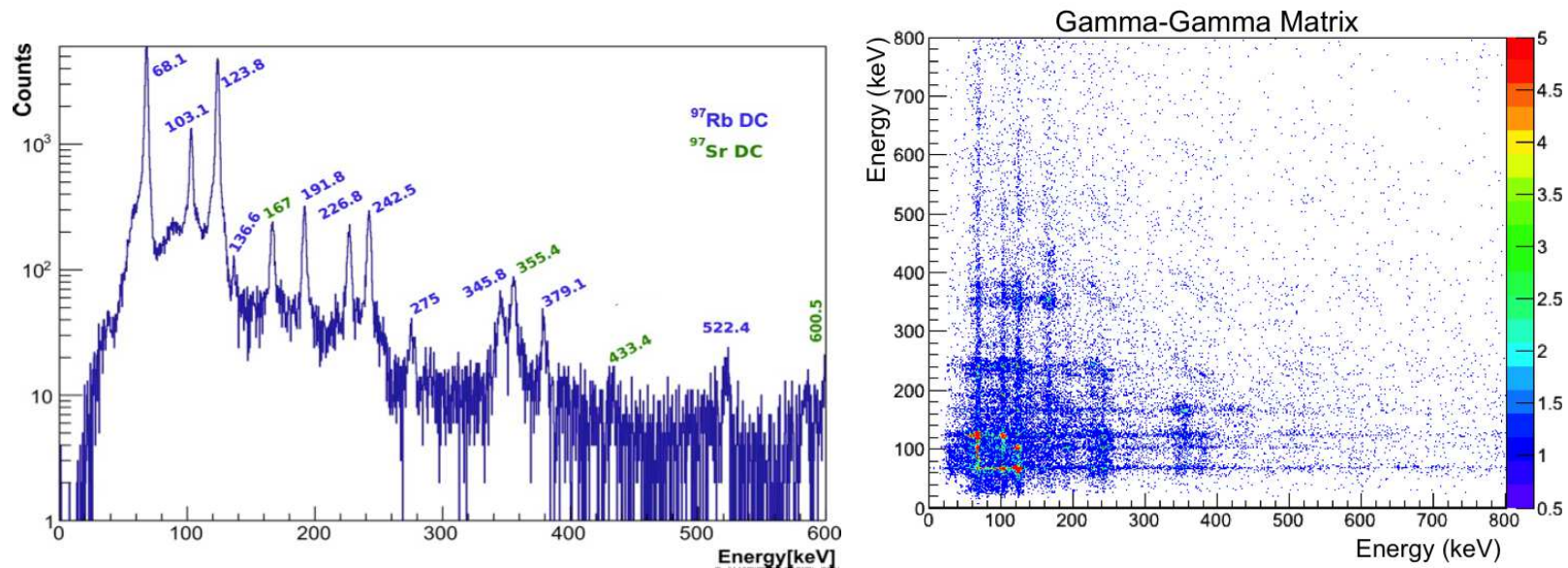

Model assumptions in Coulex analysis and other GOSIA tricks

Magda Zielińska
IRFU/SPhN, CEA Saclay

- Model assumptions for a well-deformed odd-A case: $^{97,99}\text{Rb}$
- Efficiency of particle detectors
- Optimal subdivision of Coulex data

Coulomb excitation of $^{97-99}\text{Rb}$ at ISOLDE

- identification of rotational bands in $^{97-99}\text{Rb}$ (first observation of collective states in these nuclei!)
- statistics sufficient for gamma-gamma coincidences – level schemes established

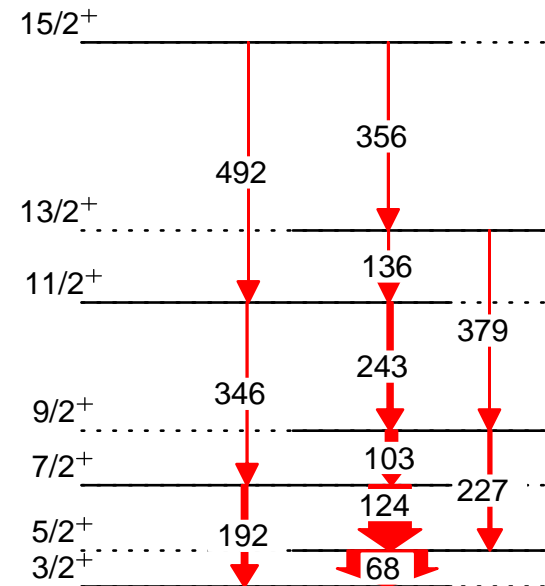


Ch. Sotty, Phys. Rev. Lett. 115 (2015) 172501

- Second step: extraction of E2 and M1 matrix elements using GOSIA code

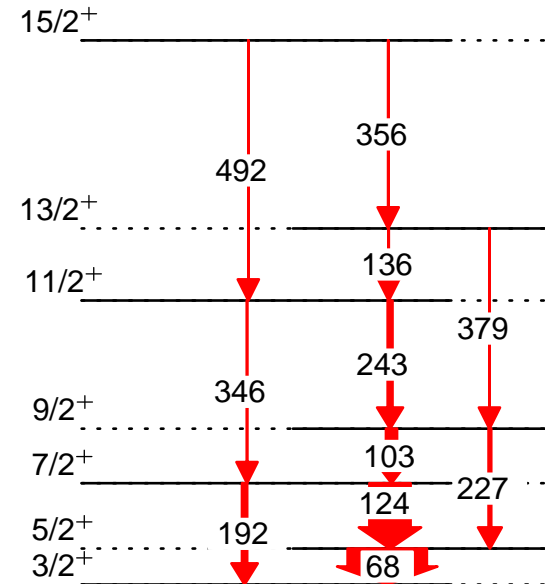
Problems in Coulex data analysis (^{97}Rb)

- Cline's safe Coulex criterion not fulfilled for high CM angles
- efficiency for the 68 keV line uncertain
- 355 keV transition obscured by a line in ^{97}Sr
- underdetermined problem: 20 gamma rays, 24 matrix elements (E2 and M1)
- very strong correlations between matrix elements



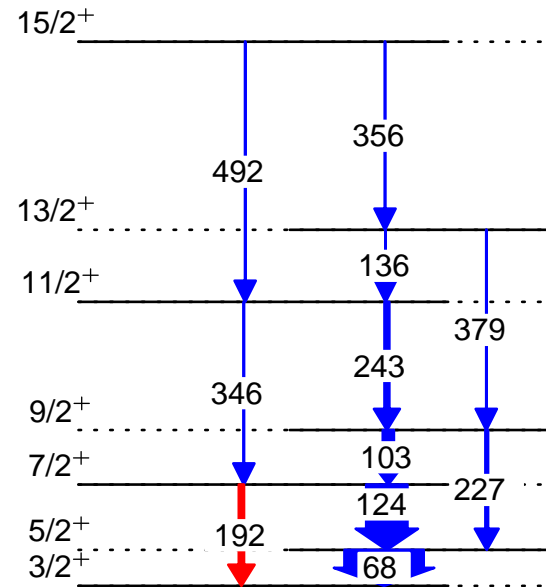
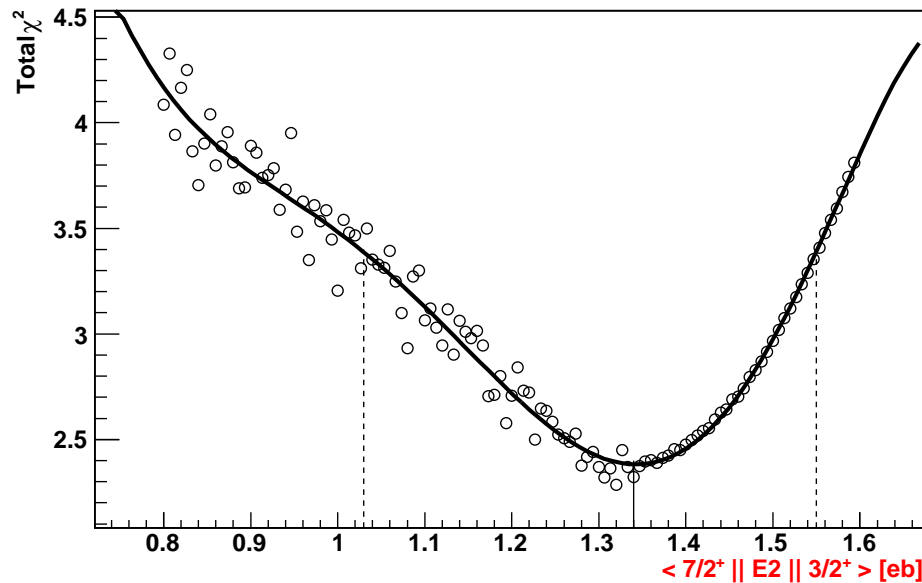
Problems in Coulex data analysis (^{97}Rb) and solutions

- Cline's safe Coulex criterion not fulfilled for high CM angles
 - 15 % of statistics excluded from the analysis
 - efficiency for the 68 keV line uncertain
 - would be a natural choice for normalisation but had to be excluded from the analysis
 - 355 keV transition obscured by a line in ^{97}Sr
 - intensity obtained from gamma-gamma coincidences
 - underdetermined problem: 20 gamma rays, 24 matrix elements (E2 and M1)
 - model assumptions necessary: Alaga rules
- $$\langle KI_f || E2 || KI_i \rangle = \sqrt{(2I_i + 1)} (I_i, K, 2, 0 | I_f, K) \sqrt{\frac{5}{16\pi}} eQ_0$$
- ⇒ within rotational model E2 branching ratio depends on spins only (Q_0 cancel out)
 - very strong correlations between matrix elements
 - large uncertainties for low-lying transitions



Normalisation to target excitation

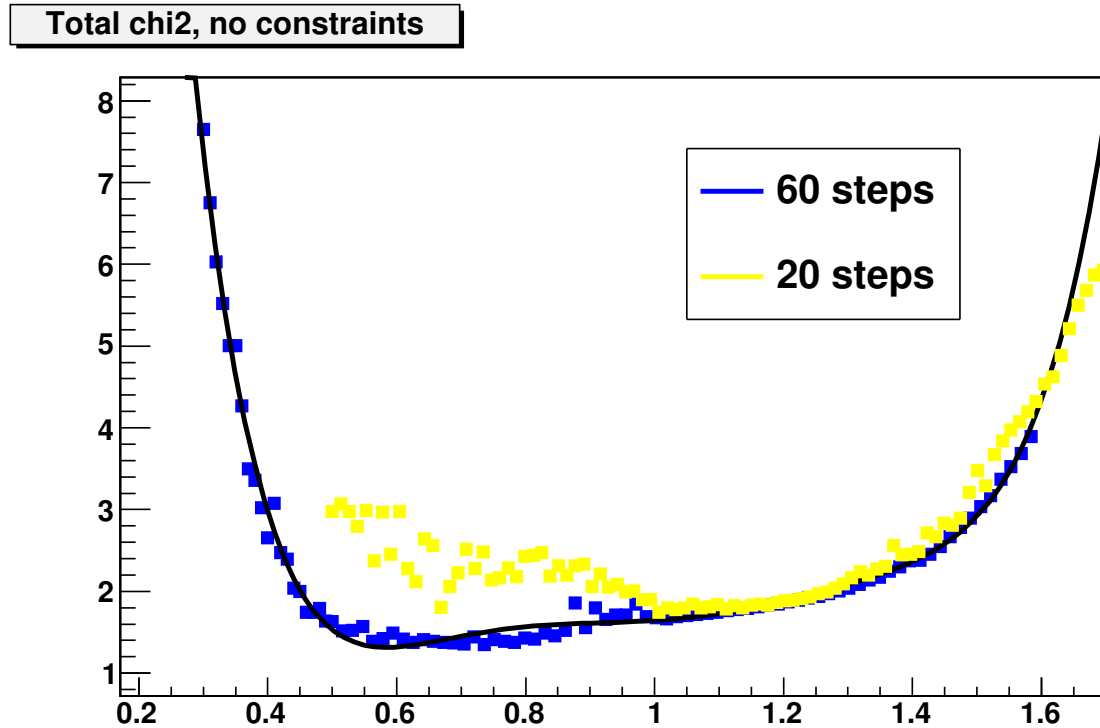
- for each value of $\langle 7/2^+ || E2 || 3/2^+ \rangle$ all remaining matrix elements in Rb and Ni are fitted to observed gamma-ray intensities and known spectroscopic data (GOSIA2)
- Alaga rules assumed for each pair of $I \rightarrow I-1$ and $I \rightarrow I-2$ E2 transitions



- for all other transitions a standard GOSIA1 analysis assuming this value of $\langle 7/2^+ || E2 || 3/2^+ \rangle$

Normalisation to target excitation

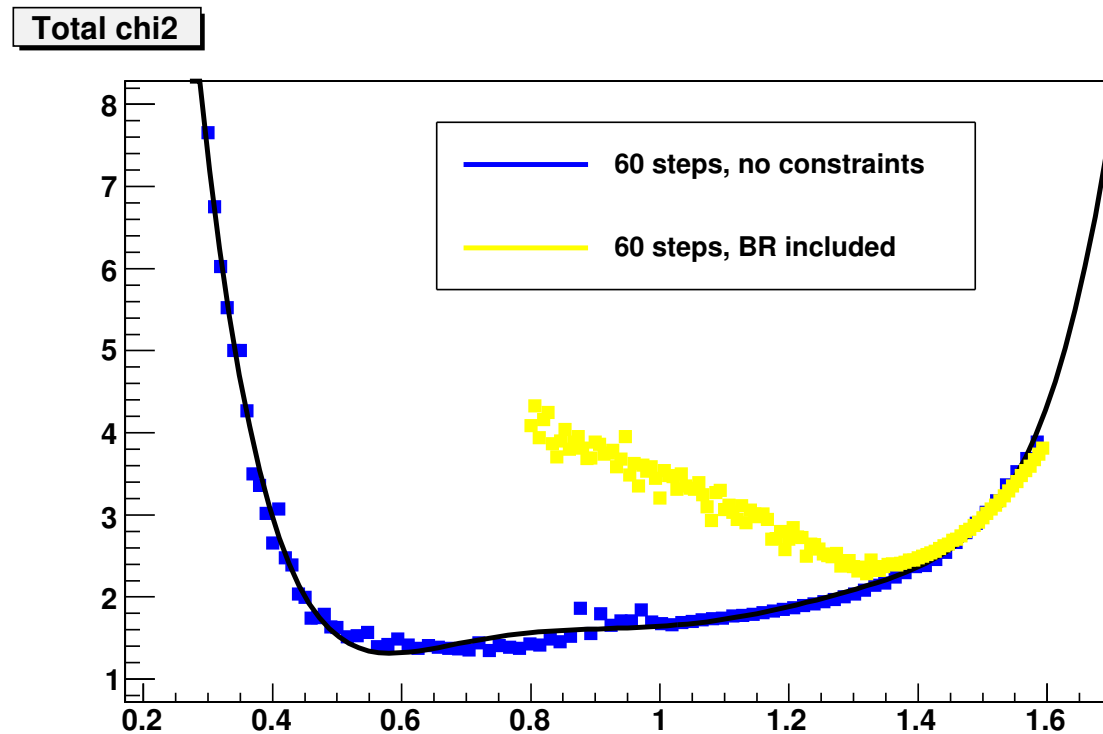
Convergence problems



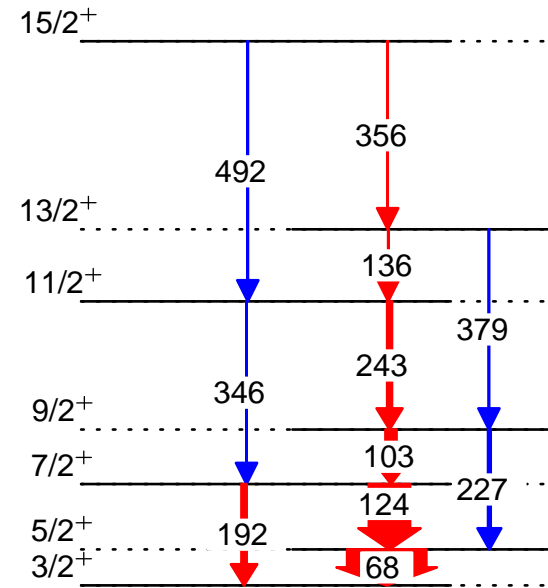
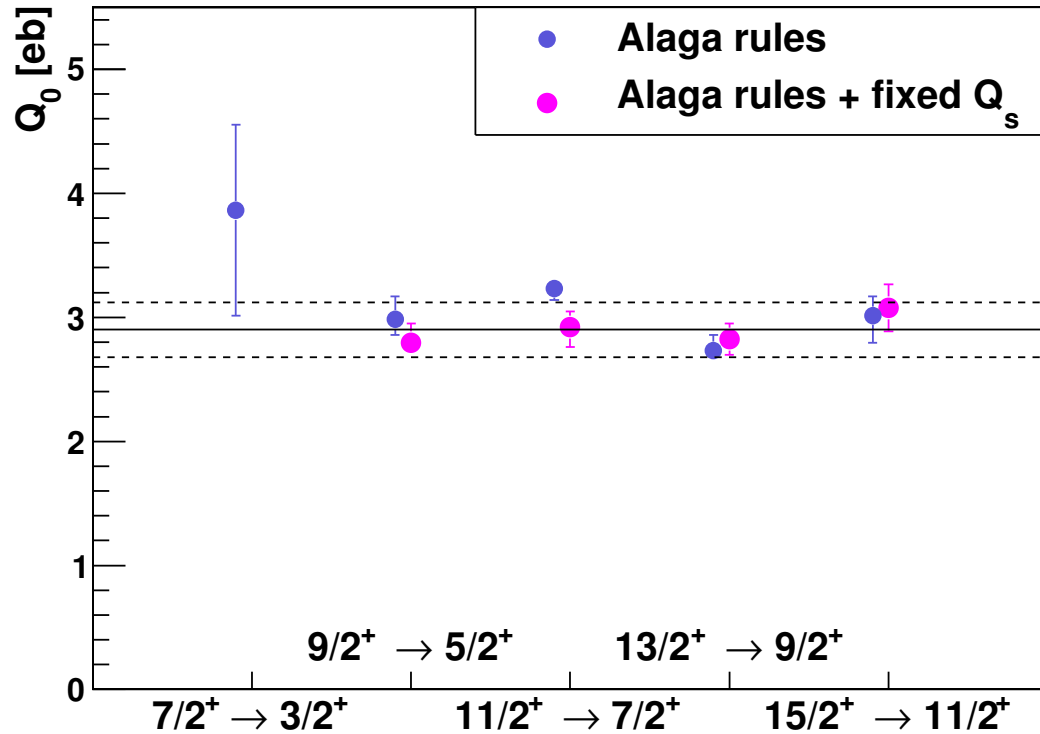
- fluctuations due to a local χ^2 minimum, more iterations give a more smooth dependence (and a new global minimum)
- smooth parts of the χ^2 curve don't change much

Normalisation to target excitation

Different minimum if E2 branching ratios imposed



Results: deformation of ^{97}Rb



- two different assumptions give consistent results for 4 matrix elements
- these 4 transitions are populated in multi-step excitation → matrix elements related to observed intensity ratios in ^{97}Rb (no need for other normalisation)
- results consistent with Q_{sp} of the g.s. measured in laser spectroscopy (horizontal lines)

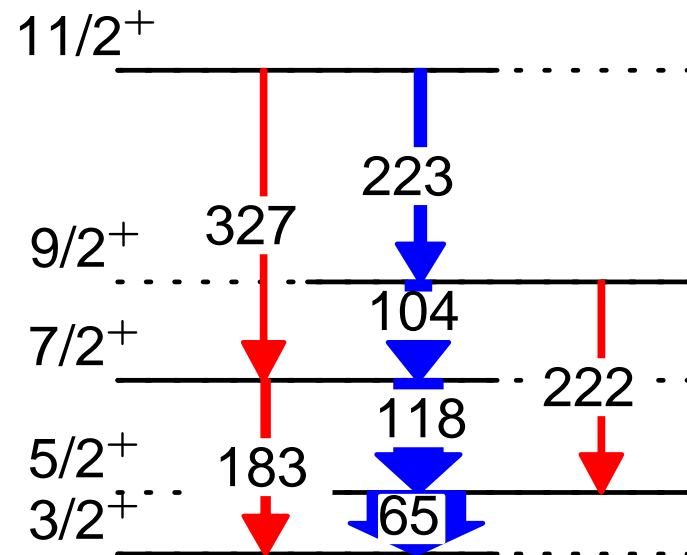
Next step: ^{99}Rb

Problems we know already from ^{97}Rb :

- Cline's safe Coulex criterion not fulfilled for high CM angles
- efficiency for the 65 keV line uncertain
- very strong correlations between matrix elements

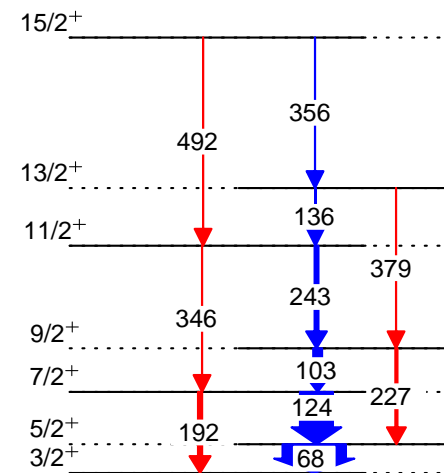
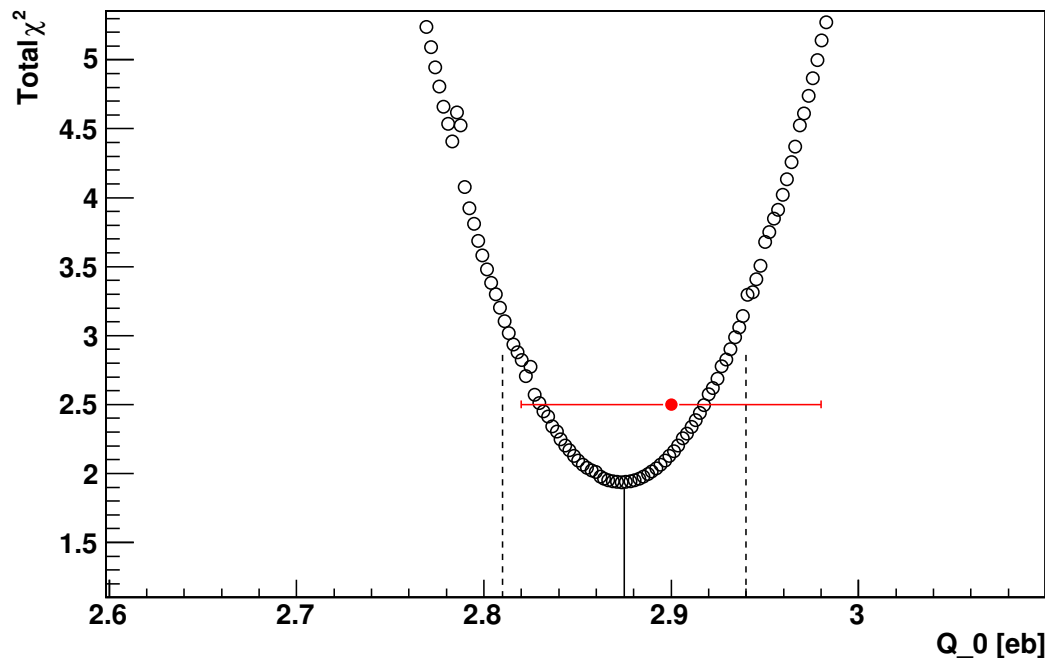
New problems:

- very low statistics (few hundred counts in the strongest line)
- target excitation not observed
- unresolved doublet at 222 keV
- extremely underdetermined problem: 6 gamma rays, 15 matrix elements)



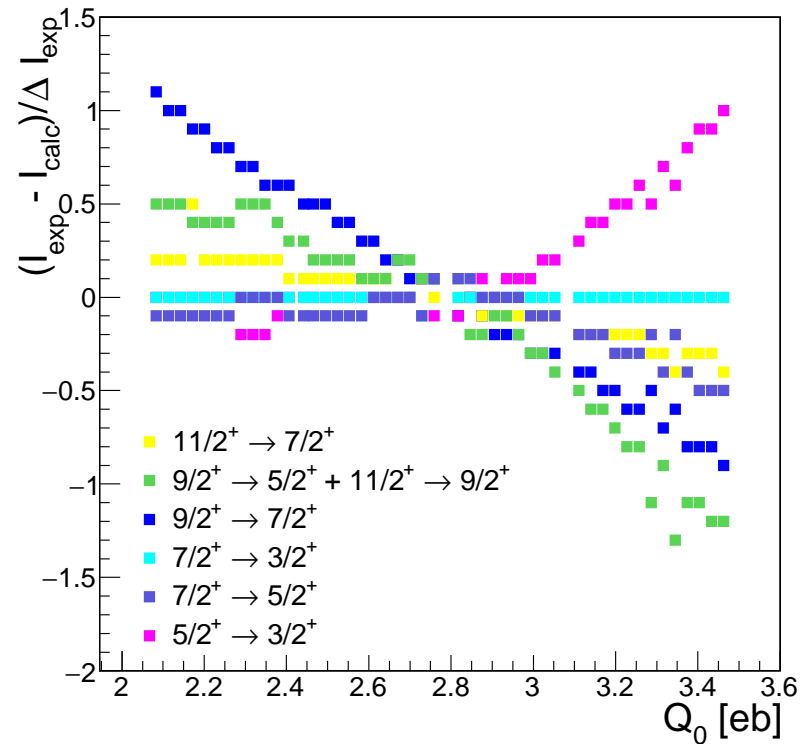
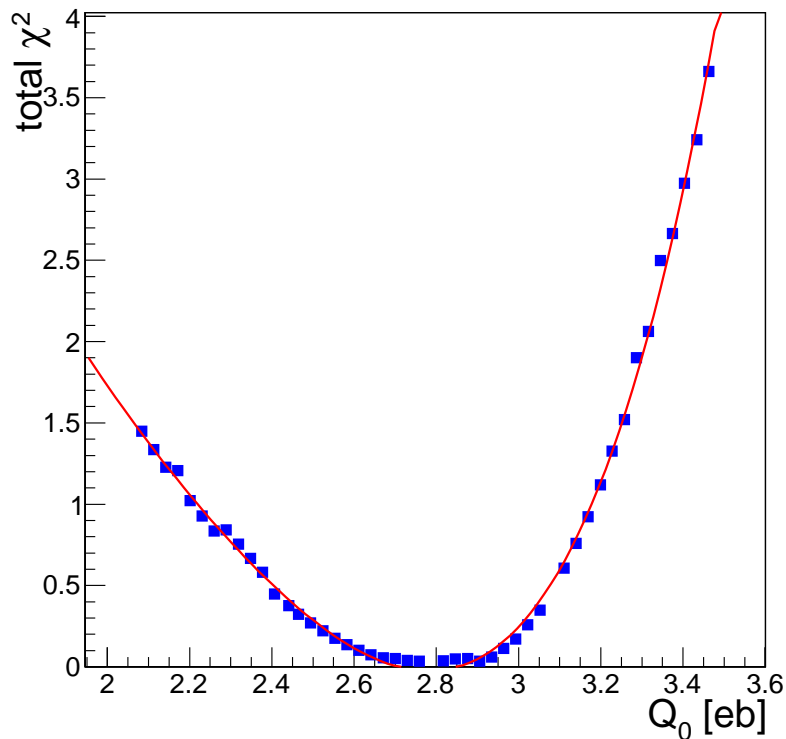
⁹⁹Rb: proposed solution and test on ⁹⁷Rb data

- matrix elements in the upper part of a strongly deformed rotational band related to observed intensity ratios in the nucleus under study (no external normalisation required)
- all E2 matrix elements (including Q_s) coupled using rotational model
- then we fit only M1 matrix elements and one Q_0 to measured gamma-ray intensities
- tested on ⁹⁷Rb data, result consistent with **weighted average of Q_0 values** obtained in standard analysis

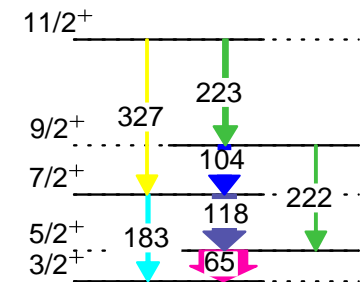


⁹⁹Rb: results

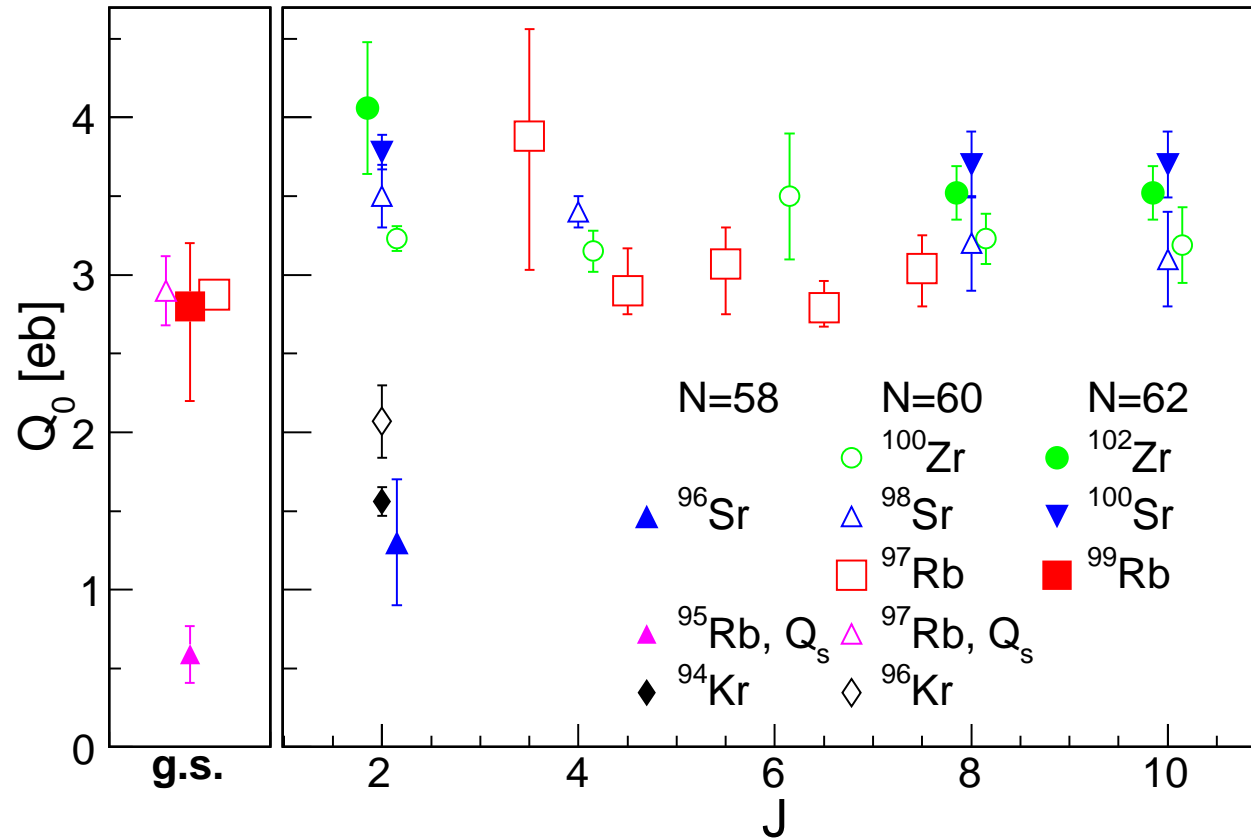
- 4 M1 matrix elements and one Q_0 fitted to measured gamma-ray intensities in ⁹⁹Rb



- one clear χ^2 minimum for all observed transitions
- precision rather low due to limited statistics



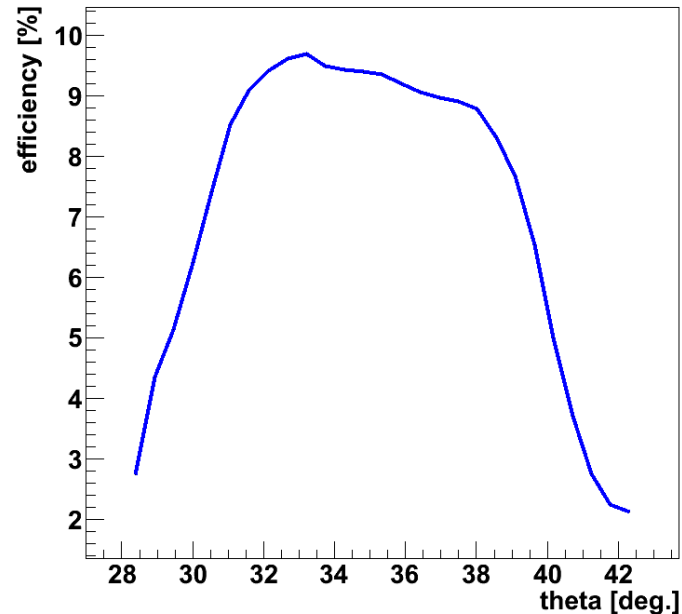
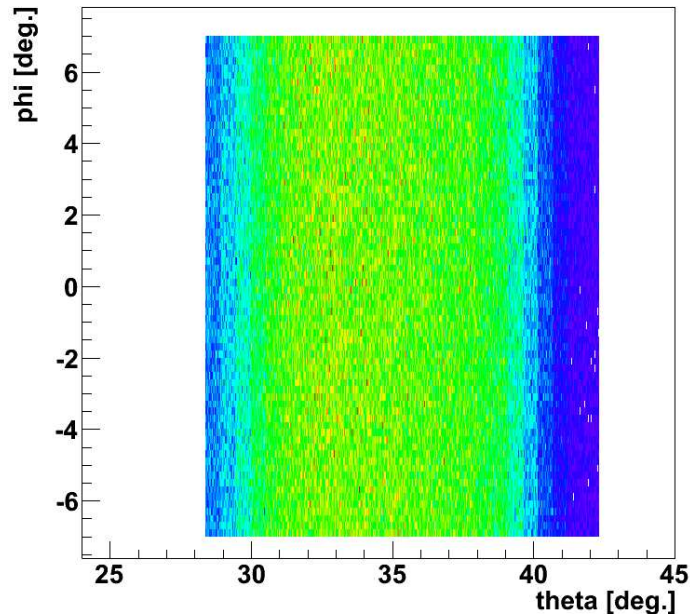
Deformation of ^{99}Rb : comparison with ^{97}Rb



Efficiency of particle detectors

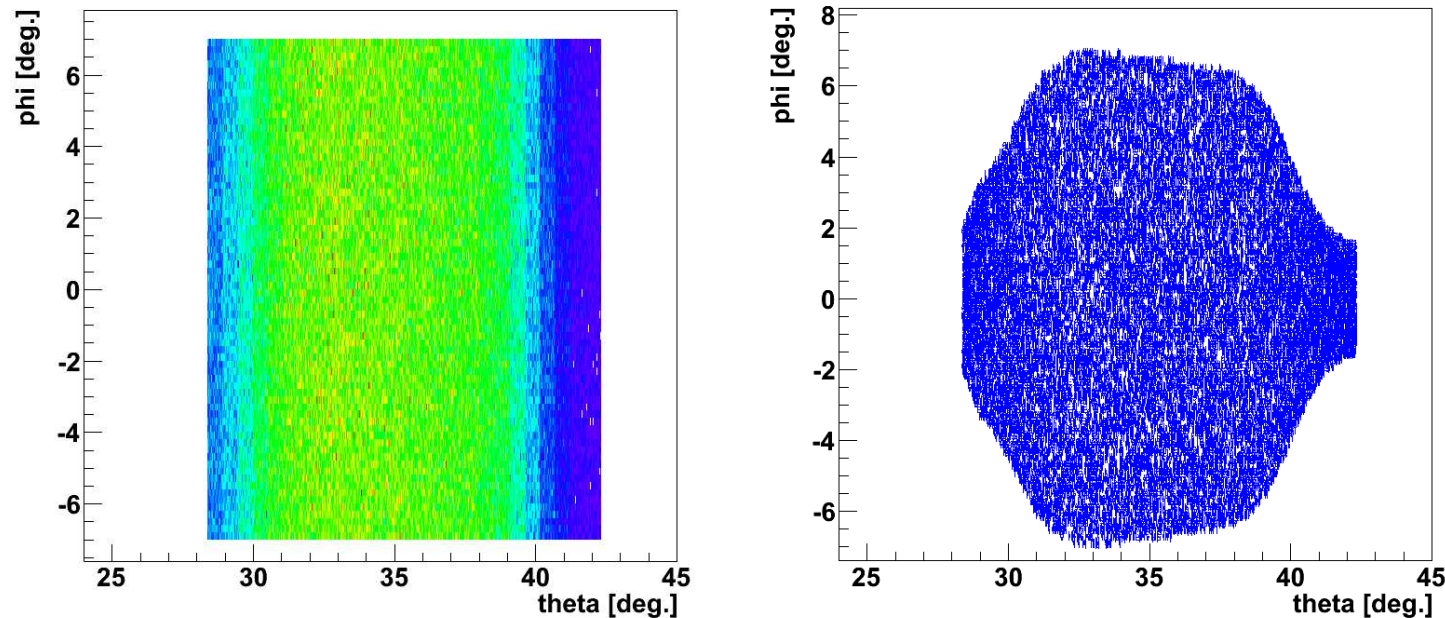
two ways to account for it

Efficiency of a particle detector



- efficiency doesn't have to be uniform for all the detector's area
- some parts of the detectors can stop working at some point
- if the detector has a uniform efficiency lower than 100% it's fine (it's included in the normalisation constant of the experiment)

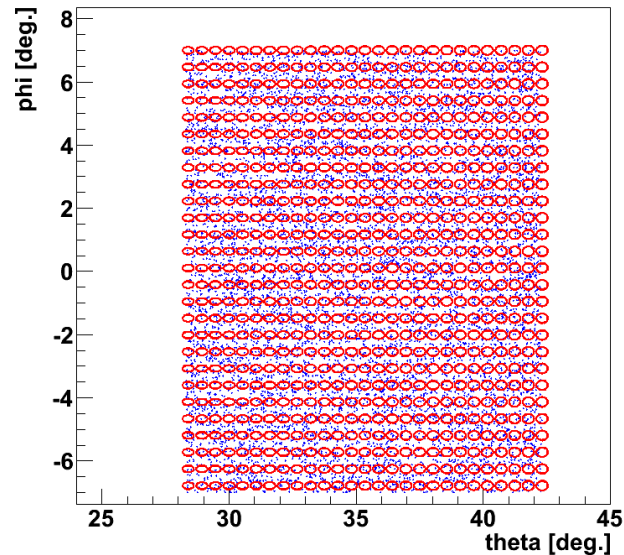
Efficiency of a particle detector



Solution 1:

- Coulomb excitation strength depends on θ scattering angle – one can modify detector shape in φ to take the efficiency into account
- applicable if we have a symmetric gamma detection set-up (gamma-particle correlations smoothed out)
- φ range covered by the detector scaled according to efficiency: true range (here: $(-7^\circ, 7^\circ)$) where efficiency is maximal, reduced to $(-3.5^\circ, 3.5^\circ)$ where it's only 50% of the maximum value, etc.

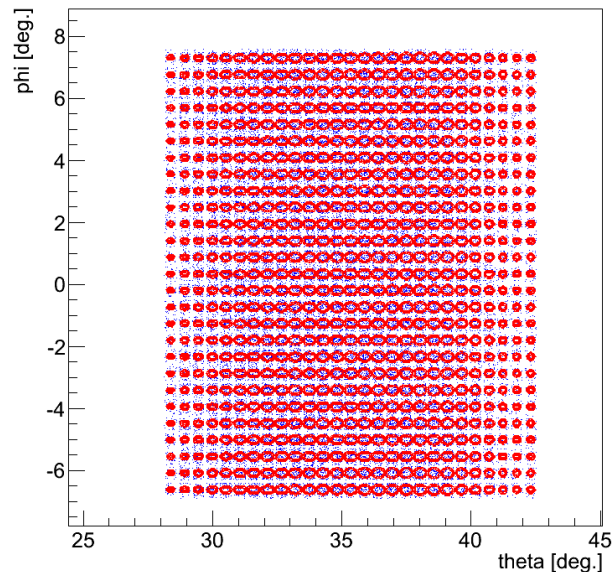
Efficiency of the particle detector: second solution



```
OP,INTG
3, 3, 683.2, 690.7, 28.38, -6.62, 0.223
683.2, 687, 690.7
3, 3, ...
...
```

- detector shape approximated by a large number (here: 729) of small circular detectors
- first step: comparison with a 100% efficiency detector, **angular range covered by a single detector** chosen to reproduce the Rutherford cross section

Efficiency of the particle detector: second solution



```
OP,INTG
3, 3, 683.2, 690.7, 28.38, -6.62, 0.119
683.2, 687, 690.7
3, 3, ...
...
```

- detector shape approximated by a large number (here: 729) of small circular detectors
- first step: comparison with a 100% efficiency detector, angular range covered by a single detector chosen to reproduce the Rutherford cross section
- second step: **detector areas** scaled according to efficiency (θ_{half} scaled as \sqrt{A})
- does not change the φ coverage of the detector – better if particle-gamma correlations important

Comparison of results

Integrated yields, normalised to $2_1^+ \rightarrow 0_1^+$ (YCOR)

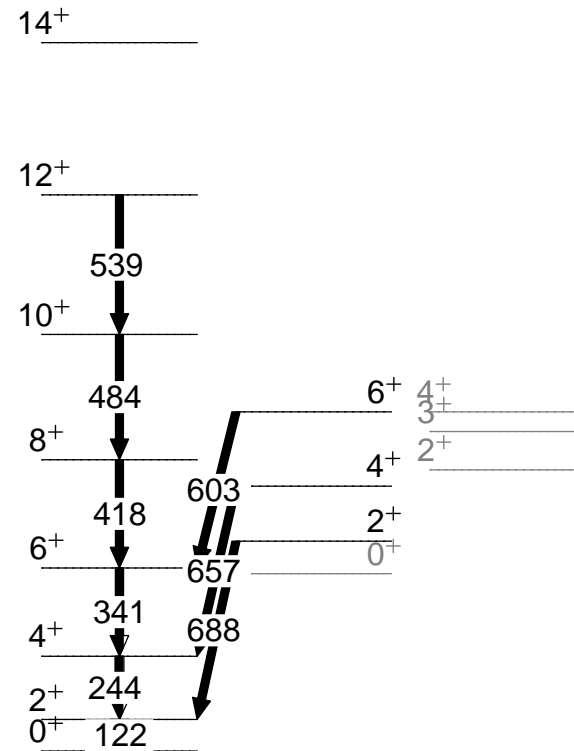
transition	eff vs standard	PIN vs standard	PIN, eff vs PIN
$14_1^+ \rightarrow 12_1^+$	18.5%	-2.8%	19.3%
$12_1^+ \rightarrow 10_1^+$	13.6%	-2.0%	13.6%
$10_1^+ \rightarrow 8_1^+$	8.2%	-1.0%	7.8%
$6_2^+ \rightarrow 6_1^+$	4.3%	-0.4%	3.5%
$8_1^+ \rightarrow 6_1^+$	0.7%	0.0%	0.0%
$4_2^+ \rightarrow 4_1^+$	-3.4%	0.7%	-4.0%
$2_2^+ \rightarrow 2_1^+$	-1.2%	0.0%	-1.2%
$6_1^+ \rightarrow 4_1^+$	-1.7%	0.7%	-2.7%
$4_1^+ \rightarrow 2_1^+$	-1.1%	0.5%	-1.6%
$2_1^+ \rightarrow 0_1^+$	0.0%	0.0%	0.0%
Rutherford	-23.2%	0.5%	-25.7%

- both solutions work reasonably well
- corrections important for multi-step and non-yrast states

Buffer states

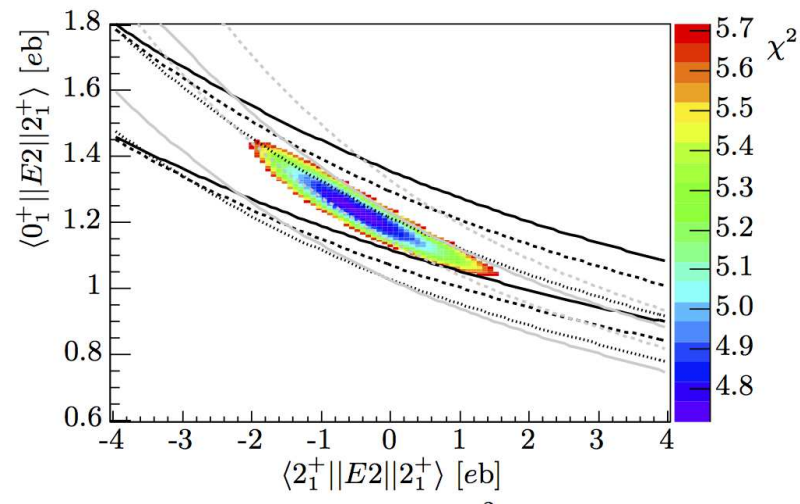
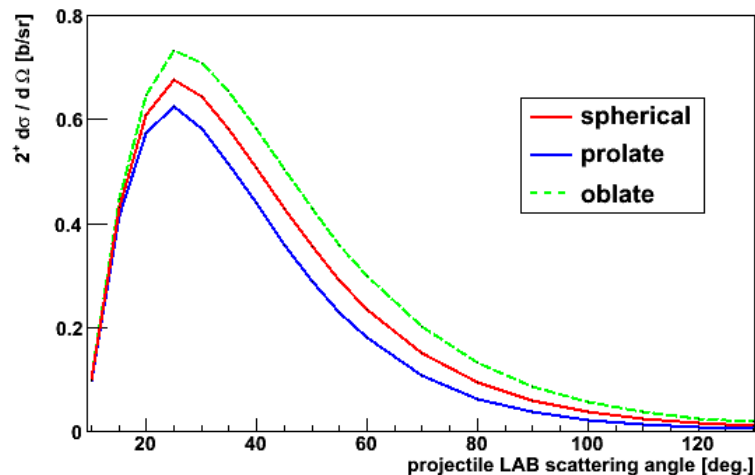
Buffer states

- reorientation effect can be comparable with population of higher-lying states
- when analysing Coulex data, we should include buffer states on top of bands to account for possible excitation of higher-lying states
- otherwise we get incorrect quadrupole moments
- rotational model can be used to estimate starting values of ME



Optimal subdivision of Coulex data

Where is sensitivity to quadrupole moments coming from?



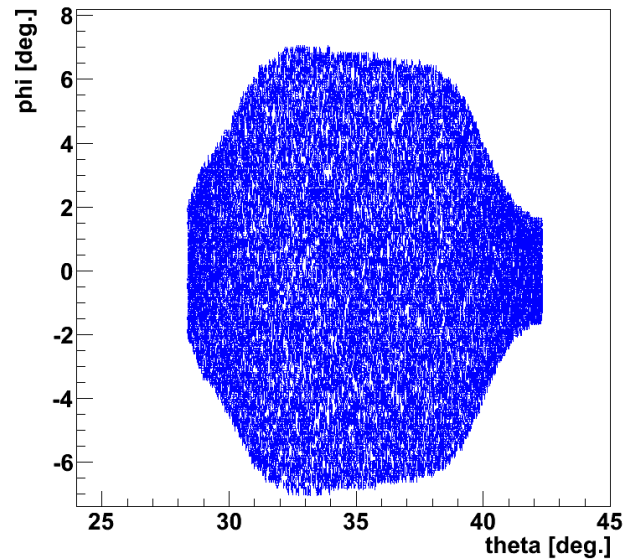
L. Gaffney et al., Phys. Rev. C 91, 064313 (2015)

- compromise between number of subdivisions and statistics
- useful to have a range where the influence of $\langle 2^+ || E2 || 2^+ \rangle$ is negligible (horizontal cut), but not always possible
- for high CM angles influence of quadrupole moment should be higher than statistical error of the gamma yield
- if two cuts in $\langle 2^+ || E2 || 2^+ \rangle$, $\langle 2^+ || E2 || 0^+ \rangle$ plane are really close, probably you will gain more by combining the statistics

Backup slides: how to describe complicated detector shapes in GOSIA

(step by step!)

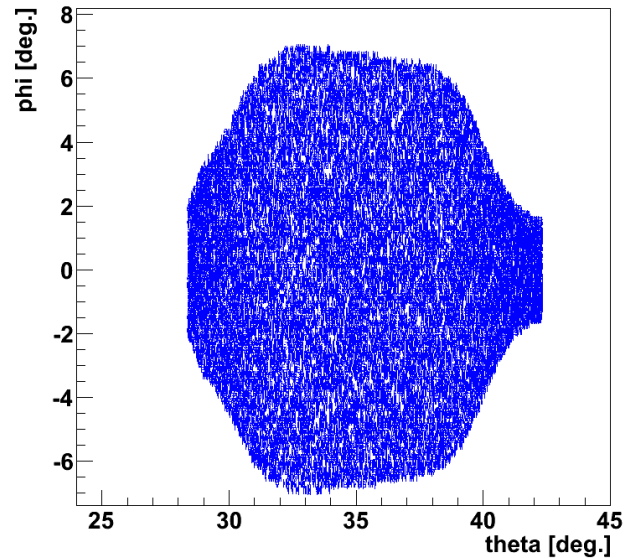
Efficiency included by modifying the detector shape



OP,INTG
3,

- number of energy meshpoints

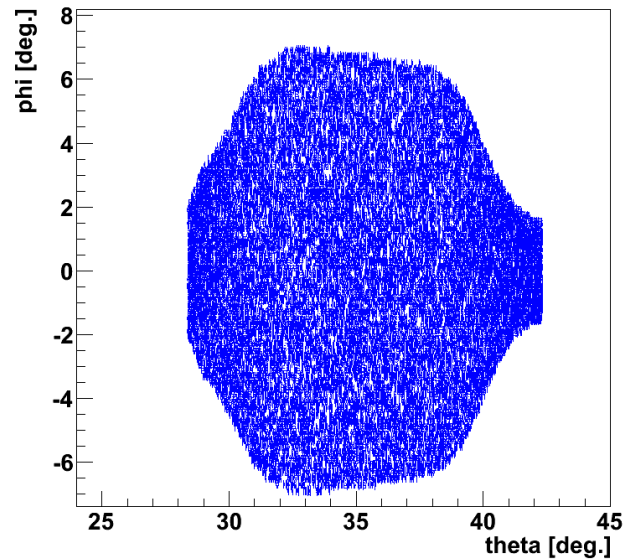
Efficiency included by modifying the detector shape



OP,INTG
3,-13,

- number of energy meshpoints
- number of θ meshpoints (with „-” sign if we plan to introduce the $\varphi(\theta)$ dependence)

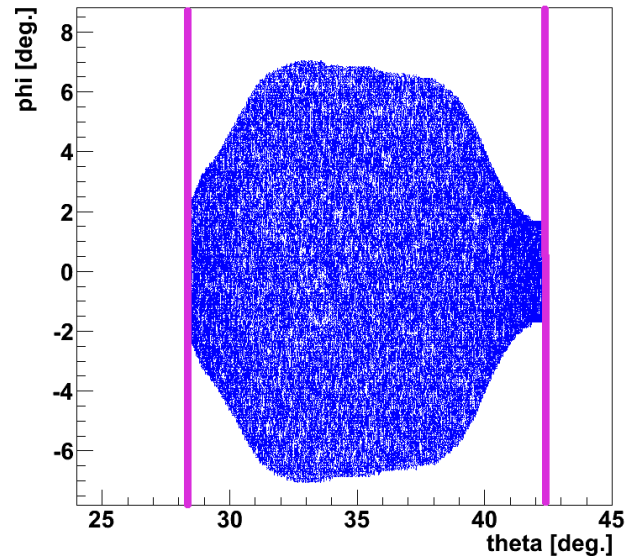
Efficiency included by modifying the detector shape



OP,INTG
3,-13,683.2,690.7,

- number of energy meshpoints
- number of θ meshpoints (with „-” sign if we plan to introduce the $\varphi(\theta)$ dependence)
- minimum and maximum bombarding energy

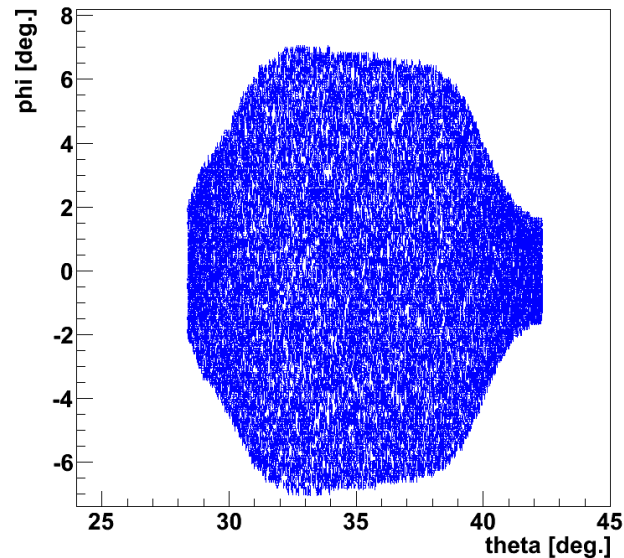
Efficiency included by modifying the detector shape



OP,INTG
3,-13,683.2,690.7,28.3,42.3,

- number of energy meshpoints
- number of θ meshpoints (with „-” sign if we plan to introduce the $\varphi(\theta)$ dependence)
- minimum and maximum bombarding energy
- minimum and maximum θ angles

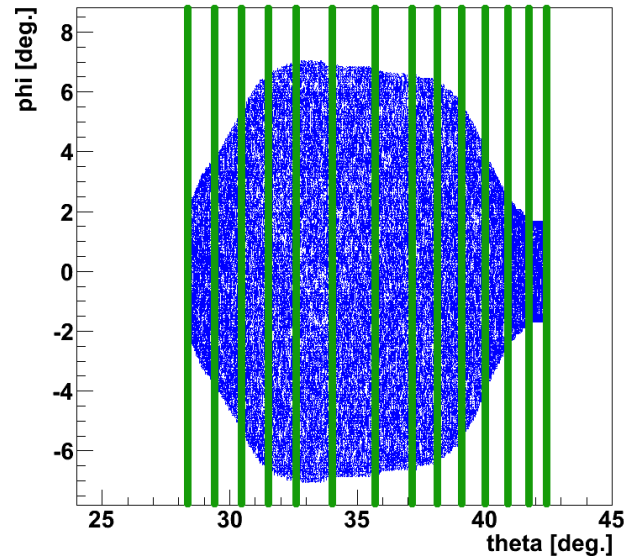
Efficiency included by modifying the detector shape



```
OP,INTG  
3,-13,683.2,690.7,28.3,42.3,  
683.2,687,690.7
```

- number of energy meshpoints
- number of θ meshpoints (with „-“ sign if we plan to introduce the $\varphi(\theta)$ dependence)
- minimum and maximum bombarding energy
- minimum and maximum θ angles
- energy meshpoints

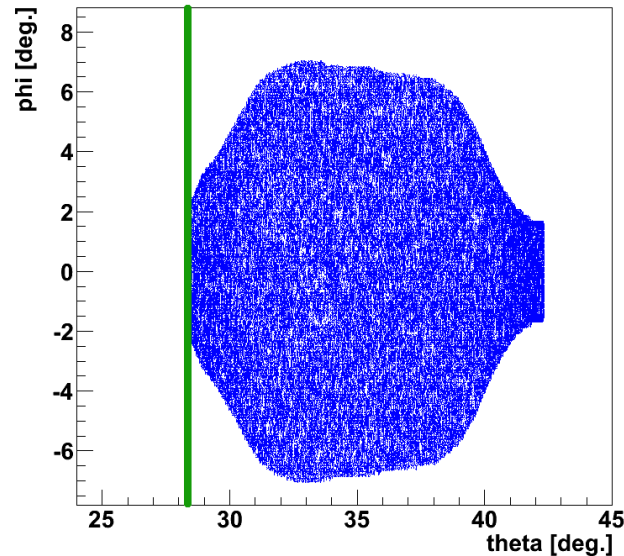
Efficiency included by modifying the detector shape



```
OP,INTG
3,-13,683.2,690.7,28.3,42.3,
683.2,687,690.7
28.3,29.3,30.3,31.5,33.,35,36.5,38.5,39.5,40.5,
41.5,42,42.3
```

- number of energy meshpoints
- number of θ meshpoints (with „-” sign if we plan to introduce the $\varphi(\theta)$ dependence)
- minimum and maximum bombarding energy
- minimum and maximum θ angles
- energy meshpoints
- theta meshpoints: among them minimum and maximum θ angles, more points where the shape is more complicated

Detector shape – continued



OP,INTG

3,-13,683.2,690.7,28.3,42.3,
683.2,687,690.7

28.3,29.3,30.3,31.5,33.,35,36.5,38.5,39.5,40.5,
41.5,42,42.3

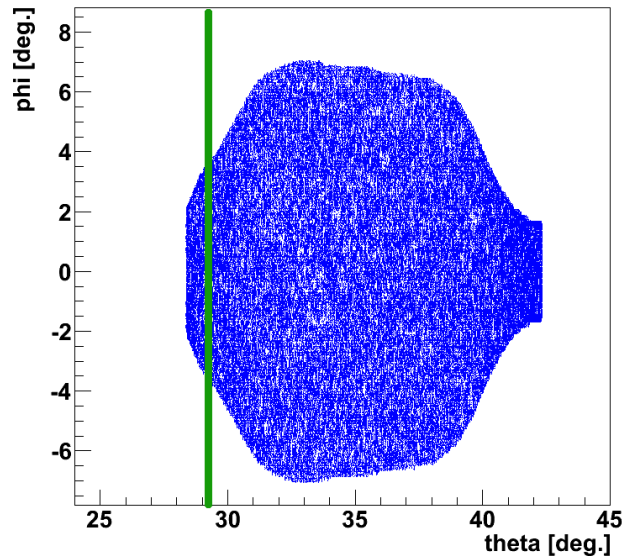
1

-2,2

Then for each of the theta meshpoints we have to give the $\varphi_{minimum}$ and $\varphi_{maximum}$; if there is more than one phi range for this θ , we have to specify more such ϕ pairs.

- first point ($\theta = 28.3^\circ$) – one φ range ($-2^\circ, +2^\circ$)

Detector shape – continued

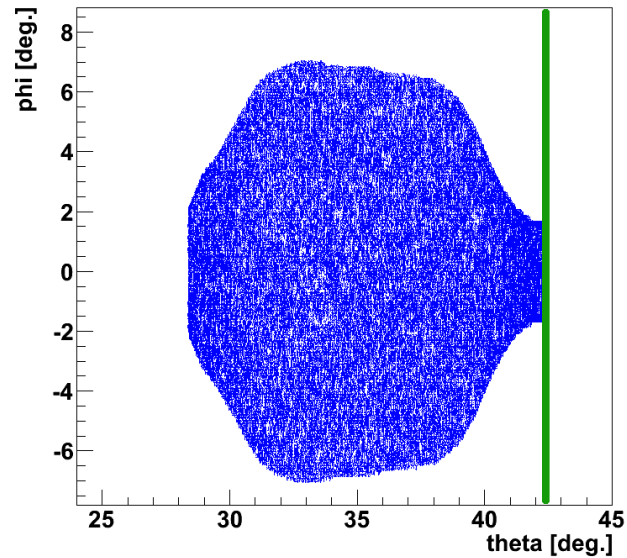


```
OP,INTG
3,-13,683.2,690.7,28.3,42.3,
683.2,687,690.7
28.3,29.3,30.3,31.5,33.,35,36.5,38.5,39.5,40.5,
41.5,42,42.3
1
-2,2
1
-3.6,3.6
```

Then for each of the theta meshpoints we have to give the $\varphi_{minimum}$ and $\varphi_{maximum}$; if there is more than one phi range for this θ , we have to specify more such ϕ pairs.

- first point ($\theta = 29.3^\circ$) – one φ range ($-2^\circ, +2^\circ$)
- second point ($\theta = 28.3^\circ$) – one φ range ($-3.6^\circ, +3.6^\circ$)
- and so on...

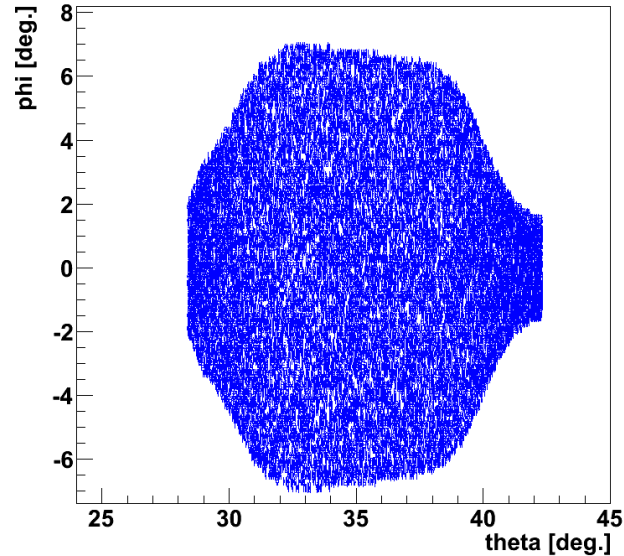
Detector shape – continued



1,
-1.5, 1.5

- ...
- last point ($\theta = 42.3^\circ$) – one φ range: $(-1.5^\circ, 1.5^\circ)$

Detector shape – continued

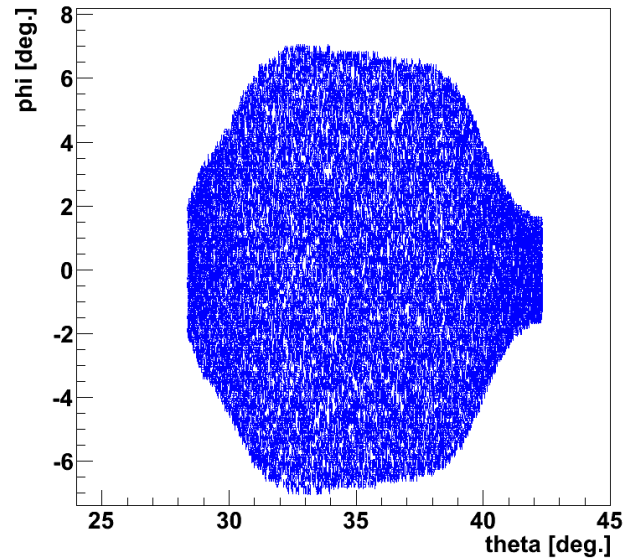


1
-1.5,1.5
3
683.2,687,690.7
30.3,30.1,29.9

Input of stopping powers:

- number of meshpoints
- energy meshpoints
- stopping powers

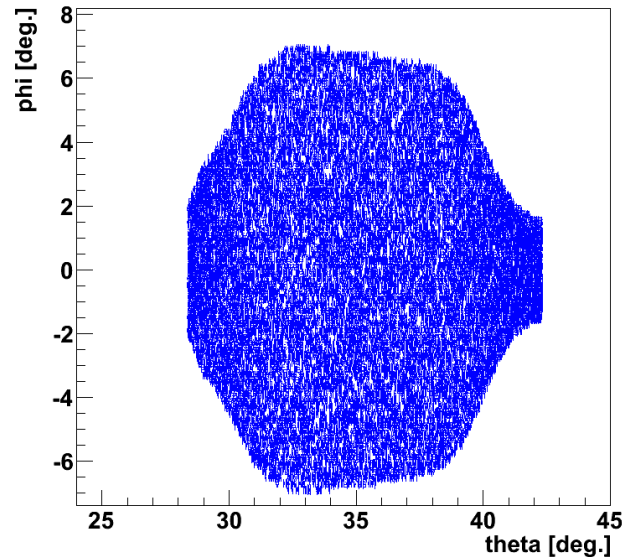
Detector shape – continued



3
683.2,687,690.7
30.3,30.1,29.9
10,

- stopping powers
- number of subdivisions of energy used for interpolation (even number, maximum value 100)

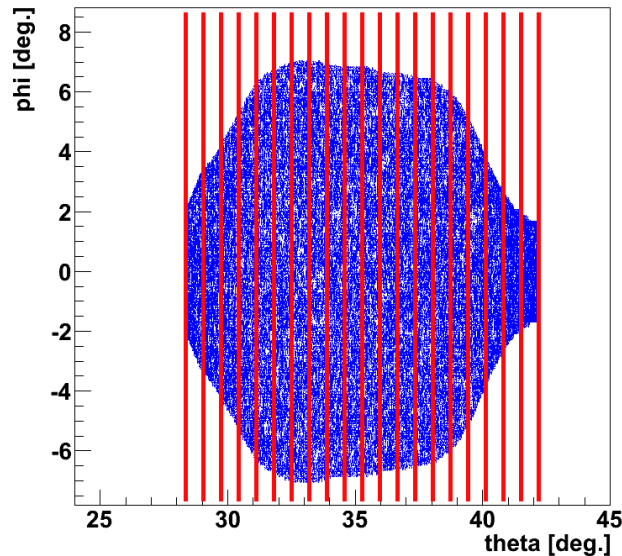
Detector shape – continued



3
683.2,687,690.7
30.3,30.1,29.9
10,-26

- stopping powers
- number of equal subdivisions of energy used for interpolation (even number, maximum value 100)
- **number of equal subdivisions of theta** used for interpolation (even number, maximum value 100, with „-” sign if we introduce the $\varphi(\theta)$ dependence). Here: **twenty six ranges**, 0.8 degree each.

Detector shape – continued



3

683.2,687,690.7

30.3,30.1,29.9

10,-26

4.0,6.3,7.4,9.0,10.7,12.3,13.1,13.6,13.9,14.0,
13.7,13.6,13.6,13.5,13.3,13.1,12.9,12.8,12.7,
12.0,11.1,9.4,7.2,5.3,4.0,3.3,3.0

- stopping powers
- number of equal subdivisions of energy used for interpolation (even number, maximum value 100)
- number of equal subdivisions of theta used for interpolation (even number, maximum value 100, with „-” sign if we introduce the $\varphi(\theta)$ dependence). Here: twenty six ranges, 0.8 degree each.
- total phi range for each cut (twenty seven points)