

Higgs boson differential cross sections

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on behalf of the CMS and ATLAS collaborations



ETH Institute for
Particle Physics



CMS

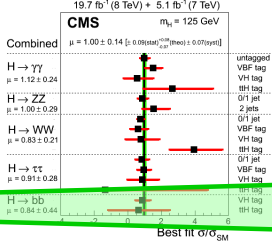
Why fiducial cross sections?



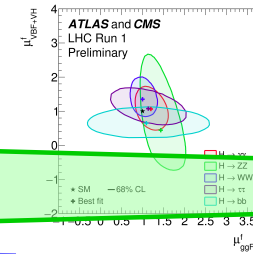
► **Experimental data** can be presented in many possible ways.

► Presentations can be classified according to different metrics: generality, power of the interpretation, longevity...

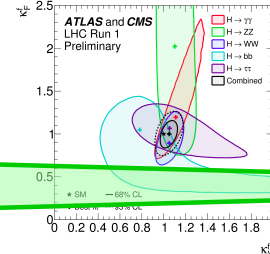
Per-channel signal strengths



“Unfolded” signal strengths



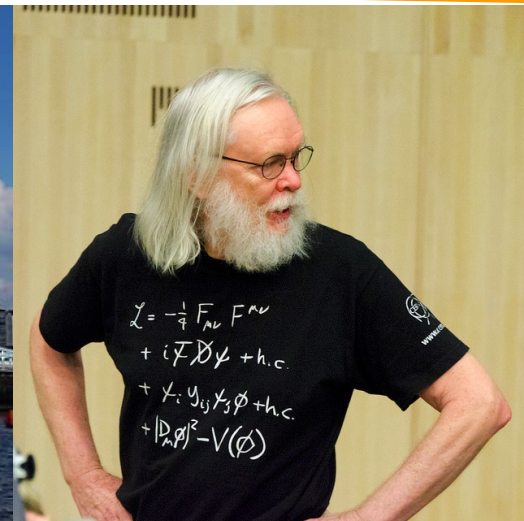
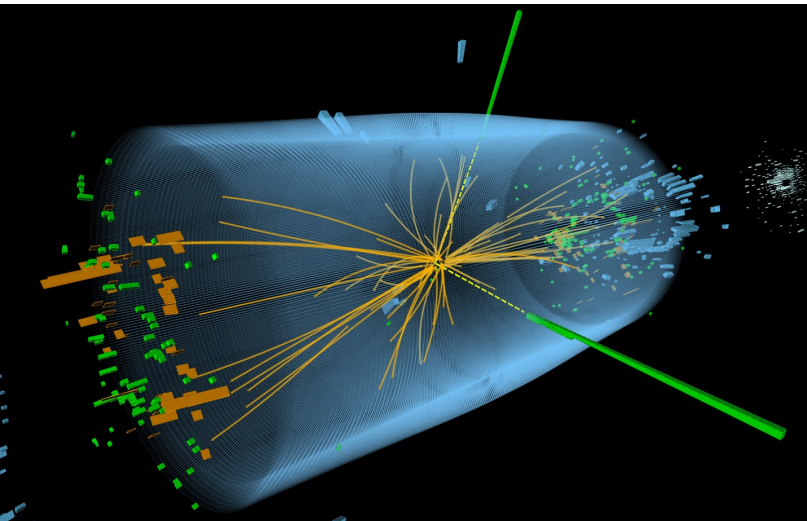
Coupling modifiers



Longevity

Generality

Interpretation



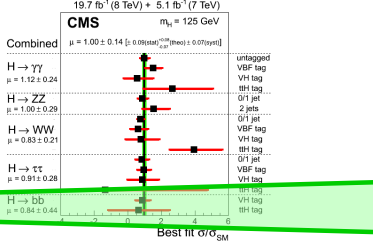
Why fiducial cross sections?



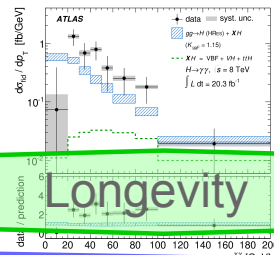
► **Experimental data** can be presented in many possible ways.

- Presentations can be classified according to different metrics: generality, power of the interpretation, longevity...
- **Differential cross sections** help maximizing **longevity** while preserving most of the power of the data.

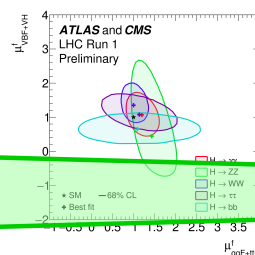
Per-channel signal strengths



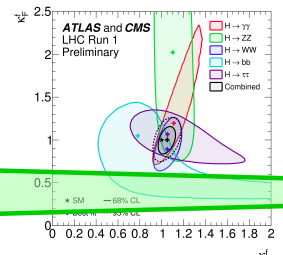
Fiducial cross sections



“Unfolded” signal strengths

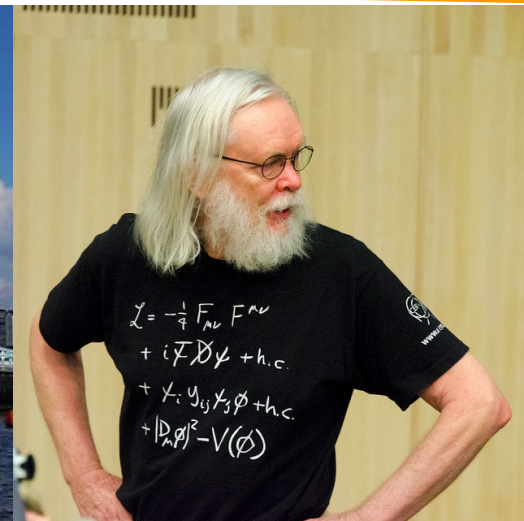
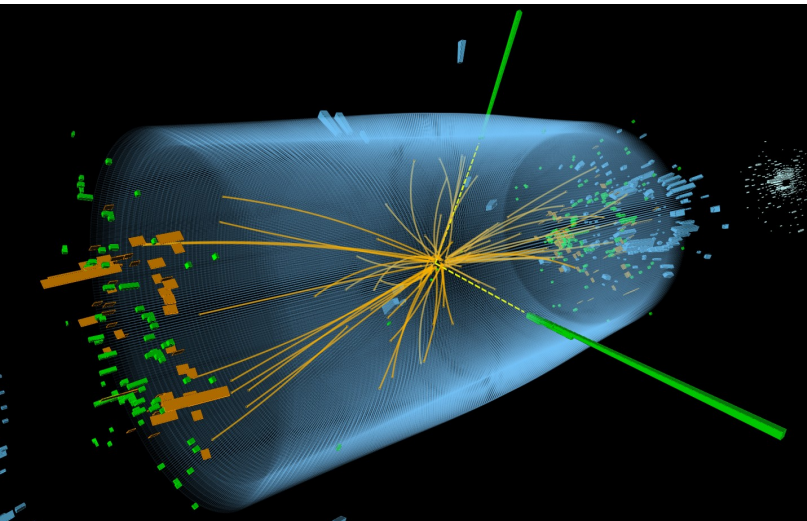


Coupling modifiers



Generality

Interpretation



Higgs differential cross sections: run 1 results



| | | |
|--|---|--------------------|
| JHEP09(2014)112 | Measurements of fiducial and differential cross sections for Higgs boson production in the diphoton decay channel at $\sqrt{s} = 8$ TeV with ATLAS | $\gamma\gamma$ |
| PLB 738 (2014) 234-253 | Fiducial and differential cross sections of Higgs boson production measured in the four-lepton decay channel in pp collisions at $\sqrt{s} = 8$ TeV with the ATLAS detector | ZZ |
| PRL 115 (2015) 091801 | Measurements of the Total and Differential Higgs Boson Production Cross Sections Combining the $H \rightarrow \gamma\gamma$ and $H \rightarrow ZZ^* \rightarrow 4\ell$ Decay Channels at $\sqrt{s} = 8$ TeV with the ATLAS Detector | $\gamma\gamma, ZZ$ |
| PLB 753 (2016) 69-85 | Constraints on non-Standard Model Higgs boson interactions in an effective Lagrangian using differential cross sections measured in the $H \rightarrow \gamma\gamma$ decay channel at $\sqrt{s} = 8$ TeV with the ATLAS detector | $\gamma\gamma$ |
| arXiv:1508.07819 (accepted by EPJC) | Measurement of differential cross sections for Higgs boson production in the diphoton decay channel in pp collisions at $\sqrt{s} = 8$ TeV | $\gamma\gamma$ |
| arXiv:1512.08377 | Measurement of differential and integrated fiducial cross sections for Higgs boson production in the four-lepton decay channel in pp collisions at $\sqrt{s} = 7$ and 8 TeV | ZZ |
| CMS-PAS-HIG-15-010 | Measurement of the transverse momentum spectrum of the Higgs boson produced in pp collisions at $\sqrt{s} = 8$ TeV using the $H \rightarrow WW$ decays | WW |





- ▶ Will show a personally biased selection of the available material.
 - ▶ Will put some more focus on how the results are obtained, rather than on the results themselves.

- ▶ Restrict presentation to total fiducial cross sections and Higgs p_T spectrum.
 - ▶ This does not exhaust the available measurements.
 - ▶ Few more distributions are in the extra material section, but please refer to the documentation above for more details.

Aren't signal strengths good enough?



▶ Signal strengths are one of the most powerful summary of Higgs data from LHC Run 1.

▶ They are also fairly general, especially within the Run 1 uncertainties.

▶ Generally defined as the ratio between the expected and observed signal cross sections.

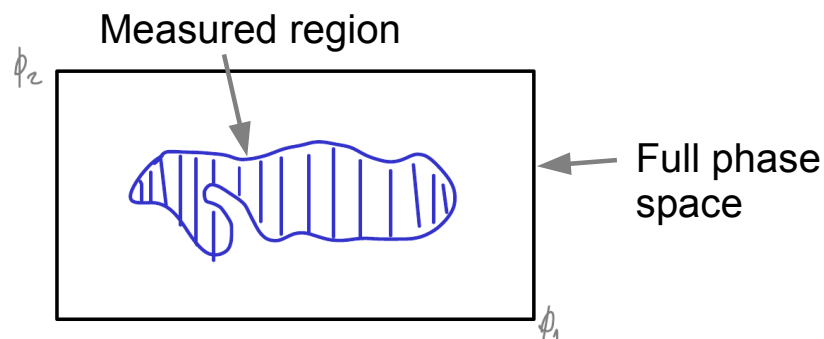
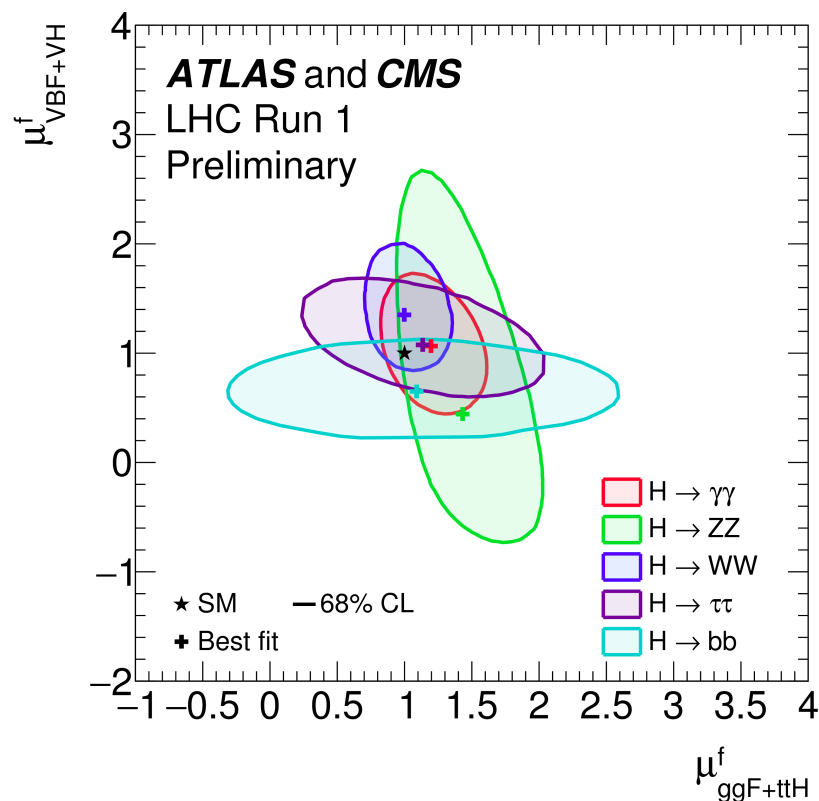
A more explicit definition is:

$$\mu = \frac{A \cdot \sigma}{A_{SM} \cdot \sigma_{SM}}$$

▶ Precision maximized by exploiting knowledge of signal characteristics.

▶ However, interpreting the signal strengths as cross sections requires a number of assumptions.

▶ Acceptance can have non trivial dependence on phase space variables.



(Fiducial) differential cross sections



Detector level observable

Particle level observable

$$\Delta N(O_j) = \sum_i [\Delta \sigma(O_i^*) \cdot R_{ij} \cdot L] + \Delta Bkg(O_j)$$

Fiducial cross-section

Includes acceptance definition

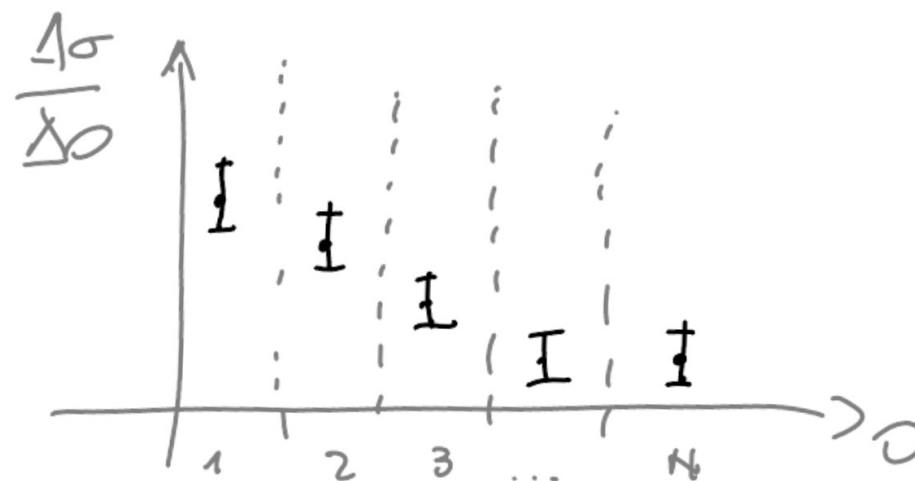
Detector response matrix

Accounts for efficiency and resolution effects

$$\Delta \sigma_i = \Delta \sigma_i(\lambda_1, \lambda_2, \dots, \lambda_N)$$

Theory degrees of freedom

Can be inferred from the fiducial cross sections



(Fiducial) differential cross sections



Detector level observable

Particle level observable

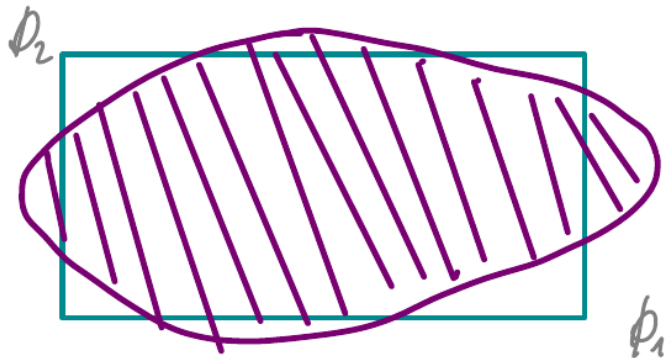
$$\Delta N(O_j) = \sum_i [\Delta \sigma(O_i^*) \cdot R_{ij} \cdot L] + \Delta Bkg(O_j)$$

Fiducial cross-section

Includes acceptance definition

Detector response matrix

Accounts for efficiency and resolution effects



► Fiducial cross sections measured in well defined phase space.

Theory degrees of freedom

Car ► Detector level selection brought as close as possible to particle level.

Detector level observable

Particle level observable

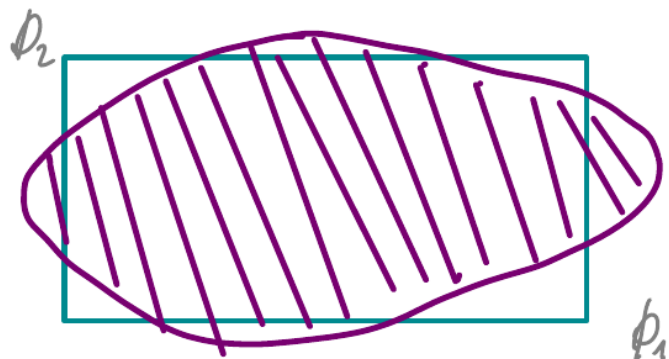
$$\Delta N(O_j) = \sum_i [\Delta \sigma(O_i^*) \cdot R_{ij} \cdot L] + \Delta Bkg(O_j)$$

Fiducial cross-section

Includes acceptance definition

Detector response matrix

Accounts for efficiency and resolution effects



► Fiducial cross sections measured in well defined phase space.

Theory degrees of freedom

Can ► Detector level selection brought as close as possible to particle level.

► Can tune selection to make measured cross sections as theory independent as possible.

$$\Delta \sigma^{SM} \sim \Delta \sigma(\lambda_{1,\dots}, \lambda_N)$$

(Fiducial) differential cross sections



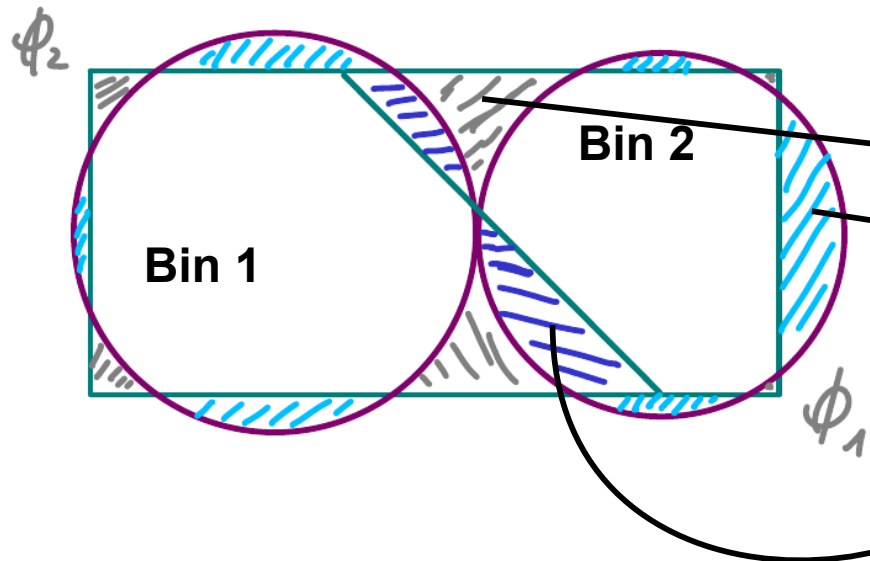
Detector level observable

Particle level observable

$$\Delta N(O_j) = \sum_i [\Delta \sigma(O_i^*) \cdot R_{ij} \cdot L] + \Delta Bkg(O_j)$$

Fiducial cross-section
Includes acceptance definition

Detector response matrix
Accounts for efficiency and resolution effects



► Measurement ↔ response matrix.

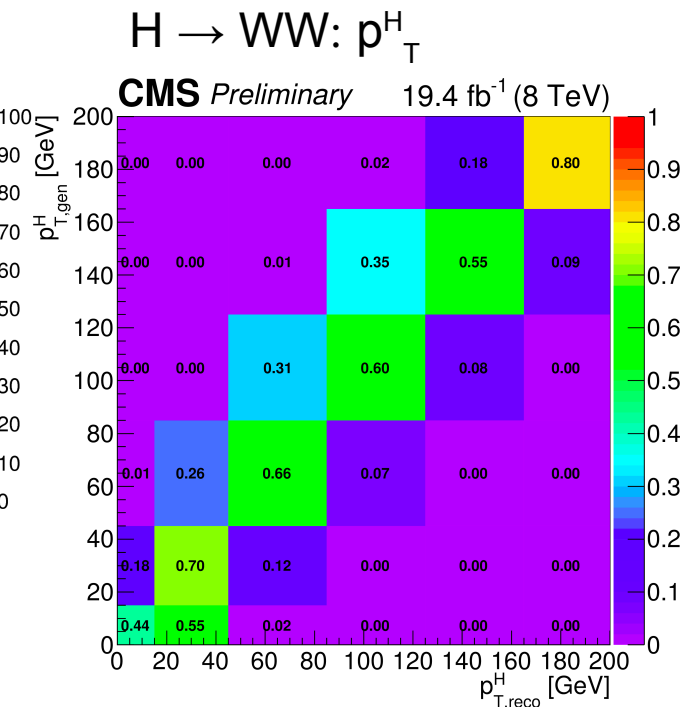
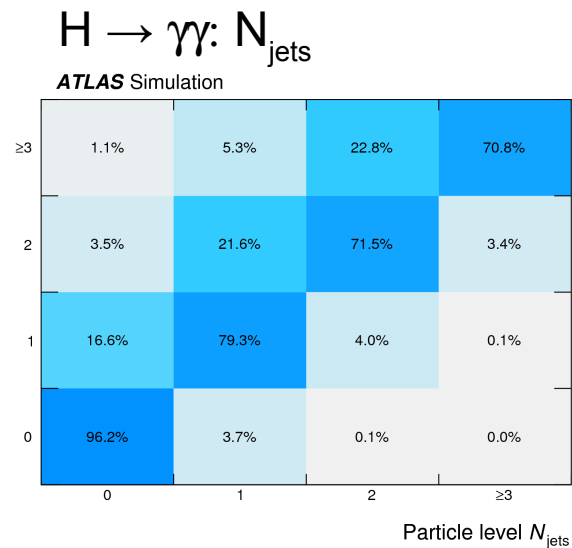
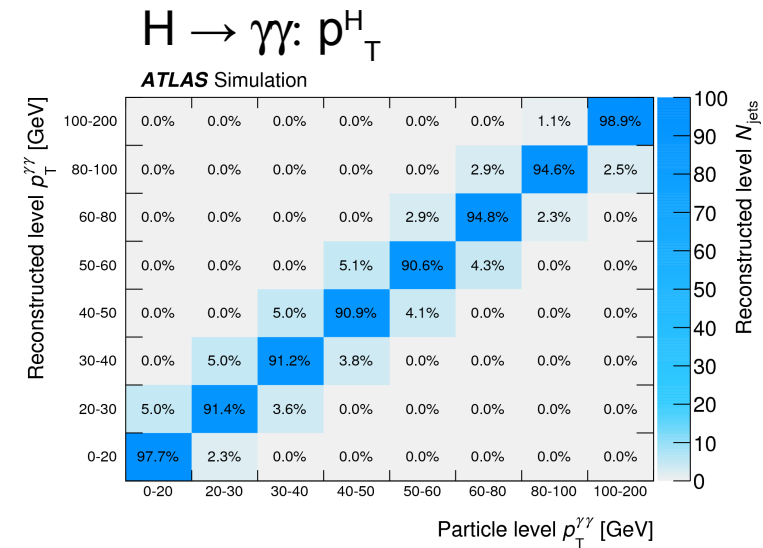
► **Efficiency.**

► Contamination from **out-of-acceptance signal.**

► Bin-to-bin **migration.**

Example of detector response matrixes

- ▶ For variables involving only high resolution objects (i.e. leptons and photons) response matrixes are almost diagonal.
- ▶ If low-resolution quantities (e.g. jets and missing energies) large non diagonal terms are present.



- ▶ Techniques used to correct the measured cross sections to particle levels go under the name of unfolding.
 - ▶ Problem is not completely well defined as some assumptions on the underlying distributions are needed in the procedure.
- ▶ Several methods on the market.
 - ▶ Problem can be phrased in terms of minimizing the following quantity.

$$\chi^2(\Delta\sigma(O_1^*) \dots \Delta\sigma(O_m^*) | \Delta\sigma(O_0)) = \sum_{j=1}^m \overbrace{\frac{\sum_{i=0}^m (LR_{ij} \Delta\sigma(O_i^*) - \Delta N(O_j))^2}{\sigma_j^2}}^{\text{Measured event yields}} + \underbrace{\tau \sum_{i=1}^m \sum_{j=1}^m \Delta\sigma(O_i^*) K_{ij} \Delta\sigma(O_j^*)}_{\text{Regularization term.}}$$

Out-of-acceptance signal.
Not measurable from data.

Regularization term.
Dumps fluctuations in measured cross sections, at the biasing the measurement.

► Different choices taken by different analyses.

- ATLAS $H \rightarrow \gamma\gamma$ and $H \rightarrow ZZ$: bin-by-bin correction.

Known to be pathological for very non diagonal response matrixes.

$$R_{ij} \rightarrow c_{ij} = \delta_{ij} \cdot \sum_{\tau=0} R_{ik} \Delta \sigma_{MC}(O_k^*)$$

- CMS $H \rightarrow \gamma\gamma$ and $H \rightarrow ZZ$: un-regularized unfolding using likelihood function instead of χ^2 .

Unbiased result, regularization can be applied a-posteriori.

$$\chi^2(\Delta \sigma) \rightarrow -2 \log L(\Delta \sigma)$$
$$\tau=0$$

- CMS $H \rightarrow WW$: regularized SVD unfolding.

Regularization term needed due to large non diagonal elements in response matrix.

▶ **Simple** final state, kinematics can be measured with **high resolution**.

▶ Good precision can be achieved.

▶ Fiducial phase space definition very similar between ATLAS and CMS.

| | ATLAS | CMS |
|--|-------|-------|
| $ \eta $ | <2.37 | <2.5 |
| p_T^1/m | <0.35 | <1/3 |
| p_T^2/m | <0.25 | <1/4 |
| $\Sigma_{\Delta R < 0.3} E_T^{\text{had}}$ | 14GeV | 10GeV |

In the case of CMS, events are categorized according to resolution.

▶ Measured **many observables** at $\sqrt{s}=8\text{TeV}$.

▶ Diphoton kinematics as well as to additional activity.

▶ **Systematic** uncertainties **negligible** wrt statistical ones.

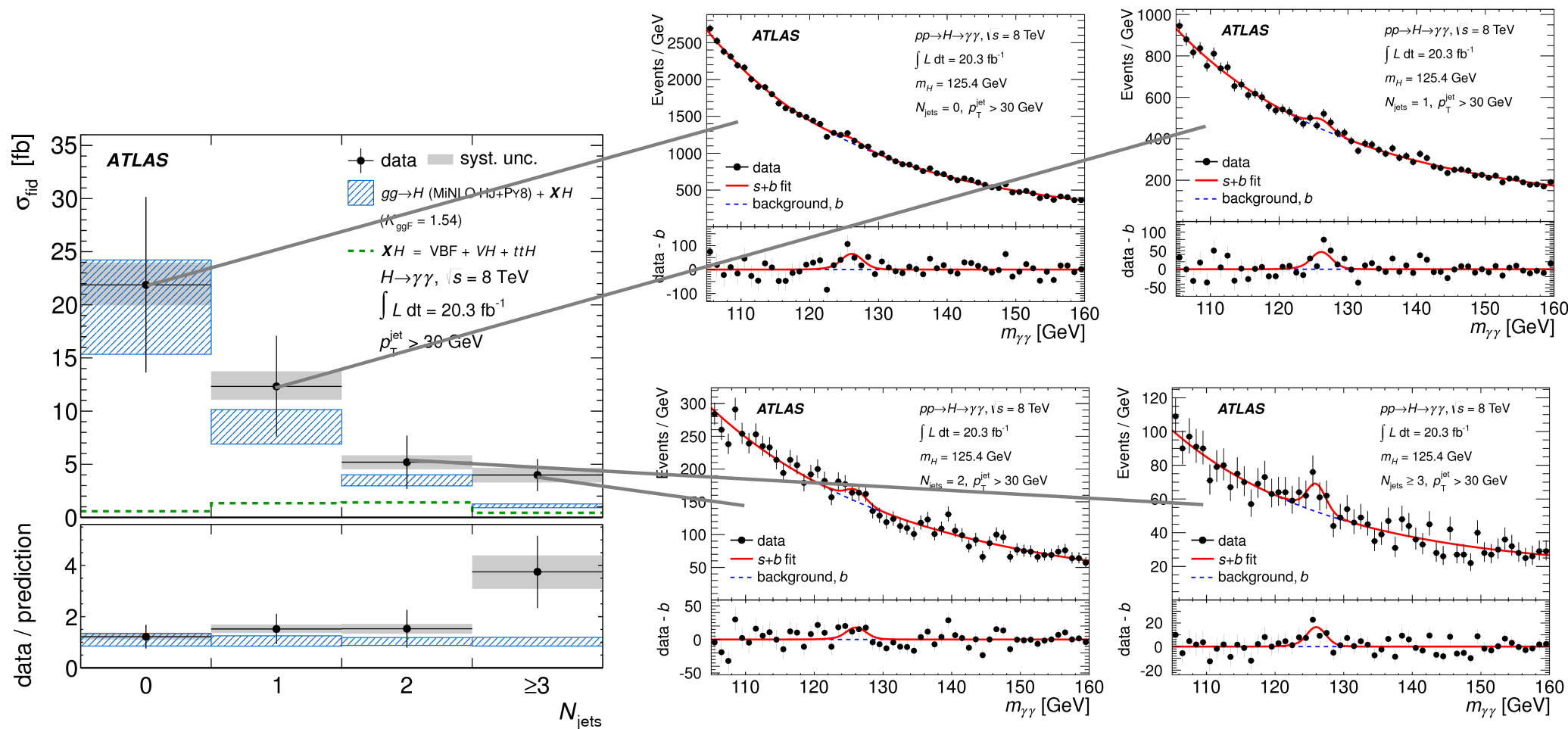
▶ It will still be the case in Run 2.

H \rightarrow $\gamma\gamma$: signal extraction



► Signal extracted from **fit** to the diphoton **invariant mass** spectrum.

► Different unfolding techniques used by CMS and ATLAS.





- ▶ Fiducial cross sections measured with an **uncertainty** of roughly **1/3 of the SM prediction**.

- ▶ Uncertainties are 10-15% larger than those on the (8TeV) signal strengths.

| $\sigma_{\text{fid}}(\text{pp} \rightarrow \text{H} \rightarrow \gamma\gamma)$ [fb] | Data | Theory (LHCHXSWG+ HRes,POWHEG,PYTHIA) |
|---|--|--|
| ATLAS (8TeV) | 43.2 \pm 9.4(stat) $^{+3.2}_{-2.9}$ (syst) \pm 1.2(lumi) | 30.5 \pm 3.3 |
| CMS (8TeV) | 32 \pm 10(stat) \pm 3(syst) | 31 $^{+3}_{-4}$ |

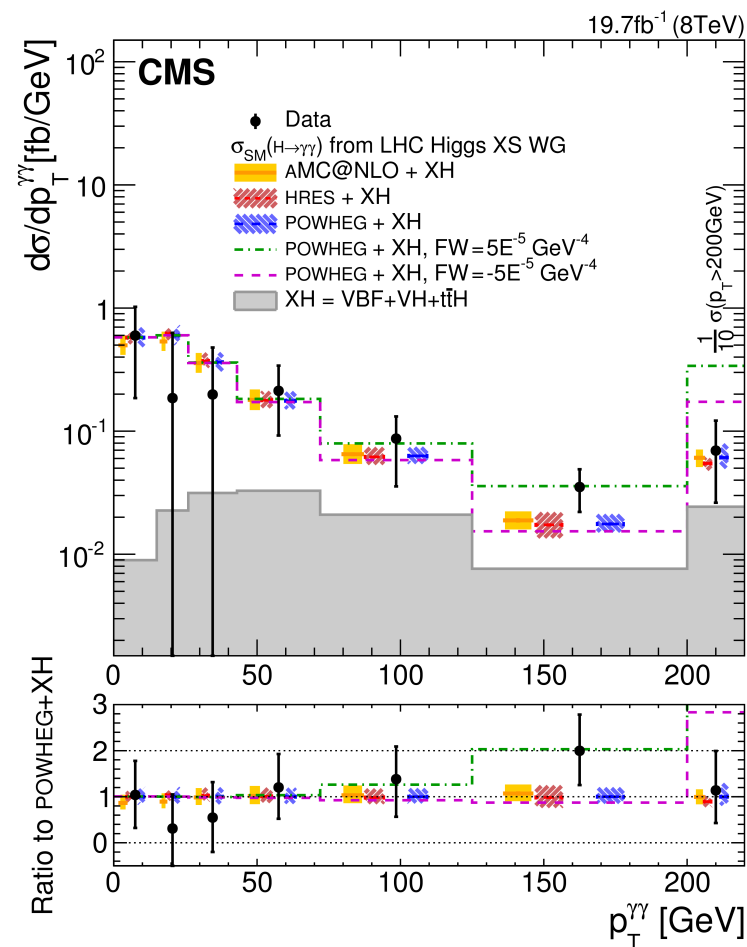
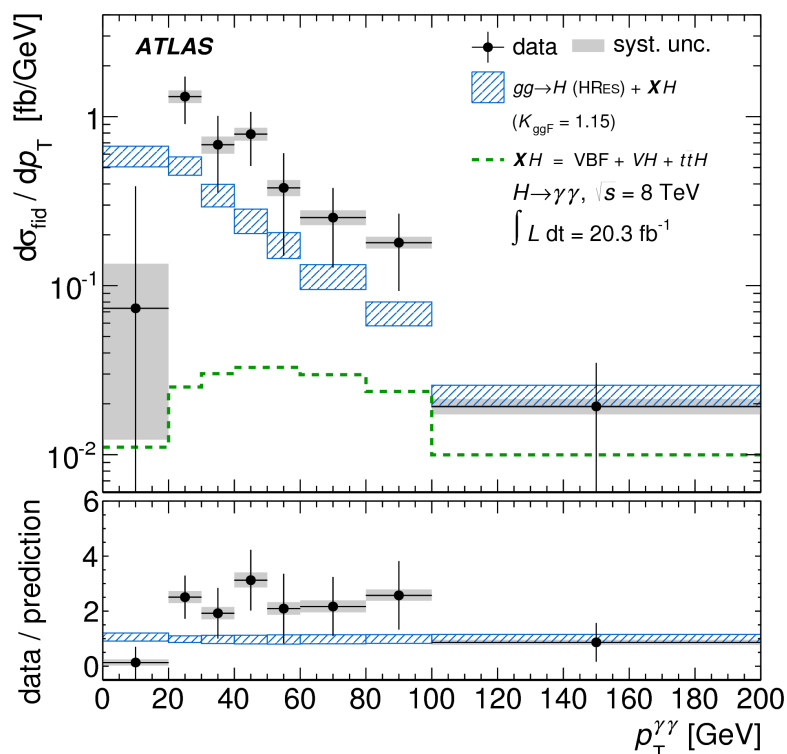
- ▶ Measurements well in agreement with SM predictions.

H $\rightarrow \gamma\gamma$: Measured p_T spectra



- Uncertainties on single bins scale as total uncertainties.
 - ATLAS: 8 bins \rightarrow unc. on average $\sim 85\%$ of SM prediction.
 - CMS: 6 bins (plus overflow) \rightarrow unc. $\sim 75\%$ of SM prediction.
- Spectra in agreement with SM expectations.

ATLAS $p(\chi^2) \sim 0.10$



- ▶ Extremely **clean** final state.

- ▶ Low event yield.
- ▶ Very low background.

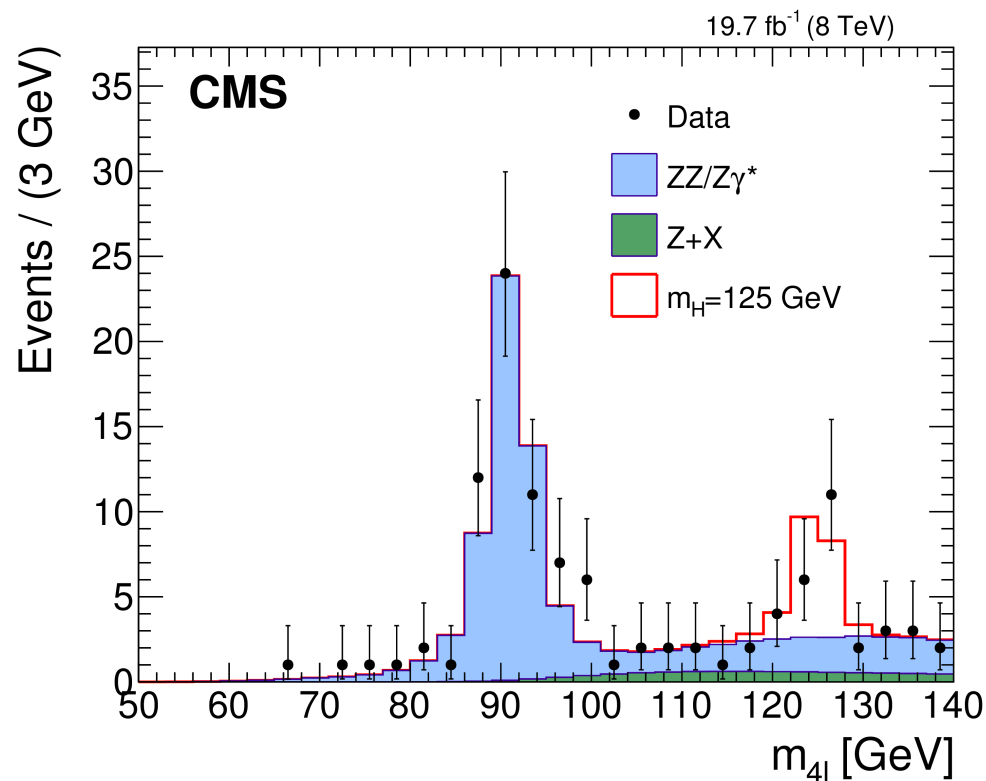
- ▶ Definition of fiducial phase space more complicated than H \rightarrow $\gamma\gamma$ (see next slide).

- ▶ Signal extraction:

- ▶ ATLAS: Event counting in m_{4l} window (after background subtraction)
- ▶ CMS: S+B fit to m_{4l} .

- ▶ Worse precision than H \rightarrow $\gamma\gamma$.

- ▶ **Many observables** measured, but using **wider binning**.



H → 4l: fiducial phase space definition



CMS

| Requirements for the H → 4l fiducial phase space | |
|---|----------------------------------|
| Lepton kinematics and isolation | |
| Leading lepton p_T | $p_T > 20$ GeV |
| Sub-leading lepton p_T | $p_T > 10$ GeV |
| Additional electrons (muons) p_T | $p_T > 7$ (5) GeV |
| Pseudorapidity of electrons (muons) | $ \eta < 2.5$ (2.4) |
| Sum of scalar p_T of all stable particles within $\Delta R < 0.4$ from lepton | $< 0.4 p_T$ |
| Event topology | |
| Existence of at least two SFOS lepton pairs, where leptons satisfy criteria above | |
| Inv. mass of the Z_1 candidate | $40 < m(Z_1) < 120$ GeV |
| Inv. mass of the Z_2 candidate | $12 < m(Z_2) < 120$ GeV |
| Distance between selected four leptons | $\Delta R(\ell_i \ell_j) > 0.02$ |
| Inv. mass of any opposite-sign lepton pair | $m(\ell_i^+ \ell_j^-) > 4$ GeV |
| Inv. mass of the selected four leptons | $105 < m_{4\ell} < 140$ GeV |

ATLAS

| | |
|--------------------|--|
| Lepton selection | |
| Muons: | $p_T > 6$ GeV, $ \eta < 2.7$ |
| Electrons: | $p_T > 7$ GeV, $ \eta < 2.47$ |
| Lepton pairing | |
| Leading pair: | SFOS lepton pair with smallest $ m_Z - m_{\ell\ell} $ |
| Subleading pair: | Remaining SFOS lepton pair with smallest $ m_Z - m_{\ell\ell} $ |
| Event selection | |
| Lepton kinematics: | $p_T > 20, 15, 10$ GeV |
| Mass requirements: | $50 < m_{12} < 106$ GeV, $12 < m_{34} < 115$ GeV |
| Lepton separation: | $\Delta R(\ell_i, \ell_j) > 0.1$ (0.2) for same- (different-) flavour leptons |
| J/ψ veto: | $m(\ell_i, \ell_j) > 5$ GeV for all SFOS lepton pairs |
| Mass window: | $118 < m_{4\ell} < 129$ GeV |

▶ Similar definitions for both experiments.

▶ In the case of CMS, lepton isolation required as part of phase space definition.
Minimizes model dependence.

▶ Leptons taken before FSR in both cases.
ATLAS checked that differences wrt dressed leptons are negligible.



- ▶ Fiducial cross sections measured with an **uncertainty** of roughly **35-40% of the SM prediction**.

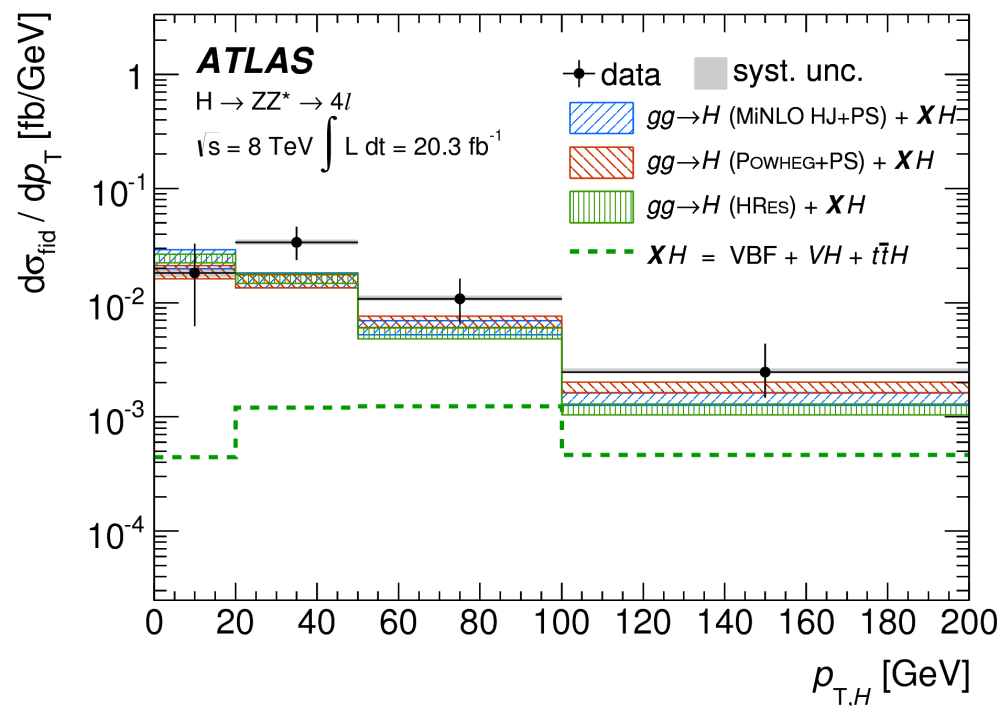
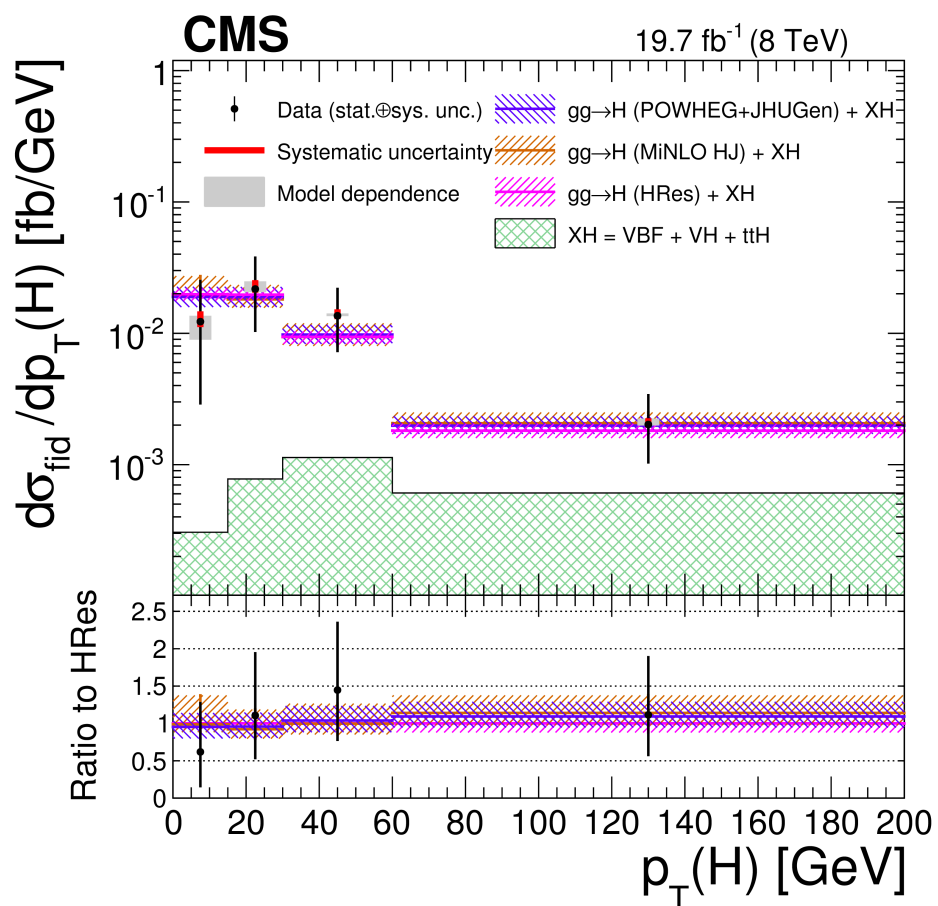
| $\sigma_{\text{fid}}(\text{pp} \rightarrow \text{H} \rightarrow 4\text{l})$ [fb] | Data | Theory (LHCHXSWG+ HRes,POWHEG,PYTHIA) |
|--|--|--|
| ATLAS (8TeV) | $2.11^{+0.53}_{-0.47}(\text{stat}) \pm 0.08(\text{syst})$ | 1.3 ± 0.13 |
| CMS (8TeV) | $1.11^{+0.41}_{-0.35}(\text{stat})^{+0.14}_{-0.10}(\text{syst})$ | 1.15 ± 0.12 |
| CMS (7TeV) | $0.54^{+0.67}_{-0.44}(\text{stat})^{+0.21}_{-0.06}(\text{syst})$ | 0.93 ± 0.10 |

- ▶ Measurements in agreement with SM predictions.

H → 4l: Measured p_T spectra



- ▶ Only four bins measured.
- ▶ No significant deviations observed.



- ▶ Analysis limited to the measurement of the Higgs candidate p_T and of the fiducial cross section.
 - ▶ Significant re-optimization of the analysis compared to the search.
 - ▶ Replace jet veto with a much looser b-jet veto.
 - ▶ Loosened selection cuts to reduce gap between reconstruction and generation level.

| Kinematic requirements for the $H \rightarrow W^+W^-$ fiducial phase space | |
|--|---|
| Leading lepton p_T | $p_T > 20$ GeV |
| Sub-leading lepton p_T | $p_T > 10$ GeV |
| Pseudorapidity of electrons and muons | $ \eta < 2.5$ |
| Invariant mass of the two leptons | $m_{\ell\ell} > 12$ GeV |
| Transverse momentum of the lepton pair | $p_T^{\ell\ell} > 30$ GeV |
| Invariant mass of the leptonic system in the transverse plane | $m_T^{\ell\ell E_T^{\text{miss}}} > 50$ GeV |
| No E_T^{miss} cut applied | |

- ▶ Fiducial phase space defined as:

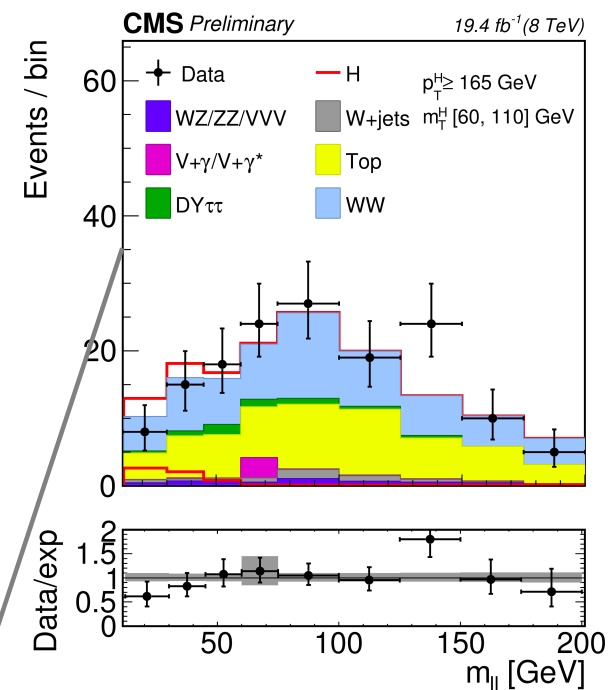
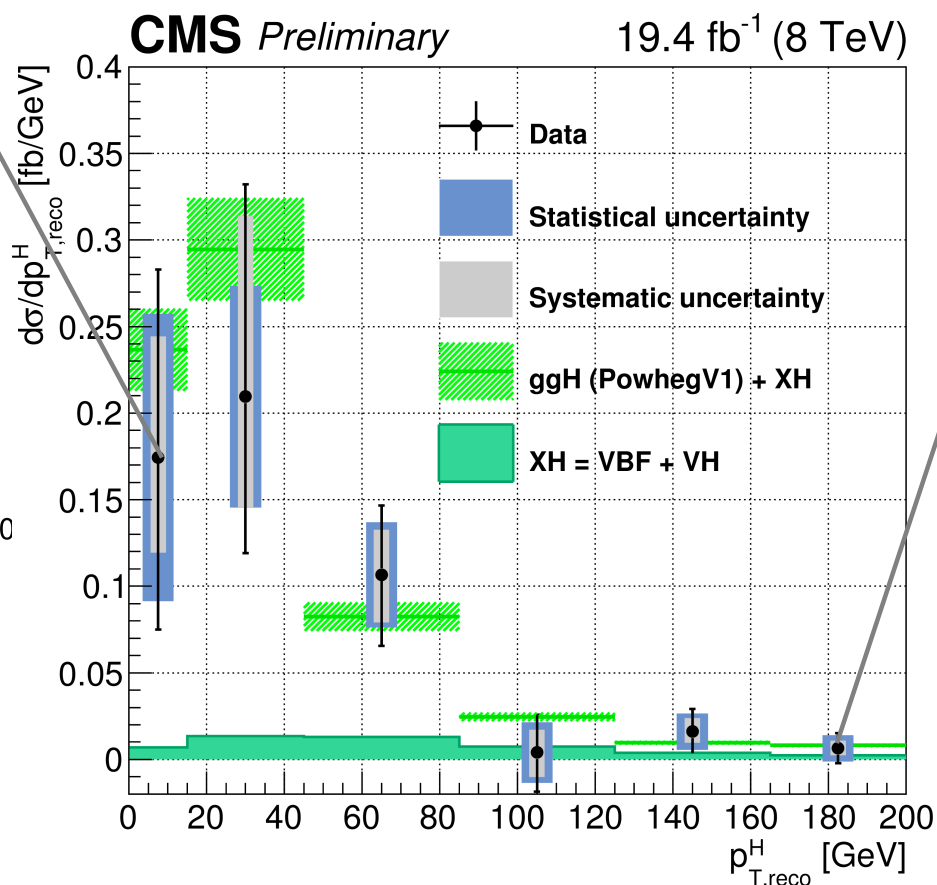
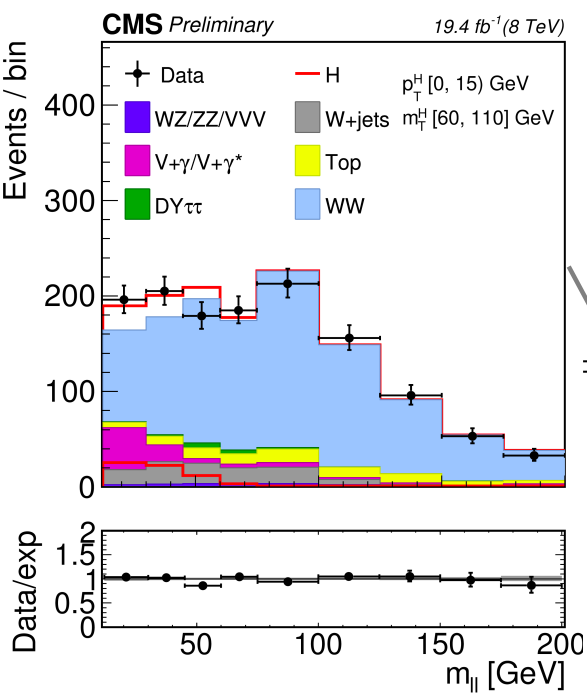
- ▶ Higgs candidate p_T reconstructed as:
$$\vec{p}_T^H = \vec{p}_T^{\ell\ell} + \vec{E}_T^{\text{miss}}$$

- ▶ Use of missing energy has large impact on resolution.
 - ▶ Measurement crucially depends on unfolding (and regularization).
- ▶ Systematic uncertainties are comparable to statistical uncertainties.

H → WW (2l2ν)

► Signal extracted from template fit in 2D ($m_{ll}, m_{T}^{ll, MET}$).

- Background shapes obtained from MC
- Normalizations constrained using data.



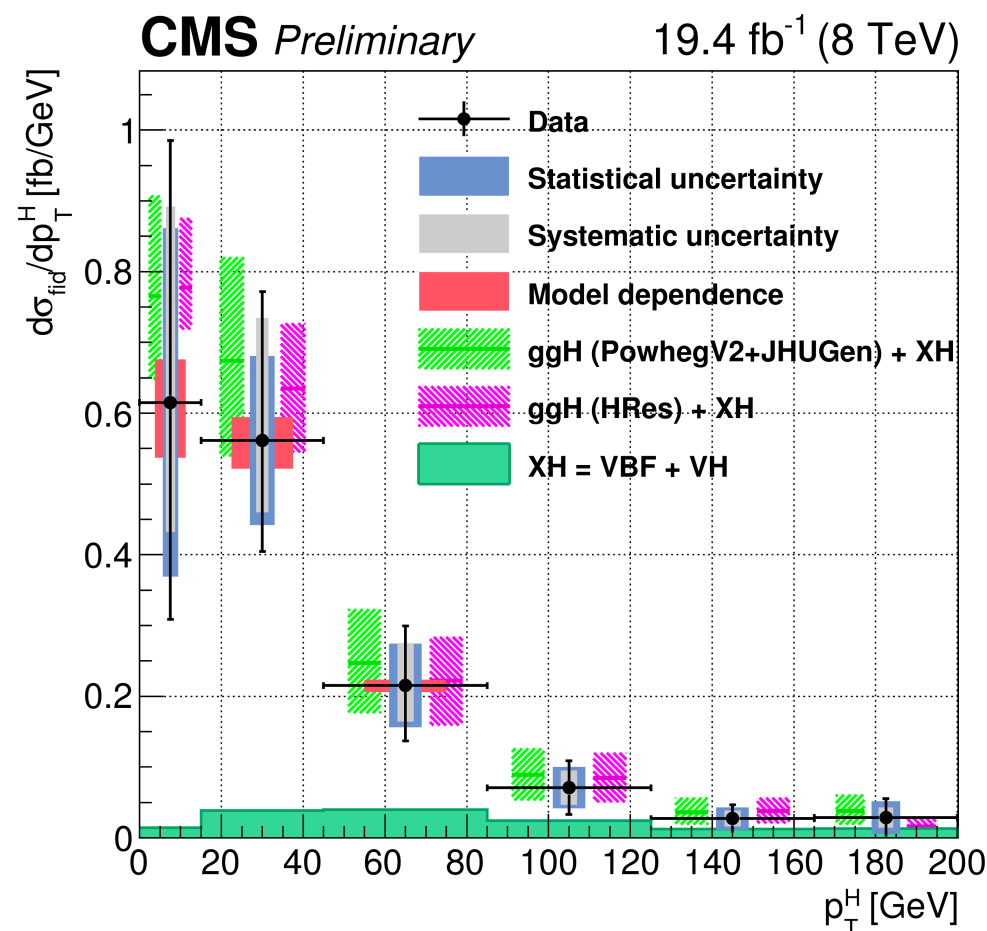
► Fiducial cross section.

- **Uncertainty ~25% of SM prediction.**
Systematic uncertainty of the same order of the statistical one.

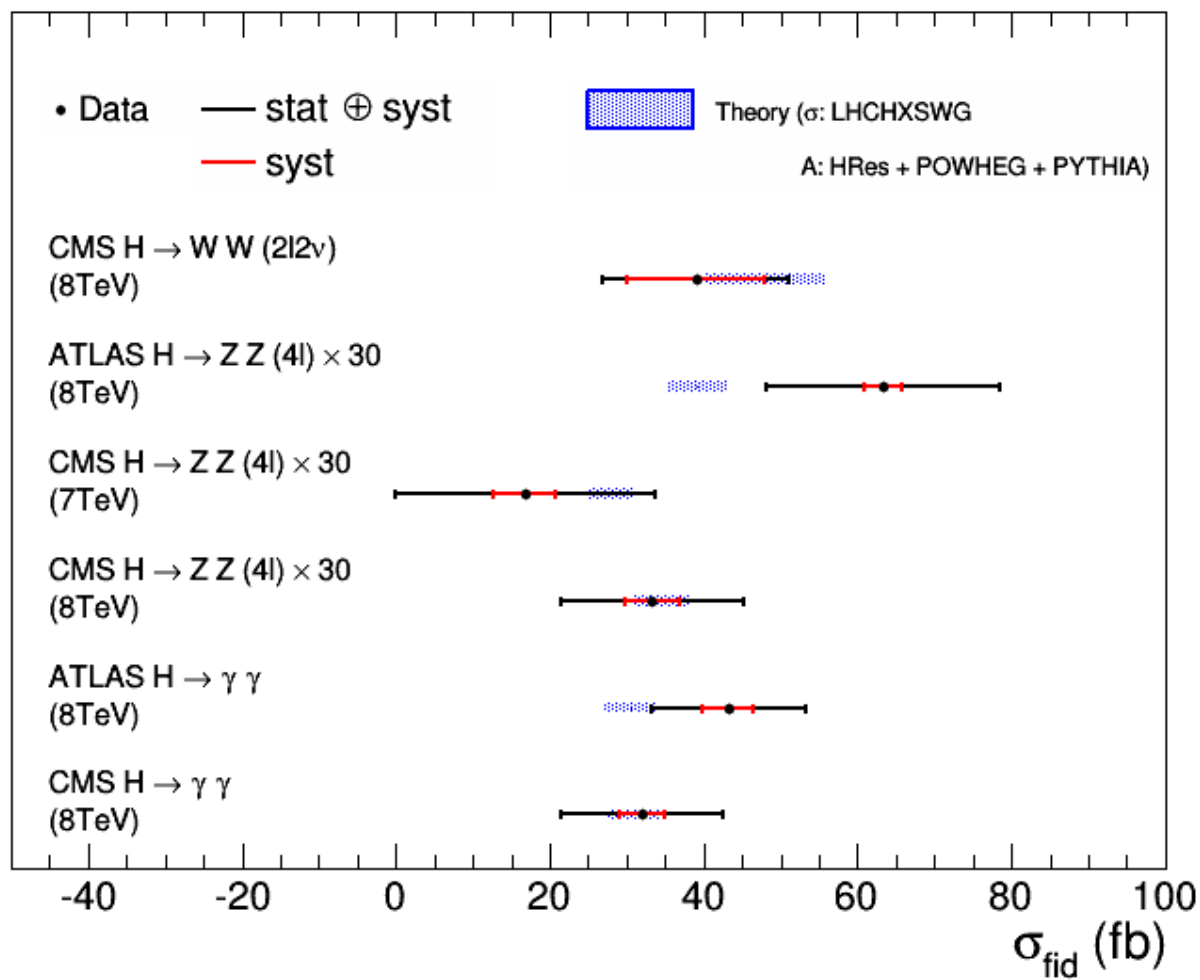
► Measured p_T spectrum in agreement with expectations.

- Note: large bin-to-bin correlations.

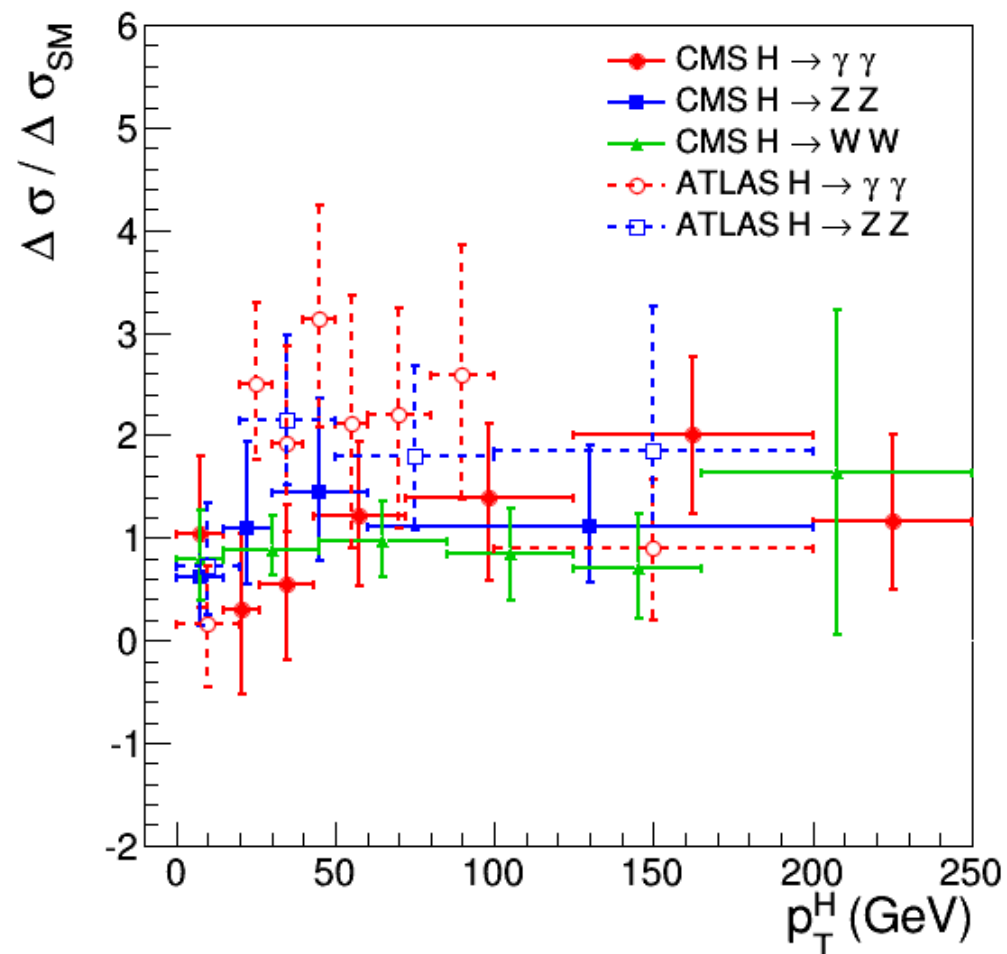
| Data | Theory (LHCHXSWG+POWHEG,PYTHIA) |
|---------------------------|------------------------------------|
| 39 ± 8(stat) ± 9(syst) fb | 48 ± 8 fb |



Fiducial cross sections: summary



- ▶ To compare all the available measurement, divide measured cross sections by common reference.
 - ▶ This is very close to a differential signal strength.
- ▶ Taking into account all measurements and using 6-7 bins could constrain shape to $\sim 35\%$.
 - ▶ By the end of Run 2 expect to have measurement at the level of 10%.

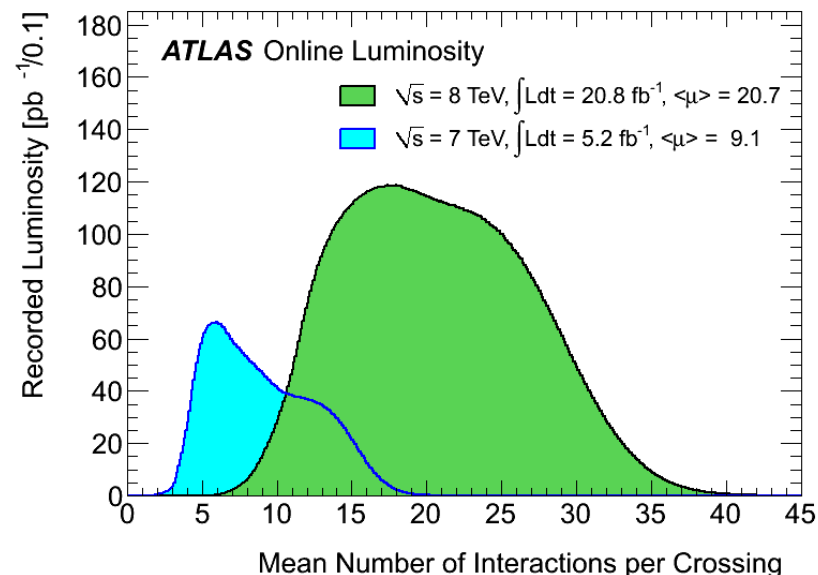
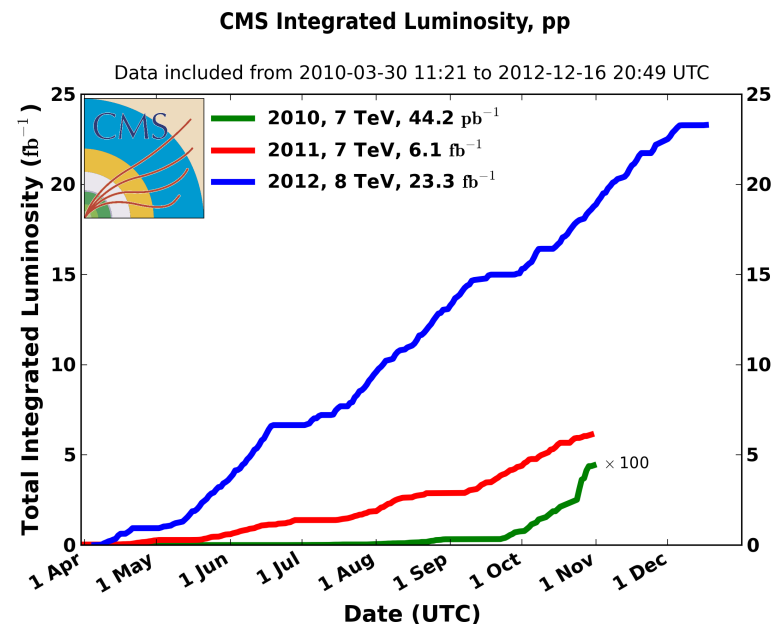




- ▶ Measuring fiducial and differential cross sections for Higgs production is of great importance.
 - ▶ Test Standard Model predictions in well defined phase space.
 - ▶ Ensure long term usability of LHC data.
- ▶ First measurement of fiducial cross sections performed by CMS and ATLAS using LHC Run 1 data.
 - ▶ Using bosonic decay channels.
 - ▶ Measurements are in most cases statistically-limited.
 - ▶ No significant deviations from expectations observed so far.
- ▶ Importance of such measurements will grow as the LHC delivers more data in Run 2.



- ▶ Excellent performance of the LHC machine throughout the Run 1.
- ▶ Also excellent performance of the CMS and ATLAS detectors
 - ▶ ~90% of the delivered data available for offline analysis.
- ▶ Available dataset:
 - ▶ $\sim 5\text{fb}^{-1} \sqrt{s}=7\text{TeV} + \sim 20\text{fb}^{-1} \sqrt{s}=8\text{TeV}$
- ▶ Challenging pile-up conditions.
 - ▶ Up to 30 average interactions per bunch-crossing.
 - ▶ Ingenious ideas needed to keep detector performances.

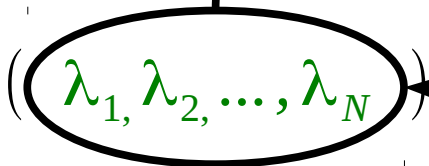


“Per-category signal strength”

$$N^{cat} = \mu^{cat} \cdot \sum_{p,d} \left[\underbrace{(\epsilon \cdot A^{SM})_{pd}^{cat}}_{\text{Theory prediction}} \cdot \underbrace{\sigma_p^{SM} \cdot BR_d^{SM}}_{\text{Theory prediction}} \cdot L \right] + Bkg^{cat}$$

Measured

$$\mu^{cat} = \mu^{cat}(\lambda_1, \lambda_2, \dots, \lambda_N)$$



Theory degrees of freedom

Statistical model

Inference

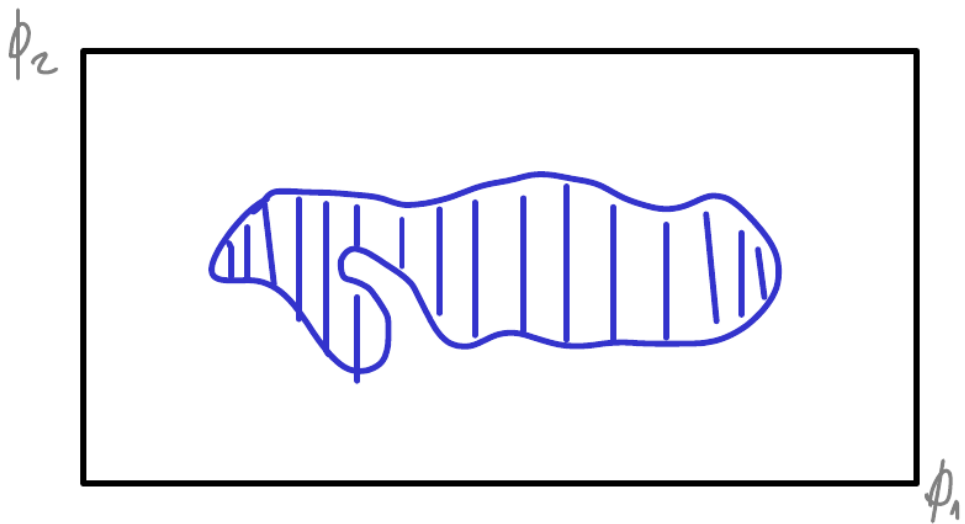
$$q(\mu) = -\ln \left[\frac{\mathcal{L}(\text{data}|\mu; \hat{\theta}_\mu)}{\mathcal{L}(\text{data}|\hat{\mu}; \hat{\theta})} \right]$$

“Per-category signal strength”

$$N^{cat} = \mu^{cat} \cdot \sum_{p,d} \left[(\epsilon \cdot A_{pd}^{SM})^{cat} \cdot \sigma_p^{SM} \cdot BR_d^{SM} \cdot L \right] + Bkg^{cat}$$

Theory prediction

Measured



► Acceptance can have complicated shape.

► Meaning of the signal strength not immediate.

► Relies on state-of-the-art theoretical predictions.

$$q(\mu) = -\ln \left[\frac{\mathcal{L}(\text{data}|\mu; \hat{\theta}_\mu)}{\mathcal{L}(\text{data}|\hat{\mu}; \hat{\theta})} \right]$$

“Per-category signal strength”

$$N^{cat} = \mu^{cat} \cdot \sum_{p,d} \left[(\epsilon \cdot A_{pd}^{SM})^{cat} \cdot \sigma_p^{SM} \cdot BR_d^{SM} \cdot L \right] + Bkg^{cat}$$

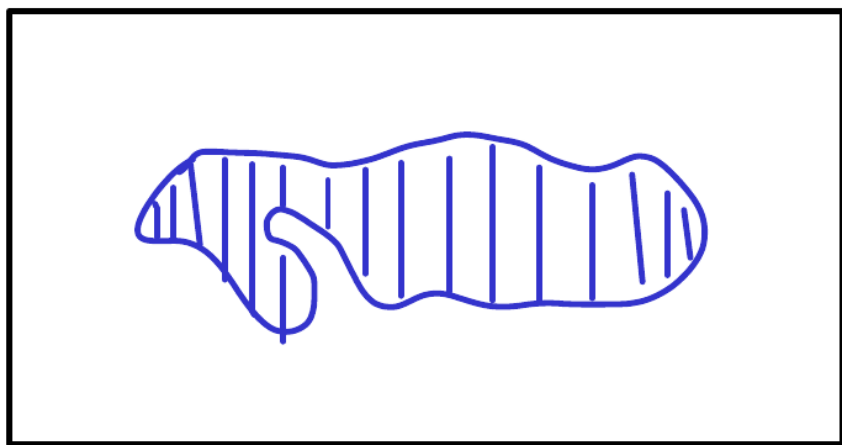
Measured

Theory prediction

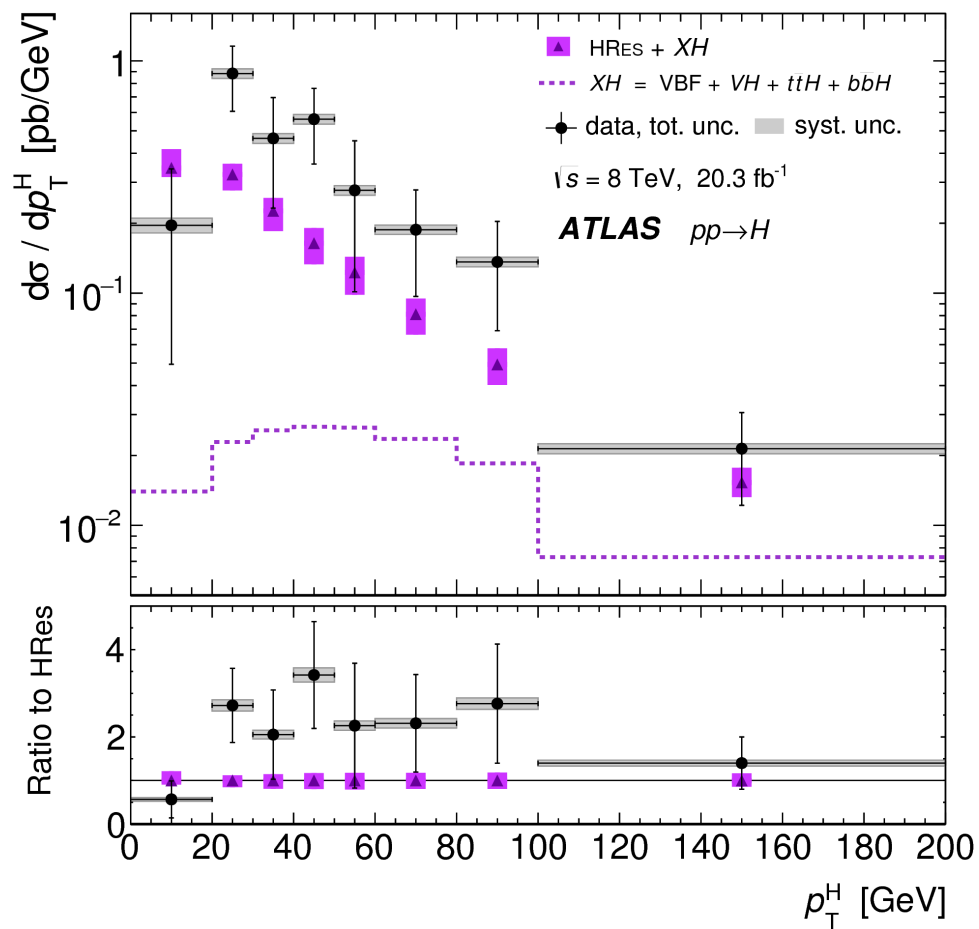
► Kinematics can be modified by BSM interactions.

$$A^{SM} \neq A(\lambda_{1,\dots}, \lambda_N)$$

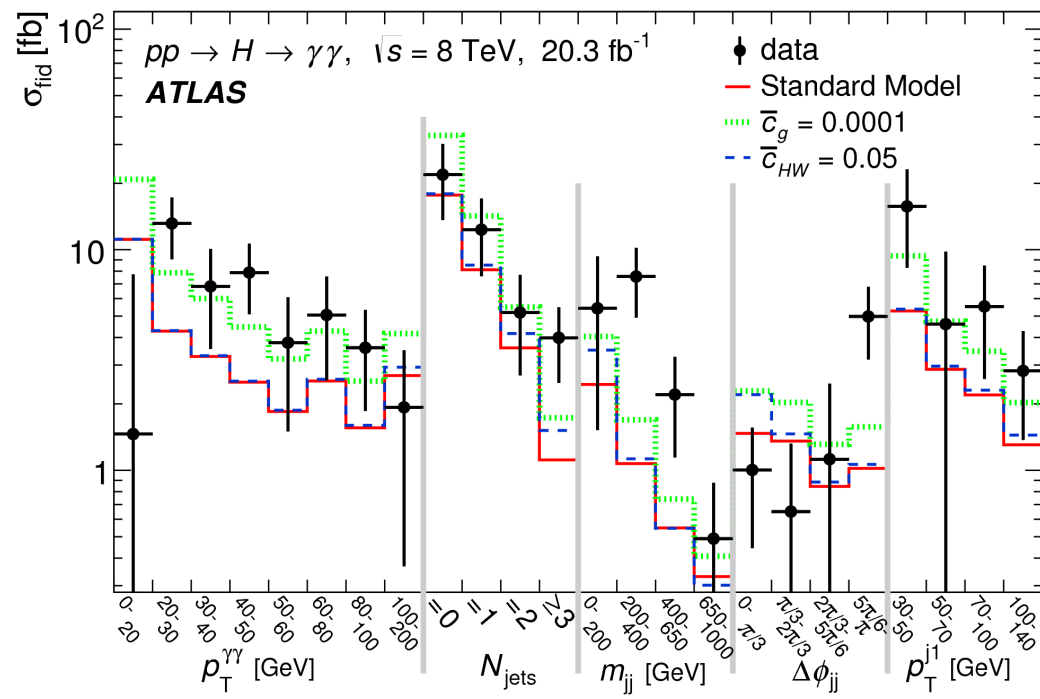
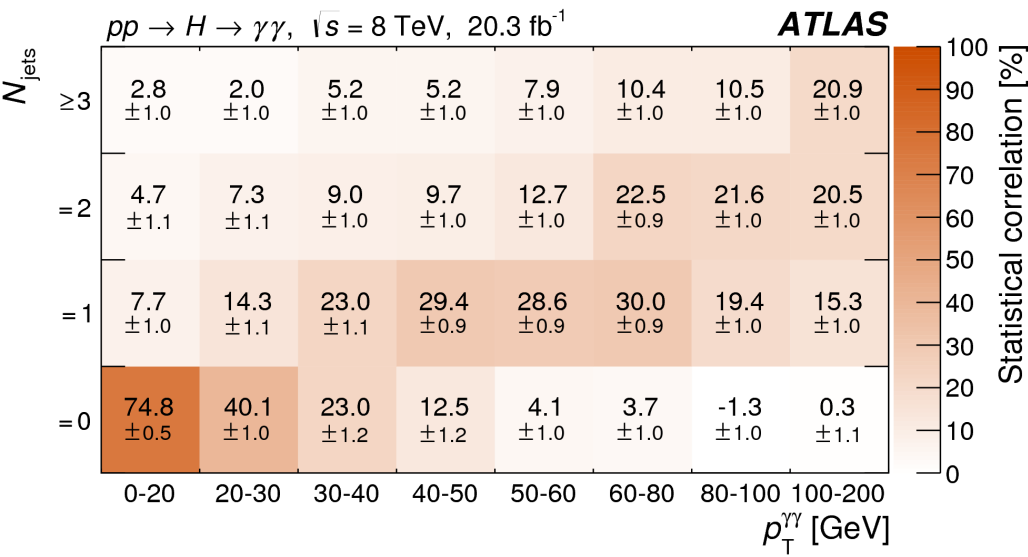
Statistical model



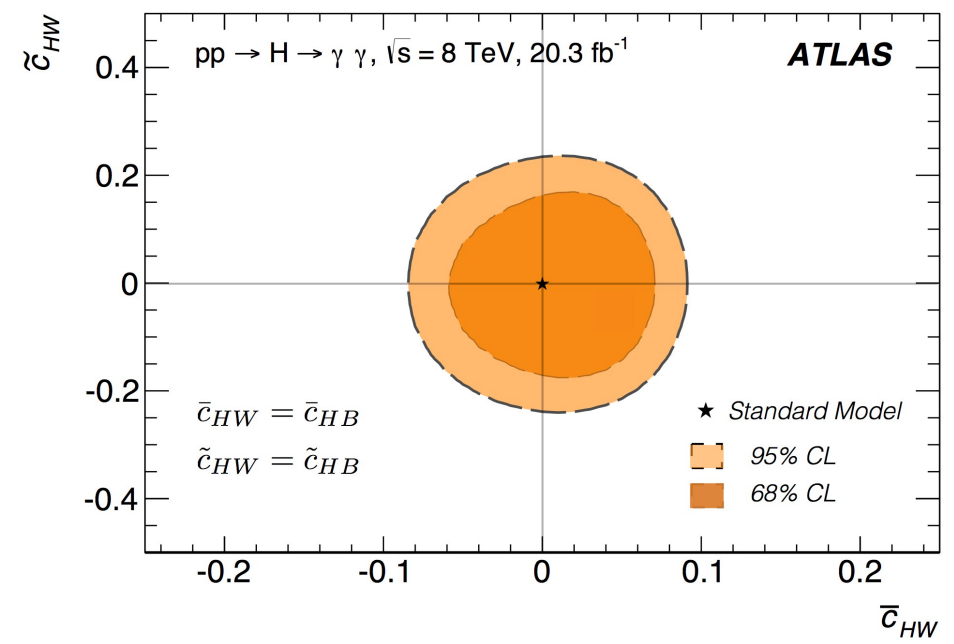
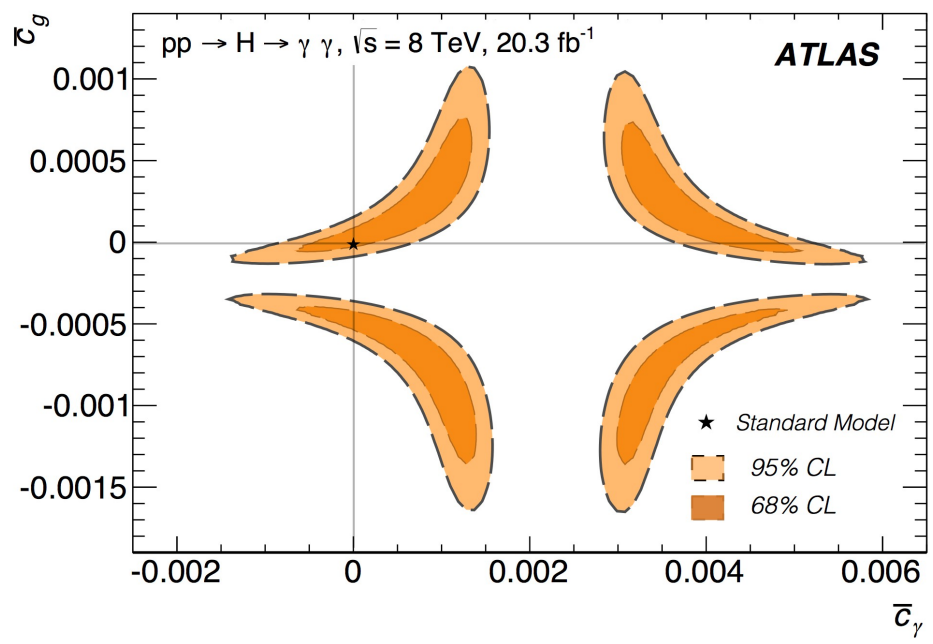
$$q(\mu) = -\ln \left[\frac{\mathcal{L}(\text{data}|\mu; \hat{\theta}_\mu)}{\mathcal{L}(\text{data}|\hat{\mu}; \hat{\theta})} \right]$$



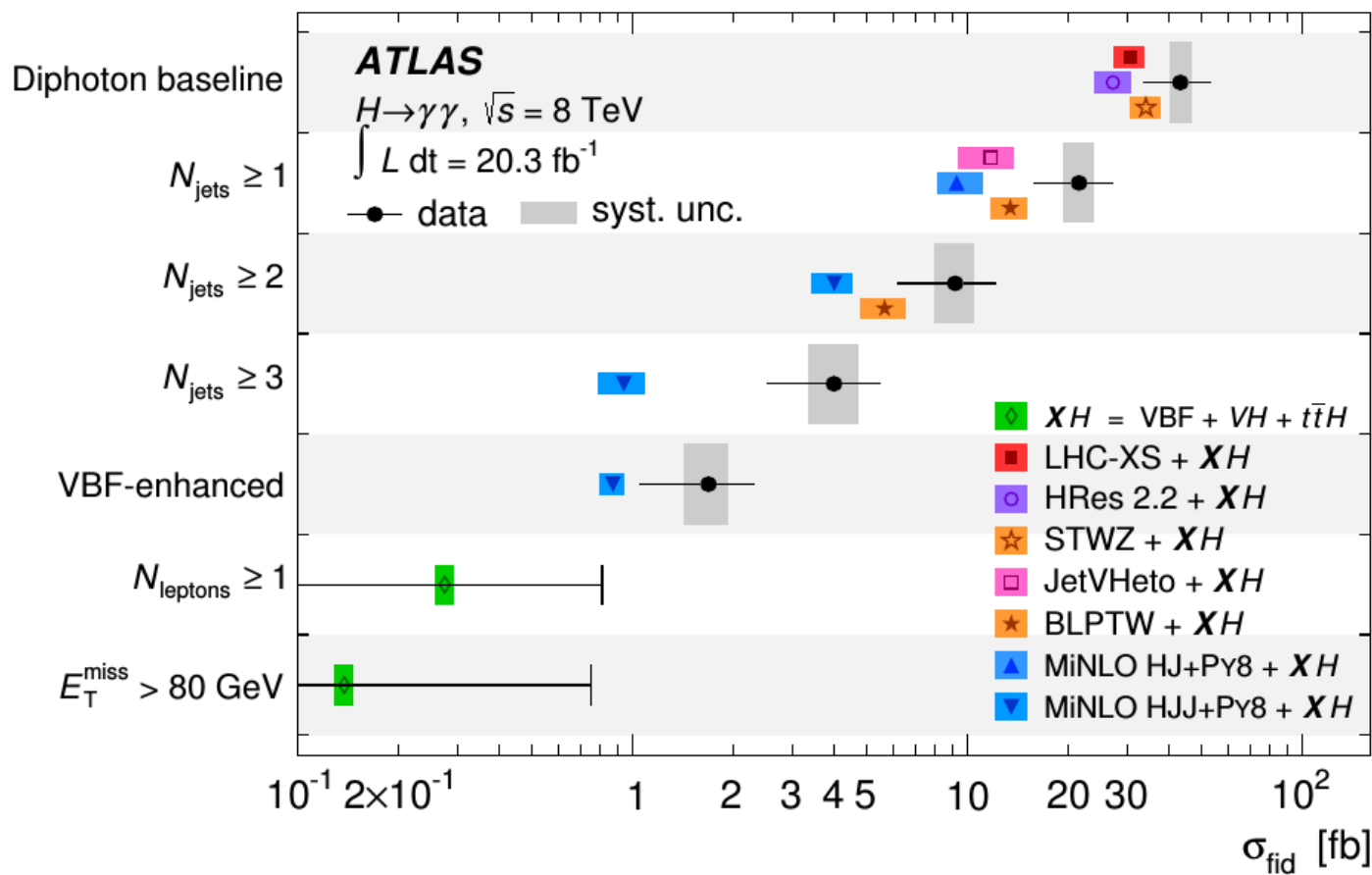
ATLAS: constraints on EFT using differential cross sections.



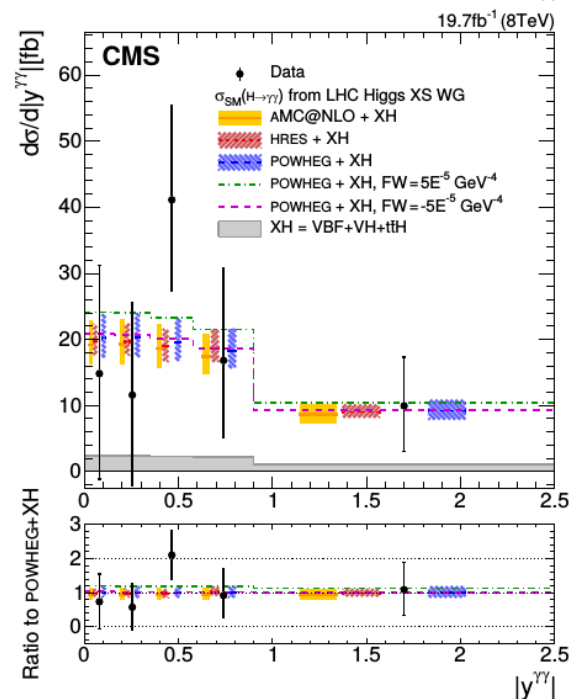
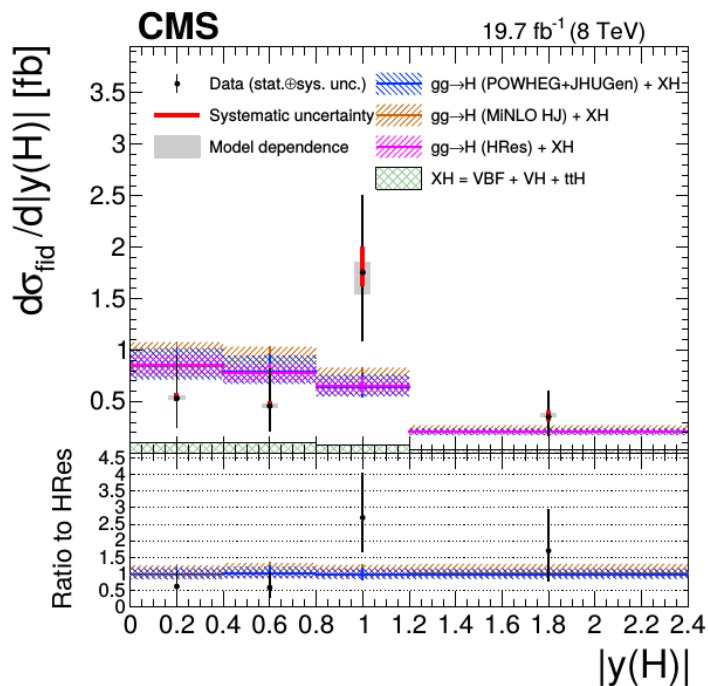
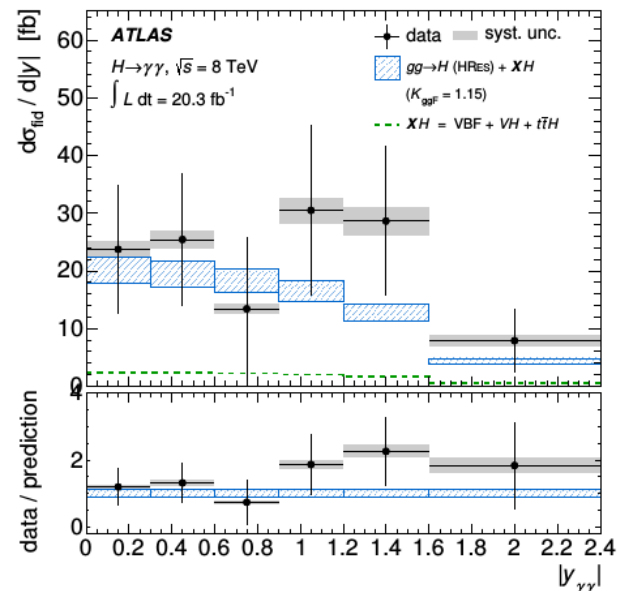
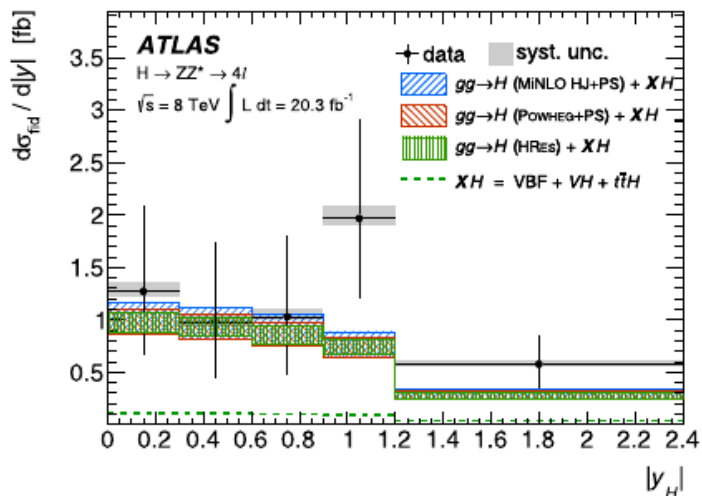
ATLAS: constraints on EFT using differential cross sections.

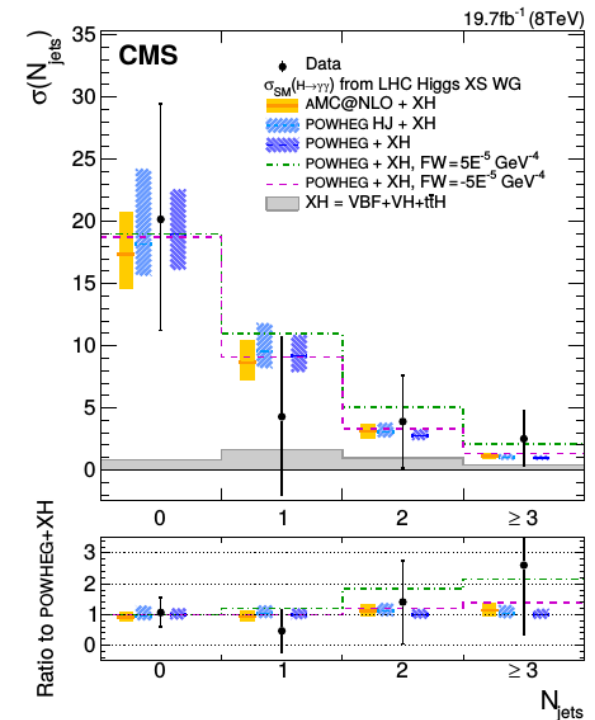
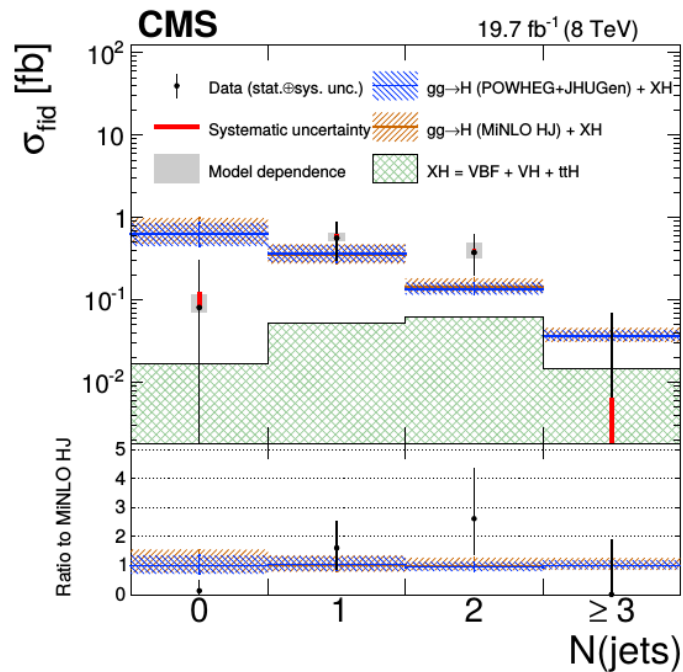
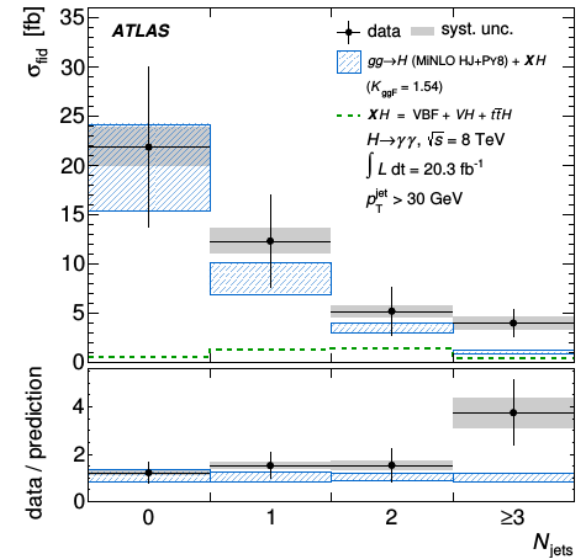
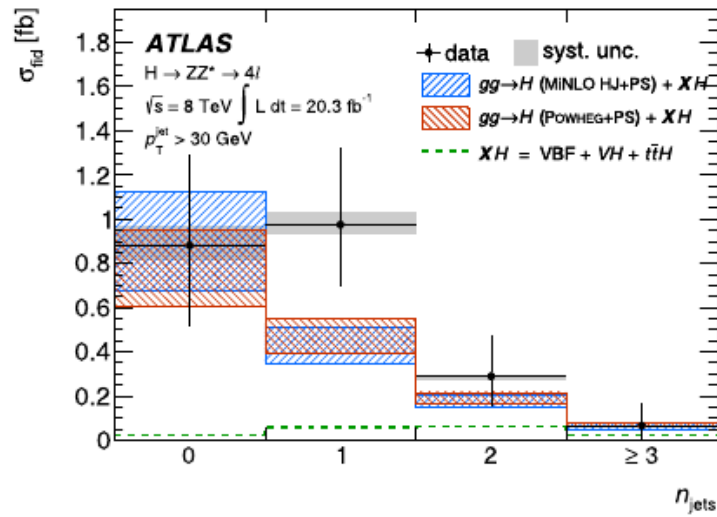


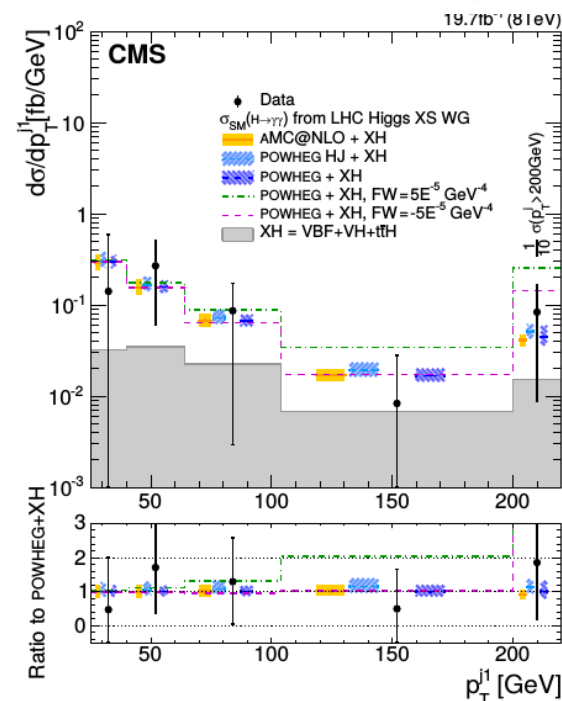
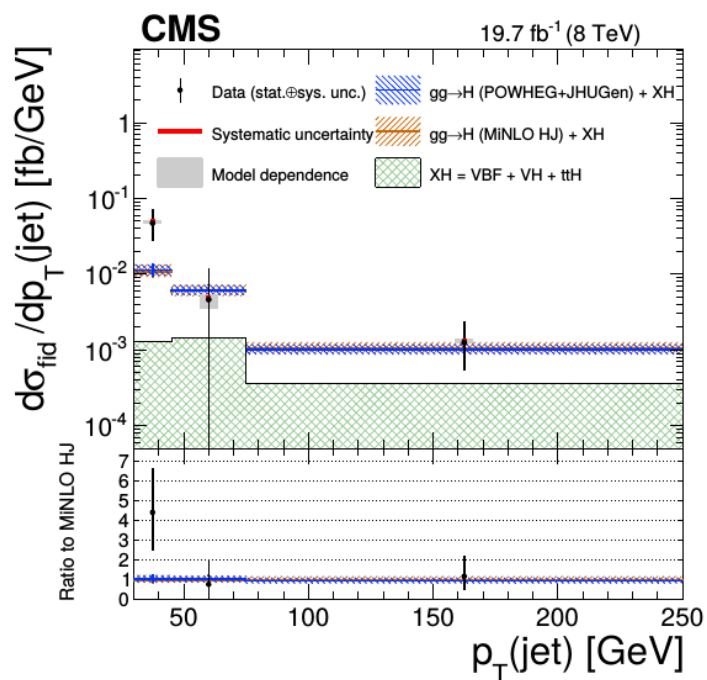
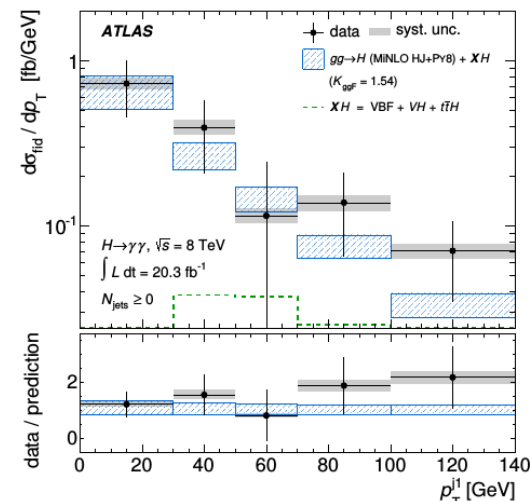
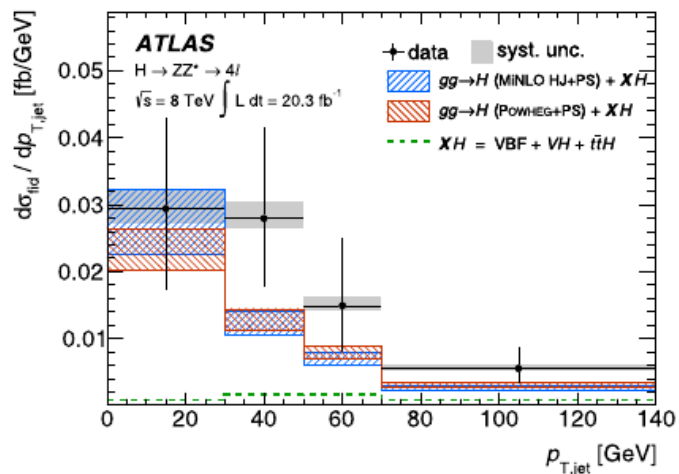
ATLAS: more H \rightarrow fiducial cross sections



Higgs rapidity distribution







Two-jets azimuthal decorrelation

