

PACMAN Workshop, June 2016

Error sources in dimensional metrology

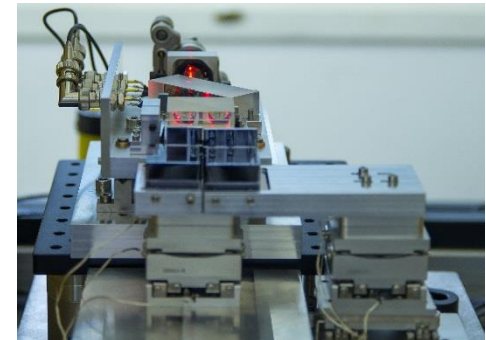
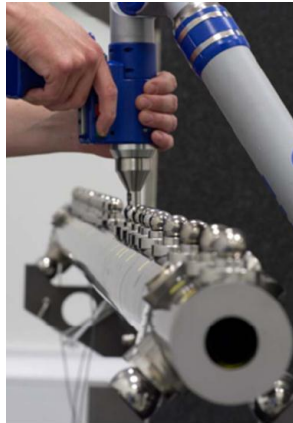
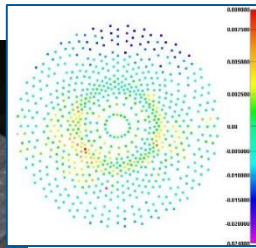
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Outline

- Dimensional metrology
- The Metrology Loop
- Error sources and mitigation

Dimensional Metrology

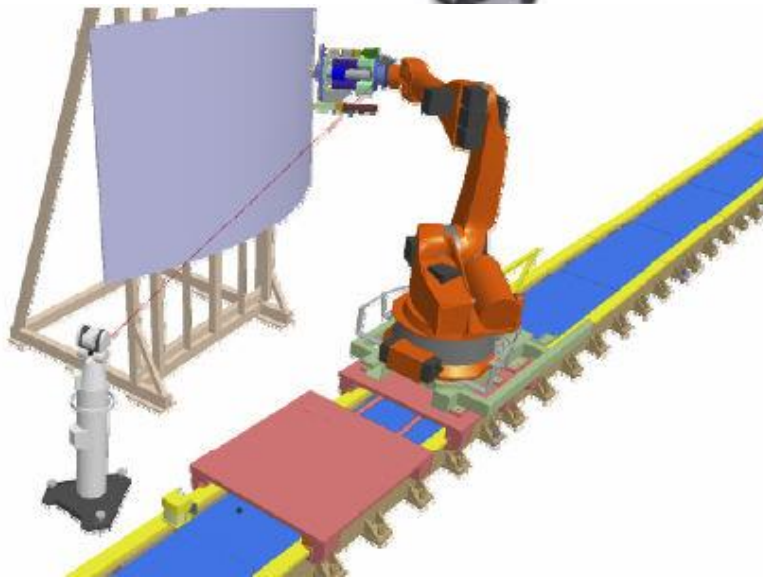
- 1D, 2D and 3D
- Contact or Non-contact
- Range based, angle based or a combination of both
- Scales from pm to ...



The Metrology Loop

- A metrology loop is the closed path containing all elements between the sensor and the part that affect the measurement.
- Often the metrology loop has elements in common with the structural or force loop.
- **Changes in the metrology loop** due to, for example, temperature change, vibration or structural forces, **are indistinguishable from changes in the dimension being measured.**

The Metrology Loop



Error Sources and Mitigation

- Thermal
- Refraction & Refractive index gradient
- Mechanical errors
- Geometric errors

Error Sources and Mitigation

■ Thermal effects

- One of the biggest potential sources of error in dimensional metrology!
- ISO 1: “*The standard reference temperature for geometrical product specification is fixed at 20 °C*”
- Dimensions measured at $T \neq 20 \text{ °C}$ must be corrected

$$L_{20} = L_T [1 - \alpha(T-20)]$$

α is coefficient of thermal expansion

e.g. $\alpha_{steel} = 12 \times 10^{-6} \text{ K}^{-1}$, $\alpha_{aluminium} = 23 \times 10^{-6} \text{ K}^{-1}$

- Thermal expansion affects the instrument too
 - Distorts the metrology loop

Error Sources and Mitigation

- Thermal effects *continued*
 - Mitigation
 - Use low CTE materials for critical parts of the metrology loop *e.g. Invar or Zerodur*
 - Minimise uncertainty in thermal expansion correction by controlling temperature close to 20 °C
 - Active environmental control
 - Local insulation
 - Avoid handling parts
 - Allow time for thermal stabilisation

Error Sources and Mitigation

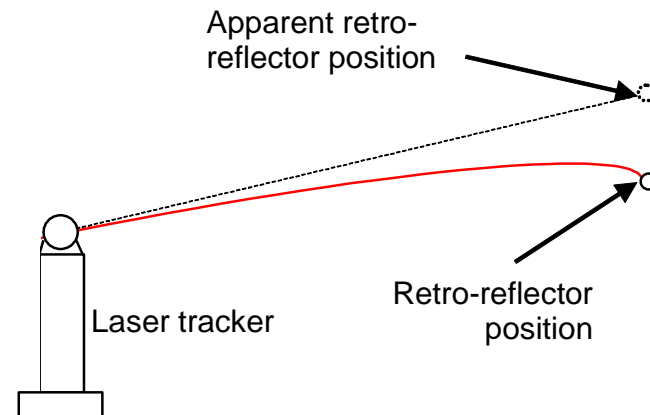
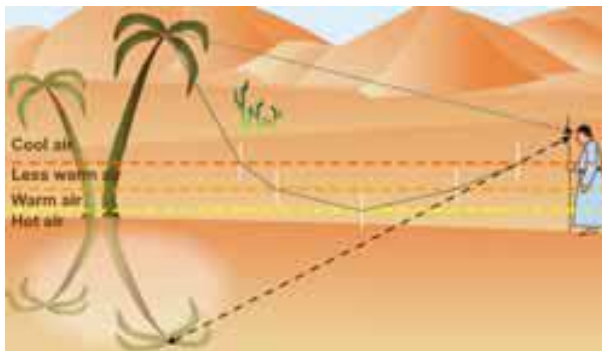
- Refractive index
 - Affects *optical length* measurements e.g. interferometers
 - Refractive index, n , determines speed of light in a medium, c' . So distances measured in terms of the speed of light must be corrected.

$$c' = c_0/n \quad c_0 = \text{speed of light in vacuum}$$

- n at standard temperature and pressure ~ 1.00027
- $dn/dT \sim -1 \times 10^{-6} \text{ K}^{-1}$
- $dn/dP \sim 2.7 \times 10^{-7} \text{ hPa}^{-1}$
- Can calculate n from air temperature and pressure readings using e.g. Edlen's formula

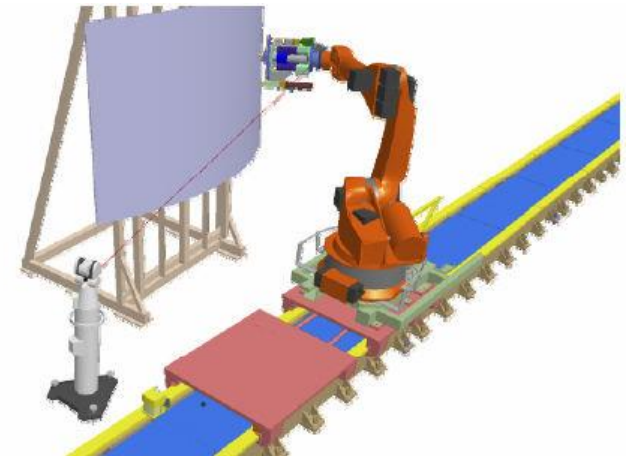
Error Sources and Mitigation

- Refractive index gradient
 - Gradient normal to direction of propagation of a beam bends the beam
 - This is how a mirage is formed!
 - Affects optical *angle* measurements e.g. laser tracker



Error Sources and Mitigation

- Mechanical - Stiffness of metrology loop
 - Instrument e.g. CMM structure
 - Instrument support e.g. laser tracker tripod
 - Part support/clamping
 - Isolate force loop from metrology loop



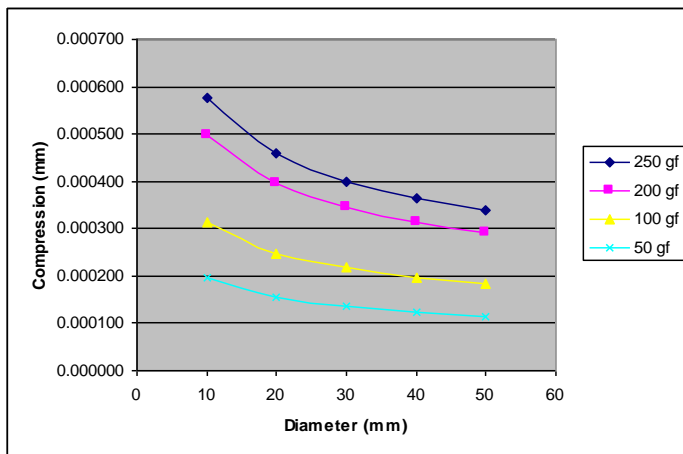
Error Sources and Mitigation

- Mechanical - Vibration induced the metrology loop
 - Eliminate/isolate source
 - Isolate metrology loop
 - Stiffen structure – high resonant frequency
 - Also air movement in optical metrology systems



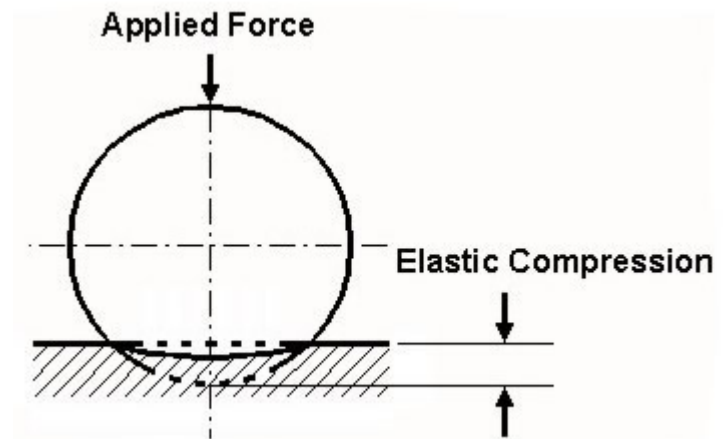
Error Sources and Mitigation

- Mechanical – elastic compression
 - Occurs whenever mechanical probing takes place
 - Depends on contact force
 - Geometry of component (e.g. flat, sphere, cylinder)
 - Component and probe materials
 - Type of contact (e.g. point, line)



Compression corrections for tungsten carbide spheres between flat steel anvils for various forces

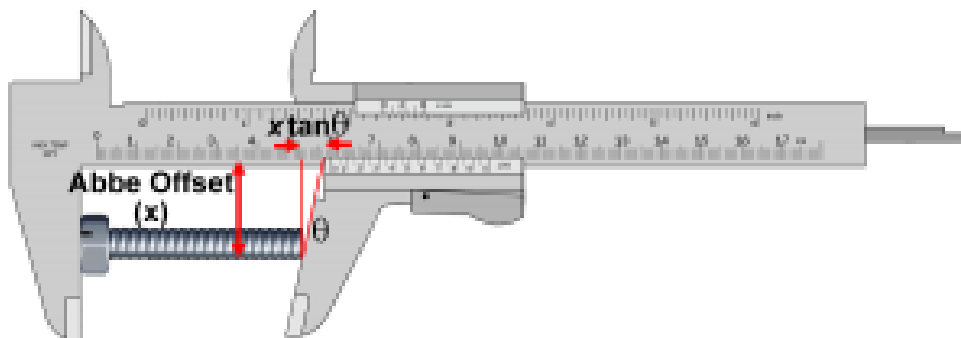
NPL GPG 80



<http://emtoolbox.nist.gov/Main/Main.asp>

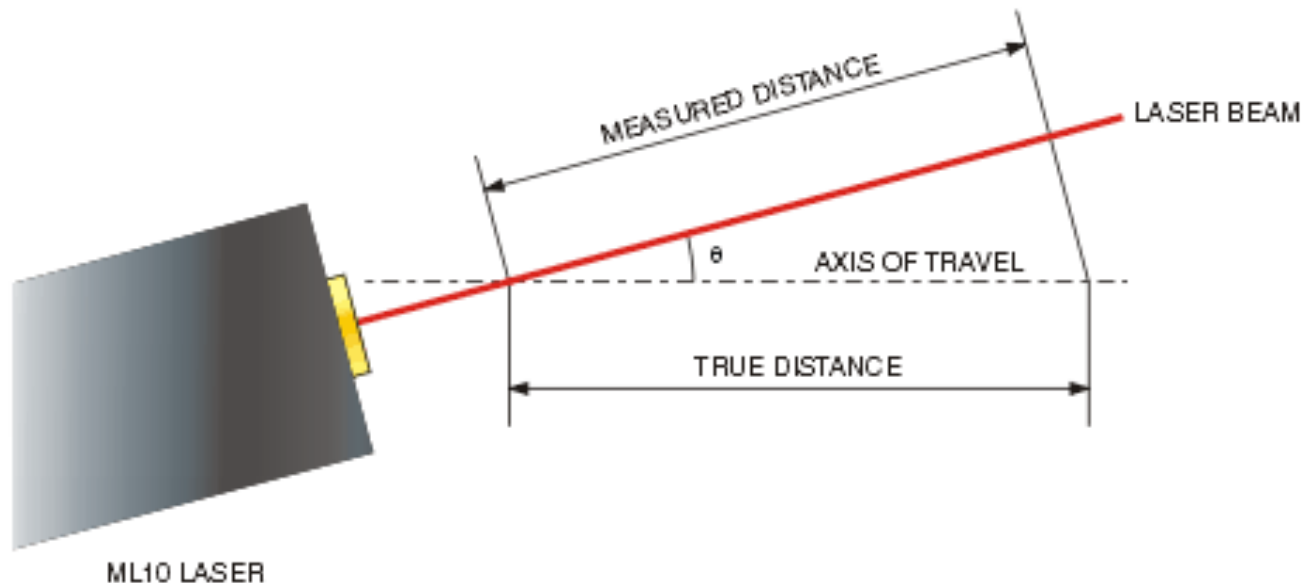
Error Sources and Mitigation

- Alignment - Abbe error
 - Measurement scale is not in line with the object being measured – Abbe offset, x .
 - Straightness of axis or sloppy fit of calliper causes angle between jaws, θ .
 - Eliminate by aligning scale coaxially with part, or compensate by measuring x and θ .



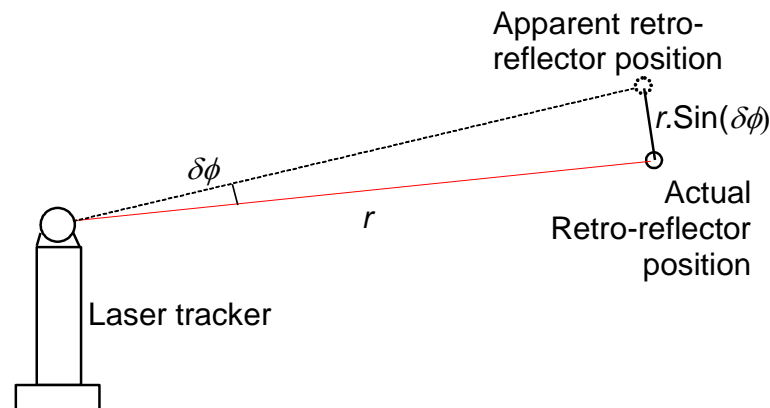
Error Sources and Mitigation

- Alignment - Cosine error
 - Angular misalignment, θ , between scale, or axis, and part.
 - Length error, $\Delta L = L(1 - \cos \theta)$.
 - Minimise by minimising θ .



Error Sources and Mitigation

- Alignment – Sine error
 - Occurs in angle-based coordinate metrology due to angle measurement error, $\delta\phi$.
 - Error proportional to range, r .
 - Reduce coordinate error by reducing $\delta\phi$ and/or r .
 - Eliminate by measuring coordinates in terms of range only.



Conclusion

- There are many sources of error in dimensional metrology
- Careful control of the metrology loop can help minimise or eliminate many sources of error

THANK YOU

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