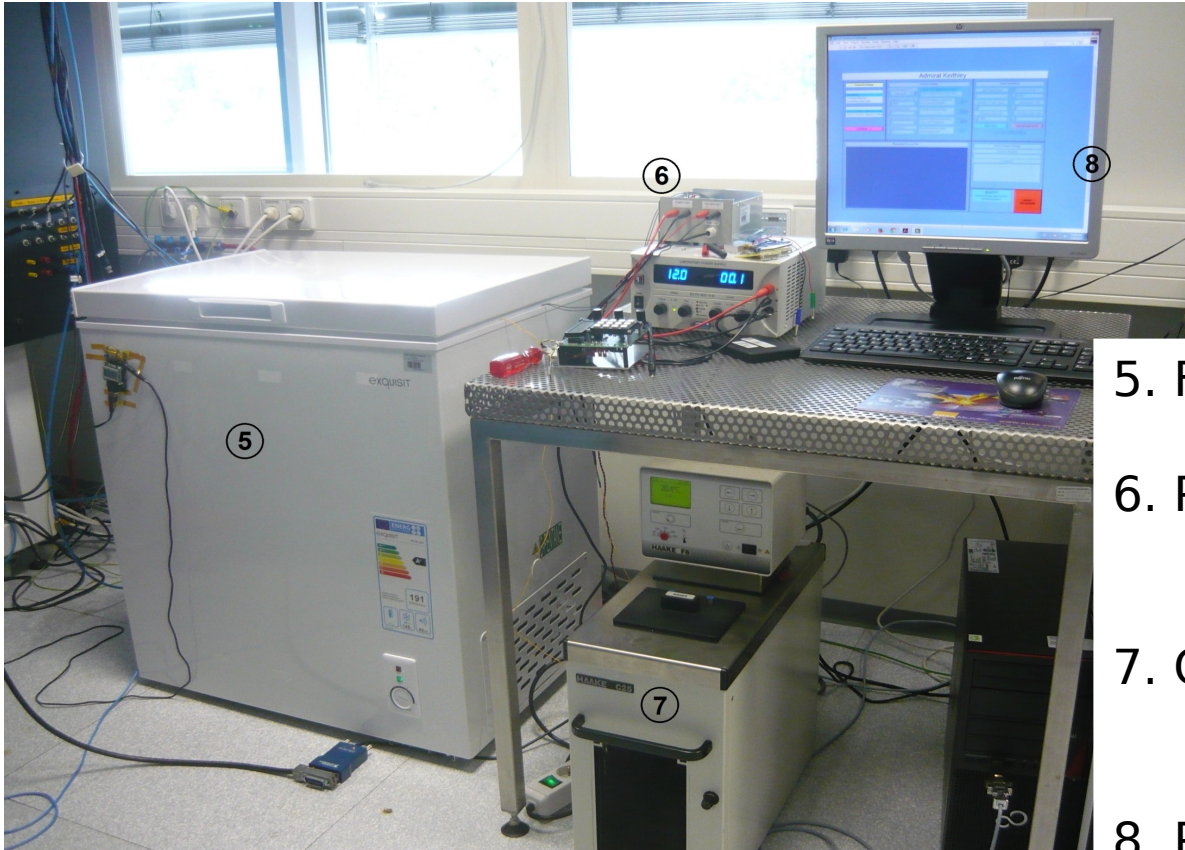
# IV-Setup



Improved features of new setup:

- Easy handling, due to PCBs
- Temperature measured by PT1000 directly on top of sensor
- No ingress of moisture
- Stable surrounding temperature (freezer)
- Temperature controlled by PID-Controller

# IV-Setup



5. Freezer

6. PR-59-temperature controller

7. Chiller with colling liquid

8. PC for data acquisition

# IV-Setup



1. „Printed Circuit board“ with sensor glued on top
2. Aluminiumjig for mounting PCB
3. Cooling unit (Peltier element, copper block)
4. Plexiglas cover

Nr.	Sensor	d [ $\mu\text{m}$ ]	$\Phi_{eq}$ [ $n_{eq}/\text{cm}^2$ ]
1	HPK W277-BZ5-P23	293	$2 \cdot 10^{14}$
2	Micron 2437-14-M	143	$2 \cdot 10^{14}$
3	Micron 2437-14-O	143	$5 \cdot 10^{14}$
4	Micron 2437-14-Q	143	$1 \cdot 10^{15}$
5	HPK W264-BZ5-P23	293	$2 \cdot 10^{15}$
6	Micron 2437-14-S	143	$2 \cdot 10^{15}$
7	HPK W72-BZ3-P18	293	$5 \cdot 10^{15}$
8	Micron 2437-14-F	143	$5 \cdot 10^{15}$
9	HPK W73-BZ2-P20	293	$1 \cdot 10^{16}$
10	Micron 2437-14-G	143	$1 \cdot 10^{16}$
11	HPK W104-BZ2-P2	293	$1,5 \cdot 10^{16}$
12	HPK W104-BZ2-P17	293	$2 \cdot 10^{16}$
13	Micron 2437-14-H	143	$2 \cdot 10^{16}$
14	Micron 3107-6-3	50	$1 \cdot 10^{15}$
15	Micron 3107-6-9	50	$2 \cdot 10^{15}$
16	Micron 3107-6-10	50	$5 \cdot 10^{15}$
17	Micron 3107-6-14	50	$1 \cdot 10^{16}$
18	Micron 3107-6-21	50	$2 \cdot 10^{16}$

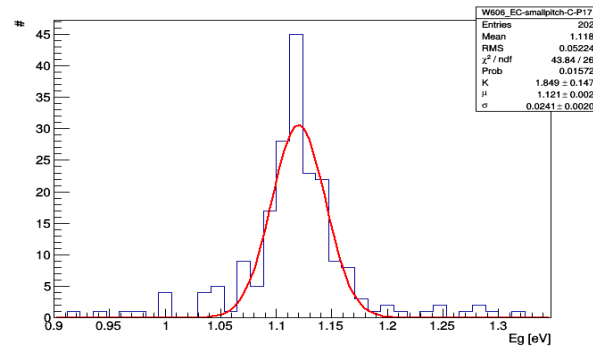
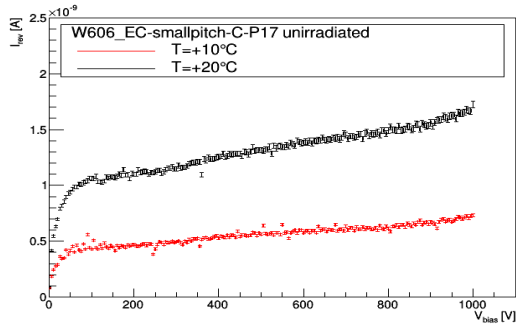
active area of sensors:

Hamamatsu (HPK): (0,8348 × 0,86)cm<sup>2</sup>

Micron: (1,0985 × 1,0973)cm<sup>2</sup>

(only n-in-p-sensors used)

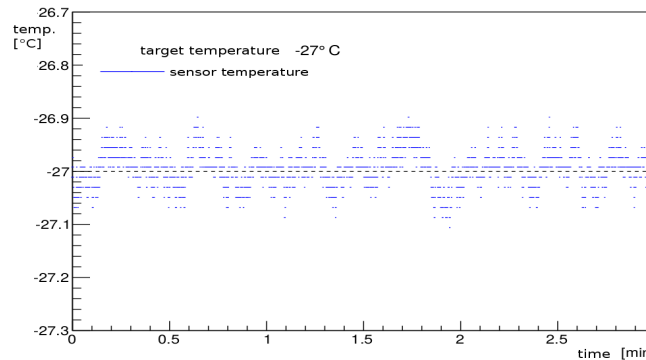
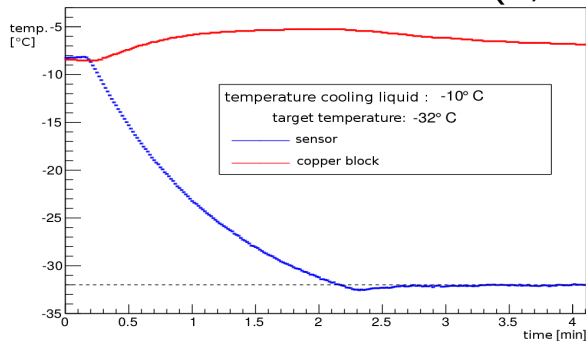
# Performance of setup



Measurement of unirradiated sensor results in expected value of  $E_{g,\text{eff}} = 1.12$  eV

Ten IV-measurements of irradiated sensor at  $T = -23^\circ\text{C}$  :

→ mean standard deviation  $(0, 926 \pm 0, 0018)$  % for every current measurement



Measured sensor temperature does not deviate by more than  $0.15^\circ\text{C}$  from target temperature. (optimized PID parameters, unbiased sensor)

# $E_{g,eff}$ - methods



Scaling method:

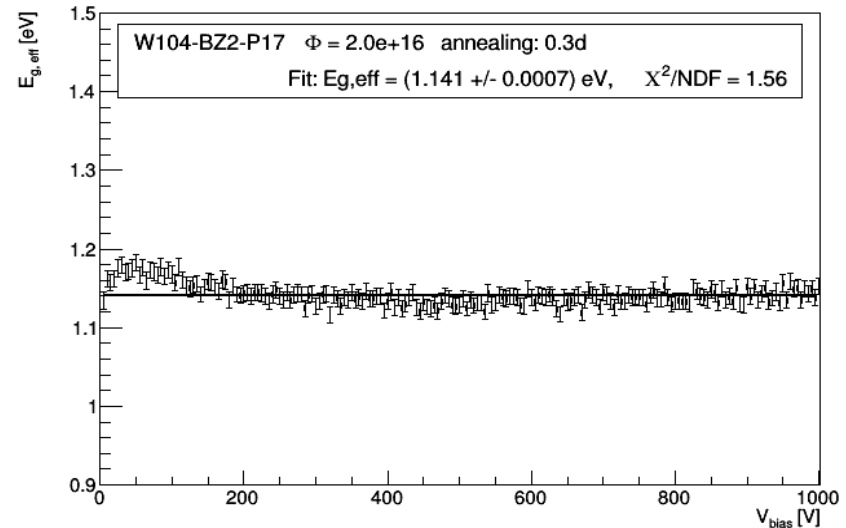
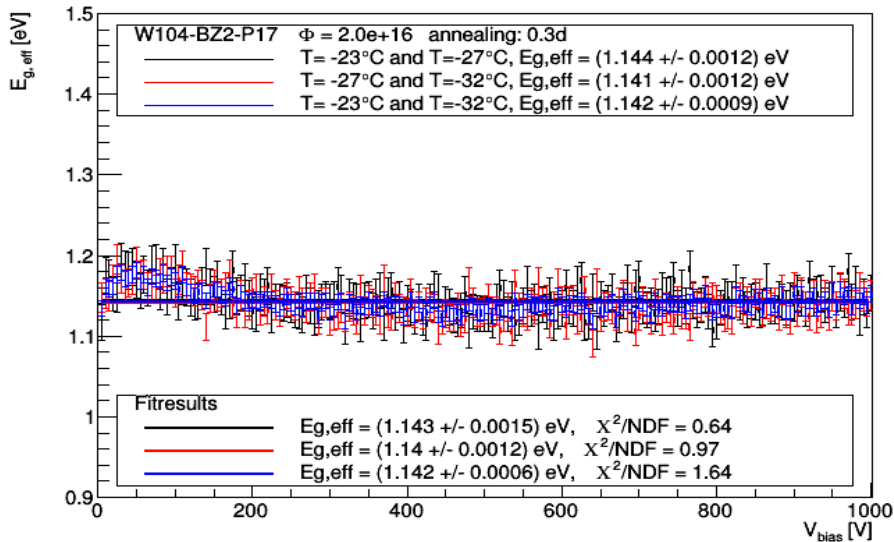
Calculate  $E_{g,eff}$  for every set of two temperatures

Fit method:

Perform fit of set of measurements

$$E_{g,eff} = -2k_B \frac{T_1 T_2}{T_1 - T_2} \cdot \ln \left[ \frac{I_2 T_1^2}{I_1 T_2^2} \right]$$

$$I(T) = A \cdot T^2 e^{-\frac{E_{g,eff}}{2k_B T}}$$

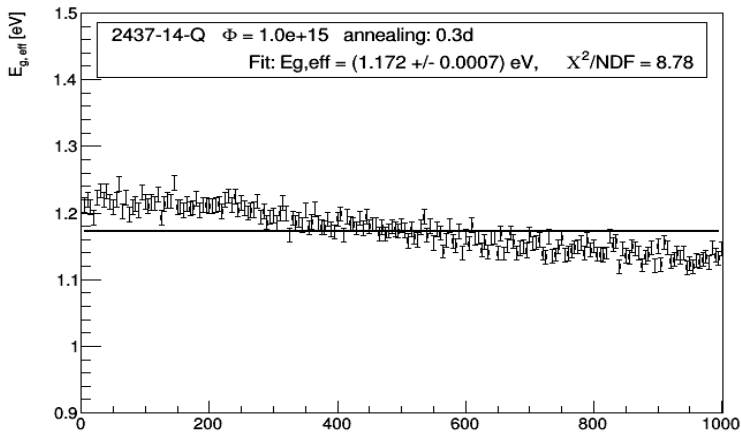


uncertainty on each value: measurement uncertainty + correlation.  
but dominant uncertainty: systematic variation of calculated values with voltage. (up to 0, 1 eV for some sensors)

HPK 293 um

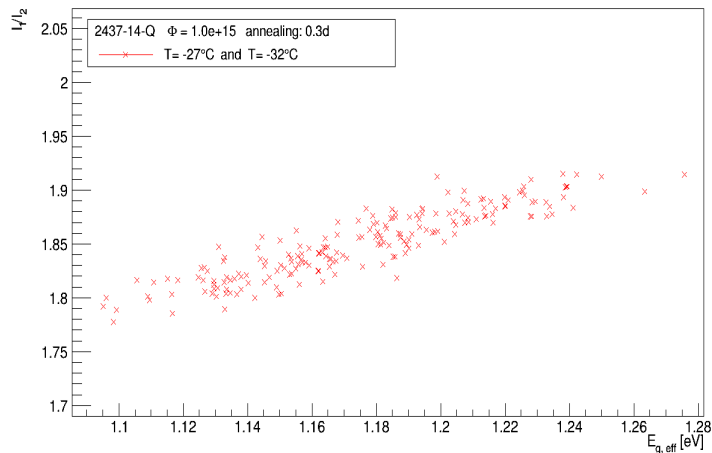


# Caveat: $E_{g,eff}$ dependence on voltage



$$\frac{I(T_2)}{I(T_1)} = \left(\frac{T_2}{T_1}\right)^2 e^{-\frac{E_{g,eff}}{2k_B} \left(\frac{1}{T_2} - \frac{1}{T_1}\right)}$$

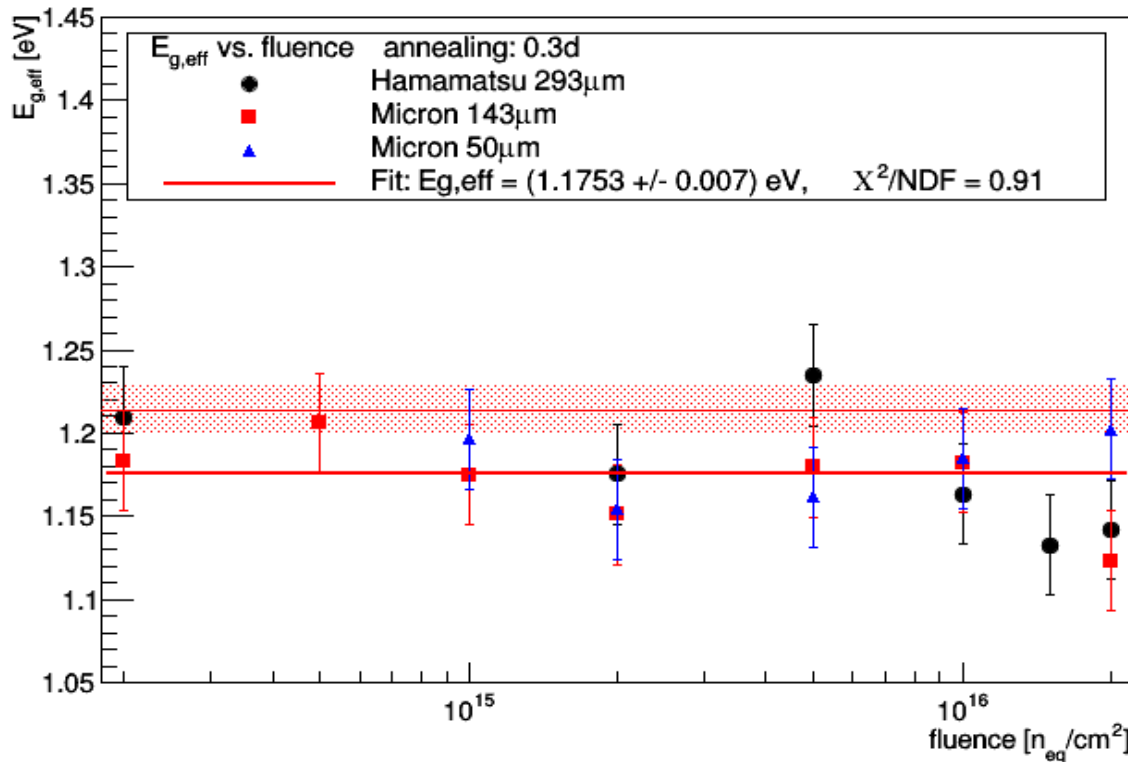
self heating of sensor might lead to incorrect temperature measurement  
 → effect more pronounced at high voltages and higher fluences



to account for unexpected voltage dependence a systematic uncertainty on the temperature measurement is assumed:

$$s_{T,sys} = 0,15 \text{ } ^\circ\text{C} \Rightarrow s_{E_{g,eff},sys} = 0,03 \text{ eV}$$

# $E_{g,eff}$ vs. fluence



Additional measurement  
at  $-43^\circ\text{C}$  and  $-39^\circ\text{C}$  of  
293 $\mu$ m HPK-sensor,  $2 \times 10^{16} \text{ neq}/\text{cm}^2$ :  
→  $E_{g,eff} = 1.116 \text{ eV} (-0.026 \text{ eV})$

## result

$E_{g,eff} = (1,18 \pm 0,03) \text{ eV}$       (Lit.  $E_{g,eff} = (1,214 \pm 0,014) \text{ eV}$  [1])

[1] A Chilingarov. *Temperature dependence of the current generated in Si-bulk*

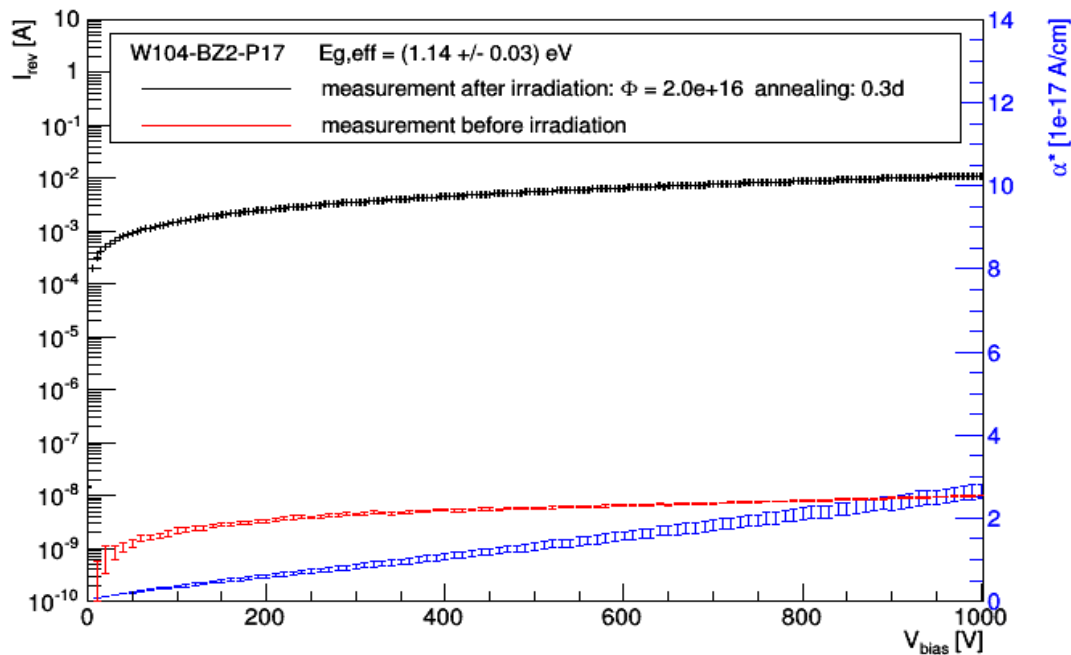


# $\alpha^*$ vs. voltage

$I(\Phi_{eq})$ : leakage current  $T = -32^\circ C$ , scaled to  $21^\circ C$   
 $I_0$ : measurement before irradiation,  $V$ : actual detector volume

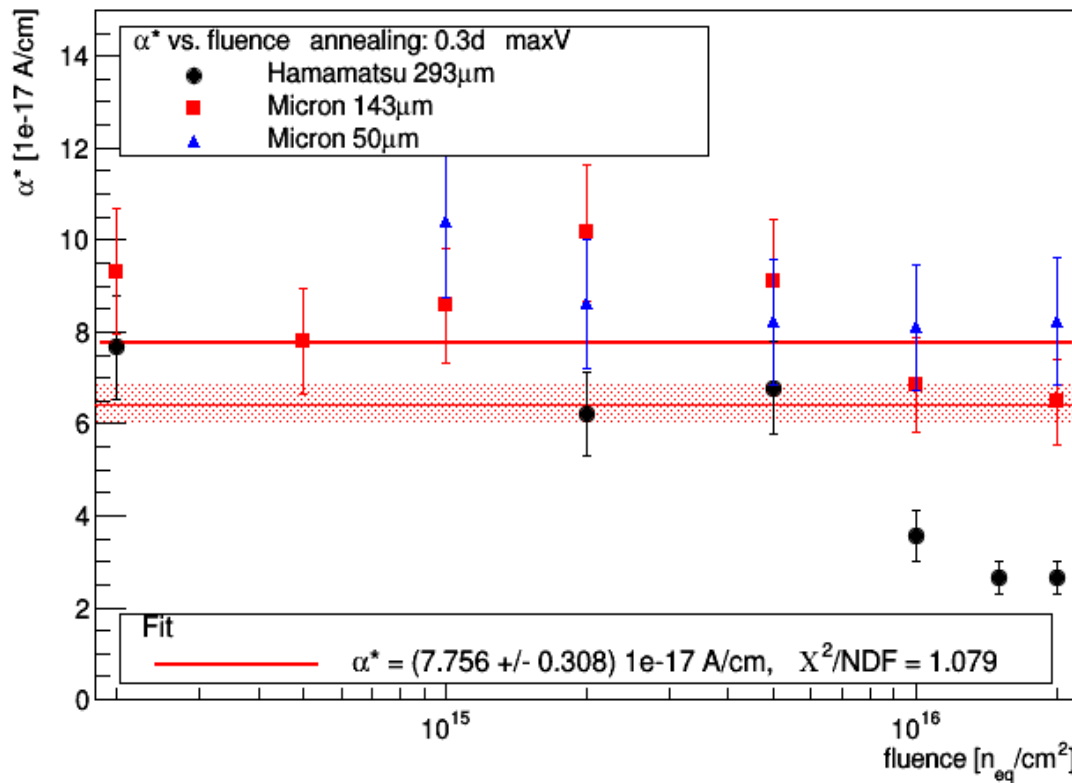
$$\alpha^* = \frac{I(\Phi_{eq}) - I_0}{\Phi_{eq} V}$$

for fully depleted sensor:  $\alpha^* \equiv \alpha = \text{const.}$   
Full depletion voltage usually not reached for high fluences.



HPK 293  $\mu\text{m}$

# $\alpha^*$ vs. fluence



$\alpha^*$  shown for highest voltage (350 V for 50  $\mu$ m-Micron, 1000 V otherwise)

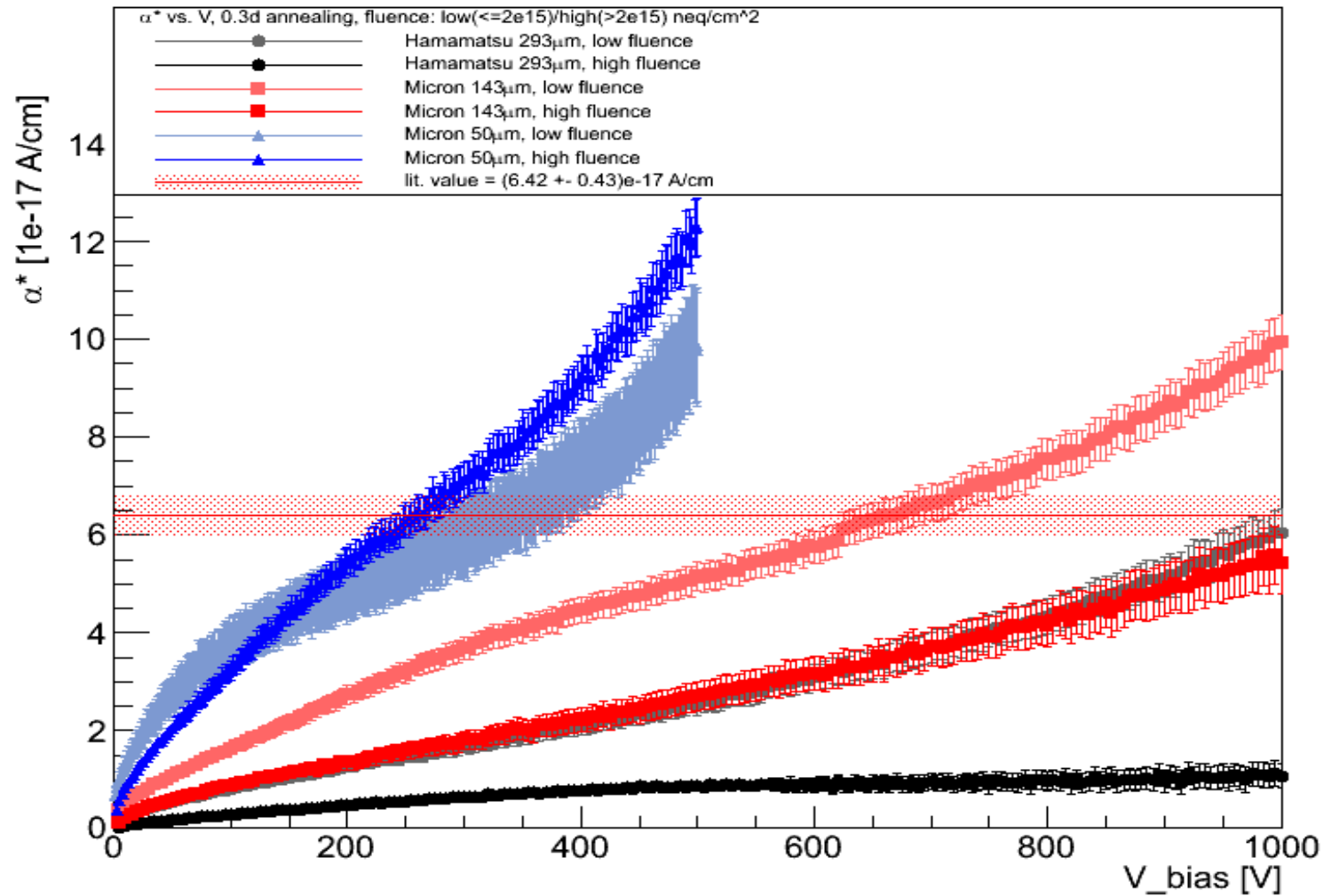
(three highest irradiated HPK-sensors not considered for fit.)

## result

$$\alpha^* = (7.8 \pm 0.9) \cdot 10^{-17} \text{ A/cm} \quad (\text{Lit. } \alpha = (6, 40 \pm 0, 43) \cdot 10^{-17} \text{ A/cm [2]})$$

[2] Sven Wonsak et al. *Measurements of the reverse current of highly irradiated silicon sensors*

# $\alpha^*$ - voltage dependence



# Conclusion



IV-measurements with new setup:

Calculated  $E_{g,eff}$  and  $\alpha^*$  for 18 irradiated sensors

Three sensor types: **293um HPK, 143um Micron, 50um Micron**

Irradiation fluences:  **$2 \times 10^{14}$  –  $2 \times 10^{16}$  neq/cm<sup>2</sup>**

- $E_{g,eff} = (1,18 \pm 0,03) \text{ eV}$   
(all measurements included)

- $E_{g,eff}^{low\Phi} = (1,19 \pm 0,03) \text{ eV}$   
(fluence up to  $10^{15}$  neq/cm<sup>2</sup>)

literature [1]:

$$E_{g,eff}^{lit} = (1,214 \pm 0,014) \text{ eV}$$

- $\alpha^* = (7.8 \pm 0.9) \cdot 10^{-17} \text{ A/cm}$   
(three sensors not included)

literature [2]:

$$\alpha_{lit}^* = (6,40 \pm 0,43) \cdot 10^{-17} \text{ A/cm}$$

$E_{g,eff}$ : Tendency to lower values at high fluences observed

*But strong dependence on efficiency of cooling system*

# Backup



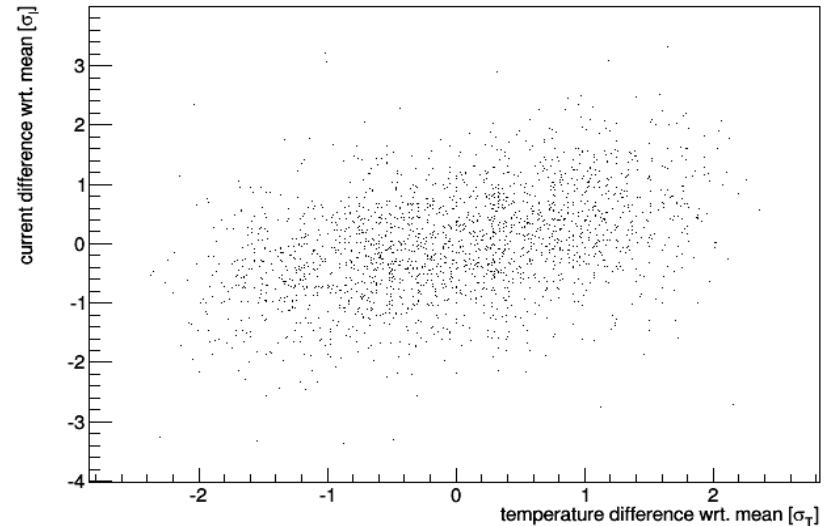
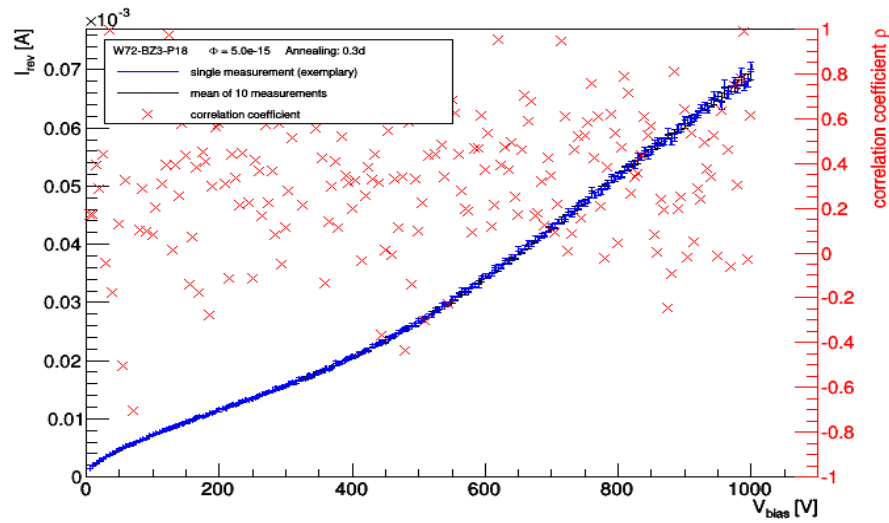
# Correlation of uncertainties



Fluctuations of sensortemperature influence current measurement.

⇒ Calculation of correlation coefficient from 10 IV-measurements ( $T = -23 \text{ }^\circ\text{C}$ )

$$\rho(I, T) = \frac{\text{cov}(I, T)}{\sigma_I \sigma_T} = \frac{1}{N \cdot \sigma_I \sigma_T} \sum_{i=1}^N (I_i - \bar{I})(T_i - \bar{T})$$





# $E_{g,eff}$ for different irradiation doses



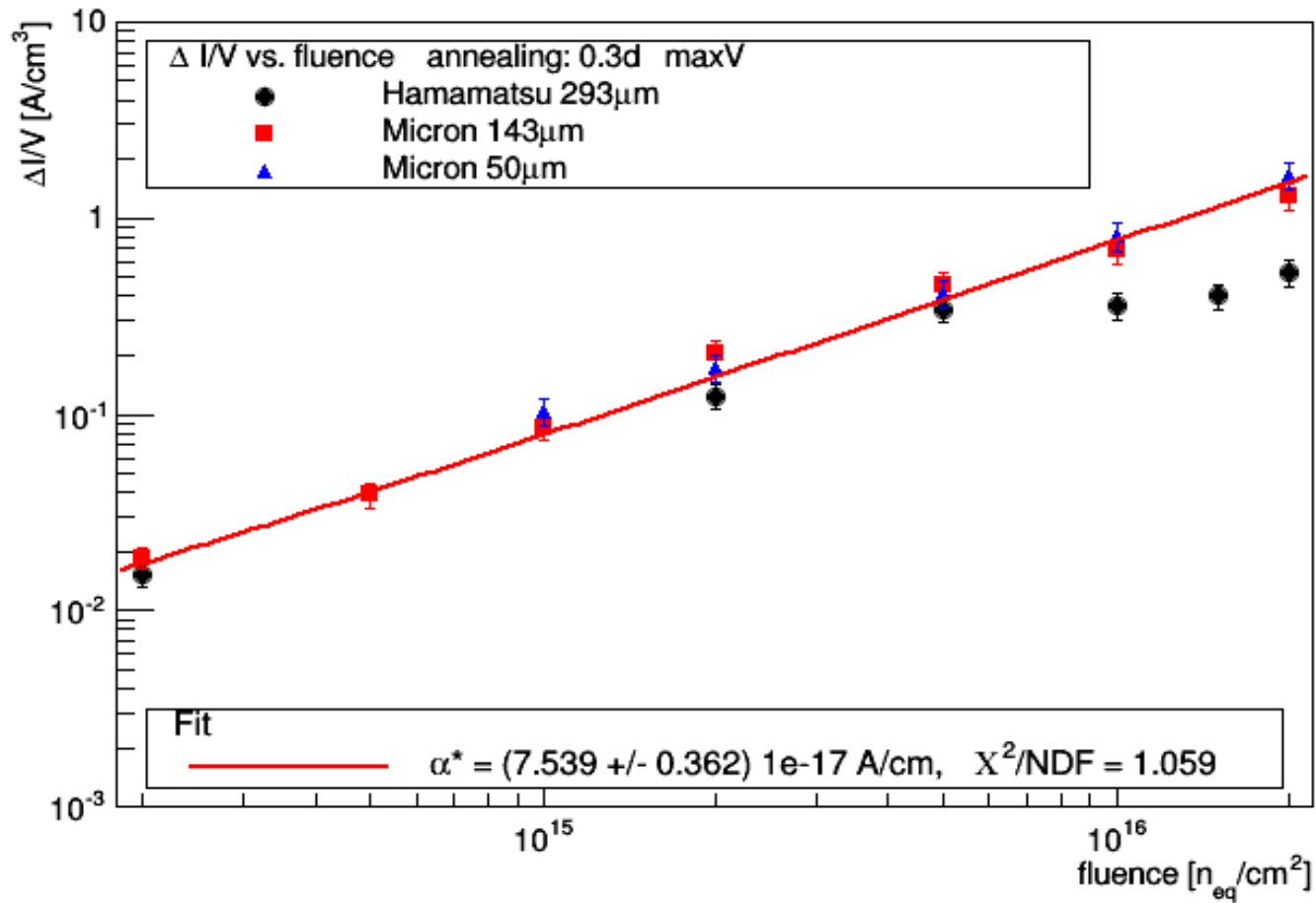
Nr.	Sensor	d [ $\mu m$ ]	$\Phi_{eq}$ [ $n_{eq} / cm^2$ ]	$E_{g,eff}^{fit}$ [eV]
1	HPK W277-BZ5-P23	293	$2 \cdot 10^{14}$	$1,2096 \pm 0,0013 \pm 0,03$
2	Micron 2437-14-M	143	$2 \cdot 10^{14}$	$1,1834 \pm 0,0015 \pm 0,03$
3	Micron 2437-14-O	143	$5 \cdot 10^{14}$	$1,2057 \pm 0,0017 \pm 0,03$
4	Micron 2437-14-Q	143	$1 \cdot 10^{15}$	$1,1747 \pm 0,0022 \pm 0,03$
5	HPK W264-BZ5-P23	293	$2 \cdot 10^{15}$	$1,1753 \pm 0,0011 \pm 0,03$
6	Micron 2437-14-S	143	$2 \cdot 10^{15}$	$1,1508 \pm 0,0019 \pm 0,03$
7	HPK W72-BZ3-P18	293	$5 \cdot 10^{15}$	$1,2347 \pm 0,0028 \pm 0,03$
8	Micron 2437-14-F	143	$5 \cdot 10^{15}$	$1,1795 \pm 0,0012 \pm 0,03$
9	HPK W73-BZ2-P20	293	$1 \cdot 10^{16}$	$1,1632 \pm 0,0014 \pm 0,03$
10	Micron 2437-14-G	143	$1 \cdot 10^{16}$	$1,1822 \pm 0,0012 \pm 0,03$
11	HPK W104-BZ2-P2	293	$1,5 \cdot 10^{16}$	$1,1327 \pm 0,0006 \pm 0,03$
12	HPK W104-BZ2-P17	293	$2 \cdot 10^{16}$	$1,1418 \pm 0,0009 \pm 0,03$
13	Micron 2437-14-H	143	$2 \cdot 10^{16}$	$1,123 \pm 0,001 \pm 0,03$
14	Micron 3107-6-3	50	$1 \cdot 10^{15}$	$1,1965 \pm 0,0015 \pm 0,03$
15	Micron 3107-6-9	50	$2 \cdot 10^{15}$	$1,1544 \pm 0,0015 \pm 0,03$
16	Micron 3107-6-10	50	$5 \cdot 10^{15}$	$1,1615 \pm 0,0017 \pm 0,03$
17	Micron 3107-6-14	50	$1 \cdot 10^{16}$	$1,1847 \pm 0,0015 \pm 0,03$
18	Micron 3107-6-21	50	$2 \cdot 10^{16}$	$1,2023 \pm 0,0012 \pm 0,03$
Lit. [1]				$1,214 \pm 0,014$

# $\alpha^*$ for different irradiation doses

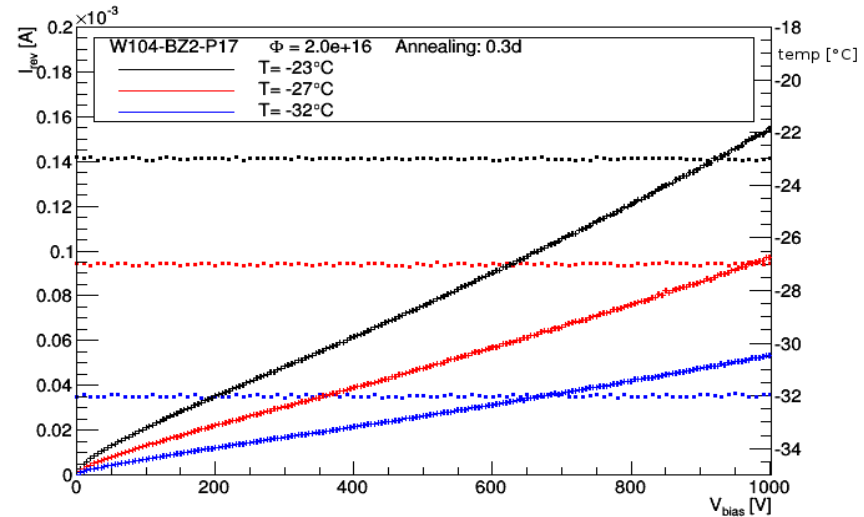
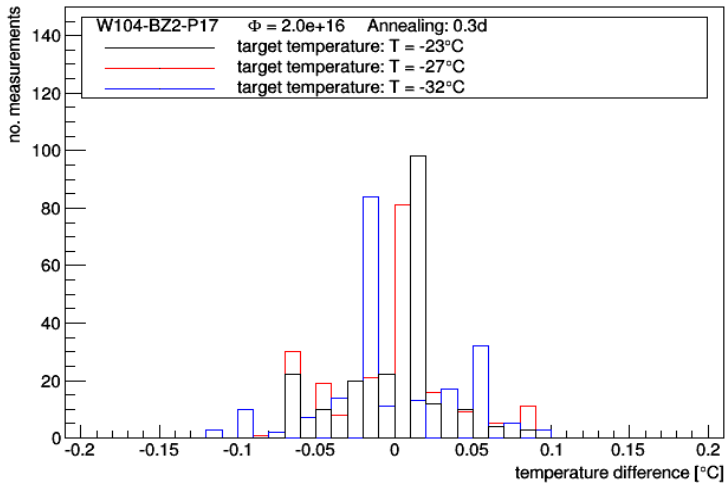


Nr.	d [ $\mu m$ ]	$\Phi_{eq}$ [ $n_{eq}/cm^2$ ]	$\alpha_{max V}^*$ [ $10^{-17}$ A/cm]
1	293	$2 \cdot 10^{14}$	$7,7 \pm 0,5 \pm 1,0$
2	143	$2 \cdot 10^{14}$	$9,3 \pm 0,7 \pm 1,2$
3	143	$5 \cdot 10^{14}$	$7,8 \pm 0,5 \pm 1,0$
4	143	$1 \cdot 10^{15}$	$8,6 \pm 0,6 \pm 1,1$
5	293	$2 \cdot 10^{15}$	$6,2 \pm 0,4 \pm 0,8$
6	143	$2 \cdot 10^{15}$	$10,2 \pm 0,7 \pm 1,3$
7	293	$5 \cdot 10^{15}$	$6,8 \pm 0,5 \pm 0,9$
8	143	$5 \cdot 10^{15}$	$9,1 \pm 0,6 \pm 1,2$
9	293	$1 \cdot 10^{16}$	$3,6 \pm 0,2 \pm 0,5$
10	143	$1 \cdot 10^{16}$	$6,9 \pm 0,5 \pm 0,9$
11	293	$1,5 \cdot 10^{16}$	$2,66 \pm 0,18 \pm 0,3$
12	293	$2 \cdot 10^{16}$	$2,64 \pm 0,18 \pm 0,3$
13	143	$2 \cdot 10^{16}$	$6,5 \pm 0,5 \pm 0,8$
14	50	$1 \cdot 10^{15}$	$10,4 \pm 1,0 \pm 1,3$
15	50	$2 \cdot 10^{15}$	$8,6 \pm 0,9 \pm 1,1$
16	50	$5 \cdot 10^{15}$	$8,2 \pm 0,8 \pm 1,1$
17	50	$1 \cdot 10^{16}$	$8,1 \pm 0,8 \pm 1,1$
18	50	$2 \cdot 10^{16}$	$8,2 \pm 0,8 \pm 1,1$
Lit. [2]			$6,40 \pm 0,43$

# $\Delta I/V$ vs. fluence



# IV-measurements at different temperatures



## Procedure:

- Temperatures of  $-23^{\circ}\text{C}$ ,  $-27^{\circ}\text{C}$  und  $-32^{\circ}\text{C}$
- Voltage supply:
  - positive high voltage on implants
  - ground on backplane
- temperatures of cooling liquid:
  - $+2^{\circ}\text{C}$  at
  - $-23^{\circ}\text{C}$ ,  $-27^{\circ}\text{C}$ -measurement
  - $-10^{\circ}\text{C}$  at  $-32^{\circ}\text{C}$ -measurement
- voltage step size: 1 V/s
- voltage constant for 10 s before starting each measurement
- measuring current in 5 V-steps while ramping down voltage to 0 V